



Broad composite resonances and their signals at the LHC

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Da Liu, Lian-Tao Wang and **Ke-Pan Xie**, arXiv: 1901.01674;
Sunghoon Jung, Dongsub Lee and **Ke-Pan Xie**, arXiv: 1903.asap

➤ The **hierarchy problem** in **Standard Model**

The **mass** of an elementary Higgs boson is sensitive to the quantum corrections of high scale.



“Naturally” $M_h \sim M_{\text{Planck}} \sim 10^{19}$ GeV



$$\delta M_h^2 \sim \left(\frac{\lambda_{\text{NP}}}{16\pi^2} \right) \left[M_{\text{NP}}^2 \frac{1}{\epsilon} + \text{finite terms} \right]$$

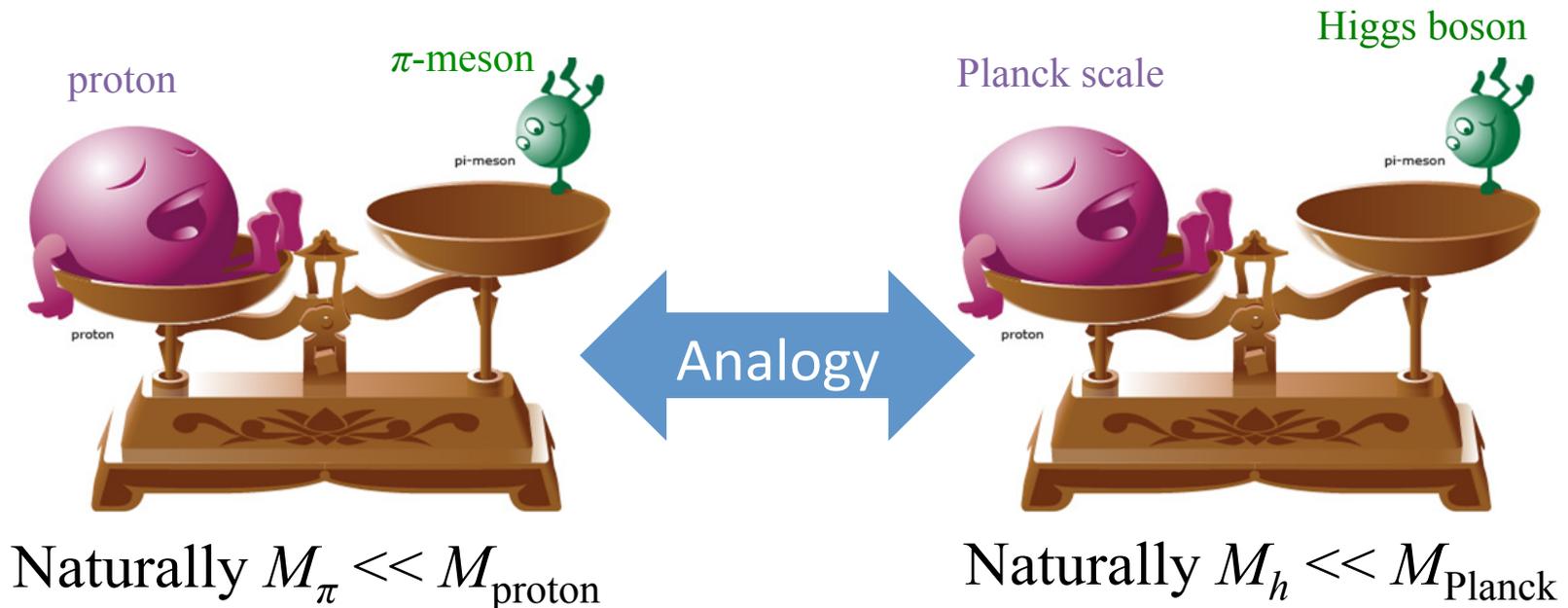
Hierarchy!



Reality $M_h = 125.09$ GeV!

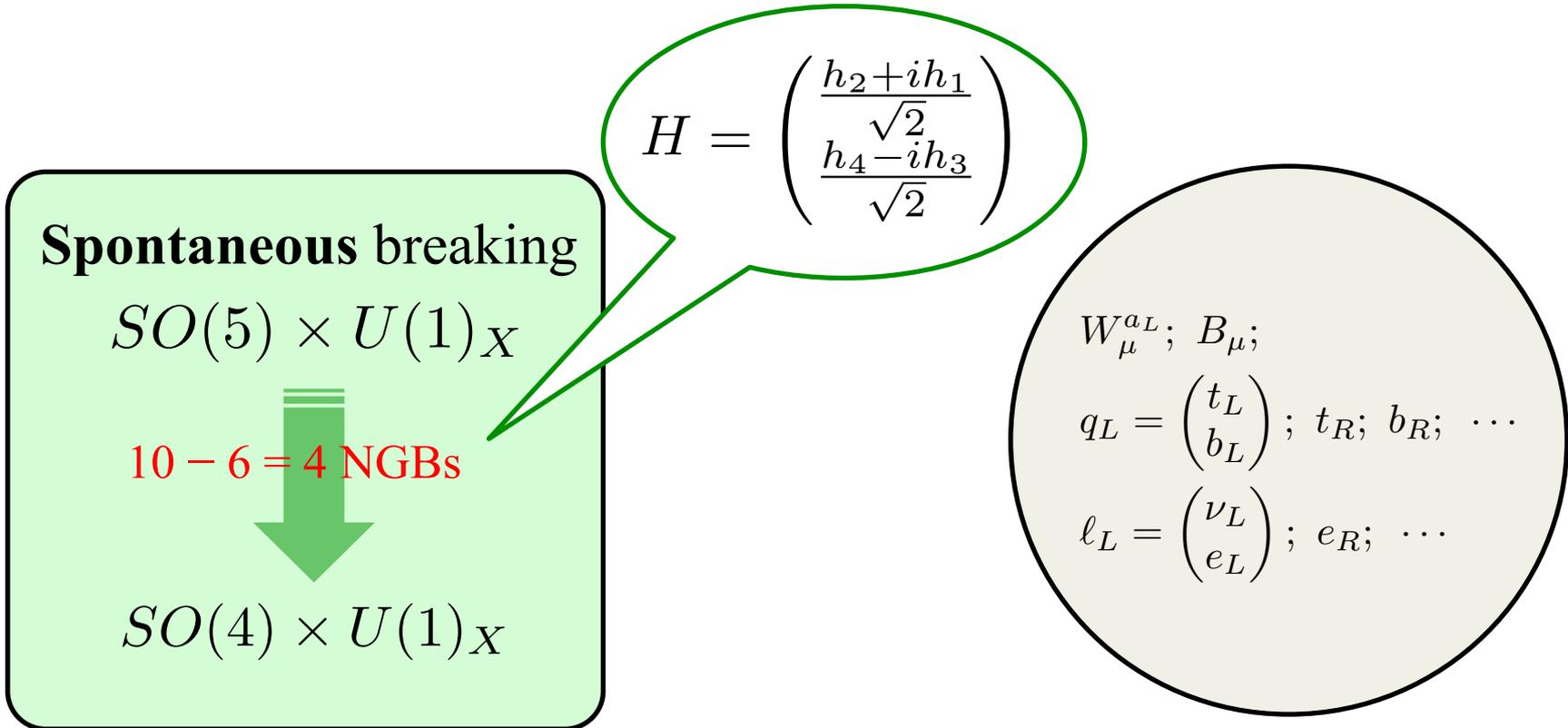
➤ The idea of the **Composite Higgs Model**

Identify the Higgs boson as the **pseudo-Nambu-Goldstone boson**, similar to the pions in low energy QCD!



➤ The Minimal Composite Higgs Model

$$\mathcal{L}_{\text{MCHM}} = \mathcal{L}_{\text{strong}} + \mathcal{L}_{\text{SM}}$$



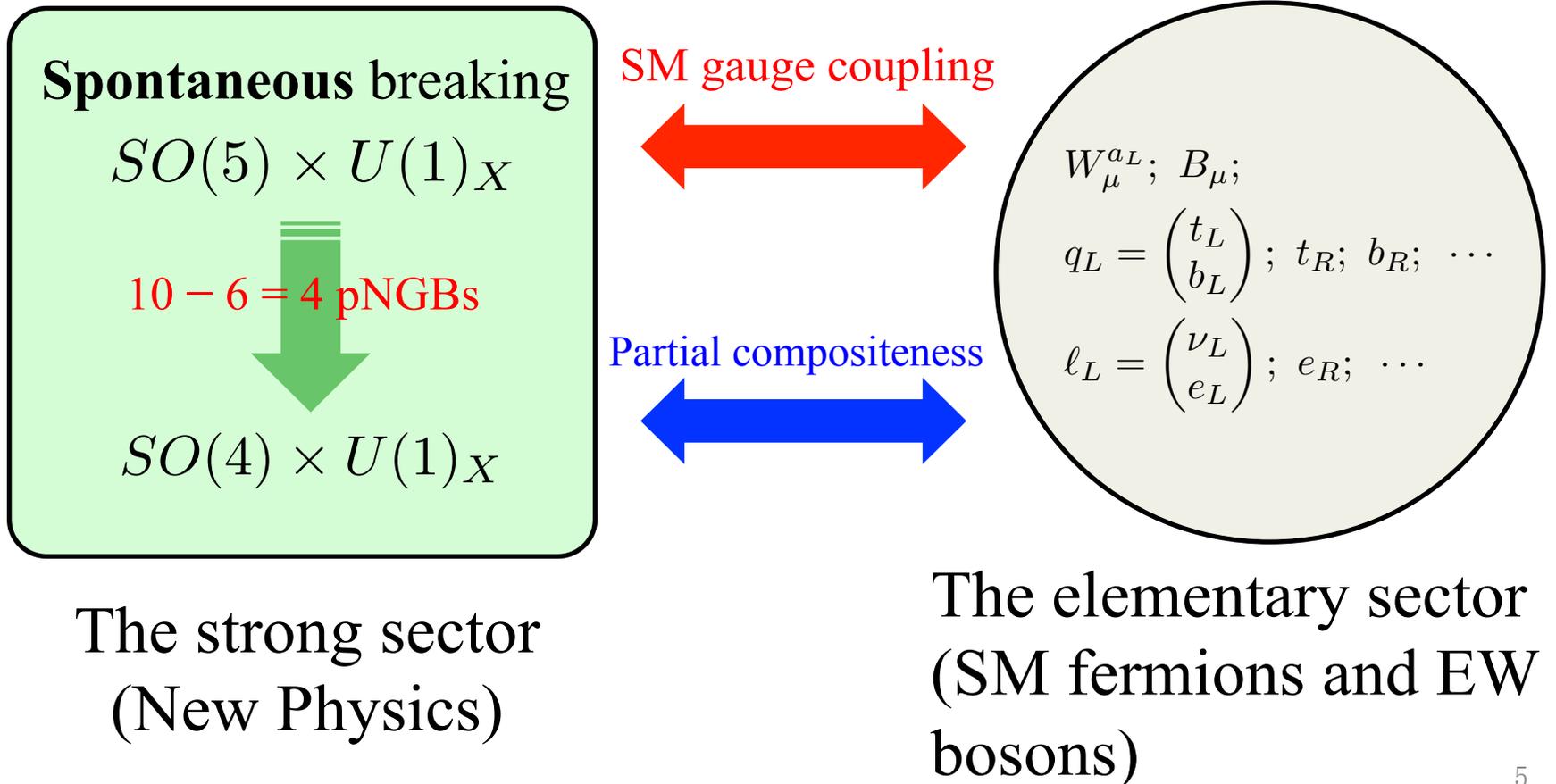
The strong sector
(New Physics)

The elementary sector
(SM fermions and EW bosons)

➤ The Minimal Composite Higgs Model

$$\mathcal{L}_{\text{MCHM}} = \mathcal{L}_{\text{strong}} + \mathcal{L}_{\text{SM}} \quad \text{Explicitly break SO(5)}$$

$$+ \mathcal{J}_{\mu}^{aL} W_{aL}^{\mu} + \mathcal{J}_{Y\mu} B^{\mu} + y_L \bar{q}_L \mathcal{O}_R + y_R \bar{u}_R \mathcal{O}_L$$



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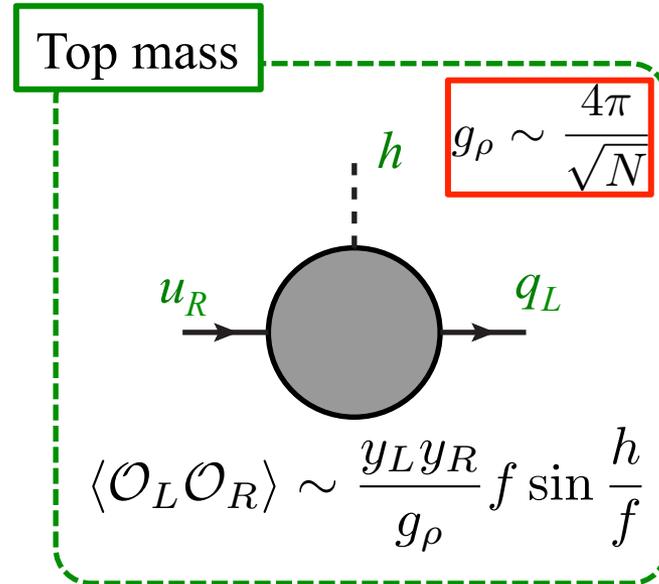
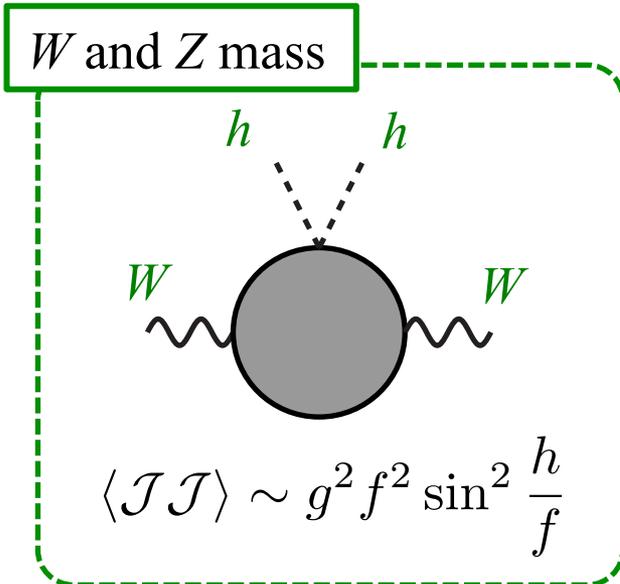
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Subgroup $SU(2)_L \times U(1)_Y$ gauged; $Y = T_R^3 + X$

q_L and u_R fill in the incomplete representation of SO(5)

$$V_{\text{eff}}(h) \approx \alpha \sin^2 \frac{h}{f} - \beta \sin^2 \frac{h}{f} \cos^2 \frac{h}{f} \quad \xrightarrow{\text{EWSB}} \quad \sin^2 \frac{\langle h \rangle}{f} = \frac{\beta - \alpha}{2\beta}$$



