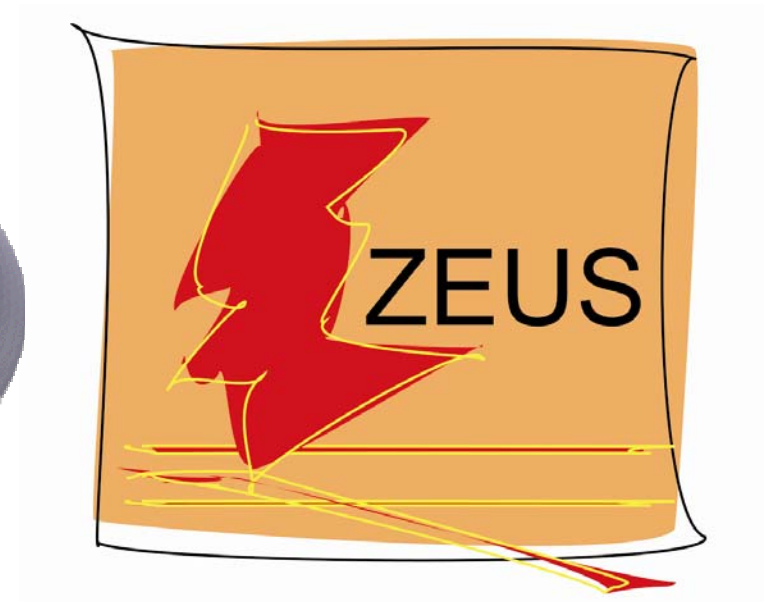


# Results on the proton structure from HERA

Shima Shimizu  
(Univ. of Tokyo)

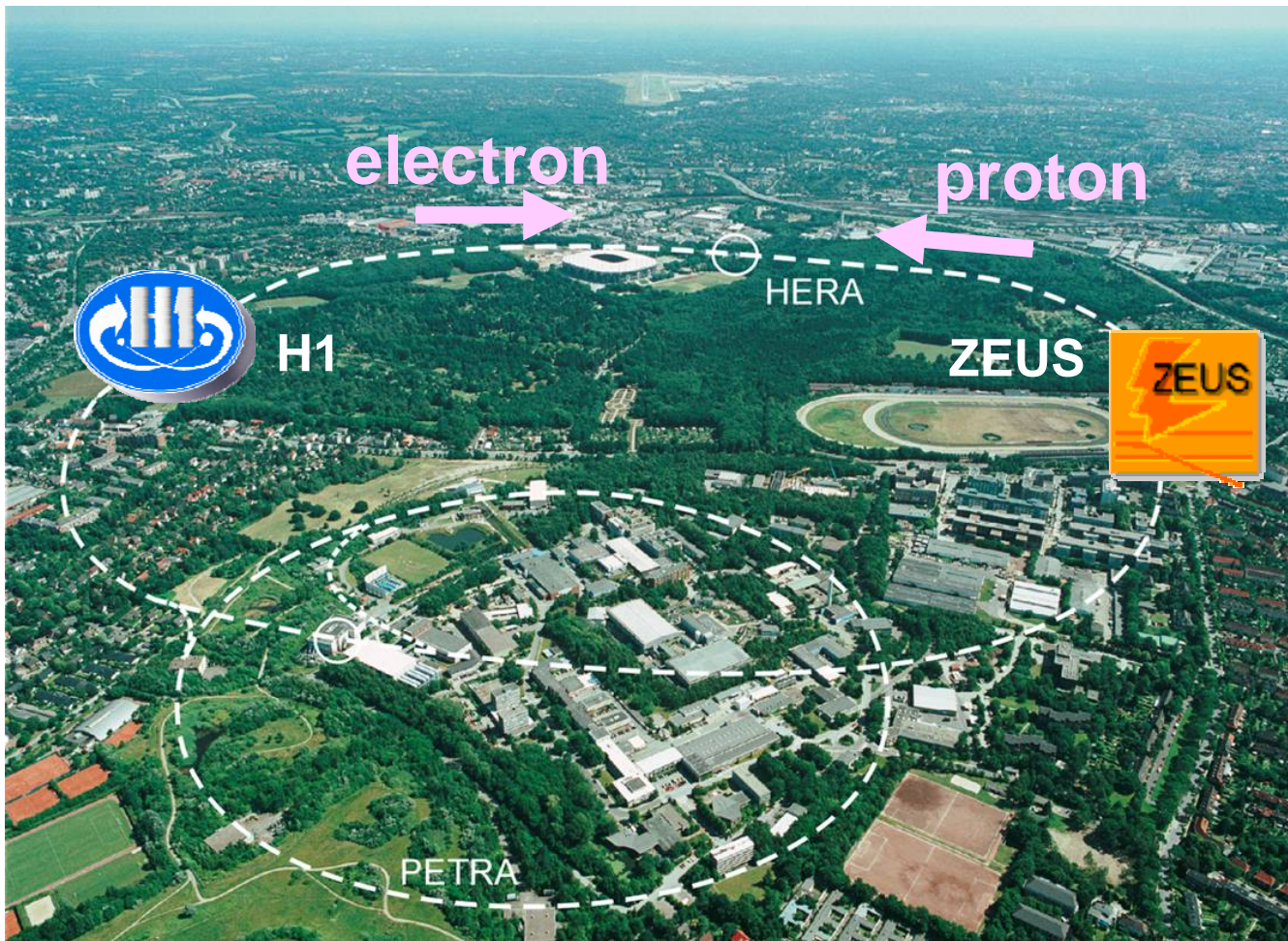


**Introduction**

HERA physics

Proton structure

# The world only e-p collider: HERA



A unique collider at  
DESY, Hamburg

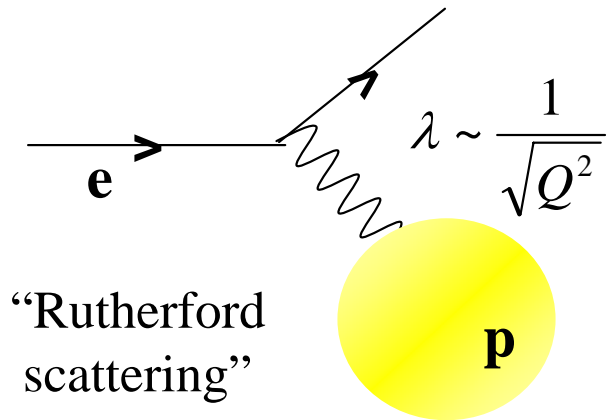
Circumference:  
6.3 km

Operated  
since 1992 to 2007

2 collider experiments:  
H1 & ZEUS

- ◆ proton 920 GeV
  - ◆ electron/positron 27.5 GeV
- center of mass energy  
 $\sqrt{s} = 318\text{GeV}$

# HERA looks into the proton

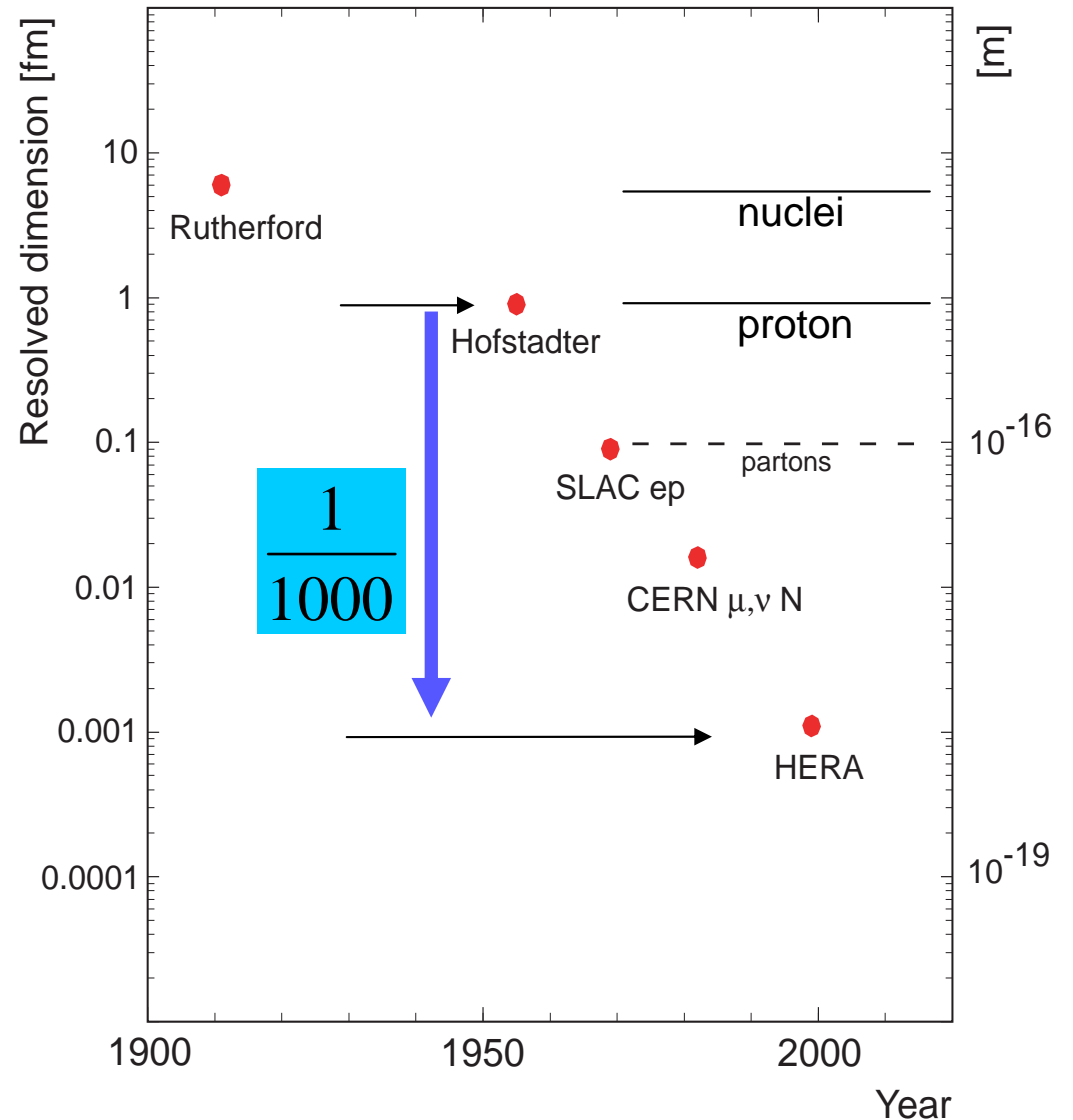


## Resolution @ HERA

$$\sqrt{s} = 318\text{GeV} \rightarrow s \sim 10^5 \text{GeV}^2$$

$$\lambda_{\text{min}} \sim \frac{1}{\sqrt{Q_{\text{max}}^2}} \sim 10^{-18} \text{m}$$

HERA can have a resolution of 1/1000 of proton size.



# Proton has a structure

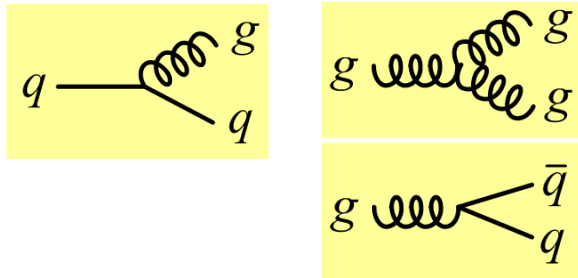
Proton has its subcomponents: **partons**

- ◆ Naive parton model
  - u u d quarks: **'valence'** quarks

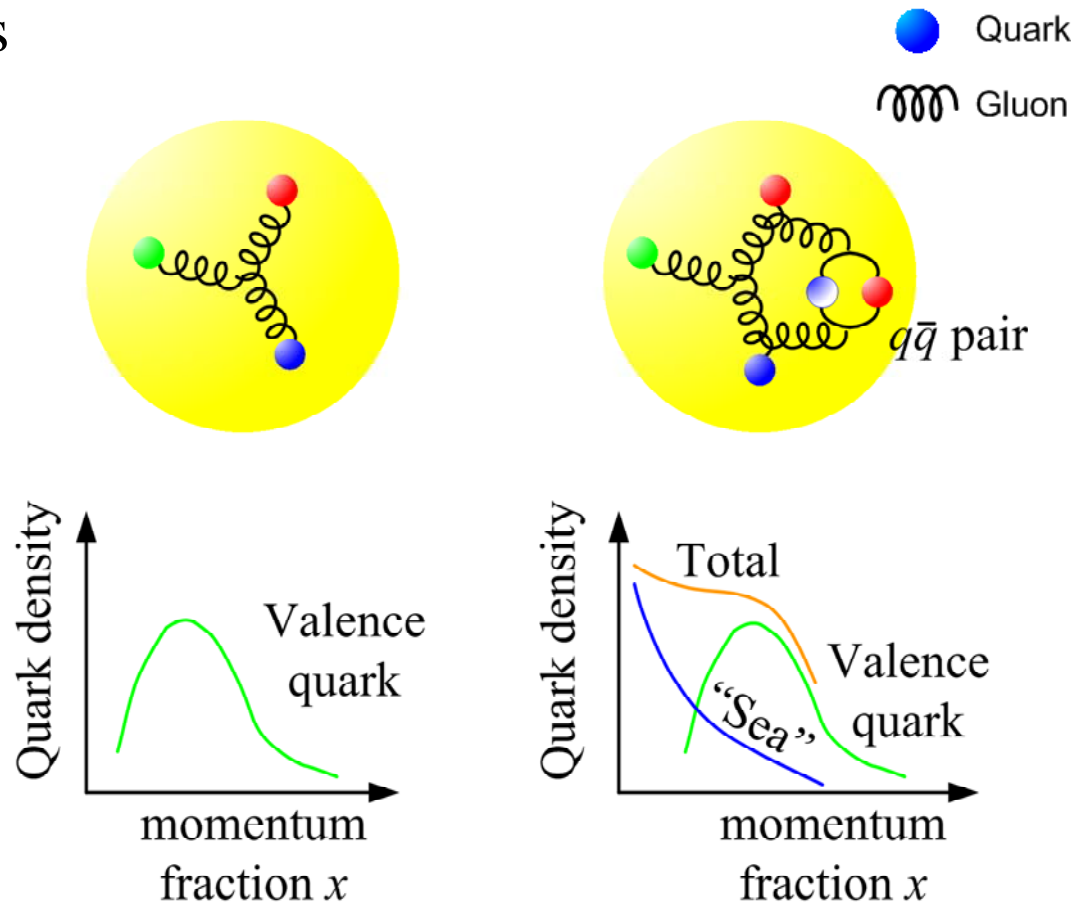
- ◆ QCD

quark emits gluon.

gluon splits to qq or gg.

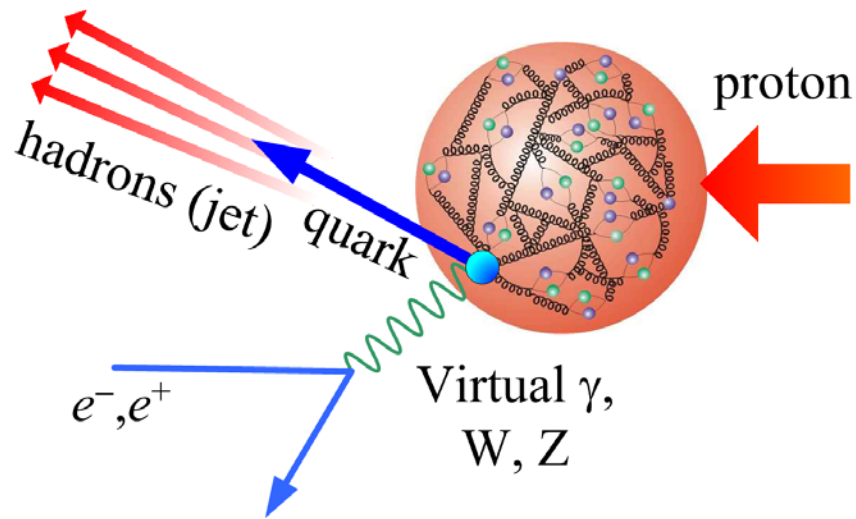


→ Many quarks with lower momentum: **'Sea'** quarks





# HERA looks into the proton



ep collision

→ scattering of electron and a quark.

It reflects the proton structure.

