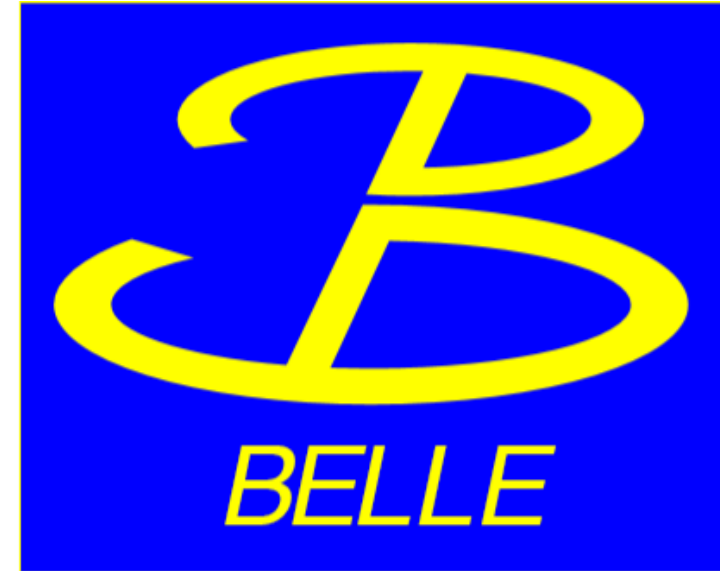


# Measurement of time-dependent CP violation in $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ decays at Belle

**Kookhyun Kang**

Kavli IPMU

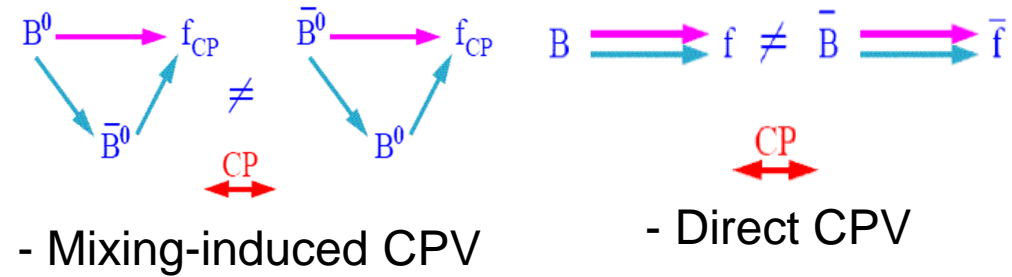
2021.11.05



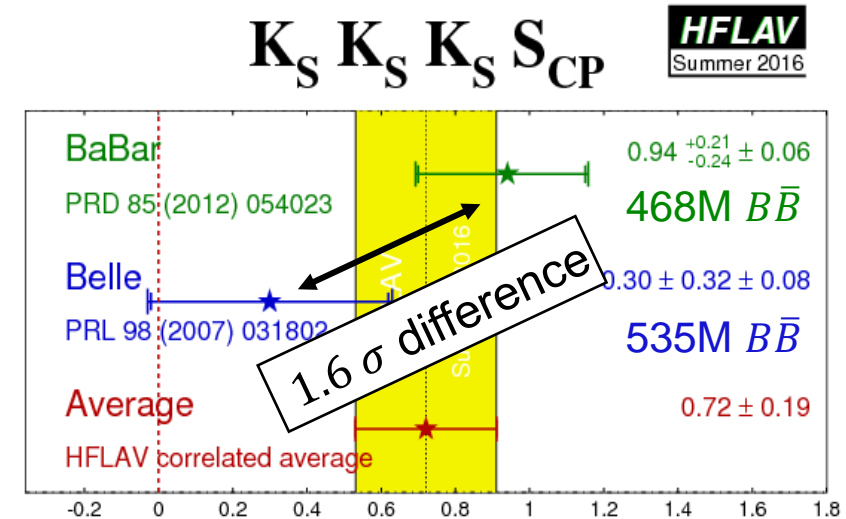
# Outline

- Introduction
- Study with Monte Carlo (MC)
  - Signal selection
  - Background suppression
- Results
- Summary

# Introduction – motivation (1)

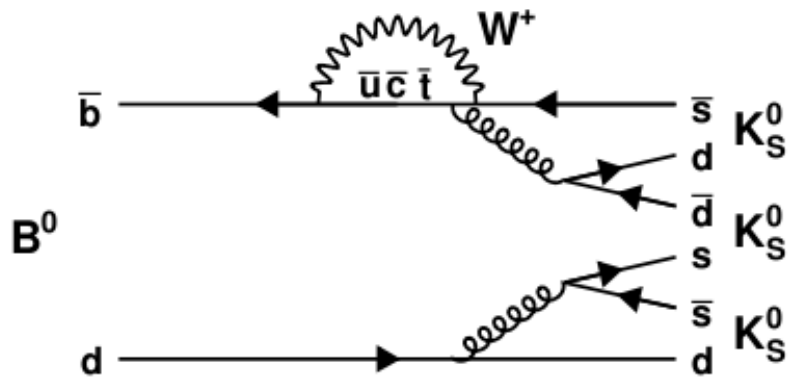


- Time-dependent CP violation (TDCPV) parameters are  $S$  and  $A$ 
  - $S$  = mixing induced CP violation
  - $A$  = direct CP violation
- Standard Model expectation in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  decays,
  - $S = \sin(2\phi_1) = 0.688$ ,  $A = 0$ ,  $\phi_1 \equiv \arg\left(\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*}\right)$
- From the results
  - Deviations from the SM expectation provide sensitivity to new physics.
  - Difference of  $S$  at previous Belle and BaBar

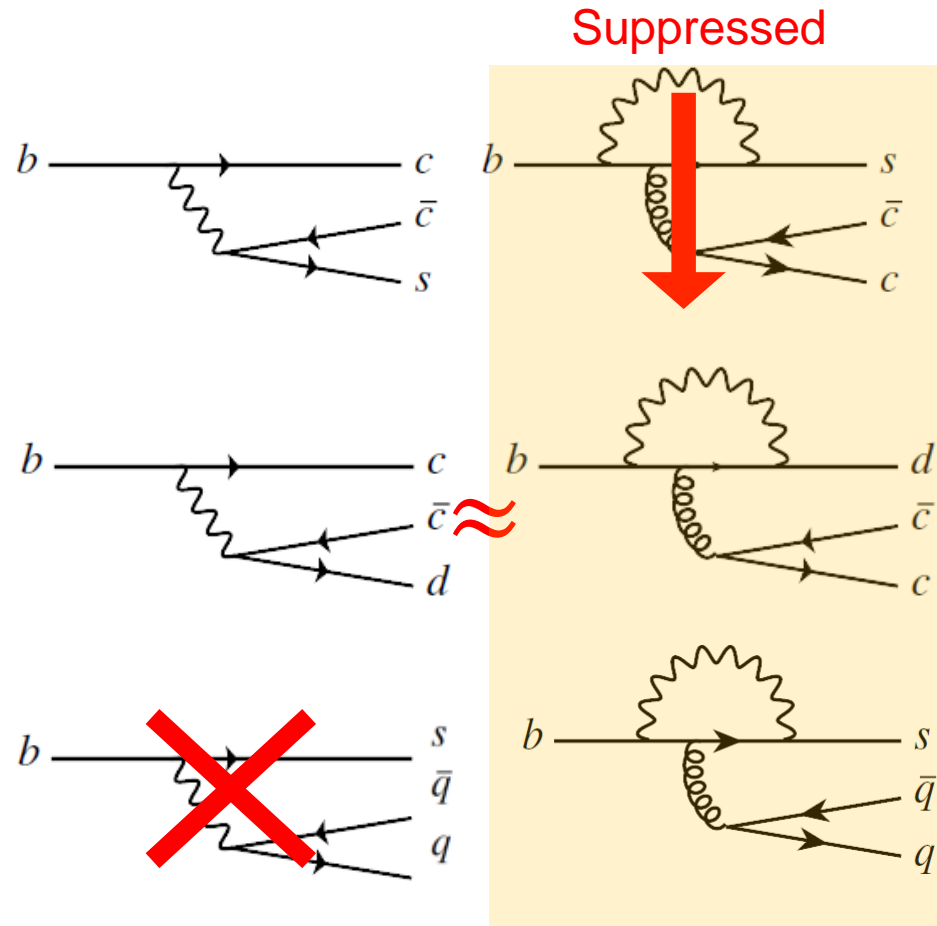


✓ We measure  $S$  and  $A$  in the  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  decays with the final Belle data set of  $772 \times 10^6 B\bar{B}$

# Introduction – motivation (2)



- Pure  $b \rightarrow s$  penguin transition by loop diagram



Forbidden in SM

$\sin 2\phi_1$   
 $b \rightarrow c \bar{c} s$   
 ex:  $B^0 \rightarrow J/\psi K_S^0$

