

Supersymmetric Super-GUT Models

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Physics is About Correlations

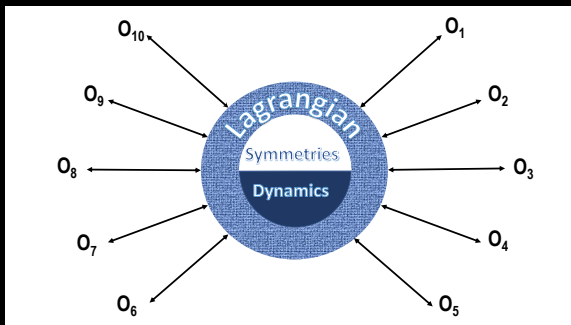
► Science explains correlation

- Naturalness: correlation between weak scale and Λ

Theory does not explain correlation, counter terms

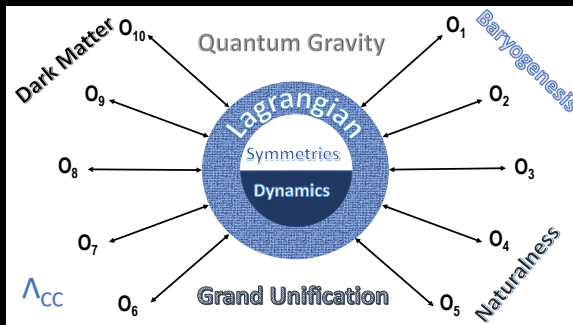
Symmetries like (SUSY) explain correlation

Dynamics relaxion field explain correlation



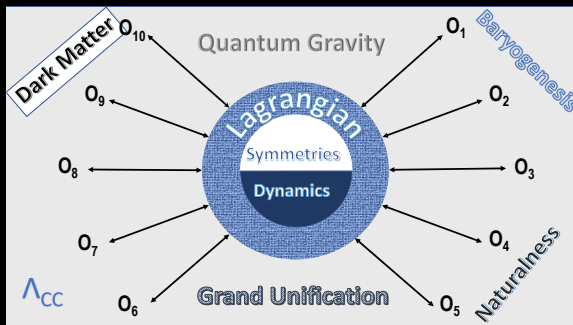
Physics is About Correlations

- ▶ Science explains correlation
- ▶ Many correlations unknown



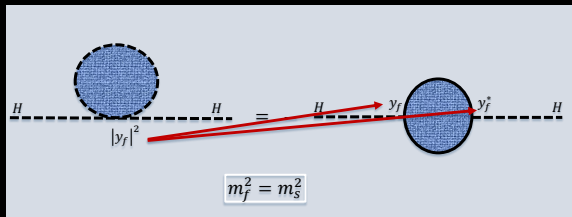
Physics is About Correlations

- ▶ Science explains correlation
- ▶ Many correlations unknown
- ▶ Good BSM explains more than one observable



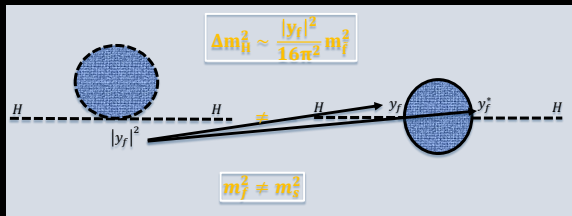
Three Triumphs of SUSY: Naturalness

- ▶ SUSY enforces relationships among parameters



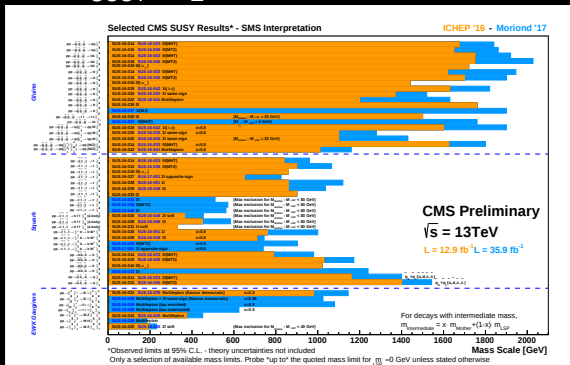
Three Triumphs of SUSY: Naturalness

- ▶ SUSY enforces relationships among parameters
- ▶ Experiment tells us SUSY must be broken
 - If breaking too large $\rightarrow$ unnatural



Three Triumphs of SUSY: Naturalness

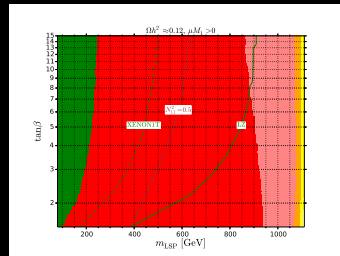
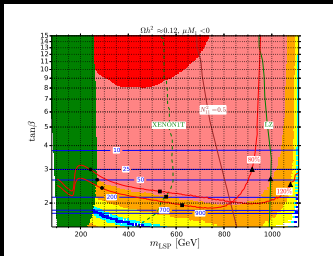
- ▶ SUSY enforces relationships among parameters
- ▶ Experiment tells us SUSY must be broken
- ▶ Not perfect but not so bad?
 - $\Delta_{BG} \sim M_{SUSY}^2 / m_Z^2$



Three Triumphs of SUSY: Dark Matter

- ▶ SUSY has many dark matter candidates
 - Some are ruled out

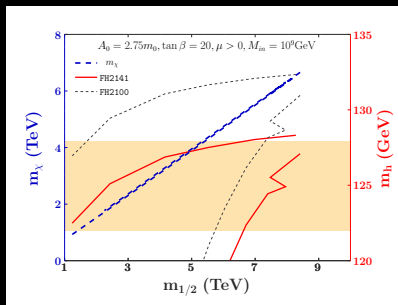
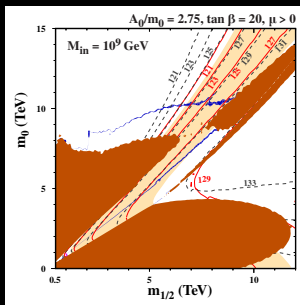
Red: LUX(SI), Green: LUX(SD), Orange: (XENON1T), Yellow: (LZ)



