

Heavy (Dynamical) Axions

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Based on [arXiv:1805.06465](https://arxiv.org/abs/1805.06465)

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Outline

1. Strong CP and axion solution
2. Heavy axion models
3. Small-size instantons
4. Massless quark: dynamical axion
5. Colour Unified Dynamical Axion

Why axion?

Strong CP problem

$$\mathcal{L}_{QCD} \supset \mathcal{L}_{CP} = -\bar{q} m e^{i\beta} q + \theta_{QCD} \frac{\alpha_s}{8\pi} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

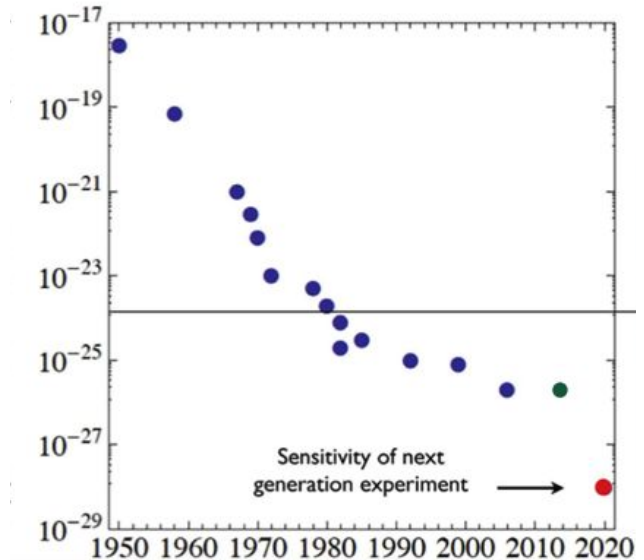
One physical CPV phase: $\bar{\theta} = \theta_{QCD} + \arg \det M$

$$d_n \approx 10^{-16} |\bar{\theta}| \text{e} \cdot \text{cm} \quad \bar{\theta} \lesssim 10^{-10}$$

Why is it so small?



Neutron EDM (Electric Dipole Moment)



[B.Fillipone via diLuzio]

Strong CP problem ~~hint~~

Neutron EDM (Electric Dipole Moment)

$\mathcal{L}_{QCD}$

→ Fine-tuning

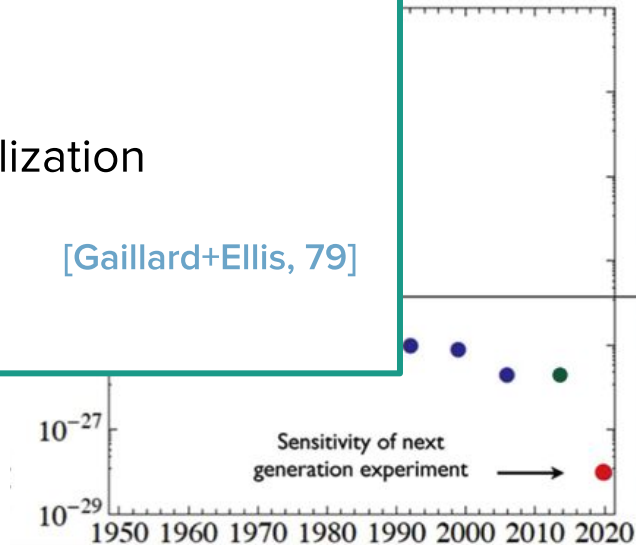
→ $\bar{\theta} = 0$ harmless under renormalization

[Gaillard+Ellis, 79]

One physi

$$d_n \approx 10^{-16} |\theta| e \cdot \text{cm} \quad \theta \lesssim 10^{-10}$$

Why is it so small?



[B.Fillipone via diLuzio]

The axion solution

→ If $\bar{\theta}$ were a scalar field, its vev would be zero [Vafa+Witten, 84]

$$\bar{\theta} \frac{\alpha_s}{8\pi} G\tilde{G} \longrightarrow \left(\bar{\theta} - \frac{a}{f_a} \right) \frac{\alpha_s}{8\pi} G\tilde{G}$$

→ Introduce a $U(1)_{PQ}$ symmetry (classically exact): [Peccei+Quinn 77]

- ◆ Spontaneously broken → pGoldstone Boson: AXION
- ◆ Anomalous: explicitly broken by QCD instantons → massive

My definition of axion:

“Any pseudo-Goldstone Boson of a global $U(1)$ symmetry, which is exact at the classical level but explicitly broken by instantons”

Invisible axion mass

→ Any model where the only PQ are QCD instantons:

$$m_a^2 f_a^2 \sim m_\pi^2 f_\pi^2 \frac{m_u m_d}{(m_u + m_d)^2}$$

→ Why does it vanish for $m_u \rightarrow 0$?

→ Both η' and axion couple to instantons:

$$\frac{\alpha}{8\pi} \left(2 \frac{\eta'}{f_\pi} - \frac{a}{f_a} \right) \tilde{G}G \quad \longrightarrow \quad m_{\eta'_{phys}}^2 = \frac{2\Lambda_{QCD}^4}{f_\pi^2}$$

→ Physical axion: orthogonal combination

Invisible axion mass

→ Any model where the only PQ are QCD instantons:

$$a \quad a \quad a \quad a \quad m_u, m_d$$

→ One source of PQ

→

→ Two anomalous pseudoscalars: a, η'

→

One must remain light

→ Physical axion: orthogonal combination

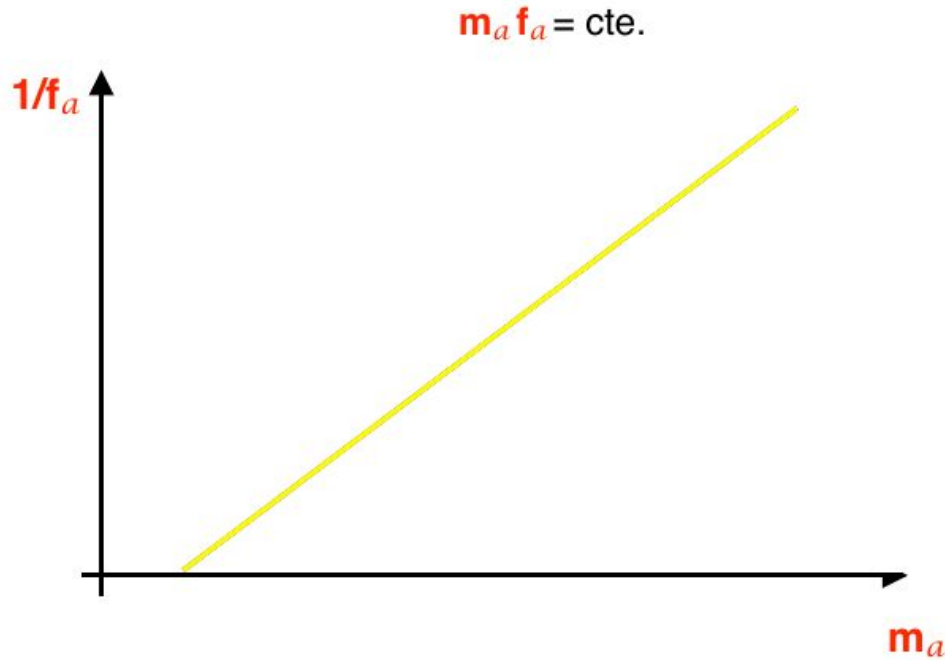
Invisible axion couplings

- KSVZ: PQ implemented with exotic vectorial quarks and a scalar
- DFSZ: PQ implemented with 2HDM + scalar