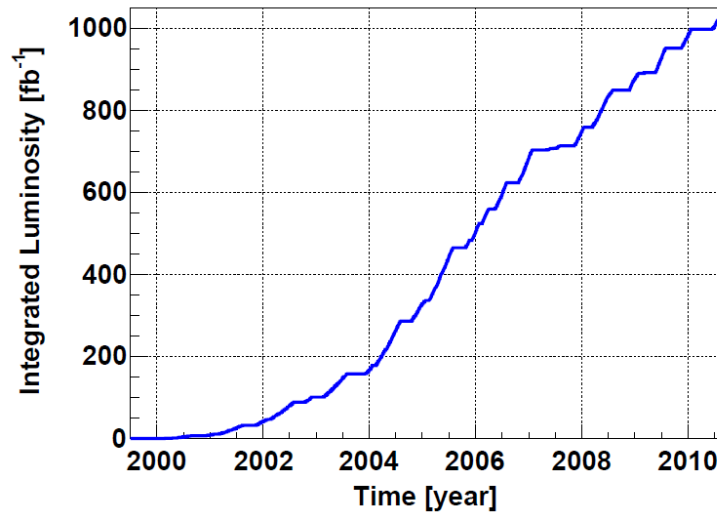
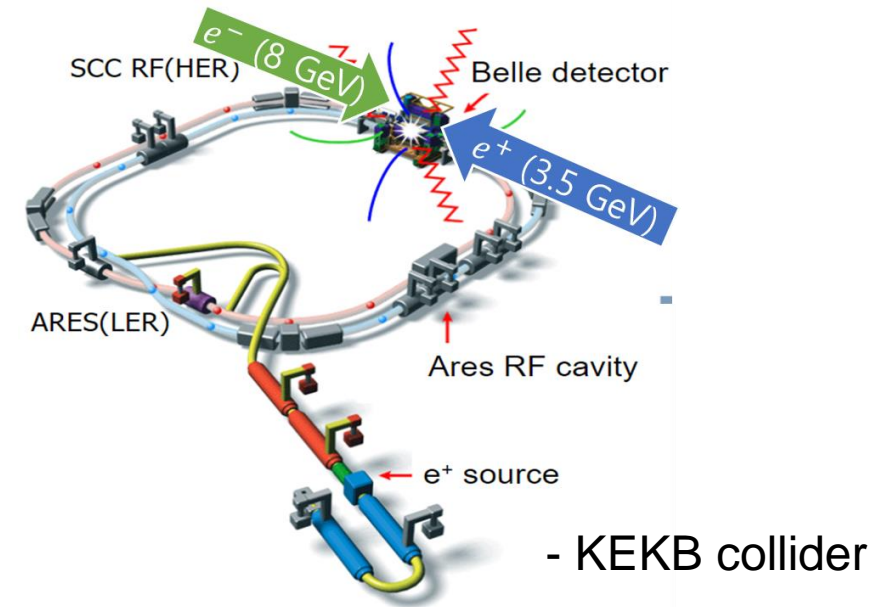
$b \rightarrow c \bar{c} d$   
 ex:  $B^0 \rightarrow J/\psi \pi^0$

$\sin 2\phi_1^{eff}$   
 $b \rightarrow s \bar{q} q$   
 ex:  $K_S^0 K_S^0 K_S^0$

✓ Significant deviation of  $\sin 2\phi_1^{eff}$  from  $\sin 2\phi_1$  indicates evidence of NP.

# Introduction - Belle experiment

- KEKB is B-meson factory in Tsukuba at Japan.
  - Asymmetric  $e^+e^-$  collider
  - LER( $e^+$ ) = 3.5 GeV
  - HER( $e^-$ ) = 8 GeV
  - Center of Mass energy = 10.58 GeV
- $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$

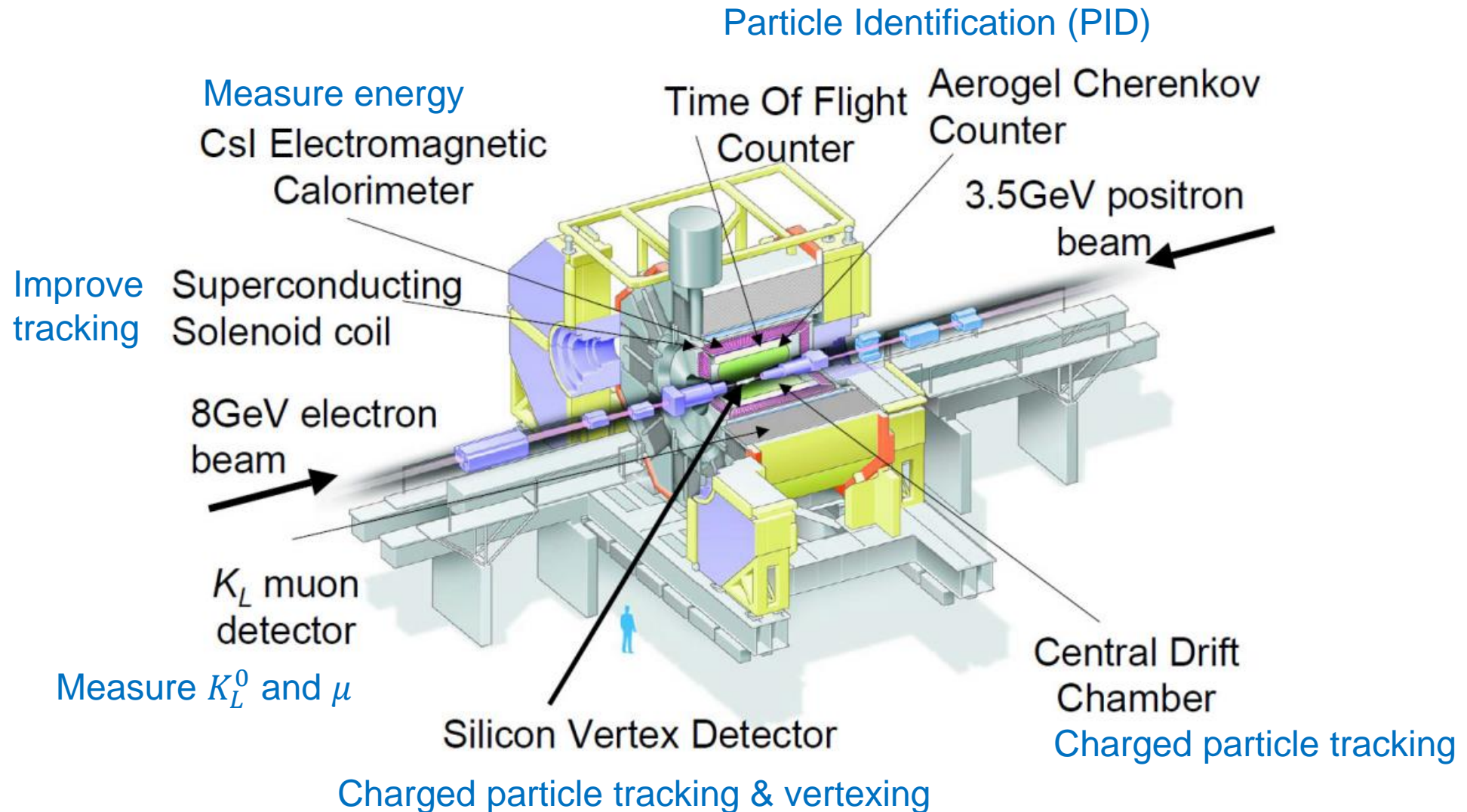


On resonance:  
 $\Upsilon(5S)$ : 121 fb<sup>-1</sup>  
 $\Upsilon(4S)$ : 711 fb<sup>-1</sup>  
 $\Upsilon(3S)$ : 3 fb<sup>-1</sup>  
 $\Upsilon(2S)$ : 25 fb<sup>-1</sup>  
 $\Upsilon(1S)$ : 6 fb<sup>-1</sup>  
Off resonance  
/scan:  
155 fb<sup>-1</sup>

✓ Verification of the Kobayashi-Maskawa theory of CP-violation in B-meson decay



# Introduction - Belle detector



# Introduction – time-dependent $CP$ violation

- The time-dependent  $CP$  violation ( $TDCPV$ ) can be caused by
  - interference between  $B^0$  decay to  $CP$  eigenstate ( $f_{CP}$ ) and  $B^0 - \bar{B}^0$  mixing.
- $\Upsilon(4S) \rightarrow B^0 \bar{B}^0$  in to  $CP$  eigenstate, the decay rate is given by

$$P = \frac{e^{-\frac{|\Delta t|}{\tau_{B^0}}}}{4\tau_{B^0}} \times (1 + q[S \sin(\Delta m_d \Delta t) + A \cos(\Delta m_d \Delta t)])$$

$S$  = mixing-induced  $CP$  violation

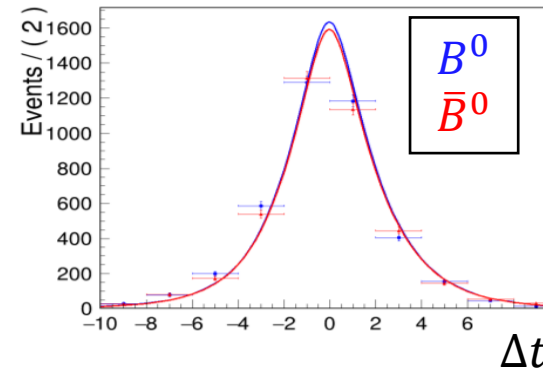
$A$  = direct  $CP$  violation

$\Delta m_d$  = mass difference between

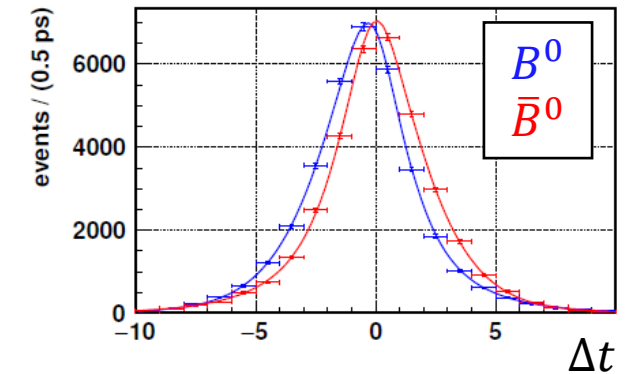
$q$  = flavor information of tag side

$\Delta t$  = distance between B-meson pairs

$$\mathcal{A}_{CP} = \frac{P(\bar{B}^0(\Delta t) \rightarrow f_{CP}) - P(B^0(\Delta t) \rightarrow f_{CP})}{P(\bar{B}^0(\Delta t) \rightarrow f_{CP}) + P(B^0(\Delta t) \rightarrow f_{CP})} = S \sin(\Delta m_d \Delta t) + A \cos(\Delta m_d \Delta t)$$

