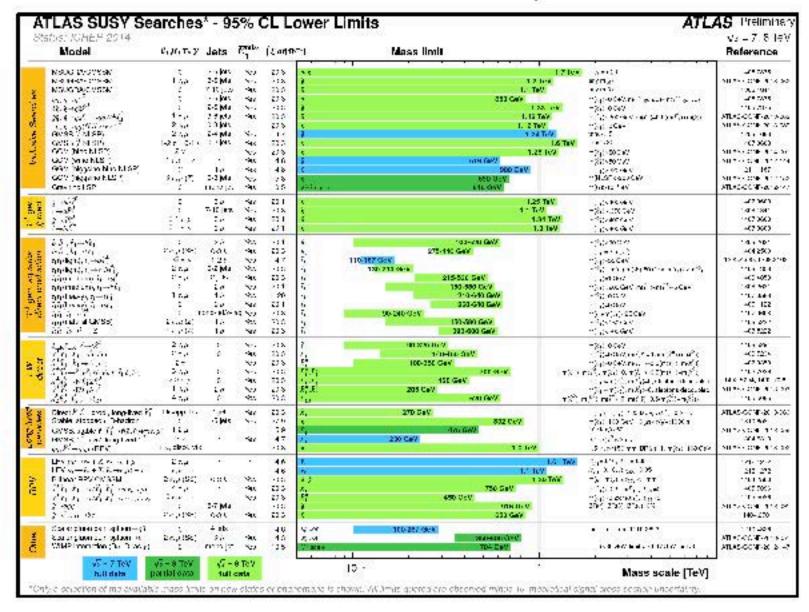
When is a top quark a parton?

Ahmed Ismail ANL/UIC

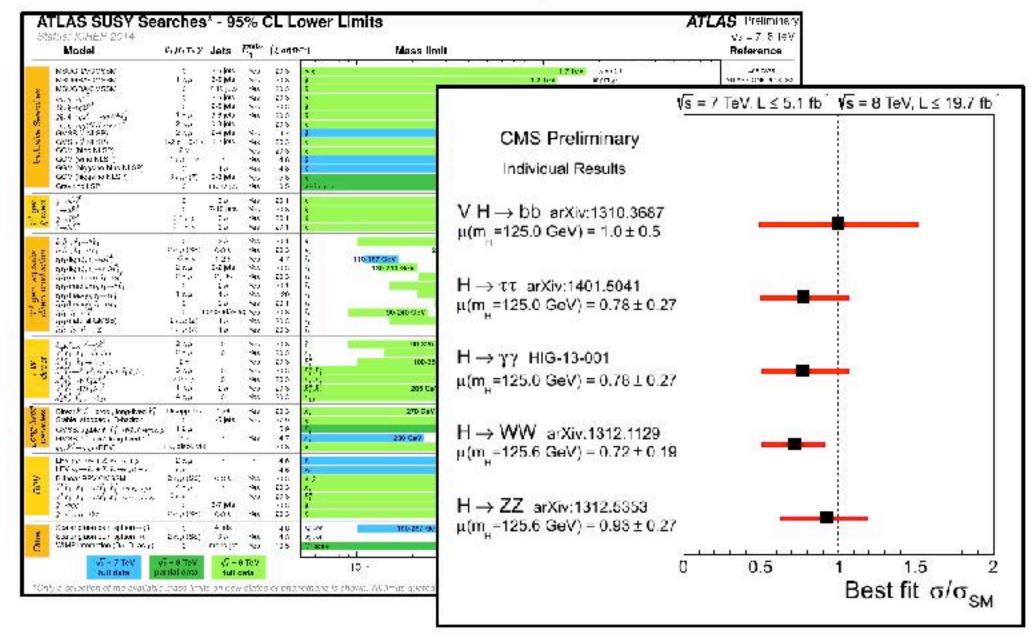
Kavli IPMU ACP Seminar September 10, 2014

1405.6211 with Sally Dawson and Ian Low

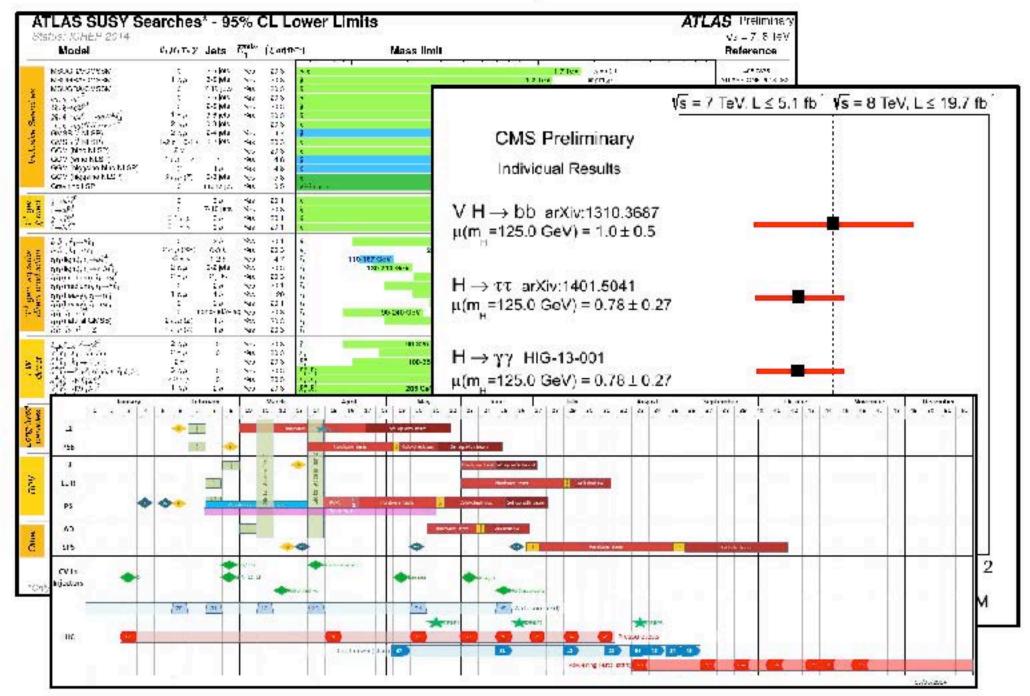
After 8 TeV at the LHC, not much is around