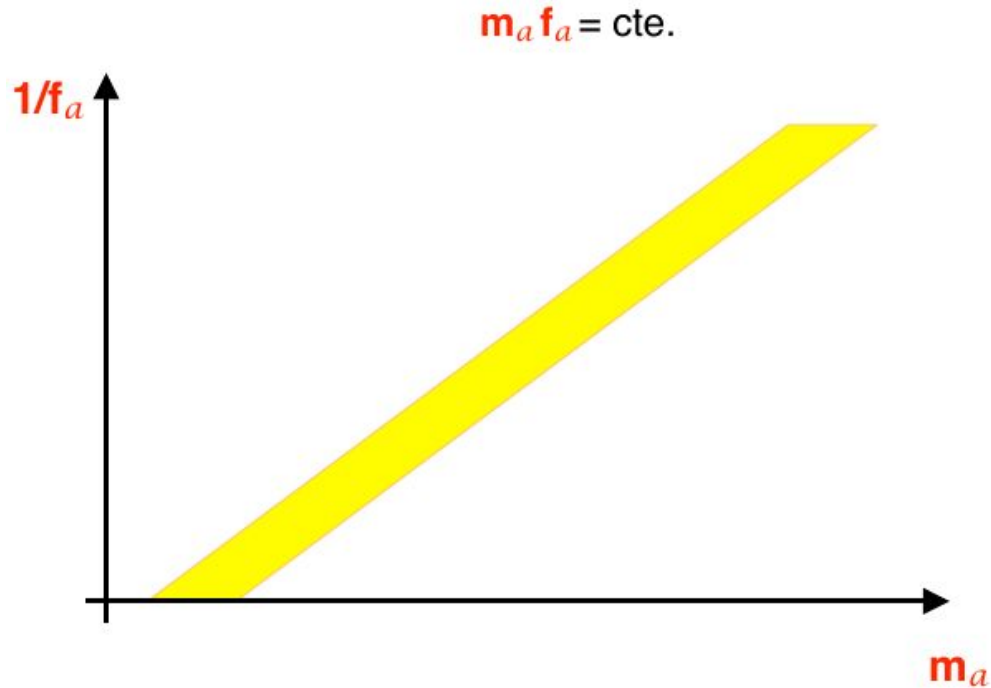
→ Couplings: $\mathcal{L} \supset \frac{1}{4} g_{a\gamma\gamma} a F \tilde{F}$

$$g_{a\gamma\gamma} \propto \frac{1}{f_a} \implies g_{a\gamma\gamma} \propto m_a$$

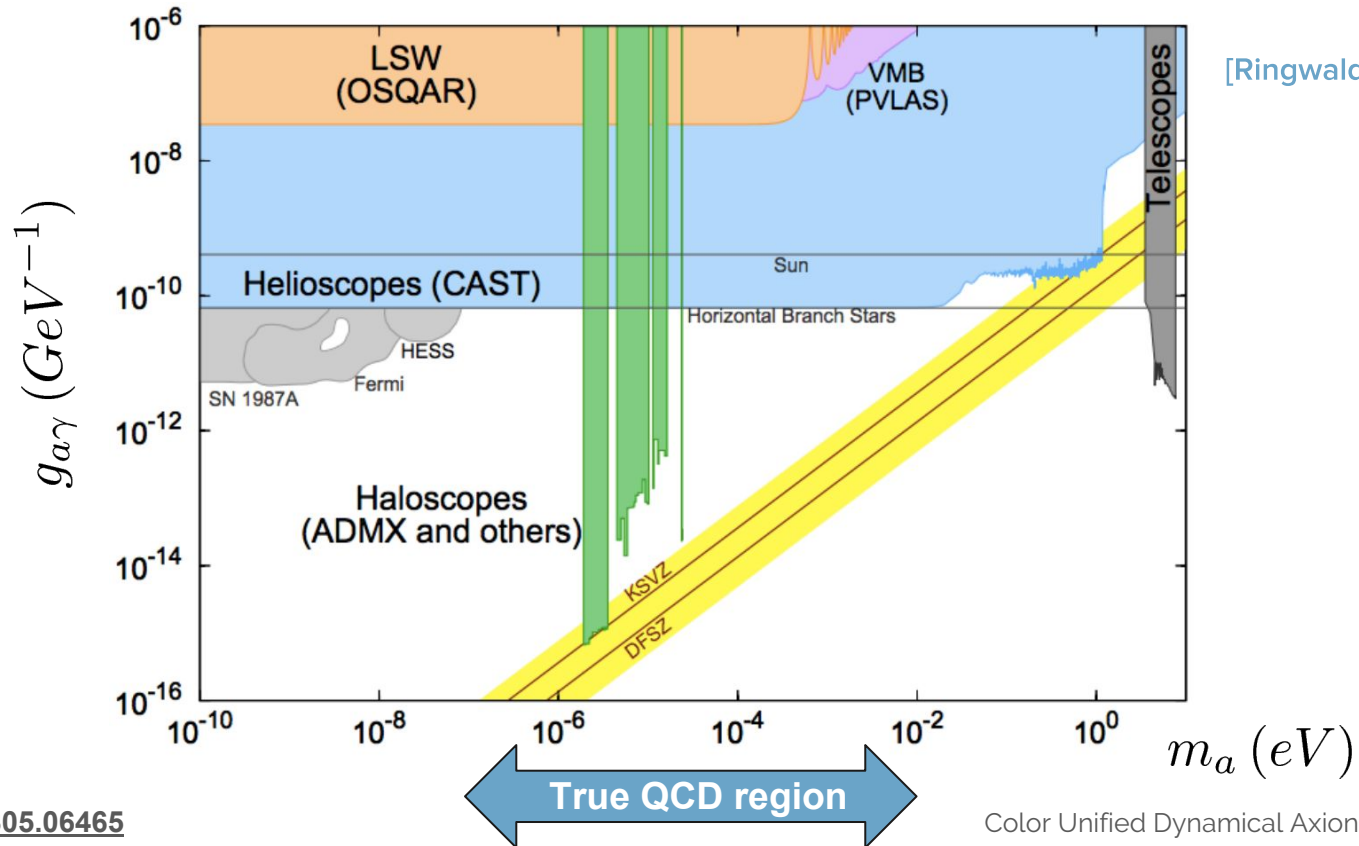
Invisible axion parameter space



Invisible axion parameter space

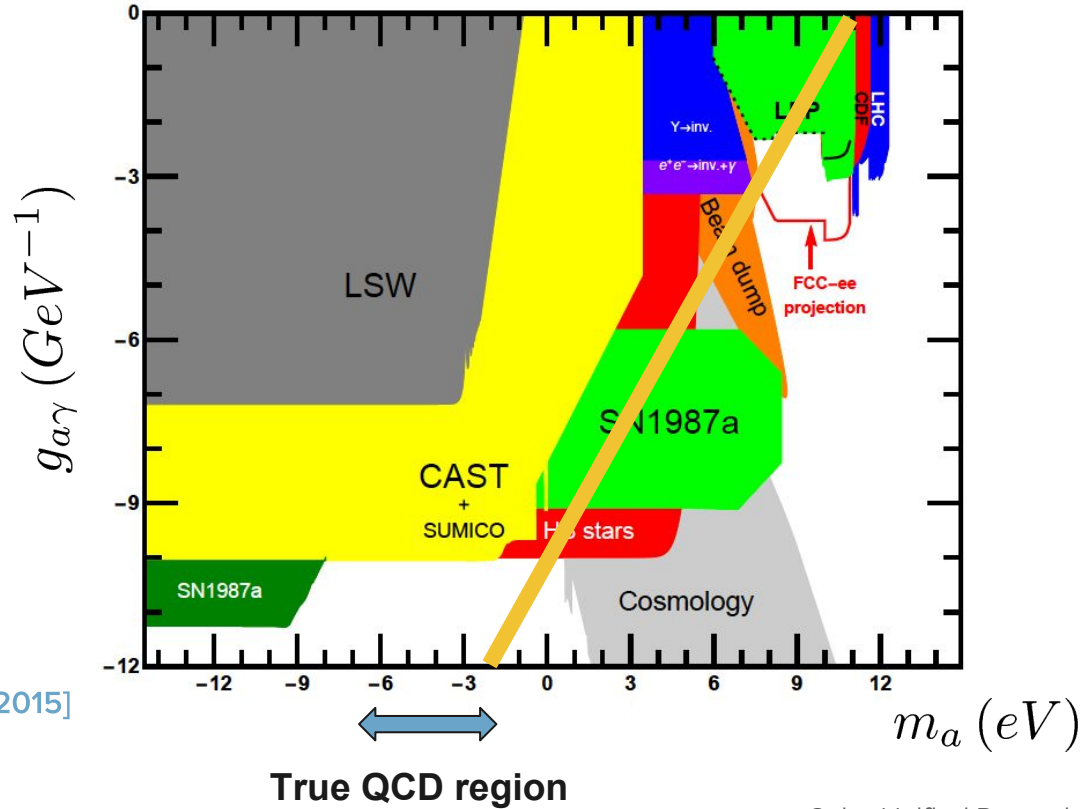


Invisible axion parameter space



[Ringwald, PDG 17]