Badziak, Olechowski, Szczerbiak

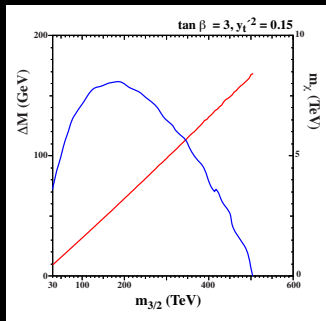
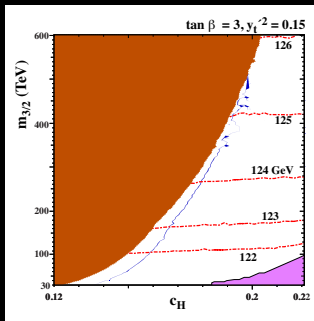
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- ▶ Stop/Gluino coannihilation still viable



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Three Triumphs of SUSY: Grand Unification

- ▶ Gauge couplings unify well in SUSY
- ▶ Quality of unification depends on μ, m_i

$$g_i^{-2}(m_Z) = g_5^{-2}(M_{GUT}) + \frac{1}{8\pi^2} \left(\beta_{SM_i} \ln \left(\frac{m_Z}{M_{GUT}} \right) + \frac{1}{3} (N_5 + 3N_{10}) \ln \left(\frac{M_{GUT}}{M_{SUSY}} \right) \right. \\ \left. + \beta_{\mu_i} \ln \left(\frac{M_{GUT}}{\mu} \right) + \beta_{m_i} \ln \left(\frac{M_{GUT}}{m_i} \right) \right)$$

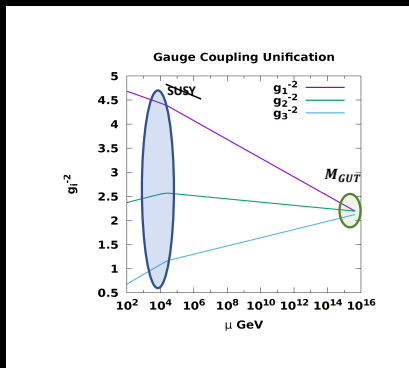
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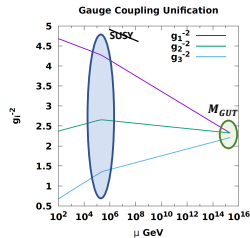
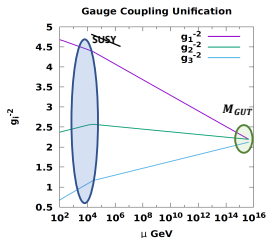
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- CMSSM with $m_0 = 20$ TeV



Three Triumphs of SUSY: Grand Unification

- ▶ Gauge couplings unify well in SUSY
- ▶ Quality of unification depends on μ, m_i
 - CMSSM with $m_0 = 20$ TeV vs $m_0 = 200$ TeV



Unification, Thresholds, and Low-Scale Observables

► Minimal Supersymmetric SU(5)

$$\Psi = \mathbf{10} \supset Q_L, \bar{U}, \bar{E} \quad \bar{\Phi} = \mathbf{5} \supset L, \bar{D} \quad (\text{and } \mathbf{1} \supset N)$$

$$\begin{aligned} W_5 = & \mu_\Sigma \text{Tr} \Sigma^2 + \frac{1}{6} \lambda' \text{Tr} \Sigma^3 + \mu_H \bar{H} H + \lambda \bar{H} \Sigma H \\ & + (h_{10})_{ij} \epsilon_{\alpha\beta\gamma\delta\zeta} \psi_i^{\alpha\beta} \psi_j^{\gamma\delta} H^\zeta + (h_{\bar{5}})_{ij} \psi_i^{\alpha\beta} \phi_{j\alpha} \bar{H}_\beta, \\ & \left[+ (h_1)_{ij} \bar{H}^\alpha \phi_{i\alpha} N_j + \frac{1}{2} M_{ij} N_i N_j \right] \end{aligned}$$

Unification, Thresholds, and Low-Scale Observables

- ▶ Minimal Supersymmetric SU(5)
- ▶ Threshold corrections $\rightarrow$ unification of couplings

$$\frac{3}{g_2^2(M_{GUT})} - \frac{2}{g_3^2(M_{GUT})} - \frac{1}{g_1^2(M_{GUT})} = -\frac{3}{10\pi^2} \ln\left(\frac{M_{GUT}}{M_{H_C}}\right)$$
$$\frac{5}{g_1^2(M_{GUT})} - \frac{3}{g_2^2(M_{GUT})} - \frac{2}{g_3^2(M_{GUT})} = -\frac{9}{2\pi^2} \ln\left(\frac{M_{GUT}}{(M_X^2 M_\Sigma)^{\frac{1}{3}}}\right)$$

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- ▶ Minimal Supersymmetric SU(5)
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 - SUSY breaking determines/constraints $M_{H_C}, M_\chi, M_\Sigma$

$$\frac{3}{\bar{g}_2^2(M_{GUT})} + \Delta_{SUSY_2} - \frac{2}{g_3^2(M_{GUT})} - \frac{1}{g_1^2(M_{GUT})} = -\frac{3}{10\pi^2} \ln\left(\frac{M_{GUT}}{M_{H_C}}\right)$$

$$\frac{5}{g_1^2(M_{GUT})} - \frac{3}{g_2^2(M_{GUT})} - \frac{2}{g_3^2(M_{GUT})} = -\frac{9}{2\pi^2} \ln\left(\frac{M_{GUT}}{(M_\chi^2 M_\Sigma)^{\frac{1}{3}}}\right)$$

Unification, Thresholds, and Low-Scale Observables

- ▶ Minimal Supersymmetric SU(5)
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 - SUSY breaking determines/constraints M_{H_C}, M_X, M_Σ
- ▶ Color Higgs $\rightarrow B, L$ violating interactions
 - This leads to nucleon decay

$$\mathcal{L}|_{\text{eff.}}^{\Delta B=1} = C_{5L}^{ijkl} \int d^2\theta \frac{1}{2} (Q_i Q_j)(Q_k L_l) + C_{5R}^{ijkl} \int d^2\theta \bar{U}_i \bar{E}_j \bar{U}_k \bar{D}_l + \text{h.c.}$$

