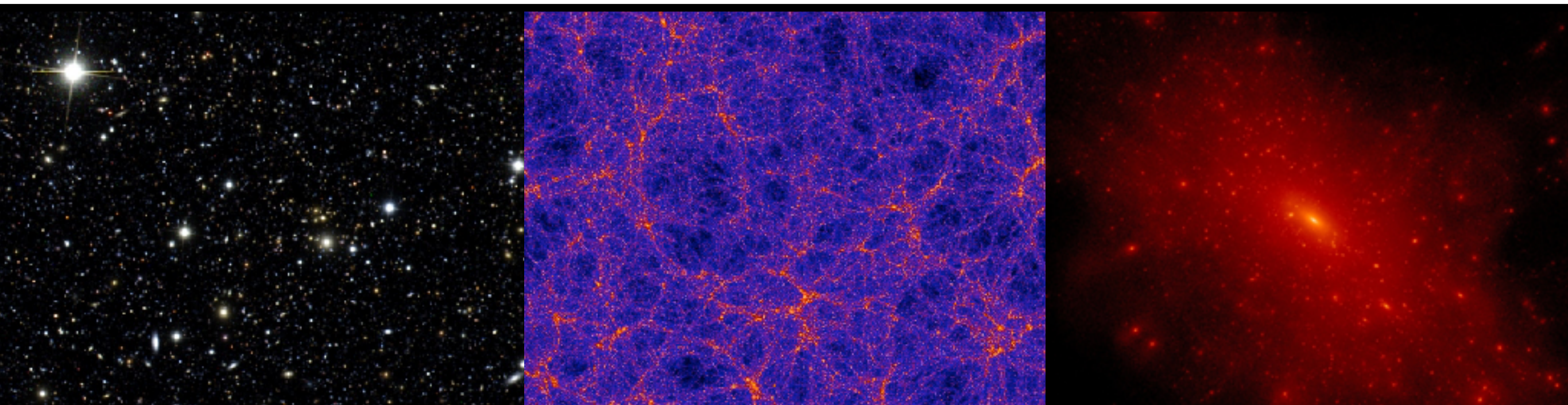


# A Flexible Halo Model for the Intrinsic Alignments of Galaxies

**Duncan Campbell**

McWilliams Fellow  
Carnegie Mellon University

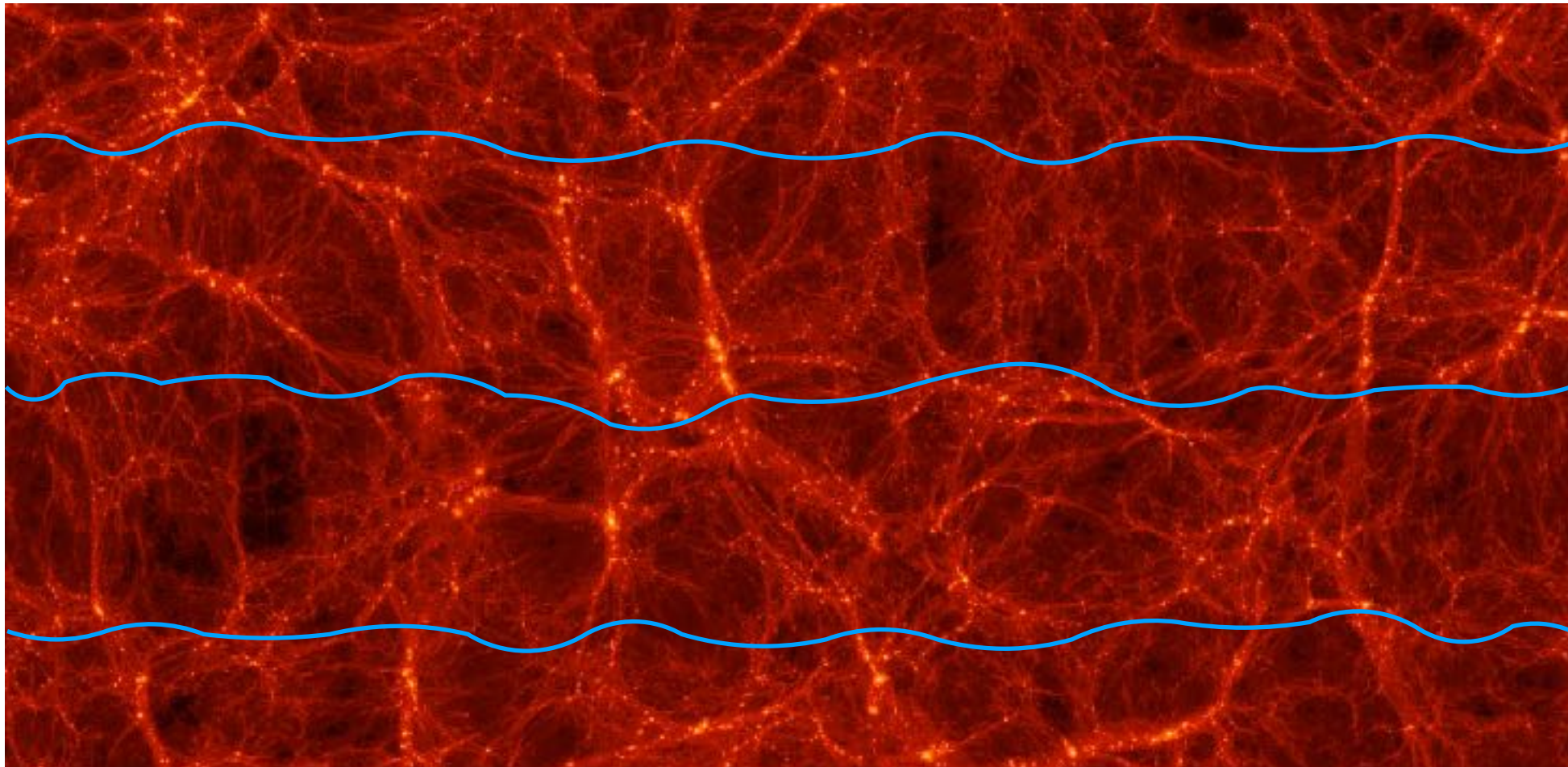


# Outline

- Overview of gravitational lensing
- Introduction to intrinsic alignments (IA)
- Review of galaxy alignment 2-point functions
- Review of previous models of IA
- Introduction to a flexible halo-based model of IA
- Phenomenology of alignment correlations in the halo model context
- Discussion of future work and applications



# Gravitational Lensing



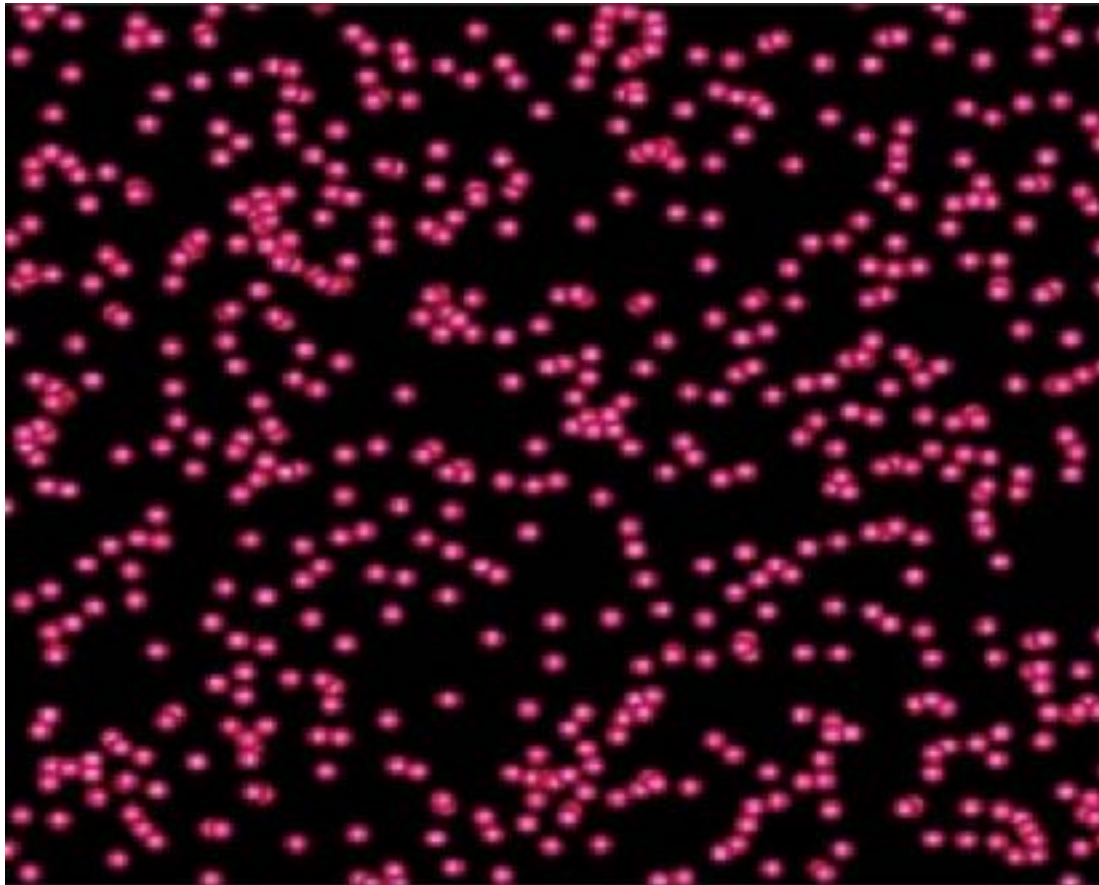
distant galaxies



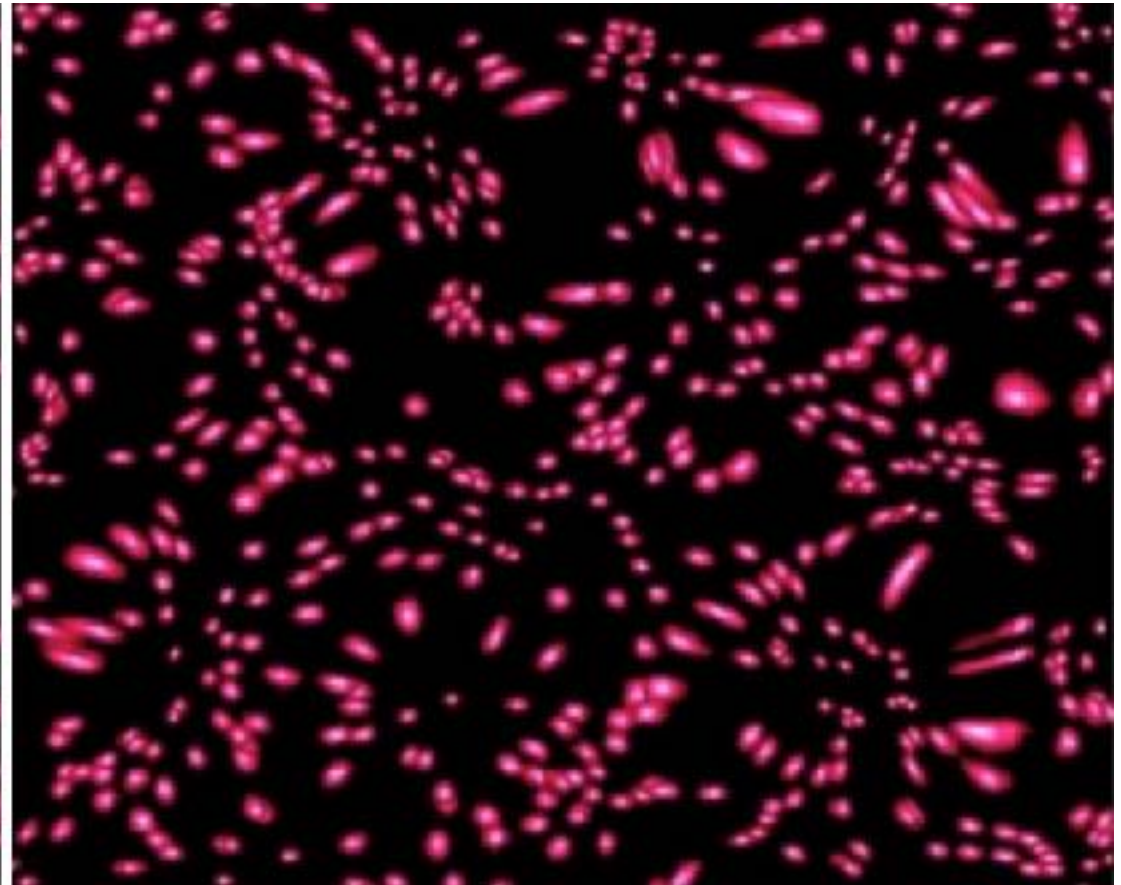
- Light from distant galaxies is deflected by the intervening matter distribution.
- Deflections result in galaxy shape distortions and magnification.

# Weak Gravitational Lensing

Un-lensed “galaxies”



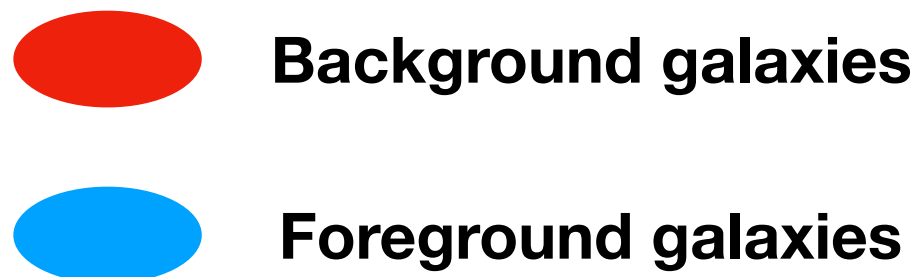
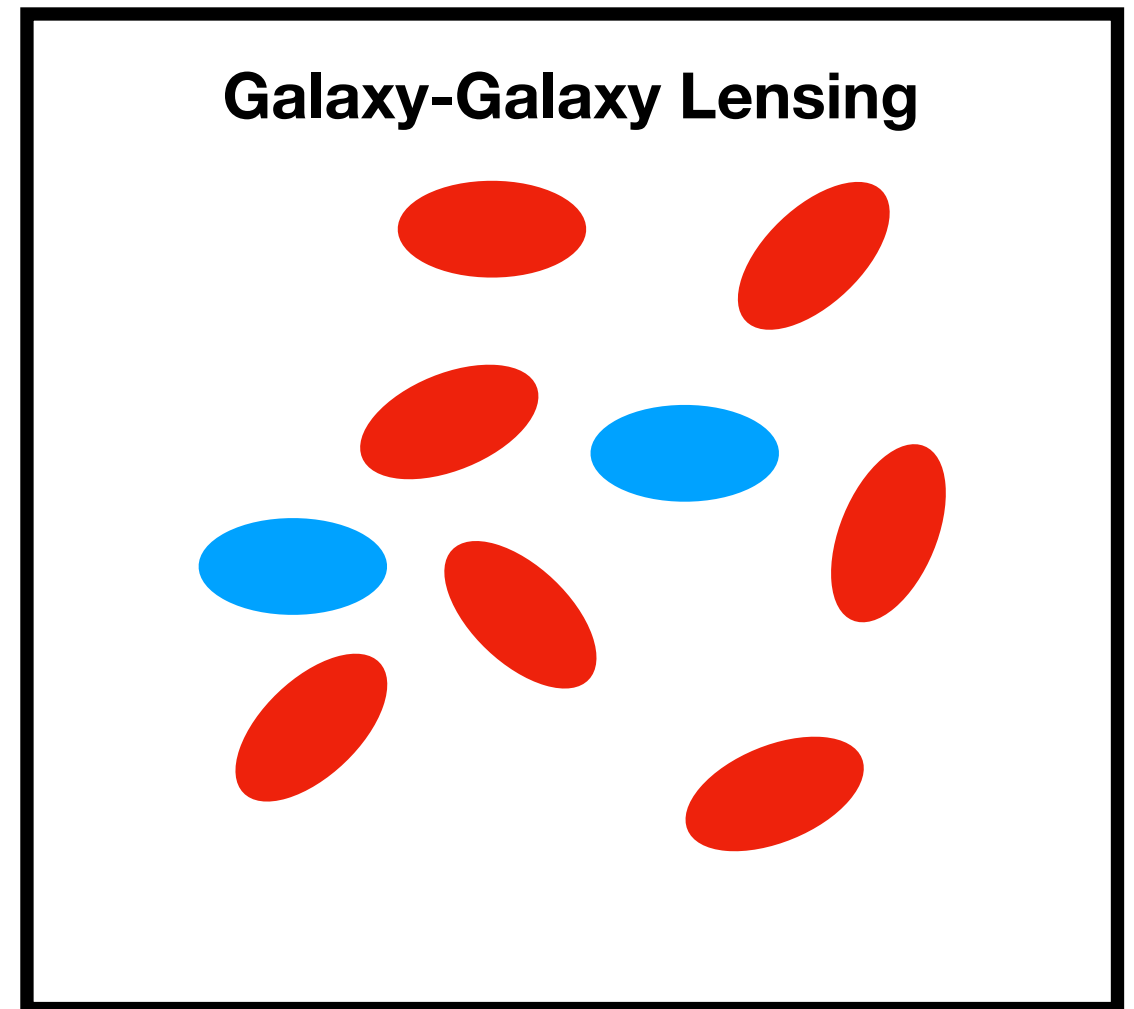
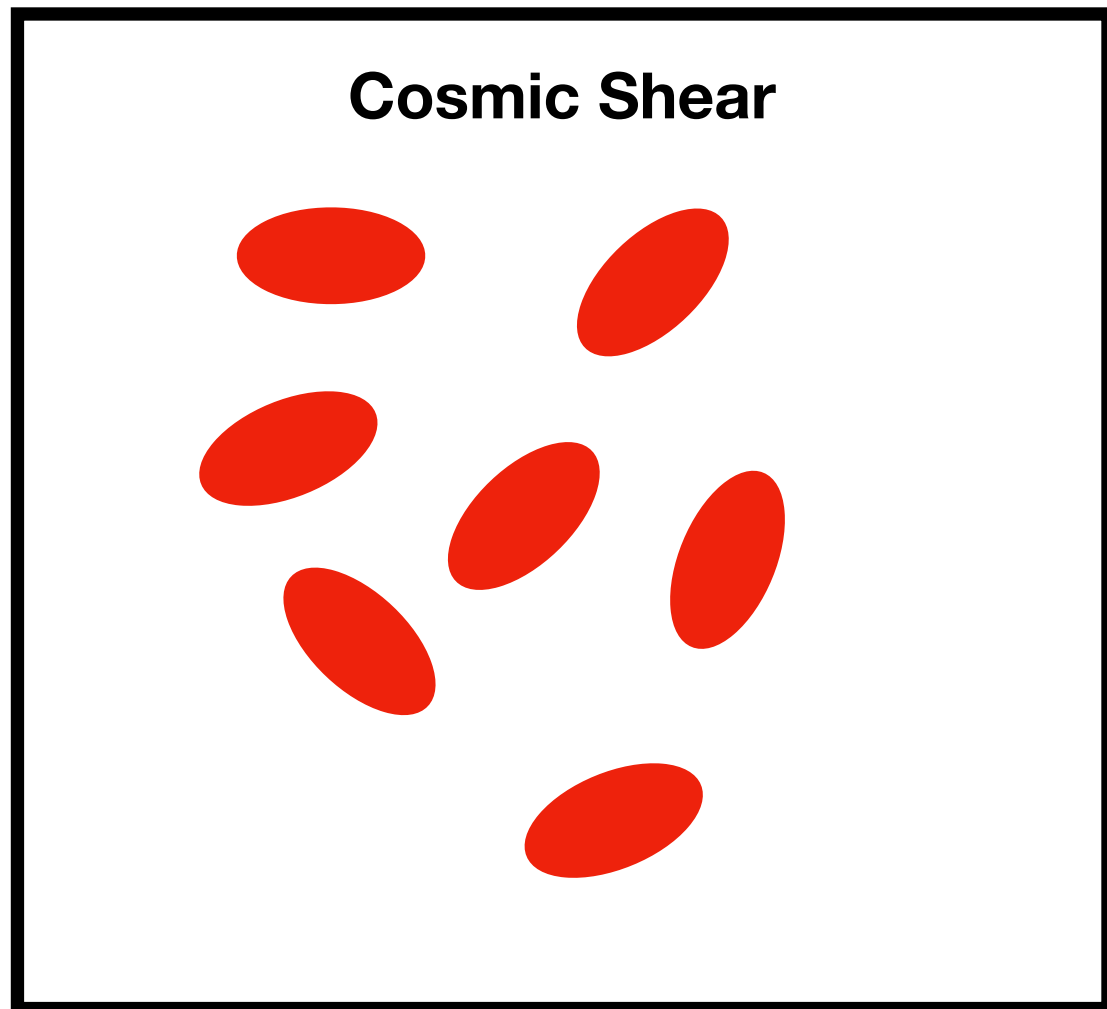
lensed “galaxies”  
(exaggerated)



- Deflections result in galaxy shape distortions and magnification.
- Weak lensing results in tangential shear in the direction of mass over densities.