Invisible axion parameter space

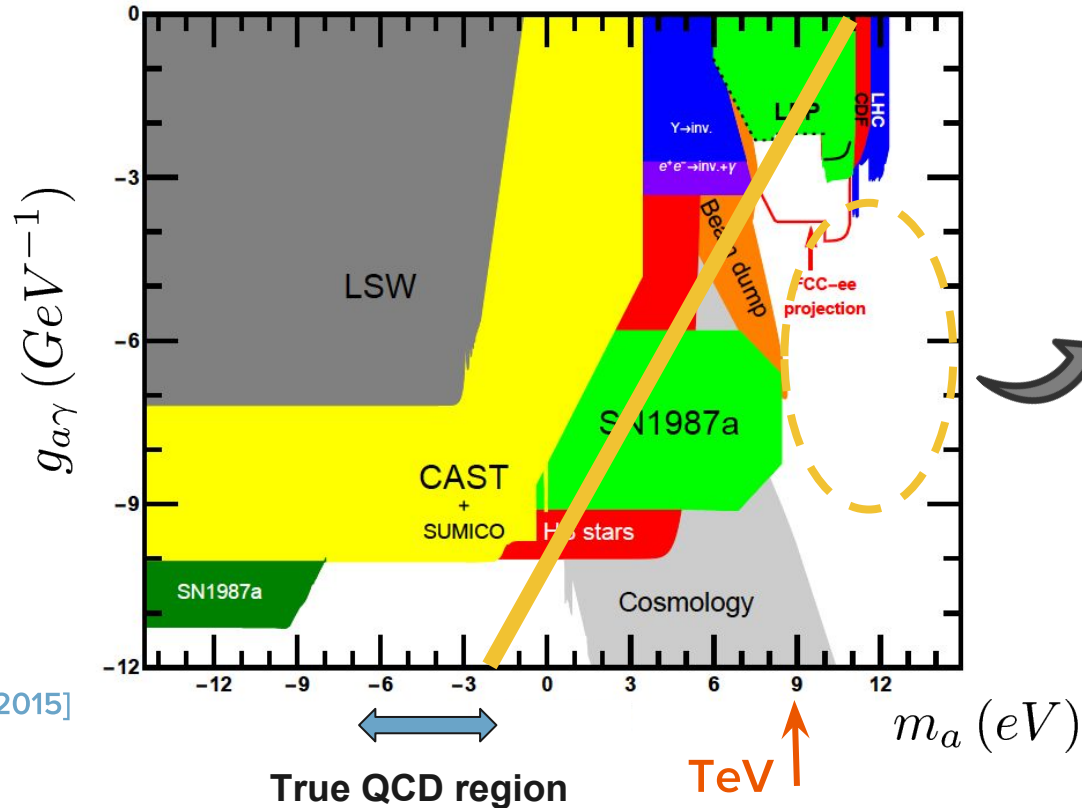


[Jaeckel+ Spannowsky 2015]

[arXiv:1805.06465](https://arxiv.org/abs/1805.06465)

Color Unified Dynamical Axion - Pablo Quilez

Invisible axion parameter space



[Jaeckel+ Spannowsky 2015]

[arXiv:1805.06465](https://arxiv.org/abs/1805.06465)

Color Unified Dynamical Axion - Pablo Quilez

Can we make it heavy?

How many light axions has your theory?

Compare the number of:

Anomalous pseudoscalars:

$$\eta'_{QCD}, a_1, a_2 \dots$$

PQV instanton sources



$$G_c \tilde{G}_c, G_1 \tilde{G}_1, G_2 \tilde{G}_2 \dots$$

Heavy axion models

→ New strong interactions with scale Λ'

$$\frac{\alpha}{8\pi} \frac{a}{f_a} \tilde{G}G + \frac{\alpha'}{8\pi} \frac{a}{f_a} \tilde{G}'G' \quad \left\{ \begin{array}{ll} m_a^2 f_a^2 \sim m_\pi^2 f_\pi^2 + \Lambda'^4 & \text{(no light } q') \\ m_a^2 f_a^2 \sim m_\pi^2 f_\pi^2 + m_\pi'^2 f_\pi'^2 & \text{(with light } q') \end{array} \right.$$

→ New confining group → New theta

→ Need some larger symmetry to align them:

◆ Z_2

◆ Unification

[Rubakov, 97]

[Berezhiani et al, 01]

[Fukuda et al, 01]

[Hsu et al, 04]

[Hook et al, 14]

[Chiang et al, 16]

[Khobadize et al,]

[Dimopoulos et al, 16]

[Gherghetta et al, 16]

[Agrawal et al, 17]

Heavy axion models

→ New strong interactions with scale Λ'

$\frac{\alpha}{8\pi}$

$$m_a^2 f_a^2 \sim \text{LARGE const}$$

→

→

◆ Unification

no light q')

with light q')

[1,01]

1]

[Chiang et al, 16]

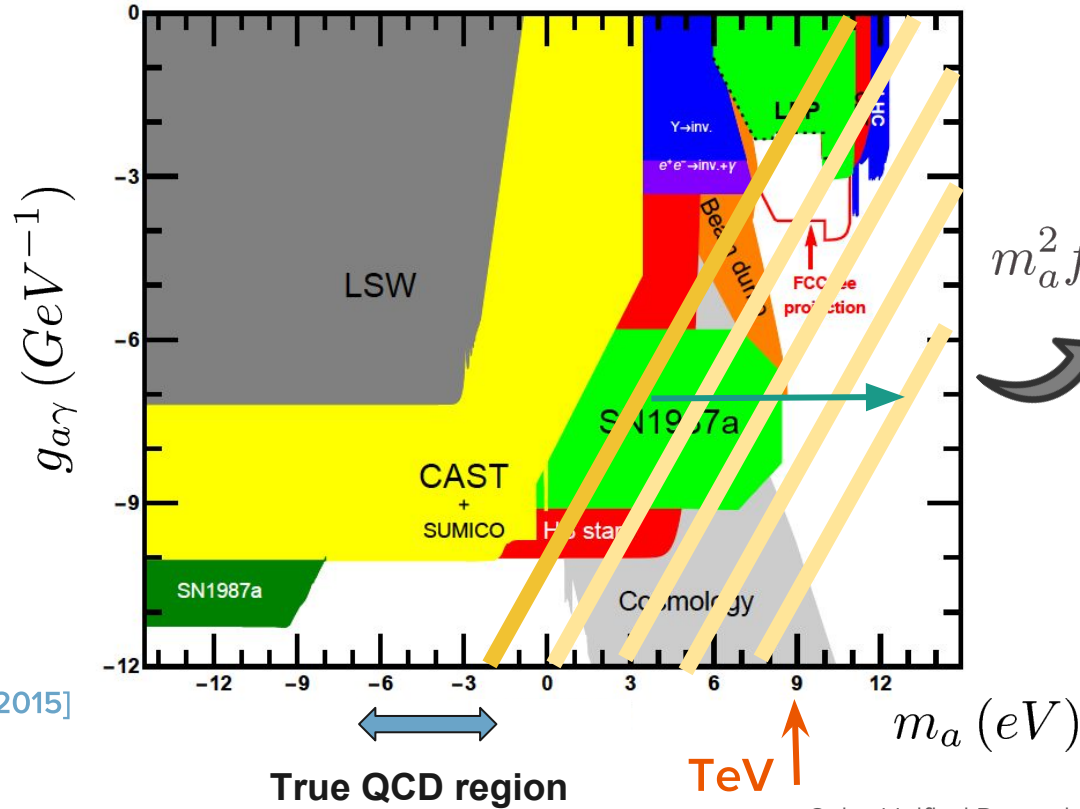
[Khobadize et al,]