➤ Down to the EW scale

$$\mathcal{L}_{\text{MCHM}} = \mathcal{L}_{\text{strong}} + \mathcal{L}_{\text{SM}}$$

UV scale

$$+ \mathcal{J}_\mu^{a_L} W_{a_L}^\mu + \mathcal{J}_{Y\mu} B^\mu + y_L \bar{q}_L \mathcal{O}_R + y_R \bar{u}_R \mathcal{O}_L$$

Non-perturbative process

The Higgs doublet
pNGB

The elementary
particules

EFT

The composite resonances

$$\langle 0 | \mathcal{J}_\mu | \rho_n \rangle = \epsilon_\mu m_{\rho_n} f_n;$$

$$\langle 0 | \mathcal{O} | \Psi_n \rangle = \Delta_n$$

A CCWZ construction of
SO(5)/SO(4) Lagrangian;
see backup

EW scale

➤ The vector ρ resonances

SU(2)_L triplet ρ resonance;
robust predictions and features

$$\mathcal{J}_\mu^{a_L} W_{a_L}^\mu \rightarrow -a_\rho^2 f^2 g_\rho \rho_\mu^{a_L} \left(g_2 W_\mu^{a_L} - \frac{i}{f^2} H^\dagger \frac{\sigma^{a_L}}{2} \overleftrightarrow{D}_\mu H \right) + \dots,$$

f : SO(5)/SO(4) scale; a_ρ : the order 1 parameter; g_ρ : strong dynamics coupling

The ρ - W mixing angle

$$\sin \theta \sim \frac{g_2}{\sqrt{g_\rho^2 + g_2^2}} \approx \frac{g_2}{g_\rho}$$

The ρ -elementary quark coupling

$$g_{\rho f_L \bar{f}_L^{(\prime)}} = g_2 \sin \theta \sim \frac{g_2^2}{g_\rho}$$

The ρ -Goldstone coupling

$$\sim g_\rho \rho_\mu^{a_L} H^\dagger \frac{\sigma^{a_L}}{2} i \overleftrightarrow{D}_\mu H,$$

$$g_\rho \sim \frac{4\pi}{\sqrt{N}}$$

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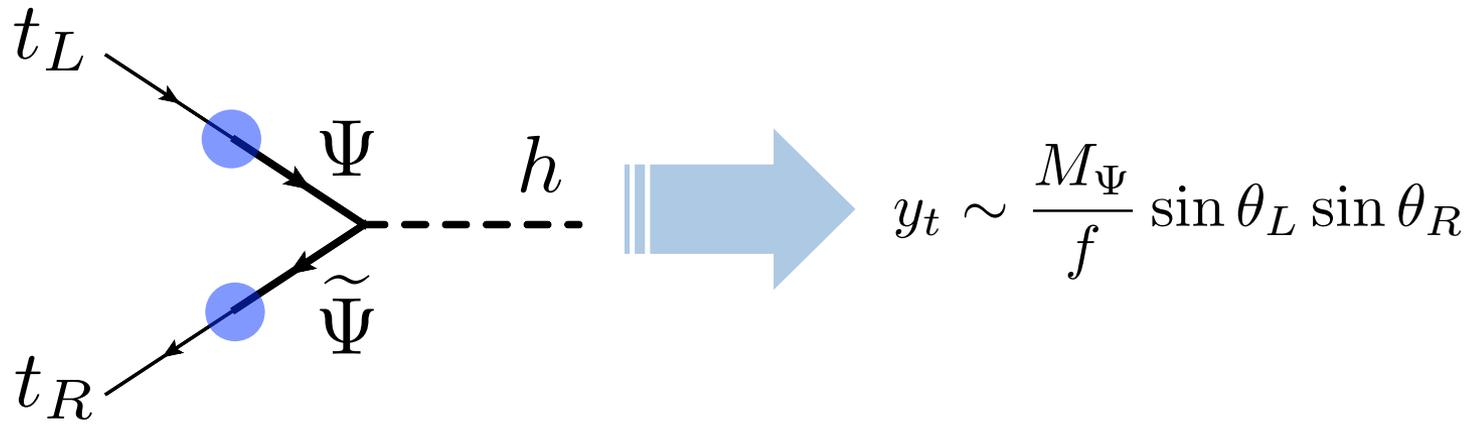
Collider phenomenology

1. **Drell-Yan** production;
2. Large partial width to SM di-boson (W^+W^- , $W^\pm Z$, $W^\pm h$, Zh) channels.

➤ The fermion Ψ resonances:

top partners;
model dependent

1. Fill the representation of SO(4);
2. Giving mass to top quark: $y_L \bar{q}_L \mathcal{O}_R + y_R \bar{t}_R \mathcal{O}_L$



3. Interactions: $\mathcal{L}_{\text{int}} \sim c_1 g_\rho \rho_\mu \bar{\Psi} \gamma^\mu \Psi$; $c_1 \sim \mathcal{O}(1)$.

$g_{\rho \Psi \bar{\Psi}} \sim g_\rho, \quad g_{\rho q_L \bar{q}_L} \sim g_\rho \sin^2 \theta_L$

➤ The fermion Ψ resonances:

$$y_L \bar{q}_L \mathcal{O}_R \rightarrow y_L f \bar{F}_L U \Psi_R;$$

$$y_R \bar{u}_R \mathcal{O}_L \rightarrow y_R f \bar{F}'_R U \Psi_L;$$

F_L and F'_R : some multiplets of SO(5);

Ψ : some multiplets of SO(4).

top partners;
model dependent

Goldstone matrix
$$U[\vec{h}] = \exp \left\{ i \frac{\sqrt{2}}{f} h^i T^i \right\}$$

 T^i : the 4 broken generators

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T^i : the 4 broken generators

The first scenario by [Agashe et al, Nucl.Phys. B719 \(2005\) 165-187](#)

$q_L = (t_L, b_L)^T$ and t_R are both embedded in **4** of SO(5):

$$q_L^4 = (t_L, b_L, 0, 0)^T; \quad t_R^4 = (0, 0, t_R, 0)^T.$$

Ψ in **(2, 1)** of SO(4) = SU(2)_L × SU(2)_R:

$$\Psi_{(2,1)} = (T, B)^T$$

The top quark mass

$$y_L f \bar{q}_L^4 U \Psi_R - i y_R f \bar{t}_R^4 U \Psi_L \Rightarrow M_t = \frac{y_L y_R v f}{2 M_\Psi} + \dots$$

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However this scenario is constrained **very stringently**:

$$-\frac{i}{4f^2} \bar{\Psi} \gamma^\mu \sigma^{aL} \Psi H^\dagger \sigma^{aL} \overleftrightarrow{D}_\mu H \rightarrow -\frac{i}{4f^2} \bar{q}_L \gamma^\mu \sigma^{aL} q_L H^\dagger \sigma^{aL} \overleftrightarrow{D}_\mu H \sin^2 \theta_L$$

Because of the EW precision test:

$$\delta g_{Z b_L \bar{b}_L} = \frac{v^2}{8f^2} \sin^2 \theta_L$$

$$|\delta g_{Z b_L \bar{b}_L}| < 0.00061 \text{ (LEP)}$$

$$\sin \theta_L = \frac{y_L f}{\sqrt{M_\Psi^2 + y_L^2 f^2}}$$

Not favored by the experiment! See [Nucl.Phys. B742 \(2006\) 59-85](#).

➤ The fermion Ψ resonances:

top partners;
model dependent

Contino *et al*, Phys.Rev. D75 (2007) 055014

$q_L = (t_L, b_L)^T$ and t_R are both embedded in $\mathbf{5}$ of SO(5):

$$q_L^{\mathbf{5}} = \frac{1}{\sqrt{2}}(ib_L, b_L, it_L, -t_L, 0)^T; \quad t_R^{\mathbf{5}} = \frac{1}{\sqrt{2}}(0, 0, 0, 0, t_R)^T$$

Ψ in $(\mathbf{2}, \mathbf{2})$ of SO(4) = SU(2)_L × SU(2)_R:

$$\Psi_{(\mathbf{2}, \mathbf{2})} = \frac{1}{\sqrt{2}} \begin{pmatrix} iB - iX_{5/3} \\ B + X_{5/3} \\ iT + iX_{2/3} \\ -T + X_{2/3} \end{pmatrix}; \quad \Rightarrow \quad \Psi = \underbrace{\begin{pmatrix} T \\ B \end{pmatrix}}_{\text{doublet } Q_{1/6}} \oplus \underbrace{\begin{pmatrix} X_{5/3} \\ X_{2/3} \end{pmatrix}}_{\text{doublet } Q_X}$$

The top quark mass

$$y_L f \bar{q}_L^{\mathbf{5}} U \Psi_R + y_L f t_R^{\mathbf{5}} U \Psi_L = y_L f \bar{q}_L Q_R + y_R \bar{t}_R \tilde{H}^\dagger Q_L - y_R \bar{t}_R H^\dagger Q_{XL} + \dots$$

$$\Rightarrow M_t = \frac{y_L f y_R v}{\sqrt{2} \sqrt{M_\Psi^2 + y_L^2 f^2}}$$

And **NO $Z b_L b_L$ deviation** at tree level!

$$\frac{1}{2} \bar{Q} \gamma^\mu Q \frac{1}{2f^2} H^\dagger i \overleftrightarrow{D}_\mu H - \bar{Q} \gamma^\mu \frac{\sigma^{aL}}{2} Q \frac{1}{f^2} H^\dagger \frac{\sigma^{aL}}{2} i \overleftrightarrow{D}_\mu H \Rightarrow \delta g_{Z b_L \bar{b}_L} = 0$$

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$q_L = (t_L, b_L)^T$ and t_R are both embedded in $\mathbf{5}$ of $SO(5)$:

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Agashe *et al*, Phys. Lett. B641, 62 (2006)

The custodial symmetry for T -parameter: $SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$;

$$\Rightarrow \delta Q_V^3 \equiv \delta(T^{3L} + T^{3R}) = 0;$$

For $\mathbf{5}$ representation, $T^{3L}(B) = T^{3R}(B) = -\frac{1}{2}$;

$$\Rightarrow \delta T^{3L}(B) = \delta T^{3R}(B); \quad \Rightarrow \delta T^{3L}(B) = 0;$$

$$\delta g_{ZB\bar{B}} = \frac{g}{c_W} (\delta T^{3L} - \delta Q_{S_W^2}) = 0;$$

Protected!

And **NO $Zb_L b_L$ deviation** at tree level!

$$\frac{1}{2}\bar{Q}\gamma^\mu Q \frac{1}{2f^2} H^\dagger i\overleftrightarrow{D}_\mu H - \bar{Q}\gamma^\mu \frac{\sigma^{aL}}{2} Q \frac{1}{f^2} H^\dagger \frac{\sigma^{aL}}{2} i\overleftrightarrow{D}_\mu H \Rightarrow \delta g_{Zb_L \bar{b}_L} = 0$$

– Other studied scenarios:

$q_L = (t_L, b_L)^T$ is elementary, embedded in **5** of SO(5);
 t_R is a **composite resonance**, embedded in **1** of SO(4);

$$q_L^5 = \frac{1}{\sqrt{2}}(ib_L, b_L, it_L, -t_L, 0)^T;$$

$$y_L f q_L^5 U t_R = -y_L \bar{q}_L \tilde{H} t_R + \dots \quad \text{Simone et al, JHEP 1304 (2013) 004}$$

$q_L = (t_L, b_L)^T$ is elementary, embedded in **14** of SO(5);
 t_R is a **composite resonance**, embedded in **1** of SO(4);

Simone et al, JHEP 1304 (2013) 004

Matsedonskyi et al, JHEP 1604 (2016) 003

.....

➤ General features of the previous models:

The existence of triplet **vector resonance** ρ , and

1. **Drell-Yan** production;
2. Strong coupling to SM di-boson (W^+W^- , $W^\pm Z$, $W^\pm h$, Zh) channels.

The top partners Ψ , and

1. Give mass to top quark through mixing and EWSB;
2. t_L is elementary and $\rho t_L t_L$ interaction suppressed by $\sin^2\theta_L$.
3. No matter t_R is elementary or composite, it couples to ρ weakly because of its $SU(2)_L$ quantum number.