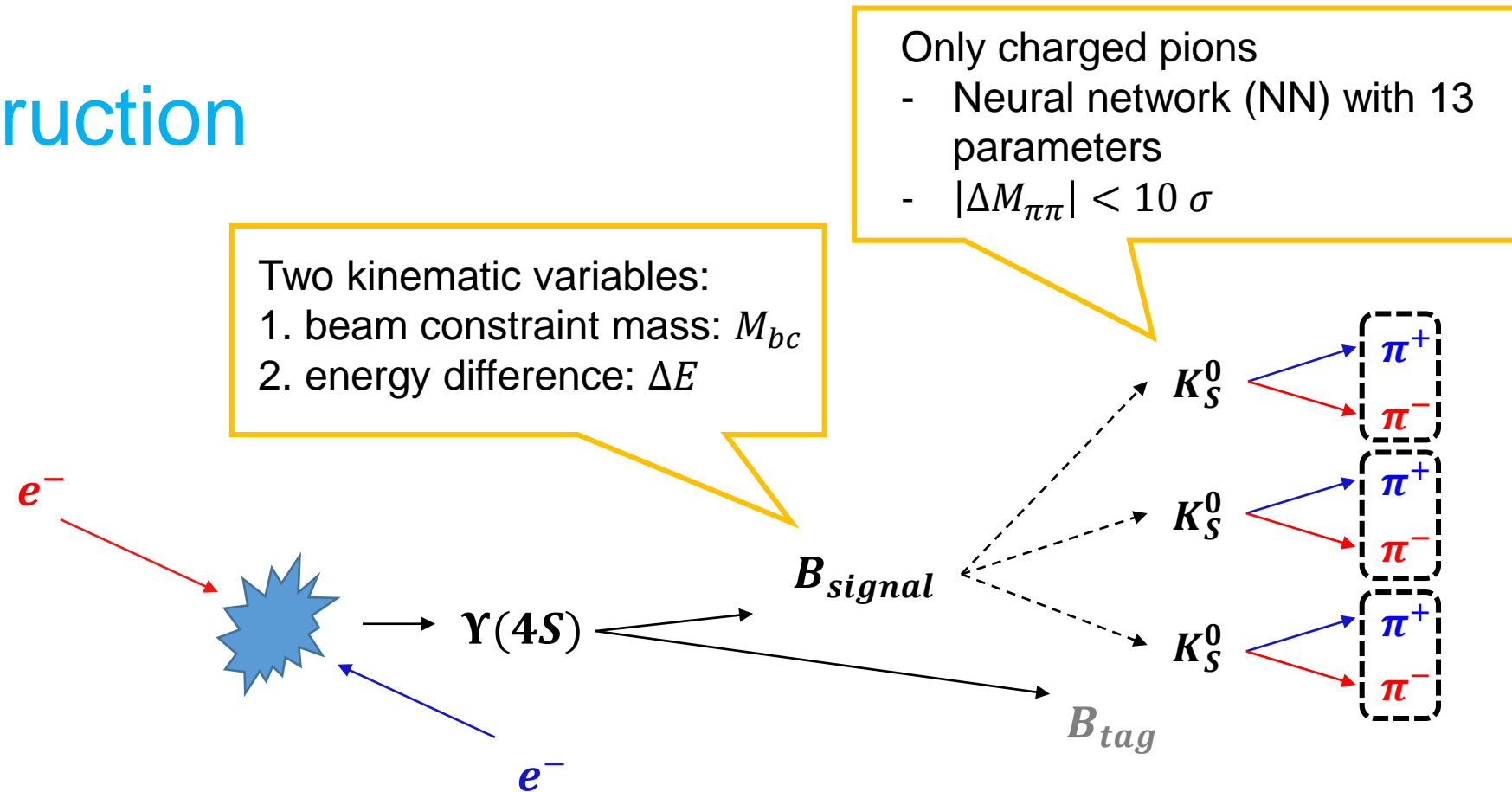


- non TDCPV



- TDCPV

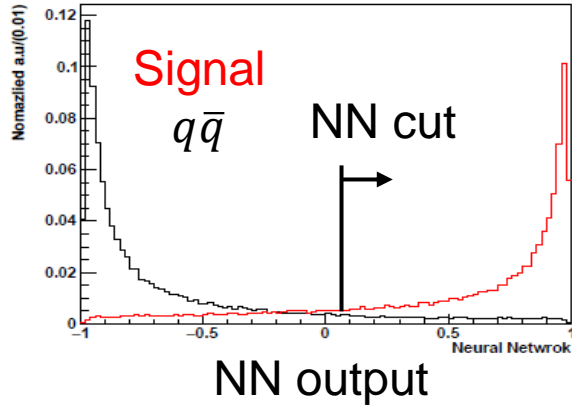
# Signal reconstruction



- $\Delta E = E_B - E_{beam}$ 
  - $E_B$  = energy of B in CM frame
  - $E_{beam}$  = half of beam energy
- $M_{bc} = \sqrt{E_{beam}^2 - p_B^2}$ 
  - $p_B$  = momentum of B in CM frame

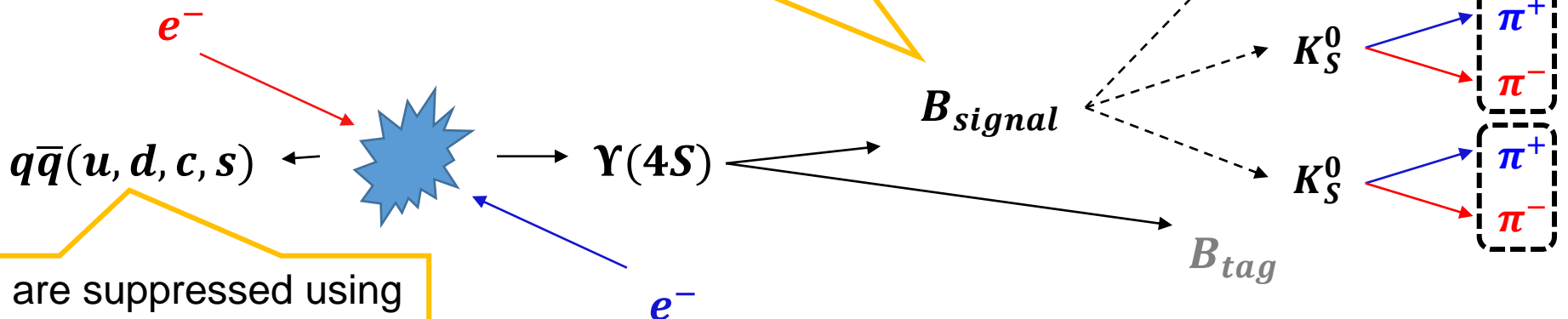


# Signal reconstruction

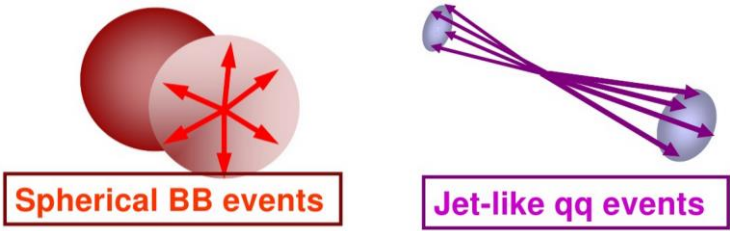


Two kinematic variables:  
 1. beam constraint mass:  $M_{bc}$   
 2. energy difference:  $\Delta E$

Only charged pions  
 - Neural network (NN) with 13 parameters  
 -  $|\Delta M_{\pi\pi}| < 10 \sigma$



Continuum backgrounds are suppressed using topology information along with the NN



- $\Delta E = E_B - E_{beam}$ 
  - $E_B$  = energy of B in CM frame
  - $E_{beam}$  = half of beam energy
- $M_{bc} = \sqrt{E_{beam}^2 - p_B^2}$ 
  - $p_B$  = momentum of B in CM frame