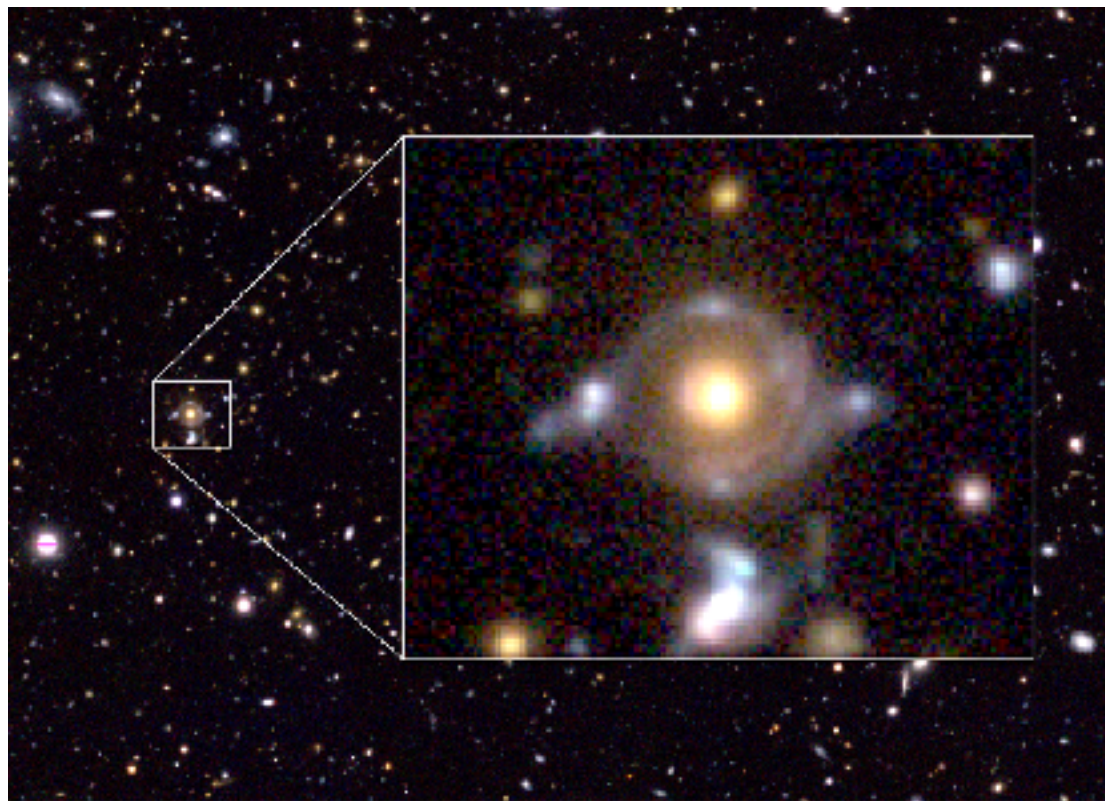
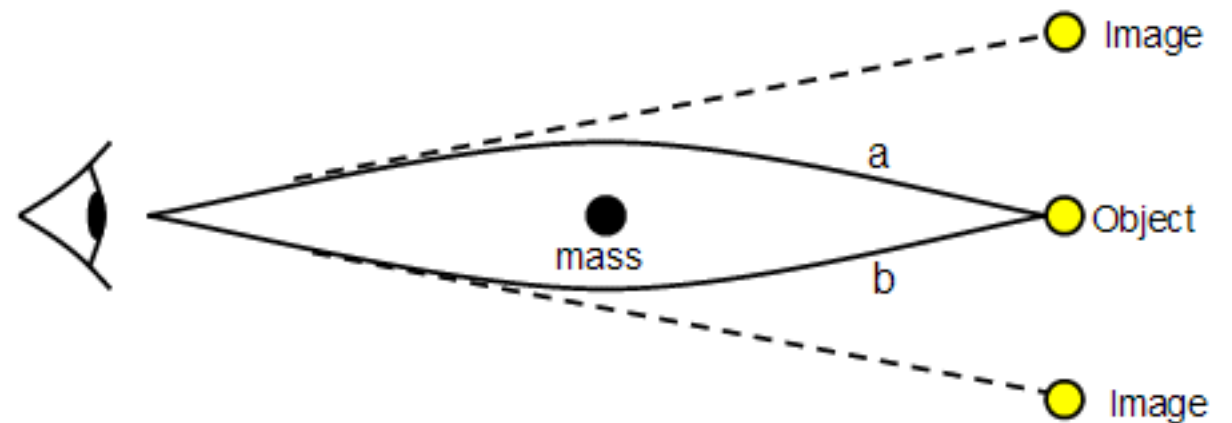
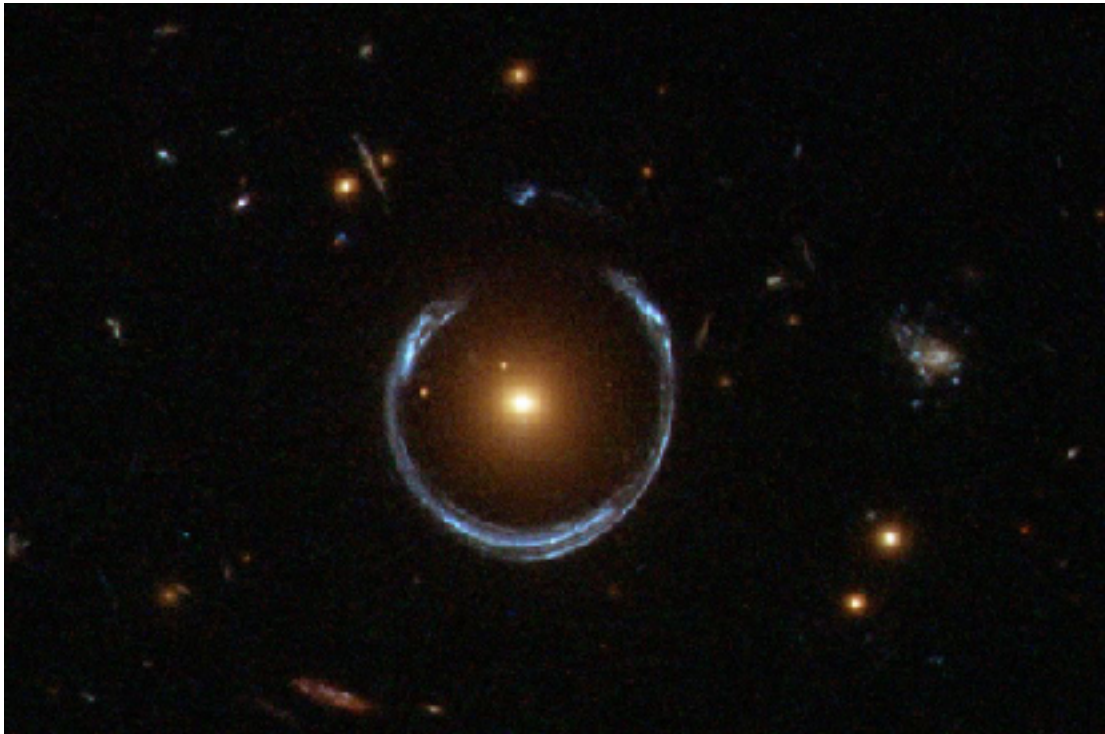


# Weak Gravitational Lensing



- Cosmic shear: correlated shapes of background galaxies
- Galaxy-galaxy lensing: correlated shapes of background and foreground galaxies

# Strong Gravitational Lensing

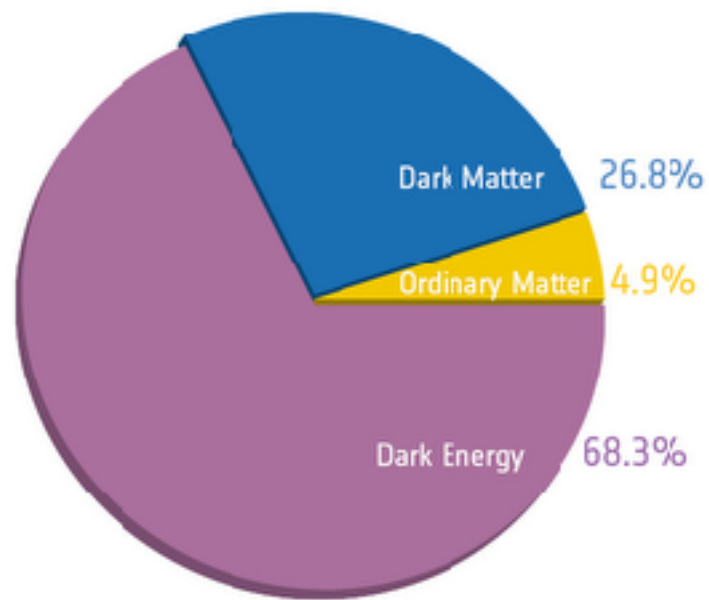


- Strong lensing results in multiple images or rings of background galaxies.
- Strong lensing probes significantly smaller scales and larger over densities.
- Strong lenses are very rare in comparison to weakly lensed galaxies.



# Weak Gravitational Lensing

## Dark Energy

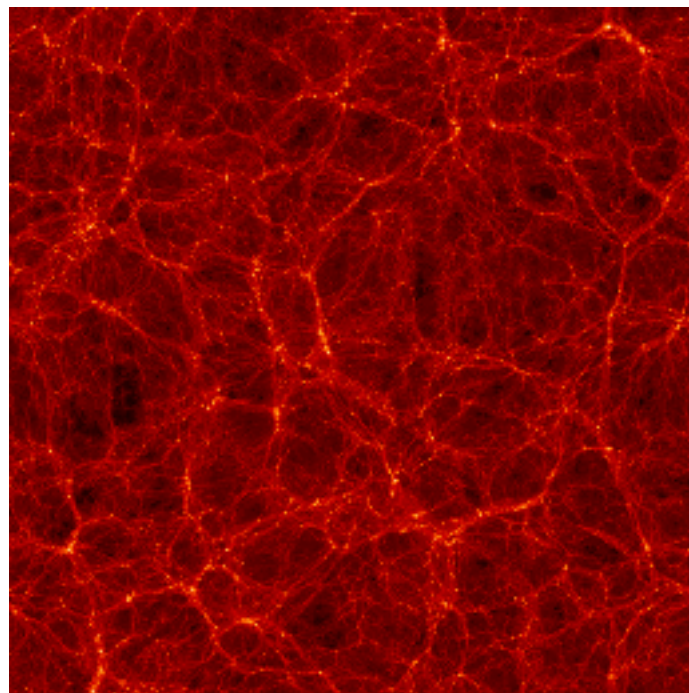


Why should you be interested in weak lensing (systematics)?

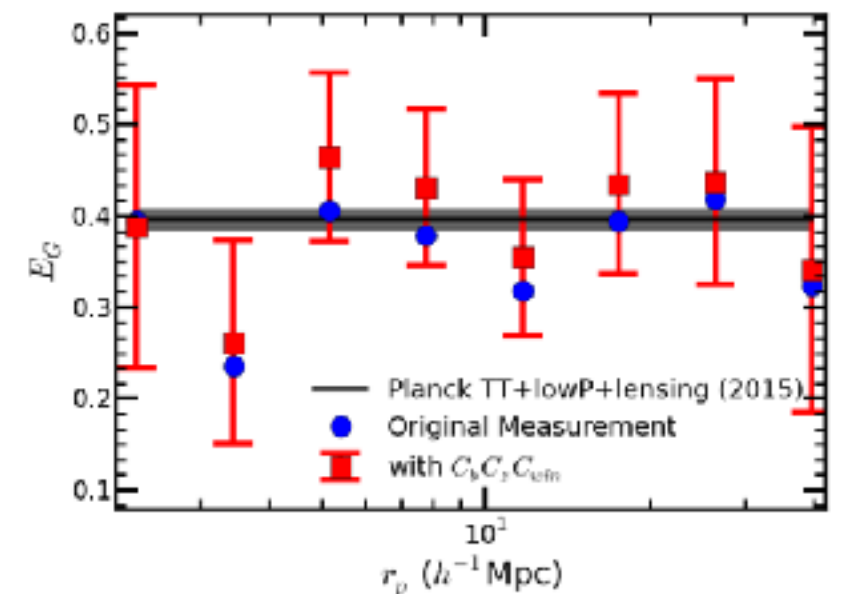
## Galaxy-Halo connection



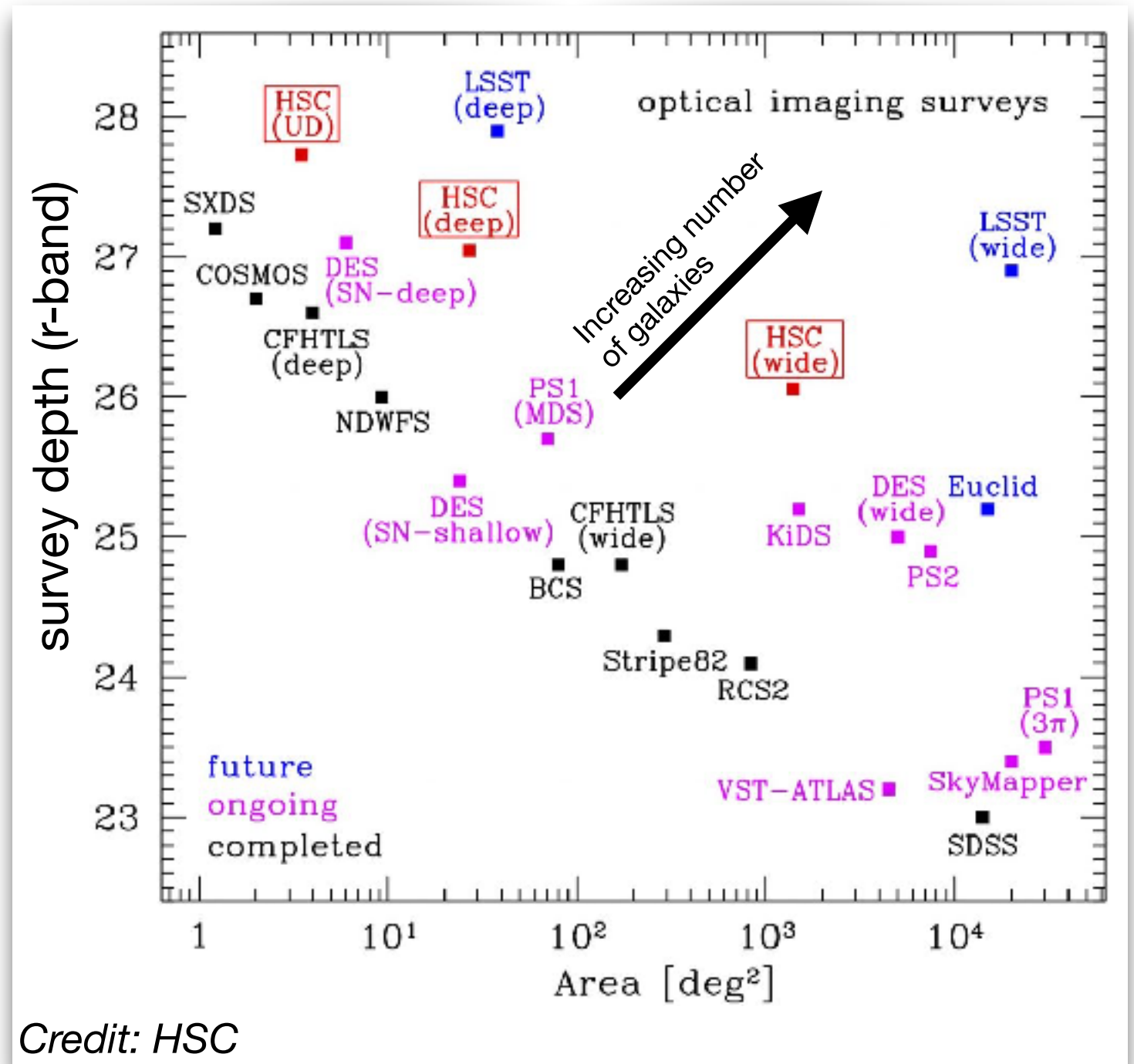
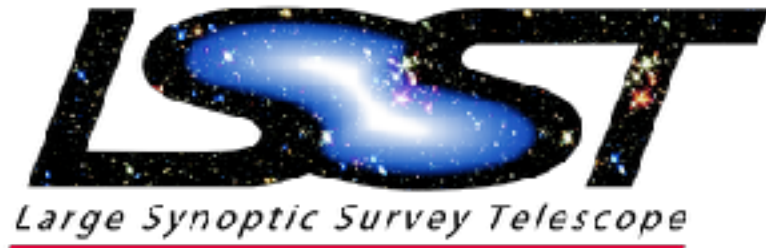
## Growth of Structure



## Testing of Gravity



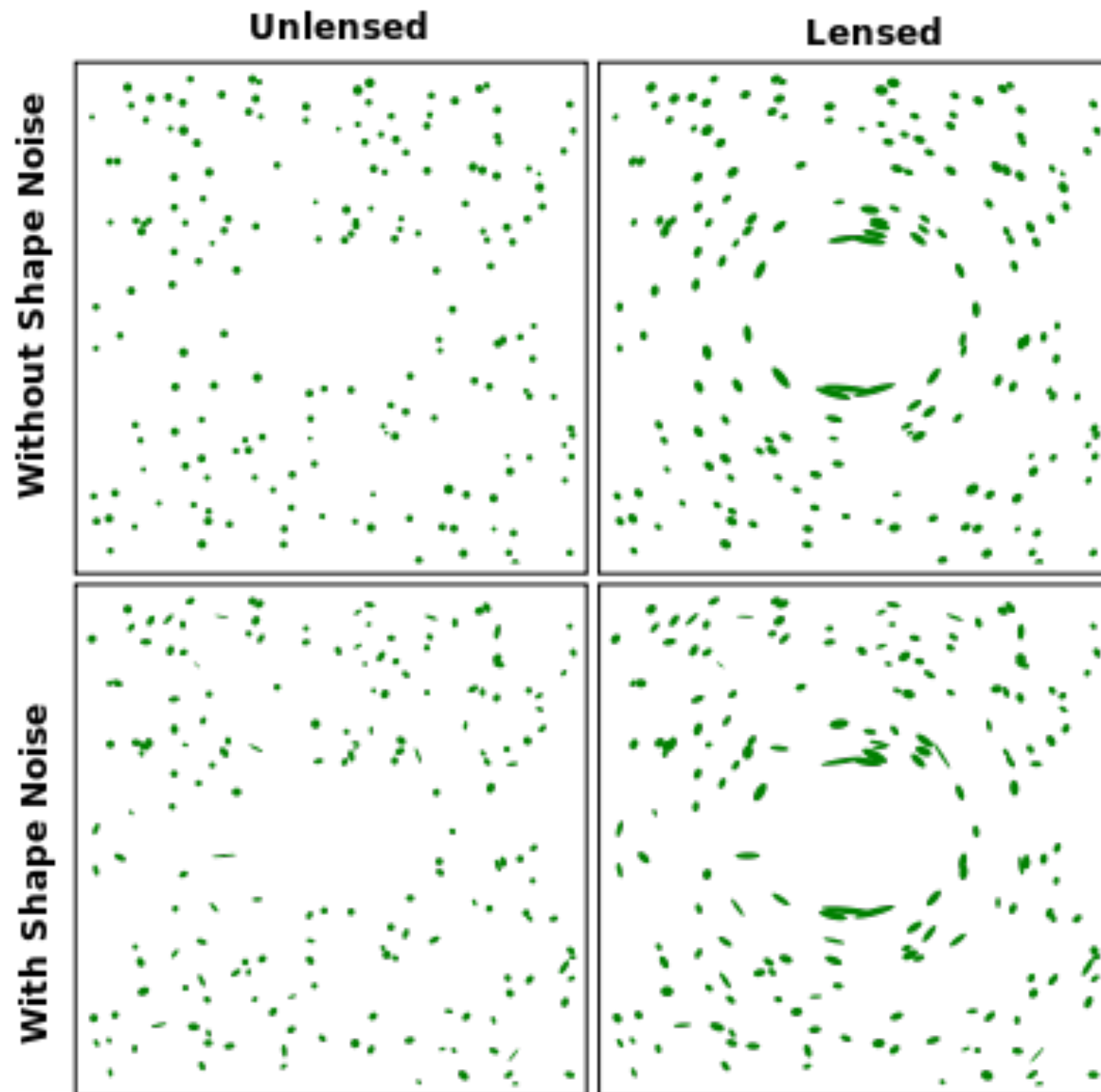
# Weak Lensing Surveys



Statical power of surveys must be matched by increasing control of astrophysical and observational systematics.