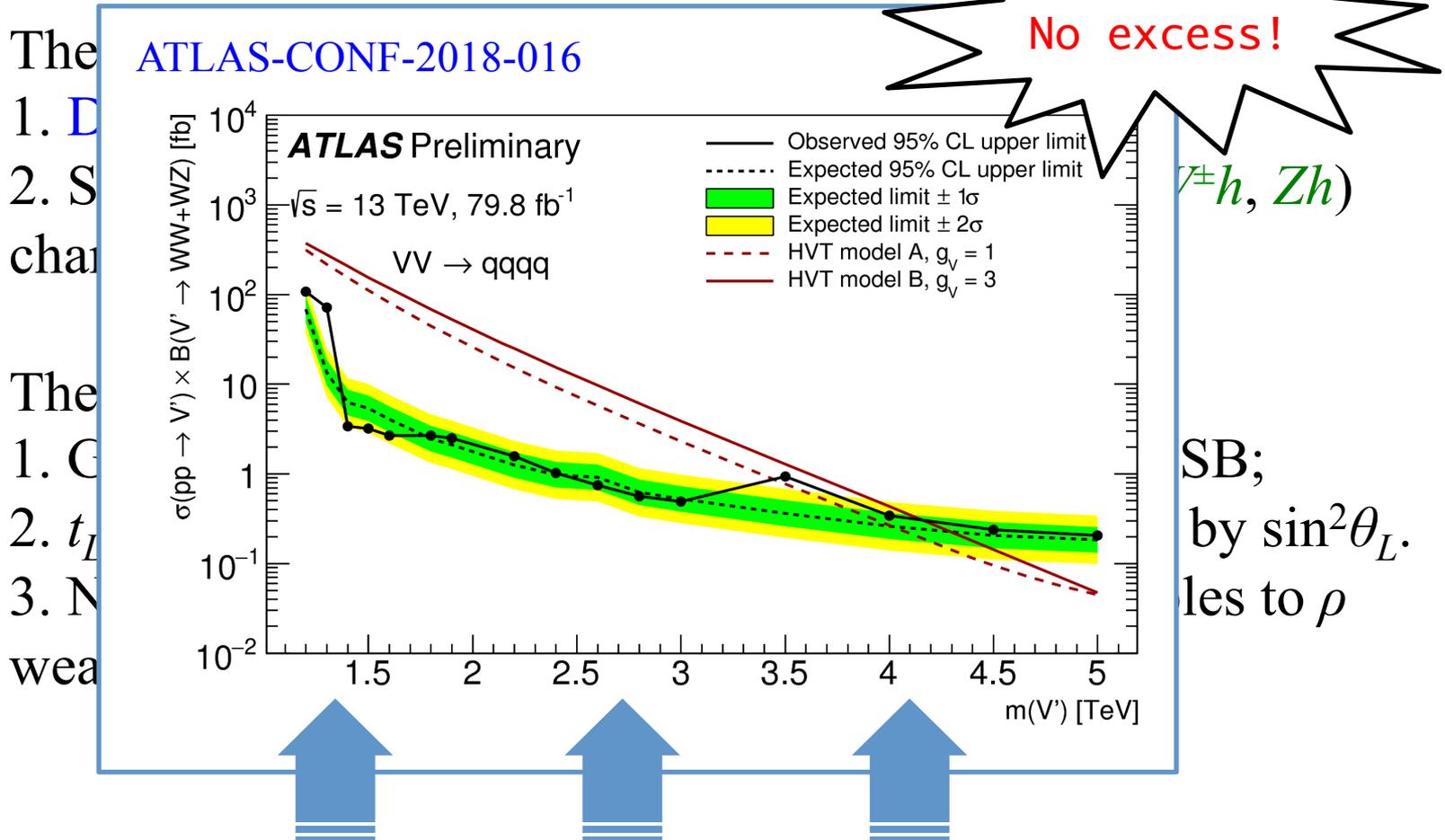


Universal prediction:

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A Drell-Yan produced ρ from the **di-boson** channel!

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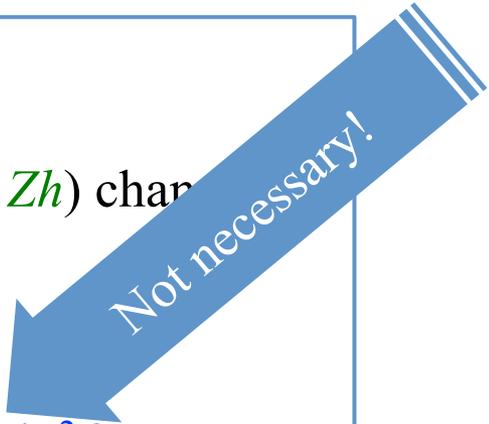
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Not necessary!

➤ A model that $q_L = (t_L, b_L)^T$ is **composite**

Da Liu, Lian-Tao Wang and **Ke-Pan Xie**, arXiv: 1901.01674;

Composite fermion sector -- **(2, 2)** of the SO(4):

$Zb_L b_L$ protected!

$$\Psi_L = \frac{1}{\sqrt{2}} \begin{pmatrix} ib_L - iX_L \\ b_L + X_L \\ it_L + iT_L \\ -t_L + T_L \end{pmatrix} = \underbrace{\begin{pmatrix} t_L \\ b_L \end{pmatrix}}_{q_L} \oplus \underbrace{\begin{pmatrix} X_L \\ T_L \end{pmatrix}}_{q_L^X}$$

Elementary fermion sector -- **5** of the SO(5):

$$t_R^5 = (0, 0, 0, 0, t_R)^T, \quad q_R^{X5} = \frac{1}{\sqrt{2}} (-iX_R, X_R, iT_R, T_R, 0)^T.$$

The **Yukawa** couplings:

$$\begin{aligned} & -y_{1R} f \bar{q}_R^{X5} U \Psi_L - y_{2R} f \bar{t}_R^5 U \Psi_L \\ = & \underbrace{-y_{1R} f \bar{q}_R^X q_L^X}_{\text{top partner mass}} - y_{2R} \underbrace{(\bar{t}_R \tilde{H}^\dagger q_L - \bar{t}_R H^\dagger q_L^X)}_{\text{top mass}} + \dots \end{aligned}$$

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The **interactions with ρ** :

$$\mathcal{L}_{\text{int}} \supset c_1 \bar{\Psi}_L \gamma^\mu T^{a_L} \Psi_L g_\rho \rho^{a_L} = c_1 g_\rho \rho_\mu^{a_L} \bar{q}_L \gamma^\mu \frac{\sigma^{a_L}}{2} q_L + \dots$$

$$g_{\rho^- t_L \bar{b}_L} = \frac{g_\rho}{\sqrt{2}}; \quad g_{\rho^0 t_L \bar{t}_L} = -g_{\rho^0 b_L \bar{b}_L} = \frac{g_\rho}{2},$$

Without suppression!

For the pNGB modes, the interactions:

$$\sim g_\rho \rho_\mu^{a_L} H^\dagger \frac{\sigma^{a_L}}{2} i \overleftrightarrow{D}_\mu H,$$

$$\frac{\Gamma_{\rho^0 \rightarrow W^+ W^-}}{M_\rho} = \frac{g_\rho^2}{192\pi};$$

$$\frac{\Gamma_{\rho^0 \rightarrow t\bar{t}}}{M_\rho} = \frac{N_c g_\rho^2}{96\pi};$$

$$\frac{\Gamma_{\rho^0 \rightarrow t\bar{t}}}{\Gamma_{\rho^0 \rightarrow W^+ W^-}} = 2N_c = 6.$$

Collider phenomenology

1. **Drell-Yan** production;
2. Dominantly decay to SM third generation quark (tb , tt , bb);

➤ A model that $q_L = (t_L, b_L)$

Da Liu, Lian-Tao Wang and Ke-Pan Xie

The **interactions with ρ** :

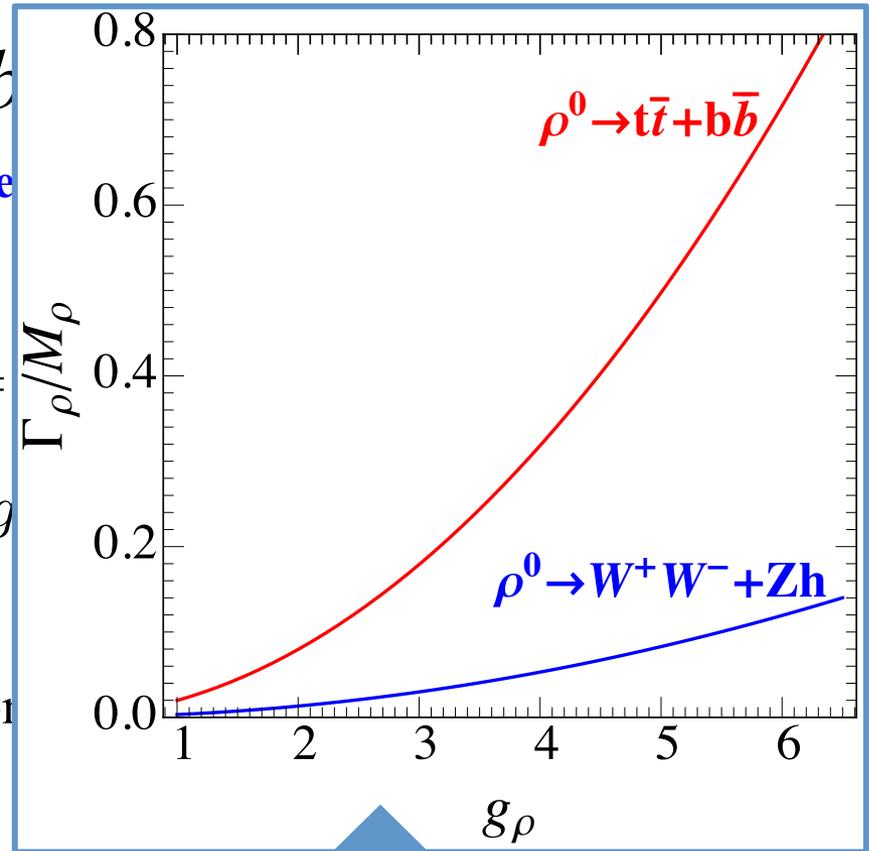
$$\mathcal{L}_{\text{int}} \supset c_1 \bar{\Psi}_L \gamma^\mu T^{a_L} \Psi_L g_\rho \rho^{a_L} =$$

$$g_{\rho^- t_L \bar{b}_L} = \frac{g_\rho}{\sqrt{2}}; \quad g_{\rho^0 t_L \bar{t}_L} = -g_\rho$$

Without suppression!

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$$\sim g_\rho \rho_\mu^{a_L} H^\dagger \frac{\sigma^{a_L}}{2} i \overleftrightarrow{D}_\mu H,$$



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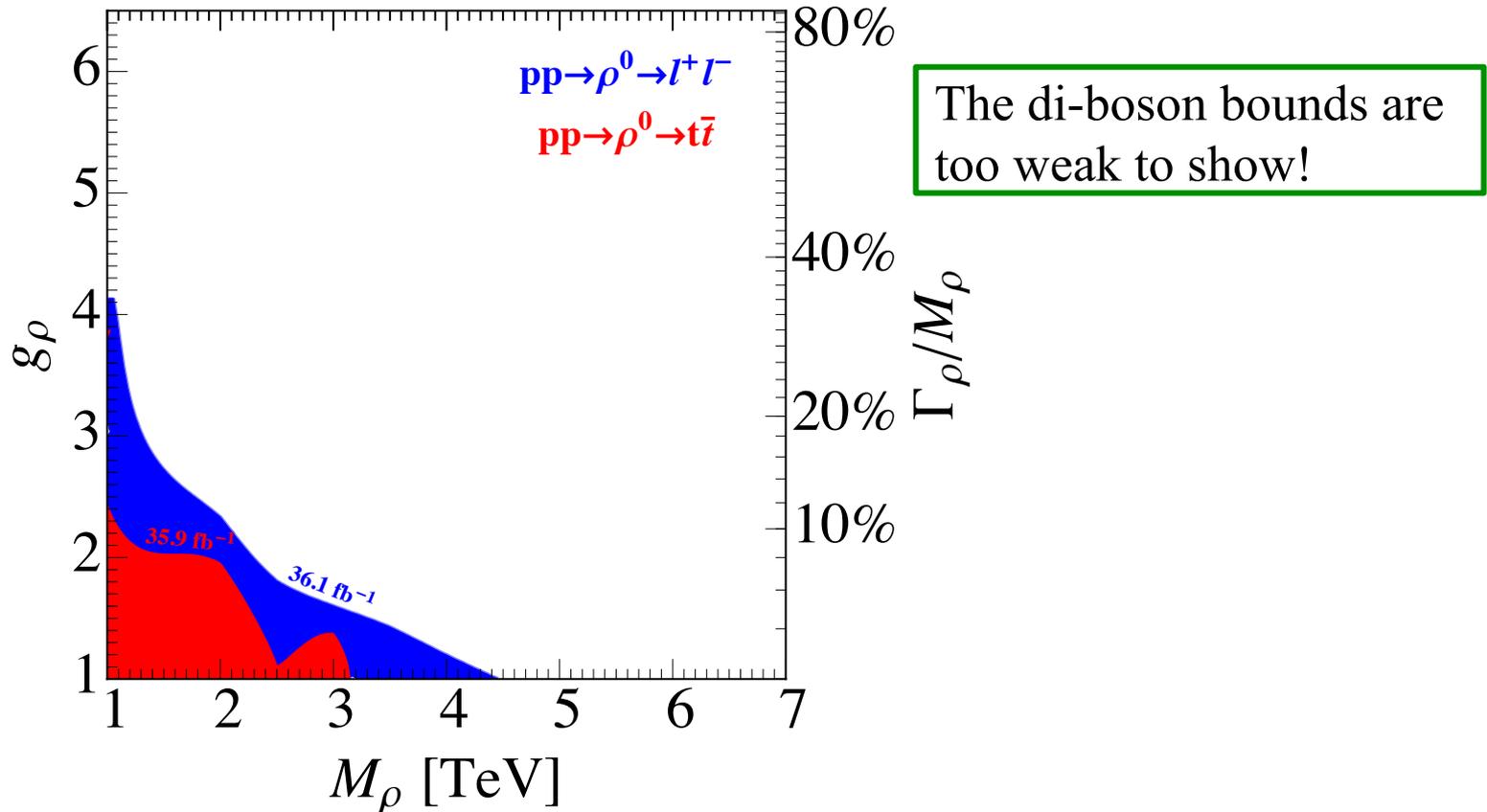
Collider phenomenology

1. Drell-Yan production;
2. Dominantly decay to SM third generation quarks (tb, tt, bb);
3. Can easily be **broad**!

➤ A model that $q_L = (t_L, b_L)^T$ is **composite**

Da Liu, Lian-Tao Wang and **Ke-Pan Xie**, arXiv: 1901.01674;

Current constraints from the experiment:

