### Exotic Branes, Double Bubbles, & Superstrata

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#### Introduction

#### "Forgotten" branes in string theory

[9707217 Elitzur+Giveon+Kutasov+Rabinovici] [9712047 Blau+O'Loughlin] [9809039 Obers+Pioline]

Type IIA	P (7), F1 (7), D0 (1), D2 (21), D4 (35), D6 (7),
	NS5 (21), KKM (42), $5_2^2$ (21), $0_3^7$ (1), $2_3^5$ (21),
	$4_3^2$ (35), $6_3^1$ (7), $0_4^{(1,6)}$ (7), $1_4^6$ (7)
Type IIB	P (7), F1 (7), D1 (7), D3 (35), D5 (21), D7 (1),
	NS5 (21), KKM (42) , $5_2^2$ (21), $1_3^6$ (7), $3_3^4$ (35),
	$5^2_3 \ ({f 21}), \ 7_3 \ ({f 1}), \ 0^{(1,6)}_4 \ ({f 7}), \ 1^6_4 \ ({f 7})$
M-theory	P (8), M2 (28), M5 (56), KKM (56),
	$5^3$ (56), $2^6$ (28), $0^{(1,7)}$ (8)

#### "Forgotten" branes in string theory



"Forgotten" branes in string theory

Co-dimension 2

Charge = U-duality monodromy

Jump by a U-duality as one goes around it

Generalization of F-theory 7-branes

"Forgotten" branes in string theory

Co-dimension 2



### Supertube effect – "bubbling"

- Codim-2 object problematic?
  - Log divergences

 $V \sim \frac{1}{r^{d-2}} \longrightarrow V \sim \log\left(\frac{\mu}{r}\right)$ 

Supertube effect = spontaneous polarization



### Exotic bubbling

#### Ordinary branes can puff up to produce exotic dipole charges



- $\rightarrow$  No log divergence
- Exotic branes relevant to non-exotic physics; More common than previously thought!

### Double bubbling

#### Bubbling can occur at multiple stages



- $\rightarrow$  "Superstratum" arbitrary surface
- Bubbling may occur repeatedly, producing all kinds of exotic charges

### Black hole microstates

- Black holes: bound states of branes
  - $\rightarrow$  Generic microstates involve exotic superstrata
  - Microstate (non-)geometries?



## Claim:

Generic microstates of black holes involve exotic non-geometric superstrata.

### Outline

- Introduction  $\checkmark$
- Exotic states & their higher-D origin
- Supertube effect
- Black hole microstates
- Conclusion

Exotic states and their higher-D origin

### Compactification to 3D

- ▶ M on T<sup>8</sup> or Type II on T<sup>7</sup>
  - $\rightarrow$  3D  $\mathcal{N} = 16$  sugra
  - $\rightarrow$  U-duality group  $E_{8(8)}(\mathbb{Z})$  : generated by T- and S-dualities
  - → 128 moduli scalars (in 3D, scalar = vector)  $\in$  SO(16)\ $E_{8(8)}(\mathbb{R})/E_{8(8)}(\mathbb{Z})$

#### Particle multiplet:

ightarrow Start from a point-like object

e.g. D7(3456789) wrapped on  $T^7$ 

 $\rightarrow$  Take T- and S-dualities to get other states

### Exotic states in 3D

Particle multiplet:

[9707217 Elitzur+Giveon+Kutasov+Rabinovici] [9712047 Blau+O'Loughlin] [9809039 Obers+Pioline]

Type IIA	P (7), F1 (7), D0 (1), D2 (21), D4 (35), D6 (7),
	NS5 (21), KKM (42), $5_2^2$ (21), $0_3^7$ (1), $2_3^5$ (21),
	$4_3^2 \ ({f 35}), \ 6_3^1 \ ({f 7}), \ 0_4^{(1,6)} \ ({f 7}), \ 1_4^6 \ ({f 7})$
Type IIB	P (7), F1 (7), D1 (7), D3 (35), D5 (21), D7 (1),
	NS5 (21), KKM (42) , $5_2^2$ (21), $1_3^6$ (7), $3_3^4$ (35),
	$5_3^2 \ ({f 21}),  7_3 \ ({f 1}),  0_4^{(1,6)} \ ({f 7}),  1_4^6 \ ({f 7})$
M-theory	P (8), M2 (28), M5 (56), KKM (56),
	$5^3$ (56), $2^6$ (28), $0^{(1,7)}$ (8)