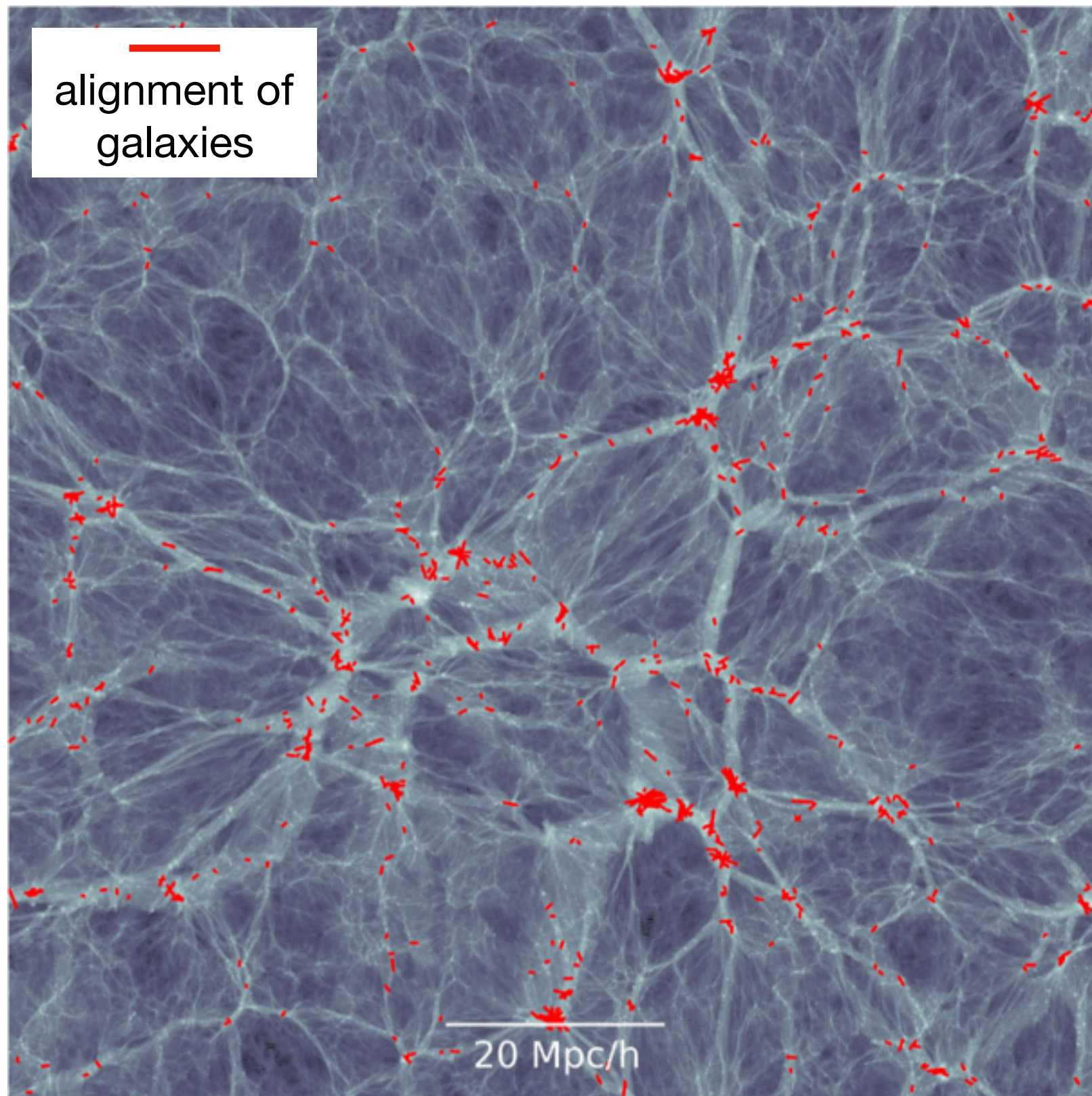


# Galaxy Shapes



- Weak lensing induces ellipticities of  $\sim 0.001$
- Intrinsic shapes of galaxies have ellipticities of  $\sim 0.1$
- Shape noise is overcome by measuring shapes of many ( $\sim 1000$ ) galaxies

# Intrinsic Alignments



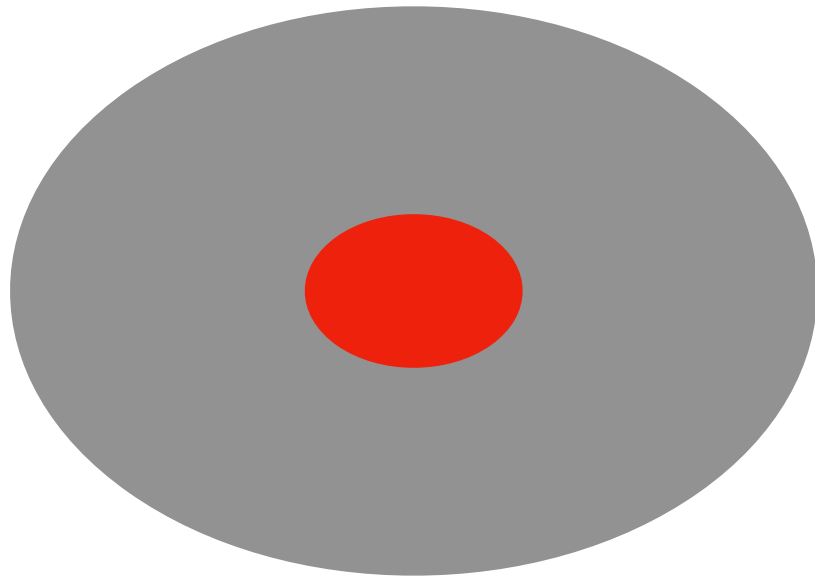
Tenneti + 2015

Hydrodynamic simulations of galaxy formation show intrinsic alignments between galaxies and large scale structure.

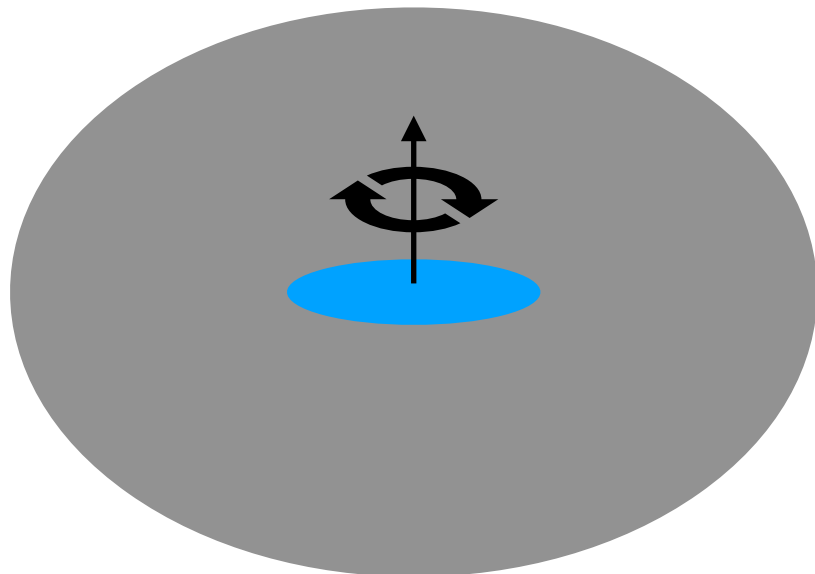
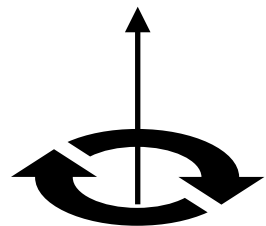
- Any correlated ellipticities not caused by lensing can contaminate lensing signals
- Galaxy alignments with large scale structure and other galaxies are seen in both simulations and observations!



# Physics of Intrinsic Alignments

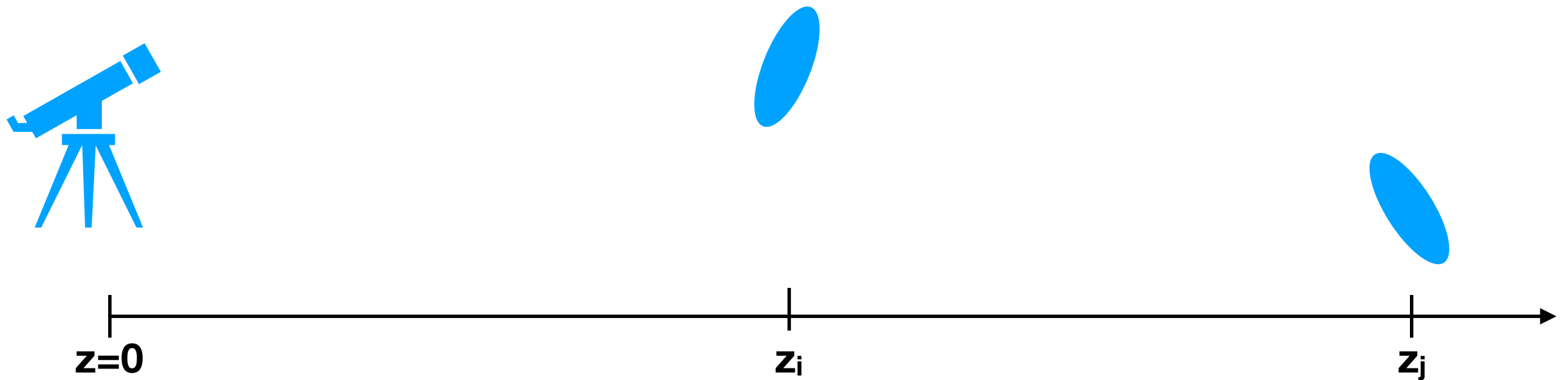


- Elliptical Galaxies (Early Type)
  - pressure supported systems
  - triaxial collapse of host halo in tidal field
  - galaxy follows halo shape



- Disk Galaxies (Late Type)
  - angular momentum supported systems
  - coupling of halo to quadrupole moment of tidal field at time of collapse
  - galaxy preserves angular momentum during formation
  - galaxy and halo spin axis align

# Intrinsic Alignments



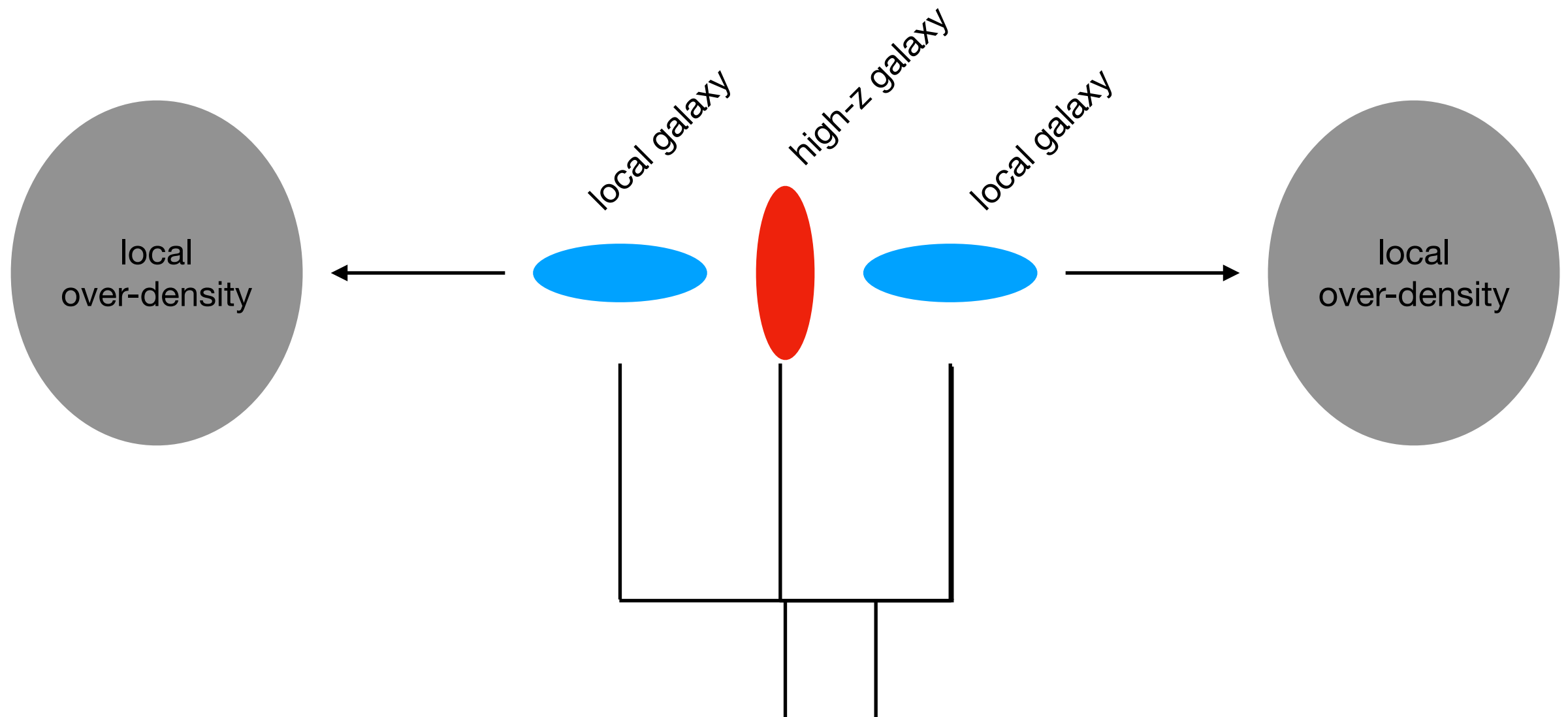
$\epsilon^I$  intrinsic ellipticity  
 $\epsilon$  observed ellipticity  
 $\gamma$  gravitational shear

observed shape  
correlation

$$\begin{array}{c}
 \text{observed shape correlation} \\
 \hline
 \langle \epsilon_i \epsilon_j \rangle = \underbrace{\langle \gamma_i \gamma_j \rangle}_{\text{cosmic shear}} + \underbrace{\langle \epsilon_i^I \epsilon_j^I \rangle}_{\text{II}} + \underbrace{\langle \gamma_i \epsilon_j^I \rangle}_{\text{zero if } z_j \gg z_i} + \underbrace{\langle \epsilon_i^I \gamma_j \rangle}_{\text{GI}}
 \end{array}$$



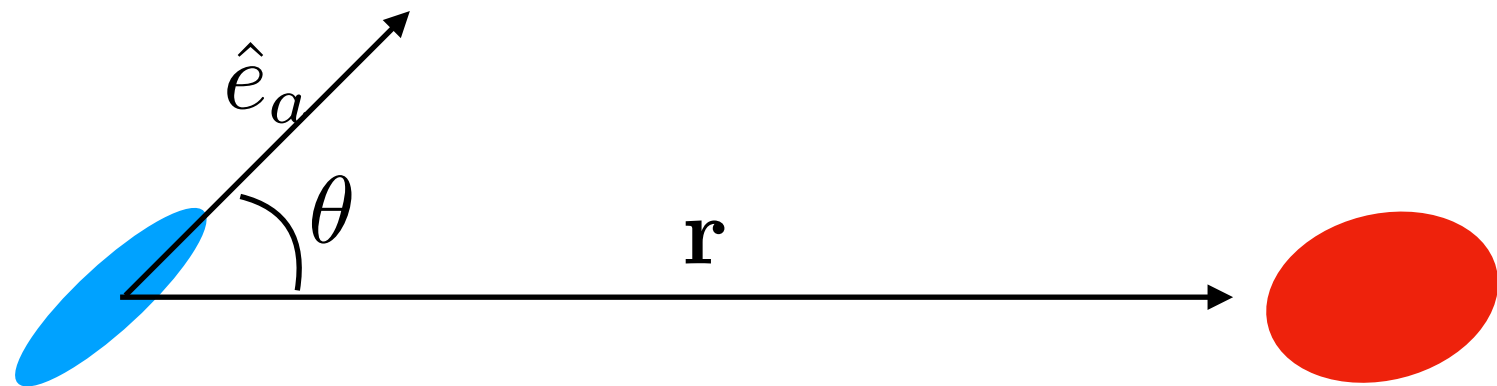
# Intrinsic Alignments



Intrinsic Alignments

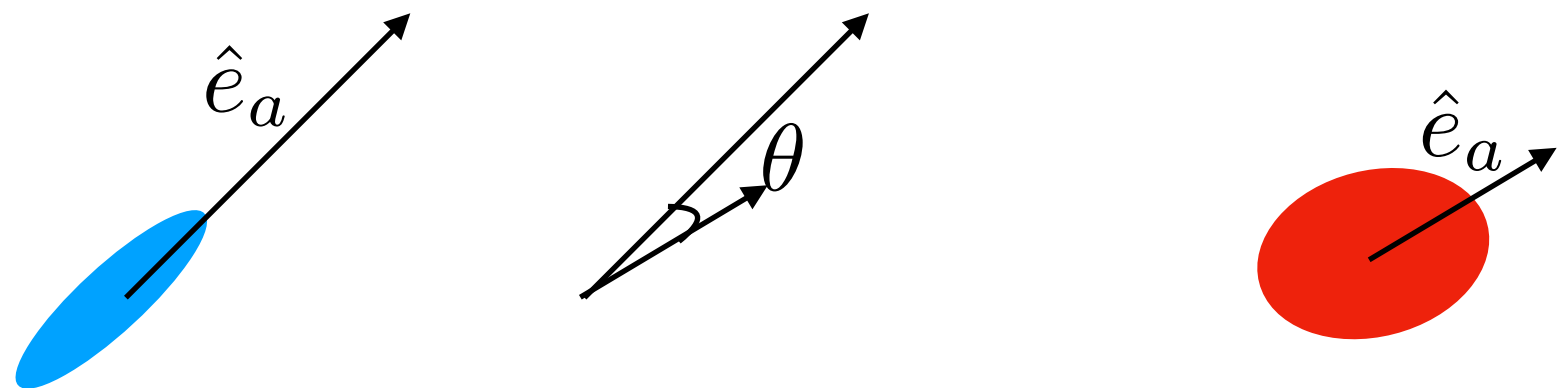
# Alignment Correlations

Ellipticity-Direction  
correlation (ED)



$$\omega(r) = \langle |\hat{e}_a(\mathbf{x}) \cdot \hat{\mathbf{r}}(\mathbf{x})|^2 \rangle - \frac{1}{3}$$

Ellipticity-Ellipticity  
correlation (EE)



$$\eta(r) = \langle |\hat{e}_a(\mathbf{x}) \cdot \hat{e}_a(\mathbf{x} + \mathbf{r})|^2 \rangle - \frac{1}{3}$$