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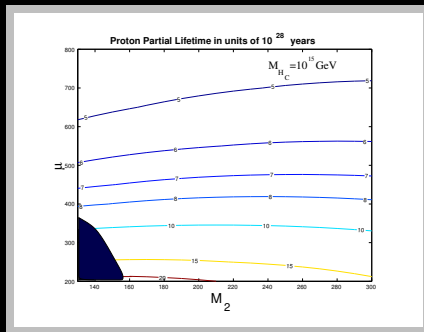
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- ▶ Proton decay determined M_{H_C} and so constrains SUSY

$$C_{5L}^{ijkl} = -\frac{1}{M_{H_C}} f_i^u e^{i\varphi_{u_i}} \delta^{ij} V_{kl}^* f_l^d \quad C_{5R}^{ijkl} = -\frac{1}{M_{H_C}} f_i^u V_{ij} V_{kl}^* f_l^d e^{-i\varphi_{u_k}}$$

Gauge Coupling Unification: Proton Decay

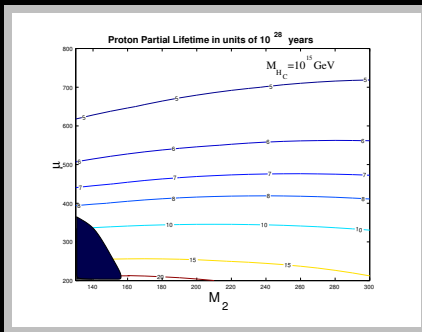
- ▶ Murayama and Pierce claim minimal SU(5) excluded
 - Non-minimal models needed (Pierce Murayama)



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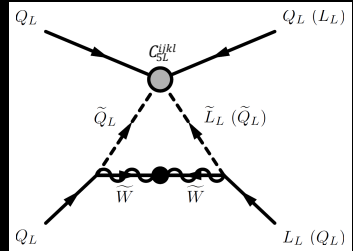
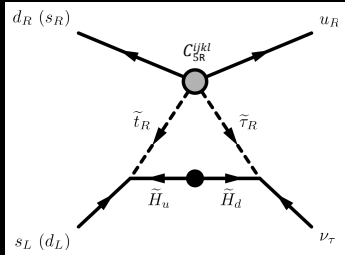
$$m_{\tilde{t}_3} = 1\text{TeV} \quad m_{\tilde{t}_{2,3}} = 10\text{TeV} \quad \mu \in (100, 1000)\text{GeV} \quad M_2 \in (100, 400)\text{GeV}$$



Details of Proton Decay Amplitude

► Amplitudes for proton decay

$$\begin{aligned}\mathcal{A}(p \rightarrow K^+ \bar{\nu}_i) = & C_{RL}(usd\nu_i) \langle K^+ | (us)_R d_L | p \rangle \\ & + C_{RL}(uds\nu_i) \langle K^+ | (ud)_R s_L | p \rangle \\ & + C_{LL}(usd\nu_i) \langle K^+ | (us)_L d_L | p \rangle \\ & + C_{LL}(uds\nu_i) \langle K^+ | (ud)_L s_L | p \rangle\end{aligned}$$



► Approximate low-scale WC of proton decay

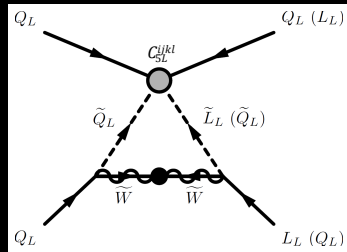
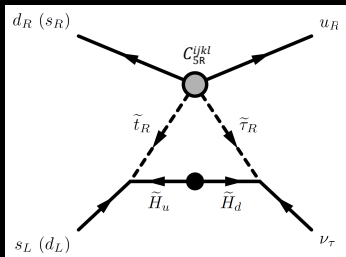
$$C_{LL} \simeq \frac{2\alpha_2^2}{\sin 2\beta} \frac{m_t m_b M_2}{m_W^2 M_{H_C} M_{\text{SUSY}}^2} V_{ub}^* V_{td} V_{ts} e^{i\phi_3} \left(1 + e^{i(\phi_2 - \phi_3)} \frac{m_c V_{cd} V_{cs}}{m_t V_{td} V_{ts}} \right)$$

$$C_{RL} \simeq -\frac{\alpha_2^2}{\sin^2 2\beta} \frac{m_t^2 m_d m_\tau \mu}{m_W^4 M_{H_C} M_{\text{SUSY}}^2} V_{tb}^* V_{ud} V_{ts} e^{-i(\phi_2 + \phi_3)}$$

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 & + C_{RL}(uds\nu_i) \langle K^+ | (ud)_R s_L | p \rangle \\
 & + C_{LL}(usd\nu_i) \langle K^+ | (us)_L d_L | p \rangle \\
 & + C_{LL}(uds\nu_i) \langle K^+ | (ud)_L s_L | p \rangle
 \end{aligned}$$



- Respective $\tau(p \rightarrow K\nu)$ for $\phi_{2,3} = 0$
- $\tau(p \rightarrow K\nu) > 6.6 \times 10^{33} \text{ yr}$

$$\Gamma_{\tilde{W}} \simeq 3.3 \times 10^{31} \text{ yr} \left(\frac{M_{HC}}{7 \times 10^{16} \text{ GeV}} \right)^2 \left(\frac{M_{SUSY}}{11 \text{ TeV}} \right)^4 \left(\frac{3.5 \text{ TeV}}{M_2} \right)^2$$

$$\Gamma_{\tilde{h}} \simeq 2.8 \times 10^{31} \text{ yr} \left(\frac{M_{HC}}{7 \times 10^{16} \text{ GeV}} \right)^2 \left(\frac{M_{SUSY}}{11 \text{ TeV}} \right)^4 \left(\frac{12 \text{ TeV}}{M_2} \right)^2$$

Proton Decay and Low-scale SUSY

- ▶ Large soft masses will help
- ▶ PGM/mini-split models give sufficient suppression
 - Strong Moduli Stabilization

$$\frac{\langle Z \rangle}{M_P} \ll 1 \quad \frac{F_Z}{M_P} \sim m_{3/2}$$

Proton Decay and Low-scale SUSY

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 - Z not a singlet suppressed in gauge kinetic function

$$h_{\alpha\beta} = \frac{Z^n}{M_P^n} \rightarrow m_{1/2} \sim \left(\frac{\langle Z \rangle}{M_P} \right)^{n-1} m_{3/2} \ll m_{3/2}$$

Proton Decay and Low-scale SUSY

- ▶ Large soft masses will help
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 - Z not a singlet suppressed in gauge kinetic function
 - Gauginos are generated by anomalies

$$M_a = \frac{b_a g_a^2}{16\pi^2} m_{3/2} \quad b_a = (-33/5, -1, 3)$$

Proton Decay and Low-scale SUSY

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 - A -terms are also suppressed

$$K = \frac{Z^\dagger Z}{M_P^2} H_u^\dagger H_u \quad \rightarrow \quad \frac{Z^\dagger}{M_P} \frac{F_Z}{M_P} H_u F_{H_u}^\dagger$$