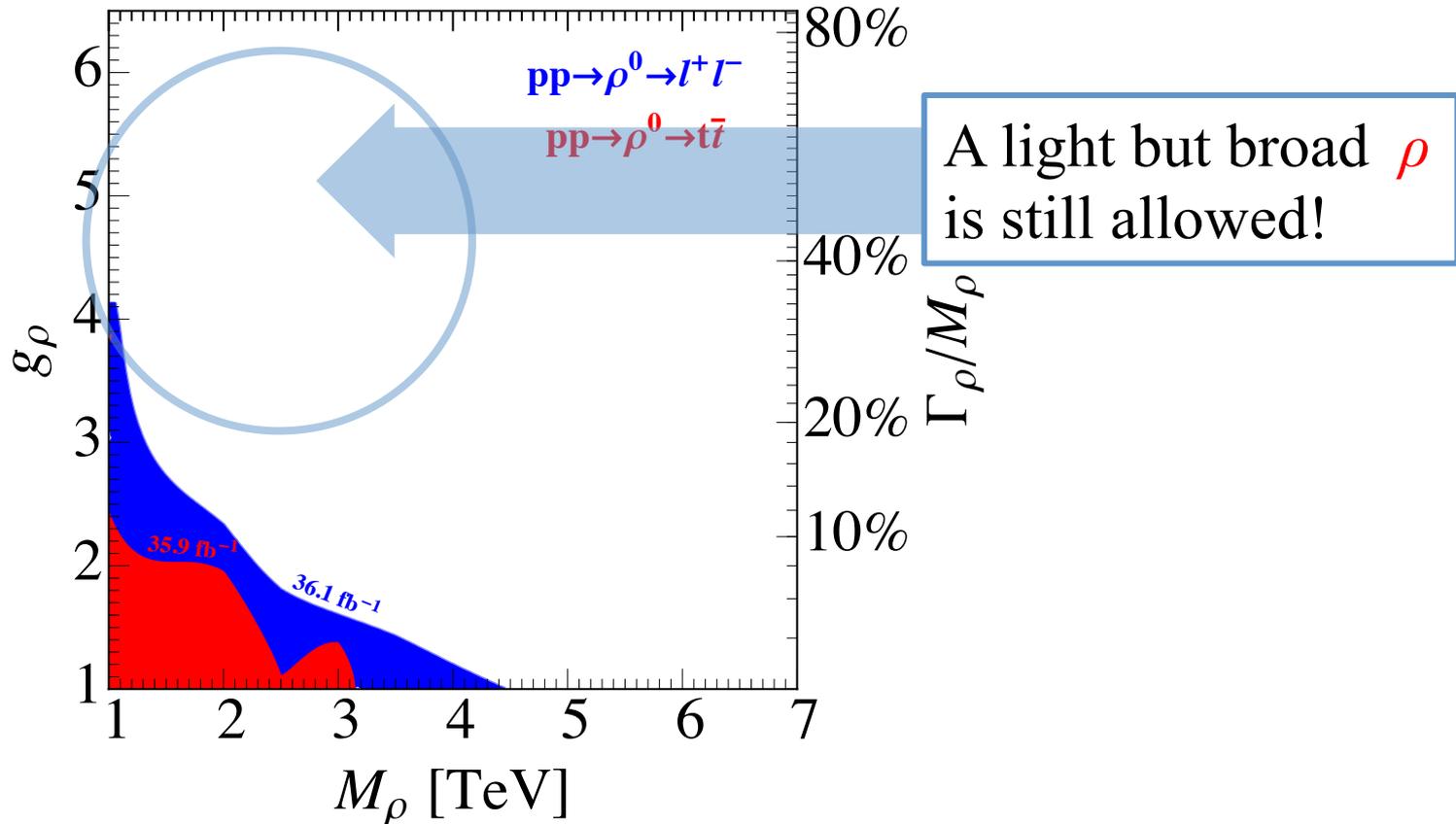


The $t\bar{t}$ constraint is from CMS 1810.05905; the l^+l^- constraint is from ATLAS 1707.02424.

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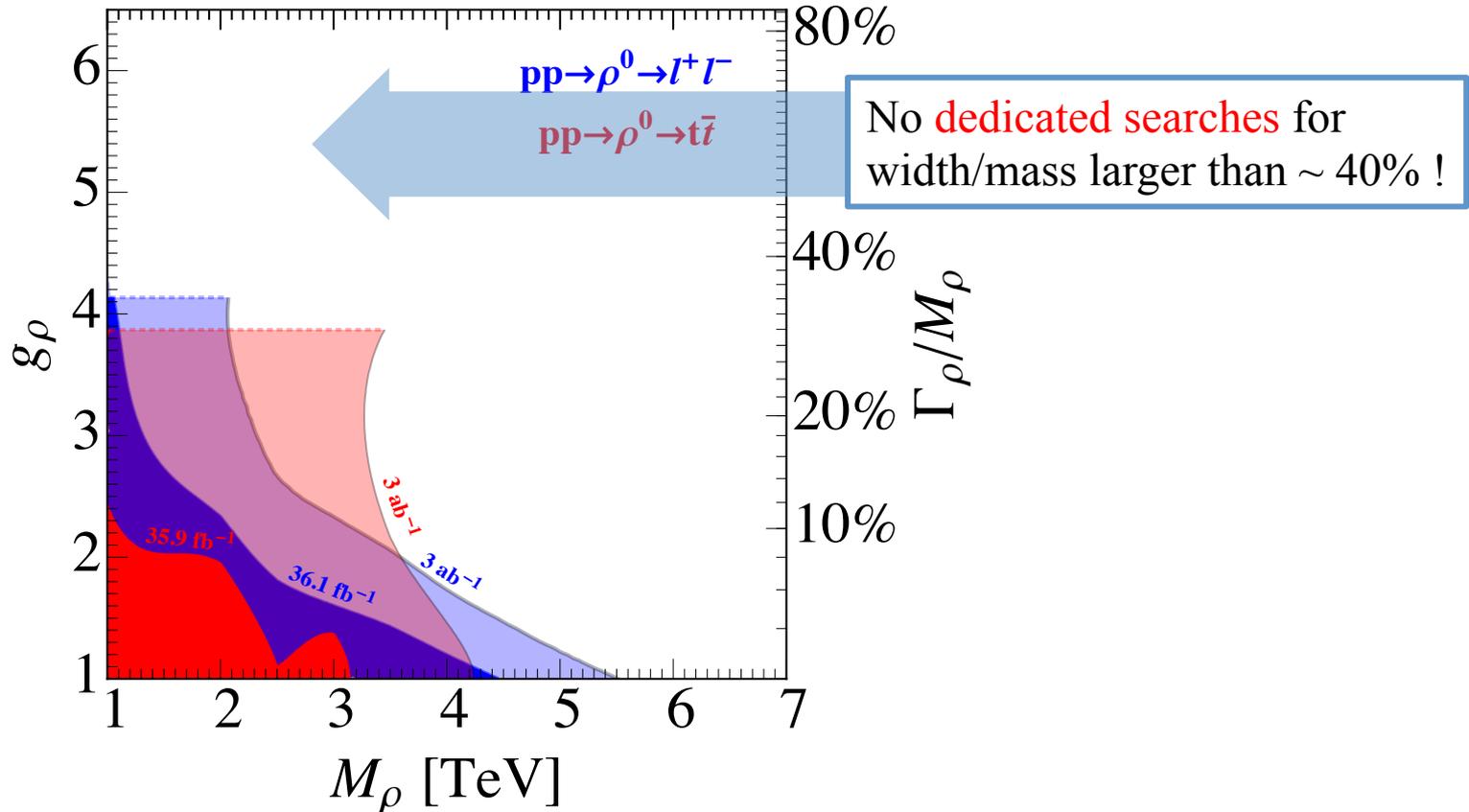


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Rescaling current constraints to the **HL-LHC**:

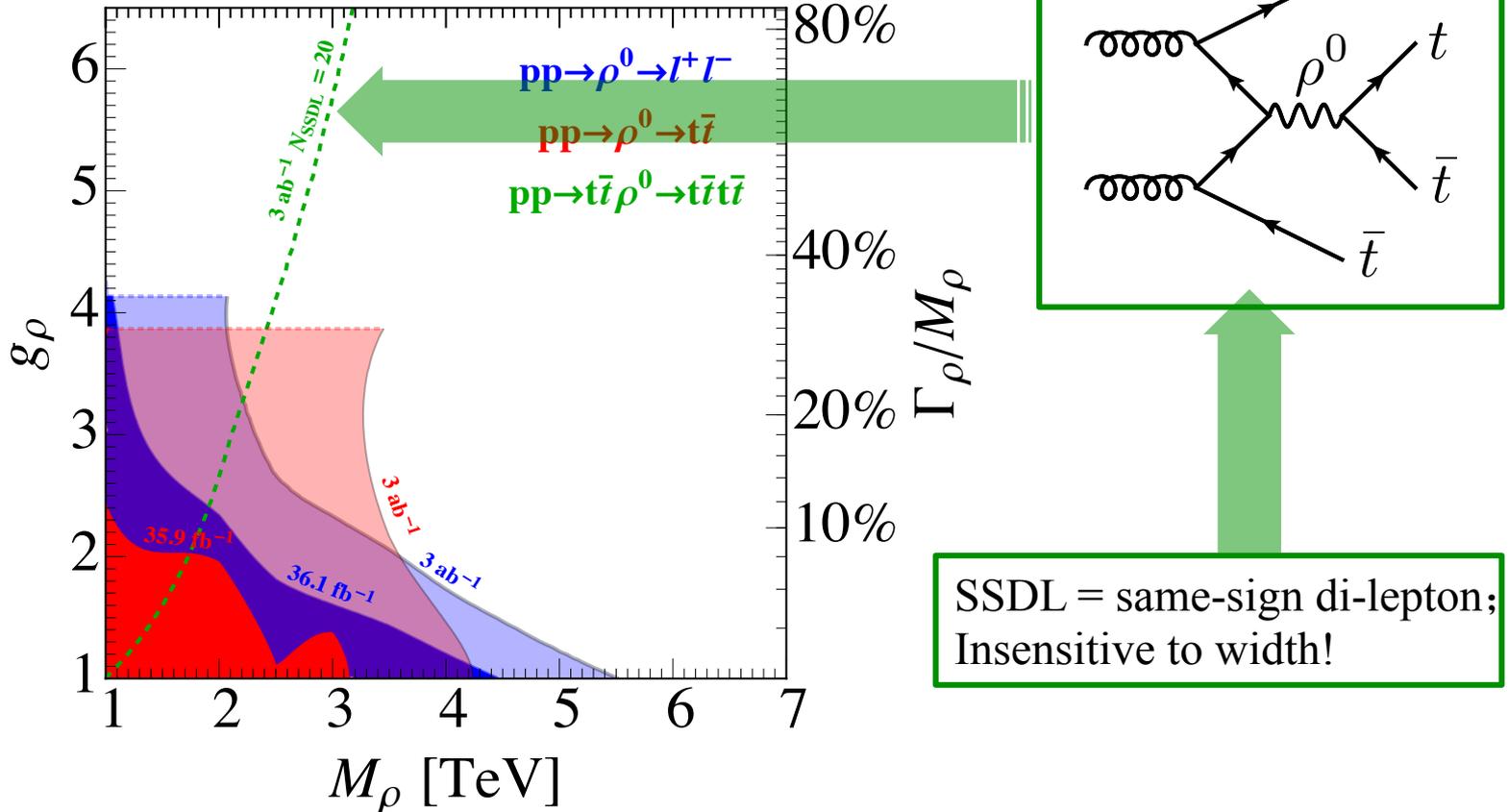


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The tt scattering process to probe large width region:



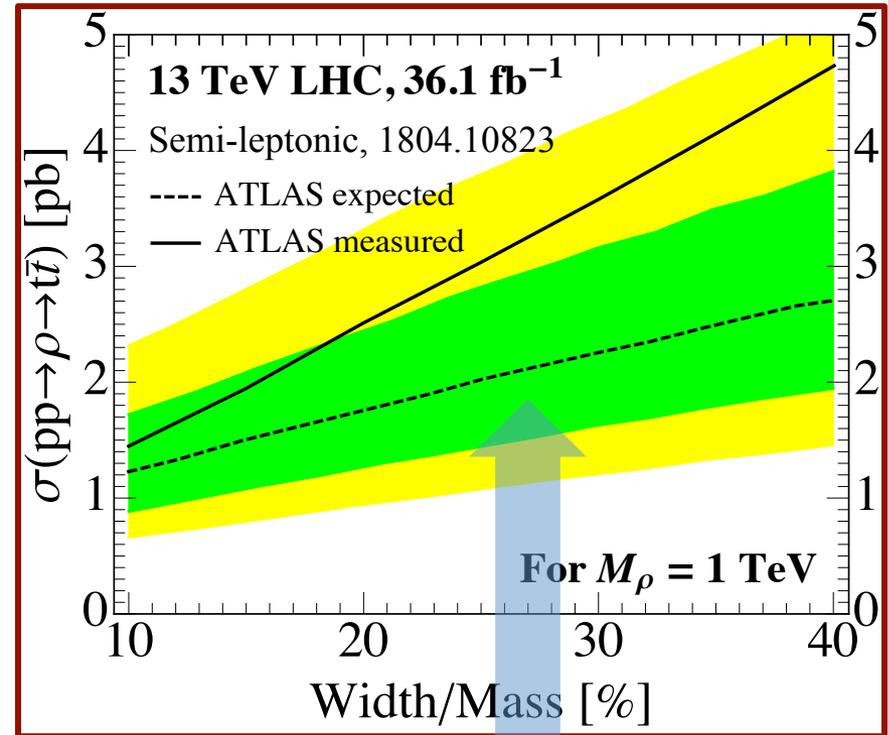
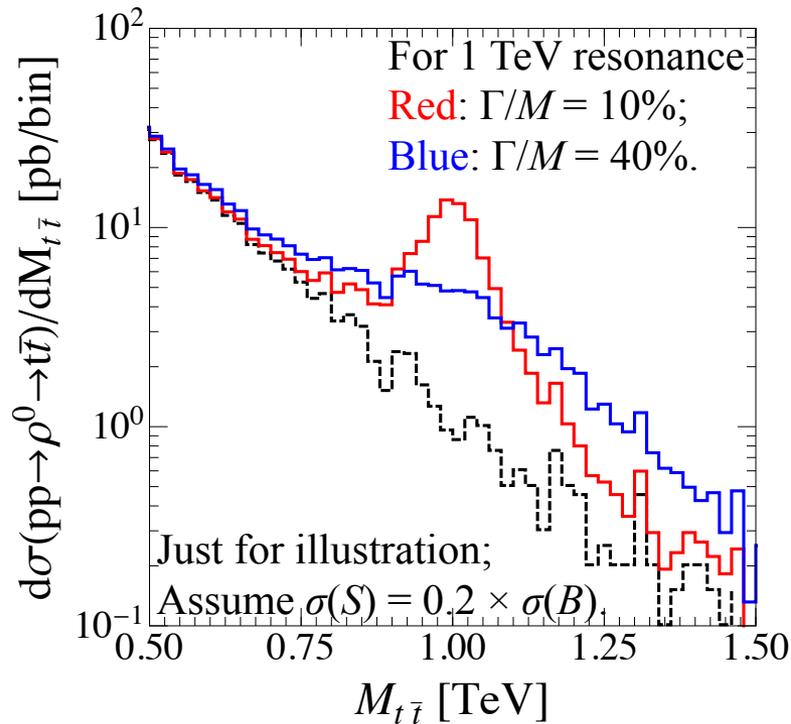
The tt constraint is from CMS 1810.05905; the $l^+ l^-$ constraint is from ATLAS 1707.02424.

