Measurement of the inclusive ν_{μ} charged current cross section on iron and hydrocarbon in the T2K on-axis neutrino beam

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We report a measurement of the ν_{μ} inclusive charged current cross sections on iron and hydrocarbon in the T2K on-axis neutrino beam. The measured inclusive charged current cross sections on iron and hydrocarbon averaged over the T2K on-axis flux with a mean neutrino energy of 1.51 GeV are $(1.444 \pm 0.002(stat.)^{+0.189}_{-0.157}(syst.)) \times 10^{-38} \text{cm}^2/\text{nucleon}$, and $(1.379 \pm 0.009(stat.)^{+0.178}_{-0.147}(syst.)) \times 10^{-38} \text{cm}^2/\text{nucleon}$, respectively, and their cross section ratio is $1.047 \pm 0.007(stat.) \pm 0.035(syst.)$. These results agree well with the predictions of neutrino interaction model and thus demonstrate the correct treatment of the nuclear effect for iron and hydrocarbon targets in the model.

I. INTRODUCTION

The T2K (Tokai-to-Kamioka) experiment is a long baseline neutrino oscillation experiment [1] whose primary goals are precise measurements of the appearance of electron neutrinos and the disappearance of muon neutrinos. An almost pure intense muon neutrino beam is produced at J-PARC (Japan Proton Accelerator Research Complex) in Tokai. The proton beam impinges on a graphite target to produce charged pions, which are focused by three magnetic horns [2]. The pions decay mainly into muon - muon-neutrino pairs during their passage through the 96-meter decay volume. The neutrinos are measured by the near detectors (INGRID [3] and ND280 [4–8]) in J-PARC and the far detector (Super-Kamiokande [9]) in Kamioka, located 295km away from J-PARC (Fig. 1).

A precise neutrino oscillation measurement requires good knowledge of neutrino interaction cross sections. The neutrino charged current (CC) interaction is especially important for neutrino oscillation measurements because the neutrino flavor is identifiable via the CC interaction. Charged current neutrino-nucleon interactions at neutrino energies around 1 GeV have been studied in the past predominantly on deuterium targets [10, 11]. Many modern neutrino oscillation experiments use heavier targets like carbon, oxygen and iron. Nuclear effects are large for those targets and, consequently, they cause large systematic uncertainties for the neutrino oscillation measurement. Therefore, it is therefore important to measure and understand these interactions to minimize systematic uncertainties for the neutrino oscillation measurement.

In this paper, we present measurements of the inclusive muon neutrino charged current cross section on iron and hydrocarbon and their cross section ratio at neutrino energies around 1 GeV using the INGRID detector. INGRID is located on the beam center axis and consists of 16 standard modules and an extra module called

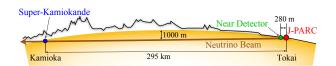


FIG. 1. Overview of the T2K experiment.

the Proton Module. Iron (Fe) makes up 96.2% of the target mass in the standard module, and hydrocarbon (CH) makes up 98.6% of the target mass in the Proton Module. Thus, the ν_{μ} CC inclusive cross sections on Fe and CH are calculated from the number of selected CC events in the standard module and the Proton Module respectively. The ν_{μ} CC inclusive cross section on Fe at neutrino energies above 3.5GeV was measured by the MINOS experiment [12], however that around 1 GeV had never been measured. Although the ν_{μ} CC inclusive cross section on CH around 1 GeV was already measured by the T2K off-axis near detector ND280 [13] and other experiments[14, 15], the Proton Module can measure the cross section for higher energy neutrinos than the ND280 measurement, because the energy distribution of the onaxis neutrinos is higher than that of the off-axis neutrinos (the average energies of the on-axis and off-axis neutrinos are 1.51 GeV and 0.85 GeV, respectively). We also measured the ν_{μ} CC inclusive cross section ratio on Fe to CH using a central standard module and the Proton Module. The central standard module and the Proton Module are on the central axis of the beam and are exposed to the same neutrino beam. Thus, this cross section ratio can be measured very precisely, since many of the large systematic errors from uncertainties on the neutrino flux and neutrino interactions will be cancelled between the two detectors. Therefore, it can provide a good test of the target dependence of the nuclear effect. Recently, the MINER ν A experiment measured the cross section ratio at neutrino energies of 2–20 GeV [16]. We can provide a result of the cross section ratio at a lower energy.