[Dimopoulos et al, 16]

[Gherghetta et al, 16]

[Agrawal et al, 17]

Invisible axion parameter space



[Jaeckel+ Spannowsky 2015]

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Color Unified Dynamical Axion - Pablo Quilez



- $SU(5) \times SU(5)' \rightarrow \theta = \theta'$
- 2HDM in each world
- One shared $U(1)_{PQ}$ through Scalar connecting both worlds
- **CONS:** tuning in the scalar sector

$$M_a \sim \left(\frac{\Lambda_{mc}}{\Lambda_{QCD}} \right)^{\frac{3}{2}} \cdot \left(\frac{v}{v_m} \right)^{\frac{1}{2}} \cdot m_{WW} \sim GeV - TeV$$

- Berherziani et al, 01 did it for the SM gauge group



- SMxSM' → theta=theta'
- Exotic vectorial fermions → KSVZ
- Nice cosmology, several DM candidates:

$$m_a^2 f_a^2 \sim m_\pi^2 f_\pi^2 + m_\pi'^2 f_\pi'^2$$

- $SU(3 + N') \rightarrow SU(3)_c \times SU(N')$
- Exotic vectorial fermions → KSVZ
- **PROS:** less matter content
- **CONS:** mass splitting of unified partners
 - ◆ Need to further enlarge the gauge group and assume no extra CP phase

$$SU(N') \times SU(3 + N') \longrightarrow SU(N') \times SU(3)_c$$

Small Size Instantons

Extra source of axion mass

Heavy axion: Small Size Instantons

- Typically, at high energies (= small size) couplings are very small.
- The instanton density has an exponential suppression:

$$D[\alpha'(\mu)] \propto e^{-2\pi/\alpha'(\mu)} \quad \text{Usually sizable only at the confinement scale} \quad \left(e^{-2\pi/0.1} \sim 10^{-28} \right)$$

- New Physics can change the RG flow and induce a new source of axion mass

[Holdom+Peskin, 82]
[Dine+Seiberg, 86]
[Agrawal+Howe, 17]
[Flynn+Randall, 87]

- Large coupling
- At some Large scale

$$\Lambda_{SSI}^4 \sim \mu^4 e^{-2\pi/\alpha}$$

Heavy axion: Small Size Instantons

- Typically, at high energies (= small size) couplings are very small.
- The instanton density has an exponential suppression:

$$\Lambda_{SSI}^4 \sim \mu^4 e^{-2\pi/\alpha}$$

→ New F

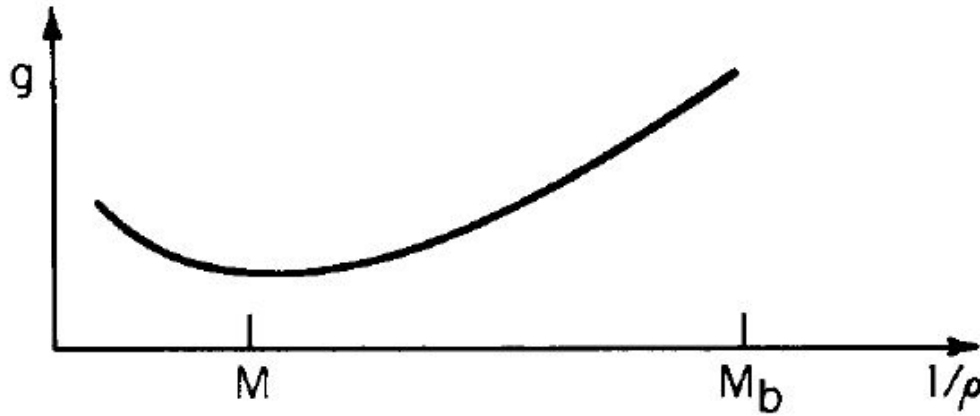
→ Large coupling

→ At some Large scale μ

**New sizable contribution to
the axion mass!!**

Small Size Instanton: Randall and Flynn, 87

- Extra coloured fermions/scalars
- Change the sign of the beta function



[Flynn+Randall, 87]

$$SU(3)_1 \times SU(3)_2 \rightarrow SU(3)_c$$

$$\frac{1}{\alpha_s(\mu)} = \frac{1}{\alpha_{s_1}(\mu)} + \frac{1}{\alpha_{s_2}(\mu)}, \quad \mu = M,$$

- 2 axions up to 1000 times heavier than invisible axion
- Some tuning in the couplings is required

Massless quark solution

Dynamical axion

Massless quark solution

→ Under a chiral rotation: $U(1)_A : \quad q \rightarrow e^{\frac{\alpha}{2} i \gamma_5} q$

$$\mathcal{L} \supset -m_q \bar{q} q - \theta \frac{\alpha_s}{8\pi} G \tilde{G} \longrightarrow -m_q \bar{q} e^{i\alpha \gamma_5} q - (\theta - \alpha) \frac{\alpha_s}{8\pi} G \tilde{G}$$

→ If $m_q = 0$, the phase θ can be fully reabsorbed $\implies$ **Strong CP Problem solved!**

→ No different from usual PQ solution [Peccei+Quinn 77]

→ Most economical option: Massless up quark, disfavored by lattice data [Manohar et al 16, PDG]

→ Exotic massless quark ψ **How do we hide it?**

→ New confining group $\tilde{\Lambda} \gg \Lambda_{QCD}$

◆ **Problem:** new CP violating phase $\tilde{\theta}$

◆ **Solution:** Add another massless quark χ

	$SU(3)_c$	$SU(\tilde{N})$
ψ	$\square$	$\square$
χ	1	$\square$

Massless quark content

→ $SU(\tilde{N})$ Confines + Chiral Symmetry Breaking: $U(4)_L \times U(4)_R \xrightarrow[\langle \bar{\psi}\psi \rangle]{\langle \bar{\chi}\chi \rangle} U(4)_V$

pseudo-Goldstone Bosons (pGB): $16 = 8 + 3 + \bar{3} + 1 + 1$

The η' become dynamical axions



→ Two axions: $a_1 = (\bar{\psi}\psi)$ $a_2 = (\bar{\chi}\chi)$

2 ~~PQ~~ instantons $\begin{cases} \Lambda_{QCD} \\ \tilde{\Lambda} \end{cases}$  3 pseudoscalars $\begin{cases} \bar{\psi}\psi \\ \bar{\chi}\chi \\ \eta'_{QCD} \end{cases}$

→ One axion remains light:

$$m_{a_1}^2 f_a^2 \sim \tilde{\Lambda}^4 \quad m_{\eta'}^2 f_\pi^2 \sim \Lambda_{QCD}^4 \quad m_{a_2}^2 f_a^2 \sim m_\pi^2 f_\pi^2 \frac{m_u m_d}{(m_u + m_d)^2}$$

UV completion of a usual invisible axion

Why dynamical?