➤ How to search for such a broad *tt* resonance via the Drell-Yan production?

Sunghoon Jung, Dongsub Lee and **Ke-Pan Xie**, arXiv: 1903.asap;



- The traditional approach: fit **one** observable: the **invariant mass**;



- The bound gets worse in large width region, as the resonant peak is **smeared out**.

- To improve the efficiency at **large width region**, **more** kinematic information is needed!

Emmmmm...Which observable(s)
should I use?
Energy? Transverse momentum?
Rapidity? Azimuthal angle?
Spin correlations?



- To improve the efficiency at **large width region**, **more** kinematic information is needed!

Just tell me **all the observables**,
and then I can find the answer
automatically.



The **D**eep **N**eural **N**etwork

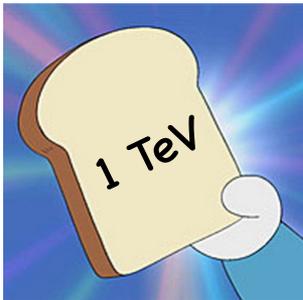


➤ The **process** considered in this work:

Signal : $pp \rightarrow \rho^0 \rightarrow t\bar{t} \rightarrow 1\ell^\pm + \text{jets}$

Background : SM $pp \rightarrow t\bar{t} \rightarrow 1\ell^\pm + \text{jets}$

– The **benchmarks**:

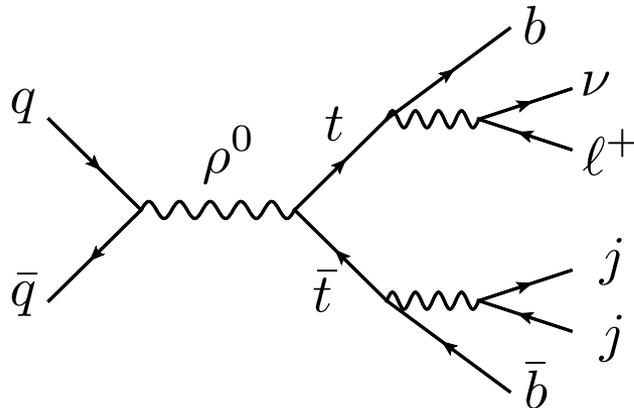


Mass $M_\rho = 1 \text{ TeV}$;
width $\Gamma_\rho/M_\rho = 10\%, 20\%, 30\% \text{ and } 40\%$;



Mass $M_\rho = 5 \text{ TeV}$;
width $\Gamma_\rho/M_\rho = 10\%, 20\%, 30\% \text{ and } 40\%$.

– We define 2 kinematic regions:



For $M_\rho = 1 \text{ TeV}$

The resolved region:

1. $1\ell^\pm$ with $p_T > 30 \text{ GeV}$ and $|\eta| < 2.5$;
2. $\cancel{E}_T > 20 \text{ GeV}$ and $\cancel{E}_T + M_T > 60 \text{ GeV}$;
3. 4 jets with $p_T > 25 \text{ GeV}$ and $|\eta| < 2.5$;

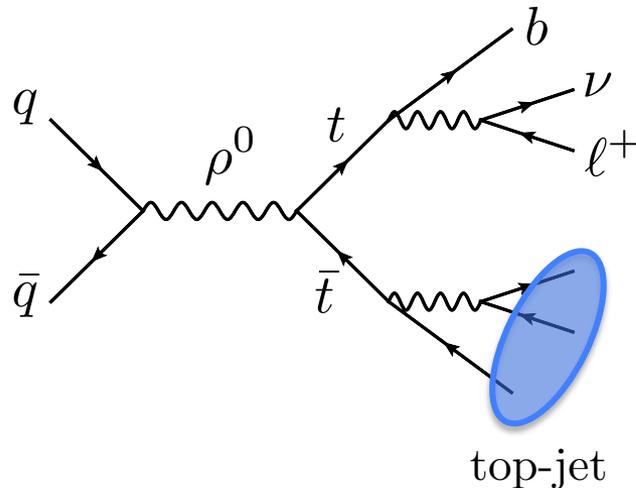
26 low-level observables can be used:

1	2	3	4	5	6	7	8	9	10	11	12	13
E^ℓ	p_T^ℓ	η^ℓ	ϕ^ℓ	\cancel{E}_T	$\phi^{\cancel{E}_T}$	E^{j1}	p_T^{j1}	η^{j1}	ϕ^{j1}	b^{j1}	E^{j2}	p_T^{j2}
14	15	16	17	18	19	20	21	22	23	24	25	26
η^{j2}	ϕ^{j2}	b^{j2}	E^{j3}	p_T^{j3}	η^{j3}	ϕ^{j3}	b^{j3}	E^{j4}	p_T^{j4}	η^{j4}	ϕ^{j4}	b^{j4}

* b^j : the b-tag observable, 1 for a b-tagged jet and 0 otherwise.

SM background cross section after cuts: 68.9 pb (K -factor included)

– We define 2 **kinematic regions**:



For $M_\rho = 1 \text{ TeV}$ and 5 TeV

The boosted region:

1. $1\ell^\pm$ with $p_T > 30 \text{ GeV}$ and $|\eta| < 2.5$;
2. $\cancel{E}_T > 20 \text{ GeV}$ and $\cancel{E}_T + M_T > 60 \text{ GeV}$;
3. 1 top jet with $p_T > 300 \text{ GeV}$ and $|\eta| < 2.0$;
4. 1 selected jet with $p_T > 25 \text{ GeV}$ and $|\eta| < 2.5$ and $\Delta R(j, \ell) < 1.5$.

15 low-level observables can be used:

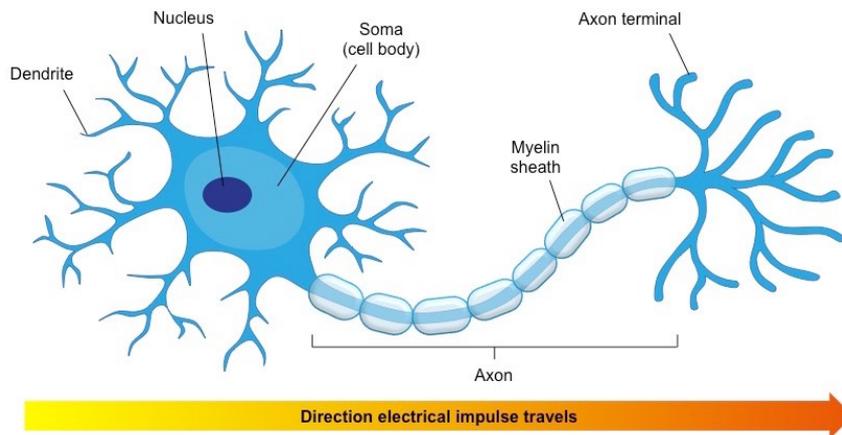
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
E^ℓ	p_T^ℓ	η^ℓ	ϕ^ℓ	\cancel{E}_T	$\phi^{\cancel{E}_T}$	$E^{j_{\text{sel}}}$	$p_T^{j_{\text{sel}}}$	$\eta^{j_{\text{sel}}}$	$\phi^{j_{\text{sel}}}$	$b^{j_{\text{sel}}}$	$E^{j_{\text{top}}}$	$p_T^{j_{\text{top}}}$	$\eta^{j_{\text{top}}}$	$\phi^{j_{\text{top}}}$

* b^j : the b-tag observable, 1 for a b-tagged jet and 0 otherwise.

SM background cross section after cuts: 2.88 pb (K -factor included)

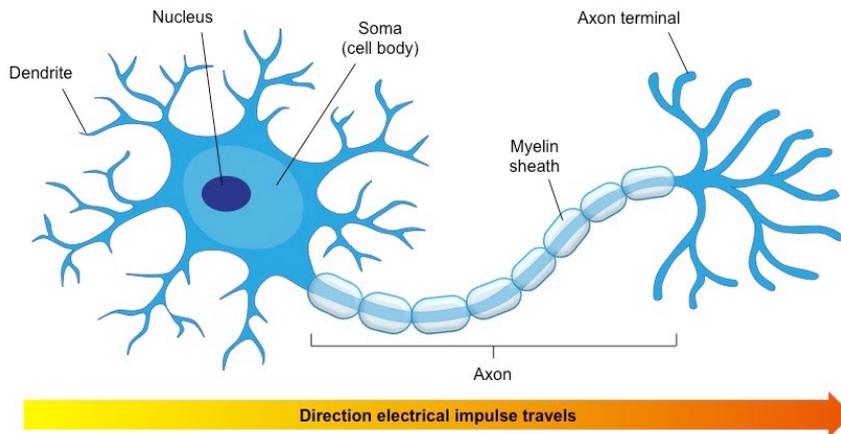
- DNN is a kind of **machine learning** technique (alternative: BDT [Boosted Decision Tree], SVM [Support Vector Machine], etc);
- It is vaguely inspired by the **biological** neural networks that constitute animal brains. [wikipedia]
- The basic unit of the DNN: **neuron**

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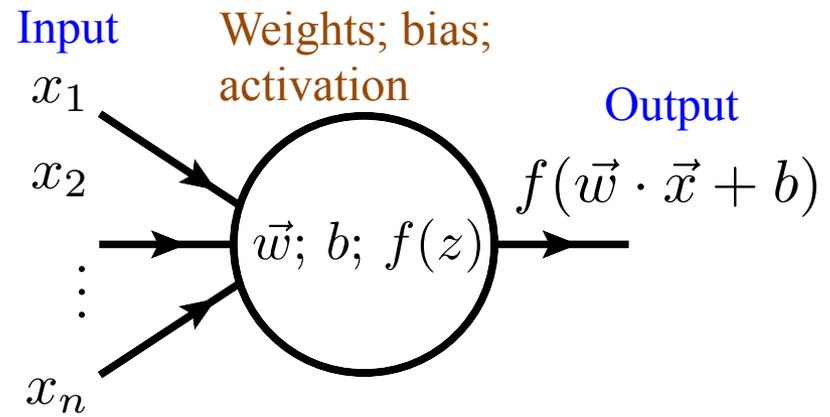


A biological neuron

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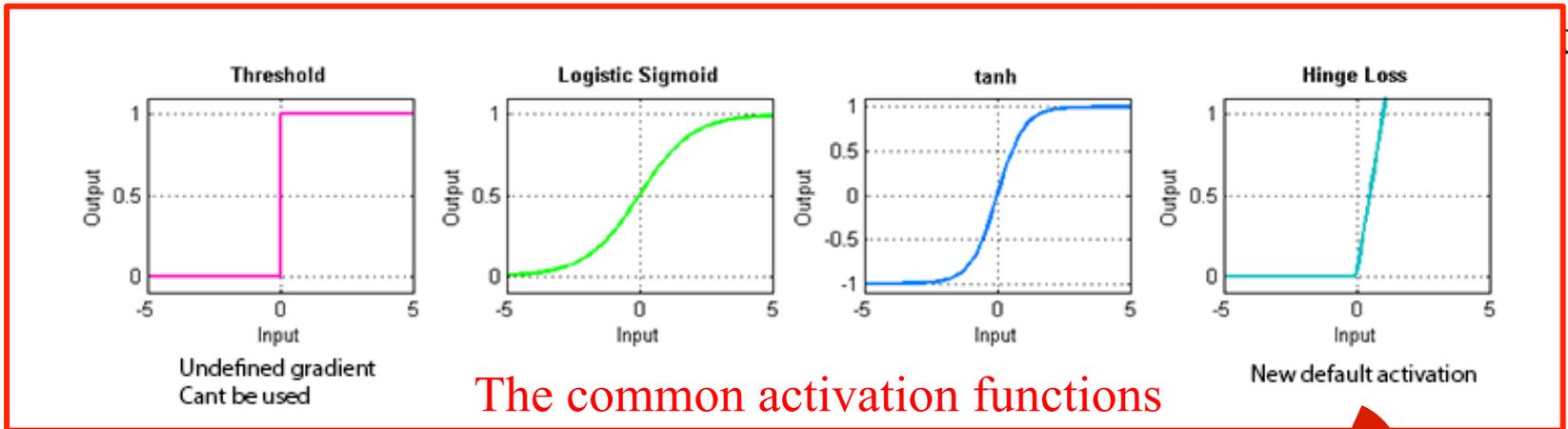


A biological neuron

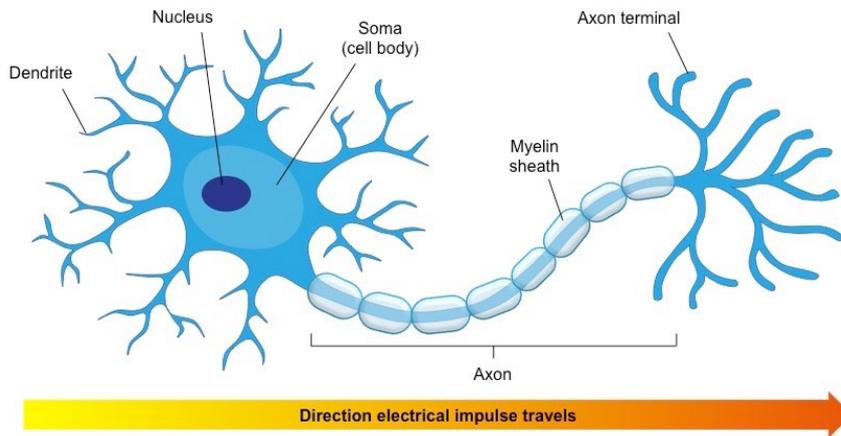


An artificial neuron

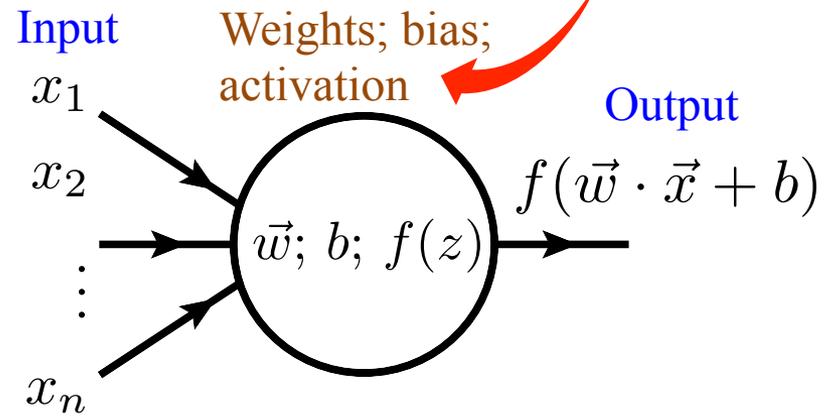
- DNN is a kind of **machine learning** technique