T2K collected data corresponding to 6.57×10^{20} protons on target (POT) during the four run periods listed in Table I, with which $\nu_{\mu} \rightarrow \nu_{e}$ appearance was observed [17]. During this time period, INGRID recorded more than 99.5% of the delivered beam data. A subset of data corresponding to 0.21×10^{20} POT from Run3 was collected with the magnetic horns operating at 205 kA instead of the nominal value of 250 kA. The Run3 periods with the magnetic horns operating at 205 kA and 250 kA are referred to as Run3b and Run3c, respectively. For the cross section measurement, data from Run1, in which the Proton Module was not installed, and Run3b are not used. The total data set for the cross section measurement corresponds to 6.04×10^{20} POT.

TABLE I. T2K data-taking periods and integrated protons on target (POT).

Run period	Dates	Integrated POT
Run 1	Jan. 2010 - Jun. 2010	0.32×10^{20}
Run 2	Nov. $2010 - Mar. 2011$	1.11×10^{20}
Run 3b	Mar. 2012	0.22×10^{20}
Run 3c	Apr. $2012 - Jun. 2012$	1.37×10^{20}
Run 4	Oct. 2012 - May. 2013	3.56×10^{20}

The remainder of this paper is organized as follows: Details of the INGRID detector and Monte Carlo sim-

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ulations are explained in Sec. II and III, respectively. Section IV summarizes the CC-inclusive event selection. The analysis method of the cross section measurement is described in Sec. V. Section VI describes the systematic errors. The results and conclusions are given in Sec. VII and VIII, respectively.

II. DETECTOR CONFIGURATION

The INGRID (Interactive Neutrino GRID) detector is an on-axis neutrino near detector located 280m downstream of the proton target. It consists of 16 identical standard modules and an extra module called Proton Module.

A. INGRID standard modules

The main purpose of the INGRID standard modules is to monitor the neutrino beam direction with a precision better than 1 mrad. The spatial width (1σ) of the neutrino beam at the location of INGRID is about 5 m. In order to cover a large enough region to see a full beam profile, INGRID is designed to sample the beam in a transverse section of 10 m×10 m, with 14 identical modules arranged in two identical groups along the horizontal and vertical axes, as shown in Fig. 2. Two separate modules are placed off the main cross to monitor the asymmetry of the beam. Each of the modules consists of nine iron target plates and eleven tracking scintillator planes, as shown in Fig. 3 left. They are surrounded by veto scintillator planes (Fig. 3 right) to reject charged particles coming from outside of the modules. The dimensions of each iron target plate are 124×124 cm² in the horizontal and vertical directions and 6.5 cm along the beam direction. The total iron mass serving as a neutrino interaction target is 7.1 tons per module. Each tracking scintillator plane consists of two scintillator layers. Each layer has 24 scintillator bars whose dimensions are $5\text{cm}\times1\text{cm}\times120\text{cm}$, making a plane of $120\times120\text{cm}^2$ in the horizontal and vertical directions and 1.0 cm along the beam direction. One layer is placed perpendicular to the other layer in a tracking scintillator plane so that it is sensitive to both horizontal and vertical positions. The veto scintillator plane consists of one scintillator layer which is made up of 22 scintillator bars segmented along the beam direction, in order to identify the incoming charged particles produced by neutrino interactions in the walls of the detector hall. Scintillation light is collected and transported to a photodetector with a wavelength shifting fiber (WLS fiber) which is inserted in a hole at the center of the scintillator strip. The light is read out by a Multi-Pixel Photon Counter (MPPC) [18, 19] attached to one end of the WLS fiber. The electrical signal from each MPPC is digitalized to integrated charge and timing information by the Trip-t front-end board (TFB) [20]. The integration cycle is synchronized with the neutrino

beam pulse structure. For the cross section measurement, only the horizontal central module was used because it is on the same beam axis as the Proton Module and provides a good cancellation of the systematic errors with the Proton Module. Details of the components and the basic performance of the INGRID standard modules are described in Ref [3].