Notation for exotic states

$$b_{n}^{C}: M = \frac{R^{b}(R^{c})^{2}}{g_{s}^{n}} \qquad b_{n}^{(d,c)}: M = \frac{R^{b}(R^{c})^{2}(R^{d})^{3}}{g_{s}^{n}}$$
  
Example: 5<sup>2</sup><sub>2</sub>(34567,89):  $M = \frac{R_{3} \cdots R_{7} (R_{8}R_{9})^{2}}{g_{s}^{2} l_{s}^{8}}$ 

### Duality rules

Duality rules can be read off from:

$$T_{y}: R_{y} \to \frac{l_{2}^{2}}{R_{y}}, g_{s} \to \frac{l_{s}}{R_{y}}g_{s} \qquad S: g_{s} \to \frac{1}{g_{s}}, l_{s} \to g_{s}^{1/2}l_{s}$$

• Example:

NS5(34567)  $\xrightarrow{T_8}$  KKM(34567,8)  $\xrightarrow{T_9}$  5<sup>2</sup><sub>2</sub>(34567,89)

$$M = \frac{R_3 \cdots R_7}{g_s^2 l_s^6} \xrightarrow{\mathsf{T}_8} \frac{R_3 \cdots R_7}{(g_s l_s / R_8)^2 l_s^6} = \frac{R_3 \cdots R_7 R_8^2}{g_s^2 l_s^8} : \mathsf{5}_2^1 = \mathsf{KKM}$$
$$\xrightarrow{\mathsf{T}_9} \frac{R_3 \cdots R_7 R_8^2}{(g_s l_s / R_9)^2 l_s^8} = \frac{R_3 \cdots R_7 (R_8 R_9)^2}{g_s^2 l_s^{10}} : \mathsf{5}_2^2$$

### Higher D origin = U-folds (1)

- Claim: higher D origin is
   U-fold = non-geometric background
- E.g. D7 on  $T^7$ 
  - (Magnetically) coupled to RR 0-form C<sub>0</sub>
  - 3D scalar  $\phi = C_0$
  - Monodromy:  $\phi \rightarrow \phi + 1$  shift (part of  $SL(2, \mathbb{Z})$  duality of IIB)



### Higher D origin = U-folds (2)

 $\bullet \phi$  gets combined with other scalars to form moduli matrix

 $M \in \mathcal{M} = SO(16) \setminus E_{8(8)}(\mathbb{R}) / E_{8(8)}(\mathbb{Z})$ 

- Shifting symmetry + S, T-dualities  $\longrightarrow E_{8(8)}(\mathbb{Z})$
- Can consider a particle with general U-duality monodromy  $q \in E_{8(8)}(\mathbb{Z}) \equiv G(\mathbb{Z})$



"Charge" of a 3D particle is U-duality monodromy around it!

### Higher D origin = U-folds (3)

In IOD/IID, we have a non-geometric U-fold



#### <u>Cf.</u> F-theory, U-branes & non-geom bg

[Greene+Shapere+Vafa+Yau] [Vafa] F-theory [Kumar+Vafa] [Liu+Minasian] [Hellerman+McGreevy+Williams] contractible U-branes [Dabholkar+Hull] [Flournoy+Wecht+Williams] ... non-contractible U-branes & moduli stabl'n

### Sugra solution for $5^2_2$

#### 5<sup>2</sup><sub>2</sub>(56789,34) metric:

$$\begin{split} ds^2 &= -dt^2 + H(dr^2 + r^2d\theta^2) + HK^{-1}dx_{34}^2 + dx_{56789}^2 \\ B_{34} &= -K^{-1}\theta\sigma, \qquad e^{2\Phi} = HK^{-1}, \qquad K \equiv H^2 + \sigma^2\theta^2 \end{split}$$