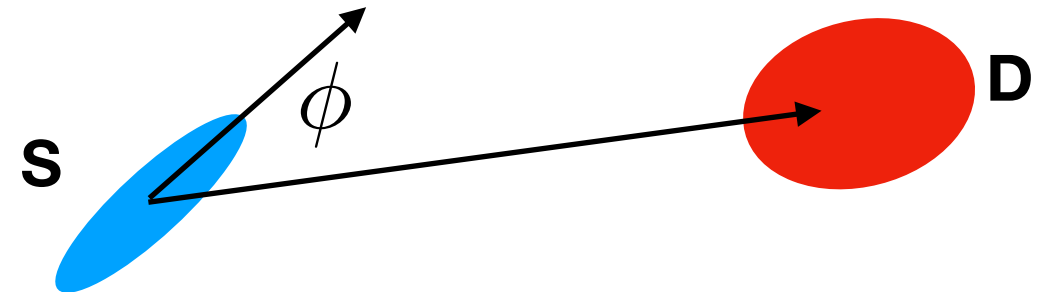


# Alignment Correlations

Gravitational shear-Intrinsic ellipticity correlation (GI)

$$\xi_{g+} = \frac{S_+ D - S_+ R_D}{R_S R_D}$$

$$S_+ X = \sum_{i \in S, j \in X} \gamma_+^{(i)} \langle j | i \rangle$$

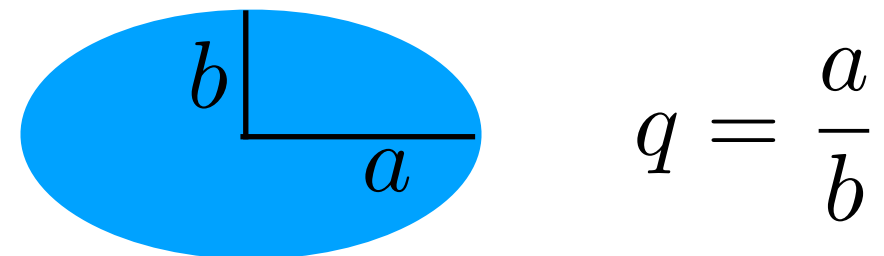


$$\gamma_+ = \frac{1 - q^2}{1 + q^2} \cos(2\phi)$$

Intrinsic-Intrinsic ellipticity correlation (II)

$$\xi_{++} = \frac{S_+ S_+}{R_S R_S}$$

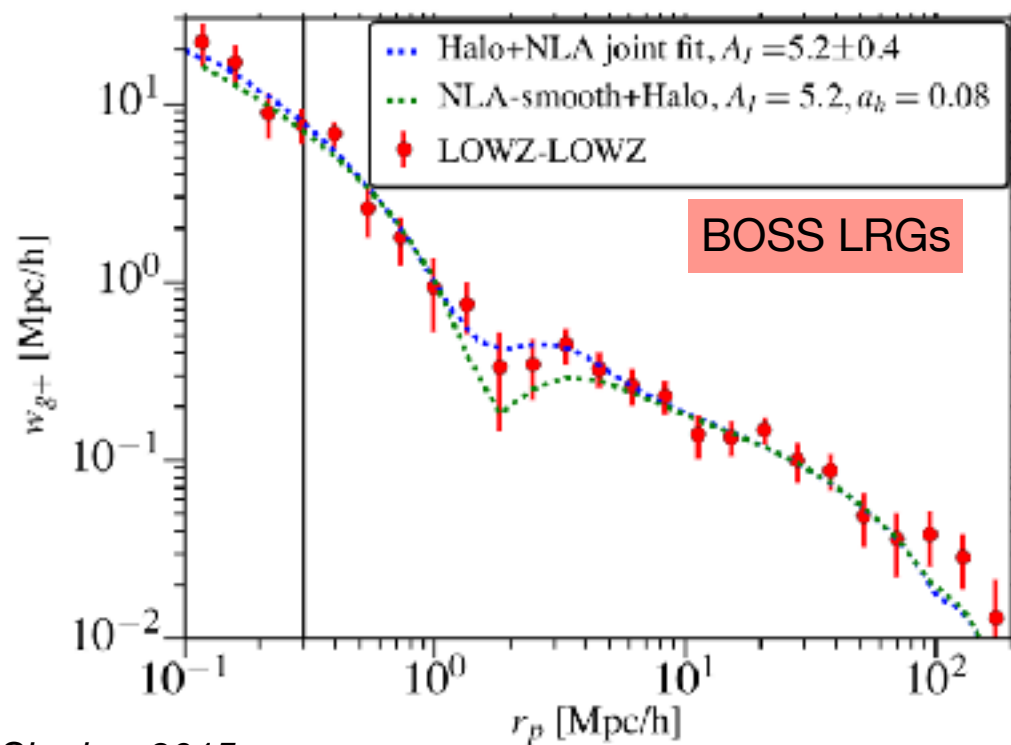
$$S_+ S_+ = \sum_{i \in S, j \in S} \gamma_+^{(i)} \gamma_+^{(j)} \langle j | i \rangle$$



**Correlations weighted by density and ellipticity**

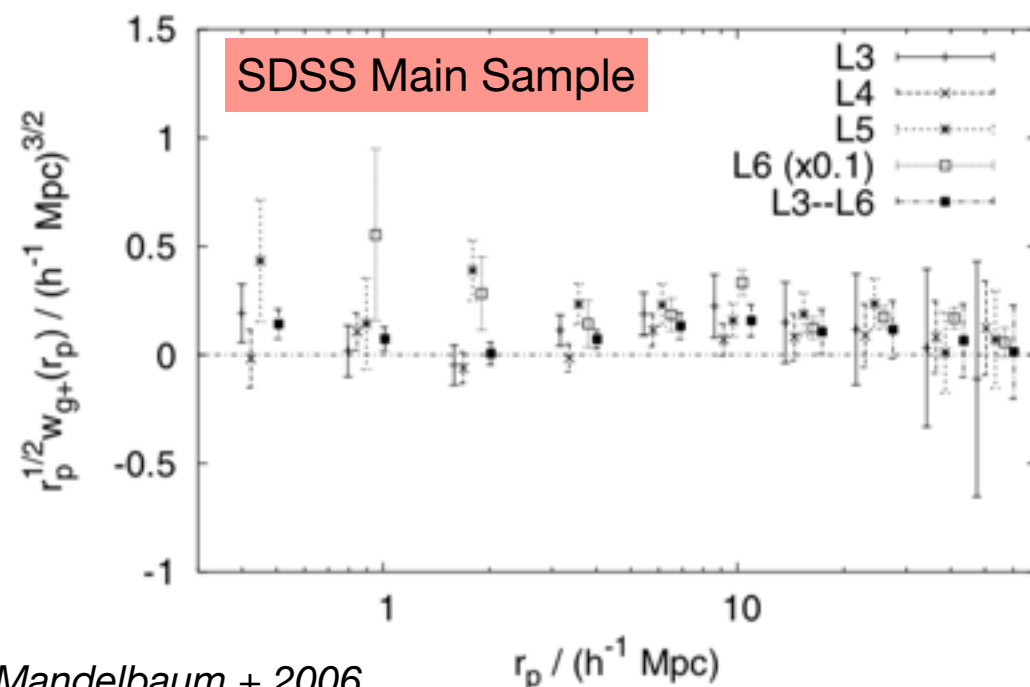
# Observations of Intrinsic Alignments

## GI correlations



Singh + 2015

## Galaxy-intrinsic shear correlation function



Mandelbaum + 2006

- Elliptical Galaxies (Early Type)
  - Consensus is that there are significant alignments
  - GI alignments are strong
  - II alignments are weak
- Disk Galaxies (Late Type)
  - most measurements are consistent with no alignments
  - How much alignment does the noisy data allow?
- Satellite Galaxies (Both)
  - Inconsistent results
  - Mounting indications for radial alignment within host halo



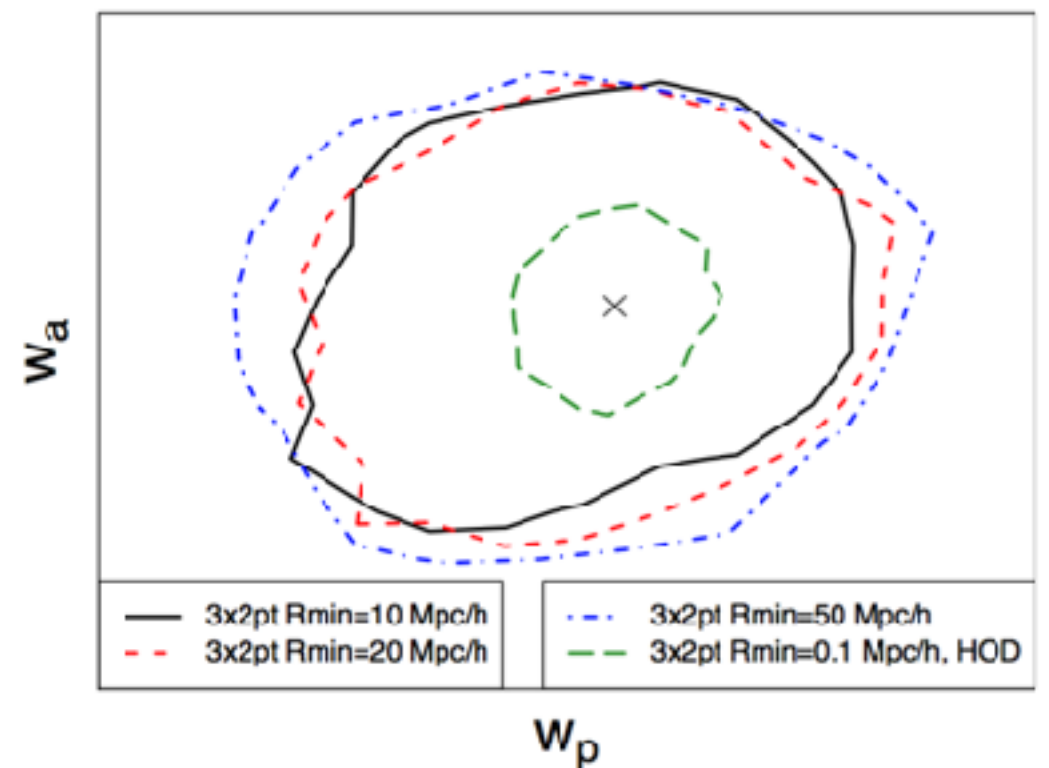
# Impact on Cosmological Surveys

- Ignoring intrinsic alignments can bias parameters by  $\sim 10\%$
- The goal is to subtract and marginalize over uncertainty in IA

We would like:

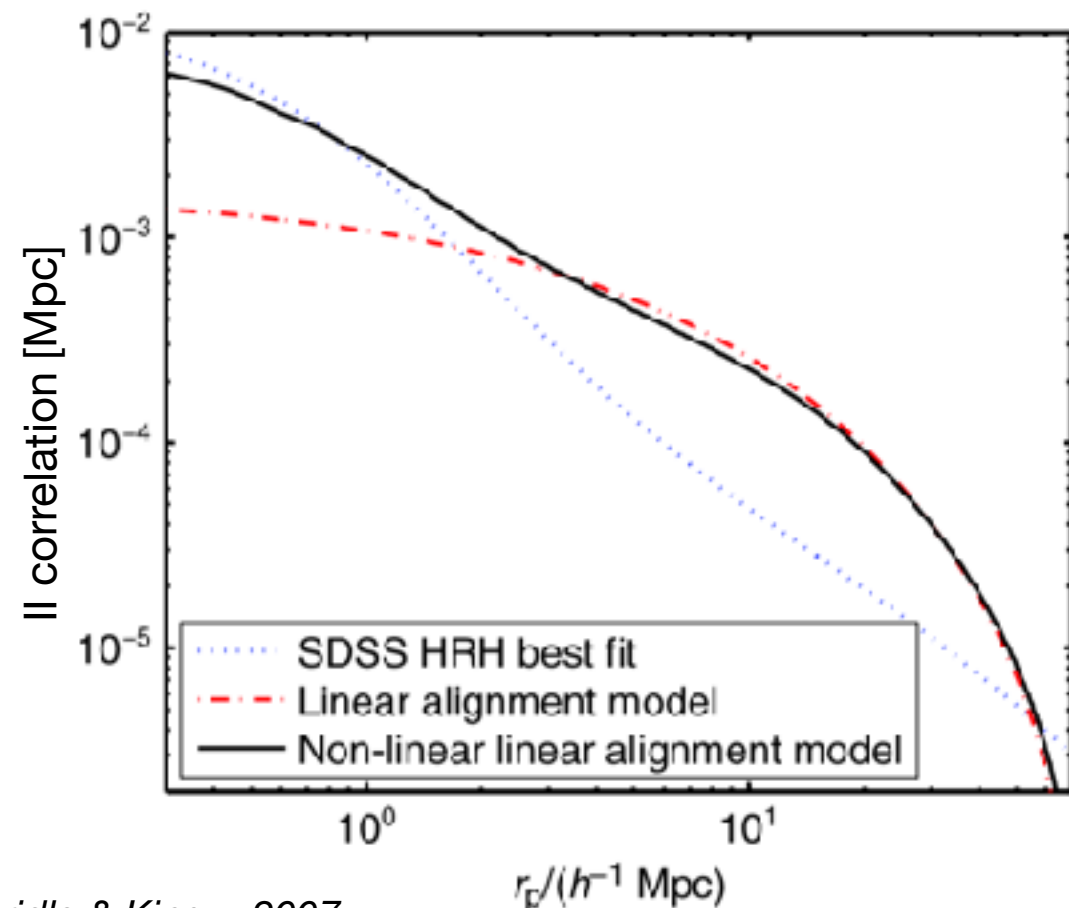
- physically motivated models for IA
- priors to go along with those models!
- the ability to create mock data sets in order to test cosmological parameter extraction from surveys
- model and therefore use small scale data
- learn about galaxy formation mechanisms

constraining dark energy

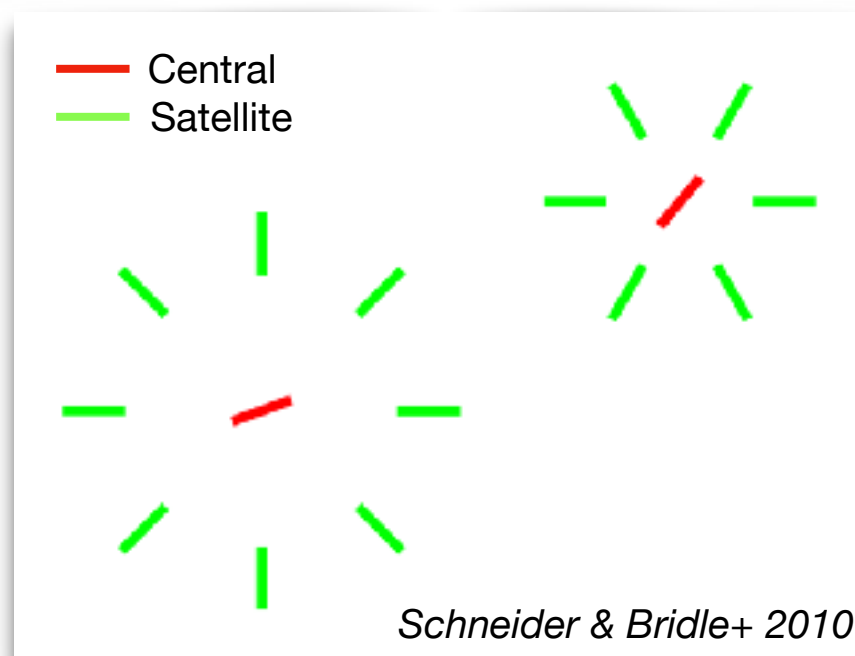


Krause & Eifler (2016)

# Mitigating Intrinsic Alignments



Bridle & King + 2007



Schneider & Bridle+ 2010

- Linear Alignment Model
  - Alignments set at formation time
  - Scaling of the linear power spectrum

$$P_{\tilde{\gamma}^I}^{\text{lin}}(k) = \frac{C_1^2 \bar{\rho}^2}{\bar{D}^2} P_{\delta}^{\text{lin}}(k) \quad \text{II}$$

$$P_{\delta, \tilde{\gamma}^I}^{\text{lin}}(k) = -\frac{C_1 \bar{\rho}}{\bar{D}} P_{\delta}^{\text{lin}}(k) \quad \text{GI}$$

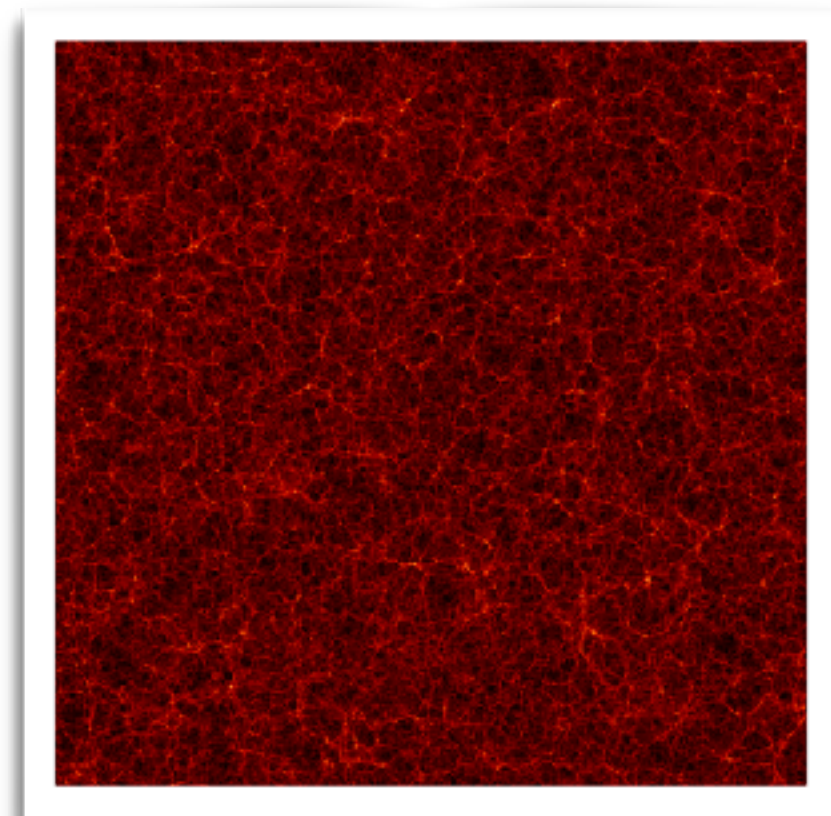
- Nonlinear Alignment Model
  - Uses nonlinear power spectrum
  - No physical motivation beyond linear model
- Schneider & Bridle Halo Model
  - Radial satellite alignments
  - Fitting function for 1-halo term

$$P_{\delta, \gamma_I}^{1h} = a_h \frac{(k/p_1)^2}{1 + (k/p_2)^{p_3}}$$



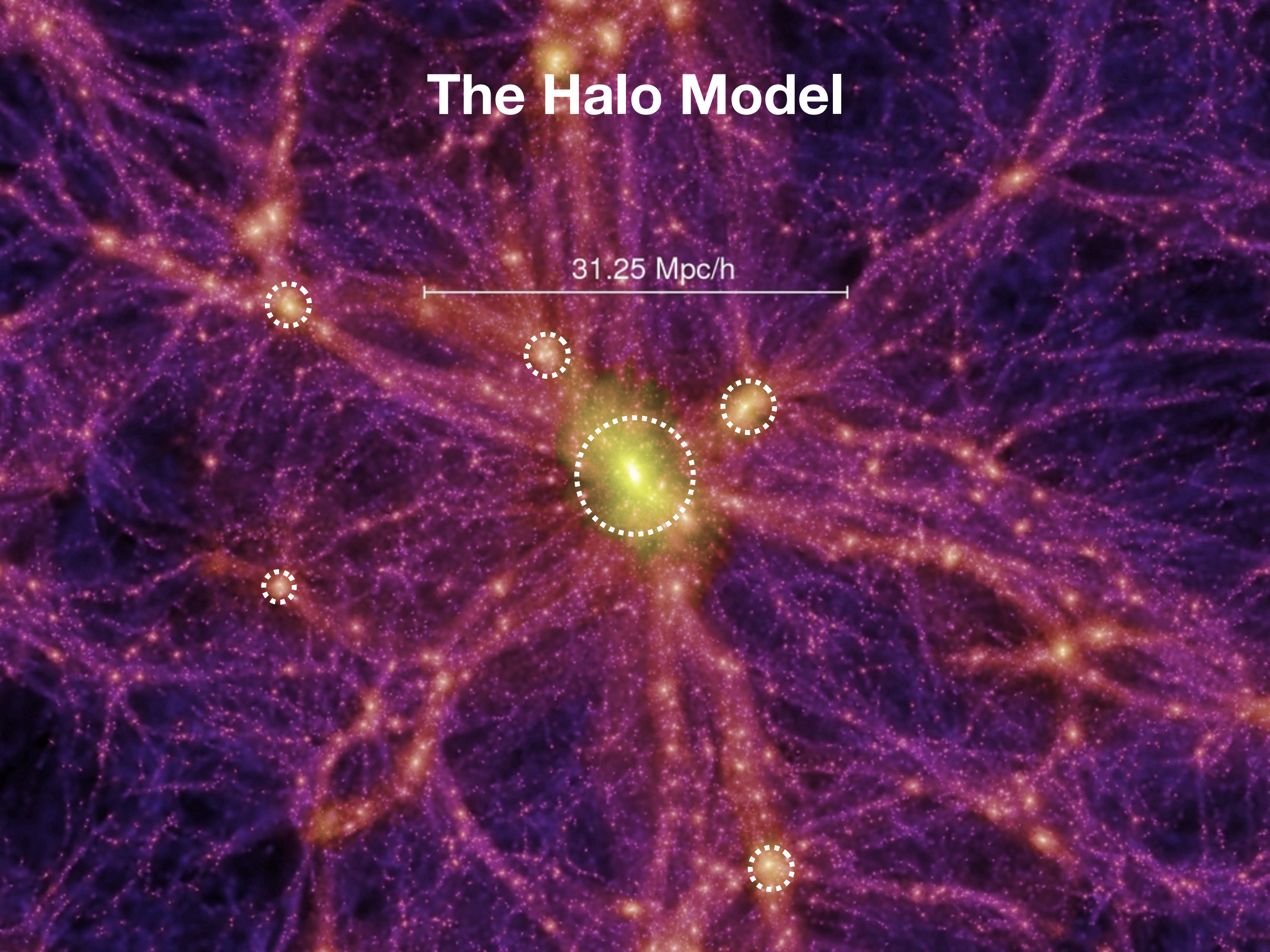
# Halo Model for IA

- Hydrodynamic simulations are too expensive for cosmological volumes
- (Non-)linear alignment models are crude, limited to  $>10$  Mpc scales
- Fitting functions provide no physical insight, no obvious way to scale for different galaxy samples
- No current model accounts for all small scale terms.
- A halo model can be used to build mocks, e.g. HOD, by populating large dark matter simulations
- A halo model naturally extends from small to large scales
- A halo model provides physical context for understanding IA