Proton Decay and Low-scale SUSY

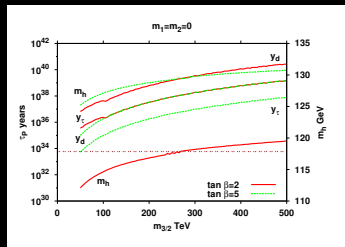
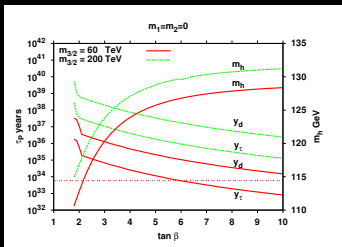
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 - Scalar masses the same as mSUGRA

$$m_0 = m_{3/2}$$

Proton Decay and Low-scale SUSY

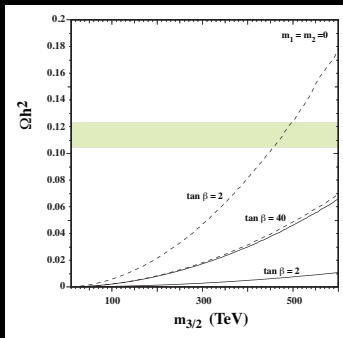
- ▶ Large soft masses will help
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$$m_{\tilde{t}} = m_{3/2} \quad m_i = \beta_i m_{3/2} \quad A_0 = 0 \quad (\mu \sim m_{\tilde{t}})$$



Proton Decay and Low-scale SUSY

- ▶ Large soft masses will help
- ▶ PGM/mini-split models give sufficient suppression
 - $m_{3/2} \lesssim 400$ TeV, DM not viable



Proton Decay and CMSSM

► What about CMSSM like models?

– M_{SUSY} is low

$$\Gamma_{\tilde{W}} \sim 10^{31} \text{ yr} \left(\frac{M_{H_C}}{7 \times 10^{16} \text{ GeV}} \right)^2 \left(\frac{M_{SUSY}}{11 \text{ TeV}} \right)^4 \left(\frac{3.5 \text{ TeV}}{M_2} \right)^2 \quad \Gamma_{\tilde{h}} \sim 10^{31} \text{ yr} \left(\frac{M_{H_C}}{7 \times 10^{16} \text{ GeV}} \right)^2 \left(\frac{M_{SUSY}}{11 \text{ TeV}} \right)^4 \left(\frac{12 \text{ TeV}}{\mu} \right)^2$$

► Contributions can add destructively

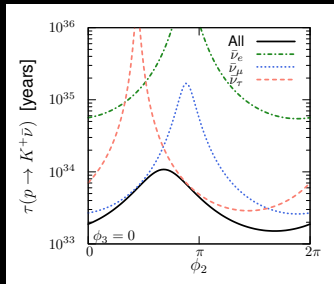
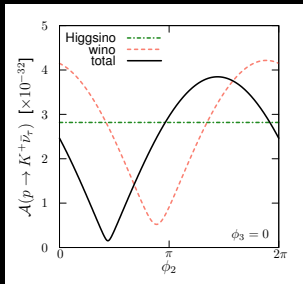
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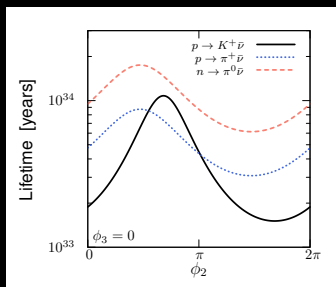
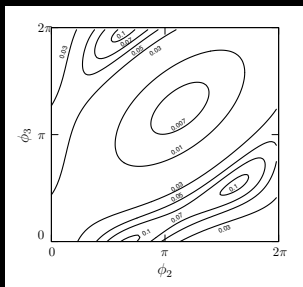
Phase Suppression of Proton Decay

- ▶ Significant suppression afforded by phases
 - Misalignment of decay to different generations limits suppression



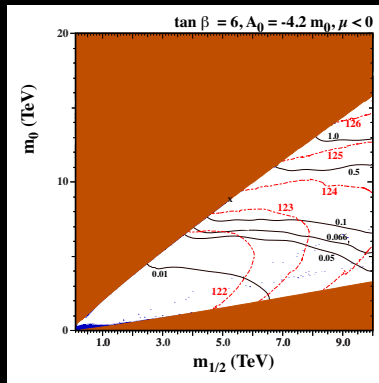
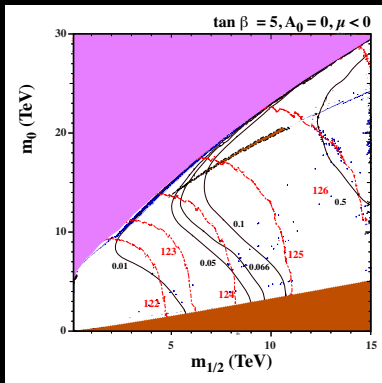
Phase Suppression of Proton Decay

- ▶ Significant suppression afforded by phases
 - Misalignment of decay to different generations limits suppression
- ▶ Suppression not so tuned in phase
- ▶ Other nucleon lifetimes also enhanced



CMSSM with Phase Suppressed Proton Decay

- ▶ Phase Suppression sufficient for viable dark matter



Super-GUT Models

- ▶ SUSY breaking mediated at some scale $M_{in} > M_{GUT}$
 - Parameters at M_{in} for CMSSM

m_0

$m_{1/2}$

$\tan \beta$

A_0

$\text{sgn}(\mu)$

Super-GUT Models

- ▶ SUSY breaking mediated at some scale $M_{in} > M_{GUT}$
 - Some matching conditions have consequences

$$B = B_H + \frac{3\lambda V\Delta}{\mu} + \frac{6\lambda}{\lambda'\mu} \left[(A_{\lambda'} - B_{\Sigma})(2B_{\Sigma} - A_{\lambda'} + \Delta) - m_{\Sigma}^2 \right] \quad \rightarrow \quad A_{\lambda'} \gtrsim 8m_{\Sigma}^2$$

$$\frac{3}{g_2^2(Q)} - \frac{2}{g_3^2(Q)} - \frac{1}{g_1^2(Q)} = -\frac{3}{10\pi^2} \ln \left(\frac{Q}{M_{H_C}} \right) \quad \rightarrow \quad M_{H_C} \sim 10^{15} \text{GeV}$$

$$\frac{5}{g_1^2(Q)} - \frac{3}{g_2^2(Q)} - \frac{2}{g_3^2(Q)} = -\frac{3}{2\pi^2} \ln \left(\frac{Q^3}{M_X^2 M_{\Sigma}} \right) \quad \& \quad M_{H_C} = \lambda \left(\frac{2}{\lambda' g_5^2} \right)^{\frac{1}{3}} \left(M_X^2 M_{\Sigma} \right)^{\frac{1}{3}}$$

$$\lambda \propto \lambda' \quad \& \quad \lambda' \sim 1 \quad \rightarrow \quad \textbf{Proton Decays too Quickly}$$