Colour Unified Dynamical Axion

M. K. Gaillard, M. B. Gavela, R. Houtz, P.Q. and R. del Rey

First colour-unified model with massless quarks

Color Unified Dynamical Axion

→ Unification allows to identify the two phases: only one massless quark needed

$$SU(6) \xrightarrow{\Lambda_{\text{CUT}}} SU(3)_c \times SU(\tilde{3}) \times U(1)$$

$$\theta_6 = \theta_c = \tilde{\theta}$$

Over Unification scale:

	$SU(6)$	$SU(2)_L$	$U(1)$
Ψ_L	20	1	0

Bellow unification scale:

	$SU(3)_c$	$SU(\tilde{3})$
ψ_L	$\square$	$\square$
ψ_L^c	$\bar{\square}$	$\square$
$2 \times \psi_\nu$	1	1

Color Unified Dynamical Axion

$$SU(6) \xrightarrow{\Lambda_{\text{CUT}}} SU(3)_c \times SU(\tilde{3}) \times U(1)$$

→ SM quarks are embedded in fundamentals of SU(6)

SM

$$Q_L \equiv (q, \tilde{q})_L \quad U \equiv (u, \tilde{u})_R \quad D \equiv (d, \tilde{d})_R$$



Problem: How do we give large masses to the unified partners?

1. Without spoiling SM quark masses
2. Without breaking EW at a high scale
3. In order to separate the running of the two groups .

Color Unified Dynamical Axion: The real thing

$$SU(6) \times SU(3') \xrightarrow{\Lambda_{\text{CUT}}} SU(3)_c \times SU(3)_{\text{diag}} \quad \text{SM}$$

→ Spontaneously broken by the vev of Δ

$$\langle \Delta \rangle = \Lambda_{\text{CUT}} \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$Q_L \equiv (q, \tilde{q})_L$$

$$q'_L \quad \text{Extra primed quarks}$$

$$\kappa_q q'_L \Delta^* Q_L \longrightarrow \Lambda_{\text{CUT}} \kappa_q q'_L \tilde{q}_L$$

$$(6, 1) (\bar{6}, 3) (1, \bar{3})$$

Color Unified Dynamical Axion: The real thing

$$SU(6) \times SU(3') \xrightarrow{\Lambda_{\text{CUT}}} SU(3)_c \times SU(3)_{\text{diag}}$$

→ Spontaneous

$$\langle \Delta \rangle =$$

Allows for a large mass for the tilde sector without spoiling the SM quark masses

$$\tilde{q})_L$$

ed quarks

$$\kappa_q q'_L \Delta^* Q_L \longrightarrow \Lambda_{\text{CUT}} \kappa_q q'_L \tilde{q}_L$$

$$\begin{array}{ccc} \swarrow & \downarrow & \searrow \\ (6, 1) & (\bar{6}, 3) & (1, \bar{3}) \end{array}$$

Color Unified Dynamical Axion

$$SU(6) \times SU(3')$$

$$\theta_6 \qquad \theta'$$

Two massless fermions to reabsorb both CP phases

	$SU(6)$	$SU(3)'$
ψ	20	1
χ	1	$\square$

	$SU(3)_c$	$SU(3)_{\text{diag}}$
ψ	$\square$	$\square$
χ	1	$\square$

→ Two dynamical axions $\eta'_\psi = (\bar{\psi}\psi)$ $\eta'_\chi = (\bar{\chi}\chi)$

Running of the gauge couplings

→ At the breaking scale:

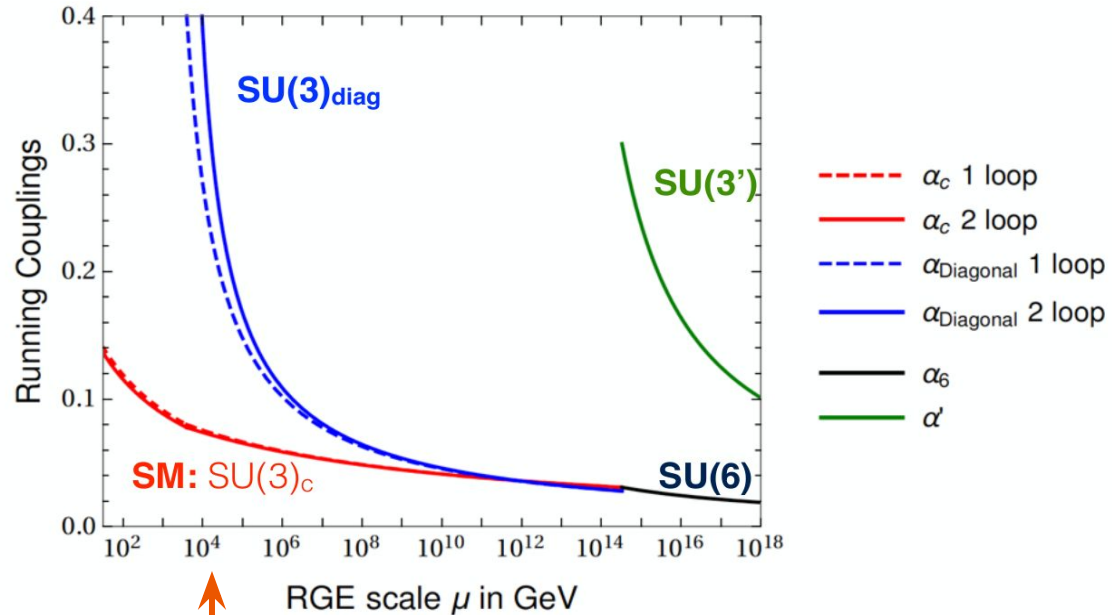
$$\frac{1}{\alpha_{\text{diag}}(\mu)} = \frac{1}{\alpha_6(\mu)} + \frac{1}{\alpha'(\mu)}$$

$$\alpha_c(\Lambda_{\text{CUT}}) = \alpha_6(\Lambda_{\text{CUT}})$$

$SU(3)_{\text{diag}}$ **confines before QCD**

$$\Lambda_d \gg \Lambda_{QCD}$$

$$SU(6) \times SU(3') \xrightarrow{\Lambda_{\text{CUT}}} SU(3)_c \times SU(3)_{\text{diag}}$$

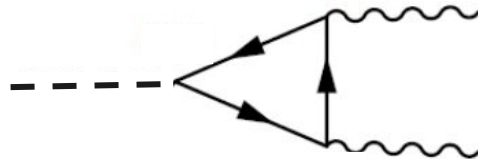


The anomalous pseudoscalars: dynamical axions + η'

→ Anomalous currents $\implies$ Anomalous couplings of the pseudoscalars:

$$j_{\psi_A}^\mu = \bar{\psi} \gamma^\mu \gamma^5 \psi \equiv f_d \partial^\mu \eta'_\psi,$$

$$j_{\chi_A}^\mu = \bar{\chi} \gamma^\mu \gamma^5 \chi \equiv f_d \partial^\mu \eta'_\chi,$$



$$\mathcal{L} \supset -\frac{\alpha_c}{8\pi} \frac{\sqrt{6} \eta'_\psi}{f_d} G_c \tilde{G}_c - \frac{\alpha_{\text{diag}}}{8\pi} \left(2 \frac{\eta'_\chi}{f_d} + \sqrt{6} \frac{\eta'_\psi}{f_d} \right) G_{\text{diag}} \tilde{G}_{\text{diag}}$$