- The basic unit of the DNN: **neuron**

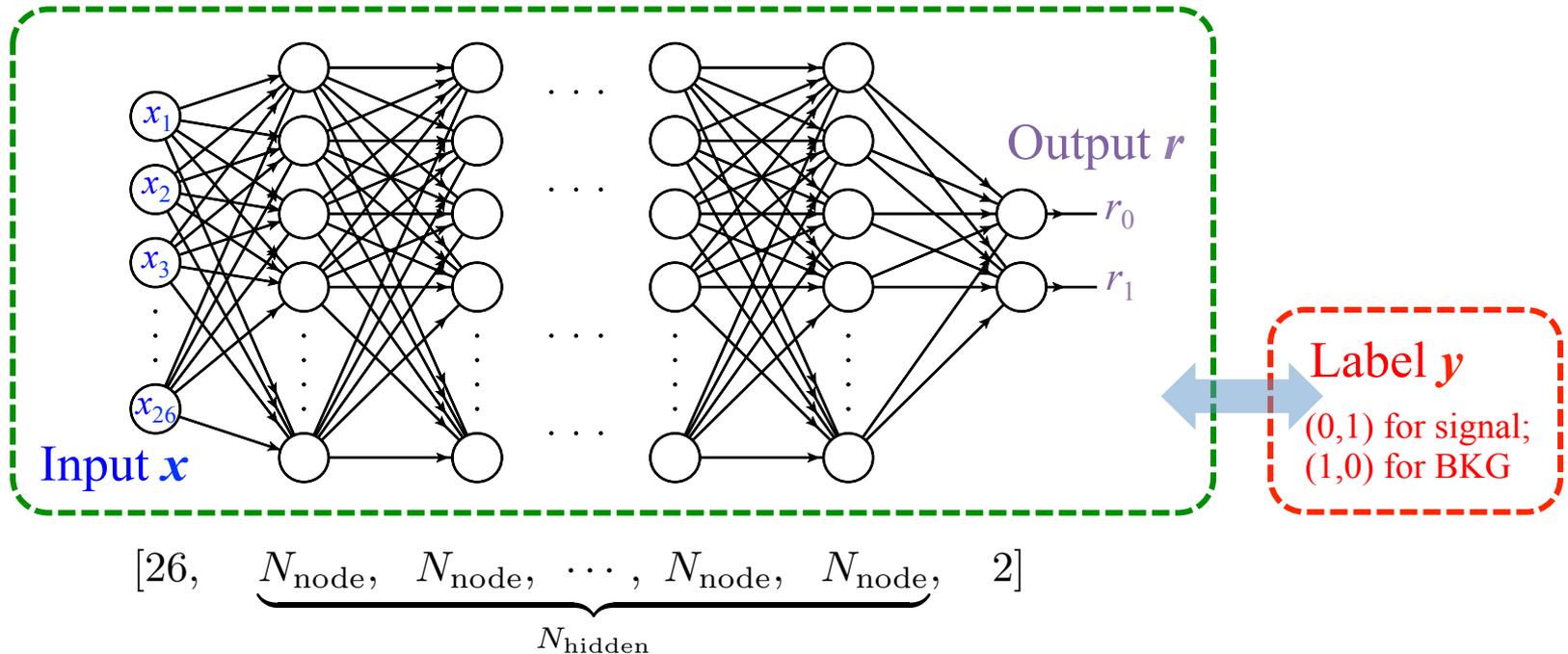


A biological neuron



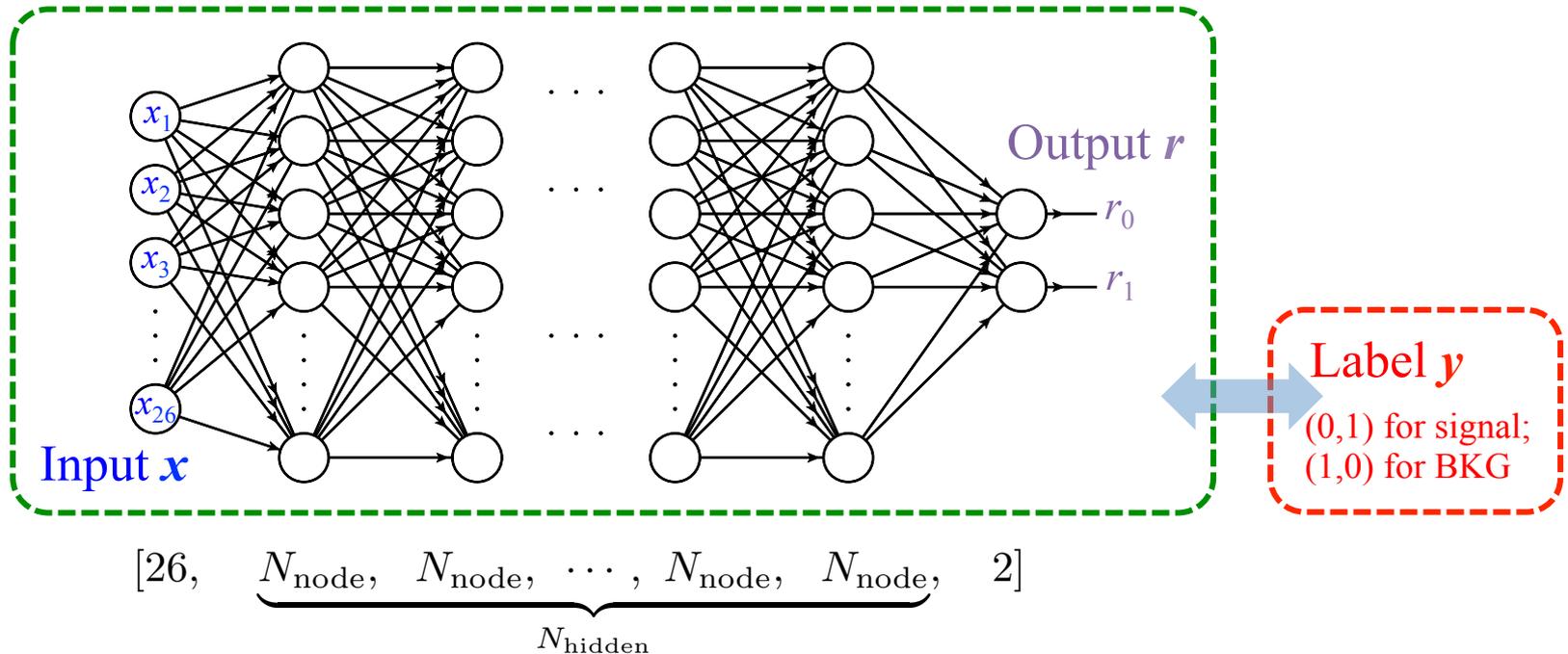
An artificial neuron

- Connecting numerous neurons to build a **neural network**:



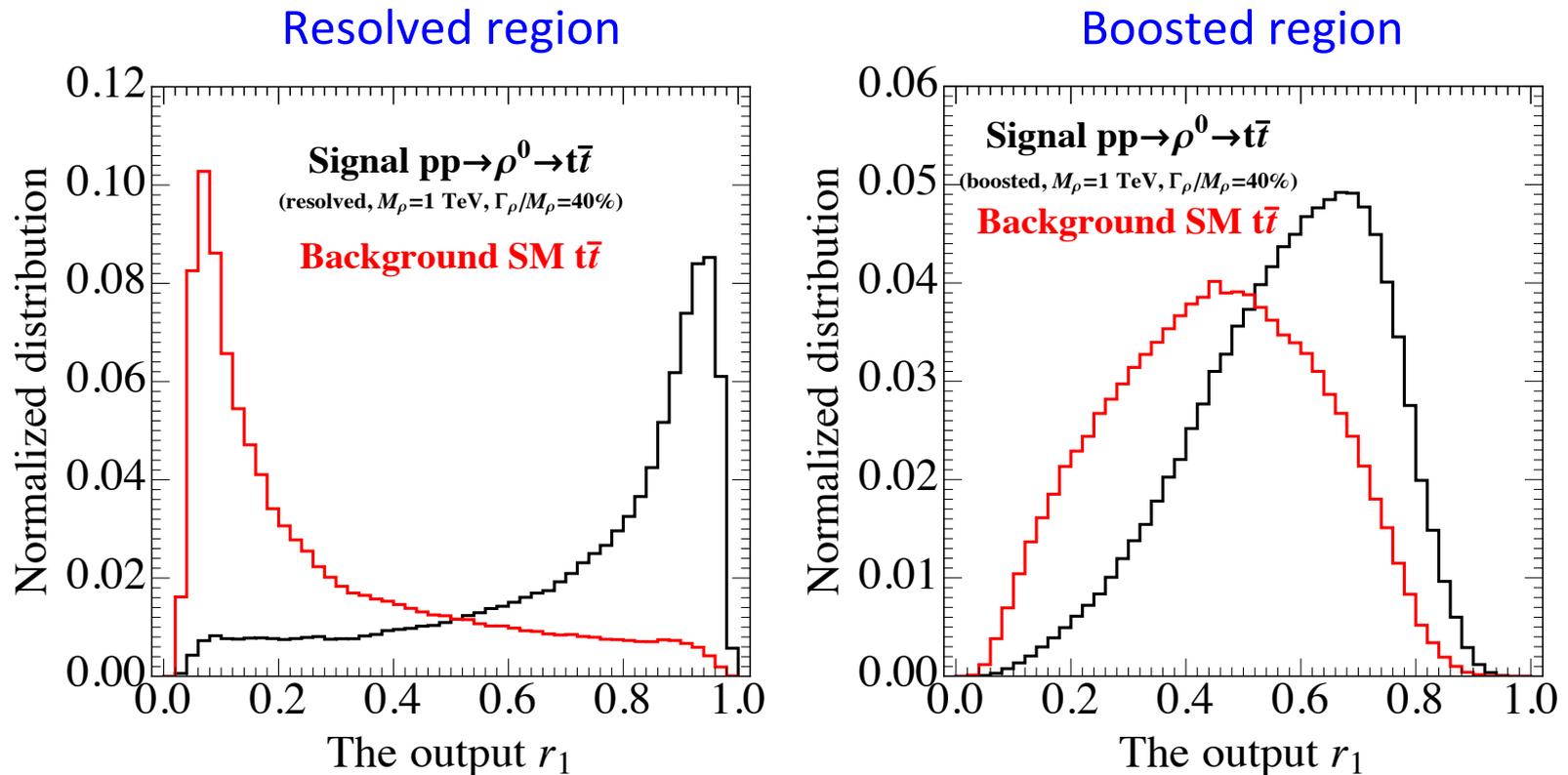
Machine learning on the DNN = Tune the w [weights] and b [biases], such that the output r and the label y are as close as possible.

- Connecting numerous neurons to build a **neural network**:



We tried $N_{\text{node}} = 200$ or 300 , $N_{\text{hidden}} = 4$ or 5 , and chose the best network configuration.

– Testing the trained network:



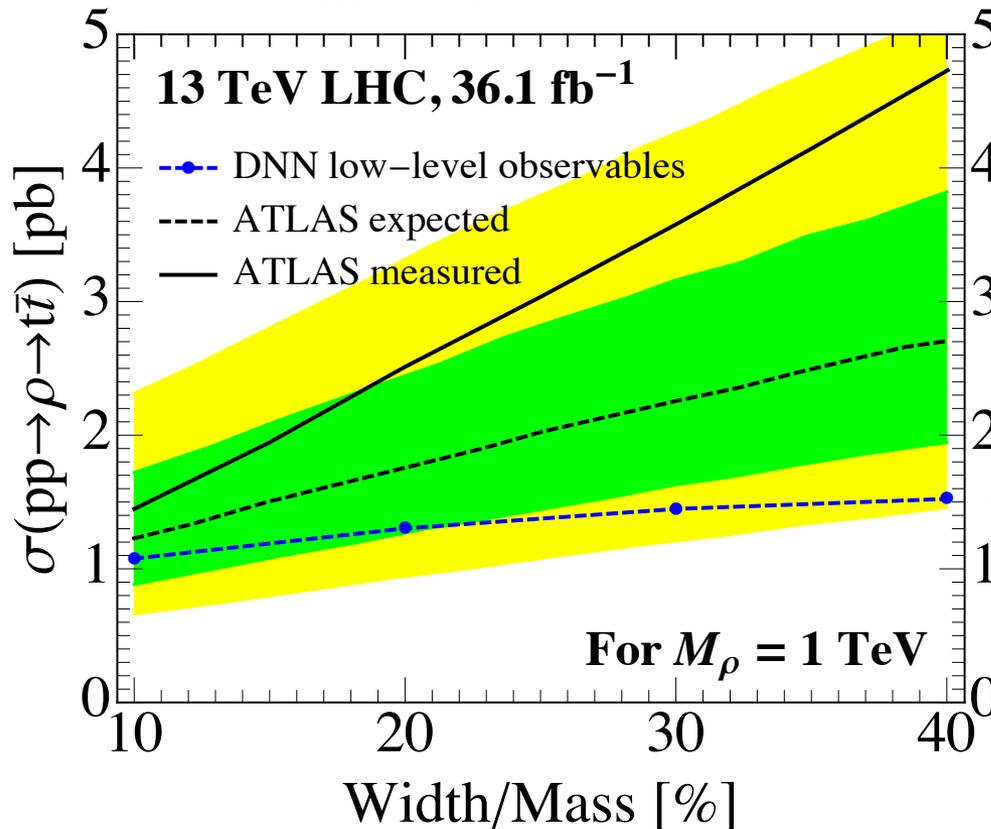
According to the given integrated luminosity, fit the neuron output to get the bounds for the signal strength!

➤ Interpret the DNN result as the cross section **upper limit** of the signal:

Combined resolved and boosted region; 12% systematic uncertainty for background is assumed.

The ATLAS result: 1804.10823

The DNN result: **this work**



The DNN results are much insensitive to the width!