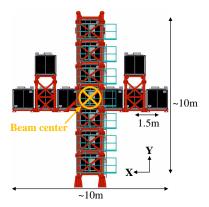


FIG. 2. Overview of the 16 INGRID standard modules viewed from beam upstream.

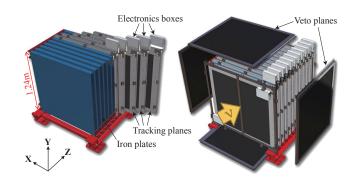


FIG. 3. Exploded view of an INGRID standard module. It consists of iron target plates and tracking scintillator planes (left), and it is surrounded by veto scintillator planes (right).

B. INGRID Proton Module

The Proton Module is an extra module located at the beam center between the horizontal and vertical standard modules (Fig. 4). It is a fully-active tracking detector which consists of only scintillator bars. It was constructed and additionally installed between Run1 and Run2. The purpose of this Proton Module is to separate the neutrino interaction channels by detecting the protons and pions together with the muons from the neutrino interactions, and to measure the neutrino cross section for each interaction channel.

It consists of 36 tracking layers surrounded by veto planes, where each tracking layer is an array of two types of scintillator bars (Fig. 5). The 16 bars in the inner region have dimensions of 2.5cm×1.3cm×120cm while the 16 bars in the outer region have dimensions of $5\text{cm}\times1\text{cm}\times120\text{cm}$, making a layer of $120\times120\text{cm}^2$ in the horizontal and vertical directions. The former is the scintillator produced for the K2K SciBar detector [21] and the latter was produced for INGRID. The tracking layers are placed perpendicular to the beam axis at 23mm intervals. Since the bars are aligned in one direction. a tracking layer is sensitive to either the horizontal or vertical position of the tracks. The tracking layers are therefore placed alternating in perpendicular directions so that three-dimensional tracks can be reconstructed. The tracking layers also serve as the neutrino interaction target. As with the standard modules, scintillation light is read out by a WLS fiber and MPPC, and electrical signal from MPPC is digitalized by TFB. The INGRID horizontal modules which lie downstream of the Proton Module are used to identify muons from the neutrino interactions in the Proton Module.

III. MONTE CARLO SIMULATION

The INGRID Monte Carlo (MC) simulation consists of three main parts. The first is a simulation of the neutrino beam production, which predicts the neutrino flux and energy spectrum of each neutrino flavor. The second is a neutrino interaction simulation, which is used to calculate the neutrino interaction cross sections and the kinematics of the final state particles taking into account the intranuclear interactions of hadrons. The third step is a detector response simulation which reproduces the final-state particles' motion and interaction with material, scintillator light yield, and the response of the WLS fibers, MPPCs, and front-end electronics.

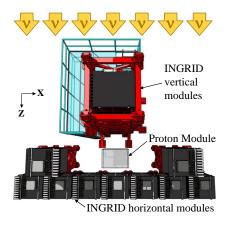


FIG. 4. The position of the Proton Module viewed from above.

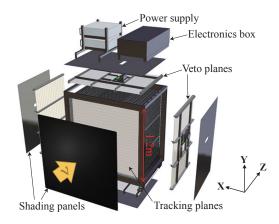


FIG. 5. Exploded view of the Proton Module.

A. Neutrino beam prediction

To predict the neutrino fluxes and energy spectra, a neutrino beam Monte Carlo simulation, called JNUBEAM [22], was developed based on the GEANT3 framework [23]. We compute the neutrino beam fluxes starting from models (FLUKA2008 [24, 25] and GCALOR [26]) and tune them using existing hadron production data (NA61/SHINE [27, 28], Eichten et al. [29] and Allaby et al. [30]). The predicted neutrino energy spectra at the center of INGRID are shown in Fig. 6. Energy spectra 10 m upstream of INGRID are predicted with the same procedure in order to simulate the background events from neutrino interactions in the walls of the experimental hall.

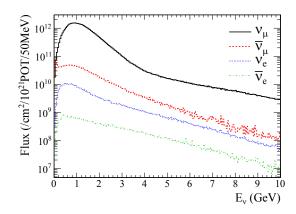


FIG. 6. Neutrino energy spectrum for each neutrino species at the central module predicted by JNUBEAM.

