Holographic superconductors from M5-branes

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Nakwoo Kim (Physics Department Kyung HiHolographic superconductors from M5-brane

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Plan

- 1 Introduction and Summary
- 2 Consistent truncations
- 8 Holographic superconductivity
- 4 N = 2, D = 4 supergravity from M5-branes
- 6 Discussion
- Based on

J. Gauntlett, A. Donos (Imperial College London), NK, O. Varela (AEI Potsdam), to appear soon.

Principle of Holography

- AdS/CFT correspondence: proposed in 1997, and has been successfully applied to *D* = 4 SYMs, and others (like AdS/QCD)
- A *d*-dimensional strongly-coupled field theory is equivalent to a weakly coupled (classical) gravity system in *d* + 1-dimensions
- Might be applicable to any strongly coupled quantum field theory?

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AdS/CMT

- We'd like to apply the holographic principle to condensed matter physics, like superconductivity.
- CMT is, unlike quantum gravity, amenable to (table-top) experiments. Then we can test the idea of holography.

Superconductivity

- First discovered in 1911 by Onnes.
- Resistivity drops to zero at low temperature.
- Meissner effect: Magnetic fields are repeled by superconductor.



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Theory of superconductivity

- Landau, Ginzburg (1950), Bardeen, Cooper, Schrieffer (1957)
- Cooper pairs : electrons bound through exchange of phonons
- Mass gap through spontaneous symmetry breaking: No scattering, so no dissipation.
- Superfluid of Cooper pairs

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Holographic superconductor?

- Gubser, 0801.2977; Hartnoll, Herzog, Horowitz, 0803.3295, 0810.1563 etc.
- For a phenomenological description, one needs minimally a D = 4 classical AdS gravity with a massless gauge field and a charged scalar.
 - On CFT side, global U(1) symmetry and an operator with nonzero charge.
 - One looks for a charged black hole with scalar hair: Holographic version of spontaneous symmetry breaking.

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• Usually, charged particles pair-created at horizon either falls into BH, or escapes to infinity.

Within AdS, the negative c.c. gives extra attraction and the charged particle can form a cloud near the horizon.

• We will make use of a generalization of Breitenlohner-Freedman bound, in a charged BH background.

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SC from M5-branes

- M5-branes are solitonic objects of M-theory (11d unification of string theories)
- Can lead to lower-dim theories through wrapping and/or intersecting.
- We considered a supersymmetric configuration of M5-branes wrapping SLAG 3-cycle (preserves SUSY and guarantees stability) and discovered there is a scalar field leading to holographic superconductivity.

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Top-down models of hol. superconductor

- We want a *D* = 4 model which captures exact string/M-theory solutions behind it.
- CONSISTENT TRUNCATION: If a lower-dim supergravity is a consistent truncation of D = 10/11 supergravity, we can construct exact higher-dim solutions for any lower-dim model solution.

Consistent truncations: Maximal susy

- For example: Maximal gauged supergravity in D = 4/5/7 are shown/believed to be consistent truncations of D = 11/10(IIB)/11 supergravity.
- For $AdS_7 \times S^4$, see Nastase, Vaman, van Nieuwenhuizen (1999)
 - For example N = 8, D = 4 gauged supergravity has $35_v + 35_s$ scalar fields.
 - Too many fields and we need a further consistent truncations, for practical reasons.

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Consistent truncations involving Sasaki-Einstein spaces

- See J.Gauntlett, S.Kim, O.Varela, D.Waldram, 0901.0676; Cassani, Dall'Agata, Faedo, 1003.4283; Liu, Szepietowski, Zhao, 1003.5374; Gauntlett, Varela, 1003.5642
- D = 11 sugra ansatz: around $AdS_4 \times SE_7$ solutions.