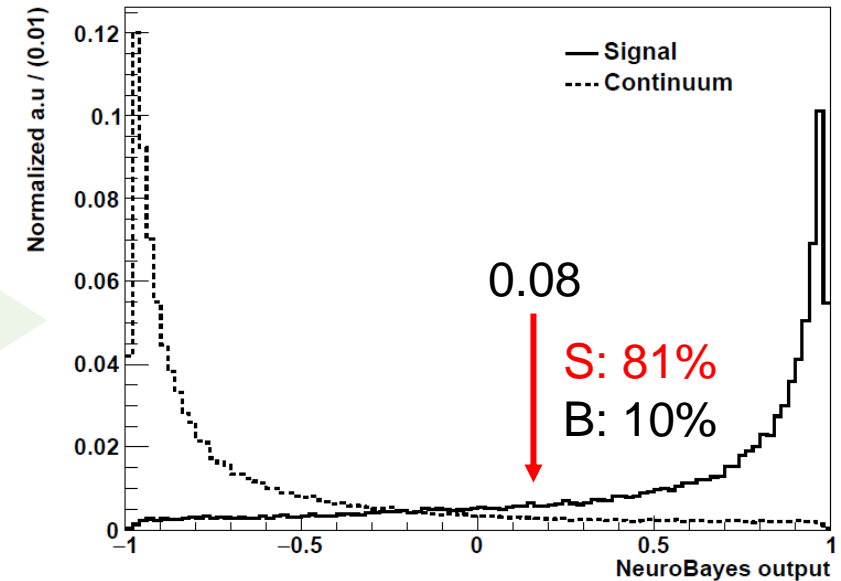
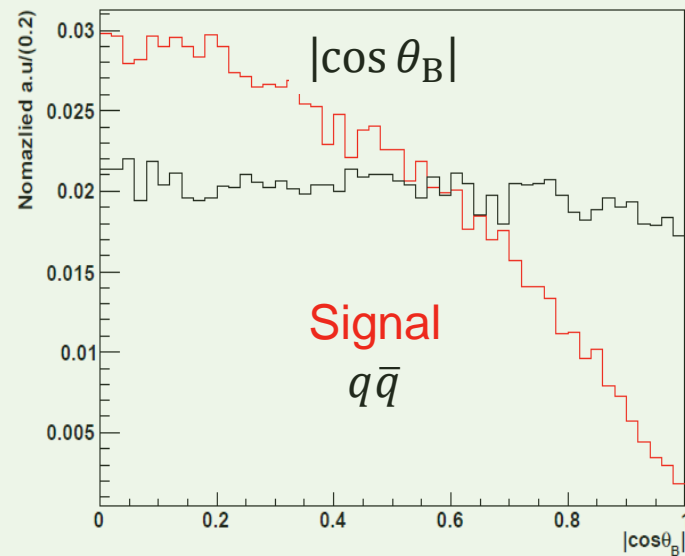
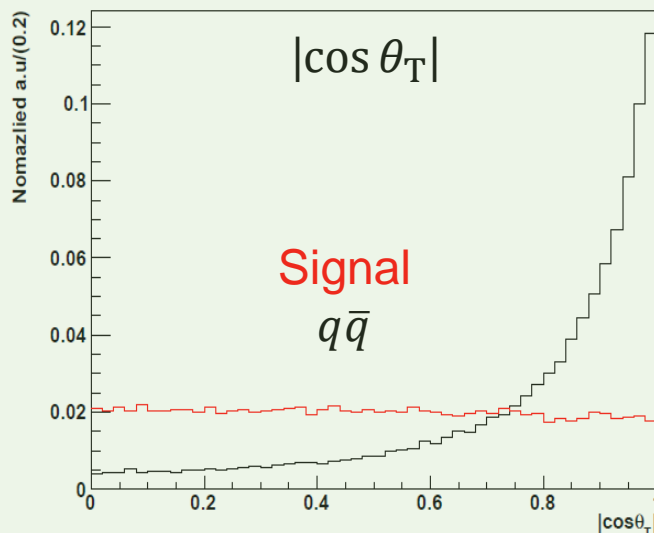
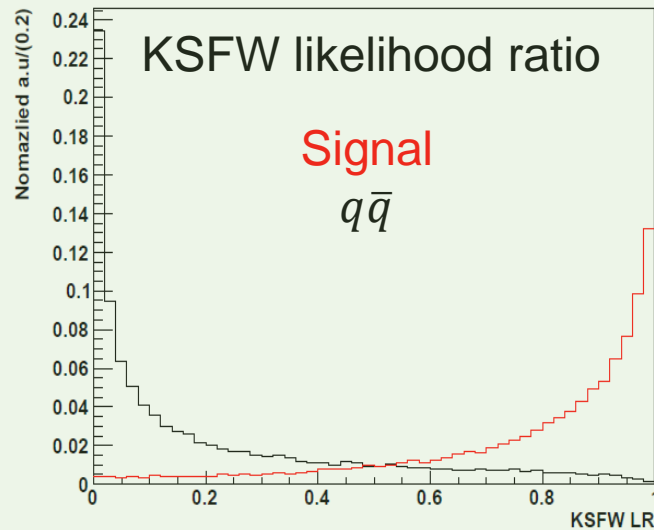
B mesons are produced all most at rest in the  $\Upsilon(4S)$  frame  
 → In contrast for  $q\bar{q}$  events, it has a large initial momentum

# Continuum background

KSFW LR – Kakuno Super Fox-Wolfram moment

$\cos\theta_B$  = cosine of the angle between beam pipe and  $B_{CP}$

$\cos\theta_T$  = cosine of the angle between thrust axis of  $B_{cp}$  and  $B_{tag}$



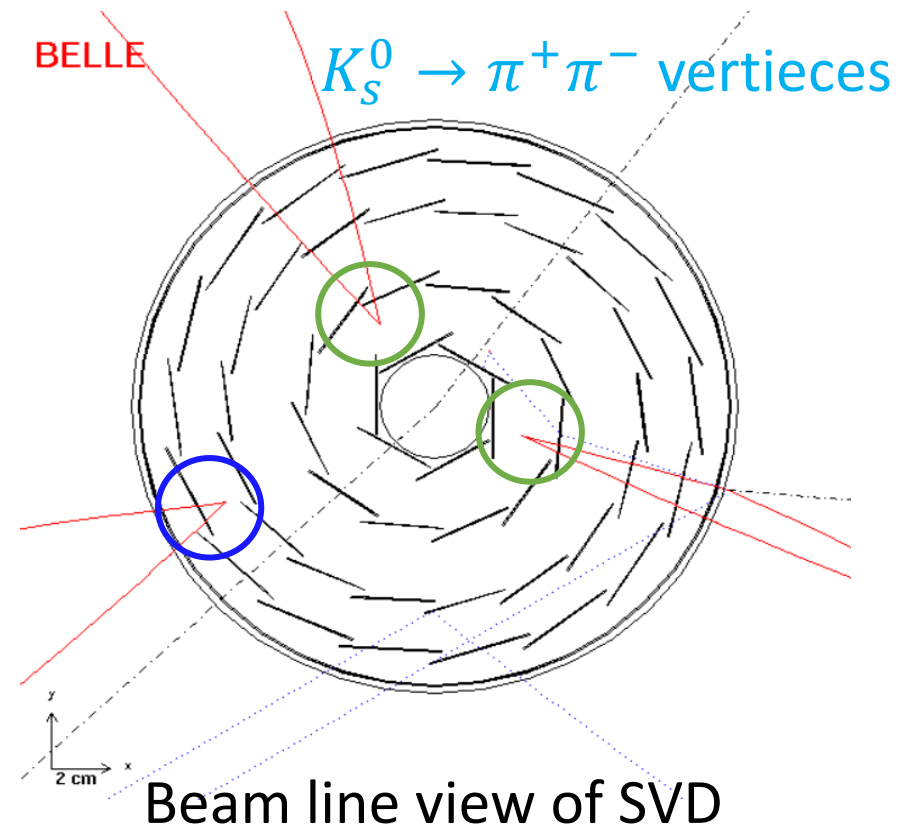
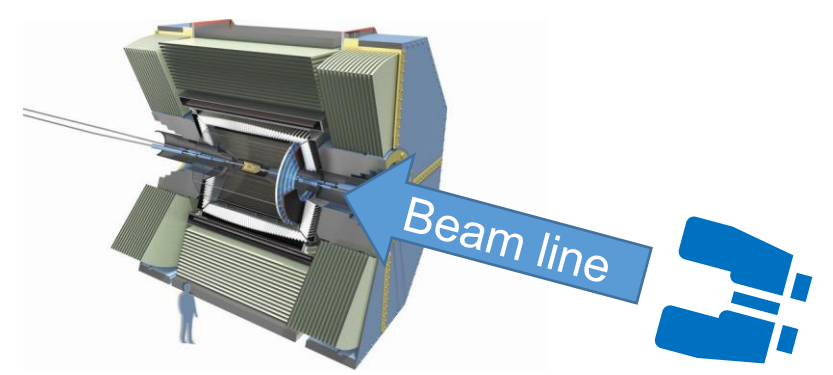
The NB cut is selected with highest figure of merit (FOM)