- We have used the **DNN** to learn new physics signal from SM background, and get expected result. Is that enough?
- **NO! We have to figure out what it has learned.**

J. K. Rowling, *Harry Potter and The Chamber of Secrets*, 1999.

**Never trust anything that can think for itself,
if you can't see where it keeps its brain!**

➤ Figuring out what the machine has learned

The first approach we tried: to test if the DNN learned the specific observables --

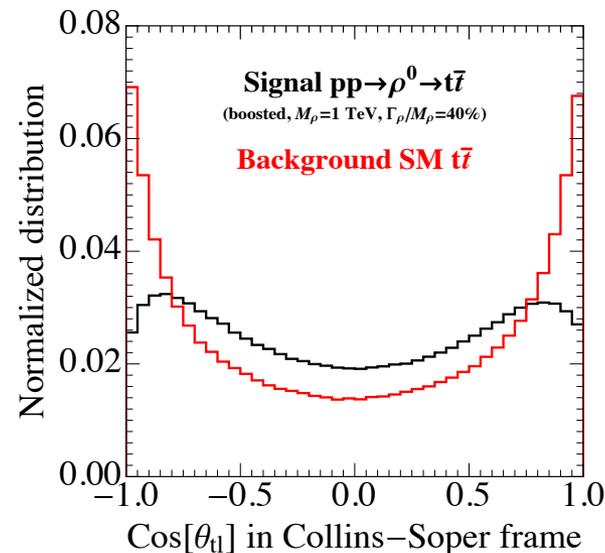
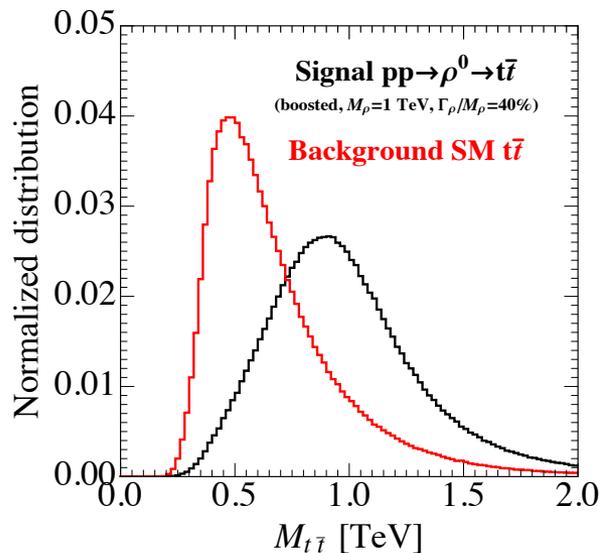
The 7 high-level observables

1	2	3	4	5	6	7
$M_{t\bar{t}}$	$\cos \theta_{t\bar{l}}^{\text{CS}}$	$\cos \theta_{t\bar{h}}^{\text{CS}}$	$\phi_{t\bar{l}}^{\text{CS}}$	$\phi_{t\bar{h}}^{\text{CS}}$	$\cos \theta_{t\bar{l}}^{\text{Mus.}}$	$\cos \theta_{t\bar{h}}^{\text{Mus.}}$

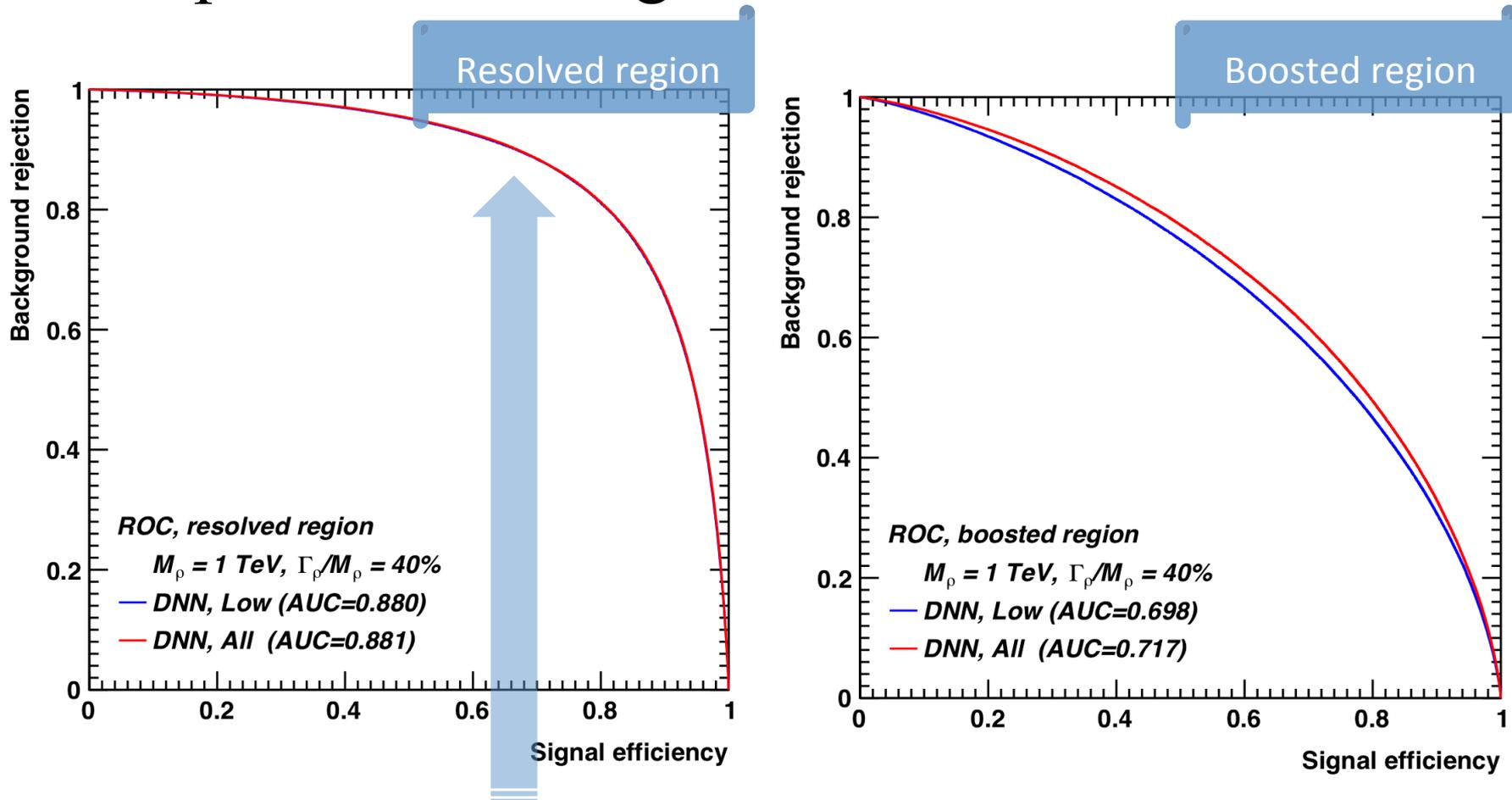


Invariant mass

Spin correlation in the $t\bar{t}$ rest frame



- We define all observables = low + high, and compare the training results:



DNN can learn the high-level observables!

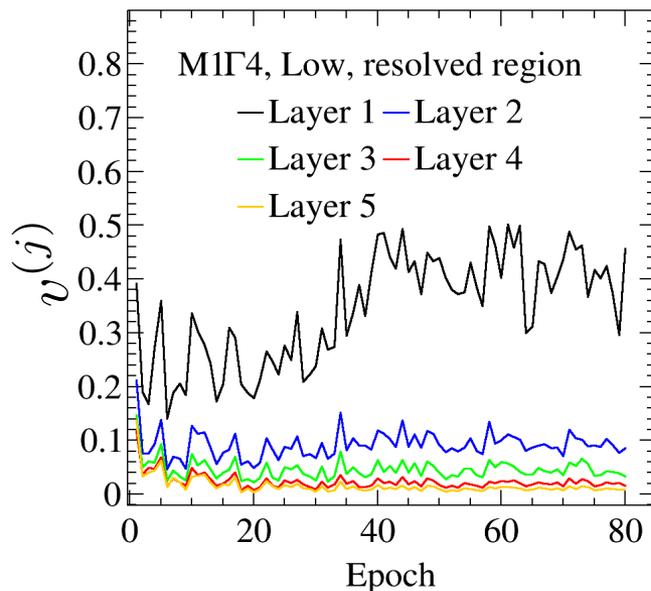
➤ Figuring out what the machine has learned

The second approach we tried: **disassemble** the machine

We define the **learning speed** of the j -th hidden layer as

$$v^{(j)} = \left| \frac{\partial \mathcal{L}_{\text{loss}}(w, b)}{\partial \vec{b}^{(j)}} \right|,$$

And what we found is:



The first hidden layer always has the largest learning speed!

➤ Figuring out what the machine has learned

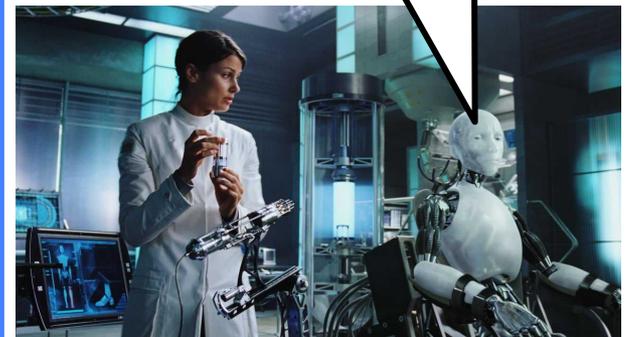
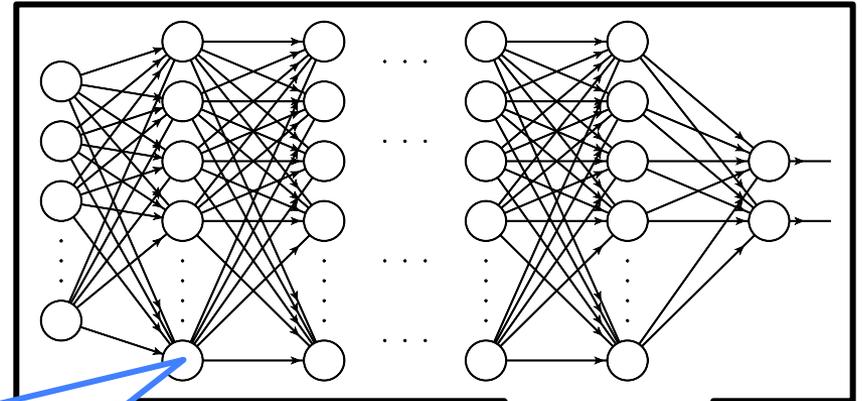
The second approach we tried: **disassemble** the machine

A weight W_m assigned for each input observable:

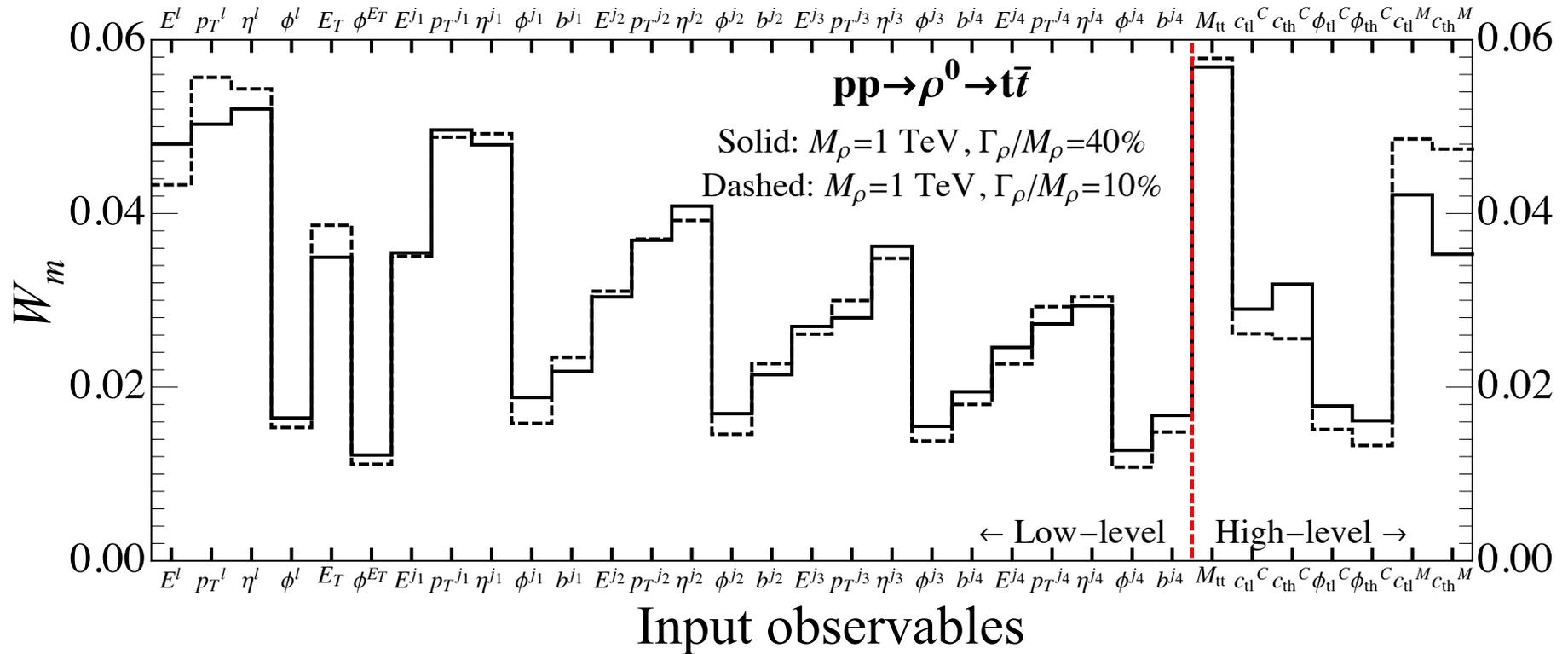
If the first hidden layer has 200 neurons, the 1st weights $w_{mn}^{(1)}$ form a 26×200 matrix. Define

$$W_m \propto \sqrt{\sum_{n=1}^{200} \left(w_{mn}^{(1)}\right)^2},$$

Then for each input observable we have a weight.