Super-GUT Models

- ▶ SUSY breaking mediated at some scale $M_{in} > M_{GUT}$
 - Some matching conditions have consequences
- ▶ Add higher dimensional operators

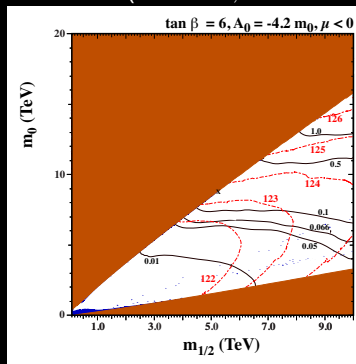
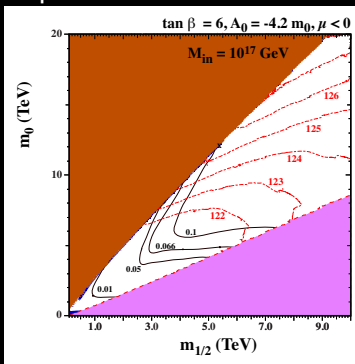
$$W_{\text{eff}}^{\Delta g} = \frac{c}{M_P} \text{Tr} [\Sigma \mathcal{W} \mathcal{W}]$$

- Alters matching condition $\rightarrow M_{H_C}$ Free

$$\frac{3}{g_2^2(Q)} - \frac{2}{g_3^2(Q)} - \frac{1}{g_1^2(Q)} = -\frac{3}{10\pi^2} \ln \left(\frac{Q}{M_{H_C}} \right) - \frac{96cV}{M_P}$$

Super-GUT Models

- ▶ SUSY breaking mediated at some scale $M_{in} > M_{GUT}$
 - Some matching conditions have consequences
- ▶ Add higher dimensional operators
- ▶ Super-GUT CMSSM versus CMSSM ($\lambda = 0.6, \lambda' = 10^{-4}$)



Minimal SU(5) + Right-Handed Neutrinos

- ▶ Neutrino seemingly benign interactions
 - Leptogenesis is viable

$$W_5 = (h_1)_{ij} \overline{H}^\alpha \Phi_{i\alpha} N_j + \frac{1}{2} M_{ij} N_i N_j$$

Minimal SU(5) + Right-Handed Neutrinos

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$$W_5 = (h_1)_{ij} \bar{H}^\alpha \Phi_{i\alpha} N_j + \frac{1}{2} M_{ij} N_i N_j$$

- ▶ Physical degrees of freedom in the Yukawa's
 - We will assume $M_R = \delta_{ij} M_{R_i}$

$$f_{ij}^u = f_i^u e^{i\varphi_{u_i}} \delta_{ij} \quad f_{ij}^d = f_i^d V_{ij}^* \quad f_{ij}^\nu = f_j^\nu e^{i\varphi_{d_i}} U_{ij}^* \quad (M_R)_{ij} = e^{i\varphi_{\nu_i}} W_{ik} (M_R^D)_k e^{2i\bar{\varphi}_{\nu_k}} W_{jk} e^{i\varphi_{\nu_j}}$$

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- ▶ PMNS has large CP violation and large flavor mixing

$$\sin^2 \theta_{12} = 0.297, \quad \sin^2 \theta_{23} = 0.425, \quad \sin^2 \theta_{31} = 0.0214, \quad \delta_{CP} = 1.38\pi$$

Kaon Mixing From Right-Handed Neutrinos

- ▶ Beta function of $\Phi_i, \overline{H}$ affected by h_1 (N_i GUT Yukawa)
 - Leading-log approximation for affected soft masses

$$(m_d^2)_{ij} \simeq -\frac{1}{8\pi^2} [f^\nu f^{\nu\dagger}]_{ij} (3m_0^2 + A_0^2) \ln \frac{M_*}{M_{GUT}}, \quad (i \neq j)$$

Kaon Mixing From Right-Handed Neutrinos

- ▶ Beta function of $\Phi_i, \bar{H}$ affected by h_1
- ▶ Mixing in down-squark soft masses $\rightarrow$ kaon mixing

$$\begin{aligned} \mathcal{H}_{\text{eff.}}^{\Delta S=2} \simeq & -\frac{\alpha_S^2}{36m_{\tilde{q}}^2} \left(\Delta_{12}^{(R)} \right)^2 F_1 \left(\frac{m_{\tilde{g}}^2}{m_{\tilde{q}}^2} \right) \bar{d}_R^\alpha \gamma_\mu s_R^\alpha \bar{d}_R^\beta \gamma^\mu s_R^\beta - \frac{\alpha_S^2}{3m_{\tilde{q}}^2} \Delta_{12}^{(L)} \Delta_{12}^{(R)} F_2 \left(\frac{m_{\tilde{g}}^2}{m_{\tilde{q}}^2} \right) \bar{d}_L^\alpha s_R^\alpha \bar{d}_R^\beta s_R^\beta \\ & - \frac{\alpha_S^2}{9m_{\tilde{q}}^2} \Delta_{12}^{(L)} \Delta_{12}^{(R)} F_3 \left(\frac{m_{\tilde{g}}^2}{m_{\tilde{q}}^2} \right) \bar{d}_L^\alpha s_R^\beta \bar{d}_R^\beta s_R^\alpha \\ (m_{\tilde{d}}^2)_{12} \simeq & -\frac{1}{8\pi^2} e^{i(\varphi_{d1} - \varphi_{d2})} U_{1k}(f_k^\nu)^2 U_{2k}^* (3m_0^2 + A_0^2) \ln \frac{M_{\text{in}}}{M_{\text{GUT}}} \end{aligned}$$