Cross section of ep scattering

= Cross section of eq scattering  $\otimes$  proton structure

Details come later, but;

$F_2$  : structure function  $\propto$  total charge-squared weighted number of quarks in the proton

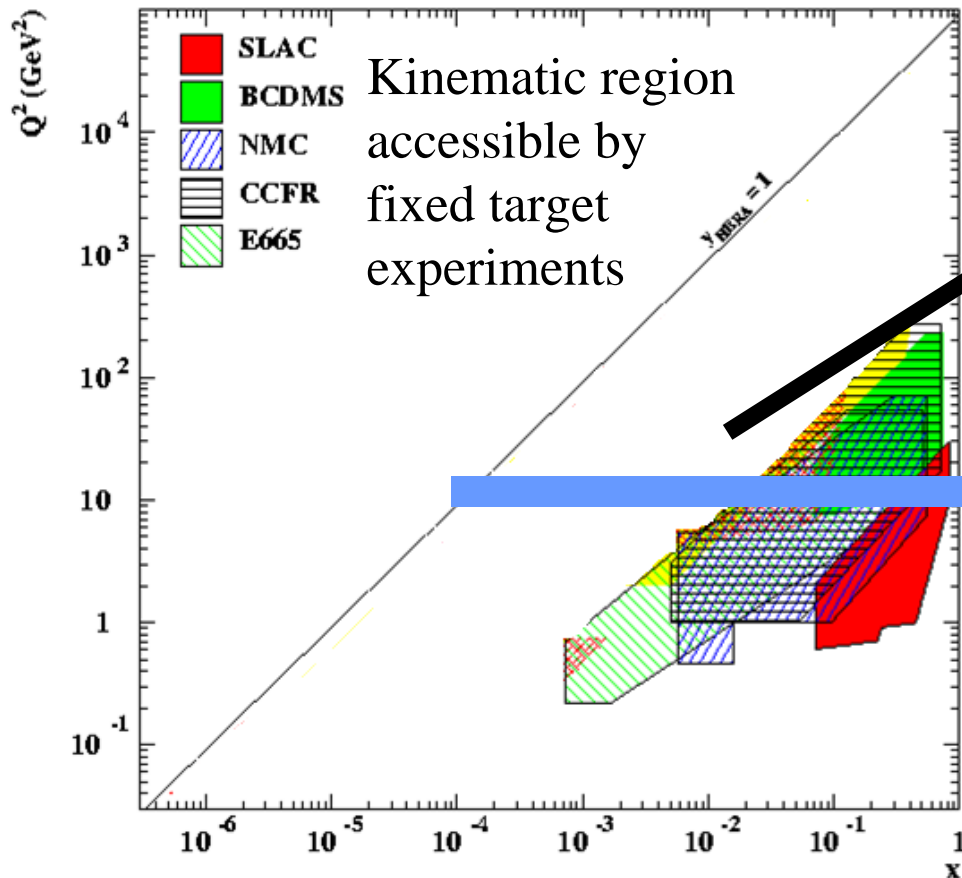
$Q^2$  : momentum transfer → resolution

$x$  : momentum fraction of a parton to the proton

# Before HERA

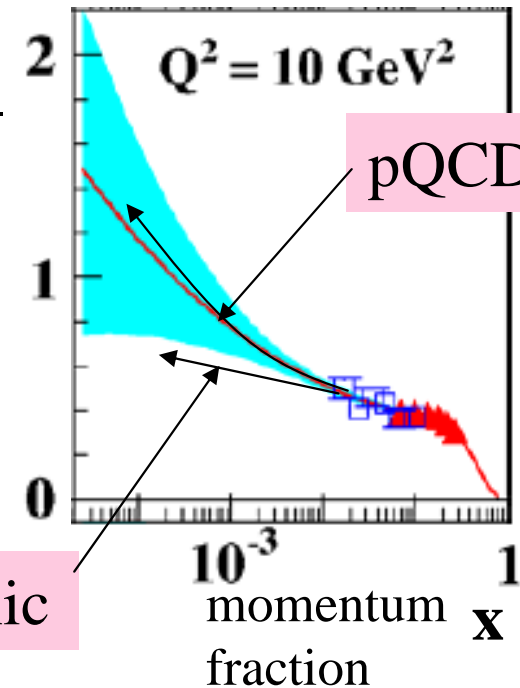
Fixed target experiments only.

- ◆ It was unclear how to describe the proton structure at low- $x$ .
  - perturbative QCD: quarks are asymptotically free.
  - hadronic view : partons are confined in the proton



momentum ( $x$ ) distribution of quarks at a certain resolution ( $Q^2=10\text{GeV}^2$ )

$F_2$   
total (charge-squared-weighted) number of quarks in the proton

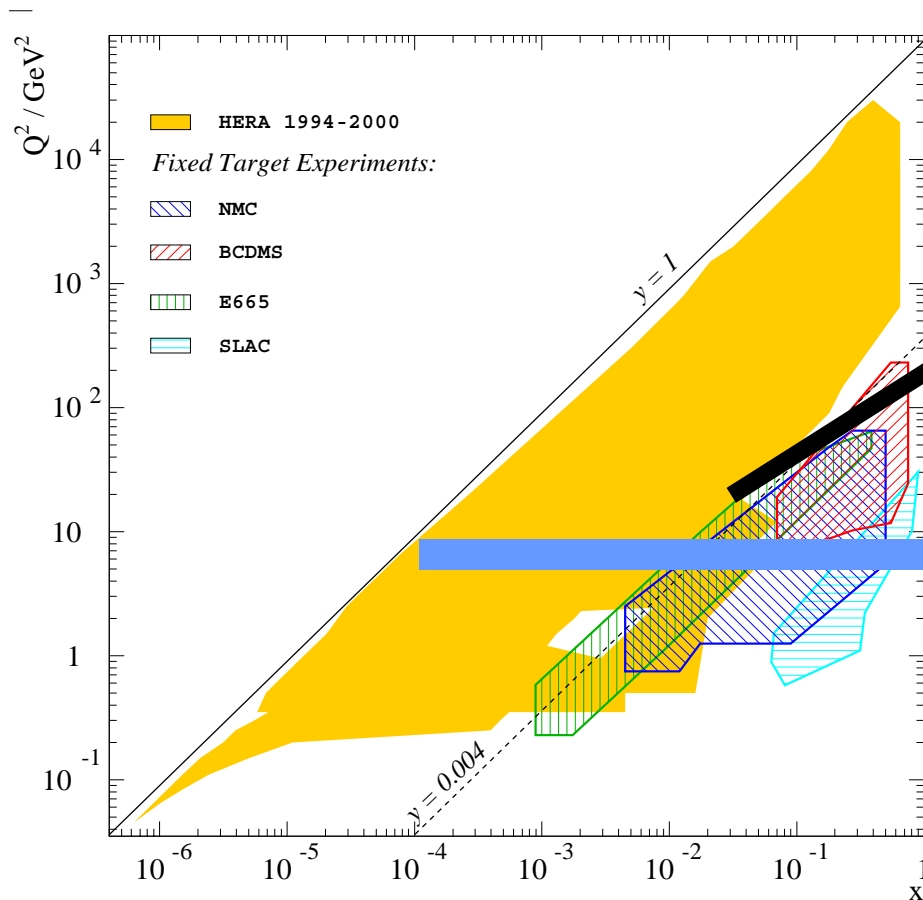


Hadronic

pQCD

# HERA opened the new kinematic region

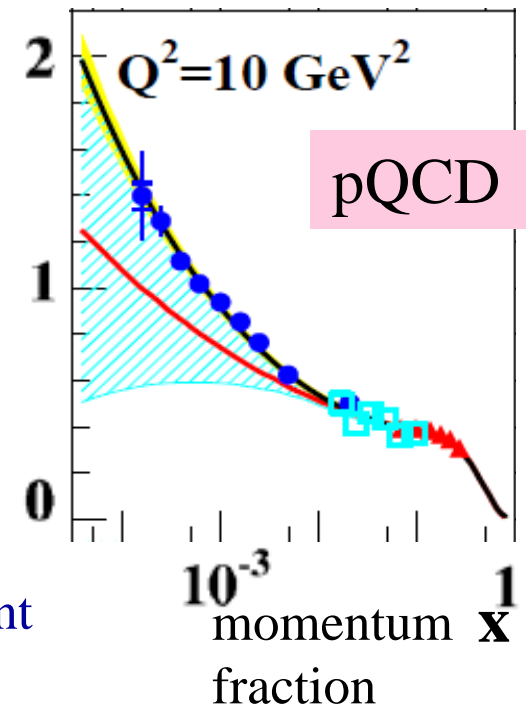
- ◆ HERA has expanded accessible kinematic region largely.
  - 2 orders in both  $x$  and  $Q^2$



With HERA data ...

$F_2$  total (charge-squared-weighted) number of quarks in the proton

• HERA measurement



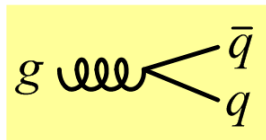
steep rise at low  $x$

→ pQCD descriptions is verified.



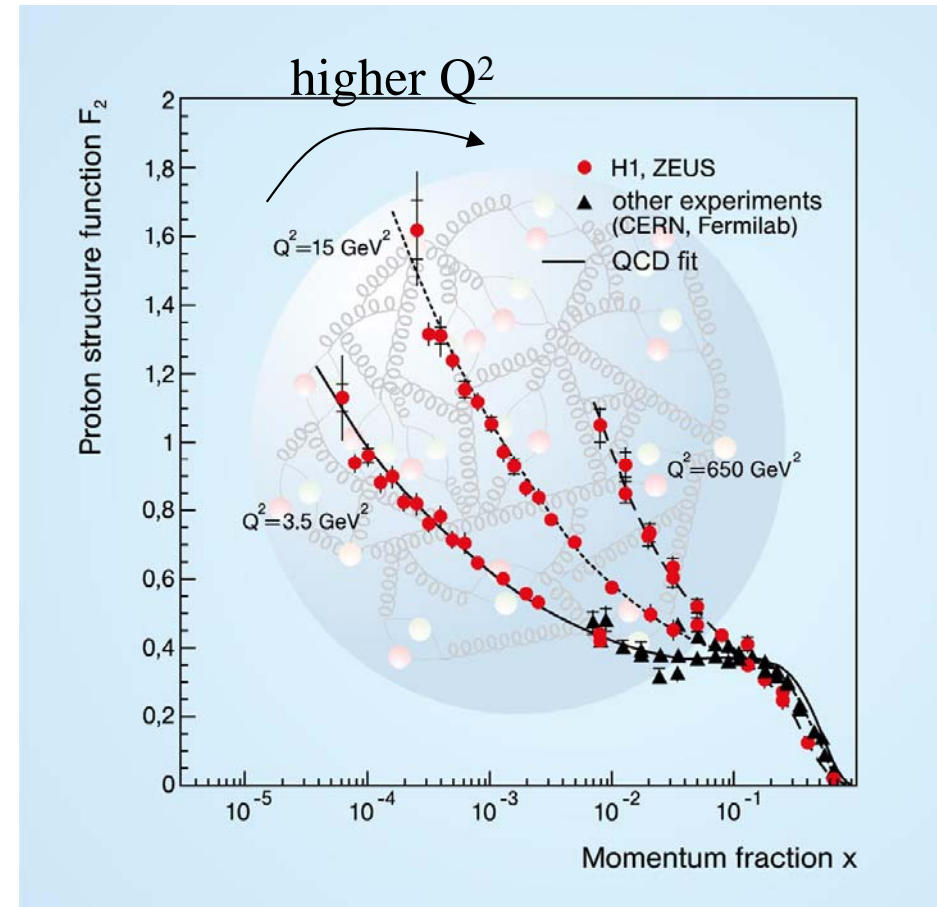
# Plenty of Gluon and Sea quarks

- ◆ Steep rise of  $F_2$  at low  $x$ .
- ◆ higher  $Q^2$  = finer resolution  
→ more low-momentum quarks are 'visible'  
i.e. Sea quarks
- ◆ Sea quarks are generated by gluon.



Abundant Sea quarks

⇔ Abundant gluons



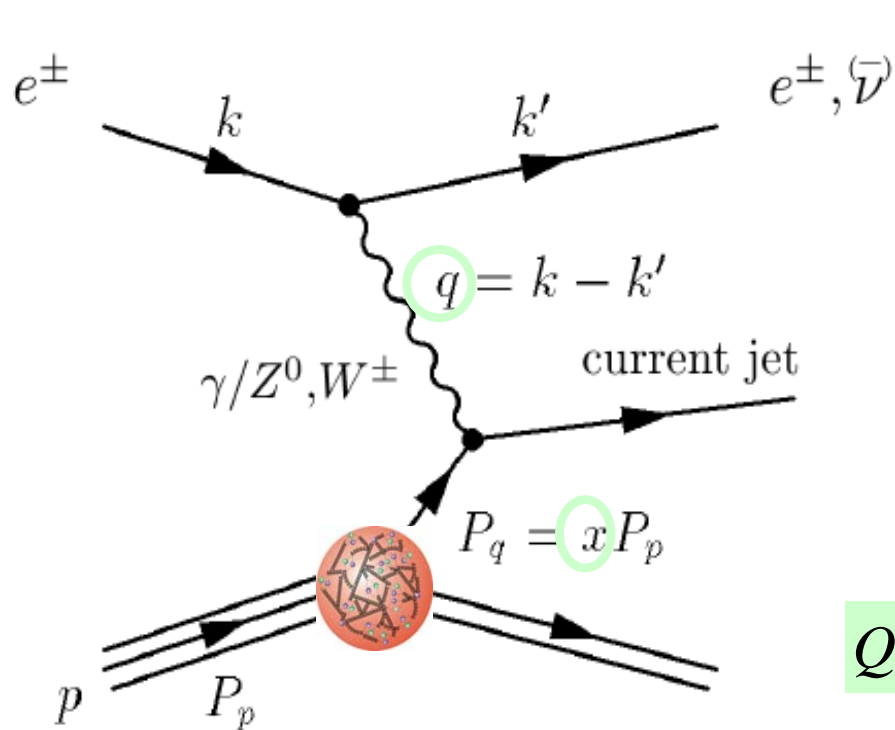
Gluon and Sea quarks' physics is started by HERA.