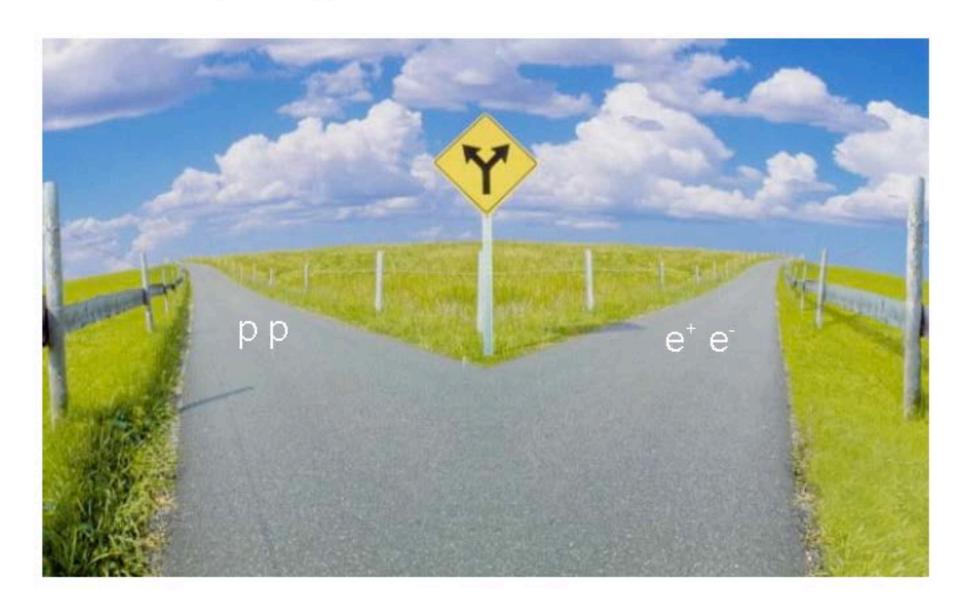
After 8 TeV at the LHC, not much is around



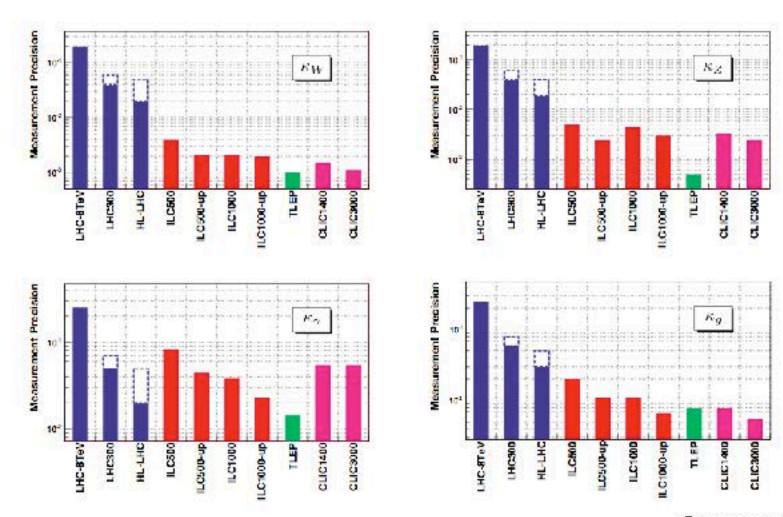
After 8 TeV at the LHC, not much is around



Two main paths possible for future colliders

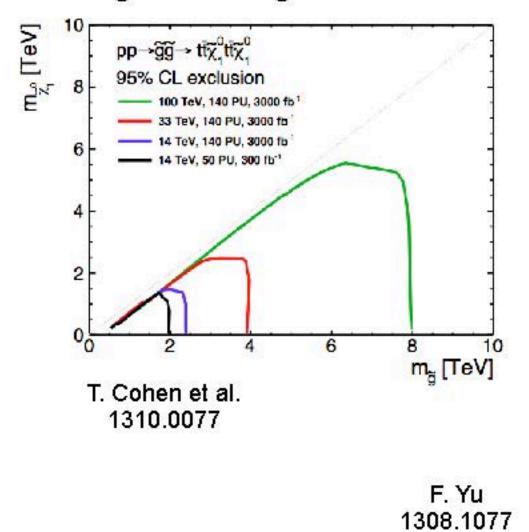


 A linear collider can do some things particularly well, e.g. measure Higgs couplings

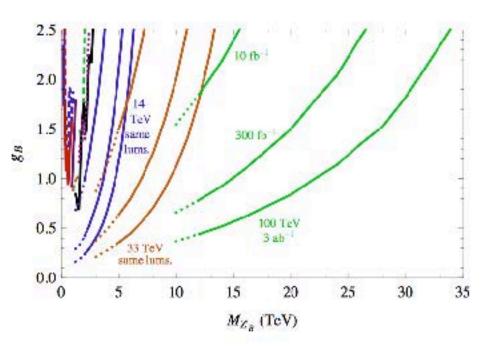


Snowmass Higgs WG report 1310.8361

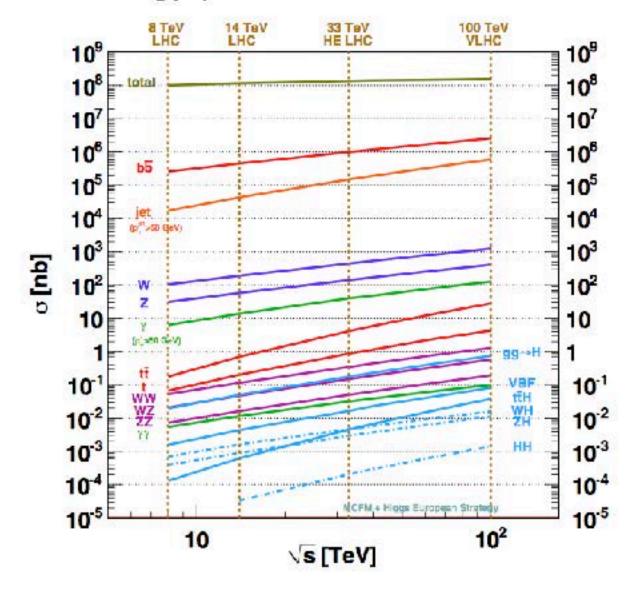
 Many studies, however, are best served by going to higher energies



Searches for heavy BSM particles are the most obvious example



 Even for processes involving SM particles only, high energy proton colliders can have something to say



Cross sections for processes involving t and H increase substantially at high energies

Snowmass QCD WG report 1310.5189

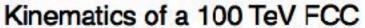
 Recently, there has been renewed interest in future high energy proton colliders, centered around the prospect of a 100 TeV machine