$$\text{FOM} = \frac{N_{sig}}{\sqrt{N_{sig} + N_{bkg}}}$$

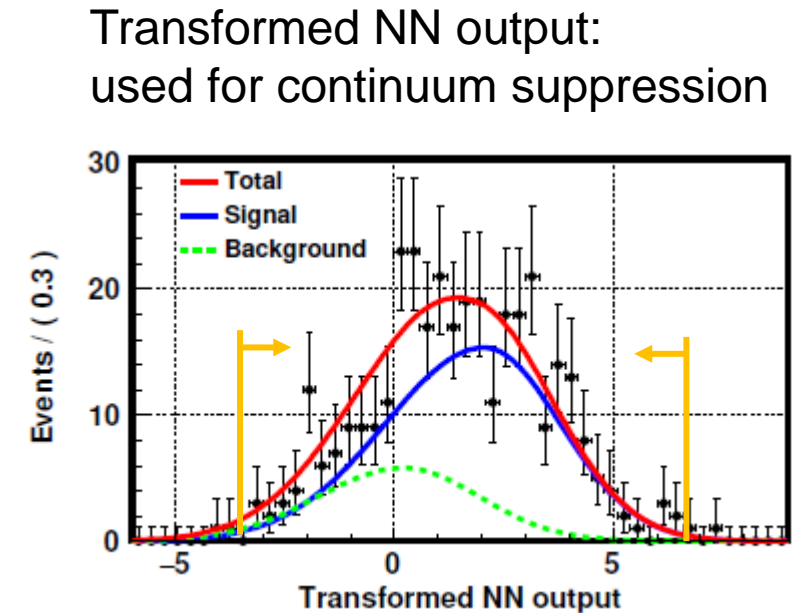
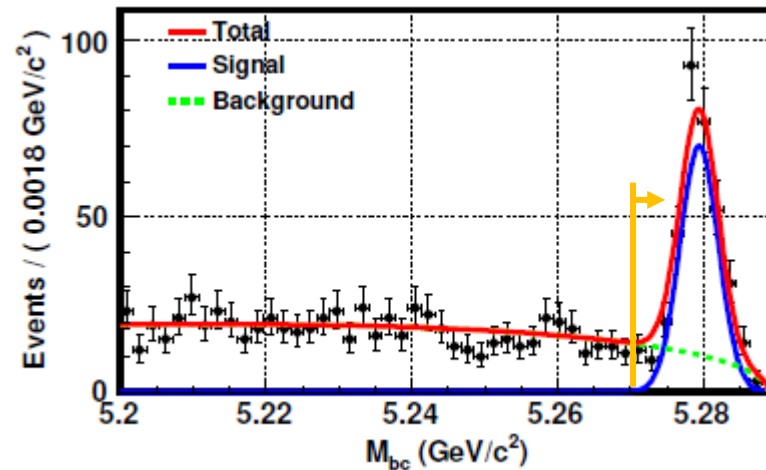
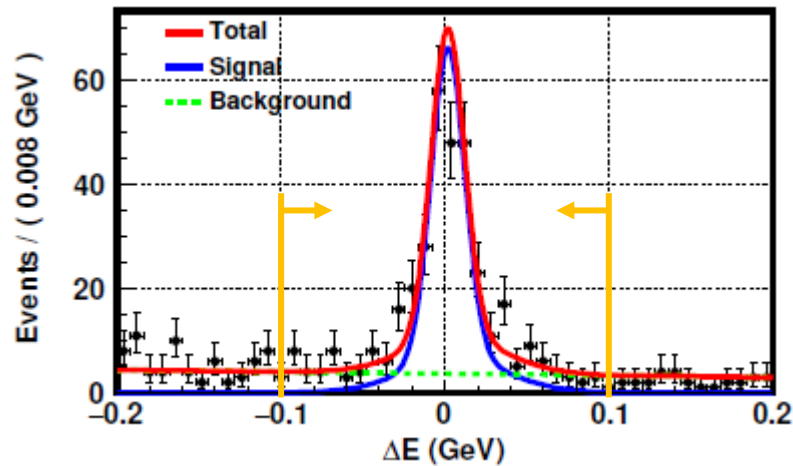


# Vertex reconstruction

- In  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ , there is no primary charged track
  - to find vertex position we make Ks trajectory using pion hit
- Resolution function of  $\Delta t$ 
  - Detector resolution
  - Non-primary track effect for  $B_{tag}$
  - Kinematical approximation due to the difference in the  $p_{lab}$  of  $B^0 \bar{B}^0$



# Results - signal extraction



- An unbinned maximum likelihood (ML) fit with 3D PDF ( $\Delta E$ ,  $M_{bc}$ , Transformed  $NN$ ).
- Signal  $B^0$  &  $\bar{B}^0$  is obtained to be  $258 \pm 17$  and the purity in the signal region is 74%.

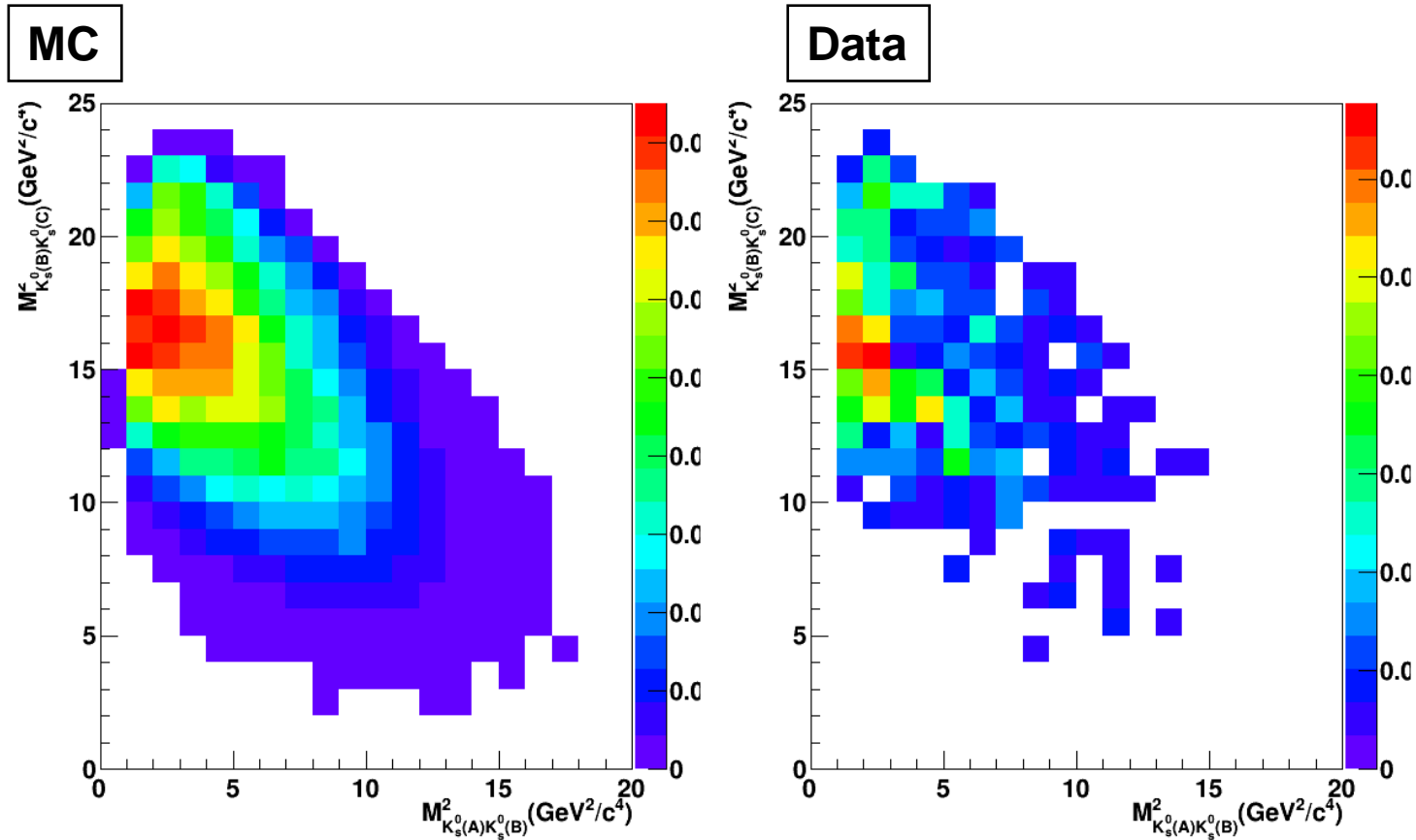
PDF	$\Delta E$	$M_{bc}$	Transformed $NN$
Signal	Double Gaussian	Gaussian	Asymmetry Gaussian
Background	1 <sup>st</sup> Polynomial	ARGUS	Asymmetry Gaussian

# List of resonance modes

Several resonance mode can be included to signal event because we require three  $K_S^0$  from  $B^0$