B. Neutrino interaction simulation

Neutrino interactions with nuclear targets are simulated with the NEUT program library [31] which has

been used in the Kamiokande, Super-Kamiokande, K2K, SciBooNE, and T2K experiments. NEUT simulates neutrino interactions with nuclear targets such as protons, oxygen, carbon, and iron, in the neutrino energy range from 100 MeV to 100 TeV. Both the primary neutrino interactions in nuclei and the secondary interactions of the hadrons in the nuclear medium are simulated. Additionally, a cross section prediction by a different neutrino interaction simulation package, GENIE [32], is used for comparison. In both NEUT and GENIE, the following neutrino interactions in both charged current (CC) and neutral current (NC) are simulated:

- quasi-elastic scattering $(\nu + N \rightarrow \ell + N')$
- resonant π production $(\nu + N \to \ell + \pi + N')$
- coherent π production $(\nu + A \rightarrow \ell + \pi + A')$
- deep inelastic scattering $(\nu + N \to \ell + N' + \text{hadrons})$

where N and N' are the nucleons (proton or neutron), ℓ is the lepton, m is the meson and A is the nucleus. Both simulators use the Llewellyn Smith formalism [33] for quasi-elastic scattering, the Rein-Sehgal model [34, 35] for single meson production and coherent π production and GRV98 (Glück-Reya-Vogt-1998) [36] parton distributions with Bodek-Yang modifications [37, 38] for deep inelastic scattering. However, the actual models used in our simulation have many differences from above original models, such as set values of the axial mass, the treatment of nuclear effects, descriptions of the non-resonant inelastic scattering, etc. More details about the simulators used are described in Ref [13]. Figure 7 shows the neutrino-nucleus cross sections per nucleon divided by the neutrino energy predicted by NEUT.

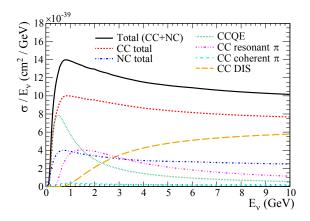


FIG. 7. Neutrino-nucleus cross sections per nucleon of carbon nucleus divided by the neutrino energy predicted by NEUT.

C. INGRID detector response simulation

The INGRID detector simulation was developed using the Geant4 framework [39]. It models the real de-

tector structures (geometries, materials). The structure of the walls of the experimental hall is also modeled to simulate background events from neutrino interactions in the walls. The particles' motion and physics interactions with the materials are simulated, and the energy deposit of each particle inside the scintillator is stored. Simulations of hadronic interactions are performed with the QGSP BERT physics list [40]. The energy deposit is converted into the number of photons. Quenching effects of the scintillation are modeled based on Birks' law [41, 42]. The effect of collection and attenuation of the light in the scintillator and the WLS fiber is modeled based on the results of electron beam irradiation tests. The non-linearity of the MPPC response is also taken into account, since the number of detectable photoelectrons is limited by the number of MPPC pixels. The number of photoelectrons is smeared according to statistical fluctuations and electrical noise. The dark count of the MPPCs is added with a probability calculated from the measured dark rate. Because the response of the ADCs on front-end electronics is not linear, its response is modeled based on the results of a charge injection test.

IV. EVENT SELECTION

A. Event selection for the Proton Module

A neutrino charged current interaction in the Proton Module is identified by a track from the fiducial volume of the Proton Module to the standard horizontal modules located behind the Proton Module, where the standard modules are used to identify a long muon track. First, hits are clustered by timing. A pre-selection is applied to reject accidental noise events. Then, tracks are reconstructed using hit information. Next, tracks matched between the Proton Module and the standard module are searched to select long muon tracks. If matched tracks are found, vertexing is applied to identify event pileup. After that, charged particles from outside the module are rejected with veto planes, and the reconstructed event vertex is required to be inside the fiducial volume (FV). The event selection criteria are described in the following subsections.

1. Time clustering

When there are four or more hits in a 100 nsec time window, all hits within ± 50 nsec of the average time make up a timing cluster.

2. Pre-selection

A tracking plane with at least one hit in both the horizontal and vertical layers is defined as an active plane.