$$ds^{2} = ds_{4}^{2} + e^{2U}(KE_{6}) + e^{2V}(\eta + A_{1})^{2}$$

$$G_{4} = 6e^{-6U-V}(1 + h^{2} + |\chi|^{2})vol_{4} + H_{3} \wedge (\eta + A_{1}) + H_{2} \wedge J$$

$$+ dh \wedge J \wedge (\eta + A_{1}) + 2hJ \wedge J$$

$$+ \sqrt{3}(\chi(\eta + A_{1}) \wedge \Omega - \frac{i}{4}D\chi \wedge \Omega + c.c.)$$

N = 2 supergravity from Sasaki-Einstein 7-manifolds

D = 4 fields: metric, massless vector A₁, real scalars U, V, h, one complex scalar χ, p-form field strength H_p for p = 2,3:

N = 2 gravity, a vector and a hypermultiplet.

- Exhibits superconductivity at skew-whiffed vacuum. (J. Gauntlett, J. Sonner, T. Wiseman 2009)
- Universal subsector of any Sasaki-Einstein.

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Crash course on Hol. Superconductors

- See e.g. Denef and Hartnoll, 0901.1160
- Minimally, we need AdS gravity, a Maxwell field and at least one charged field which will spontaneously break U(1).

$$L = \frac{M^2}{2}R + \frac{3M^2}{L^2} - \frac{1}{4g^2}F_{\mu\nu}F^{\mu\nu} - |\nabla\phi - iqA\phi|^2 - m^2|\phi|^2$$

- Planck mass M, AdS_4 radius L, gauge coupling g, scalar field ϕ with mass m and charge q.
- In supergravity, we usually have a number of charged fields. Can be tachyonic, but always above the Breitenlohner-Freedman bound around a supersymmetric vacuum.

• For
$$AdS_{d+1}$$
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Cont'd: Hol. Superconductor

• Standard AdS/CFT dictionary relates a CFT operator with a bulk scalar field. For AdS₄/CFT₃,

$$\Delta(\Delta-3)=(mL)^2$$

- BF bound makes sure Δ is non-negative.
- Superconductivity occurs when the RN AdS black is unstable to condensation of $\phi.$

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* Within AdS, the negative c.c. gives extra attraction and the charged particle can form a cloud near the horizon.

- From the gauge coupling, $g^{tt}q^2A_t^2$ gives extra (negative) mass \rightarrow Higher BF bound.
- In the near horizon limit, we have AdS_2 instead of AdS_4 . Again, more stringent stability bound.

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Bound for Holographic Superconductivity

- From Denef and Hartnoll, 0901.1160
- One solves the equation for charged scalar field in AdS RN background and look for threshold unstable mode.
- With $\gamma^2 = 2g^2(ML)^2$, we have instability (Hol. SC) if

$$q^2\gamma^2 \ge 3 + 2\Delta(\Delta - 3)$$

Maximal gauged supergravity in D = 7

- M-theory compactified on S^4 . The susy vacuum corresponds to $AdS_7 \times S^4$. M5-brane geometry.
- SL(5, R) global symmetry, SO(5) is gauged.
 - Scalar manifold: SL(5, R)/SO(5) and 14 scalars 14
 - SO(5) gauge group, 10 vector fields $10 \times (7-2) = 50$
 - Five 3-form fields $5 \times (5 \cdot 4 \cdot 3/3 \cdot 2) = 50$
 - Metric $5 \cdot 6/2 1 = 14$
- Known to be a consistent truncation of D = 11 supergravity. (Nastase, Vaman, van Nieuwenhuizen 1999)

SUSY of SLAG cycles

- SUSY cycles are subspace of special holonomy manifolds.
- They do not have special holonomy in general, but when branes are wrapped around them some fraction of susy is preserved.
 - In Math, they are called calibrated.
 - Roughly speaking, the nontrivial spin connection is cancelled by gauge connection (physically this is from the curvature of transverse space within the special holonomy manifold)
- For SLAG *p*-cycle,

Spin connection $SO(p) \leftrightarrow$ Gauge connection SO(p)

- M5-brane has SO(5) global symmetry from 5d transverse space.
- *SO*(3) spin-connections should be cancelled by turning on the bulk gauge fields in supergravity
 - SLAG 3-cycle in CY3 (1/4-BPS) $SO(5) \rightarrow SO(3)$
 - Associative 3-cycle in G_2 manifold (1/8-BPS): $SO(5) \rightarrow SO(4) \approx SU(2) \times SU(2)$
- In the near-horizon limit, the D = 4 theories have N = 2 and N = 1 supersymmetry, respectively.