	Decay mode	$B(B^0 \rightarrow XK_S^0)$	$B(X \rightarrow K_S^0 K_S^0)$	Expected events
Background $b \rightarrow c$ CP odd	$B^0 \rightarrow D^0 K_S^0$	$(2.6 \pm 0.35) \times 10^{-5}$	$(1.7 \pm 0.12) \times 10^{-4}$	$0.3 \pm 0.0$
	$B^0 \rightarrow \eta_c K_S^0$	$(3.45 \pm 0.6) \times 10^{-4}$	$< 3.1 \times 10^{-4}$ 90%	$< 7.6 \pm 1.2$
	$B^0 \rightarrow J/\psi K_S^0$	$(4.35 \pm 0.16) \times 10^{-4}$	$< 1.4 \times 10^{-8}$	$< 0.0 \pm 0.0$
	$B^0 \rightarrow \psi(2S) K_S^0$	$(2.9 \pm 0.25) \times 10^{-4}$	$< 4.6 \times 10^{-6}$	$< 0.1 \pm 0.0$
	$B^0 \rightarrow \chi_{c0} K_S^0$	$(0.73 \pm 0.13) \times 10^{-4}$	$(3.16 \pm 0.17) \times 10^{-3}$	<b><math>16.3 \pm 3.1</math></b>
	$B^0 \rightarrow \chi_{c1} K_S^0$	$(1.96 \pm 0.13) \times 10^{-4}$	$< 6 \times 10^{-5}$ CL=90%	$< 0.8 \pm 0.1$
	$B^0 \rightarrow \chi_{c2} K_S^0$	$(0.75) \times 10^{-5}$ CL = 90%	$(2.6 \pm 0.2) \times 10^{-4}$	$0.3 \pm 0.0$
Signal $b \rightarrow s$	$B^0 \rightarrow f_2(1270) K_S^0$	$(1.35^{+0.65}_{-0.6}) \times 10^{-6}$	$(1.15^{+0.12}_{-0.1}) \times 10^{-2}$	$1.1^{+0.5}_{-0.5}$
	$B^0 \rightarrow f_0(1500) K_S^0$	$(0.65^{+0.35}_{-0.25}) \times 10^{-5}$	$(2.15 \pm 0.25) \times 10^{-2}$	$9.9^{+5.5}_{-4.0}$
	$B^0 \rightarrow f'_2(1525) K_S^0$	$(1.5^{+2.5}_{-2.0}) \times 10^{-7}$	$(22.17 \pm 0.55) \times 10^{-2}$	$2.4^{+3.9}_{-3.1}$
	$B^0 \rightarrow f_0(980)(K_S^0 K_S^0) K_S^0$	$(2.7 \pm 1.8) \times 10^{-6}$		$191.3 \pm 127.6$
	$B^0 \rightarrow f_0(1710)(K_S^0 K_S^0) K_S^0$	$(5.0^{+5.0}_{-2.6}) \times 10^{-7}$		$35.4^{+35.4}_{-18.4}$
	$B^0 \rightarrow f_2(2010)(K_S^0 K_S^0) K_S^0$	$(5 \pm 6) \times 10^{-7}$		$35.4 \pm 42.5$

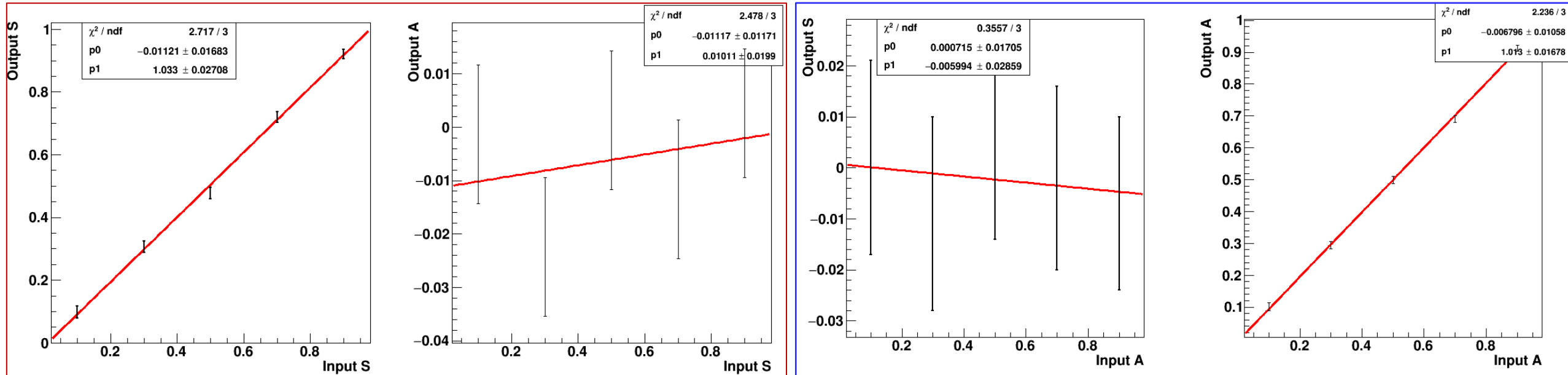
# Results - Dalitz plot



✓ Compare the dalitz plot for MC and data, our evtgen model for MC generation by PHSP well describes data.

# CP fitting – linearity check using signal MC

- Input  $S$  : 0.1, 0.3, 0.5, 0.7, 0.9 with  $A = 0$
- Input  $A$  : 0.1, 0.3, 0.5, 0.7, 0.9 with  $S = 0$



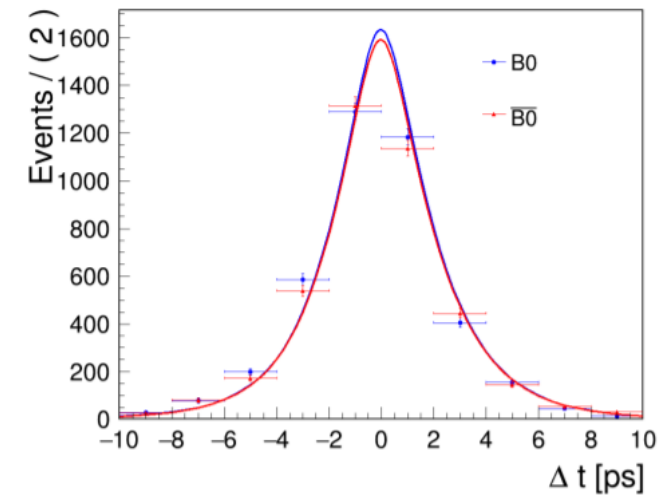
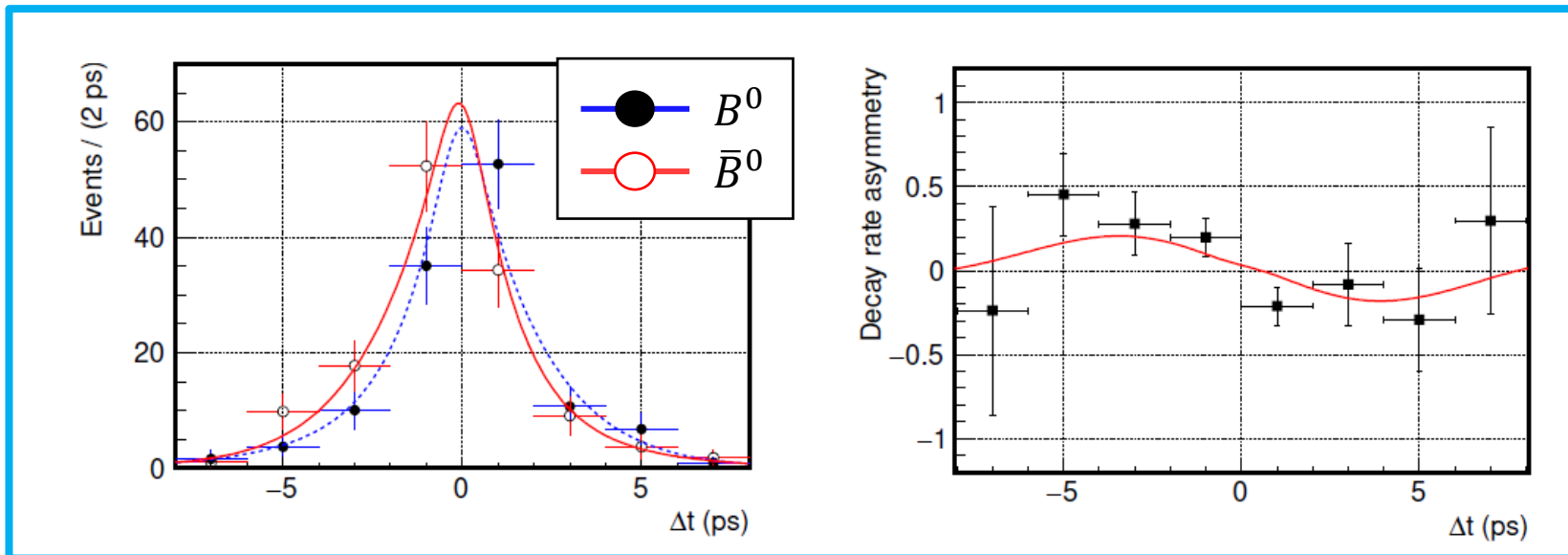
For  $S$  variation

For  $A$  variation



# Measurement of TDCPV parameters

- Fitting results
  - $S = -0.71 \pm 0.23$  (stat)  $\pm 0.05$  (syst)
    - $-\sin 2\phi_1$  in  $b \rightarrow c\bar{c}s = -0.699$
  - $A = 0.12 \pm 0.16$  (stat)  $\pm 0.05$  (syst)