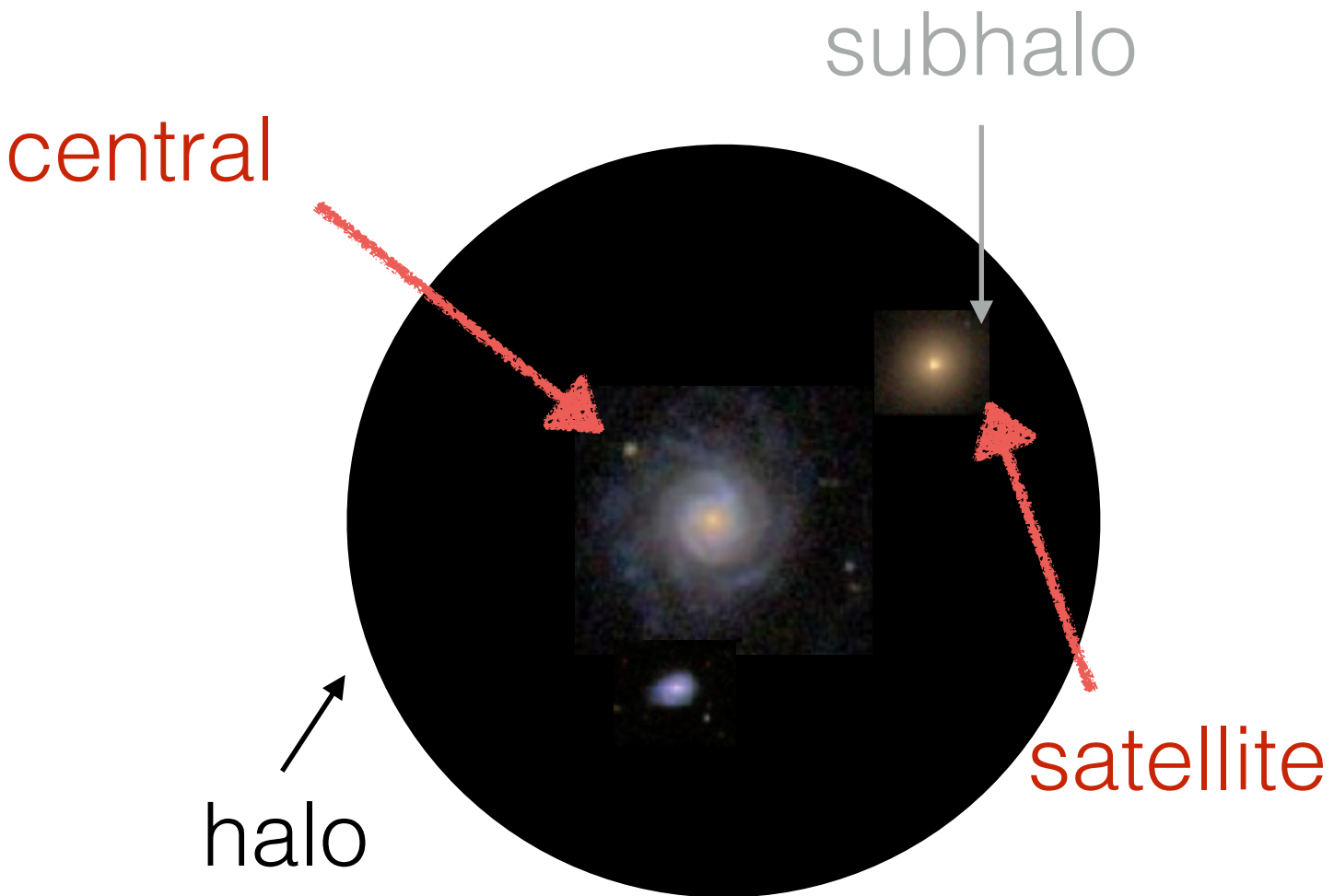


# The Halo Model





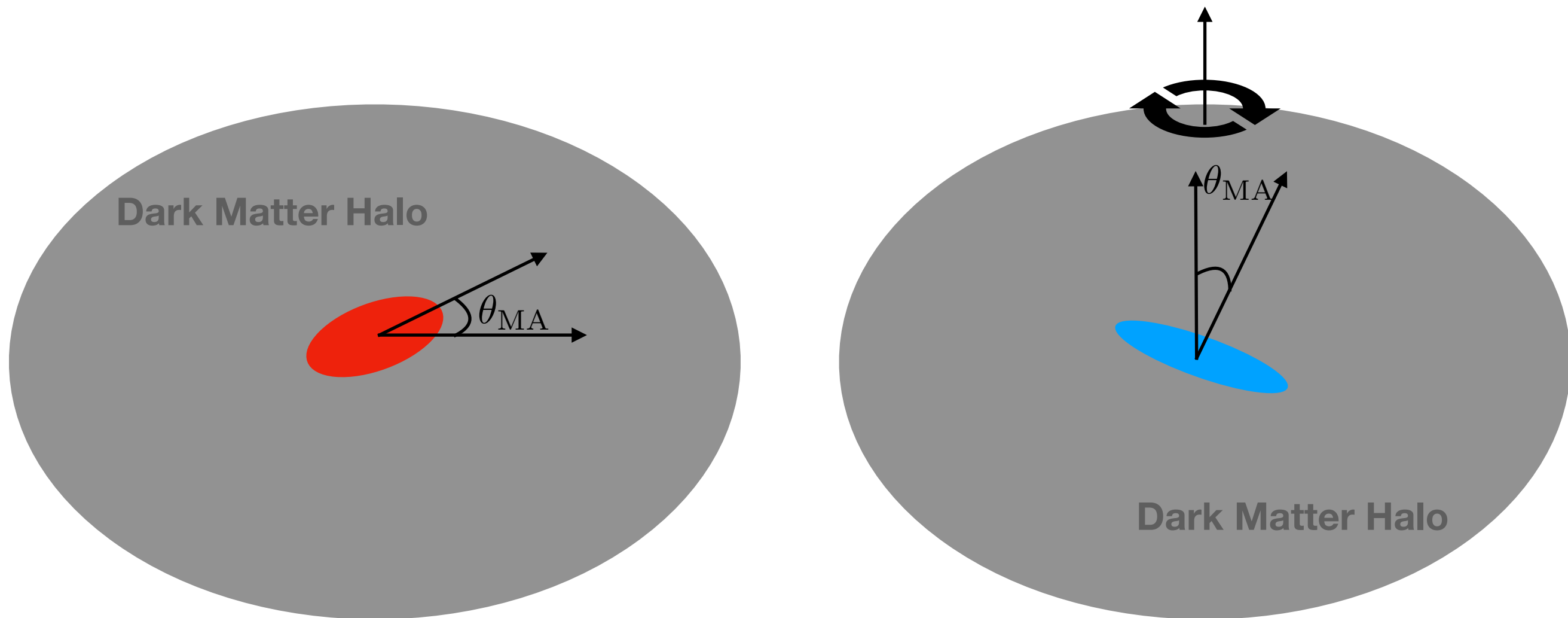
# The Halo Model



- Quasi-spherical haloes form in the large scale structure
- Haloes form hierarchically
- Previously distinct haloes become substructure in more massive haloes
- Galaxies form in haloes
- Massive central galaxies occupy the central regions of haloes
- Satellites live in sub-haloes



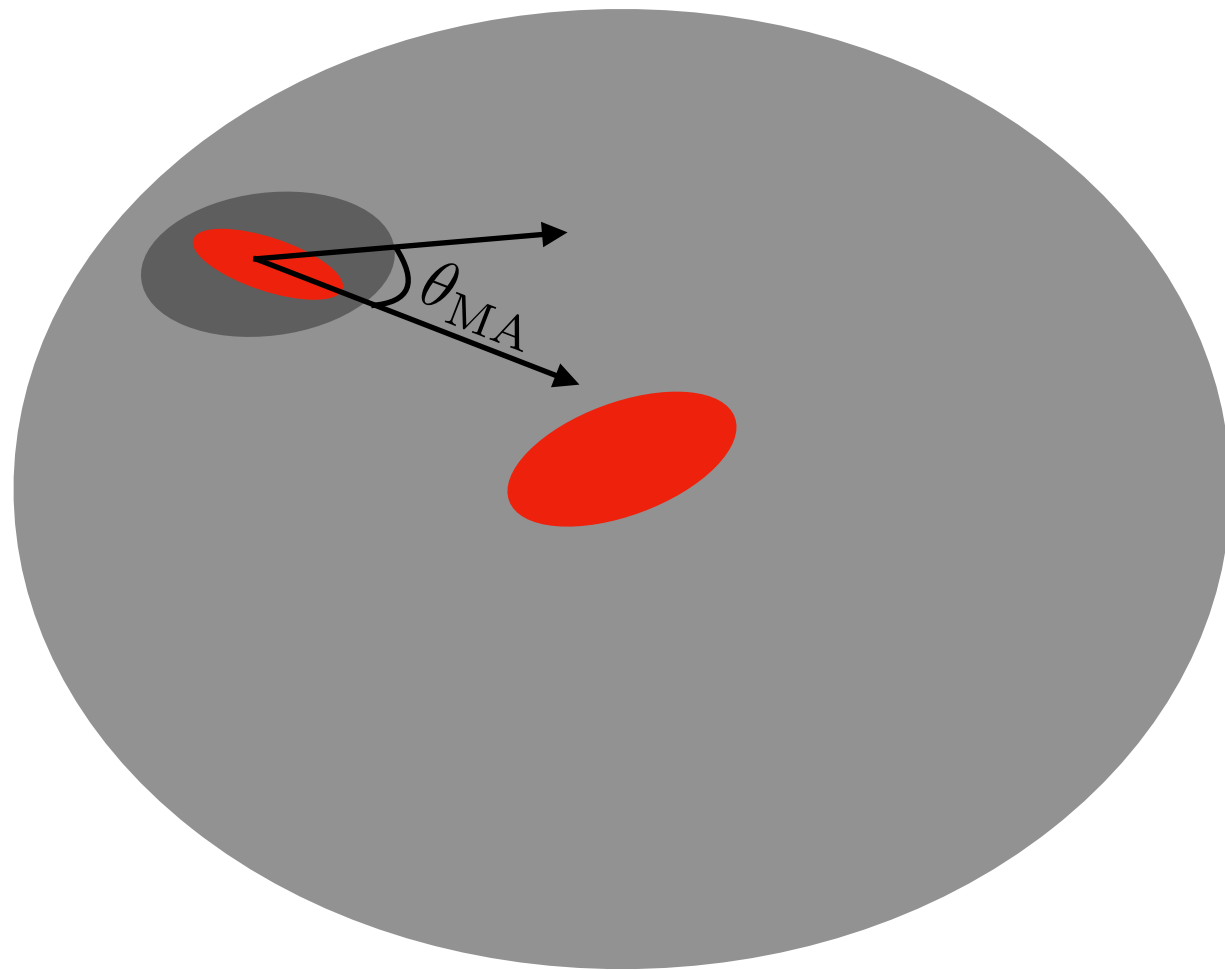
# Alignment Halo Model: Centrals



- define halo alignment vector
  - Halo major axis for elliptical galaxies
  - Halo spin axis for disk galaxies
- define galaxy alignment vector
  - major/minor axis
  - spin axis
- specify distribution of misalignments

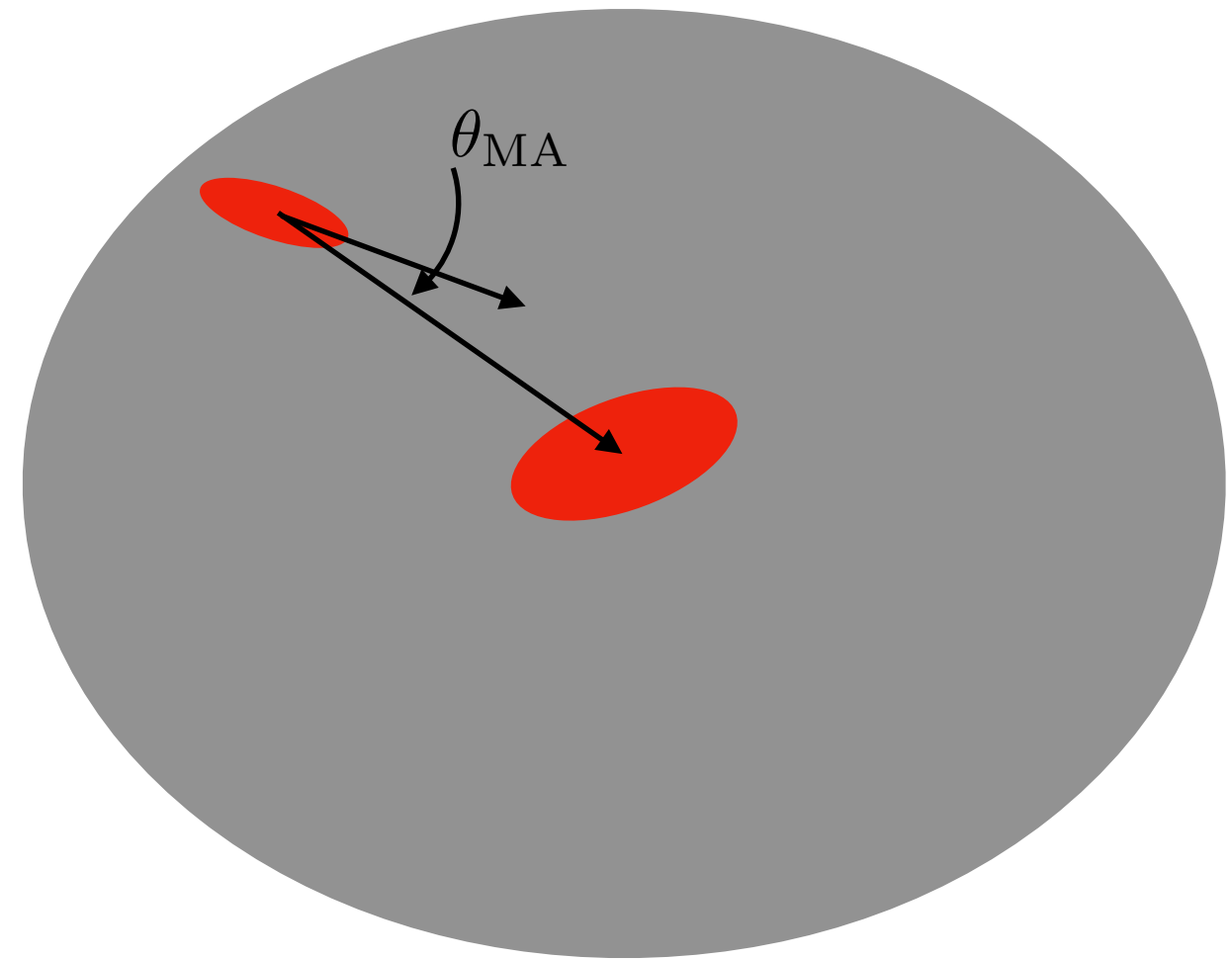
# Alignment Halo Model: Satellites

With sub-haloes



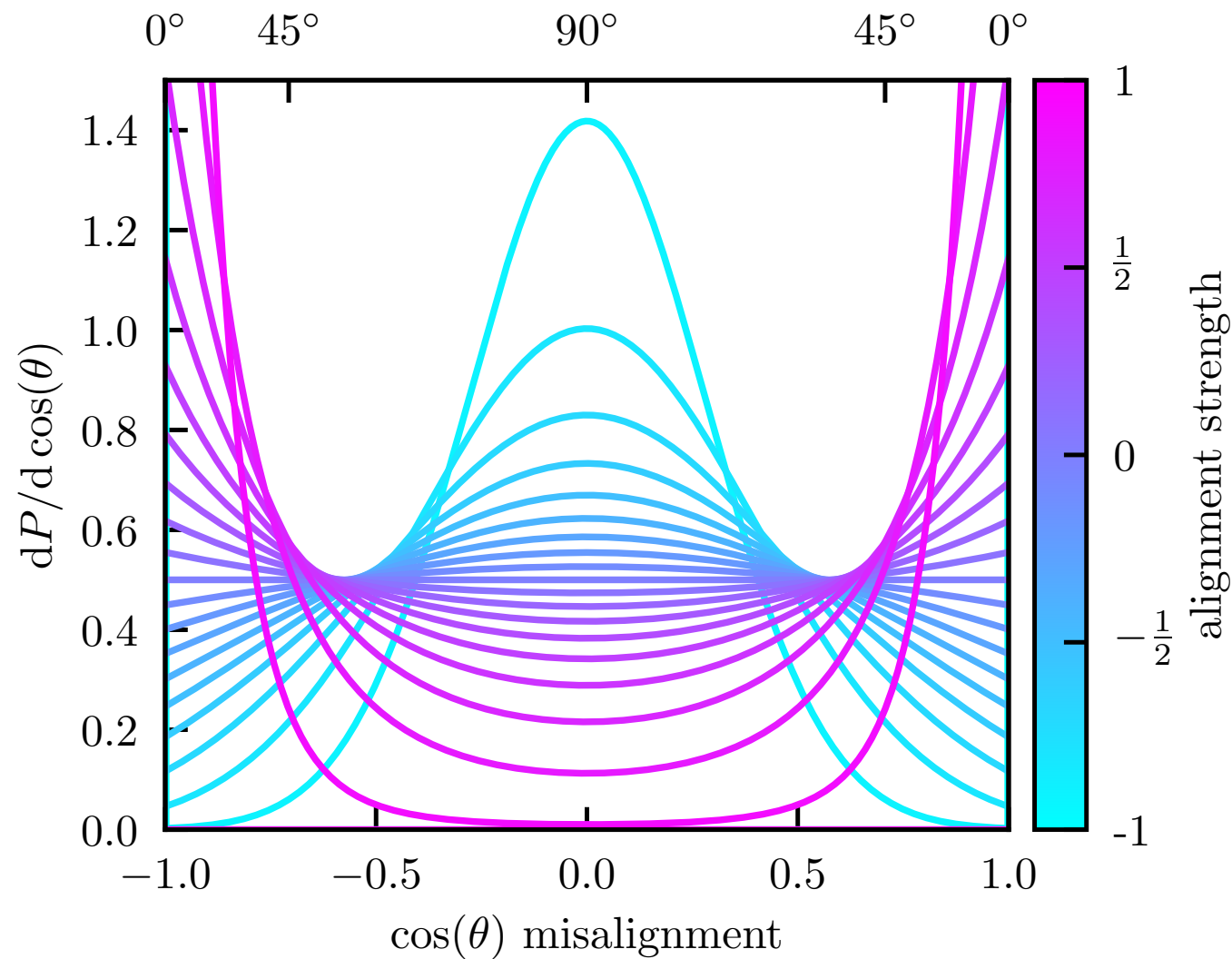
- use sub-halo orientations
- limited to use in 'high resolution' simulations