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D = 7 supergravity

• SL(5,R) matrix T, SO(5) gauge field strength $F_{(2)}^{ij}$, 3-form fields $S_{(3)}^{i}$.

$$\mathcal{L}_{7} = R * \mathbf{1} - \frac{1}{4} T_{ij}^{-1} * DT_{jk} \wedge T_{k\ell}^{-1} DT_{\ell i} - \frac{1}{4} T_{ik}^{-1} T_{j\ell}^{-1} * F_{(2)}^{ij} \wedge F_{(2)}^{k\ell}$$

$$- \frac{1}{2} T_{ij} * S_{(3)}^{i} \wedge S_{(3)}^{j} + \frac{1}{2g} S_{(3)}^{i} \wedge DS_{(3)}^{i} - \frac{1}{8g} \epsilon_{ij_{1}\cdots j_{4}} S_{(3)}^{i} \wedge F_{(2)}^{j_{1}j_{2}} \wedge F_{(2)}^{j_{3}j_{4}}$$

$$+ \frac{1}{g} \Omega_{(7)} - V * \mathbf{1},$$

• Scalar potential $V = \frac{g^2}{2} (2T_{ij}T_{ij} - (T_{ii})^2)$

•
$$\delta\Omega_{(7)} = \frac{3}{4} \delta^{klmn}_{ijpq} F^{ij} \wedge F^{kl} \wedge F^{mn} \wedge \delta A^{pq}$$

M5 on SLAG3 (or 3 in 6)

Metric ansatz

$$ds_7^2 = ds_4^2 + ds^2(\Sigma_3)$$

with $\Sigma_3 = S^3$ or H^3 .

• Break $SO(5) \rightarrow SO(3)$, and identify the gauge connection with spin connection on Σ_3 .

•
$$a, b = 1, 2, 3, \alpha, \beta = 4, 5$$

$$A^{ab} = \frac{1}{g}\omega^{ab}$$
, others vanish

•
$$T = \text{diag}(e^{-4\lambda}, e^{-4\lambda}, e^{-4\lambda}, e^{6\lambda}, e^{6\lambda})$$

• Allows a fixed point for $\Sigma_3 = H^3$: $AdS_4 \times H^3/\Gamma$ solution

Fluctuations and a bigger truncated set

- Allow all fields consistent with $SO(5) \rightarrow SO(3)$ breaking.
 - From metric, we have D = 4 metric and a scalar (breathing mode).

$$ds_7^2 = e^{-6\phi} ds_4^2 + e^{4\phi} ds^2 (\Sigma_3)$$

• Gauge fields: real scalar β , complex scalar θ , graviphoton A_1 .

$$\begin{aligned} A^{ab}_{(1)} &= \frac{1}{g} \bar{\omega}^{ab} + \beta \epsilon_{abc} \, \bar{e}^{c} \\ A^{aa}_{(1)} &= -A^{\alpha a} = \theta^{\alpha} \bar{e}^{a} \\ A^{\alpha\beta}_{(1)} &= \epsilon^{\alpha\beta} A_{1} \end{aligned}$$

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Dimensional reduction cont'd

• 3-form fields: 2-form B_2 , 1-form C_1 , complex 3-form h_3 , complex scalar χ

$$S^{a}_{(3)} = B_{2} \wedge \bar{e}^{a} + C_{1} \wedge \epsilon_{abc} \bar{e}^{b} \wedge \bar{e}^{c}$$

$$S^{a}_{(3)} = h_{3}^{a} + \chi^{a} \operatorname{vol}(\Sigma_{3})$$

• From scalars T, we have a charged scalar \mathcal{N} .

$$T_{ab} = e^{-4\lambda} \delta_{ab}$$
, $T_{a\alpha} = 0$, $T_{\alpha\beta} = e^{6\lambda} \mathcal{N}_{\alpha\beta}$

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Counting of the modes

- Metric, graviphoton A₁ should make sugra multiplet.
- 10 scalars ϕ , λ , $\mathcal{N}_{\alpha\beta}$, β , θ_{α} , B_2 , χ_{α}
- 1 (massive) vector C₁
- h_3 is non-dynamical.
- In total, we have 2 hypers and 1 massive vector multiplet.