The timing clusters with three or more active planes are selected as shown in Fig. 8.

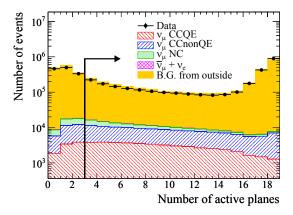


FIG. 8. Number of active planes for the Proton Module. Events with more than two active planes are selected. The background events from the walls of the detector hall is normalized with beam induced muon backgrounds, as described in Sec. IV A 9

3. Two-dimensional track reconstruction

Tracks are reconstructed in the XZ and YZ planes independently. We developed a track reconstruction algorithm based on a cellular automaton. The cellular automaton is the dynamical system which was used for the track reconstruction for the K2K SciBar detector [43], and our track reconstruction algorithm is analogous with it. This algorithm can reconstruct one or more tracks in a timing cluster.

4. Track matching

When two-dimensional tracks are reconstructed in both horizontal central standard module and the Proton Module in the same integration cycle, they are merged if they meet the following four requirements:

- The upstream edge of the standard module track is in either of the most upstream two layers.
- 2. The downstream edge of the Proton Module track is in either of the most downstream two layers.
- 3. The difference between the reconstructed angles of the standard module and Proton Module tracks with respect to z axis is less than 35° .
- 4. At the halfway point between standard module and the Proton Module, the distance between the extrapolated standard module track and the Proton Module track is less than 85mm.

Figure 9 shows an example of a merged track. This track matching is applied to select long muon tracks from CC interactions and reject short tracks caused by neutral particles from outside, like neutrons and gammas which cannot be rejected by a VETO cut, or NC interactions.

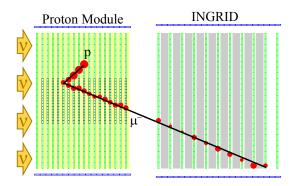


FIG. 9. MC event display of a charged current neutrino event in the Proton Module. Red circles and black lines represent observed hits and reconstructed tracks, respectively. Areas of red circles correspond to light yields.

5. Three-dimensional tracking

Three-dimensional tracks are searched for among pairs of two-dimensional merged tracks in the XZ-plane (X track) and YZ-plane (Y track) according to the following rules. If the difference of the upstream Z point of an X track and a Y track is smaller than three layers, they are combined into a three-dimensional track. If a two-dimensional X or Y track meets the above condition with more than one two-dimensional Y or X track, the pair of tracks with the smallest difference in the upstream Z point is combined.

6. Vertexing

After the reconstruction of a three-dimensional track, the upstream edge of the three-dimensional track is identified as a reconstructed vertex. If a pair of three-dimensional tracks meet the following conditions, they are identified as tracks coming from a common vertex:

- 1. The sum of the Z position differences between the upstream edges of the two tracks in XZ and YX planes is less than two planes.
- 2. The distance between the upstream edges of the two tracks in the XY-plane is less than 150mm.

This vertexing is performed for all combinations of threedimensional tracks, allowing more than two tracks to be associated with the same reconstructed vertex. The following event selection cuts are applied to every vertex, since each one is expected to correspond to a single neutrino interaction. This means that, as long as the vertices are distinguishable, events with multiple neutrino interactions (event pileup) are handled correctly.

7. Timing cut

The T2K neutrino beam is pulsed. Each pulse has an eight-bunch structure and each bunch has a width of 58 nsec. To reject off-timing events, such as cosmic-ray events, only events within ± 100 nsec from the expected timing in each bunch are selected (Fig.10). The expected timing is calculated from the primary proton beam timing, the time of flight of the particles from the target to INGRID, and the delay of the electronics and cables. The event time is defined by the time of the hit at the start point of the track.

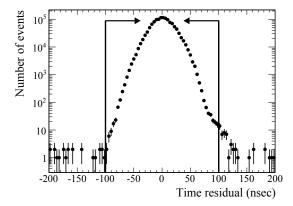


FIG. 10. Time difference between the measured event timing and the expected neutrino event timing for the Proton Module. Events within ± 100 nsec are selected.