Introduction

**HERA physics**

Proton structure

# Deep Inelastic Scattering (DIS)



◆ Kinematic variables to describe DIS

$Q^2$ : Virtuality

→ probing power

$x$ : Bjorken scaling variable

→ momentum fraction of struck quark

$y$ : Inelasticity

$$Q^2 = -q^2 = -(k - k')^2$$

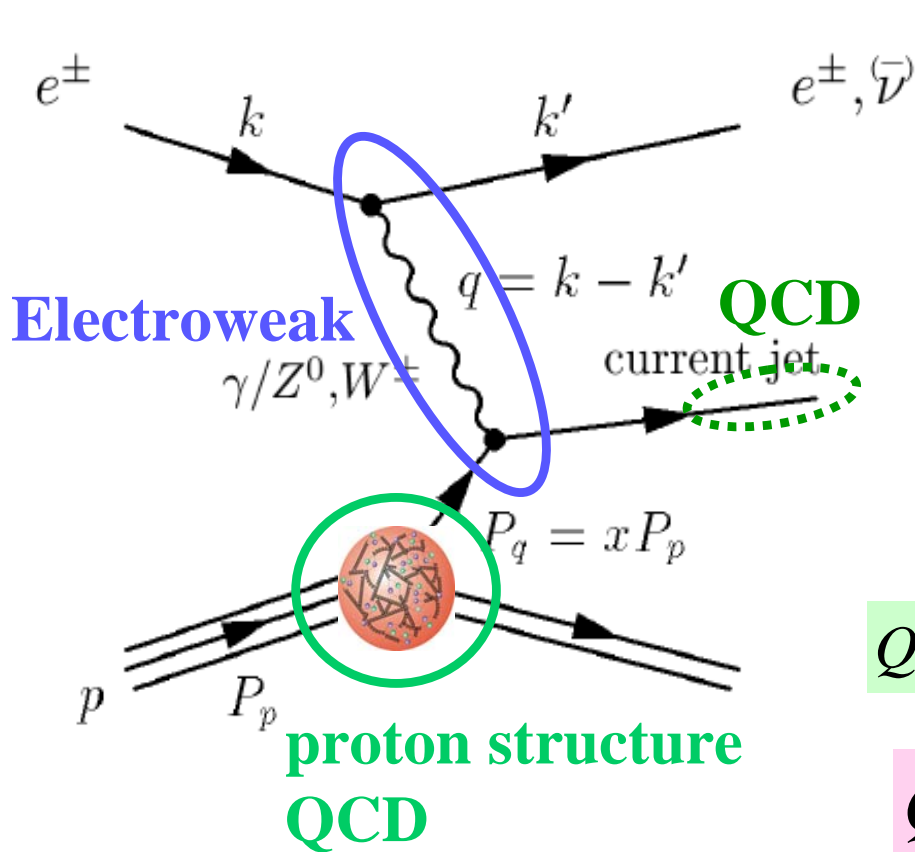
$$x = \frac{Q^2}{2p \cdot q}$$

$$y = \frac{p \cdot q}{p \cdot k}$$

$$Q^2 = sxy$$

$\sqrt{s}$  = center of mass energy

# Deep Inelastic Scattering (DIS)



- ◆ Kinematic variables to describe DIS

$Q^2$ : Virtuality

→ probing power

$x$ : Bjorken scaling variable

→ momentum fraction of struck quark

$y$ : Inelasticity

$$Q^2 = -q^2 = -(k - k')^2$$

$$x = \frac{Q^2}{2p \cdot q}$$

$$y = \frac{p \cdot q}{p \cdot k}$$

$$Q^2 = sxy \quad \sqrt{s} = \text{center of mass energy}$$

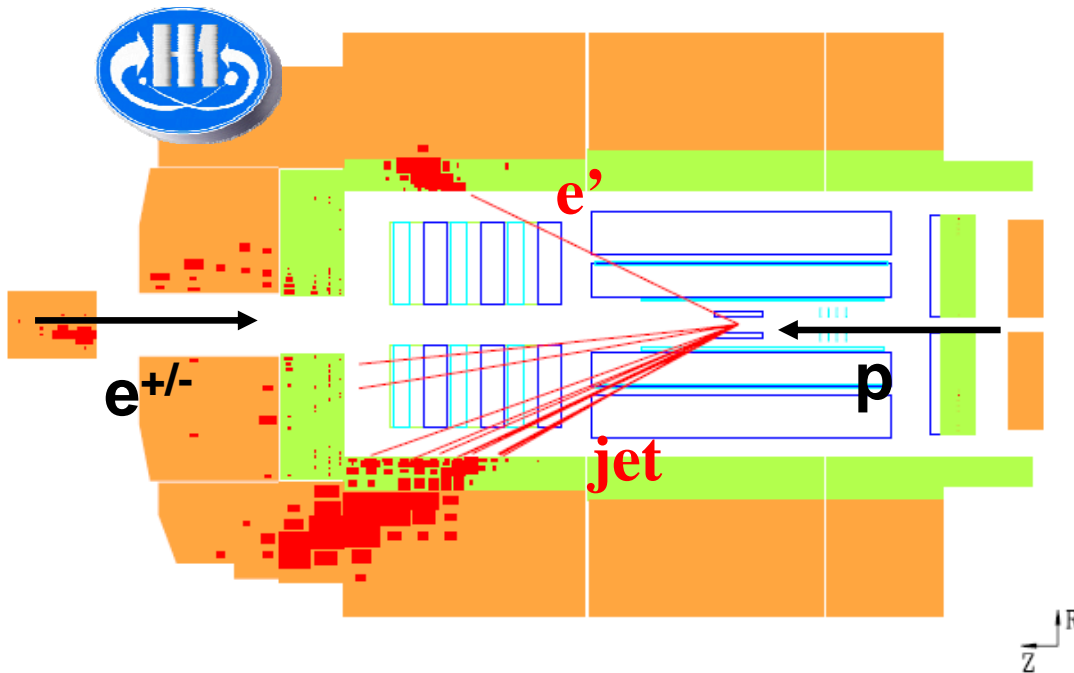
- ◆ DIS is a convolution of **electroweak (EW)** physics and the **proton structure**.
  - Good probe to the proton structure
  - Sensitive to EW physics from space-like view.
- ◆ Hadronic final state is also sensitive to QCD. (not covered in this talk)

# DIS in the detectors

## Neutral current (NC) process

$\gamma / Z^0$  exchange

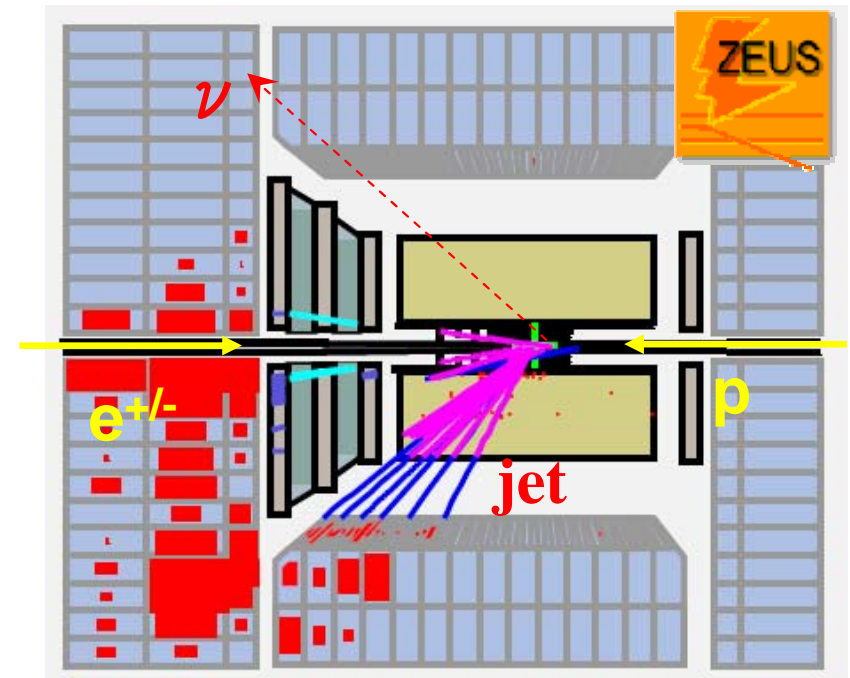
$ep \rightarrow e' X$



## Charged current (CC) process

$W^+$  exchange

$ep \rightarrow \nu X$

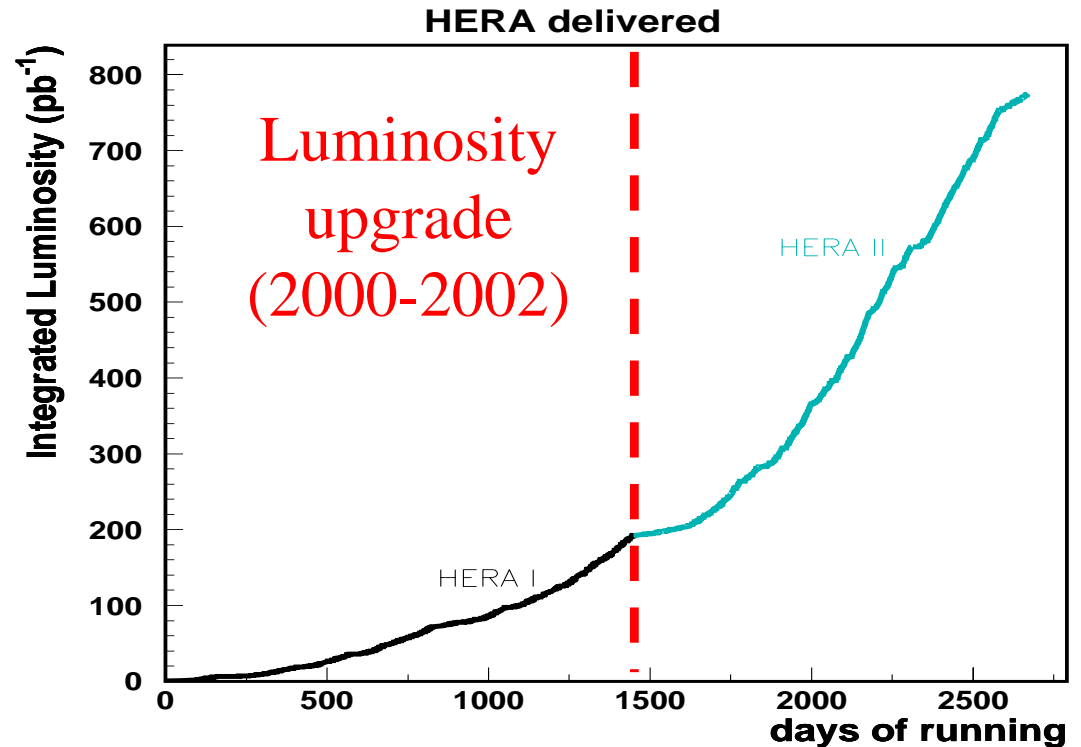


- ◆ Kinematic variables are reconstructed by two of measured variables;

$\left[ \begin{array}{l} \text{energy} \\ \text{angle} \end{array} \right]$  of  $\left[ \begin{array}{l} \text{scattered electron} \\ \text{jet } (\sim \text{struck quark}) \end{array} \right]$

# History of HERA

- ◆ 1992-2000: HERA-I
  - (started with  $E_p=820\text{GeV}$ , until 1997)
  - measurements go down to low- $Q^2$
  - Make full use of large kinematic region.  
 $1.5\text{GeV}^2 < Q^2 < 30000\text{GeV}^2$



- ◆ 2002-2007: HERA-II
  - High luminosity to collect high- $Q^2$  data.  
(high- $Q^2 \leftrightarrow$  Weak boson exchange)
  - lepton beams are polarized.
  - Increased sensitivity to EW.

Some of results will be shown in next slides.

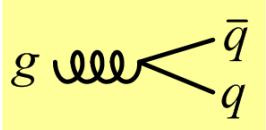


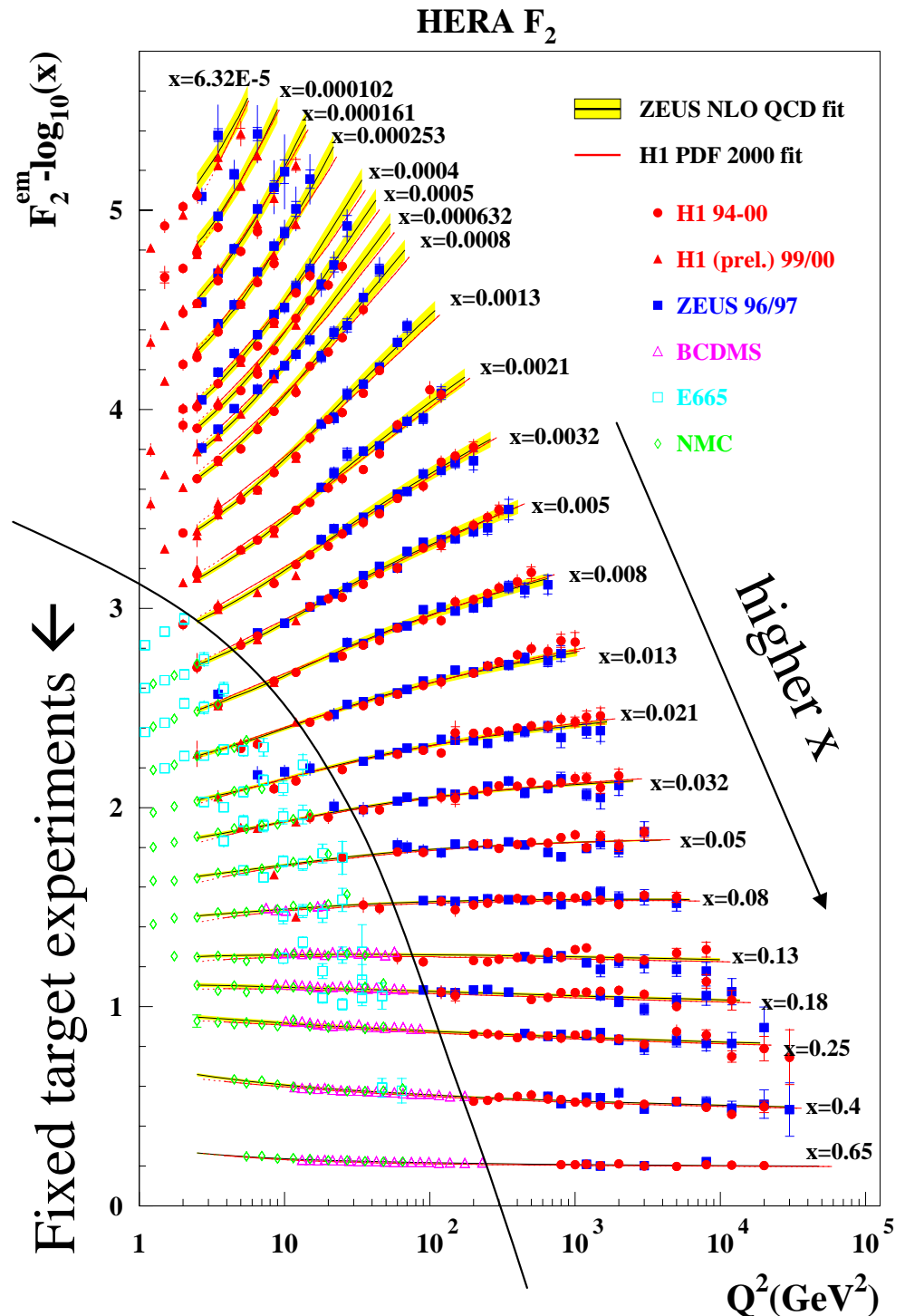
# F<sub>2</sub> measurement

- ◆ F<sub>2</sub> is measured over 4 orders of magnitude in (x, Q<sup>2</sup>).

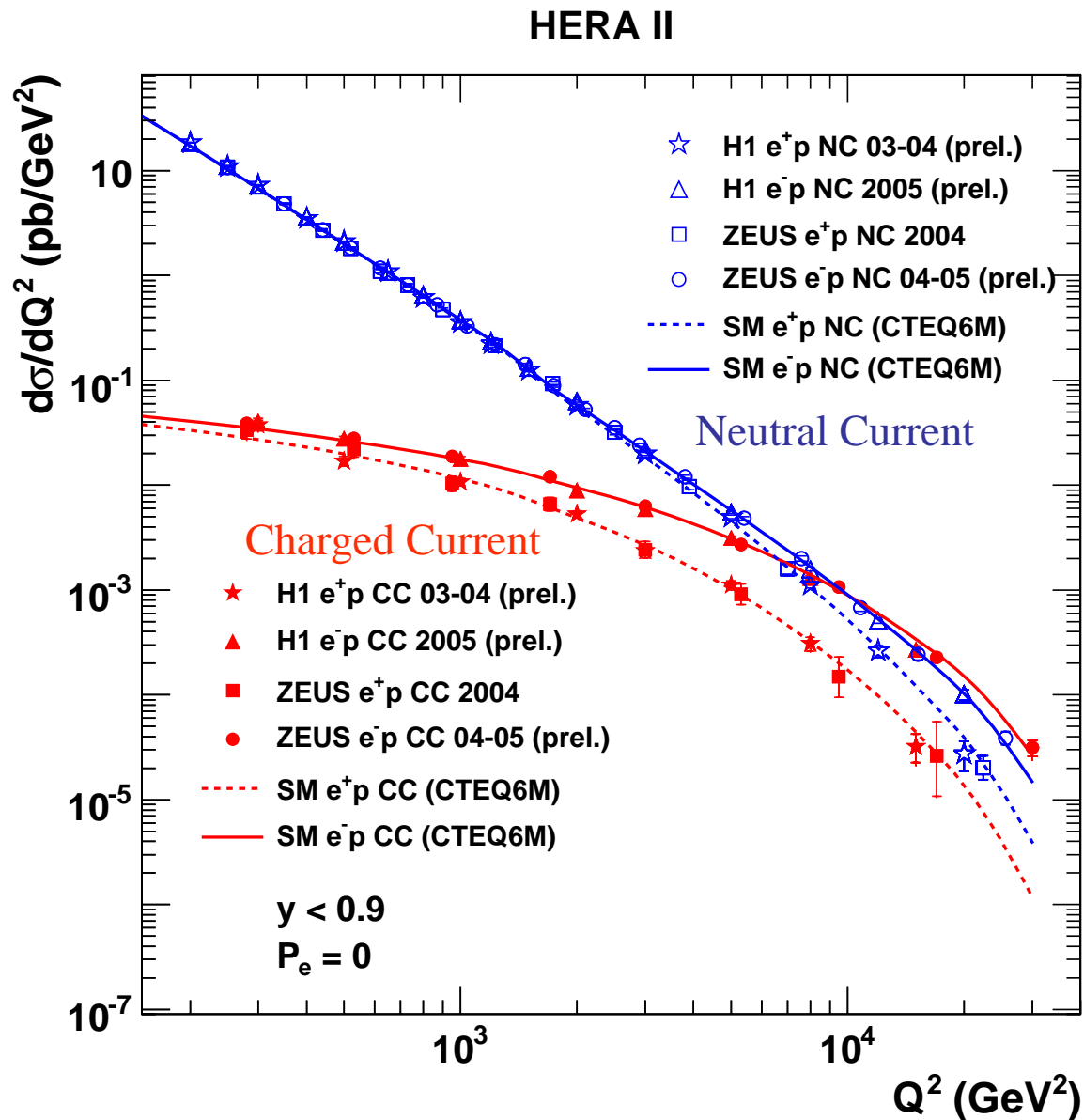
low x

→ strong dependence on Q<sup>2</sup>  
“scaling violation”

more  is visible.



# EW unification (NC/CC cross sections)



$$\frac{d\sigma}{dQ^2} \propto \left( \frac{1}{Q^2 + M_{\text{boson}}^2} \right)^2$$

Weak bosons are heavy.