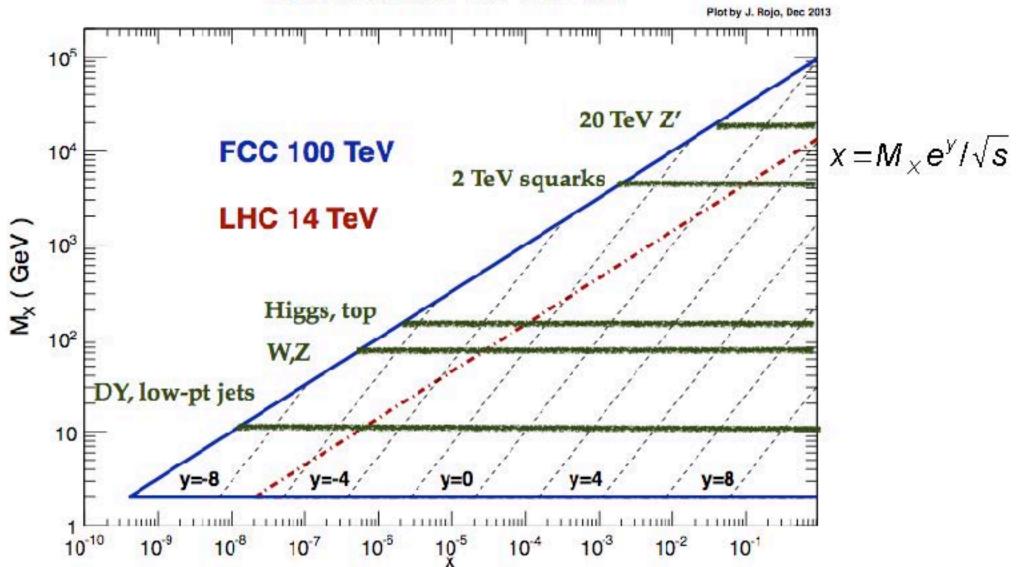








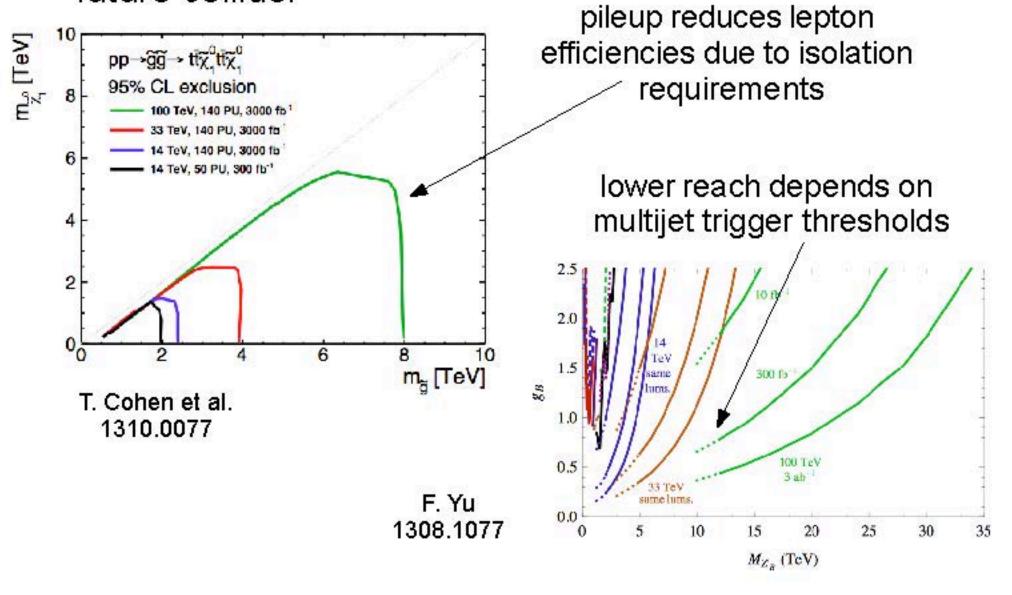




New reach at both high and low scales

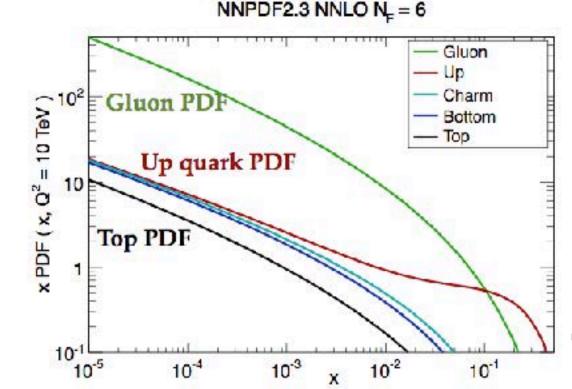
- Work is clearly needed to investigate the power of a future collider
- BSM particle reach, Higgs couplings, rare SM processes are in principle all feasible studies; of course, the results depend on (and influence!) machine considerations
 - Calorimeter resolution?
 - How much luminosity is needed to attain real gains in physics?
 - Trigger, pileup considerations

 Work is clearly needed to investigate the power of a future collider



- There are also qualitatively new effects at high energies ~ 100 TeV
- As an example, electroweak radiation in jets is expected to become more important Manohar et al., 1409.1918
- Exotic signatures possible, e.g. W radiation from neutrinos Hook and Katz, 1407.2607
- Additionally, essentially all SM particles can now be routinely produced with high boost
- Motivates further development of jet substructure techniques Larkoski and Thaler, 1406.7011

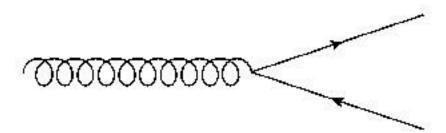
- At 100 TeV, even "heavy" quarks have masses below scales of new processes
- Do we need to consider a top PDF?
- Most PDF sets only include five flavors



If included, top PDF is non-trivial in size at high scales

J. Rojo, Future Circular Collider Study Kickoff Meeting

Arise from gluon splitting at scales above quark mass



Should be able to approximate heavy quark PDF

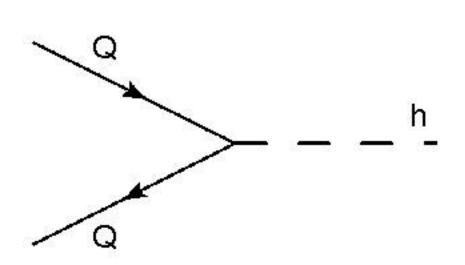
$$\tilde{f}_Q(x,\mu) = \frac{\alpha_s(\mu)}{2\pi} \log \frac{\mu^2}{m_Q^2} \int_x^1 \frac{dz}{z} P_{qg}(z) f_g(\frac{x}{z},\mu)$$

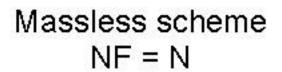
splitting function

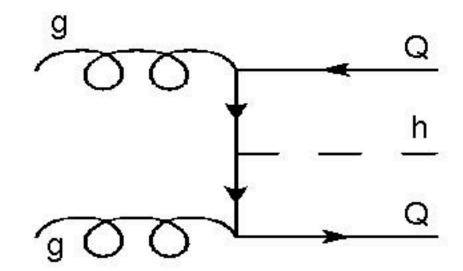
$$P_{qg}(z) = \frac{1}{2} (z^2 + (1-z)^2)$$

gluon PDF

- If we could calculate to infinite order, it wouldn't matter whether we used a heavy quark PDF or not
- As an example, consider h + X production in the PDF schemes with and without the heavy quark