8. Veto and fiducial volume (FV) cuts

Two selections are applied to reject incoming particles produced by neutrino interactions in upstream materials. such as the walls of the experimental hall. First, the upstream veto cut is applied. The first tracker plane is used as the front veto plane, and events which have a vertex in the plane are rejected as shown in Fig. 11. The events rejected by this front veto cut are identified as beam induced muon backgrounds. Furthermore, events which have a hit in a side veto plane at the upstream position extrapolated from the reconstructed track are rejected. After the veto cut, a fiducial volume (FV) cut is applied. The FV of each module is defined as a volume within ± 50 cm from the module center in the X and Y directions, and from the third to the sixteenth tracker plane in the Z direction. The ratio of the FV to the total target volume is 58.1%. Events having a vertex inside the FV are selected as shown in Fig. 12.

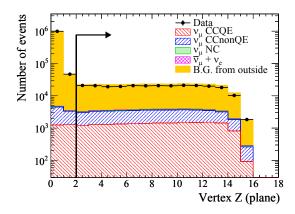


FIG. 11. Vertex Z distribution for the Proton Module before applying the veto and fiducial volume cuts.

9. Summary of the event selection for the Proton Module

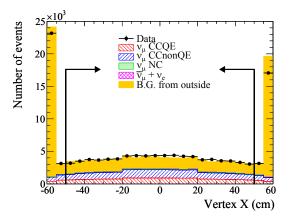
The results of the event selection for the Proton Module are summarized in Table II. Figure 13 shows the vertex distributions in the X, Y and Z directions after all cuts. The MC simulation includes neutrino interactions on the wall of the detector hall. The MC prediction of the beam induced muon backgrounds is 35% smaller than the observation. This is likely due to the uncertainties of the density of the walls, the neutrino flux and the neutrino interaction model. Thus, the number of neutrino interactions on the walls in the MC simulation is normalized by the observed number of the beam induced muon backgrounds.

TABLE II. Number of events passing each selection step for the Proton Module. The MC assumes 6.04×10^{20} POT and uses the nominal NEUT model. The efficiency is defined as the number of selected CC events divided by the number of CC interactions in the FV. The purity is defined as the fraction of the ν_{μ} CC events on CH among the selected events.

Selection	Data		Efficiency	Purity
Vertexing			65.6%	3.9%
Timing cut			65.6%	3.9%
Veto cut	1.281×10^5		53.0%	29.9%
FV cut	3.618×10^4	3.585×10^4	41.2%	89.4%

B. Event selection for the standard module

The event selection for the standard module is the same as that for the Proton Module except for two differences. One is that track matching is not applied for the standard module, and the other is an additional acceptance cut. The event selection for the standard module is as follows. First, time clustering, pre-selection (Fig. 14) and two-dimensional track reconstruction are applied as



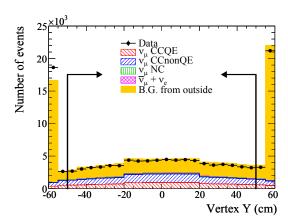


FIG. 12. Vertex X and Y distributions for the Proton Module after applying the veto cut. A volume within ± 50 cm in the X and Y directions from the module center is defined as fiducial volume (FV). Most of the background events which pass the FV cut in one direction (X or Y) are actually rejected by the FV cut in the other direction (Y or X).

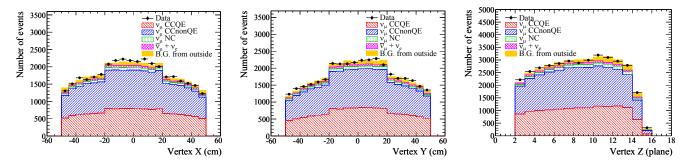


FIG. 13. Vertex X, Y and Z distributions for the Proton Module following event selection. There are jumps at X or Y = ± 20 cm because the Proton Module uses thicker scintillators in the inner region (-20cm $\sim +20$ cm).