Without sub-haloes



- use host-satellite radial vector
- can be scaled up to large simulations

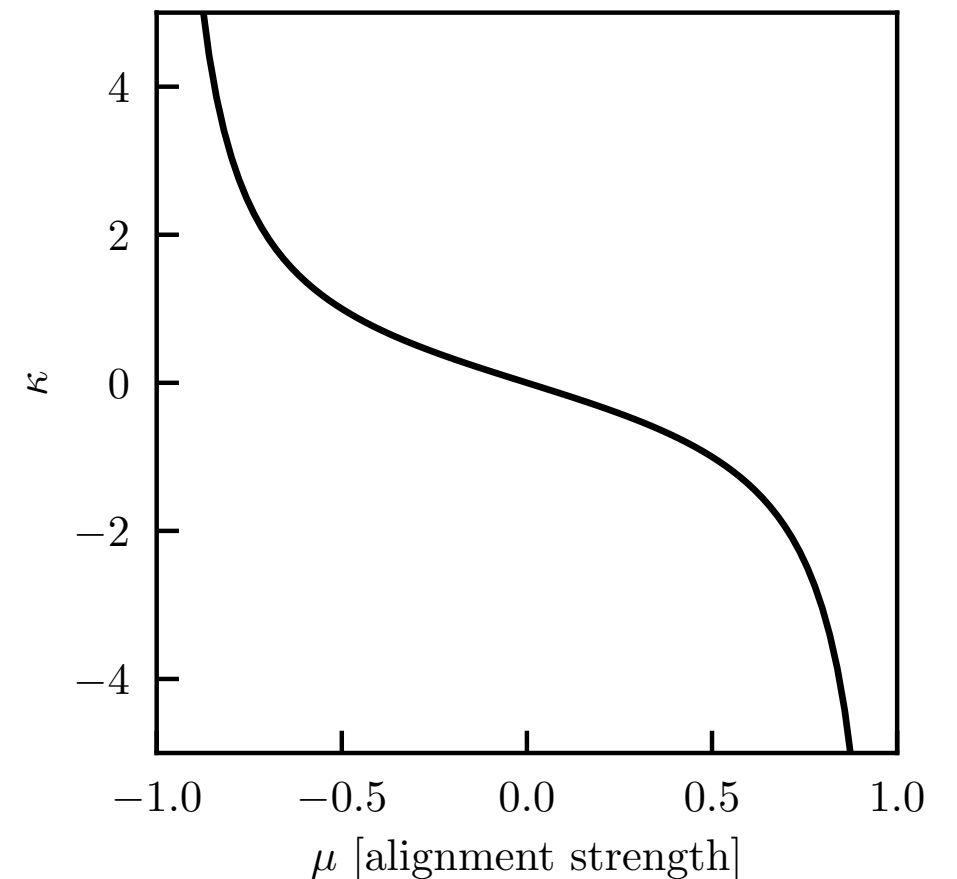
# Misalignment Model



## Watson Distribution

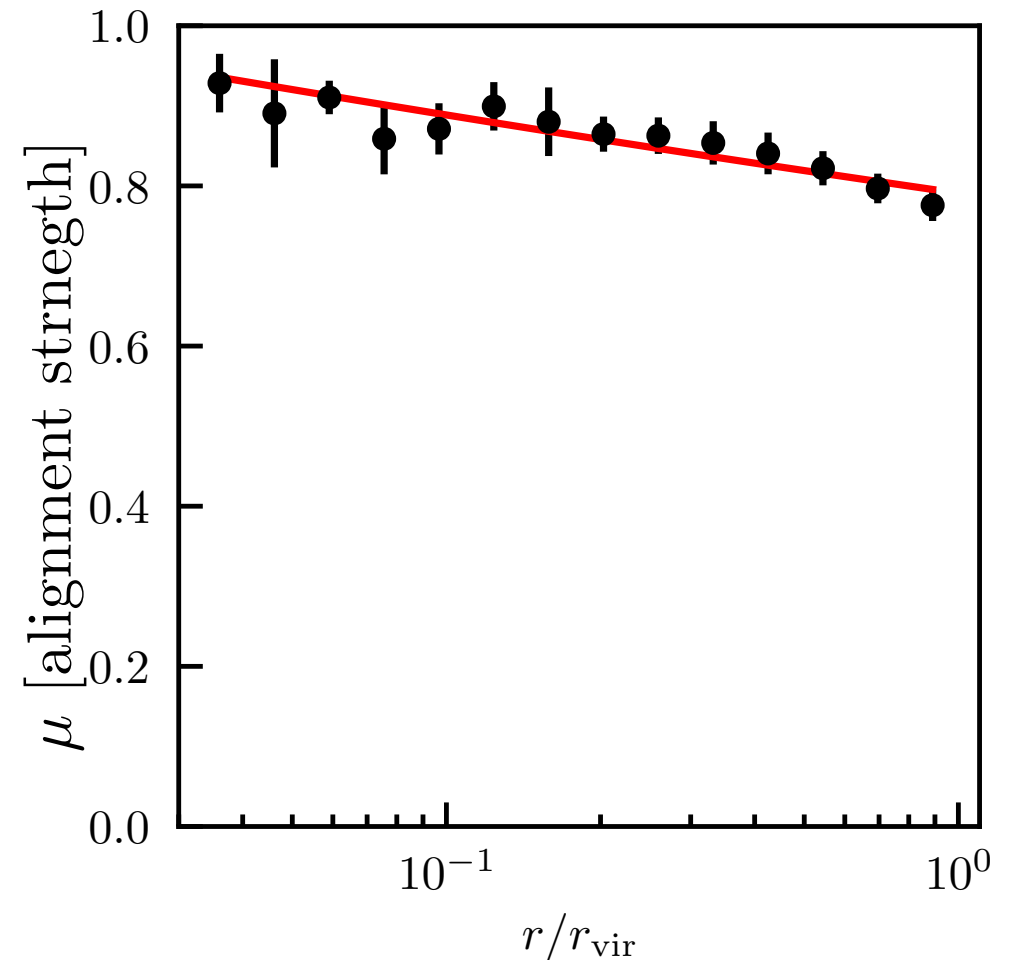
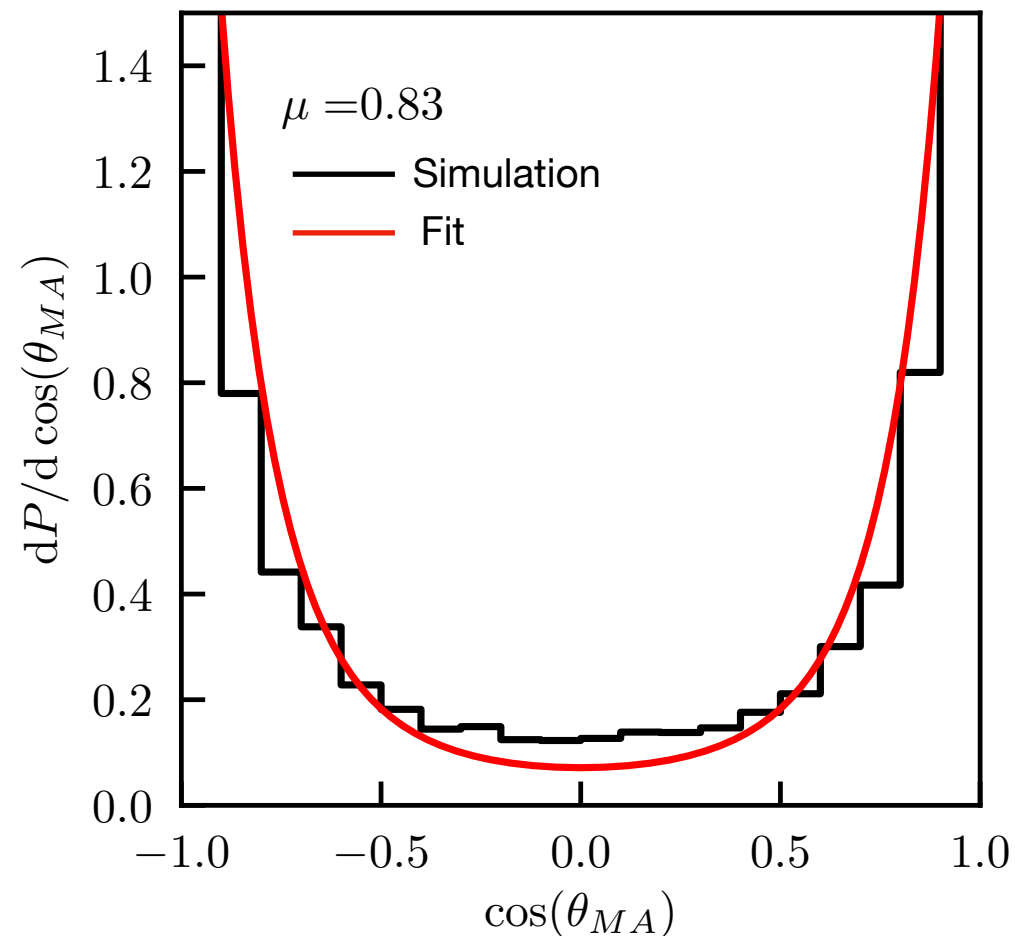
$$P(\theta, \phi) = \frac{B(\kappa)}{2\pi} e^{-\kappa \cos^2 \theta} \sin \theta d\theta d\phi$$

Parameterize the alignment strength





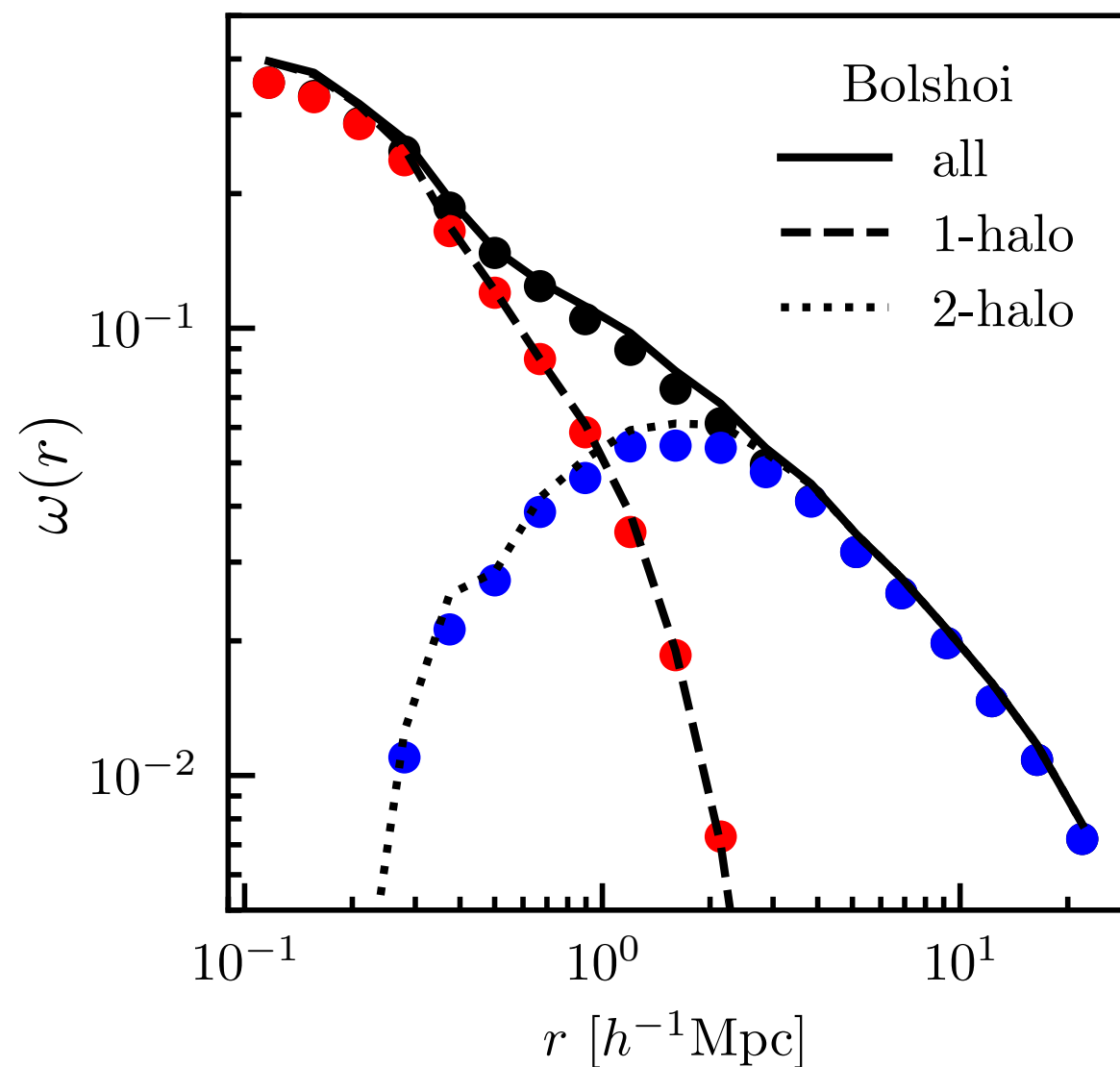
# Subhalo Alignments



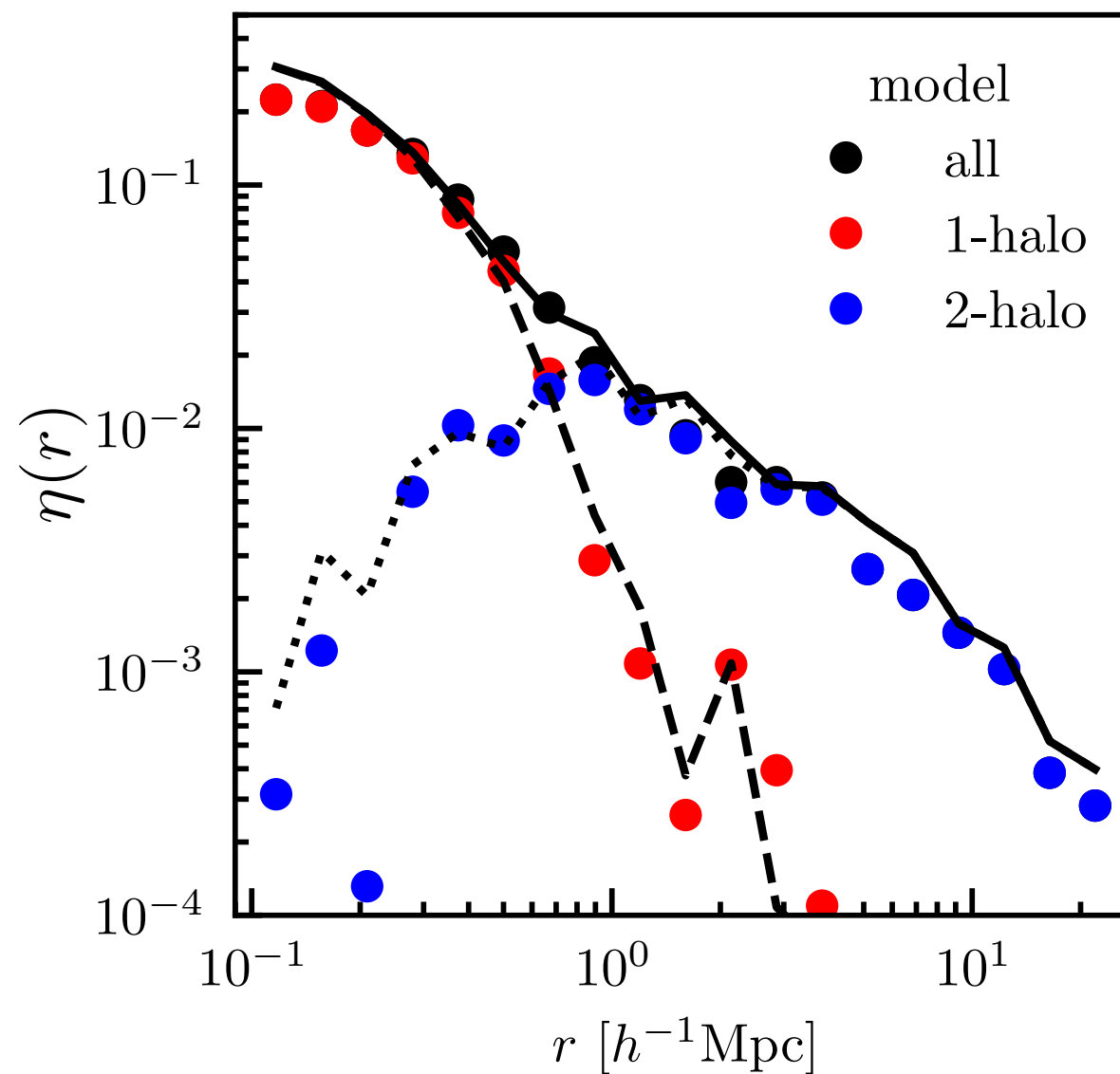
- Sub-haloes display strong radial alignment.
- Distribution of misalignment angles is fit well by a Watson distribution.
- Some radial dependence is seen in alignment strength within haloes.