Confinement

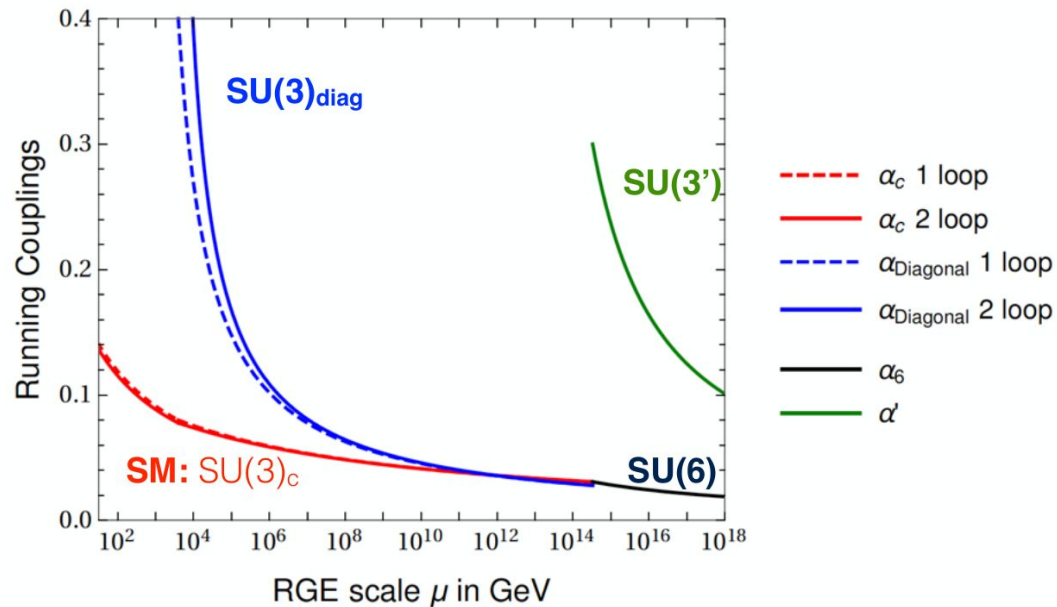
$$\mathcal{L} \supset \Lambda_{\text{diag}}^4 \cos \left(2 \frac{\eta'_\chi}{f_d} + \sqrt{6} \frac{\eta'_\psi}{f_d} \right) + \Lambda_{\text{QCD}}^4 \cos \left(2 \frac{\eta'_{\text{QCD}}}{f_\pi} + \sqrt{6} \frac{\eta'_\psi}{f_d} \right)$$

Incorporating η'_{QCD}

- 3 anomalous pseudoscalars
- 2 sources of mass/breaking

Another light axion model?

Small Size Instantons and axion mass



→ Large coupling $\alpha' \sim 0.3$

→ Large breaking scale

$$\Lambda_{\text{CUT}} \sim 10^{14-18} \text{ GeV}$$

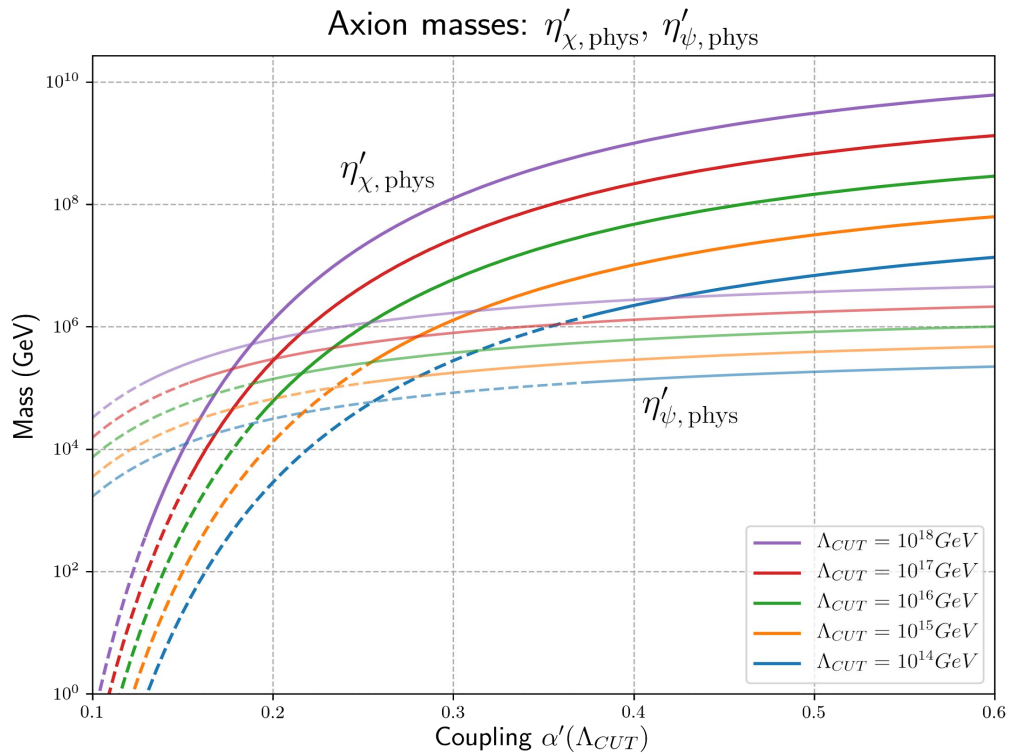
**New sizable contribution
to the axion mass!!**

Dynamical axion potential and masses

$$\mathcal{L}_{eff} = \underbrace{\Lambda_{\text{SSI}}^4 \cos\left(2 \frac{\eta'_\chi}{f_d}\right)}_{SU(3') \text{ SSI Instantons}} + \underbrace{\Lambda_{\text{diag}}^4 \cos\left(2 \frac{\eta'_\chi}{f_d} + \sqrt{6} \frac{\eta'_\psi}{f_d}\right)}_{SU(3)_{\text{diag}} \text{ Instantons at conf.}} + \underbrace{\Lambda_{\text{QCD}}^4 \cos\left(2 \frac{\eta'_{\text{QCD}}}{f_\pi} + \sqrt{6} \frac{\eta'_\psi}{f_d}\right)}_{SU(3)_c \text{ Instantons at conf.}}$$

$$M_{\eta'_\chi, \eta'_\psi, \eta'_{\text{QCD}}}^2 = \begin{pmatrix} 4 \frac{(\Lambda_{\text{SSI}}^4 + \Lambda_d^4)}{f_d^2} & 2\sqrt{6} \frac{\Lambda_d^4}{f_d^2} & 0 \\ 2\sqrt{6} \frac{\Lambda_d^4}{f_d^2} & 6 \frac{(\Lambda_d^4 + \Lambda_{\text{QCD}}^4)}{f_d^2} & 2\sqrt{6} \frac{\Lambda_{\text{QCD}}^4}{f_\pi f_d} \\ 0 & 2\sqrt{6} \frac{\Lambda_{\text{QCD}}^4}{f_\pi f_d} & 4 \frac{\Lambda_{\text{QCD}}^4}{f_\pi^2} \end{pmatrix}$$

Dynamical axion masses



Solution to the Strong CP problem

- Any source of axion mass breaks the PQ symmetry, **do SSI spoil the Strong CP solution?**
- Breaking pattern imposes:

$$\mathcal{L} \supset \bar{\theta}_6 \frac{\alpha_6}{8\pi} G_6 \tilde{G}_6 + \bar{\theta}' \frac{\alpha'}{8\pi} G' \tilde{G}' \longrightarrow (\bar{\theta}_6 + \bar{\theta}') \frac{\alpha_{\text{diag}}}{8\pi} G_{\text{diag}} \tilde{G}_{\text{diag}} + \bar{\theta}_6 \frac{\alpha_c}{8\pi} G_c \tilde{G}_c$$

- Therefore the potential reads:

$$\mathcal{L}_{eff} = \Lambda_{\text{SSI}}^4 \cos\left(-2 \frac{\eta'_\chi}{f_d} + \bar{\theta}'\right) + \Lambda_{\text{diag}}^4 \cos\left(-2 \frac{\eta'_\chi}{f_d} - \sqrt{6} \frac{\eta'_\psi}{f_d} + \bar{\theta}' + \bar{\theta}_6\right) + \Lambda_{\text{QCD}}^4 \cos\left(-\sqrt{6} \frac{\eta'_\psi}{f_d} + \bar{\theta}_6\right)$$

- The alignment of the 3 terms in the potential result in a CP-conserving minimum

$$\left\langle \bar{\theta}' - 2 \frac{\eta'_\chi}{f_d} \right\rangle = 0, \quad \left\langle \bar{\theta}_6 - \sqrt{6} \frac{\eta'_\psi}{f_d} \right\rangle = 0$$