with the Proton Module. When the tracks are reconstructed, three-dimensional tracking is done for all reconstructed tracks, while it is done only for the merged tracks in the case of the Proton Module. Then, the vertexing, timing cut (Fig. 15), and veto and fiducial volume cuts (Fig. 16) are applied as with the Proton Module. The ratio of the FV to the total target volume is 61.7% for the standard modules. CC interactions in the standard module can be selected with sufficiently high purity by the above event selection. However, there are large differences in the selection efficiency between the standard module and the Proton Module, as shown in Fig. 17. This is because the acceptance of the Proton Module is limited by the required track matching with the standard module. These differences enlarge the systematic error on the measurement of the CC-inclusive cross section ratio on Fe to CH. To minimize this difference, the following acceptance cut is added to the event selection for the standard module. First, an imaginary standard module is defined directly behind the standard module. The distance between the standard module and the imaginary module is the same as that between the Proton Module and the standard module. The reconstructed tracks are then extended further downstream, even if the track has stopped in the module. If no tracks

from the vertex reach the imaginary module, the event is rejected as shown in Fig.18. After applying this acceptance cut, the difference in the selection efficiencies between the standard module and the Proton Module is greatly reduced, as shown in Fig. 17. The results of the event selection are summarized in Table III. Figure 19 shows the vertex distributions in the X, Y and Z directions after all cuts. As with the Proton Module, the number of neutrino interactions on the walls in the MC simulation is normalized with the beam induced muon backgrounds.

C. Event pileup correction

When a track from a neutrino event piles up with a track from another neutrino event, vertices may fail to be reconstructed. Because this results in the loss of events, this event-pileup effect needs to be corrected for. The event-pileup effect is proportional to the beam intensity. Hence, the correction factor is estimated as a linear function of the beam intensity. The slope of the linear function is estimated from beam data as follows. First, the beam data is categorized into sub-samples according to the beam intensity. In each sub-sample, all

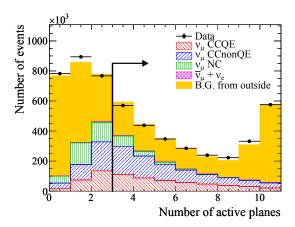


FIG. 14. Number of active planes for the standard module. Events with more than two active planes are selected.

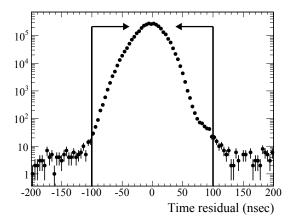


FIG. 15. Time difference between the measured event timing and expected neutrino event timing for the standard module. Events within ± 100 nsec are selected.

hits in INGRID from two beam bunches are summed together to make one new pseudo beam bunch. This procedure effectively doubles the beam intensity observed by INGRID. A slope is estimated from the number of selected events in an original beam bunch and the a pseudo beam bunch for each sub-sample. The slopes estimated from all sub-samples are consistent with each other, and the average value of this slope is used for the correction. This event pileup correction is applied module-by-module and bunch-by-bunch using the slope and POT per bunch which corresponds to the relevant beam intensity. The event pileup correction gives 0.85% and 0.40% differences in the number of selected events in the standard module and the Proton Module respectively.

V. ANALYSIS METHOD

The flux-averaged ν_{μ} CC inclusive cross section is calculated from the number of selected events using the

TABLE III. Number of events passing each selection step for the standard module. The MC assumes 6.04×10^{20} POT and uses the nominal NEUT model. The efficiency is defined as the number of selected CC events divided by the number of CC interactions in the FV. The purity is defined as the fraction of the ν_{μ} CC events on Fe among the selected events.

Selection	Data	MC	Efficiency	Purity
Vertexing		3.194×10^6	96.7%	35.9%
Timing cut		3.194×10^{6}	96.7%	35.9%
Veto cut		1.418×10^{6}	88.8%	74.2%
FV cut	8.875×10^{5}	9.169×10^{5}	74.4%	86.6%
Acceptance cut	5.185×10^5	5.130×10^5	42.7%	88.8%

background subtraction and efficiency correction:

$$\sigma_{\rm CC} = \frac{N_{\rm sel} - N_{\rm BG}}{\phi T \varepsilon},\tag{1}$$