→  $\sigma_{\text{weak}}$  is small

◆ low  $Q^2$

NC:  $\gamma$ -exchange

CC: W-exchange

→  $\sigma(\text{NC}) \gg \sigma(\text{CC})$

◆ high  $Q^2$

NC:  $\gamma/Z$

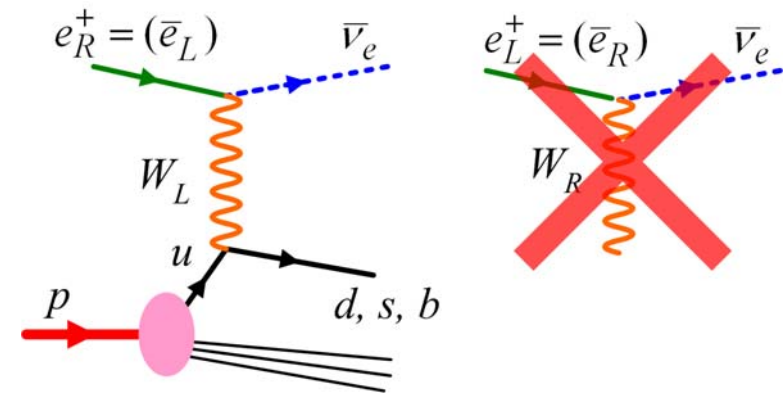
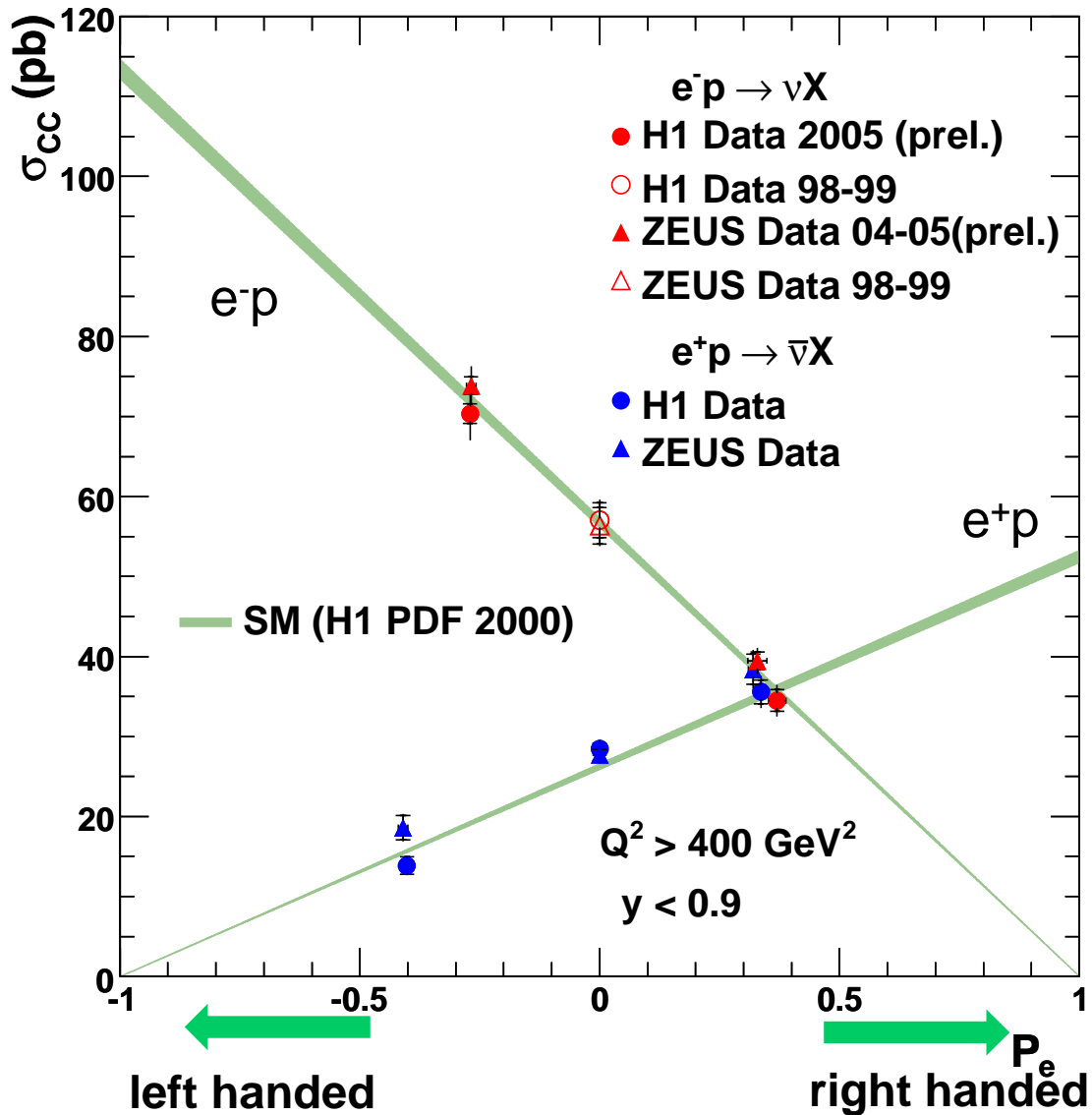
CC: W-exchange

→  $\sigma(\text{NC}) \sim \sigma(\text{CC})$

Electroweak unification

# Polarized CC cross sections

Charged Current  $e^\pm p$  Scattering



Weak process  
= No right-handed current  
CC is purely weak process  
→ linear dependence on polarization.

Introduction

HERA physics

**Proton structure**

# Parton Distribution Function (PDFs)

- ◆ Parton distribution functions are used to describe the proton structure.

$$q(x, Q^2) \quad \bar{q}(x, Q^2) \quad g(x, Q^2)$$

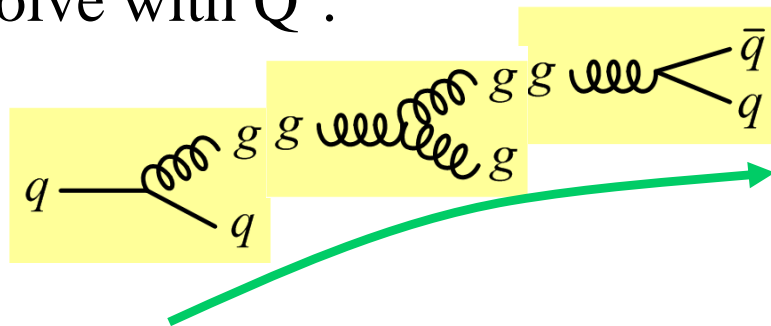
- Valence quarks:

$$u_{\text{Val}}(x, Q^2) = u(x, Q^2) - u_{\text{Sea}}(x, Q^2), \text{ same for d quark}$$

- Sea quarks:

$$u_{\text{Sea}}(x, Q^2) = \bar{u}(x, Q^2) = s(x, Q^2) = \bar{s}(x, Q^2) \dots \text{etc.}$$

- ◆ PDFs evolve with  $Q^2$ .



Larger  $Q^2$  allows to see more quarks.

- ◆ The  $Q^2$  evolution is described by **DGLAP equation**, based on pQCD.

$$\frac{dF_2}{d \ln Q^2} = \sum_q e_q^2 \frac{\alpha_s(Q^2)}{2\pi} \int_x^1 \frac{dy}{y} \left[ P_{qq}(x/y) \cdot q(y, Q^2) + P_{qg}(x/y) \cdot g(y, Q^2) \right]$$

# Structure functions

- DIS cross sections can be written with structure functions.

$$\frac{d^2\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4} Y_\pm \left[ F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2) \mp \frac{Y_-}{Y_+} xF_3(x, Q^2) \right] \quad Y_\pm = 1 \pm (1 - y^2)$$

cross section with point-like particle

**Structure functions:**  
they reflect momentum distribution of partons in the proton.

Structure functions are sensitive to PDFs.

- $F_2$  : total number of quarks

$$F_2 = \sum A_q x(q + \bar{q})$$

- $F_L$  : longitudinal structure function  $\longrightarrow$  gluon  
only sizable at high- $y \rightarrow$  Details will come up later

- $xF_3$  : parity violation term

$$xF_3 = \sum B_q x(q - \bar{q}) \longrightarrow \text{Valence quarks}$$

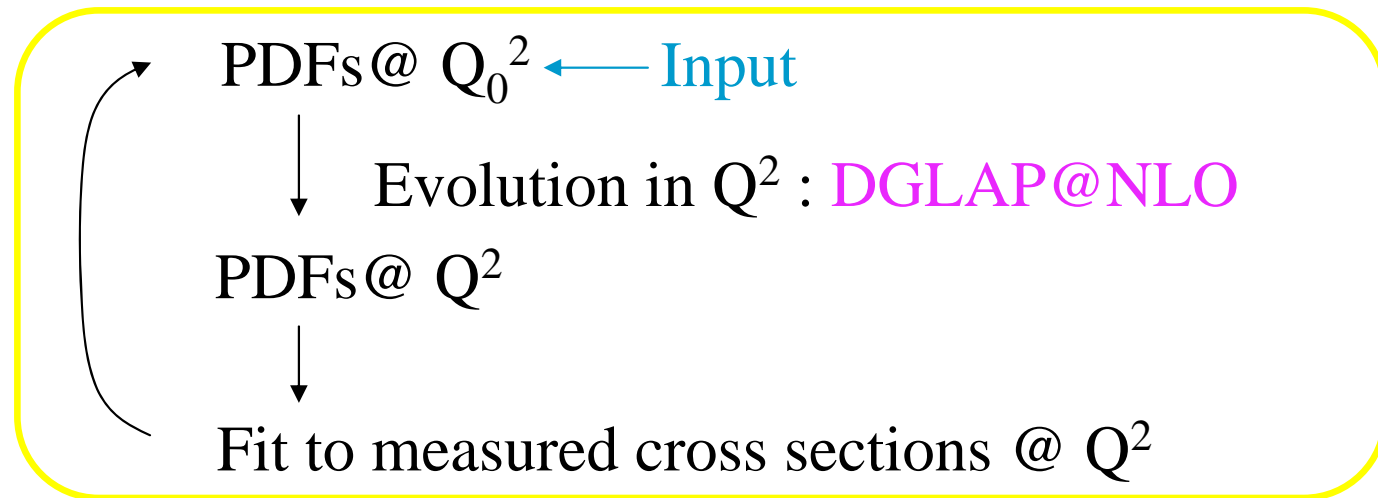


# Extraction of PDFs

$q(x, Q^2)$

$g(x, Q^2)$

- ◆  $Q^2$  evolution of PDFs can be **predicted** by perturbative QCD, i.e. by DGLAP equation.
- ◆  $x$ -dependence of PDFs can be **extracted** from fits to measured cross sections.



PDFs are parameterized @  $Q_0^2 = 7\text{GeV}^2$

@ZEUS

$$x f(x) = A x^b (1-x)^c (1+dx) \quad \text{for } xu_v, xd_v, xS, xg, x\Delta (= x\bar{d} - x\bar{u})$$

A: Normalization,  $b$ : Low  $x$ ,  $c$ : High  $x$ ,  $d$ : smoothing for middle  $x$

Constraints from momentum and number sum rule, etc.

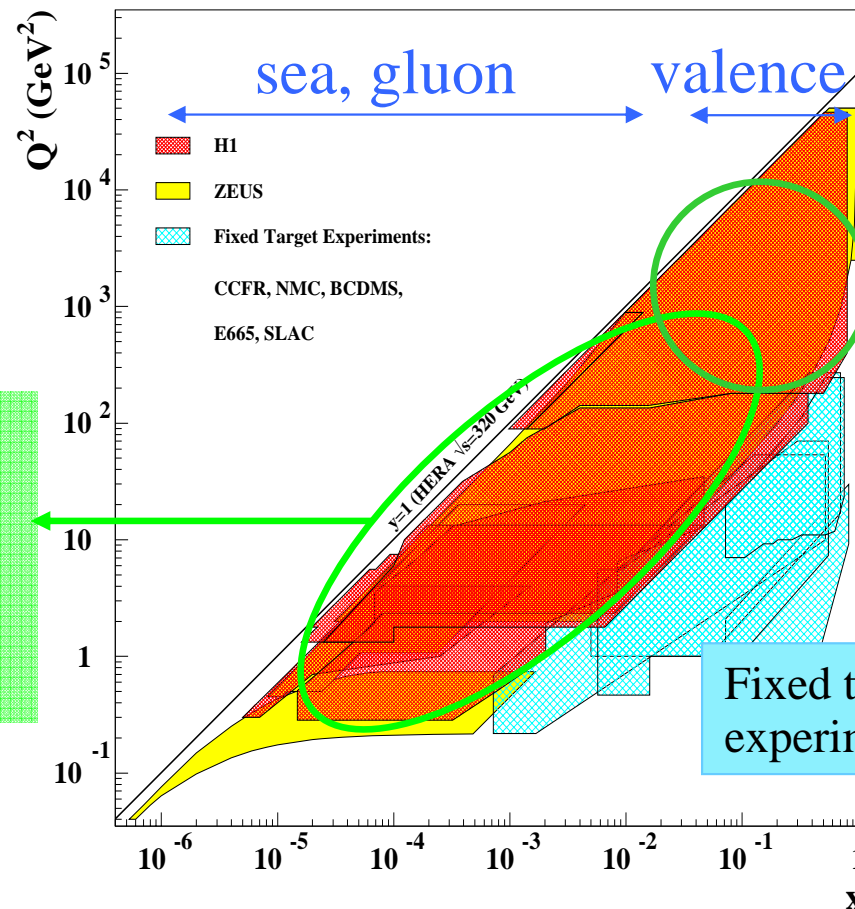
→ 11 free parameters

# PDF extraction at HERA

A single experiment can determine PDFs.

Jets cross sections  
→ gluon

$\gamma$  exchange  
→ sea  
scaling violation  
→ gluon

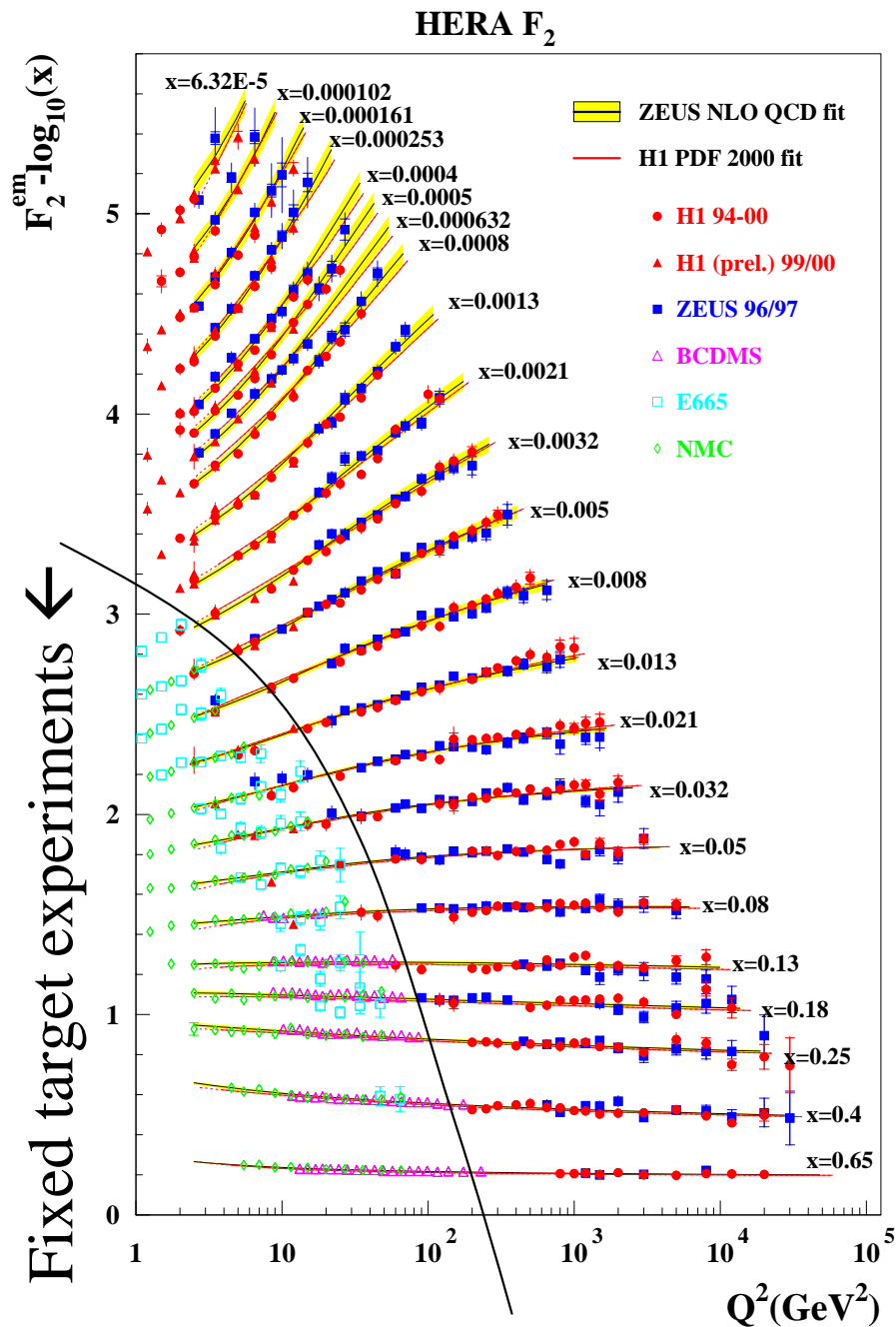


QCD + EW physics

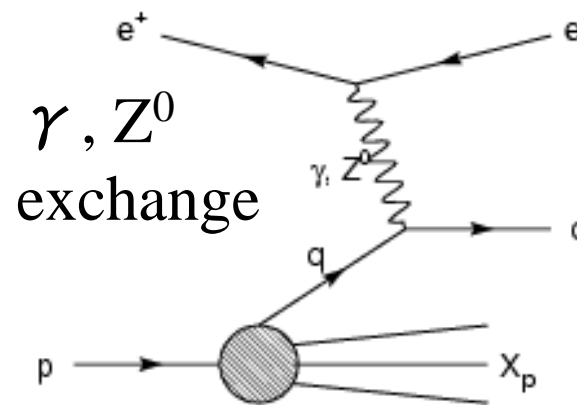
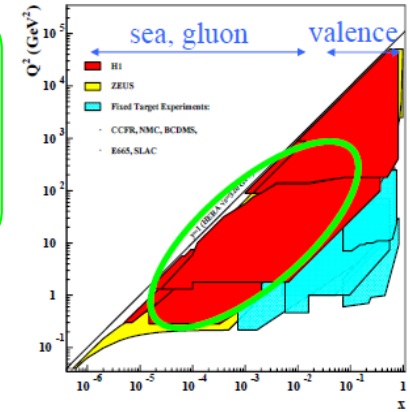
$Z^0$  exchange  
→ • sea + valence  
• valence only  
 $W^\pm$  exchange  
- charge selective  
→ u or d quark

- ◆ Pure proton target → Free from target correction, nuclear effect.
- ◆ Single experiment → systematic uncertainties are well understood.