# Subhalo Alignments

ED correlation

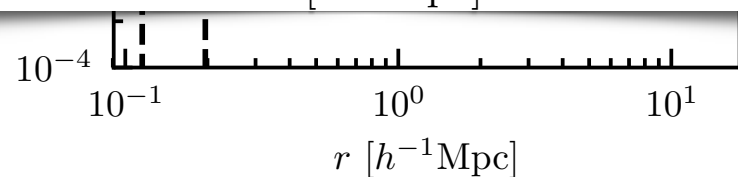
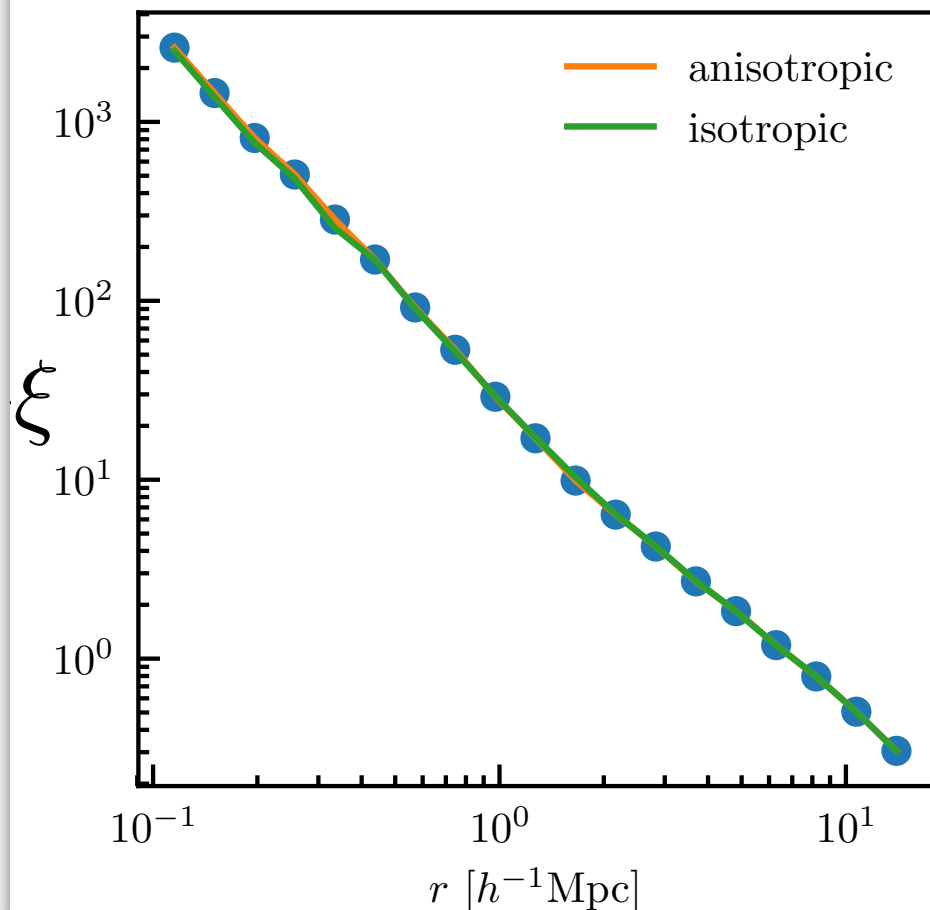
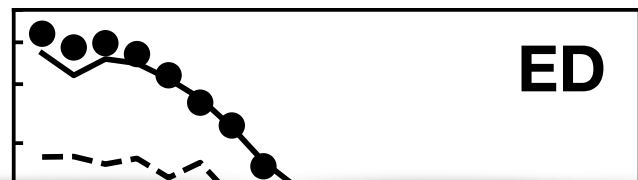


EE correlation

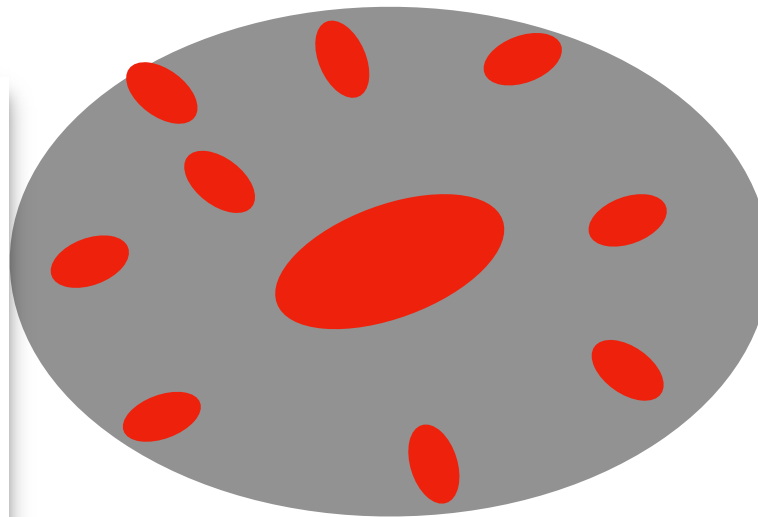


A radial alignment model can reproduce  
1-halo alignment correlations down to  $\sim 100$  kpc!

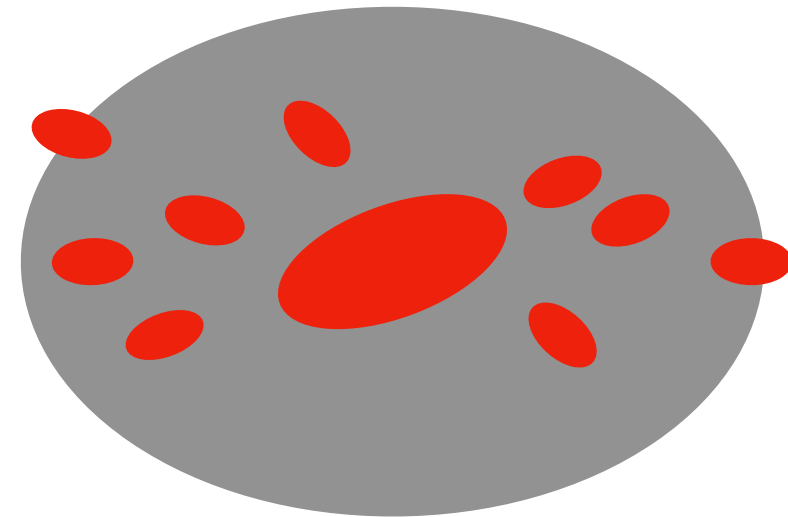
# Sub-halo Anisotropy



Isotropic Distribution

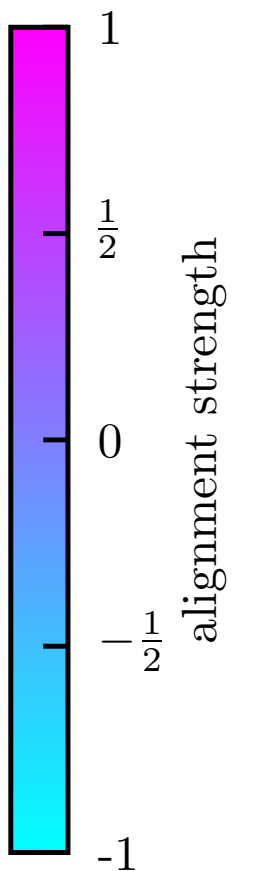
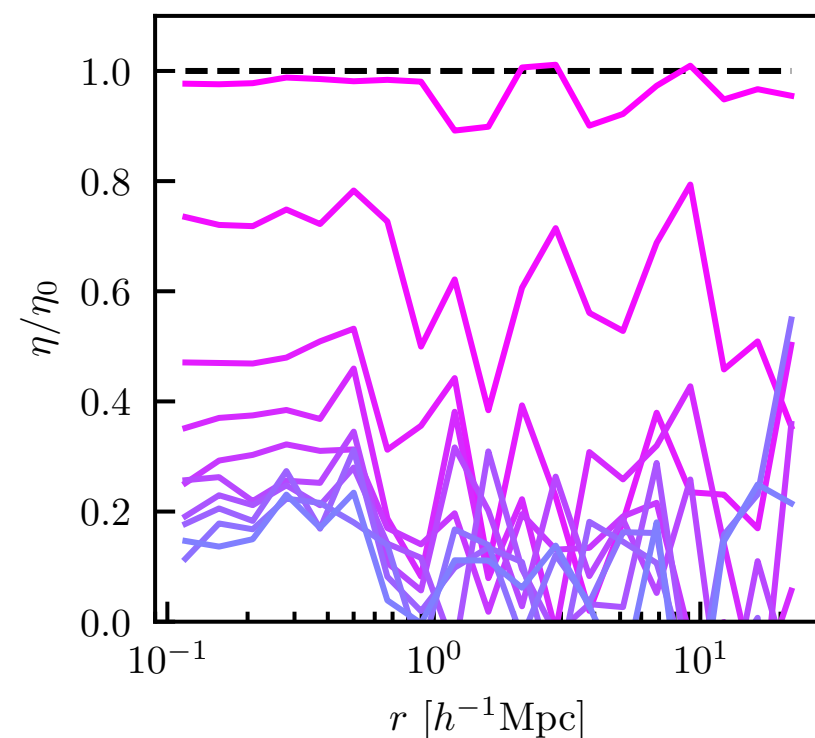
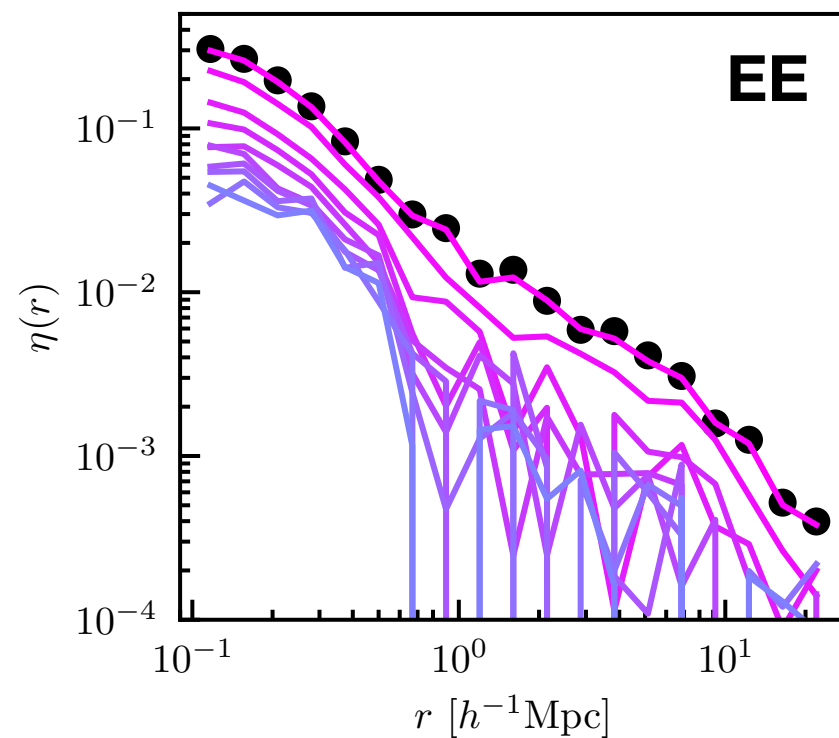
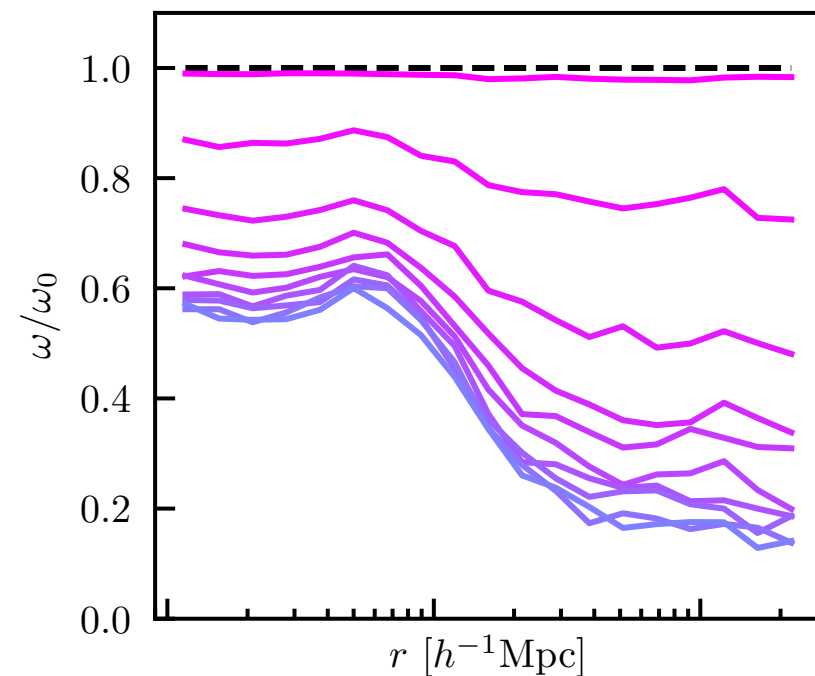
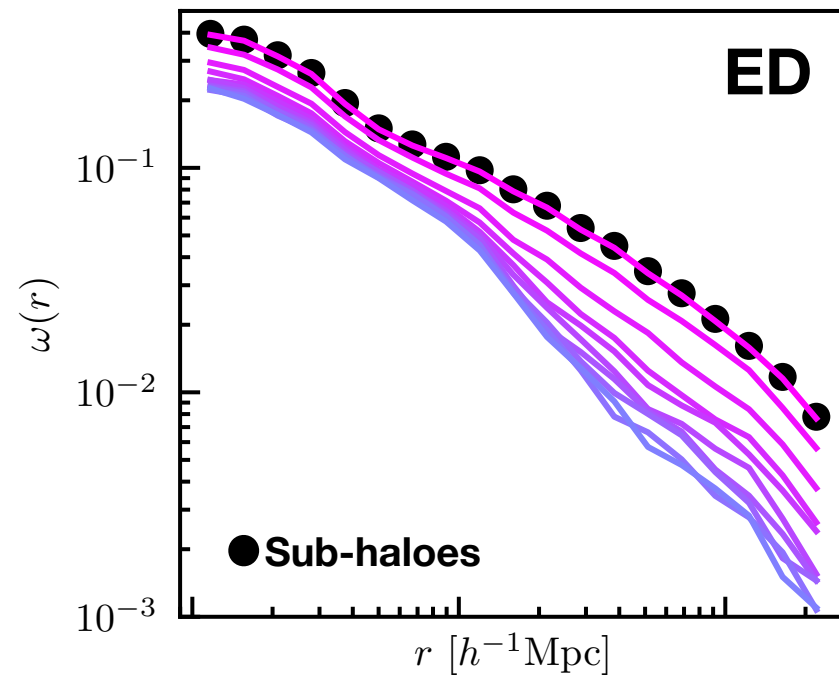


Anisotropic Distribution



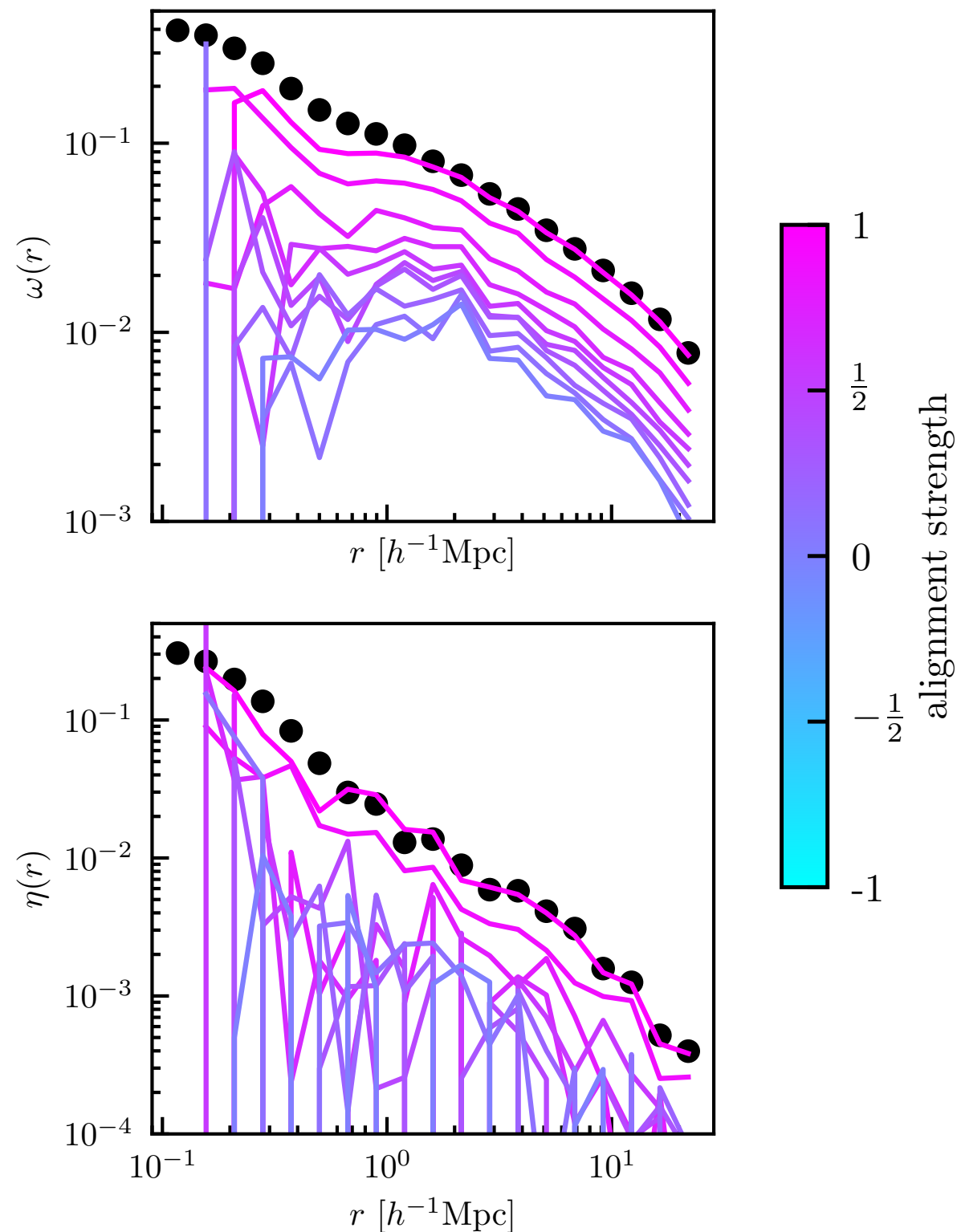
- Spatial distribution of satellites has a significant effect on IA correlations
- EE correlation function is especially sensitive to anisotropy
- EE will go to zero for an isotropic radial model
- Large scale correlations show effect of  $\sim 10\%$  due to satellite anisotropy