SUSY contributions

$$\begin{aligned} \Delta m_K^{\text{SUSY}} &= 2\text{Re} \left\langle \bar{K}^0 \right| \mathcal{H}_{\text{eff.}}^{\Delta S=2} \left| K^0 \right\rangle, \\ \epsilon_K^{\text{SUSY}} &= \frac{1}{\sqrt{2}\Delta m_K} \text{Im} \left\langle \bar{K}^0 \right| \mathcal{H}_{\text{eff.}}^{\Delta S=2} \left| K^0 \right\rangle \end{aligned}$$

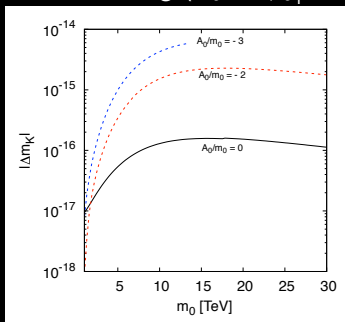
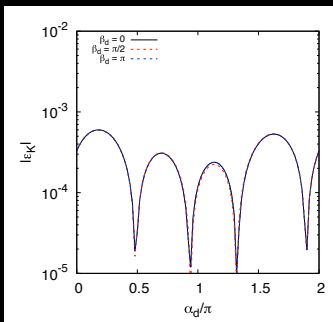
Hadron matrix elements:

SM op.: [FLAG average '16]

BSM ops.: [SWME collaboration '15]

Kaon Mixing From Right-Handed Neutrinos

- ▶ Beta function of $\Phi_i, \bar{H}$ affected by h_1
- ▶ Mixing in down-squark soft masses $\rightarrow$ kaon mixing
- ▶ Irreducible contributions to Kaon mixing ($\alpha_d = \phi_{d_1} - \phi_{d_2}$)



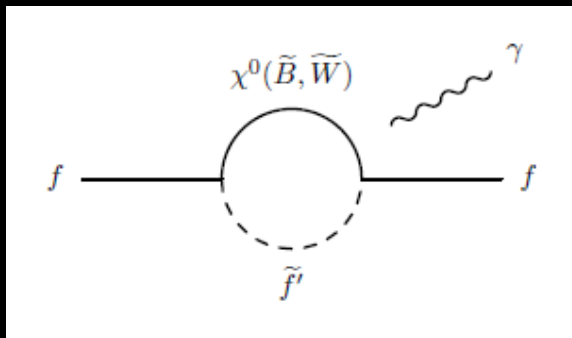
eEDM From Right-Handed Neutrinos

- ▶ Right-handed neutrino Yukawa's also affect leptons
 - Super-GUT RG running enhances FV+CP violation
 - Effect maximized for $Y_\nu \sim 1 \rightarrow M_{N_R} \sim 10^{15}$

$$(m_L^2)_{ij} \simeq -\frac{1}{8\pi^2} \sum_k \hat{f}_{ik}^\nu (\hat{f}^{\nu\dagger})_{kj} (3m_0^2 + A_0^2) \ln \frac{M_*}{(M_R^D)_k}, \quad (i \neq j)$$

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- ▶ Generated FV+CP violation lead to eEDM's



eEDM From Right-Handed Neutrinos

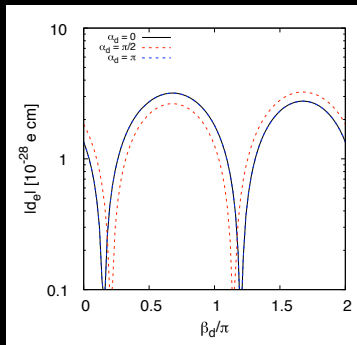
- ▶ Right-handed neutrino Yukawa's also affect leptons
- ▶ Generated FV+CP violation lead to eEDM's

$$\frac{d_e}{e} \sim \frac{g_Y^2}{32\pi^2} \frac{m_\tau}{m_l^2} \frac{\mu M_1}{m_l^2} \text{Im}[(\Delta_l^{(L)})_{13}(\Delta_l^{(R)})_{31}] f(x)$$

$$(\Delta_l^{(L)})_{ij} \equiv \frac{(m_L^2)_{ij}}{m_l^2}, \quad (\Delta_l^{(R)})_{ij} \equiv \frac{(m_e^2)_{ij}}{m_l^2}$$

eEDM From Right-Handed Neutrinos

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- ▶ Generated FV+CP violation lead to eEDM's
- ▶ Irreducible contribution to eEDM ($\beta_d = \phi_{d_1} - \phi_{d_3}$)



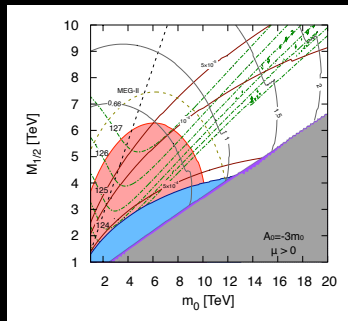
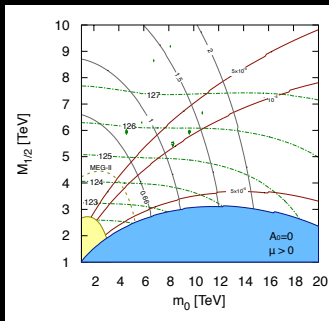
Consequences for Super-GUT Models

- ▶ Super-GUT CMSSM with right-handed neutrinos

$$m_0 \quad m_{1/2} \quad A_0 \quad \tan \beta \quad \text{sgn}(\mu) \quad M_{in} \quad M_R \quad \lambda \quad \lambda' \quad \phi_{u_i} \quad \phi_{d_i}$$

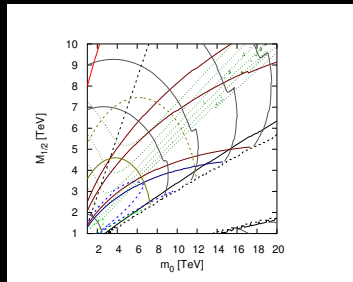
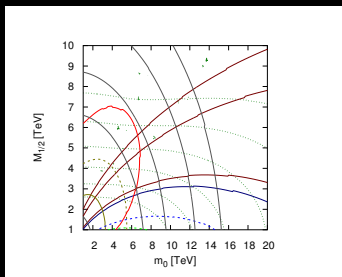
Consequences for Super-GUT Models

- ▶ Super-GUT CMSSM with right-handed neutrinos
 - yellow: $\mu \rightarrow e\gamma$ Cyan: $e\text{EDM}(9.3 \times 10^{-29})$ Red: ε_K