# NC cross sections for PDF extraction



Large kinematic coverage  
 $3 < Q^2 < 30000 \text{ GeV}^2$   
 $6 \times 10^{-5} < x < 0.6$



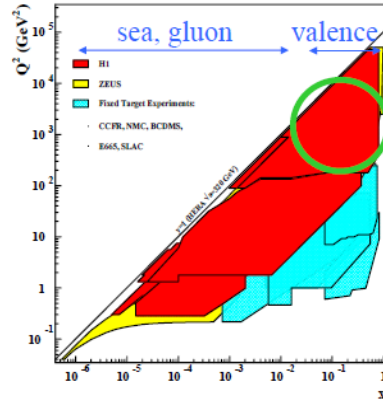
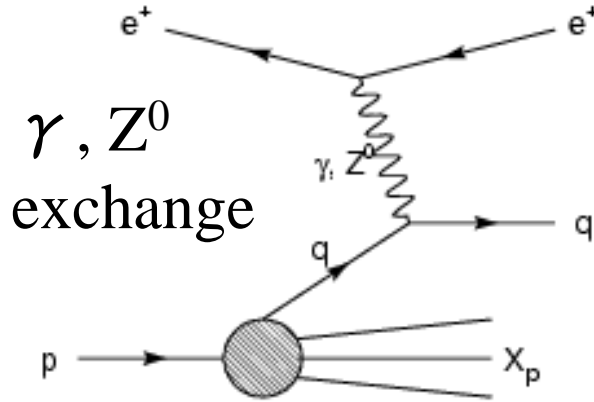
$$F_2 \propto \sum x(q + \bar{q})$$

Sea + valence quark

scaling violation of  $F_2$

$$\frac{\partial F_2}{\partial \ln Q^2} \propto xg \quad \text{gluon}$$

# NC cross sections @ high- $Q^2$



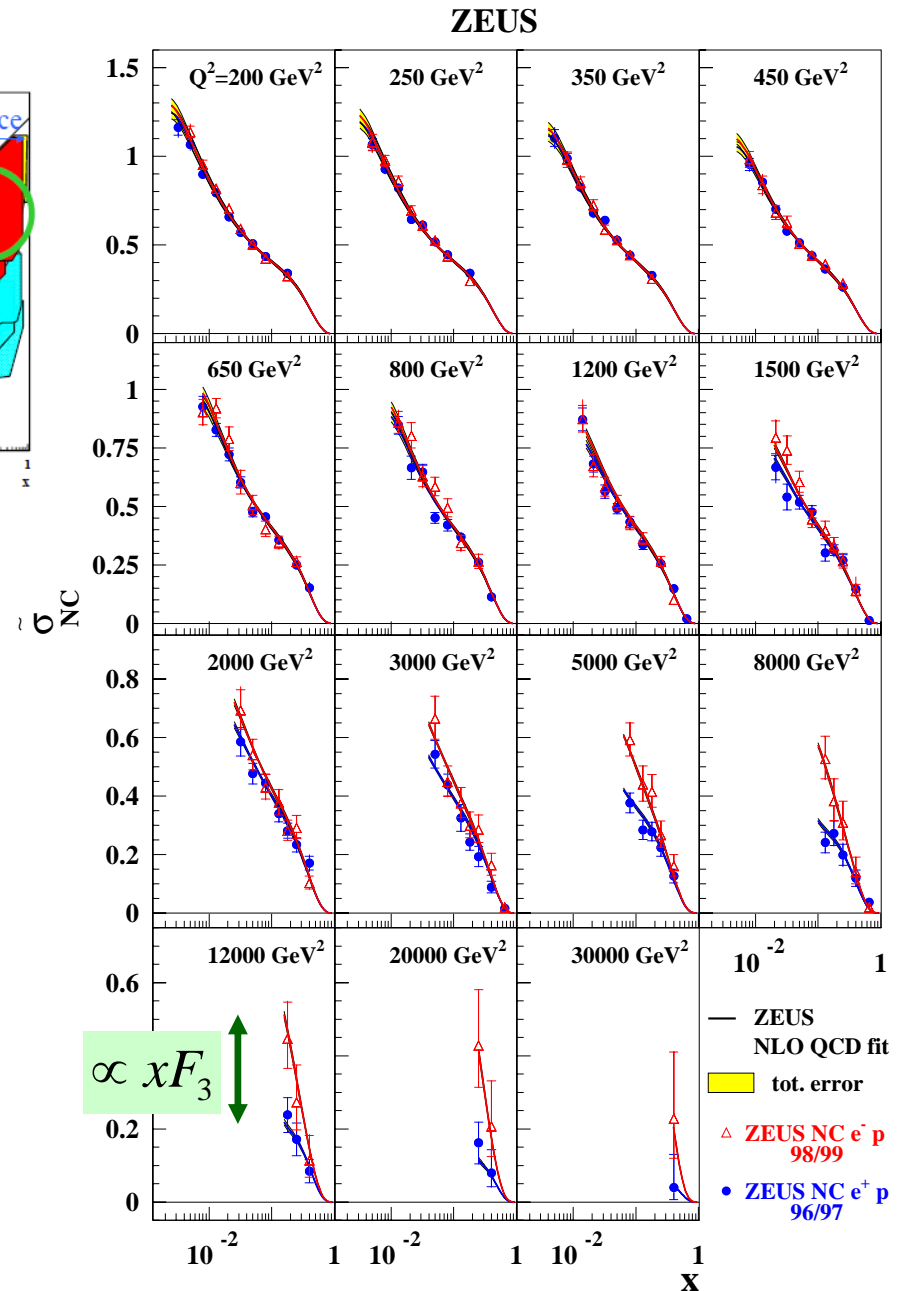
- At high  $Q^2$ , weak current ( $Z^0$ ) introduces parity violation.

$$\tilde{\sigma}(e^\pm p) = F_2(x, Q^2) \mp \frac{Y_-}{Y_+} xF_3(x, Q^2)$$

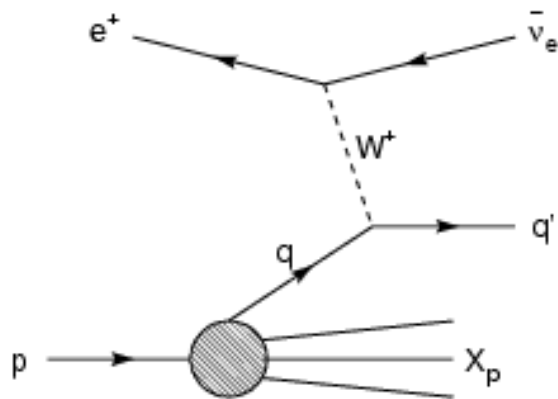
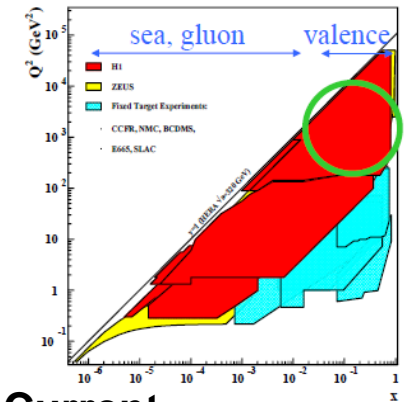
$$\tilde{\sigma}(e^- p) - \tilde{\sigma}(e^+ p)$$

$$\longrightarrow xF_3 \propto \sum x(q - \bar{q})$$

valence quark



# CC cross sections for PDF extraction



$$e^+ q^{(-)} \rightarrow \bar{\nu} q^{(+)}$$

$$e^- q^{(+)} \rightarrow \nu q^{(-)}$$

HERA  $e^+p$  Charged Current

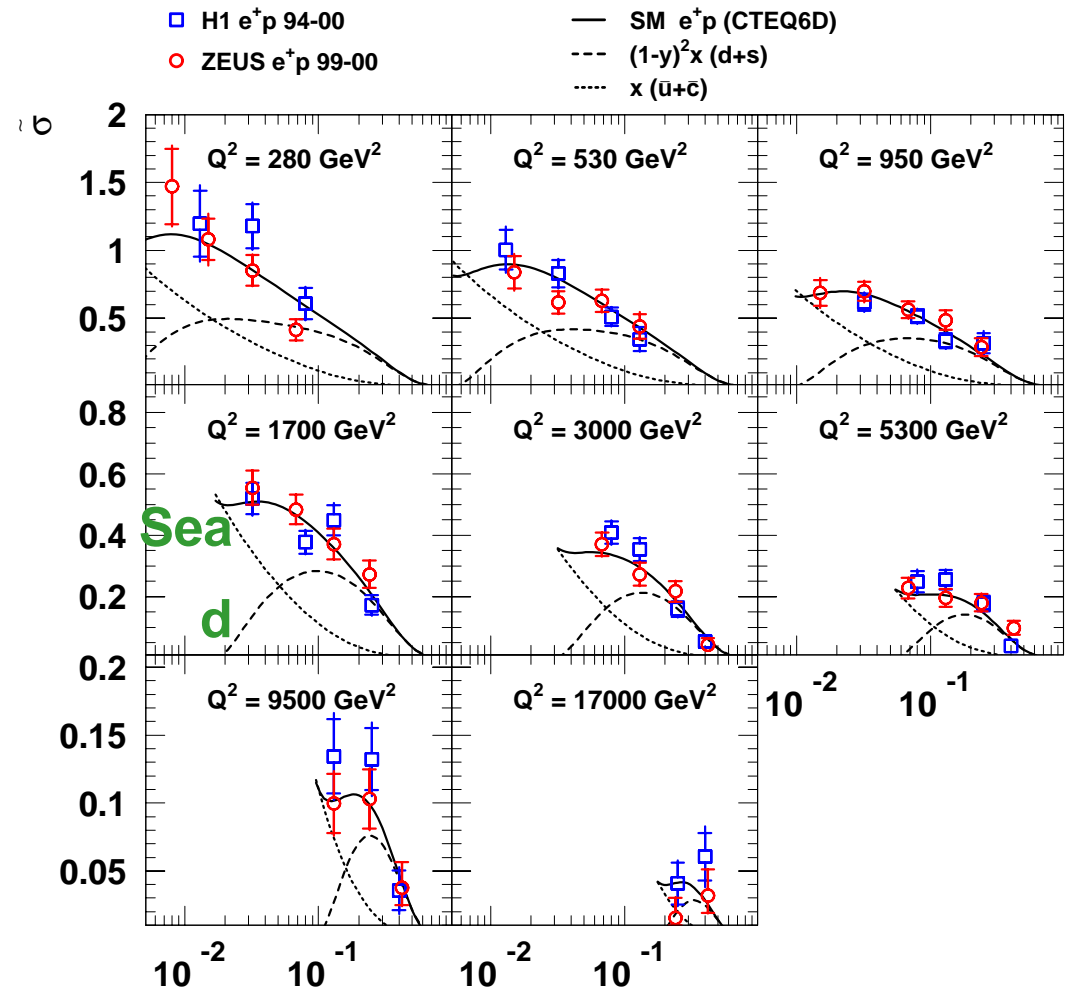
CC is charge selective interaction.

- ♦ positron-induced  
→ negative-charged partons  
 $\tilde{\sigma}(e^+ p) \propto [(\bar{u} + \bar{c}) + (1-y)^2 (d + s)]$

d quark

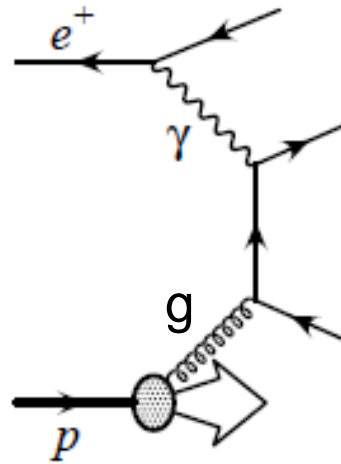
- ♦ electron-induced  
→ positive-charged partons  
 $\tilde{\sigma}(e^- p) \propto [(u + c) + (1-y)^2 (\bar{d} + \bar{s})]$

u quark

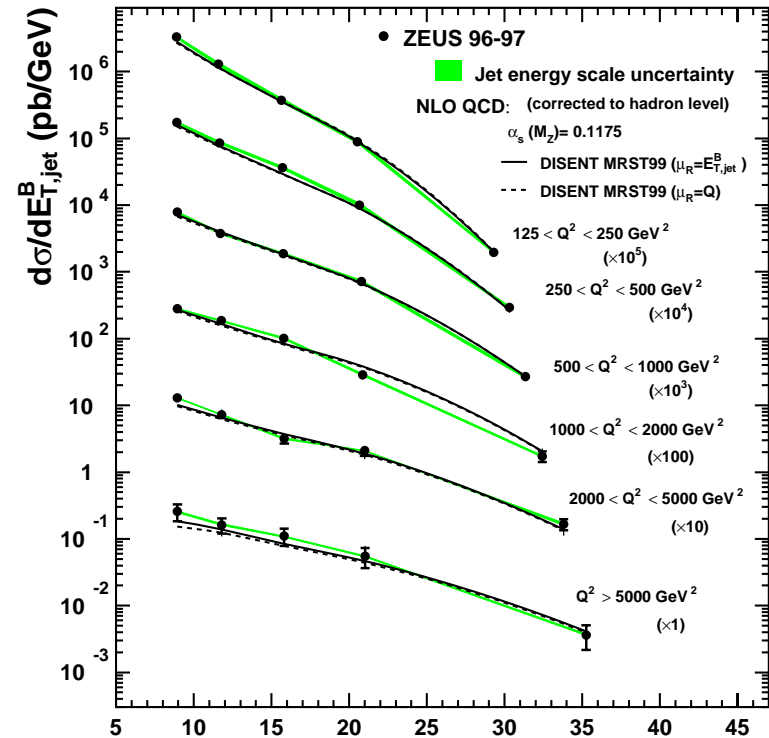


# Jet Cross sections for PDF extractions

Directly sensitive  
to gluon density



ZEUS



DIS inclusive jet  $E_{T,jet}^B$  (GeV)