Massive scheme NF = N - 1

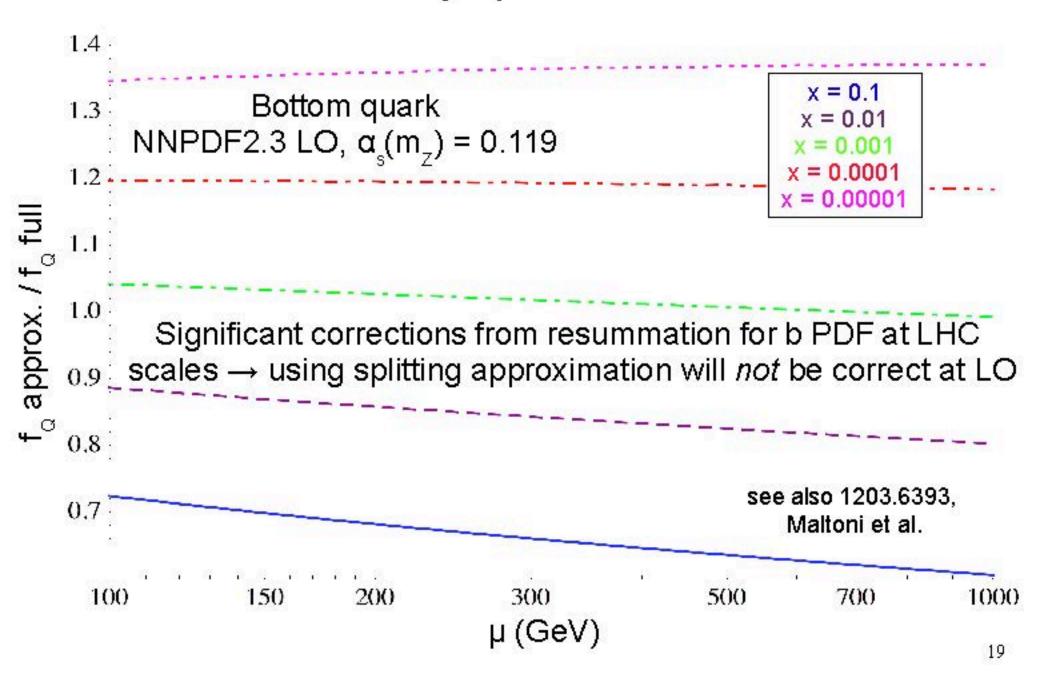
- In the scheme without a heavy quark PDF, the leading diagram for h + X production has a collinear divergence
- When we integrate over the phase space for Q, we pick up a factor log(m_h / m_Q), as the quark mass regulates this divergence
- At large m_h, this is just the approximate heavy quark distribution

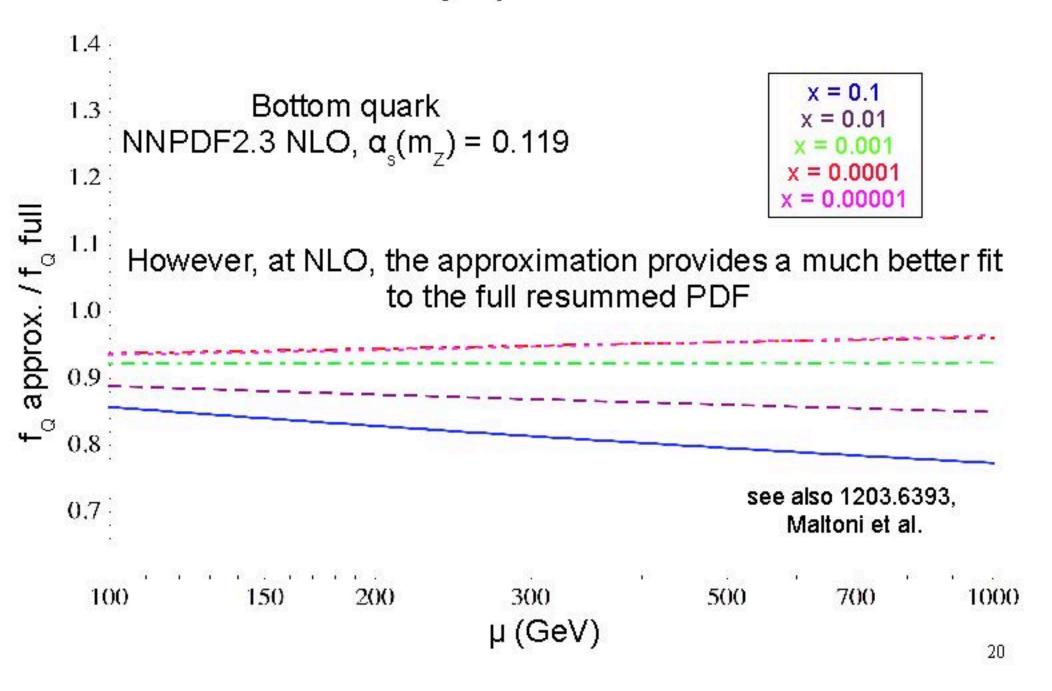
$$\tilde{f}_Q(x,\mu) = \frac{\alpha_s(\mu)}{2\pi} \log \frac{\mu^2}{m_Q^2} \int_x^1 \frac{dz}{z} P_{qg}(z) f_g(\frac{x}{z},\mu) \qquad \qquad - \frac{h}{2\pi} \int_z^1 \frac{dz}{z} P_{qg$$

 To get the full heavy quark PDF at leading order, we would have to numerically solve the LO DGLAP equations

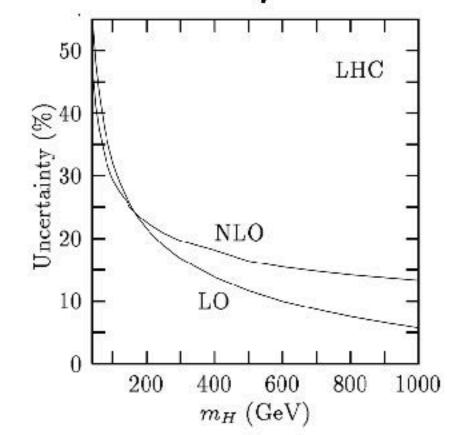
$$\frac{d}{d\log\mu^2} f_Q(x,\mu) = \frac{\alpha_s(\mu)}{2\pi} \int_x^1 \frac{dz}{z} \left(P_{qq}(z) f_Q(\frac{x}{z},\mu) + P_{qg}(z) f_g(\frac{x}{z},\mu) \right)$$
$$f_Q(x,m_Q) = 0$$

- Physically, the difference between our approximation and the full LO heavy quark PDF is the resummation of the logarithms corresponding to multiple parton splittings that are strongly ordered
- How important is this resummation?





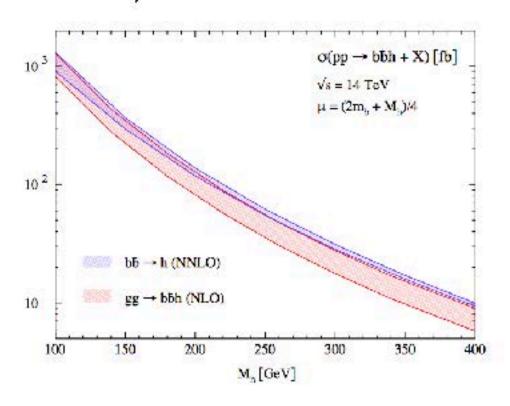
- So, for inclusive Higgs production in association with bottom quarks, the 4- and 5-flavor number schemes should give similar predictions at NLO for the LHC
- Scale uncertainties are sizable at NLO, unfortunately....