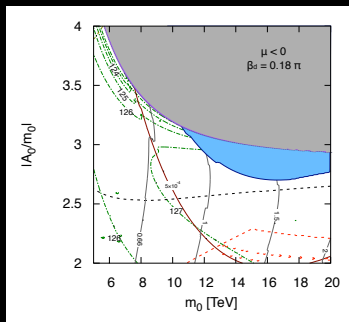
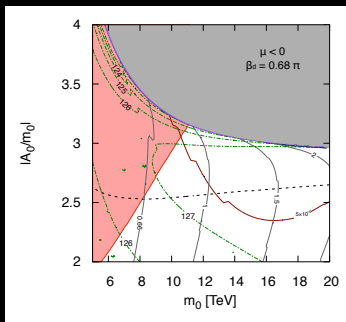
Consequences for Super-GUT Models

- ▶ Super-GUT CMSSM with right-handed neutrinos
 - yellow: $\mu \rightarrow e\gamma$ Cyan: $e\text{EDM}(1.1 \times 10^{-29})$ Red: ε_K



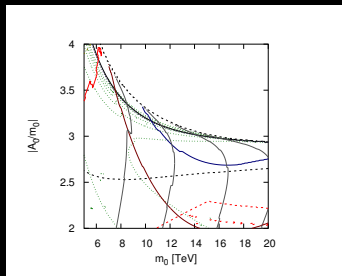
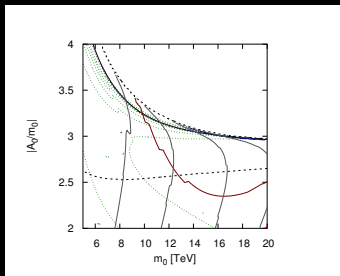
Consequences for Super-GUT Models

- ▶ Super-GUT CMSSM with right-handed neutrinos
- ▶ Constraints depend on β_d
 - Cyan: $e\text{EDM}(9.3 \times 10^{-29})$
 - Red: ε_K



Consequences for Super-GUT Models

- ▶ Super-GUT CMSSM with right-handed neutrinos
- ▶ Constraints depend on β_d
 - Cyan: $eEDM(1.1 \times 10^{-29})$
 - Red: ε_K



Super-GUT PGM

- ▶ CMSSM required Planck suppressed operators
 - M_{H_C} was required to be too small

$$\frac{3}{g_2^2(Q)} - \frac{2}{g_3^2(Q)} - \frac{1}{g_1^2(Q)} = -\frac{3}{10\pi^2} \ln\left(\frac{Q}{M_{H_C}}\right) - \frac{96cV}{M_P}$$

Super-GUT PGM

- ▶ CMSSM required Planck suppressed operators
- ▶ PGM proton decay is suppressed by soft masses
 - M_{H_C} is relatively unconstrained
 - No Planck Suppressed operators needed

$$\Gamma_{\tilde{W}} \sim 10^{31} \text{ yr} \left(\frac{M_{H_C}}{7 \times 10^{16} \text{ GeV}} \right)^2 \left(\frac{M_{SUSY}}{11 \text{ TeV}} \right)^4 \left(\frac{3.5 \text{ TeV}}{M_2} \right)^2 \quad \Gamma_{\tilde{h}} \sim 10^{31} \text{ yr} \left(\frac{M_{H_C}}{7 \times 10^{16} \text{ GeV}} \right)^2 \left(\frac{M_{SUSY}}{11 \text{ TeV}} \right)^4 \left(\frac{12 \text{ TeV}}{\mu} \right)^2$$

Super-GUT PGM

- ▶ CMSSM required Planck suppressed operators
- ▶ PGM proton decay is suppressed by soft masses
- ▶ PGM restricts $\tan \beta$
 - soft masses larger gaugino small
 - Stop masses driven lighter
 - More difficult to drive Higgs mass negative

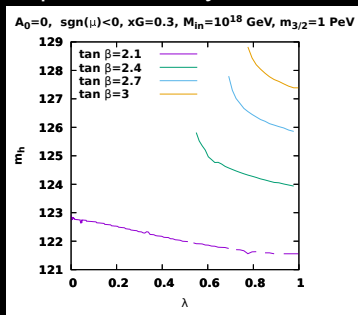
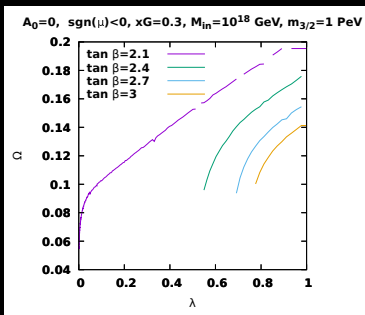
Super-GUT PGM

- ▶ CMSSM required Planck suppressed operators
- ▶ PGM proton decay is suppressed by soft masses
- ▶ PGM restricts $\tan \beta$
- ▶ Super-GUT RG running allows for larger $\tan \beta$

$$W_5 \supset \lambda \bar{H} \Sigma H \quad \rightarrow \quad \Delta \beta_{m_{H_u}^2} = \frac{|\lambda|^2}{8\pi^2} \left(m_\Sigma^2 + m_H^2 + m_H^2 + |A_\lambda|^2 \right)$$

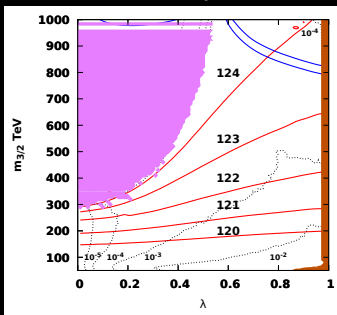
Super-GUT PGM

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 - Wino dark matter with acceptable density



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Non-Renormalizeable Operators in Super-GUT PGM

- ▶ Supersymmetric Non-Renormalizable operators

$$W_{\text{eff}}^{\Delta g} = \frac{c}{M_P} \text{Tr} [\Sigma \mathcal{W} \mathcal{W}] \quad \rightarrow \quad \lambda' \text{ Free Parameter}$$

- ▶ Heavy gauge bosons can be suppressed

$$\frac{5}{g_1^2(M_{GUT})} - \frac{3}{g_2^2(M_{GUT})} - \frac{2}{g_3^2(M_{GUT})} = -\frac{9}{2\pi^2} \ln \left(\frac{M_{GUT}}{(M_X^2 M_\Sigma)^{\frac{1}{3}}} \right) \quad M_\Sigma = \frac{5}{2} \lambda' V$$