– Disassembling the machine



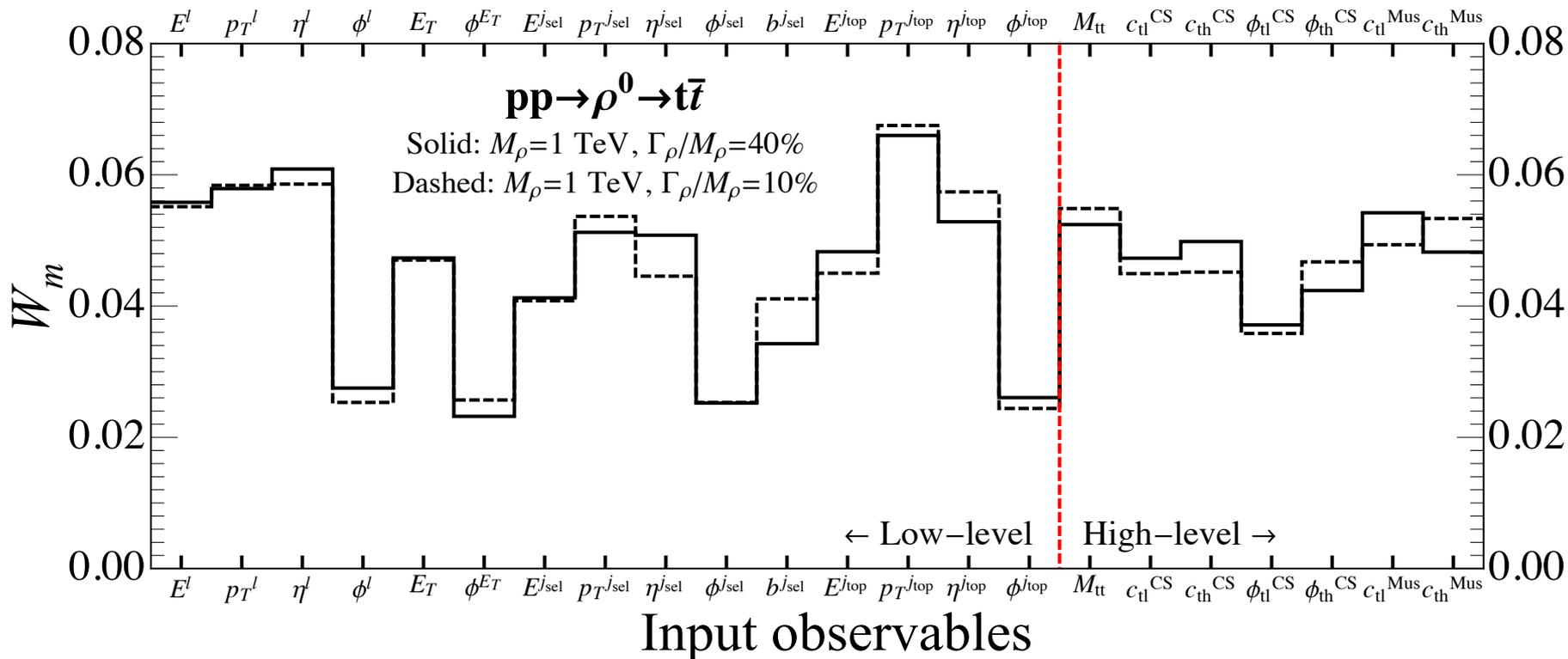
Low-level

1	2	3	4	5	6	7	8	9	10	11	12	13
E^ℓ	p_T^ℓ	η^ℓ	ϕ^ℓ	\cancel{E}_T	$\phi^{\cancel{E}_T}$	E^{j1}	p_T^{j1}	η^{j1}	ϕ^{j1}	b^{j1}	E^{j2}	p_T^{j2}
14	15	16	17	18	19	20	21	22	23	24	25	26
η^{j2}	ϕ^{j2}	b^{j2}	E^{j3}	p_T^{j3}	η^{j3}	ϕ^{j3}	b^{j3}	E^{j4}	p_T^{j4}	η^{j4}	ϕ^{j4}	b^{j4}

High-level

1	2	3	4	5	6	7
$M_{t\bar{t}}$	$\cos \theta_{t\bar{t}}^{\text{CS}}$	$\cos \theta_{t\bar{t}}^{\text{CS}}$	$\phi_{t\bar{t}}^{\text{CS}}$	$\phi_{t\bar{t}}^{\text{CS}}$	$\cos \theta_{t\bar{t}}^{\text{Mus.}}$	$\cos \theta_{t\bar{t}}^{\text{Mus.}}$

– Disassembling the machine



Low-level

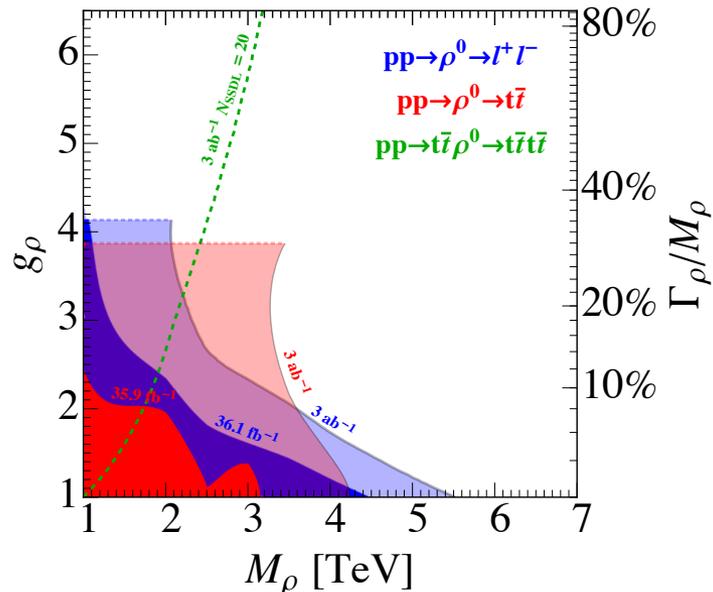
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
E^ℓ	p_T^ℓ	η^ℓ	ϕ^ℓ	E_T	ϕ^{E_T}	$E^{j_{sel}}$	$p_T^{j_{sel}}$	$\eta^{j_{sel}}$	$\phi^{j_{sel}}$	$b^{j_{sel}}$	$E^{j_{top}}$	$p_T^{j_{top}}$	$\eta^{j_{top}}$	$\phi^{j_{top}}$

High-level

1	2	3	4	5	6	7
$M_{t\bar{t}}$	$\cos \theta_{tl}^{CS}$	$\cos \theta_{th}^{CS}$	ϕ_{tl}^{CS}	ϕ_{th}^{CS}	$\cos \theta_{tl}^{Mus.}$	$\cos \theta_{th}^{Mus.}$

➤ Conclusion

1. The composite vector ρ resonances may be hidden in their large width and the dominant tb , tt and bb decay channels;



2. Deep learning can help to reveal such a broad tt resonance at the LHC.



Thank you!

– The CCWZ construction: $\underbrace{\{T^{a_L}, T^{a_R}, T^i\}}_{SO(5)} \rightarrow \underbrace{\{T^{a_L}, T^{a_R}\}}_{SO(4) \cong SU(2)_L \times SU(2)_R}$

Pseudo NGBs h : forming the Goldstone matrix

$$U[\vec{h}] = \exp \left\{ i \frac{\sqrt{2}}{f} h^i T^i \right\} \quad U[\vec{h}] \rightarrow \mathcal{G}U[\vec{h}]\mathcal{H}^{-1}[\vec{h}; \mathcal{G}]$$

\mathcal{G} : group element of SO(5)
 \mathcal{H} : group element of SO(4)

f : SO(5)/SO(4) scale; T^i : the 4 broken generators

Elementary particles: embedded in SO(5) representation

$$t_L, b_L \rightarrow F_L; \quad F_L \rightarrow \mathcal{G}_{F_L} F_L; \quad F_R \rightarrow \mathcal{G}_{F_R} F_R;$$

$$t_R \rightarrow F_R.$$

$F_{L,R}$: some multiplet of SO(5); **model dependent**

The **composite resonances**: fulfill SO(4) representation

$$\rho_\mu = \rho_\mu^{a_L} T^{a_L} + \rho_\mu^{a_R} T^{a_R}; \quad \rho_\mu \rightarrow \mathcal{H}(\rho_\mu + i\partial_\mu)\mathcal{H}^{-1};$$

$$\Psi. \quad \Psi \rightarrow \mathcal{H}_{\mathbf{r}_\Psi} \Psi$$

– The CCWZ construction: operators

Pure **bosonic** interactions: constructed by d and e symbols

$$U^\dagger (g_2 W_\mu^{a_L} T^{a_L} + g_1 B_\mu T^{3_R} + i\partial_\mu) U = d_\mu^i T^i + e_\mu^{a_L} T^{a_L} + e_\mu^{a_R} T^{a_R},$$

$$d_\mu \rightarrow \mathcal{H} d_\mu \mathcal{H}^{-1}, \quad e_\mu \rightarrow \mathcal{H} (e_\mu + i\partial_\mu) \mathcal{H}^{-1}$$

$$d_\mu^i = -\frac{\sqrt{2}}{f} D_\mu h_i + \dots,$$

$$e_\mu^{a_L} = g_2 W_\mu^{a_L} - \frac{i}{f^2} H^\dagger \frac{\sigma^{a_L}}{2} \overleftrightarrow{D}_\mu H + \dots,$$

$$e_\mu^{3_R} = g_1 B_\mu - \frac{i}{2f^2} H^\dagger \overleftrightarrow{D}_\mu H + \dots$$

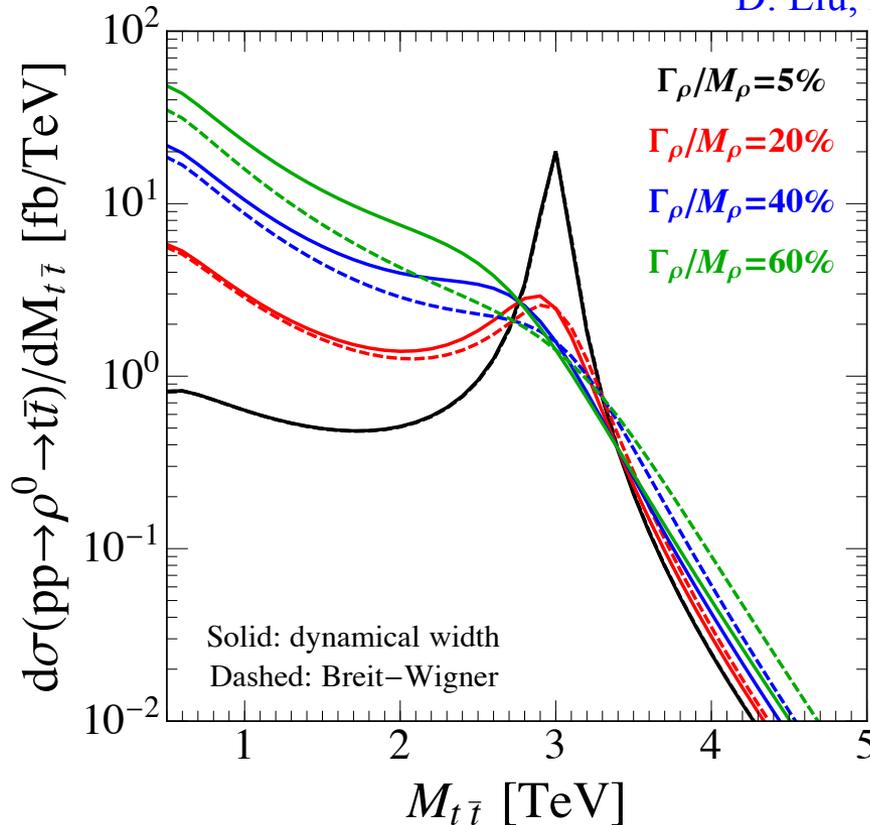
$$g_\rho \sim \frac{4\pi}{\sqrt{N}}$$

$$\frac{f^2}{4} d_\mu^i d^{i\mu} \approx \left(1 - \frac{2|H|^2}{3f^2}\right) D_\mu H^\dagger D^\mu H + \frac{1}{6f^2} (\partial_\mu |H|^2)^2,$$

$$\frac{M_\rho^2}{2g_\rho^2} (g_\rho \rho_\mu^{a_L} - e_\mu^{a_L})^2 \approx \frac{M_\rho^2}{2g_\rho^2} \left(g_\rho \rho_\mu^{a_L} - g_2 W_\mu^{a_L} + \frac{i}{f^2} H^\dagger \frac{\sigma^{a_L}}{2} \overleftrightarrow{D}_\mu H \right)^2$$

➤ The invariant mass of a resonance

D. Liu, L.-T. Wang and K.-P. Xie, arXiv:1901.01674



$$\frac{1}{(\hat{s} - M_\rho^2)^2 + M_\rho^2 \Gamma_\rho^2}$$

Breit-Wigner

v.s.

$$\frac{1}{(\hat{s} - M_\rho^2)^2 + \hat{s}^2 \Gamma_\rho^2 / M_\rho^2}$$

dynamical width

- Breit-Wigner distribution is commonly used, but a more suitable treatment is the dynamical width approach!

➤ The technical details of DNN

The configurations we tried

N_{hidden}	N_{node}	Learning rate (L_r)	Dropout rate (D_r)	Batch size (B_s)
4, 5	200, 300	0.001, 0.003	0.1, 0.2, 0.3	$10^3, 10^4$

Table 1: The configurations we have tried when finding the best model. For each signal model we try $2 \times 2 \times 3 \times 2 \times 2 = 48$ different configurations, and choose the one with best performance.

The best networks we chose

Signal model	Kinematic region	$N_{\text{hidden}}, N_{\text{node}}, L_r, D_r, B_s, N_{\text{epochs}}$	Accuracy reach
M1 Γ 1	resolved	5, 200, 0.001, 0.2, 10^3 , 150	85.2%
	boosted	5, 200, 0.001, 0.2, 10^4 , 55	67.9%
M1 Γ 2	resolved	4, 300, 0.003, 0.2, 10^3 , 35	83.2%
	boosted	5, 200, 0.001, 0.2, 10^4 , 45	65.8%
M1 Γ 3	resolved	4, 300, 0.001, 0.2, 10^3 , 30	81.6%
	boosted	4, 300, 0.003, 0.2, 10^4 , 30	65.1%
M1 Γ 4	resolved	5, 200, 0.001, 0.2, 10^3 , 80	80.8%
	boosted	4, 300, 0.001, 0.2, 10^4 , 20	64.3%

Table 1: The best networks for $M_\rho = 1$ TeV. N_{epochs} is the number of epochs when we cut the training; while “accuracy reach” is the accuracy for the test data.

➤ One slide for the 5 TeV case

The ATLAS result: 1804.10823

The **DNN** results: **this work**