Scale uncertainty of NLO inclusive Higgs production in association with bottom quarks, calculated in 5-flavor number scheme

Dicus et al., hep-ph/9811492

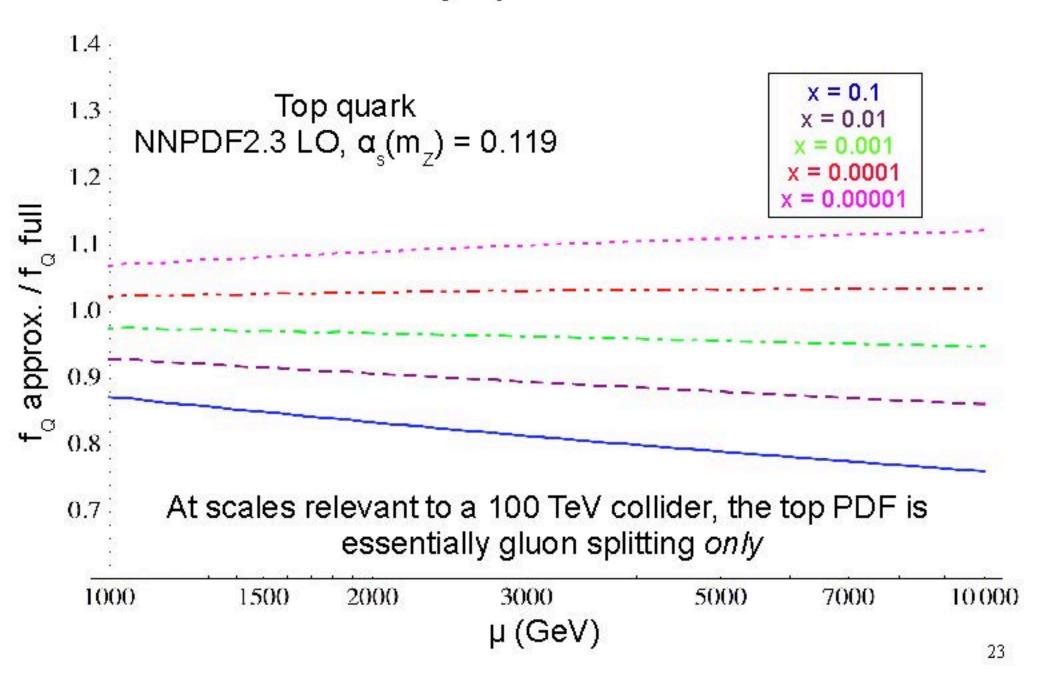
 After going to NNLO, different schemes agree quite well, with smaller scale uncertainties



Inclusive Higgs production in association with bottom quarks, 4FNS vs. 5FNS

Campbell et al., hep-ph/0405302

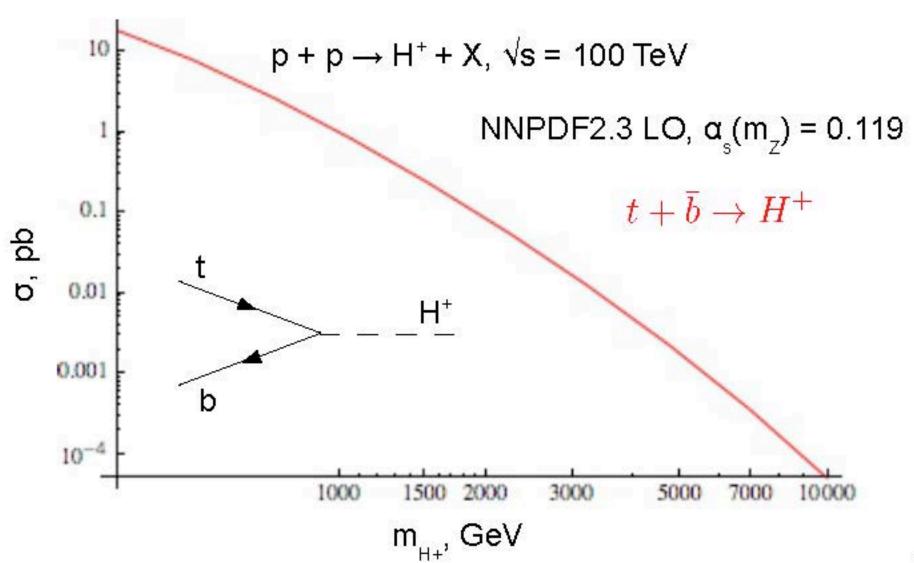
 Much more has been said about the role of heavy quark PDFs in b-initiated Higgs processes at the LHC



- The approximate top PDF at 100 TeV works better than the approximate bottom PDF at the LHC
- The difference can be attributed to the fact that $\alpha_s(\mu) \log(\mu / m_0)$ is smaller in the former case
- So we should expect that in general, the 5- and 6flavor schemes give similar results at a 100 TeV collider for processes involving top quarks
- Only at very high scales, when the log gets large, should there be any appreciable difference between the schemes

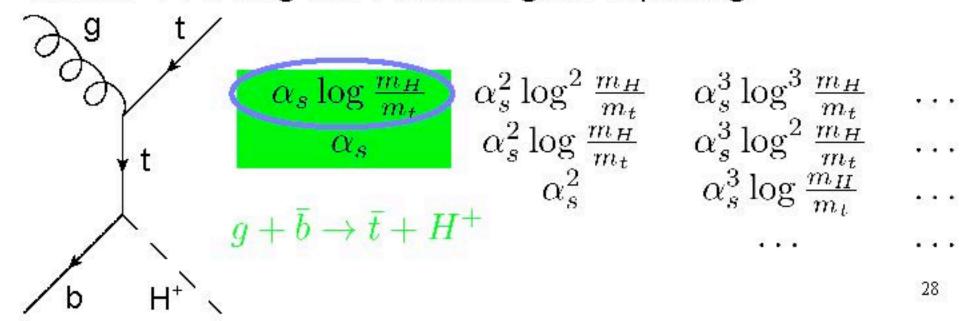
- We can now apply our PDF studies to a sample process at 100 TeV
- Charged Higgses are generic in models with additional Higgs multiplets, with significant couplings to heavy quarks
- To what extent must we calculate H⁺ production using a top PDF? Barnett, Haber and Soper, Nucl. Phys. B306 (1988) 697 Olness and Tung, Nucl. Phys. B308 (1988) 813
- We will outline the computation of the cross section in the NF = 6 scheme, including the top PDF
- Assume MSSM-type couplings with tan β = 5 for numerics, but this is just an overall factor

• Leading diagram is $t + \bar{b} \rightarrow H^+$



- Can organize terms in charged Higgs production cross section according to powers of strong coupling and large logs; first term in 6FNS gives leading log
- The different flavor number schemes sum these terms differently, but of course the final results would be identical if we could work to infinite order

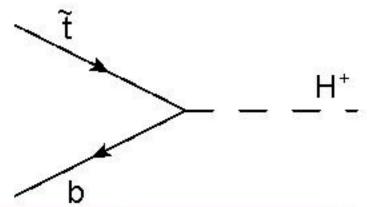
- In 6FNS, next we have g+b→t+H⁺
 (note this is the leading diagram for NF = 5)
- In the limit m_t → 0, this process has a divergence, but it's regulated by the top mass
- Adding it to the previous process would be double-counting the collinear gluon splitting



- To avoid double-counting, need to perform subtraction
- Use approximate top PDF

$$\tilde{f}_Q(x,\mu) = \frac{\alpha_s(\mu)}{2\pi} \log \frac{\mu^2}{m_Q^2} \int_x^1 \frac{dz}{z} P_{qg}(z) f_g(\frac{x}{z},\mu)$$