Without TCPV

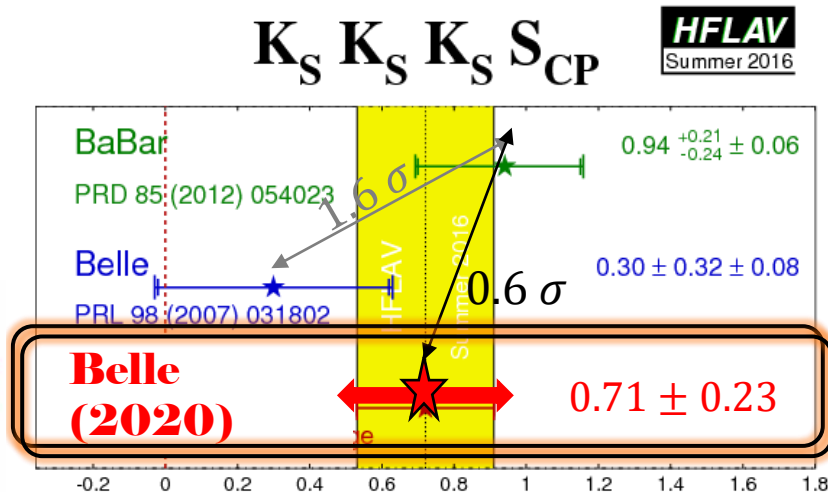
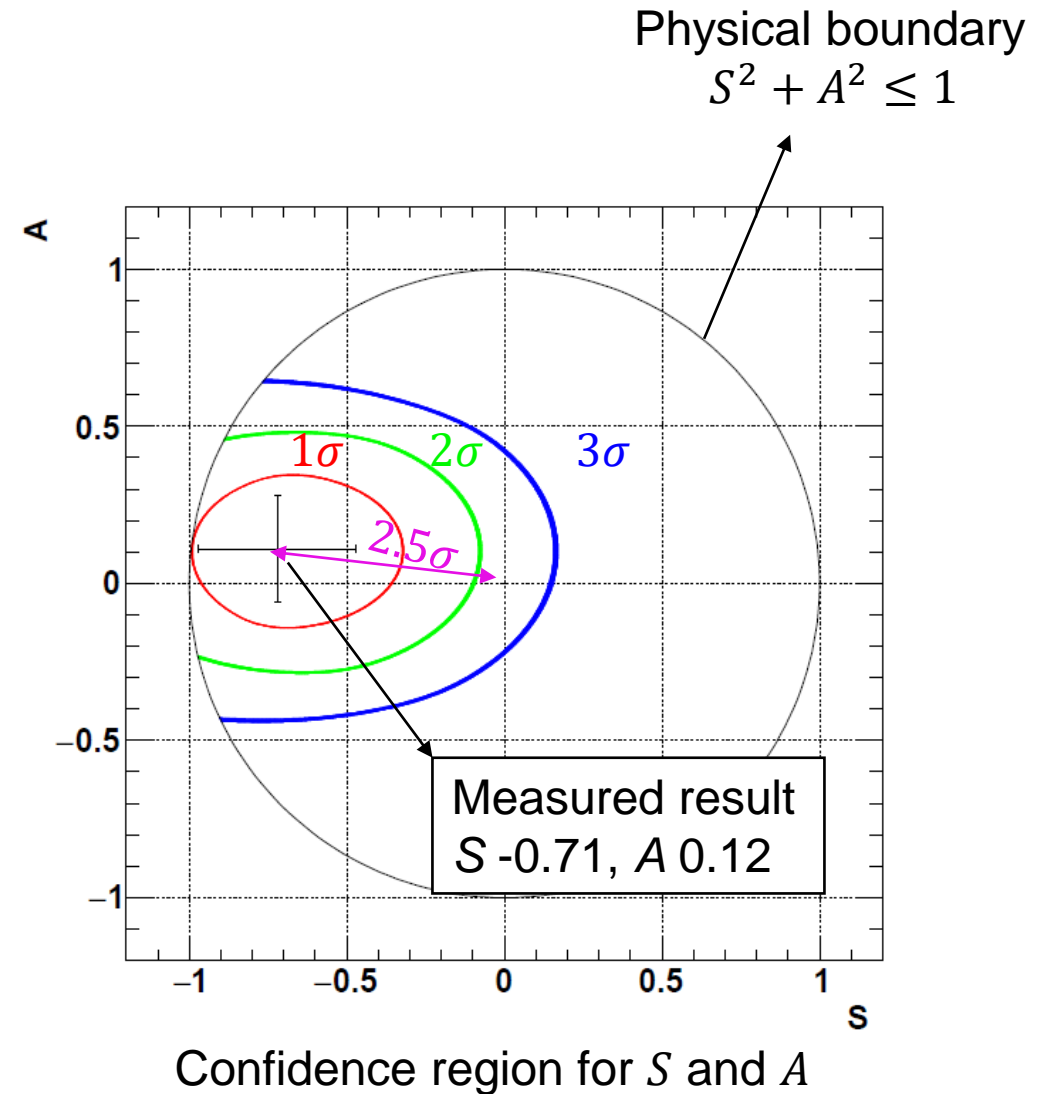
# Systematic error

Source	$S$	$A$
Vertex reconstruction	0.031	0.038
Flavor tagging	0.002	0.004
Resolution function	0.016	0.014
Physics parameters	0.004	0.001
Fit bias	0.012	0.009
Signal fraction	0.024	0.021
Background $\Delta t$ shape	0.016	0.001
SVD misalignment	0.004	0.005
$\Delta z$ bias	0.002	0.004
Tag-side interference	0.001	0.008
Total	0.05	0.05

Main source of systematic error comes from non-primary charged track.

# Significance of $CP$ violation

- The significance is calculated using the Feldman-Cousins approach.
  - Frequentist approach
    - ↔ Bayesian approach (PDF based on hypothesis)
- The significance of  $CP$  violation is determined to be  $2.5\sigma$  away from (0,0)



Consistent with previous measurements and  $b \rightarrow c\bar{c}s$

# Summary

- The measurements of time-dependent  $CP$  violation in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  decays using the final data sample ( $772 \times 10^6 B\bar{B}$ ):
  - $S = -0.72 \pm 0.23$  (stat)  $\pm 0.05$  (syst)
  - $A = 0.11 \pm 0.16$  (stat)  $\pm 0.05$  (syst)
- The results are
  - The results are consistent with SM expectation (-0.70)
  - Previous Belle & BaBar result
- PHYSICAL REVIEW D 103, 032003 (2021)
  - <https://doi.org/10.1103/PhysRevD.103.032003>

# Backup

# Signal reconstruction

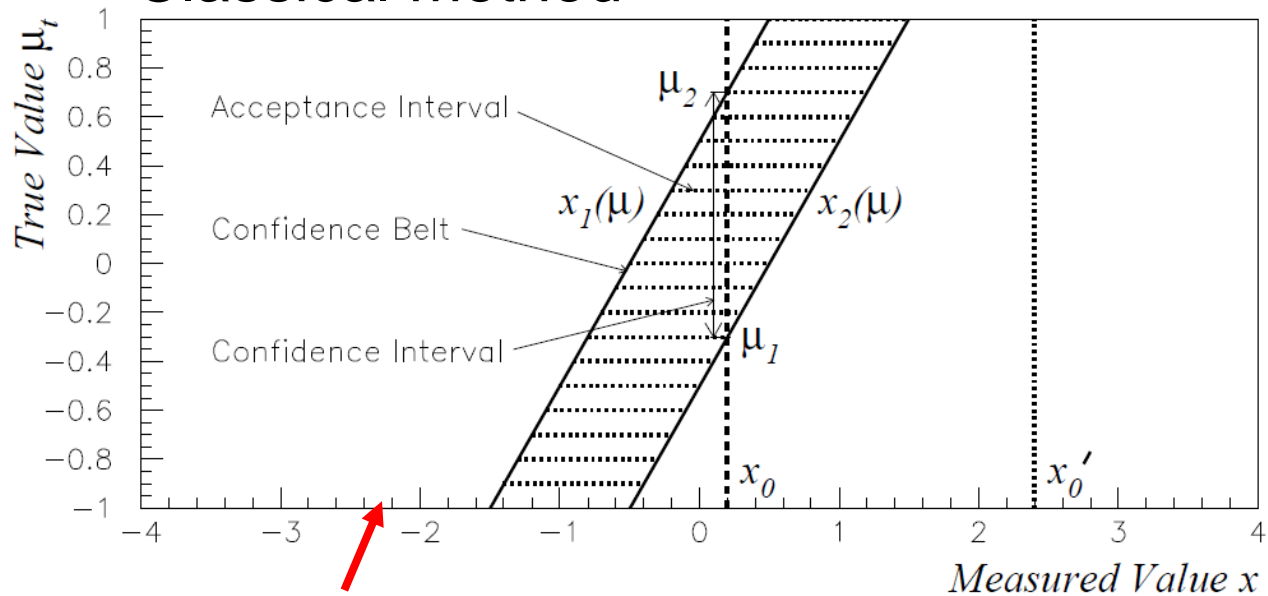
## – selection criteria and best candidate selection

- We use  $K_S^0$  only from charged decay to avoid background.