 $r, \theta: \mathbb{R}^2$  $x^{3,4}: T^2$  $x^{5...9}: T^6$ 

$$H(r) = h + \sigma \log\left(\frac{\mu}{r}\right)$$
  $\sigma = \frac{R_3 R_4}{2\pi \alpha'}$  Cf. [6]

Cf. [Blau+O'Loughlin]: 6<sup>1</sup><sub>3</sub>

T-fold structure:

$$\theta = 0: G_{33} = G_{44} = H^{-1},$$
  
 $\theta = 2\pi: G_{33} = G_{44} = \frac{H}{H^2 + (2\pi\sigma)^2}$ 

 $\rightarrow x_3$ - $x_4$  torus size doesn't come back to itself!

### T-fold structure of $5_2^2$

Package 3-4 part of G, B:

$$M = \begin{pmatrix} G^{-1} & G^{-1}B \\ -BG^{-1} & G - BG^{-1}B \end{pmatrix}$$

T-duality acts as

$$M \to M' = \Omega^t M \Omega, \qquad \Omega \in SO(2,2,\mathbb{R})$$

T-duality monodromy around  $5_2^2$ :

$$\Omega = \begin{pmatrix} 1 & 0 \\ 2\pi\sigma & 1 \end{pmatrix} : \qquad M(\theta = 0) \to M(\theta = 2\pi)$$



### Comments

Not well-defined as stand-alone objects

Log divergence

→ Superpositions (cf. F-theory 7-branes)

Origs with higher codims. (we turn to this next!)

Easy to get sugra metric for other exotic branes

• Questionable for states with  $M \sim g_s^{-3}$ ,  $g_s^{-4}$ 

### Lesson I:

# Exotic branes = Non-geometric U-folds

Supertube effect and exotic branes

### Supertube effect



- Spontaneous polarization effect (cf. Myers effect)
- Produces new dipole charge
- Cross section = arbitrary curve
- Fluctuations of curve  $\rightarrow$  large degeneracy  $\sim e^{\#\sqrt{N_{F1}N_{D0}}}$

### Dualizing supertubes

dualize!

Original supertube effect:

 $D0 + F1(1) \rightarrow D2(1\psi)$  •

Various other known puff-ups:

 $F1(1) + P(1) \rightarrow F1(\psi)$  FP sys  $D1(1) + D5(12345) \rightarrow KKM(2345\psi, 1)$  LM geom  $M2(12) + M2(34) \rightarrow M5(1234\psi)$  black ring

### "Exotic" supertubes



Exotic puff-up:  $D4(6789) + D4(4589) \rightarrow 5_2^2(4567\psi, 89)$ More exotic:  $D3(589) + NS5(46789) \rightarrow 5_3^2(4567\psi, 89)$ Still more exotic:  $NS5(46789) + KKM(46789,5) \rightarrow 1_4^6(\psi, 456789)$ 

Ordinary branes can polarize into exotic branes

• Only dipoles  $\rightarrow$  no log divergence

### Example: D4+D4 $\rightarrow$ 5<sup>2</sup><sub>2</sub>

Basic sugra supertube



### Metric for D4+D4 $\rightarrow$ 5<sup>2</sup><sub>2</sub>

#### $D4(6789)+D4(4589)\rightarrow 5_2^2(4567\psi, 89)$

$$ds^{2} = -\frac{1}{\sqrt{f_{1}f_{2}}}(dt - A)^{2} + \sqrt{f_{1}f_{5}} dx_{123}^{2} + \sqrt{\frac{f_{1}}{f_{2}}} dx_{45}^{2} + \sqrt{\frac{f_{2}}{f_{1}}} dx_{67}^{2} + \frac{\sqrt{f_{1}f_{2}}}{f_{1}f_{2} + \gamma^{2}} dx_{89}^{2},$$