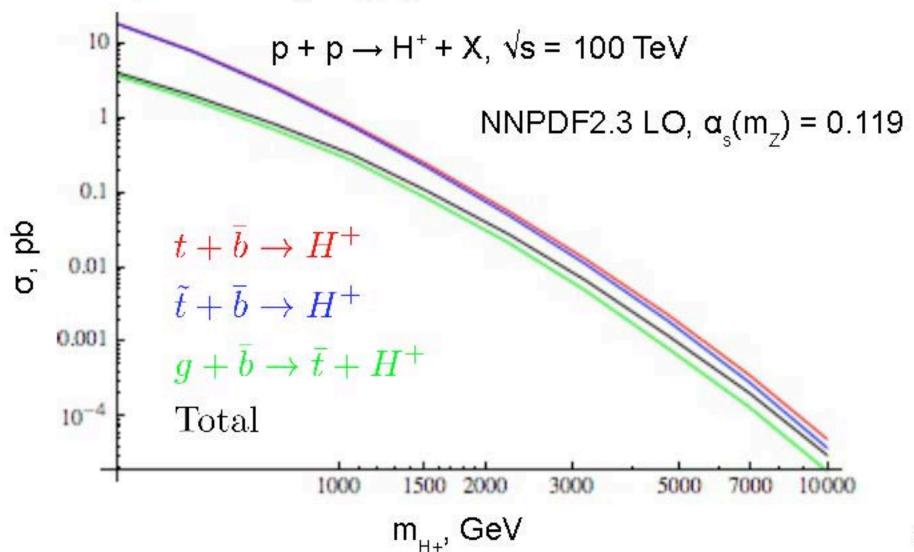
Subtract from sum of previous two processes



| $\alpha_s \log \frac{m_H}{m_t}$ | $\alpha_s^2 \log^2 \frac{m_H}{m_t}$ | $\alpha_s^3 \log^3 \frac{m_H}{m_t}$ | |
|-----------------------------------------------------------------|-------------------------------------|-------------------------------------|--|
| $lpha_s$ | $\alpha_s^2 \log \frac{m_H}{m_t}$ | $\alpha_s^3 \log^2 \frac{m_H}{m_t}$ | |
| $\tilde{\iota}$ $\tilde{\iota}$ $\tilde{\iota}$ $\tilde{\iota}$ | α_s^2 | $\alpha_s^3 \log \frac{m_H}{m_t}$ | |
| $t + \theta \rightarrow H$ | | | |

29

 Subtraction term matches leading log well up to high scales, indicating negligible resummation effects



- As expected, the full top PDF is well approximated by single gluon splitting, and the difference between full LL and gluon splitting is only significant at large scales
- This indicates that the effect of resumming large logs coming from the top phase space is small
- In fact, phase space suppression yields a log even smaller than the ratio of scales we would roughly estimate

$$\log \frac{\mu^2}{m_t^2} \leftarrow \mu^2 = m_{H^+}^2 \frac{(1-z)^2}{z}, z = m_{H^+}^2/\hat{s}$$

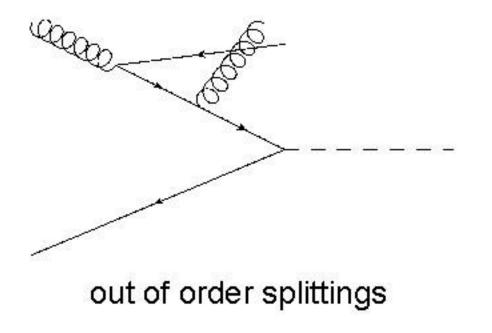
 This phase space suppression is generic for processes involving heavy quarks

- The cross section is now complete up to terms of order α_s² (log m_H / m_t) and higher
- Full NLL requires a few more components

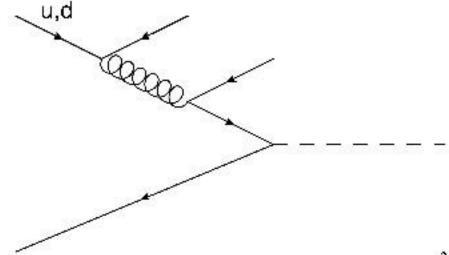
(so far: leading order plus leading log)

| $\alpha_s \log \frac{m_{II}}{m_L}$ | $\alpha_s^2 \log^2 \frac{m_H}{m_t}$ | $\alpha_s^3 \log^3 \frac{m_H}{m_t}$ | |
|------------------------------------|-------------------------------------|-----------------------------------------------------------------------------|--|
| $lpha_s$ | $\alpha_s^2 \log \frac{m_H}{m_t}$ | $\frac{\alpha_s^3 \log^2 \frac{m_H}{m_t}}{\alpha_s^3 \log \frac{m_H}{m_t}}$ | |
| | α_s^2 | $\alpha_s^3 \log \frac{m_H}{m_t}$ | |
| | | | |

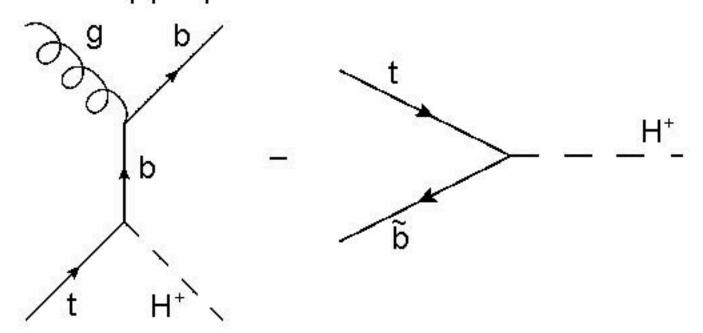
- The cross section is now complete up to terms of order α_{s^2} (log $m_{_H}$ / $m_{_t}$) and higher
- Full NLL requires a few more components
 - NLO PDFs rather than LO PDFs



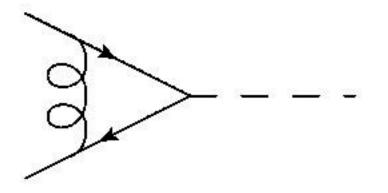
splittings from light quarks

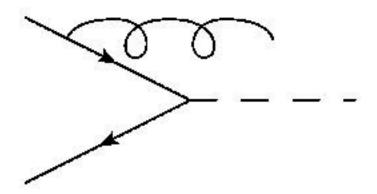


- The cross section is now complete up to terms of order α_s² (log m_H / m_t) and higher
- Full NLL requires a few more components
 - NLO PDFs rather than LO PDFs
 - The log-suppressed process $g+t \rightarrow b+H^+$ with the appropriate subtraction term



- The cross section is now complete up to terms of order α_s² (log m_H / m_t) and higher
- Full NLL requires a few more components
 - NLO PDFs rather than LO PDFs
 - The log-suppressed process $g+t \rightarrow b+H^+$ with the appropriate subtraction term
 - The virtual and real corrections to $t + \bar{b}
 ightarrow H^+$