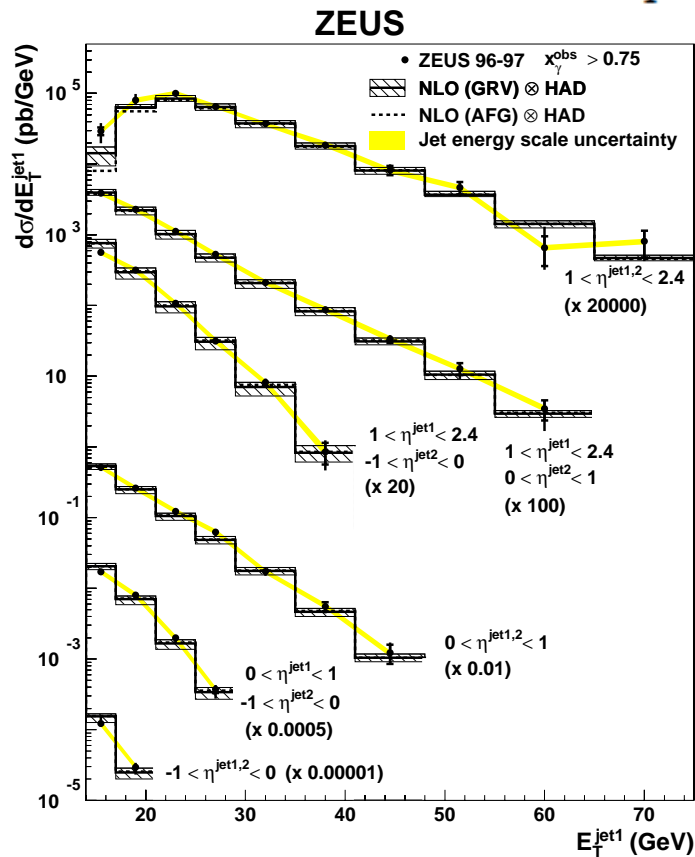


Photo-production ( $Q^2 \sim 0$ ) dijets



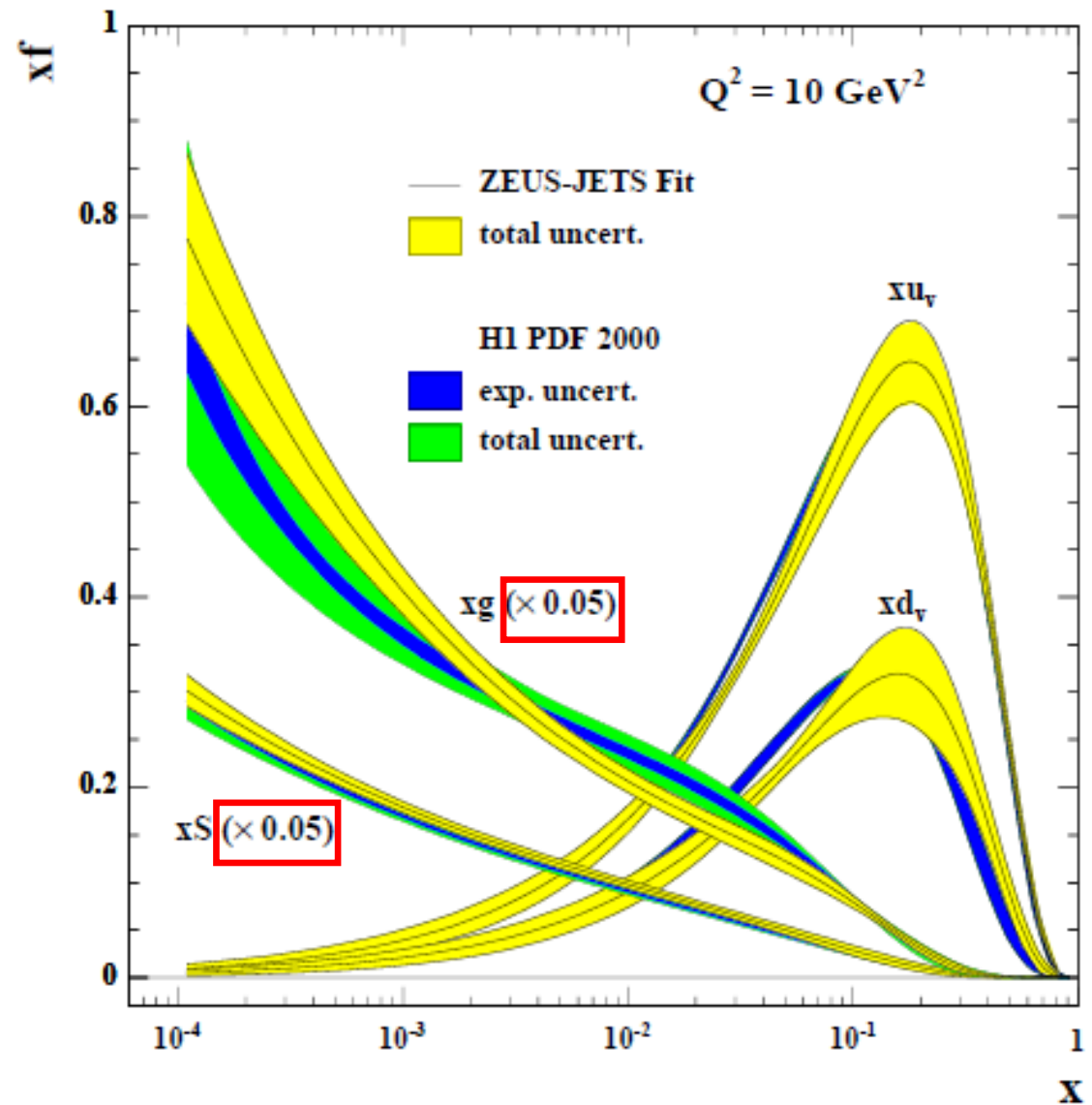
# PDFs from HERA

All 547 data points (ZEUS)  
are fitted simultaneously.  
→ PDF extraction.

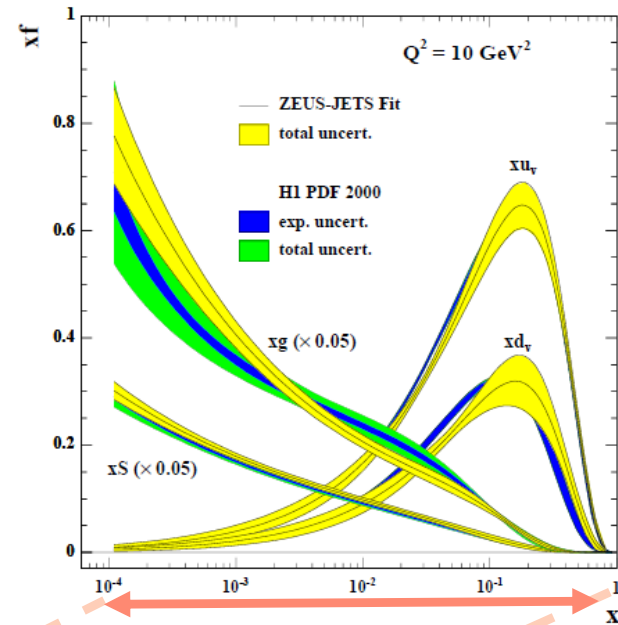
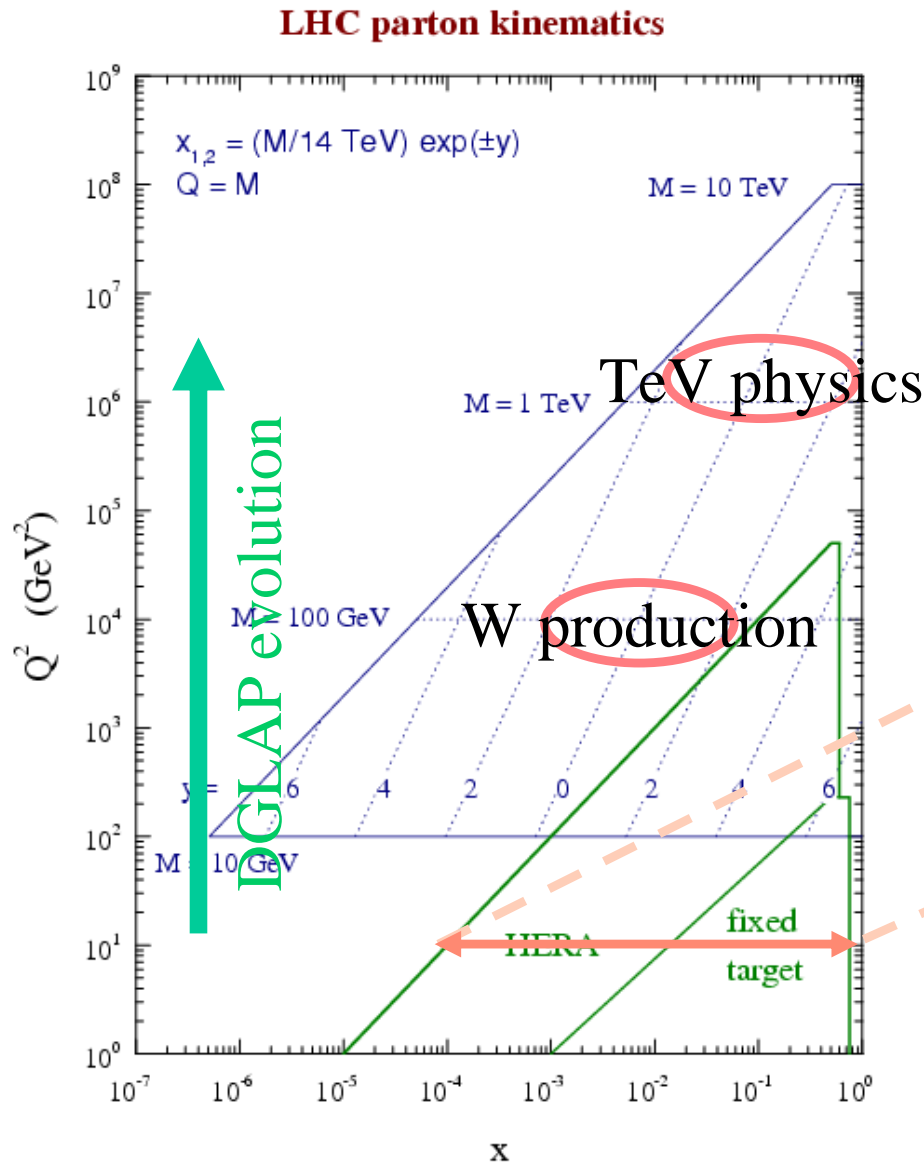
- ◆ Strong rise of gluon PDF at low  $x$ .
- ◆ Sea quarks are also many.  
(Note: in the plot they are 1/20)

## H1/ZEUS difference

- data set  
(H1 does not have jets, but results from fixed target exp.)
- parameterization
- systematic uncertainty



# Why is PDF extraction at HERA important?



- ◆ LHC: proton-proton collision  
 → Definitely needs PDFs.
- ◆ Main physics of LHC are at the  $x$  range which HERA covers.

# We can improve our understanding further

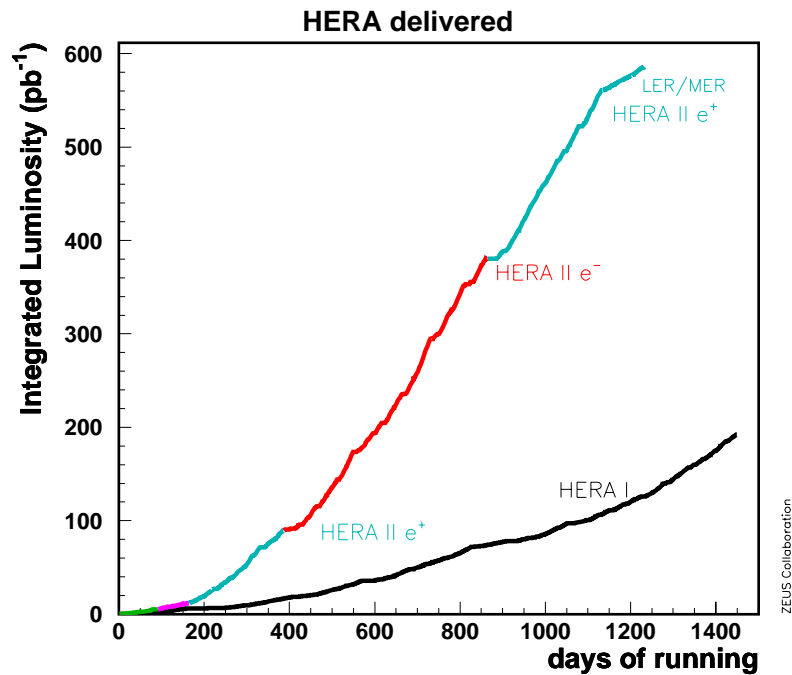
Other (and/or more) measurements

- ◆ NC/CC
  - More statistics with polarized beam.
- ◆ Heavy Flavour production
  - Large statistics with the updated detector in HERA-II.
- ◆  $F_L$ 
  - First direct measurement at the end of HERA.

Understanding of systematic uncertainties of measured cross section in  
HERA-I

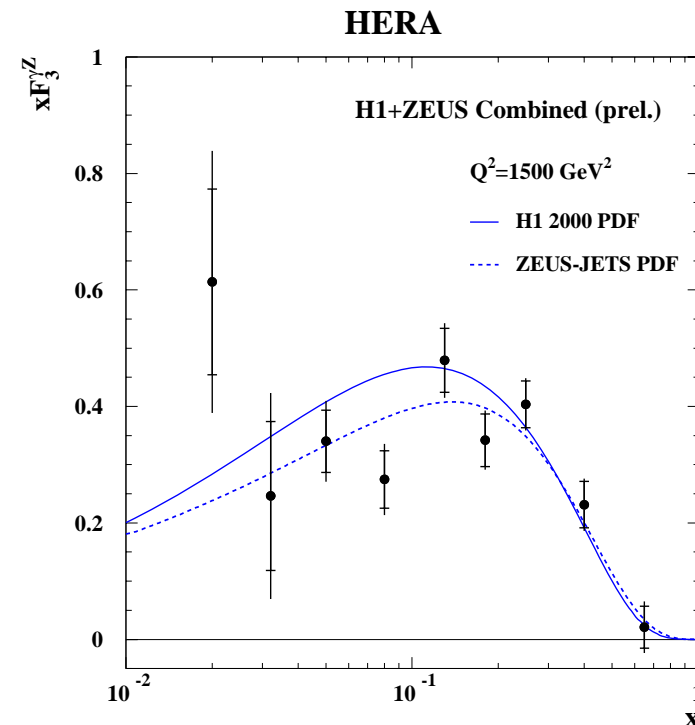
- ◆ Combining cross sections from the H1 and ZEUS experiments.

# NC/CC cross sections with more statistics



	HERA-I	HERA-II
$e^-p$	$20\text{pb}^{-1}$	$180\text{pb}^{-1}$
$e^+p$	$100\text{pb}^{-1}$	$170\text{pb}^{-1}$

- ◆ Increase of electron data  
NC  $\rightarrow$  More sensitivity to  $xF_3$   
i.e. valence quarks (u+d)
- ◆ Increase of positron data  
CC  $\rightarrow$  More sensitivity to d quark



# Heavy Flavour production

- ◆ Dominant process of heavy quark production:

## **Boson-Gluon-Fusion (BGF)**

- ◆ Two schemes to treat heavy quarks in pQCD;

- massive scheme (FFN)

appropriate for  $Q^2 \sim M_q^2$

Heavy quarks are produced via BGF.

→ Sensitive to gluon PDFs

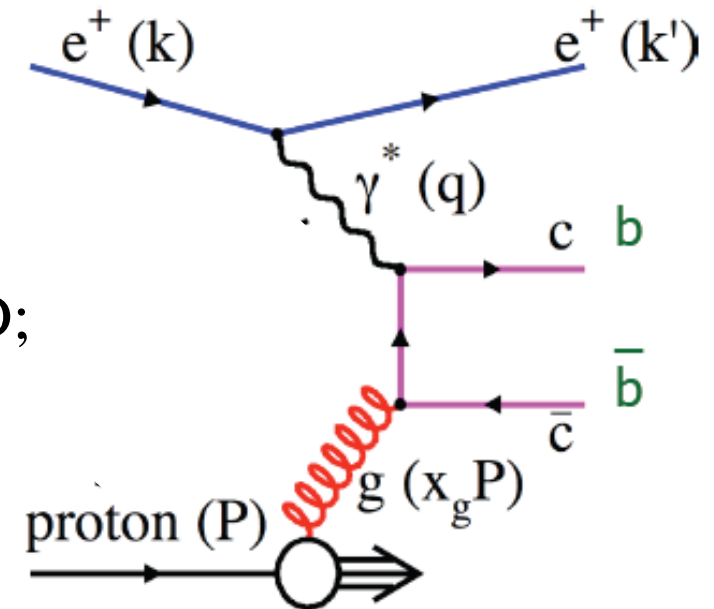
- massless scheme (ZMVFN)

appropriate for  $Q^2 \gg M_q^2$

Heavy quarks are massless and exist in the proton if  $Q^2$  is above the mass threshold.