$$f_{i}, A: \text{ sourced along curve}$$

$$f_{1} = 1 + \frac{Q_{1}}{L} \int_{0}^{L} \frac{dv}{|\vec{x} - \vec{F}(v)|}, \quad f_{2} = 1 + \frac{Q_{1}}{L} \int_{0}^{L} \frac{|\vec{F}(v)|^{2}}{|\vec{x} - \vec{F}(v)|} dv, \quad A_{i} = -\frac{Q_{1}}{L} \int_{0}^{L} \frac{\dot{F}_{i}(v)}{|\vec{x} - \vec{F}(v)|} dv = *_{3} dA, \quad d\beta_{I} = *_{3} df_{I}$$

$$\gamma, \beta_{i} \text{ have monodromy around curve}$$

$$\gamma \rightarrow \gamma - 2q, \quad \beta_{I} \rightarrow \beta_{I} - 2Q_{I} \rightarrow \text{T-fold structure}$$

$$just as before$$
Asymptotically flat 4D

### Metric for D4+D4 $\rightarrow$ 5<sup>2</sup><sub>2</sub>

Other fields:

$$e^{2\Phi} = \frac{\sqrt{f_1 f_2}}{f_1 f_2 + \gamma^2}, \quad B_{89}^{(2)} = \frac{\gamma}{f_1 f_2 + \gamma^2}, \quad C^{(3)} = -\gamma \rho + \sigma$$

 $\rho = (f_2^{-1} + dt - A) \wedge dx^4 \wedge dx^5 + (f_1^{-1} + dt - A) \wedge dx^6 \wedge dx^7$  $\sigma = (\beta_1 - \gamma dt) \wedge dx^4 \wedge dx^5 + (\beta_2 - \gamma dt) \wedge dx^6 \wedge dx^7$ 

### Lesson 2:

# Exotic branes are important for generic physics of string theory



# Exotic branes and black hole microstates

### Black hole microstates

#### BH has thermodynamic entropy



- Is a BH an ensemble? If so, where are microstates?
  - Not visible in gravity?
  - No-hair theorem in 4D Einstein gravity

### Mathur's fuzzball proposal

#### A BH is filled with stringy "fuzz"



No horizon No singularity

- BH microstates = different configurations of the fuzz
- BH entropy = stat. mech. entropy of the fuzz

$$S_{\rm BH} = \frac{A}{4G_N} \stackrel{?}{=} S_{\rm fuzz}$$

### Sugra microstates

Supersym. BHs



Microstates describable within sugra as smooth, horizonless solutions?

- 2-charge system: Successful [Lunin+Mathur] [Lunin+Maldacena+Maoz] [Rychkov]
  - All microstates have been constructed within sugra
  - Counting sugra sol'ns reproduces micro entropy:  $S_{sugra} = S_{micro}$
  - But horizon vanishes classically
- 3-charge system: Not so successful
  - Many sugra microstates have been constructed [Bena+Warner] [Berglund+Gimon+Levi]
  - Evidence that they are not enough [Bena+Bobev+Ruef+Warner]

They looked for *geometric* solutions in sugra and didn't find enough microstates.

But this seems just in accord with what we saw:

Generic BH microstates involve exotic charges and are non-geometric!

### "Single bubbling"

DI(5)

#### 2-charge system ("small" BH)



KKM(6789 $\psi$ ;5)



I-dim curve  $\in \mathbb{R}^4$ 

geometric microstates (Lunin-Mathur)

 $S_{\rm micro} = S_{\rm geom}$ 

### "Double bubbling" (1)

#### 3-charge system: 5D BH : Well studied for microstate geometry

M2(56) M2(78) M2(9A) M5(789A $\psi$ ) M5(569A $\psi$ ) M5(5678 $\psi$ )

arbitrary curve

"supertube"

cf. black ring

5<sup>3</sup>(789Aφ,56ψ) 5<sup>3</sup>(569Aφ,78ψ) 5<sup>3</sup>(5678φ,9Aψ)



arbitrary surface "superstratum"

non-geometric microstates

 $S_{\rm micro} \stackrel{?}{=} S_{\rm nongeom}$ 

### "Double bubbling" (2)

#### • 4-charge system: 4D BH : Well studied for microstate counting

[Maladacena+Strominger+Witten]