**Strong CP problem
solved**

Confinement and χ SB of the $SU(3)_{\text{diag}}$

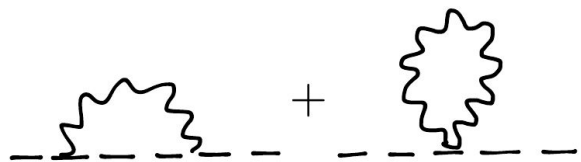
→ Chiral symmetry breaking by the condensates: $\langle \bar{\psi}\psi \rangle$, $\langle \bar{\chi}\chi \rangle$

$$U(4)_L \times U(4)_R \xrightarrow{\Lambda_d} U(4)_V$$

	$SU(3)_c$	$SU(3)_{\text{diag}}$
ψ	$\square$	$\square$
χ	1	$\square$

→ Results in 16 pGB's: $16 = 8_c + 3_c + \bar{3}_c + 1_c + 1_c$ **become dynamical axions**

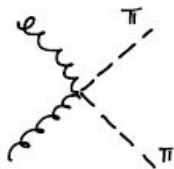
→ The “axipions”, through quadratically divergent gluon loops, get a large mass:



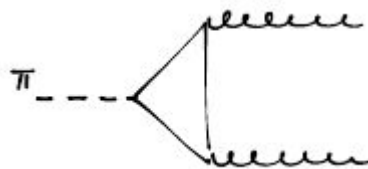
$$\Rightarrow \begin{aligned} m^2(8_c) &\approx \frac{9\alpha_c}{4\pi} \Lambda_{\text{diag}}^2 & \bar{\psi} t^a \psi, \\ m^2(3_c) &\approx \frac{\alpha_c}{\pi} \Lambda_{\text{diag}}^2 & \bar{\psi} \chi, \bar{\chi} \psi \end{aligned}$$

Low energy Spectrum and Phenomenology

- No light axion.
 - ◆ Both axions too heavy for colliders
- Sterile fermions ψ_ν with couplings suppressed by Λ_{CUT} (basically invisible)
- QCD Coloured “axipions” are collider accessible, octets:



Pair produced

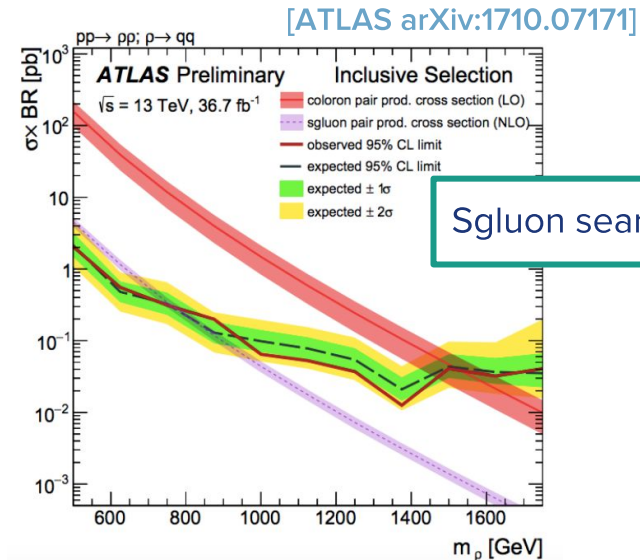


Anomalous decay

$$m(8_c) \gtrsim 770 \text{ GeV}$$

$$m^2(8_c) \approx \frac{9\alpha_c}{4\pi} \Lambda_{\text{diag}}^2$$

$$\Lambda_{\text{diag}} \gtrsim 3 \text{ TeV}$$



Color Unified Dynamical Axion: model II

$$SU(6) \xrightarrow{\Lambda_{\text{CUT}}} SU(3)_c \times SU(\tilde{3}) \times U(1)$$

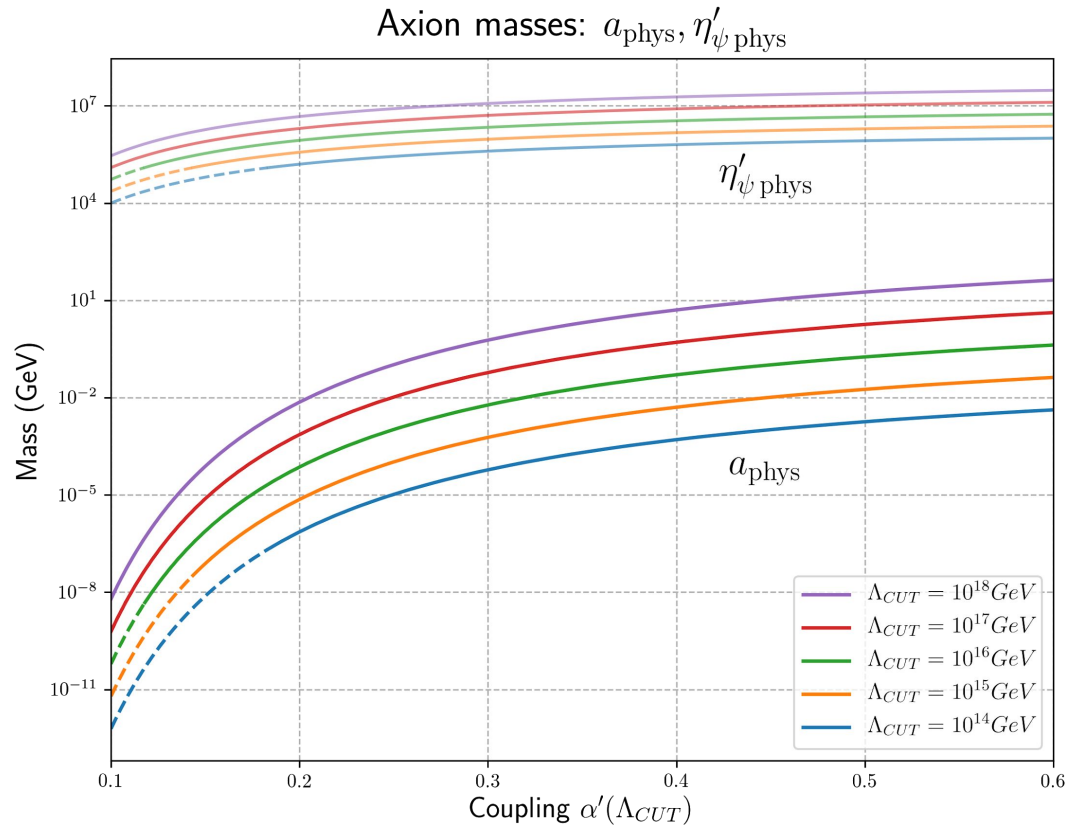
Instead of adding a second massless fermion:

	$SU(6)$	$SU(3)'$
Model I	ψ	20
	χ	1
		$\square$

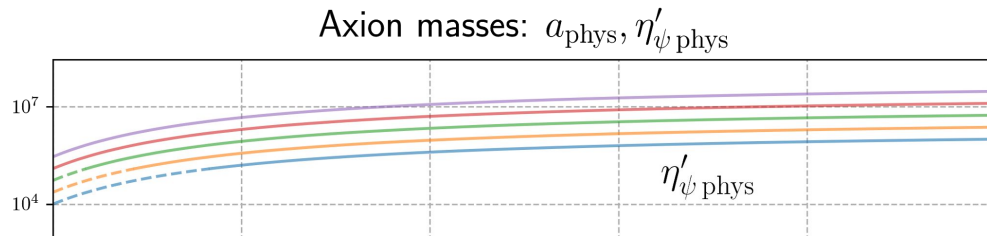
We added a second scalar Δ_2

	$SU(6)$	$SU(3)'$
Model II	ψ	20
	Δ_2	$\square$
		$\overline{\square}$

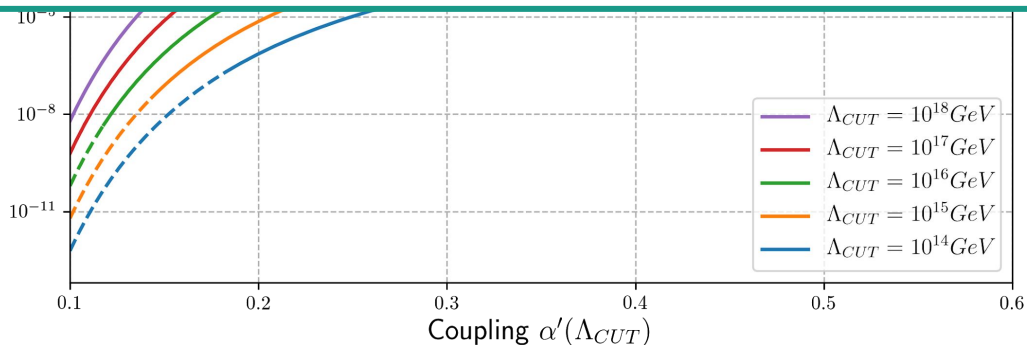
Color Unified Dynamical Axion: model II



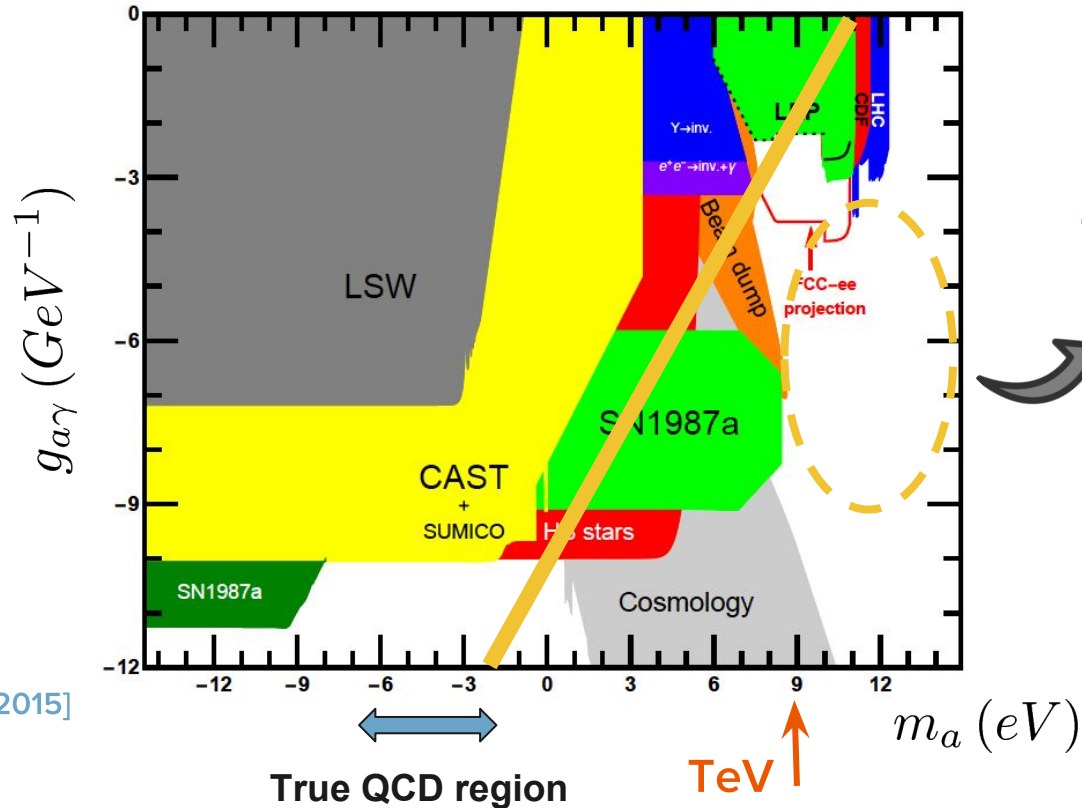
Color Unified Dynamical Axion: model II



- Dynamical axion still very heavy
- Fundamental axion a can be $\sim \text{GeV}$ or lower
- **CONS:** Large scalar vev → contributes to the EW hierarchy problem



Much territory to explore



[Jaeckel+ Spannowsky 2015]

[arXiv:1805.06465](https://arxiv.org/abs/1805.06465)

Color Unified Dynamical Axion - Pablo Quilez

Conclusions

- Strong CP problem solved with **massless quarks** and **unification**.

$$SU(6) \times SU(3') \xrightarrow{\Lambda_{\text{CUT}}} SU(3)_c \times SU(3)_{\text{diag}}$$

- Axions are heavy due to Small size instantons
- Colored mesons observable at colliders

The $\{m_a, f_a\}$ region that solves the strong CP problem is amplified

Thank you!

Color Unified Dynamical Axion: The real thing

$$SU(6) \times SU(3') \xrightarrow{\Lambda_{\text{CUT}}} SU(3)_c \times SU(3)_{\text{diag}}$$

→ Spontaneously broken by the vev of Δ

$$\langle \Delta \rangle = \Lambda_{\text{CUT}} \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

Allows for a large mass for the tilde sector without spoiling the SM quark masses

$$\kappa_q q'_L \Delta^* Q_L \longrightarrow \Lambda_{\text{CUT}} \kappa_q q'_L \tilde{q}_L$$

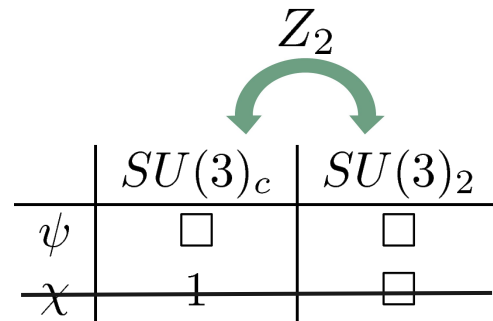
	$SU(6)$	$SU(3')$
Q_L	$\square$	1
U_L^c	$\bar{\square}$	1
D_L^c	$\bar{\square}$	1
Ψ_L	20	1
q'_L	1	$\bar{\square}$
$u_L'^c$	1	$\square$
$d_L'^c$	1	$\square$
Δ	$\square$	$\bar{\square}$

	$SU(3)_c$	$SU(3)_{\text{diag}}$	$SU(2)_L$	$U(1)_Y$
q_L	$\square$	1	$\square$	$\frac{1}{6}$
$\tilde{q}_L$	1	$\square$	$\square$	$\frac{1}{6}$
u_L^c	$\bar{\square}$	1	1	$-\frac{2}{3}$
$\tilde{u}_L^c$	1	$\bar{\square}$	1	$-\frac{2}{3}$
d_L^c	$\bar{\square}$	1	1	$\frac{1}{3}$
$\tilde{d}_L^c$	1	$\bar{\square}$	1	$\frac{1}{3}$
ψ_L	$\square$	$\bar{\square}$	1	0
ψ_L^c	$\bar{\square}$	$\square$	1	0
$2 \times \psi_\nu$	1	1	1	1
q'_L	1	$\bar{\square}$	$\square$	$-\frac{1}{6}$
$u_L'^c$	1	$\square$	1	$\frac{2}{3}$
$d_L'^c$	1	$\square$	1	$-\frac{1}{3}$
—	—	—	1	0

Alternatives to the dynamical Axion

- Only one massless quark and a Z_2 [Hook 15]
- Complete copy of the SM
- The Z_2 ensures $\theta_2 = \theta_{QCD}$
- No light axion: $m^2 \sim \frac{\Lambda_2^4}{f_a^2}$
- The mirror EW sector has a large vev:

$$v_2 \gg v \implies m'_q \gg m_q, \implies \Lambda' \gg \Lambda_{QCD}$$



In our work: UNIFICATION



- $SM \times SM' \rightarrow \theta = \theta'$
- 2HDM + S
- Like Rubakov but without SU(5)
- One shared U(1)PQ:
 - ◆ PQWW axion with respect to the mirror world
 - ◆ KSVZ axion with respect to SM