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Scalar potential

$$V = -g^{2} \Big\{ 3le^{-10\phi} - \frac{3}{8}e^{8\lambda - 14\phi} (l - 2\beta^{2} - 2\theta^{T}\theta)^{2} \\ + \frac{1}{2}e^{-6\phi} \Big[3e^{-8\lambda} + e^{12\lambda} [(\operatorname{Tr}\mathcal{N})^{2} - 2\operatorname{Tr}(\mathcal{N}\mathcal{N})] + 6e^{2\lambda}\operatorname{Tr}\mathcal{N} \Big] \\ - \frac{3}{2}e^{-10\phi} \Big[e^{10\lambda} (\theta^{T}\mathcal{N}\theta) - 2\theta^{T}\theta + e^{-10\lambda} (\theta^{T}\mathcal{N}^{-1}\theta) \Big] \\ - 6e^{-2\lambda - 14\phi}\beta^{2} (\theta^{T}\mathcal{N}^{-1}\theta) - \frac{1}{2g^{2}}e^{6\lambda - 18\phi} (\chi^{T}\mathcal{N}\chi) \Big\}$$

* $l = \pm 1$ is the sign of scalar curvature for Σ_3

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Vacua

SUSY vacuum

- With l = -1, $e^{-20\phi} = e^{10\lambda} = 2$.
- AdS radius $g^2 R^2 = 2$.
- ϕ , λ with masses $M^2 R^2 = 3 \pm \sqrt{17}$.
- β with $M^2 R^2 = 2$.
- χ, θ with $M^2 R^2 = 5$, $3/2 + \sqrt{17}/2$.
- \mathcal{N} with $M^2 R^2 = 4$.
- NON-susy vacuum
 - With l = -1, $e^{-20\phi} = 486/625$, $e^{10\lambda} = 10$.
 - $g^2 R^2 = 5\sqrt{6}/9$.
 - Can also compute mass spectrum: all above the BF bound (in fact, no tachyons)

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Einstein-Maxwell sector and charged BH

• In the action, we have couplings like

$$-\frac{1}{2}e^{-12\lambda+6\phi}F_2\wedge *F_2-\frac{3}{2}e^{-4\lambda+2\phi}B_2\wedge *B_2-\frac{3gl}{2}B_2\wedge F_2+\cdots$$

• At the susy vacuum, if we set other fields to zero the eoms are reduced to

$$L = R + 3\sqrt{2}g^2 - \frac{1}{\sqrt{2}}F \wedge *F$$

which allows ordinary AdS RN black hole solutions.

• Then, do we have superconductivity?

Unstable mode

- We have charged scalars $\chi, \theta, \mathcal{N}$.
- Would like to use DH bound: For us, $M_{DH}^2 = 2$, $g_{DH}^2 = 1/\sqrt{2}$, $L_{DH}^2 = R^2$, $\gamma_{DH}^2 = 2\sqrt{2}R^2$.
- For χ , θ , $q_{DH} = g$ DH bound requires $M^2 R^2 \le 1/2$. They are too massive and do not destabilze the RN BH.
- For N, $q_{DH} = 2g$ and DH bound requires $M^2 R^2 \le 13/2$. With $M^2 R^2 = 4$, they lead to spontaneous symmetry breaking and superconductivity!

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Discussion

- Things to do now
 - Compute transport coefficients
 - Draw the phase diagram: Temperature vs. Condensates
 - Find the Lifshitz-like (anisotropic) solution.
 - etc...

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