	$B^0 \rightarrow K_S^0 K_S^0 K_S^0$
$K_S^0 (\pi^+ \pi^-)$ selection in <code>mdst_vee2</code>	$ \Delta M_{\pi\pi}  < 10 \sigma,$ <code>nisKsfinder</code> cut ( <code>nb_vlike</code> >0.2)
$\Delta E$ [GeV]	$-0.2 < \Delta E < 0.2$
$M_{bc}$ [GeV/ $c^2$ ]	$5.2 < M_{bc}$
Best candidate selection	smallest of $\chi^2 = \sum_{i=1}^3 \left( \frac{M_{\pi\pi}^i - M_{K_S^0}}{\sigma_{\pi\pi}} \right)^2$
Continuum BKG suppression	KSFW LR, $\cos\theta_B$ , $\cos\theta_T$ <i>NeuroBayes</i> output>0.08

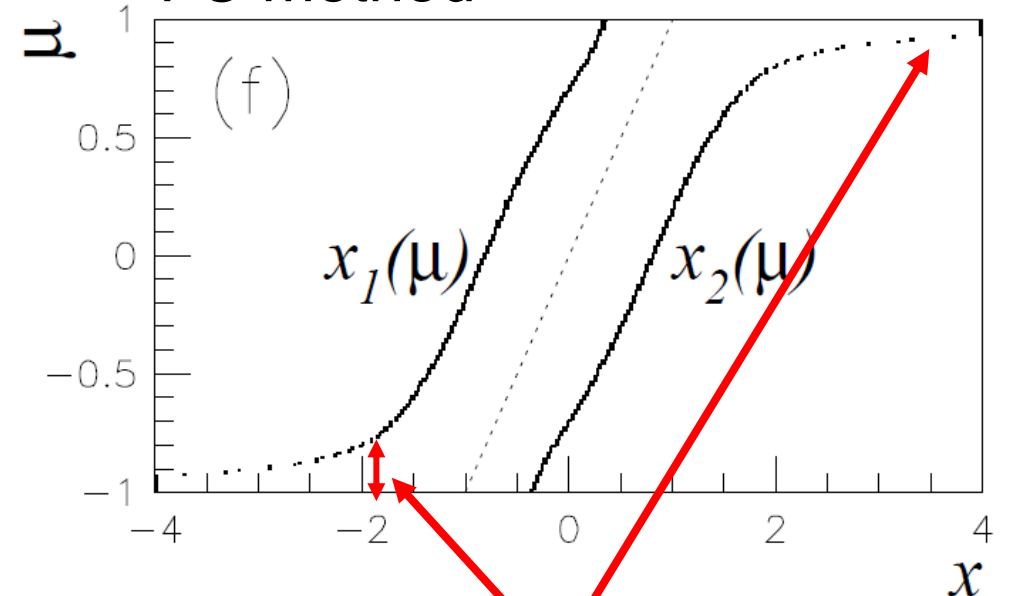
# Classical and FC frequentist

## Classical method



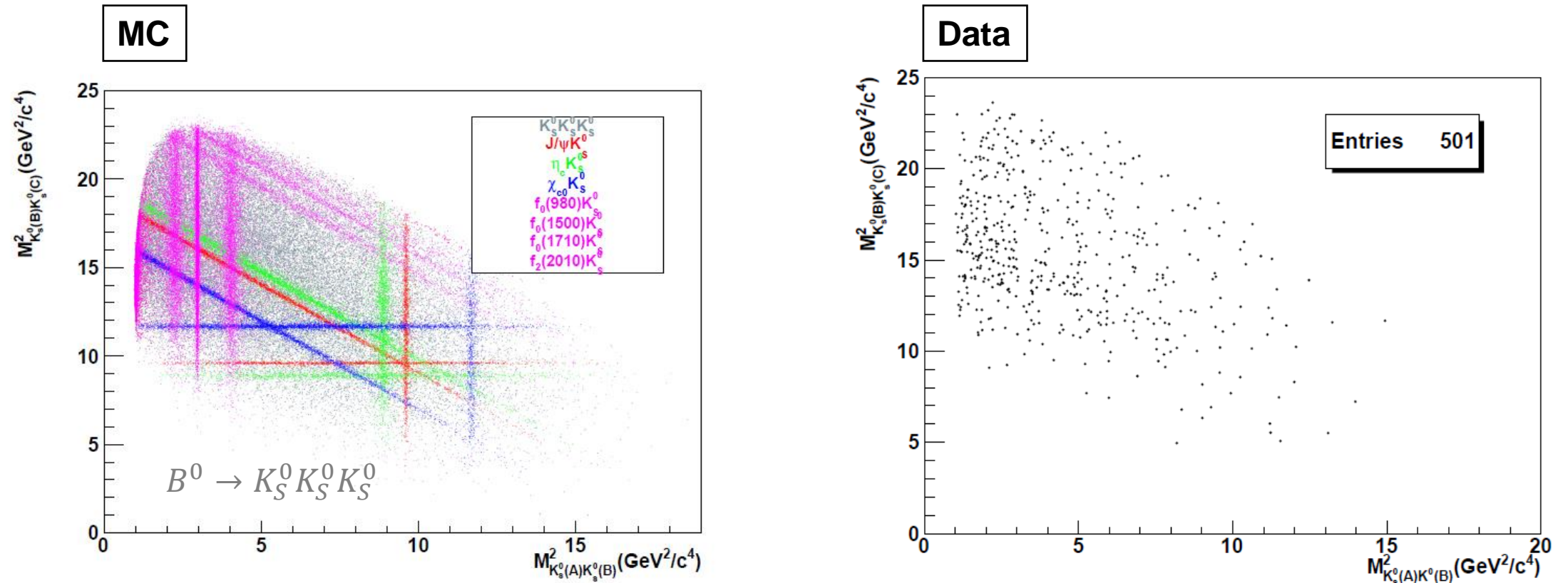
Confidence belt is empty  
when measured value  $x$  is far from physical region

## FC method



Confidence belt is never empty!  
By ordering principle

# Dalitz plot

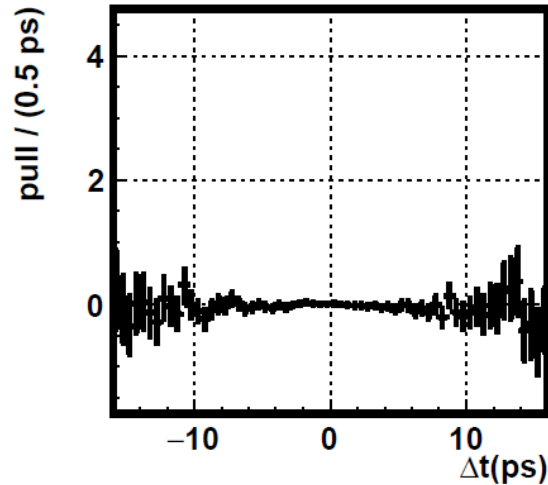
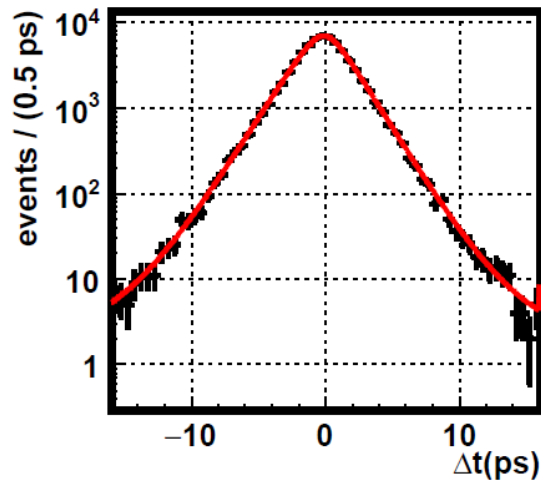


- Compare the dalitz plot for MC and data, our evtgen model for MC generation, PHSP\_CP, well describes data.

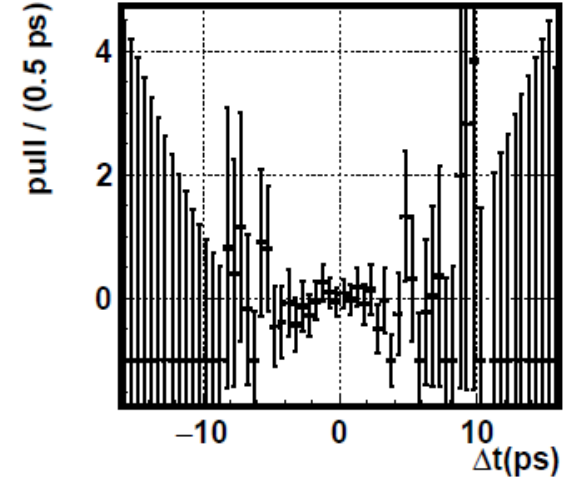
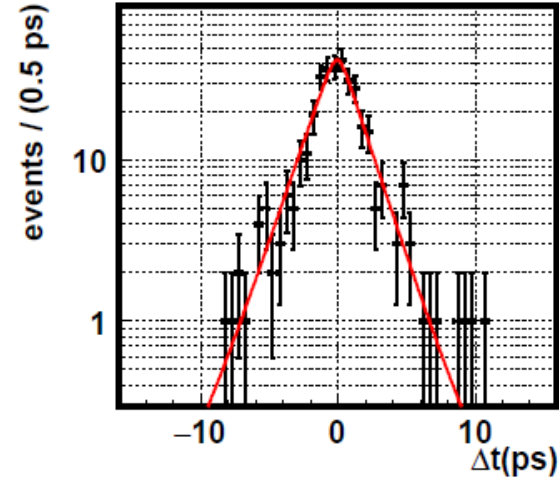


# CP fitting – lifetime measurement

MC



Data



- Using 1M signal MC with input  $\tau_B$  is 1.5367
  - Fitting result:  $1.5461 \pm 0.0072$  ps
  - Difference (fitting result - input) : 0.0106 ps

- Data result
  - Fitting result:  $1.4271 \pm 0.1129$  ps
  - PDG value ( $1.520 \pm 0.004$  ps)

✓ The result of lifetime fitting is consistent with PDG value