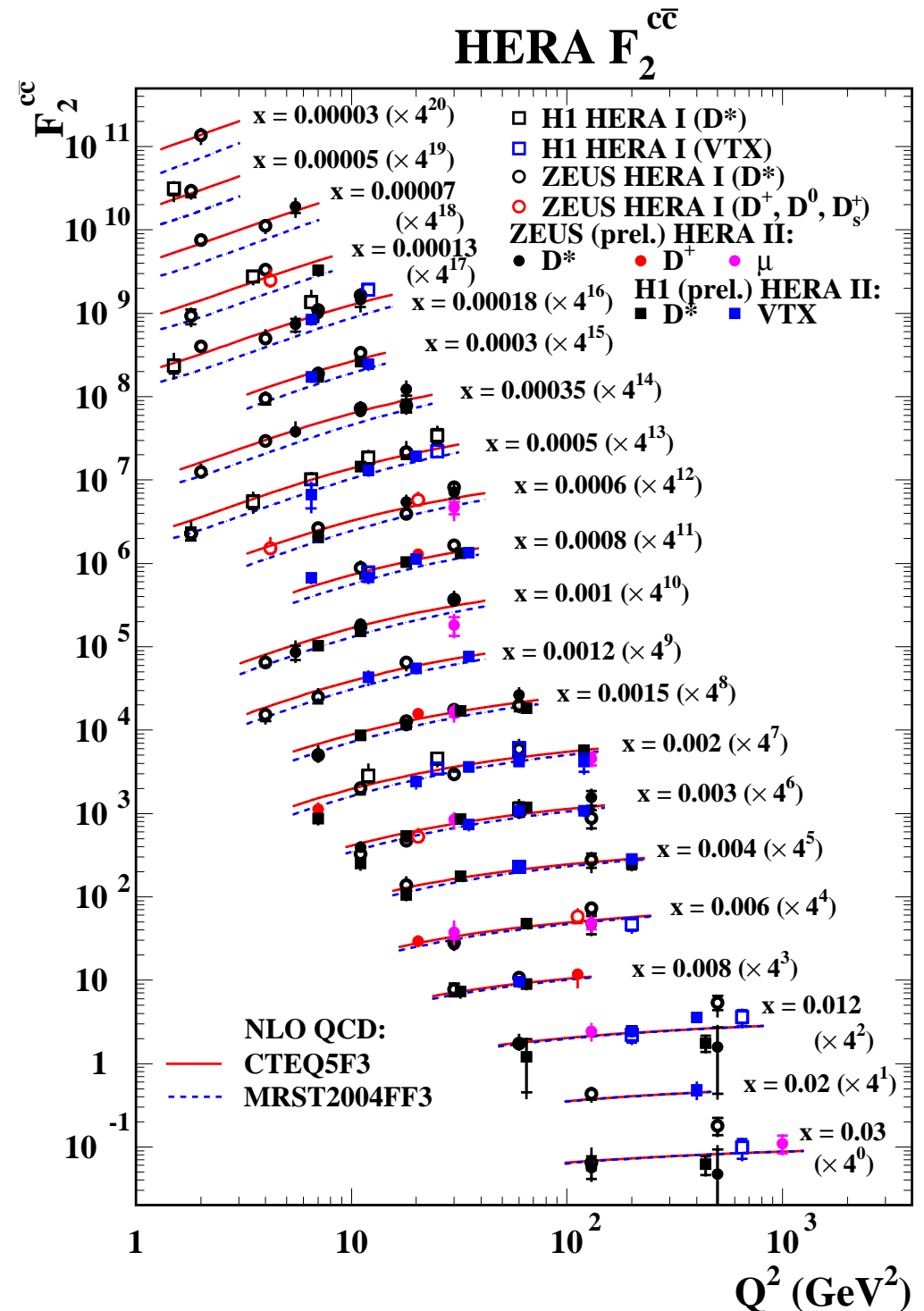
→ Intrinsic heavy quarks' PDFs

- ◆ Cross check for current pQCD description for the proton.



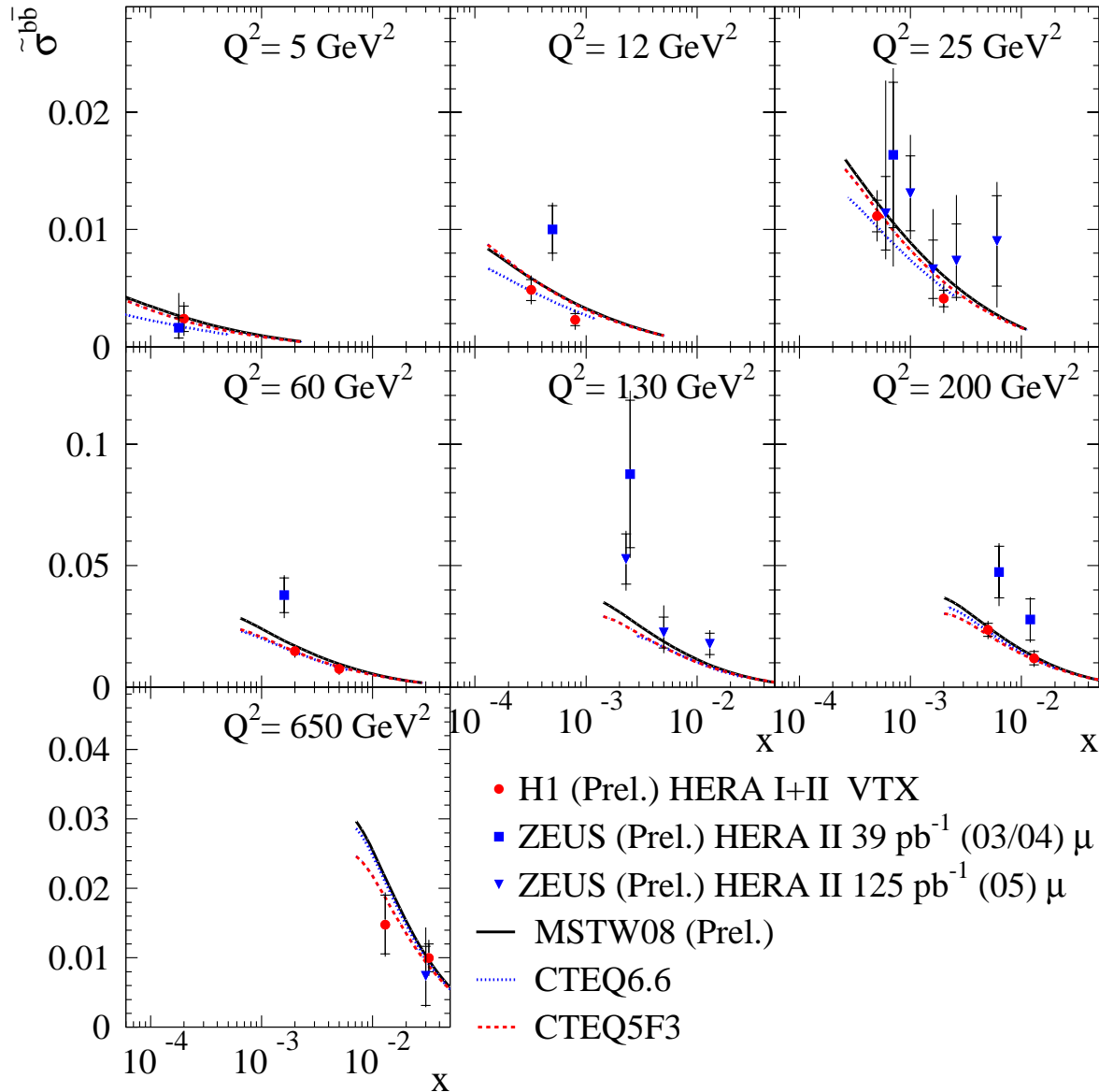
# $F_2^{cc}$

- ◆  $F_2^{cc}$  is extracted for large kinematic region.
  - different methods
    - D mesons by slow pions
    - Impact parameter tagging
  - different data sets, theory
    - In good agreement
- ◆ Scaling violation is seen.
- ◆ Well described by NLO-QCD.



# $F_2^{bb}$

## H1+ZEUS BEAUTY CROSS SECTION in DIS

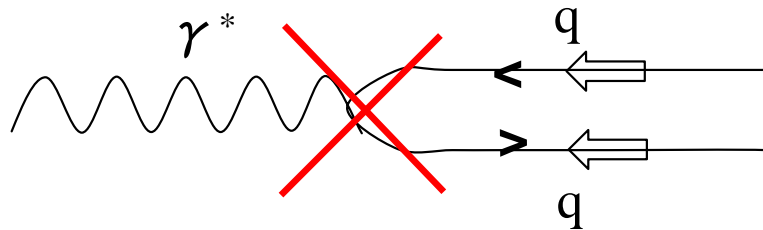


- ◆ First measurement of  $F_2^{bb}$  at HERA.
- ◆ Different methods
  - H1: Impact parameter tagging
  - ZEUS:  $\mu$  + jet
- ◆ More data to come



# Longitudinal structure function: $F_L$

- ◆ Proportional to longitudinal photon interacting with proton.
- ◆ In naive QPM, proton has co-linear spin  $\frac{1}{2}$  quarks only.



Longitudinal photon cannot interact with a quark  $\rightarrow F_L=0$

- ◆ gluon emission in the proton  $\rightarrow F_L \neq 0$   
i.e.  $F_L$  directly reflects gluon dynamics in the proton.

$$\text{In pQCD: } F_L = \frac{\alpha_s}{4\pi} x^2 \int_x^1 \frac{dz}{z^3} \left[ \frac{16}{3} F_2 + 8 \sum_q e_q^2 \left( 1 - \frac{x}{z} \right) z g(z) \right]$$

gluon PDF

Measurement of  $F_L$  is good test for the current understanding of proton structure and QCD.

# $F_L$ @ HERA

$F_L \leftrightarrow$  gluon  $\rightarrow$  Probably HERA is the best place to measure  $F_L$ .

- ◆ Why had  $F_L$  not been measured before the end of HERA?

Ans. Technical difficulties

- Needs cross section measurements with different beam energies.
- Needs to tag scattered electrons with lowest energies as possible.

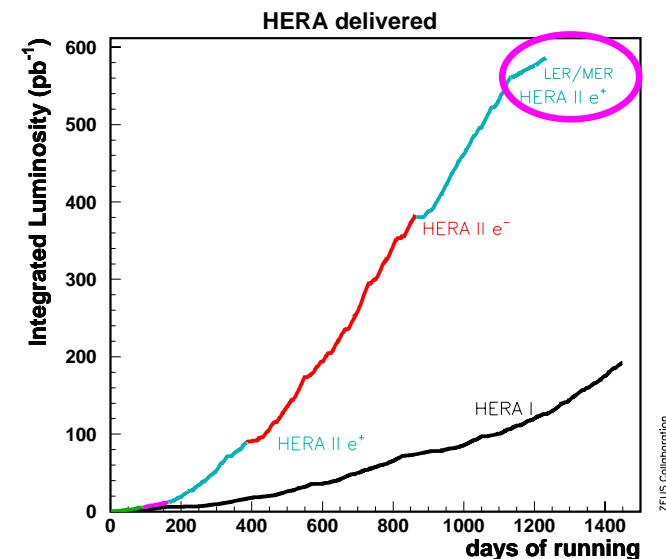
- ◆ The last 4 months of HERA operation were dedicated to  $F_L$  measurement.

$\rightarrow$  Operation with lowered proton beam energy.

$$E_p = 460 \text{ GeV} \quad : \quad 14 \text{ pb}^{-1}$$

$$E_p = 575 \text{ GeV} \quad : \quad 8 \text{ pb}^{-1}$$

**Successfully done!**



# $F_L$ measurement

- ◆ Cross section is combination of  $F_2$  and  $F_L$ .

$$\tilde{\sigma} = \frac{Q^4 Y_+}{2\pi\alpha^2} \frac{d^2\sigma}{dx dQ^2} = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2)$$

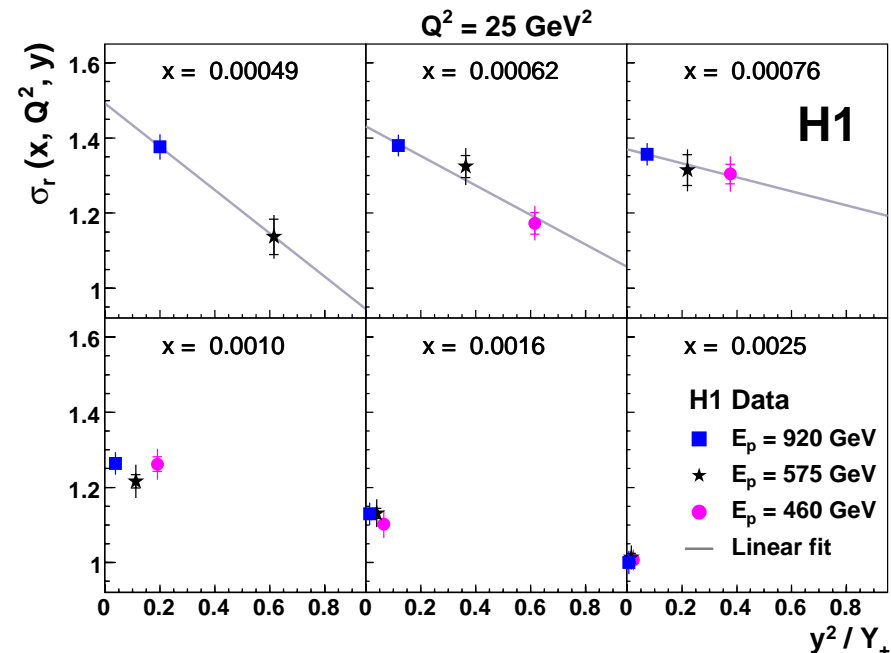
- ◆  $F_L$  ← Comparison of  $\tilde{\sigma}$  at the same  $(x, Q^2)$  but different  $y$

$$Q^2 = sxy \quad \rightarrow \text{different beam energy}$$

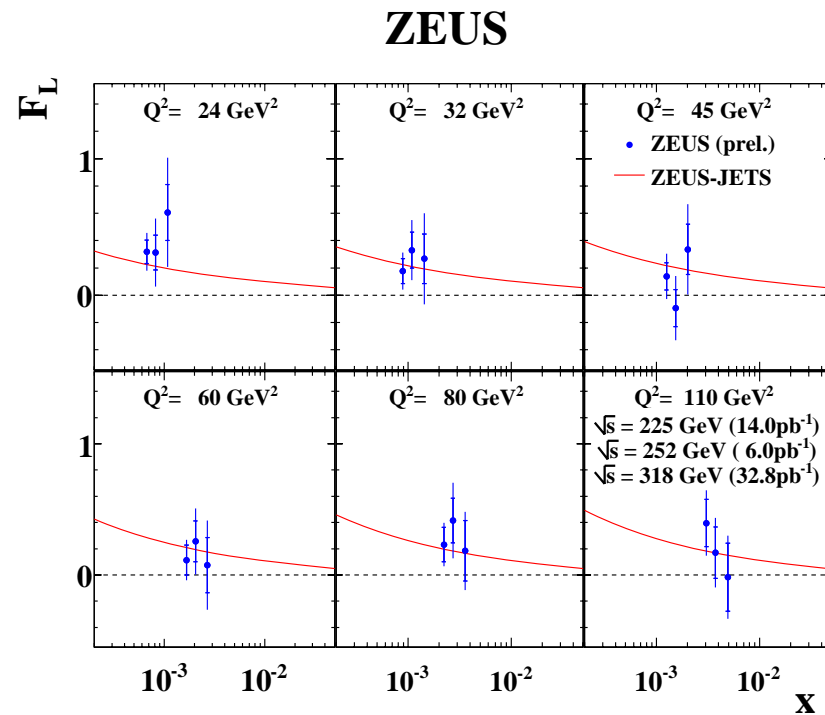
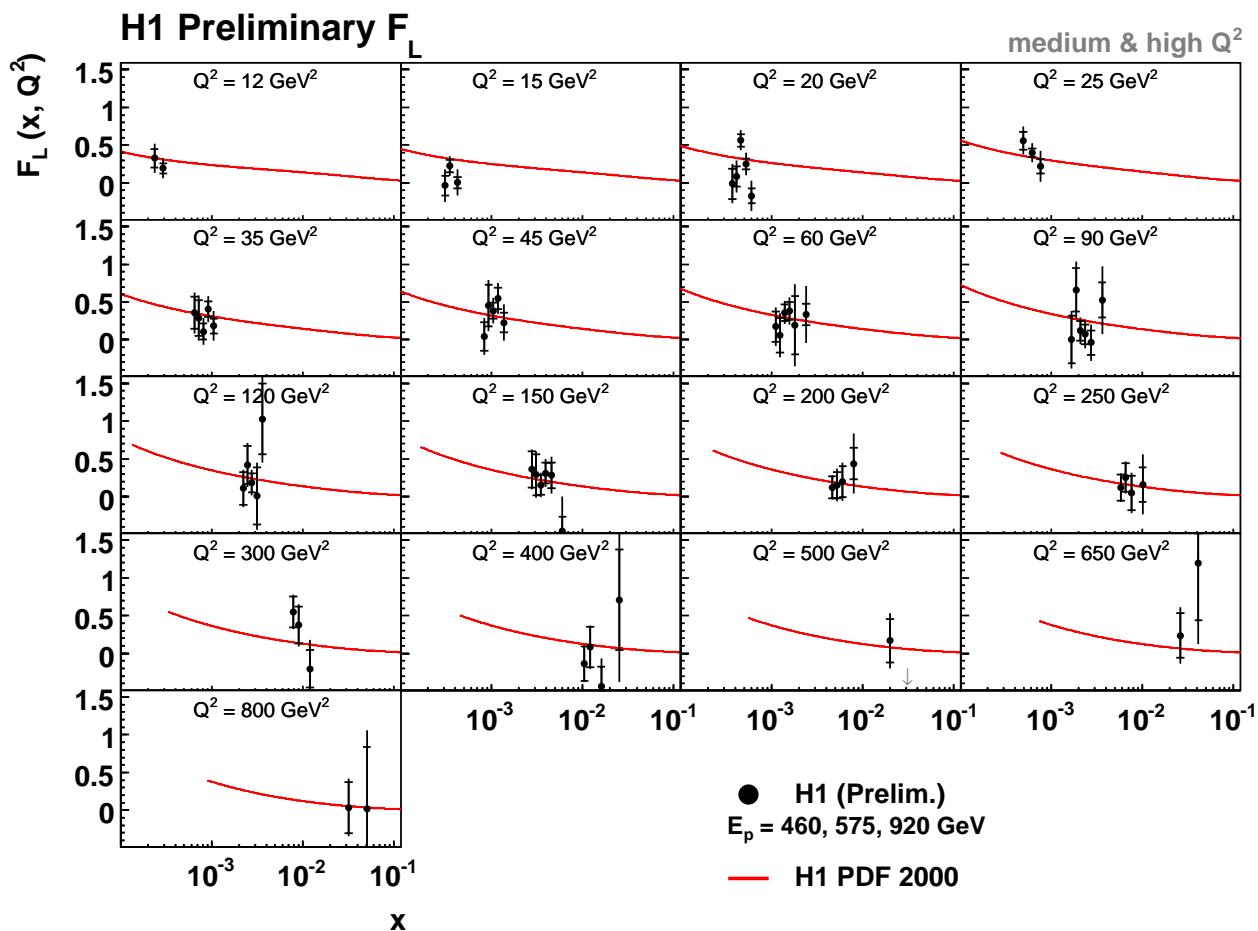
Sizable only at high- $y \Leftrightarrow$  Low energy of scattered electron.