- ▶ Large sfermion masses allow for large λ'
 - Dim-6 proton decay enhanced

$P \rightarrow \pi e$ in Minimal Supersymmetric SU(5)

- ▶ Heavy gauge bosons violate B,L

$$\mathcal{L}_{\text{int}} = \frac{g_5}{\sqrt{2}} \left[-\overline{d_{Ri}^c} \not{X} L_i + e^{-i\varphi_i} \overline{Q_i} \not{X} u_{Ri}^c + \overline{e_{Ri}^c} \not{X} (V^\dagger)_{ij} Q_j + \text{h.c.} \right]$$

- ▶ Amplitudes for $P \rightarrow \pi e$

$$\mathcal{A}_L(p \rightarrow \pi^0 e^+) = -\frac{g_5^2}{M_X^2} \cdot A_1 \cdot \langle \pi^0 | (ud)_R u_L | p \rangle ,$$

$$\mathcal{A}_R(p \rightarrow \pi^0 e^+) = -\frac{g_5^2}{M_X^2} (1 + |V_{ud}|^2) \cdot A_2 \cdot \langle \pi^0 | (ud)_R u_L | p \rangle ,$$

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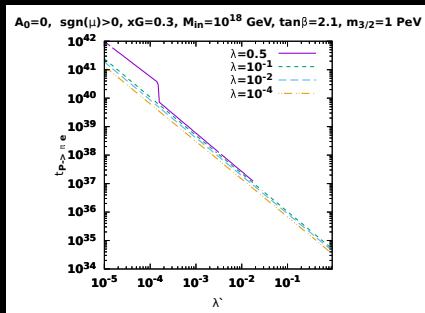
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Planck Corrections to Gauge Kinetic Terms

- ▶ For larger λ' Dim-6 Proton decay most important
 - Dim-5 suppressed by larger sfermion masses.



SUSY Breaking Planck Suppressed operators

- ▶ Planck Suppressed operators and SUSY breaking field

$$\Delta W = \frac{Z}{\sqrt{3}M_P} \mu \Phi \Psi + \frac{Z}{\sqrt{3}M_P} \Phi \Psi X \qquad \Delta K = \kappa_i \frac{Z}{\sqrt{3}M_P} |\Phi_i|^2 + \frac{Z}{\sqrt{3}M_P} \Phi \Psi$$

SUSY Breaking Planck Suppressed operators

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- ▶ Shift symmetry on Z restricts allowed operators

SUSY Breaking Planck Suppressed operators

- ▶ Planck Suppressed operators and SUSY breaking field
- ▶ Shift symmetry on Z restricts allowed operators
- ▶ A-terms and B-terms get corrections of order $m_{3/2}$

$$\Delta A = (\kappa_1 + \kappa_2 + \kappa_3)m_{3/2} \quad \Delta B = (\kappa_1 + \kappa_2)m_{3/2}$$

$$W = \mu\phi_1\phi_2 + y\phi_1\phi_2\phi_3$$

SUSY Breaking Planck Suppressed operators

- ▶ Planck Suppressed operators and SUSY breaking field
- ▶ Shift symmetry on Z restricts allowed operators
- ▶ A-terms and B-terms get corrections of order $m_{3/2}$

$$\Delta A = (\kappa_1 + \kappa_2 + \kappa_3)m_{3/2} \quad \Delta B = (\kappa_1 + \kappa_2)m_{3/2}$$

- ▶ A and B-terms give large corrections to gaugino masses

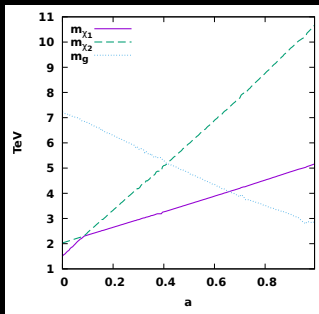
$$M_1 = \frac{g_1^2}{g_5^2} M_5 - \frac{g_1^2}{16\pi^2} \left[10M_5 - 10(A_{\lambda'} - B_{\Sigma}) - \frac{2}{5}B_H \right] - \frac{4cg_1^2 V(A_{\lambda'} - B_{\Sigma})}{M_P}$$

$$M_2 = \frac{g_2^2}{g_5^2} M_5 - \frac{g_2^2}{16\pi^2} [6M_5 - 6A_{\lambda'} + 4B_{\Sigma}] - \frac{12cg_2^2 V(A_{\lambda'} - B_{\Sigma})}{M_P}$$

$$M_3 = \frac{g_3^2}{g_5^2} M_5 - \frac{g_3^2}{16\pi^2} [4M_5 - 4A_{\lambda'} + B_{\Sigma} - B_H] + \frac{8cg_3^2 V(A_{\lambda'} - B_{\Sigma})}{M_P}$$

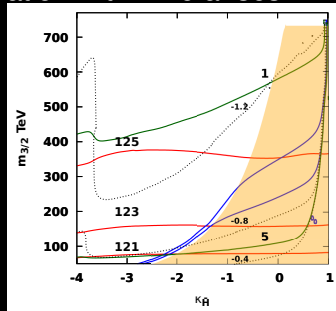
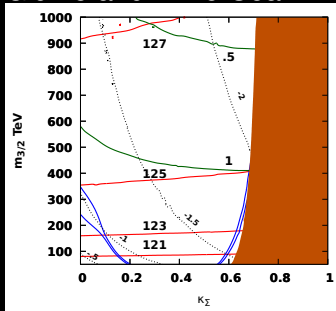
Dark Matter in PGM

- ▶ Guaginos change so much that LSP changes



Dark Matter in PGM

- ▶ Guaginos change so much that LSP changes
- ▶ Gluino and Wino Coannihilation with Bino arises



Conclusions

- ▶ Science is about interrelating parameters
- ▶ Supersymmetric models are still true to goals of science
- ▶ Gauge couplings unify in SUSY
 - Important guided for BSM
- ▶ Min-SUSY SU(5) models have low-scale consequences
 - Proton decay requires large soft masses
 - Matching conditions prefer large A -terms
- ▶ Right-handed neutrinos lead to additional constraints
 - Generated mixing in $m_{\tilde{d}}^2$ can lead to large ε_K
- ▶ Right-handed neutrinos also leads to additional signals
 - Irreducible FV+CPV lead to future detectable eEDM's
- ▶ Higher Dim Operators can have important Consequences