# Scale Dependence: Central IA



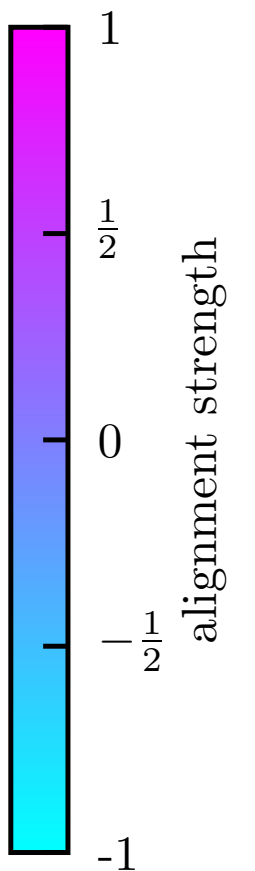
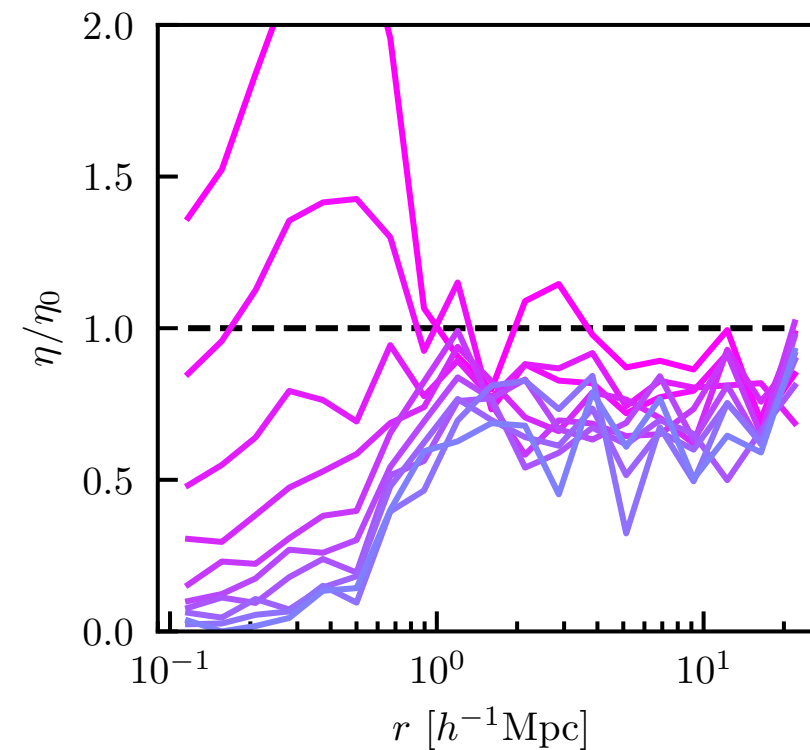
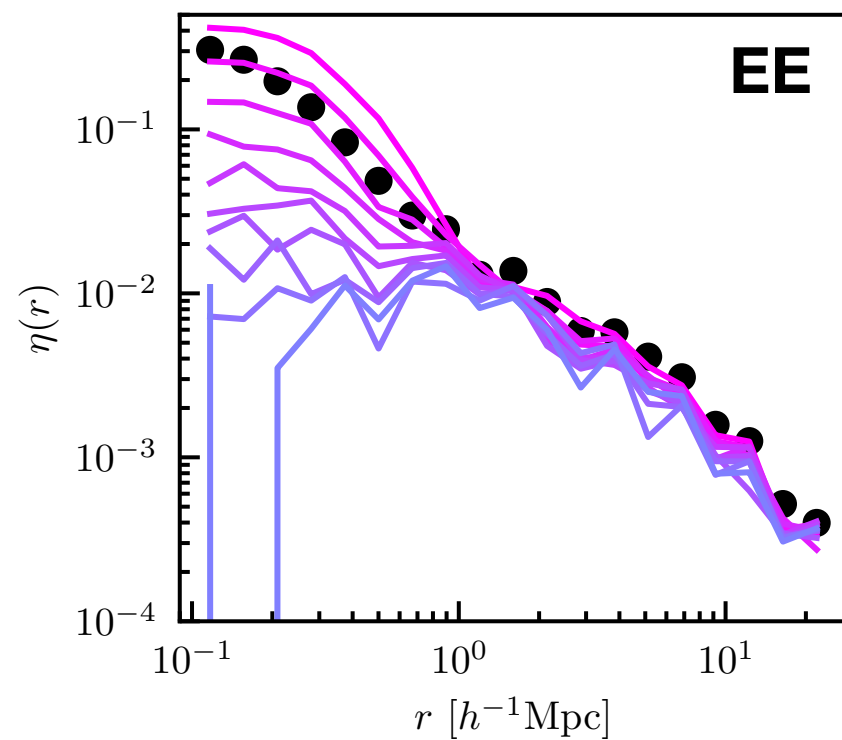
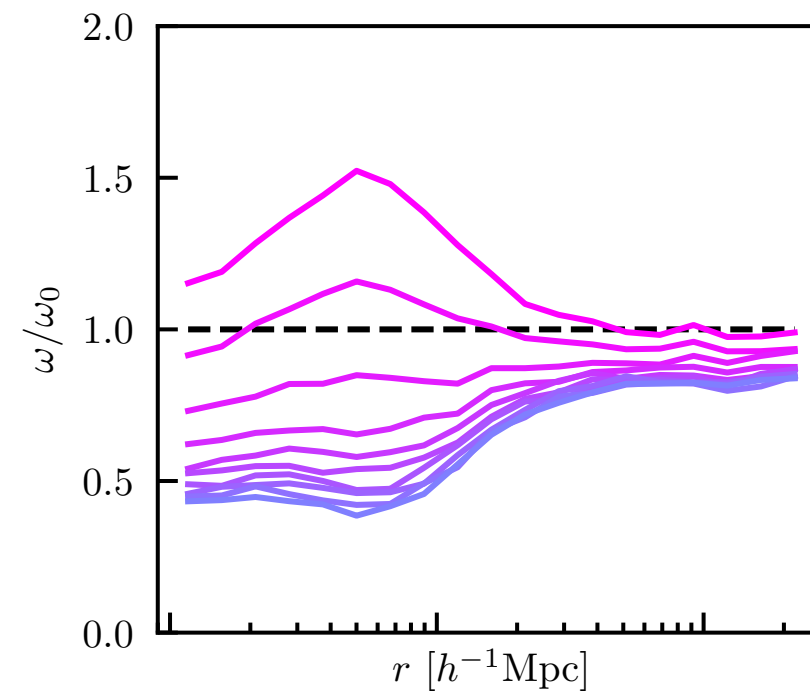
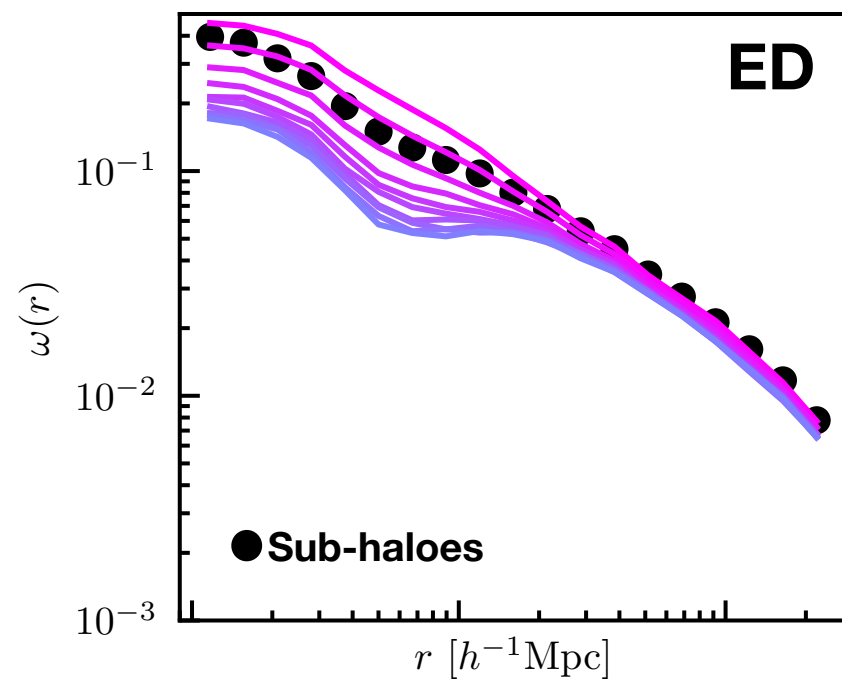


# Scale Dependence: Central IA



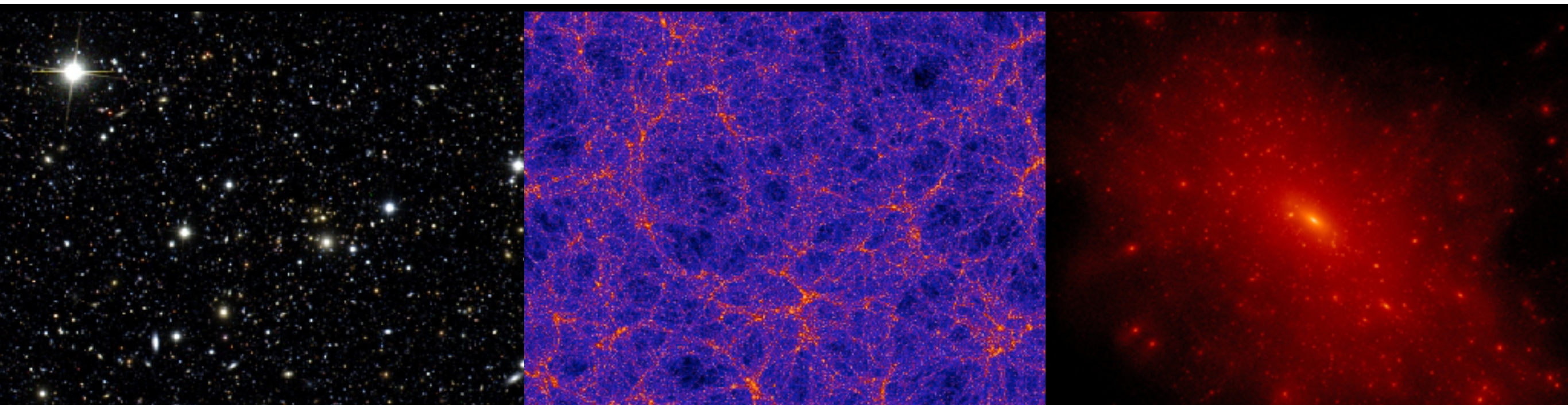
Anisotropic satellite distribution cause central-satellite alignments to decrease more rapidly on small scales as central IA decreases

# Scale Dependence: Satellite IA

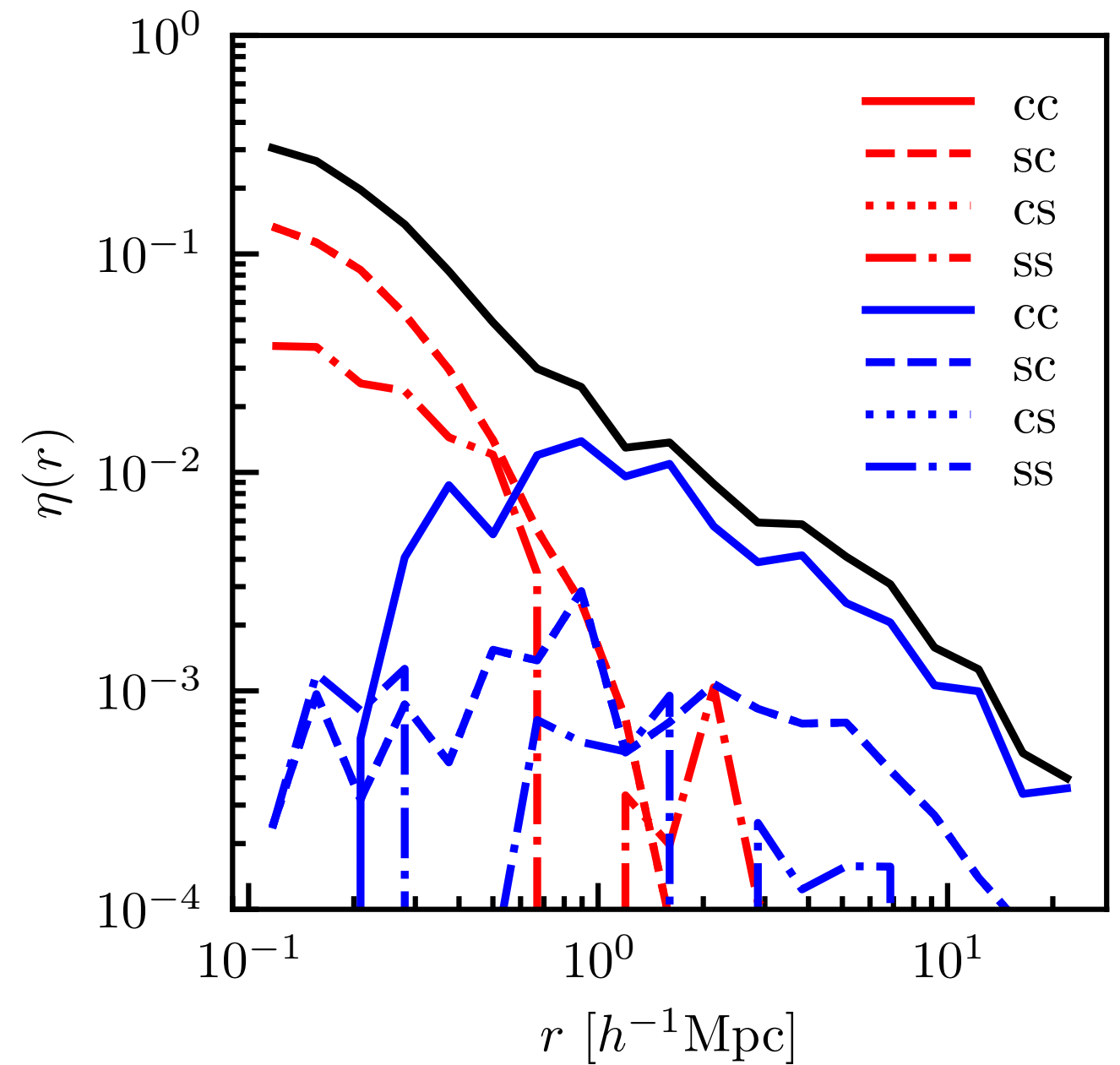
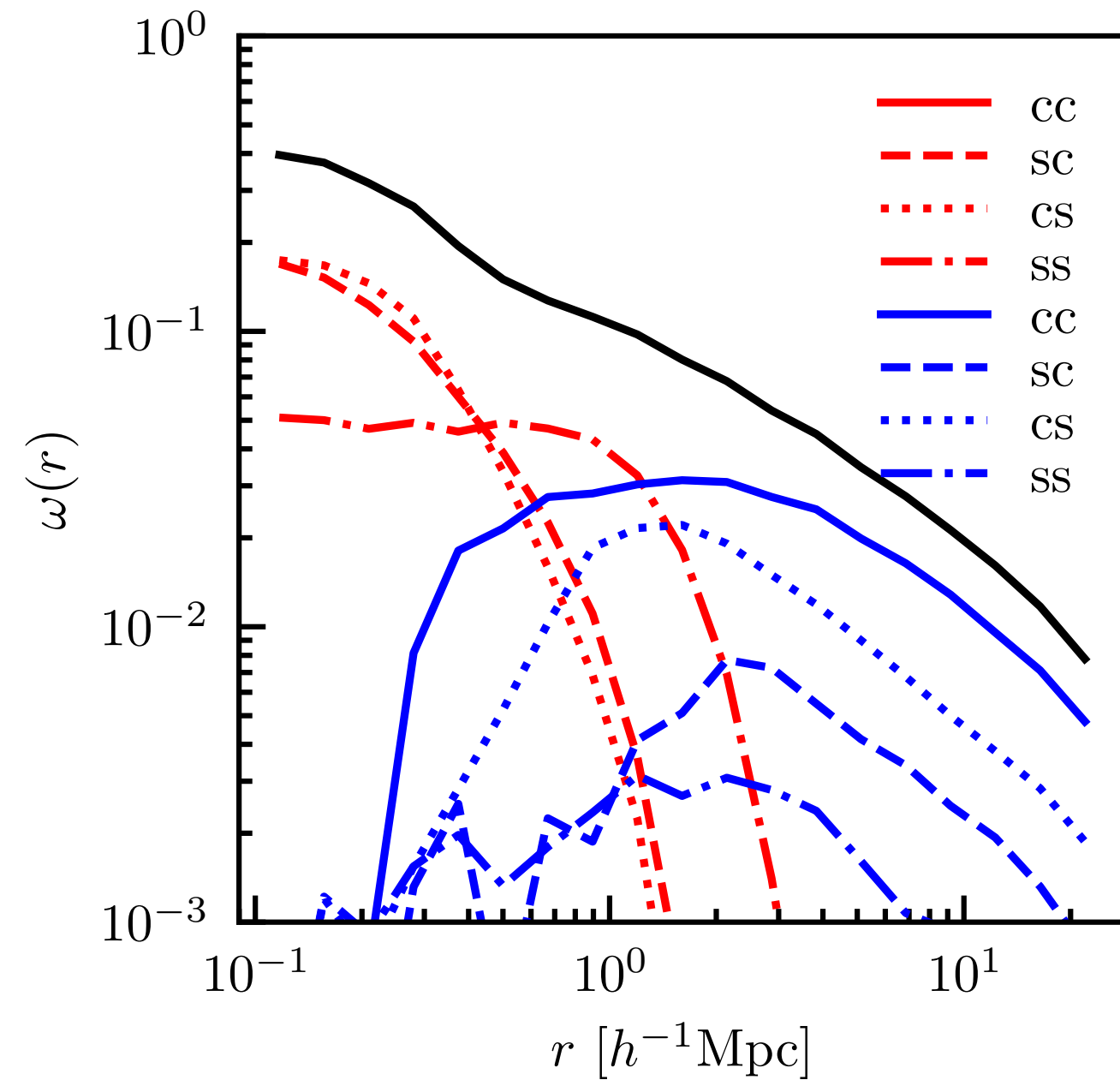


# Future Work and Applications

- add model for galaxy shapes
- explore alternate alignment models, e.g. tidal field, spin axis, etc
- compare predictions to (non-)linear alignment models
- constrain alignment parameters in SDSS
- add alignments into cosmology mocks to test mitigation schemes

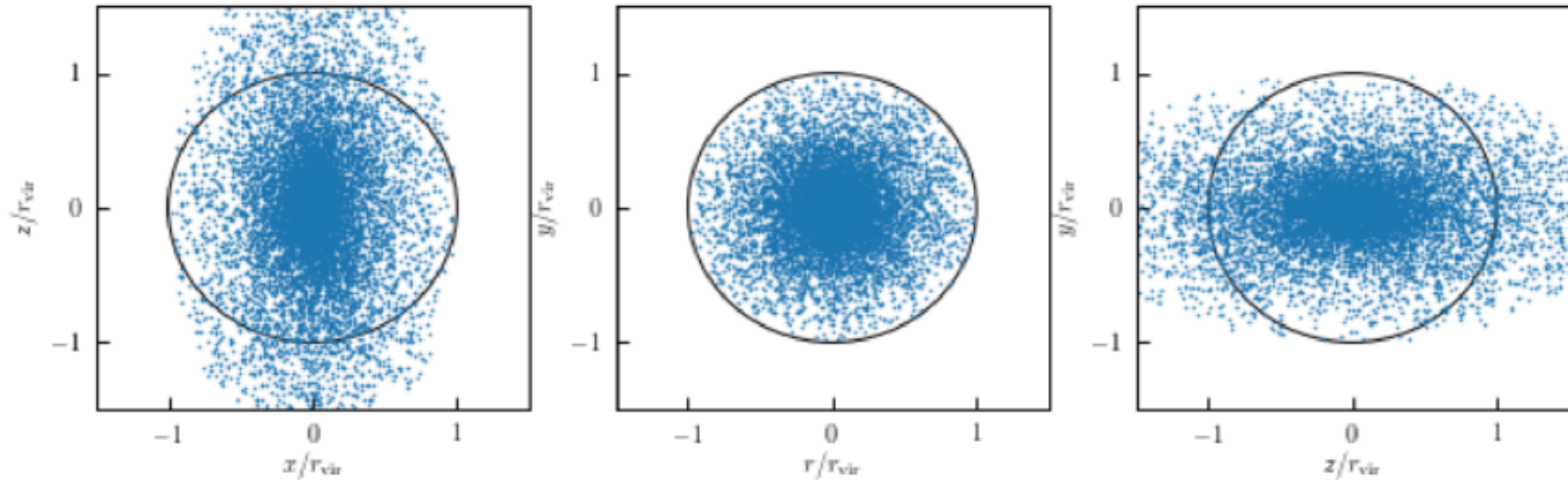


# Extra: alignment decomposition





# Extra: Anisotropic NFW



$$\rho(R) = \frac{\rho_c}{R/R_s(1 + R/R_s)^2}$$

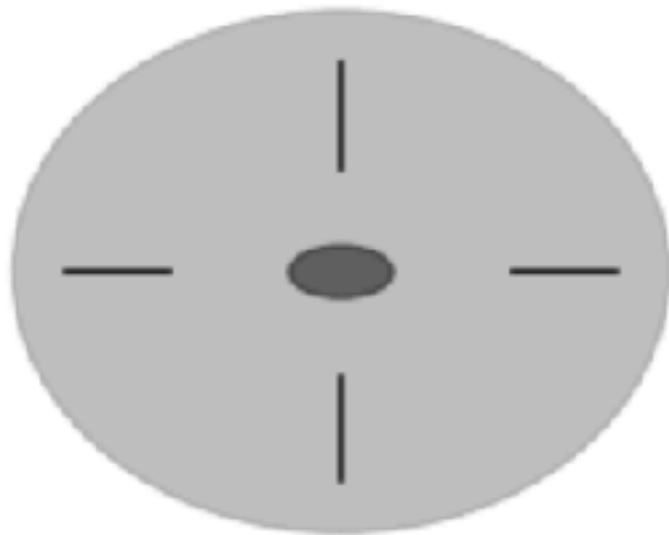
$$x = r \sin\theta \cos\phi = R \frac{a}{c} \sin\Theta \cos\Phi$$

$$y = r \sin\theta \sin\phi = R \frac{b}{c} \sin\Theta \sin\Phi$$

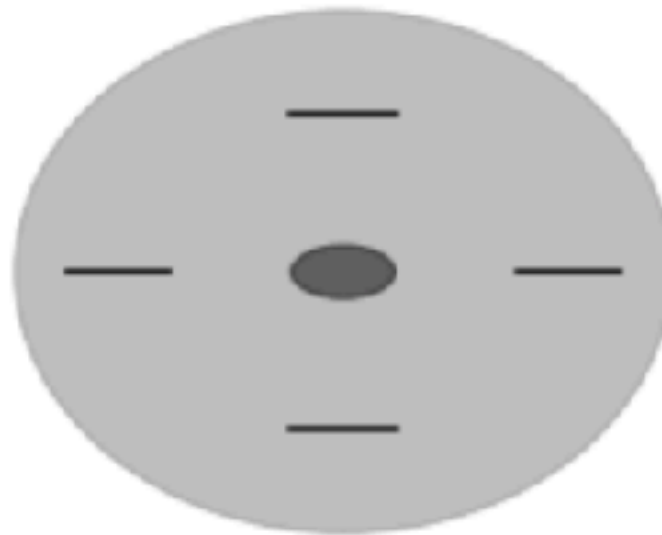
$$z = r \cos\theta = R \cos\Theta,$$

# Extra: Satellite Alignment Models

Radial Alignment Model



Major Axis Alignment Model



Hybrid Model