- ◆ Linear fit on cross sections at each  $(x, Q^2)$  bin.

→ slope =  $F_L$



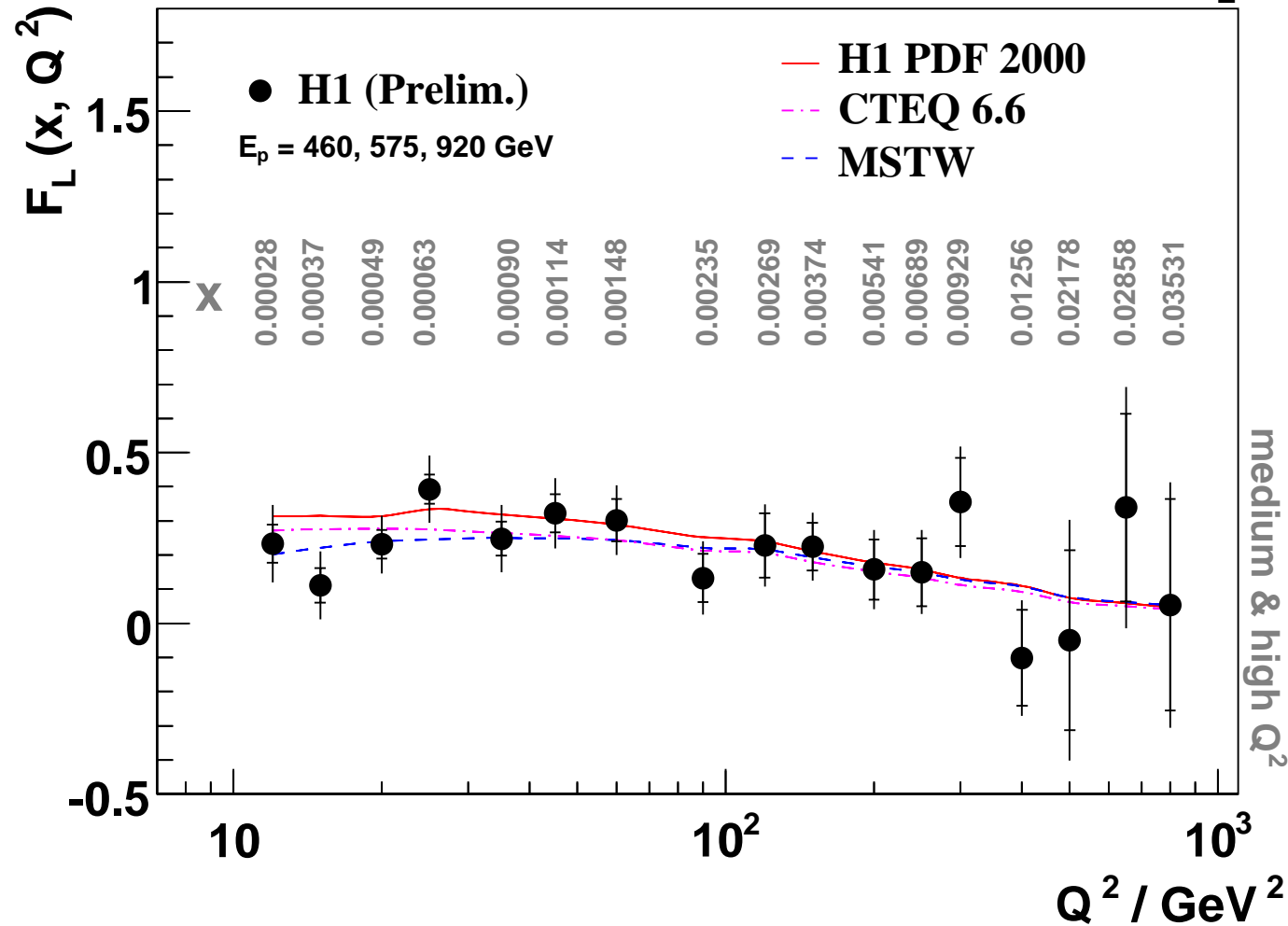
# $F_L$ from two experiments



- ◆ The first  $F_L$  measurement at low  $x$ .
- ◆ The measured  $F_L$  is consistent with pQCD description.

# x-averaged $F_L$

H1 Preliminary  $F_L$



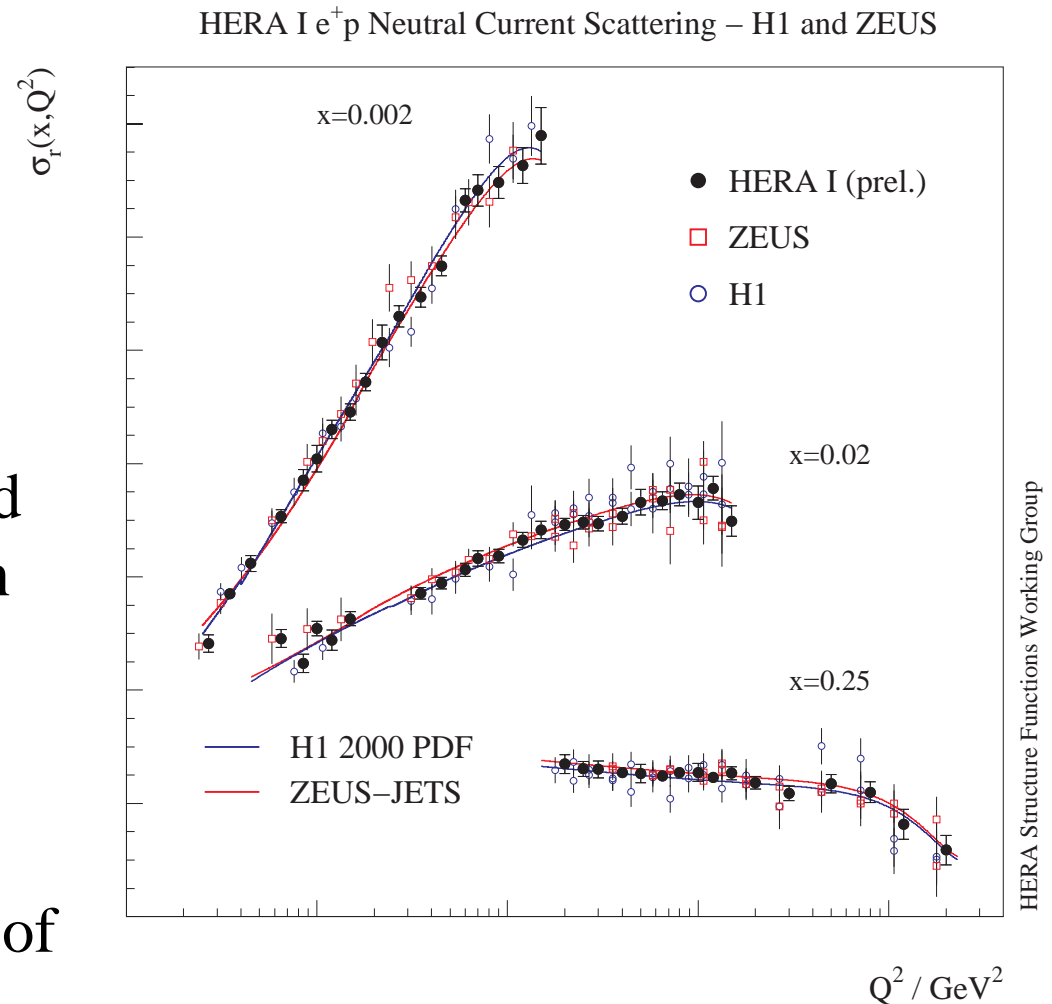
- ◆ Again, consistent with pQCD prediction.

# Combining H1 and ZEUS cross sections

All HERA-I inclusive DIS cross sections from H1 and ZEUS are combined by averaging.

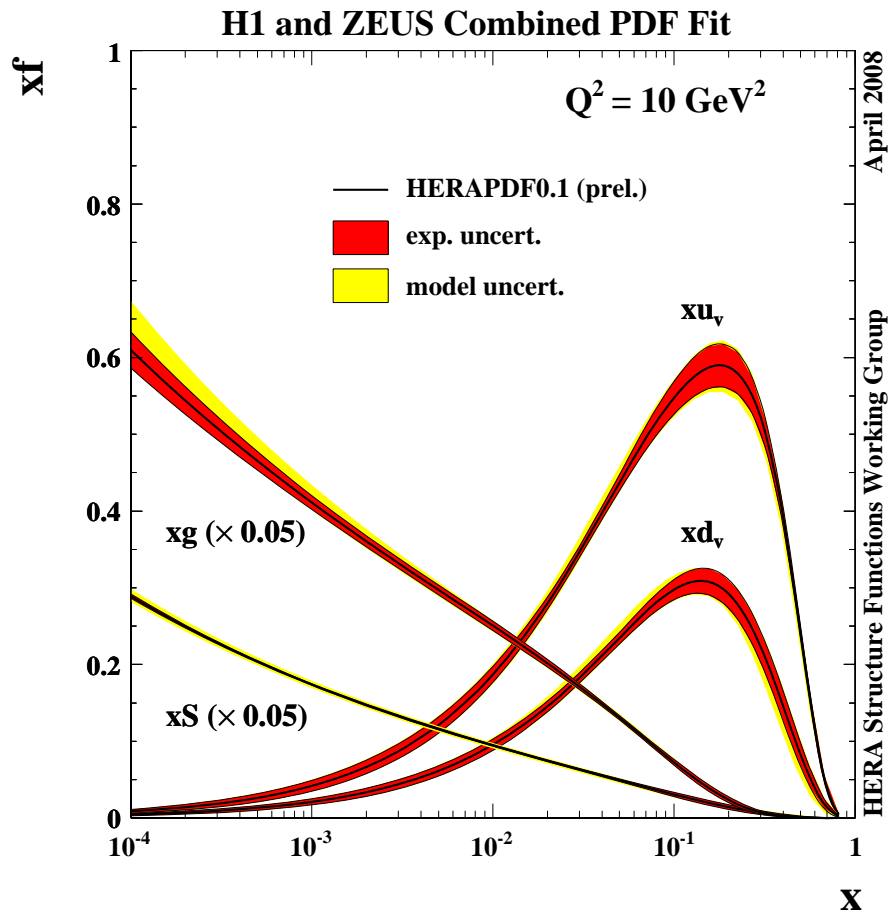
- ◆ Averaged each data point by simultaneous  $\chi^2$  fit.
  - Assumption:  
H1 and ZEUS measure the same cross sections.
  - taking account of correlated systematics within/between experiments.
- ➔ Cross calibration  
Reduction of sys. errors.
- ◆ It is also an consistency check of two experiments.

Uncertainty gets improved by more than  $\sqrt{2}$ .



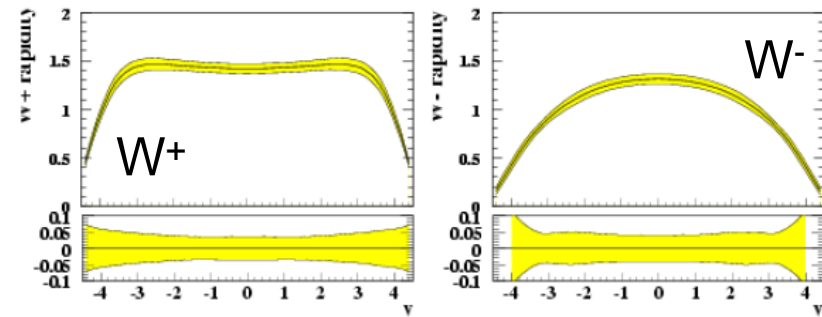
# PDFs from combined cross sections

- ◆ QCD-Fit on combined cross section.
  - Good constraint on PDFs.



## W rapidity @ LHC

A. M. Cooper-Sarker



ZEUS  
-JETS

HERA  
PDF0.1

\* Not include model uncert.

- ◆ HERA PDFs have strong impact on W/Z physics at LHC.
- ◆ Combination is done only for HERA-I. → HERA-II will come.

# Summary

- ◆ During its operation over 15 years, HERA provided plenty of physics through electron-proton collision.
  - Not only the proton structure, but Electroweak and QCD physics.
- ◆ Proton structure has been vigorously investigated at HERA.

We have precise understanding of the proton structure.

  - Steep rise of gluons and Sea quarks at low- $x$
  - Good description by pQCD

→ Good input to LHC!
- ◆ Still, many results from HERA will come up.
  - We can improve our understanding of the proton structure.



**Backup**

# $W_R$ boson

Extrapolation to  $P_e = \pm 1 \rightarrow$  limits on RH  $\sigma_{CC}$

$\sigma_{CC}(e^-p)$ [pb] extrapolated to $P_e = +1$	
H1 (prel.)	$-0.9 \pm 2.9_{\text{stat}} \pm 1.9_{\text{syst}} \pm 2.9_{\text{pol}}$
ZEUS (prel.)	$0.8 \pm 3.1_{\text{stat}} \pm 5.0_{\text{syst+pol}}$

$\sigma_{CC}(e^+p)$ [pb] extrapolated to $P_e = -1$	
H1 (pub.)	$-3.9 \pm 2.3_{\text{stat}} \pm 0.7_{\text{syst}} \pm 0.8_{\text{pol}}$
ZEUS (pub.)	$7.4 \pm 3.9_{\text{stat}} \pm 1.2_{\text{syst+pol}}$

95% CL on heavy  $W_R$  boson

- ◆  $M_{WR} > 208 \text{ GeV}$  (H1, e+p)
- ◆  $M_{WR} > 186 \text{ GeV}$  (H1, e-p)
- ◆  $M_{WR} > 180 \text{ GeV}$  (ZEUS, e-p)

assuming  $g_L = g_R$  and  $\nu_R$  is light

# Chi2 definition for averaging

Fit for data points (554 of them)

And  $j$  systematic uncertainties

$$\chi_e^2(\{\mu\}, \{r\}) = \sum_{i=1}^N \left( \frac{m_i^e - \mu_i - \sum_{j=1}^{Ke} \beta_{ji}^e r_j^e}{\sigma_i^e} \right)^2 + \sum_{j=1}^{Ke} (r_j^e)^2$$

$m_i^e$  = measured cross section in bin  $i$  by exp  $e$

$\mu_i^e$  = true cross section in bin  $i$

$\sigma_i^e$  = statistical uncertainty in bin  $i$  by exp  $e$

$\beta_{ji}^e$  = correlated syst. unc. in bin  $i$  by exp  $e$

$s_i, r_j \sim N(0,1)$

# $\alpha_s$ measurement