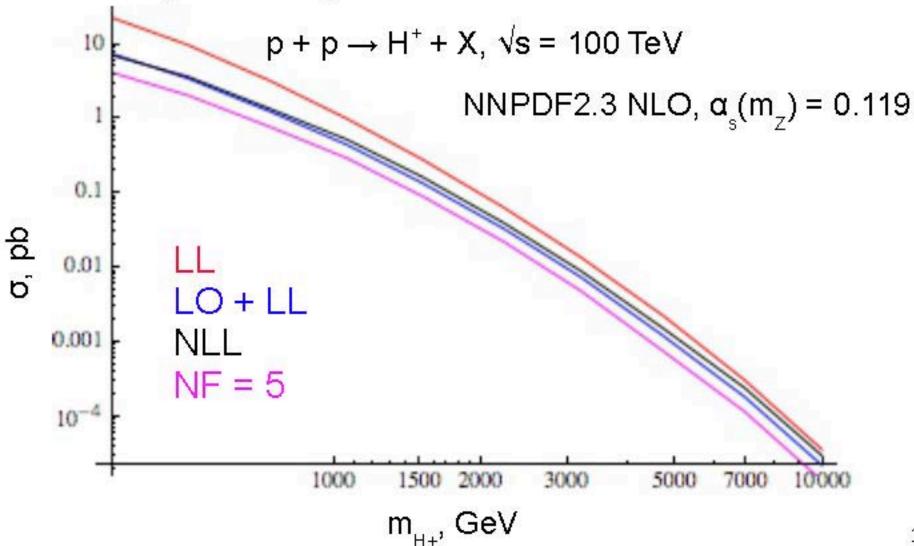




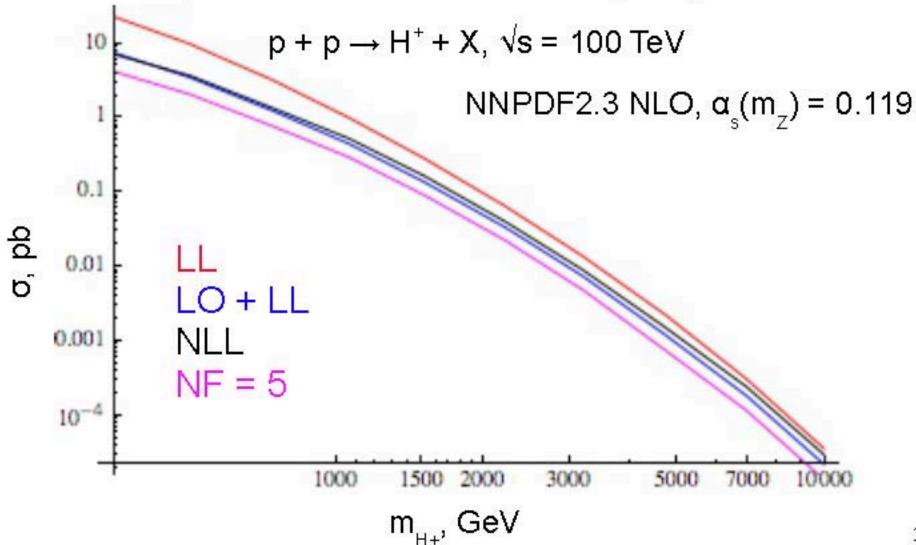
- The cross section is now complete up to terms of order α_s² (log m_H / m_t) and higher
- Full NLL requires a few more components
 - NLO PDFs rather than LO PDFs
 - The log-suppressed process $g + t \rightarrow b + H^+$ with the appropriate subtraction term
 - The virtual and real corrections to $t + \bar{b} \rightarrow H^+$

... ...

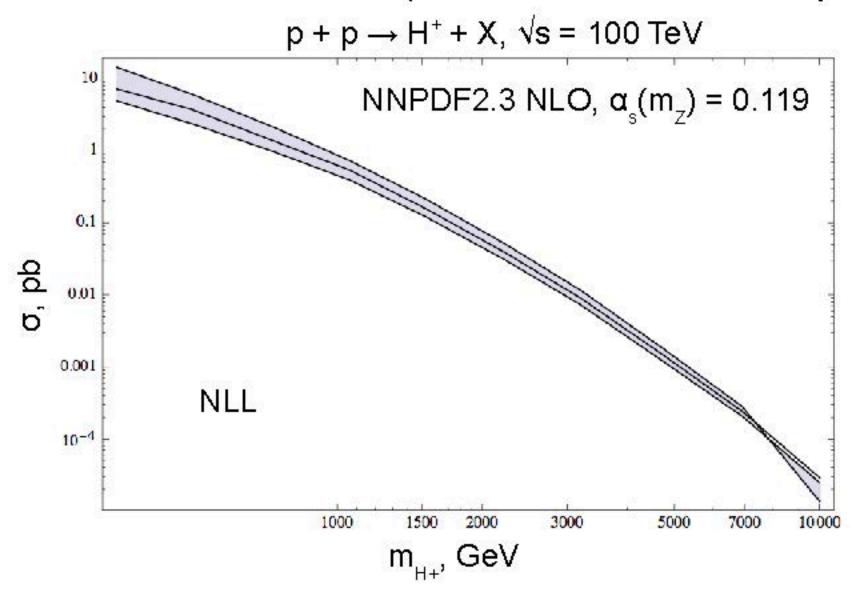
 Going from LO + LL to full NLL doesn't change much, indicating that the perturbation series is under control



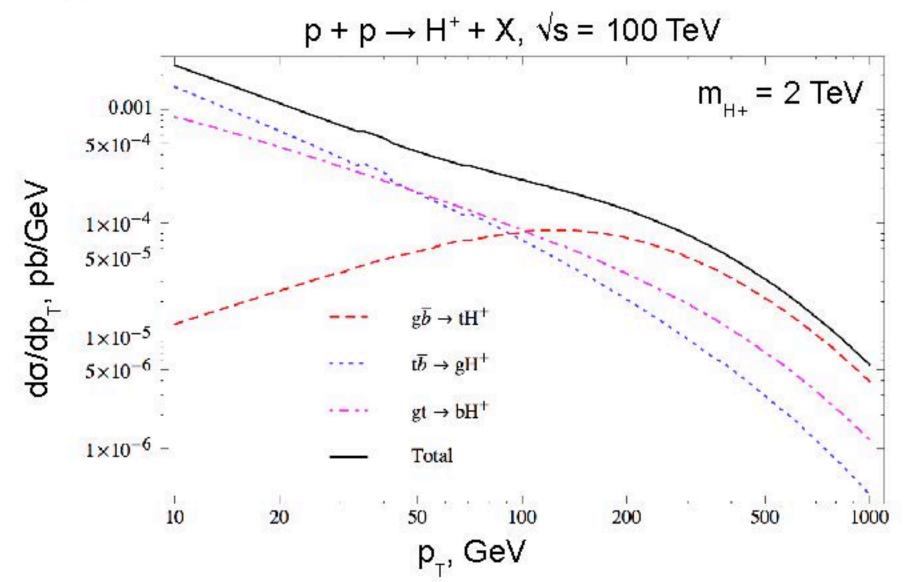
Total cross section is well approximated by the NF = 5
scheme up to factors of a few at very large H+ mass



 At high charged Higgs mass, differences between schemes is small compared to scale uncertainty