### Endless bubbling??



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### Susy in supertube [Bena+c

[Bena+de Boer+Warner+MS 1107.2650]



Preserves  $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4} \text{ susy}$ 

FI+D0

- Locally  $\frac{1}{2}$  BPS
- Which <sup>1</sup>/<sub>2</sub> is preserved
   depends on local orientation
- Common susy preserved = original <sup>1</sup>/<sub>4</sub> susy

This is why supertube can be along an arbitrary curve.

### Susy in superstratum



Preserves  $\frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{8}$  susy

- Locally  $\frac{1}{2}$  BPS
- Which <sup>1</sup>/<sub>2</sub> is preserved
   depends on local orientation
- Common susy preserved = original <sup>1</sup>/<sub>8</sub> susy

If true, superstratum can be along an arbitrary surface in principle!

### Example: F1-P $\rightarrow$ D2



### General formula for $1 \rightarrow 2$ puff-up

Projectors before puffing up:

$$\Pi_1 = \frac{1}{2}(1+P_1), \qquad \Pi_2 = \frac{1}{2}(1+P_2)$$

Projector after puffing up:



$$\Pi = \frac{1}{2} [1 + c^2 P_1 + s^2 P_2 - sc \Gamma^{0\psi} + sc \Gamma^{0\psi} P_1 P_2]$$
  
=  $c (c - s\Gamma^{0\psi}) \Pi_1 + s (s - c\Gamma^{0\psi}) \Pi_2 + 2sc \Gamma^{0\psi} \Pi_1 \Pi_2$ 

### D1-D5-P (1)



Original config.

Infinite straight supertube = tilted and boosted DI-D5

puffs up just like DI-D5 → KKM (LM geom.) Infinite straight superstratum

Special case; superstratum is purely geometric

### D1-D5-P (2)









$$\widehat{\Pi} = \frac{1}{2} (1 + s_4^2 \widehat{P}_1 + c_4^2 \widehat{P}_2 - s_4 c_4 \Gamma^{0\psi} + s_4 c_4 \Gamma^{0\psi} \widehat{P}_1 \widehat{P}_2)$$

Same 1/8 susy preserved

### Backreacted strata

- Dynamics of superstrata
  - Arbitrary surface possible?



- ► 6D sugra (DI-D5-P) [Gutowski+Martelli+Reall] [Cariglia+Mac Conamhna] [Bena+Giusto+Warner+MS | | 10.2781]
  - Linear problem, if solved in the right order
    - $\rightarrow$  Linearity was crucial for previous microstate solutions.
    - $\rightarrow x^5$ -dep 4D almost-HK base. Functions & forms on it.
  - Given superstratum data, should be possible to find solutions

### Geometric superstrum (1)

#### Double bubbling of DI-D5-P system



### Geometric superstrata

#### So far we could construct:



N strands of DI-P and D5-P supertube spirals along arbitrary curves  $\vec{F}^{(i)}$ , i = 1, ..., N

Next step: KKM dipole (work in progress)

# Lesson 3: Exotic branes are ingredients of BHs

#### Conclusions

### Conclusions

- Exotic branes = non-geometries (U-folds)
- Exotic charges = U-duality monodromies
- Relevant even for non-exotic physics by supertube effect

Exotic branes are not at all exotic; They are everywhere!

Essential ingredients of BHs

### Future directions

- Geometric superstrata
- Non-geometric superstrata
  - More generic
  - Locally geometric
  - Generalize susy sol'n ansatz
  - Generalized geometry, DFT

[Berman, Hohm, Hull, Perry, Zwiebach, ...]

# Conjecture:

Generic microstates of black holes involve non-geometric superstrata.



Thanks!