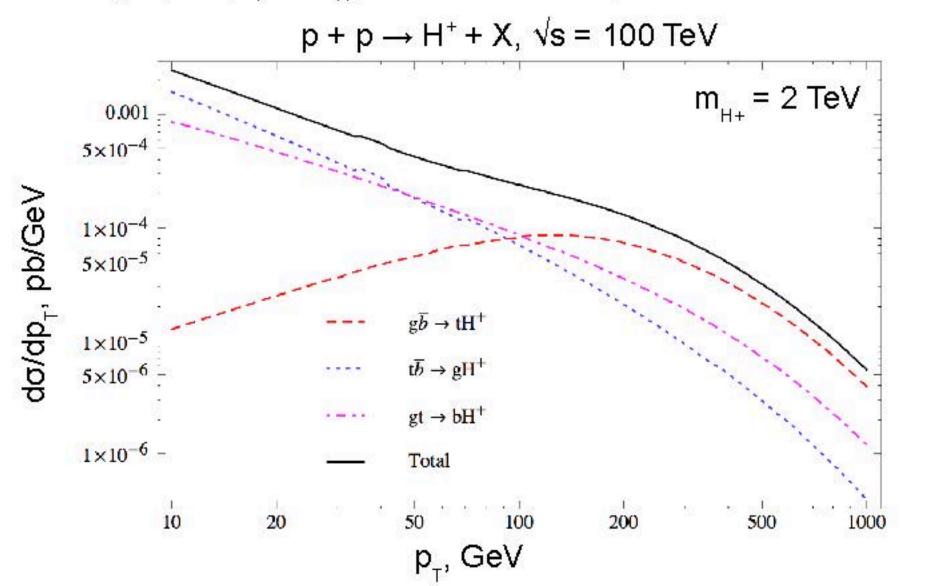


 Higgs p_τ spectrum dominated by gluon emission at low p_τ, which doesn't exist at LO in NF = 5 scheme



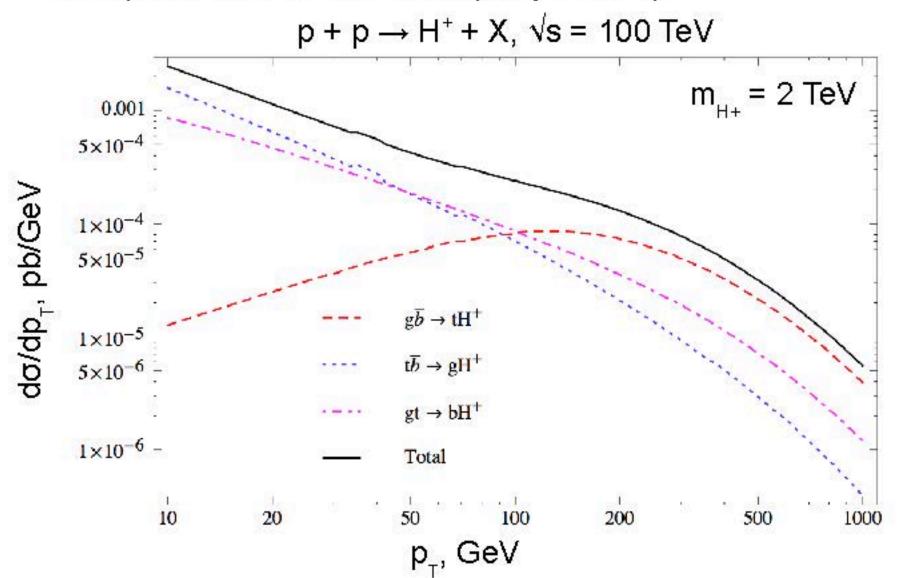
40

 For production of charged Higgs plus X, turnover is roughly at p_T ~ m_X; this is more important than before!

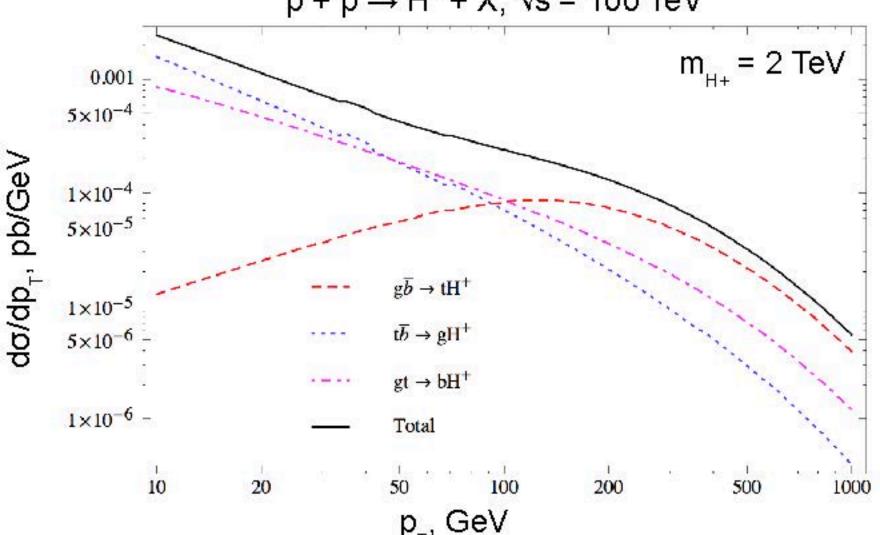


41

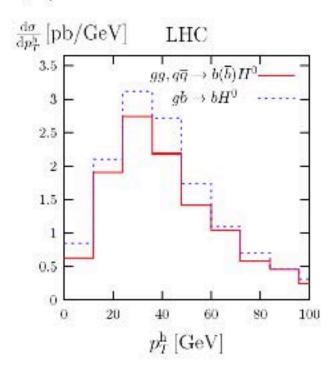
 At low Higgs p_T, need to do 5FNS NLO calculation to compare with 6FNS NLL (stay tuned)



Mass effects at low p_T only included to LO in this calculation, using the S-ACOT (FONLL-A) scheme
 p + p → H⁺ + X, √s = 100 TeV



- For bottom quarks at the LHC, "low p_↑" roughly corresponds to transverse momentum below the bottom mass, so this issue isn't as crucial
- Nevertheless, similar analogous studies suggest that we can do much better in predicting the charged Higgs p_T distribution in the 5FNS by going to NLO



p_⊤ distribution for Higgs production in association with at least one b quark NLO 4FNS vs. 5FNS

Dawson et al., hep-ph/0508293

Summary

- Because of α_s running and the heavy top mass, the gain from using a top PDF at a future pp collider is less than that from using a bottom PDF at the LHC
- At very high scales, effect of resummed logs contained in top PDF can change calculated cross sections by a factor of a few, which would seemingly translate into only slight changes in search reach
- However, kinematic distributions such as the p_⊤
 spectrum need more care, with effects that are more
 important for the top quark than for the bottom quark
- For these, going to NLO in the 5FNS is probably needed

Backup

Mass effects

- Point of using a heavy quark PDF is to make predictions at scales >> the heavy quark mass
- At scales ~ the quark mass, finite mass effects enter
- S-ACOT: take heavy quark to be massless
- FONLL-A: LO massive quark function at low Q, NLO massless function at high Q (used by NNPDF2.3 NLO) equivalent to S-ACOT
- FONLL-B: NLO massive quark function at low Q, NLO massless function at high Q
- FONLL-C: NLO massive quark function at low Q, NNLO massless function at high Q