where $N_{\rm sel}$ is the number of selected events from real data, $N_{\rm BG}$ is the number of selected background events predicted by MC simulation, ϕ is the integrated ν_{μ} flux, T is the number of target nucleons, and ε is the detection efficiency for CC events predicted by MC simulation. The ν_{μ} CC inclusive cross sections on Fe and CH are measured from the number of selected events in the standard module and the Proton Module, respectively. The ν_{μ} CC inclusive cross section ratio on Fe to CH is measured using the results from both detectors. The background events for this analysis consist of NC events, $\bar{\nu}_{\mu}$ events, ν_{e} events, interactions on elements other than the measuring elements in the detector (Ti or O for the Proton Module, C or H for the standard module), and background events created by neutrino interactions in the material surrounding the detector. The expected breakout of the selected events are summarized in Table IV. The rate of the background events from outside for the Proton Module is much larger than that for the standard module. It is because the number of neutrino interactions in the Proton Module is much smaller than that in the standard module while the number of background events from outside is comparable level. $N_{\rm BG}$, ϕ , and ε are estimated using MC simulation and T is calculated from the target mass measured prior to detector assembly. These quantities are summarized in Table V.

VI. SYSTEMATIC ERRORS

Uncertainties on $N_{\rm BG}$, ϕ , T, and ε are sources of systematic errors on the cross section results. The sources of systematic error can be categorized into three groups: those from the neutrino flux prediction, the neutrino interaction model including intra-nuclear interactions, and the detector response.

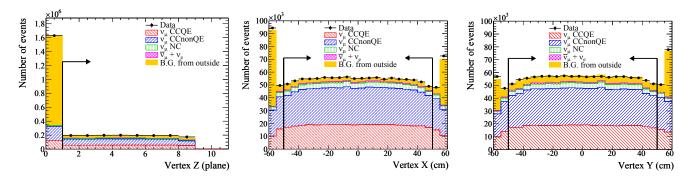


FIG. 16. Vertex Z distribution for the standard module before applying the veto and fiducial volume cuts (left) and vertex X and Y distributions after applying the veto cut (center and right).

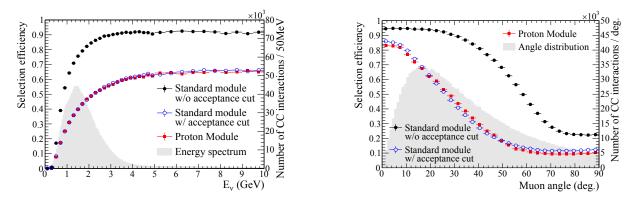


FIG. 17. Event selection efficiency of CC interactions for the standard module and the Proton Module as a function of true neutrino energy (left) and true muon scattering angle (right). The energy spectrum and angle distribution of the CC interactions in the standard module are overlaid.

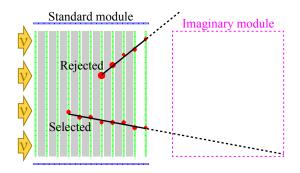


FIG. 18. MC event display of a selected event and a rejected event by the acceptance cut.

TABLE IV. Expected breakout of the selected events. The CCQE and CCnonQE events are signal events and others are background events for this measurement.

	Standard module	Proton Module
CCQE events	35.34%	34.90%
CCnonQE events	51.70%	50.53%
NC events	6.44%	4.19%
$\bar{\nu}_{\mu}$ events	2.04%	2.39%
ν_e events	0.99%	0.73%
Other target element	2.67%	1.39%
Backgrounds from outside	0.82%	5.87%

A. Neutrino flux uncertainties

The neutrino flux uncertainty sources can be separated into two categories: hadron production uncertainties and T2K beamline uncertainties. The uncertainties on hadron production are mainly driven by the NA61/SHINE measurements [27, 28] and the Eichten and Allaby data [29, 30], and constitute the dominant component of the flux uncertainty. They include the uncertainties on the production cross section, the secondary nu-

TABLE V. Summary of the inputs for the cross section calculation.

	BCI	N_{BG}	ϕ	T	ε
			$2.999 \times 10^{13} \text{cm}^{-2}$		
$\sigma_{ m CC}^{ m CH}$	36330	5385.5	$3.025 \times 10^{13} \text{cm}^{-2}$	1.799×10^{29}	0.4122

cleon production, the pion production multiplicity, and the kaon production multiplicity. The second category of flux uncertainties is associated with inherent uncer-

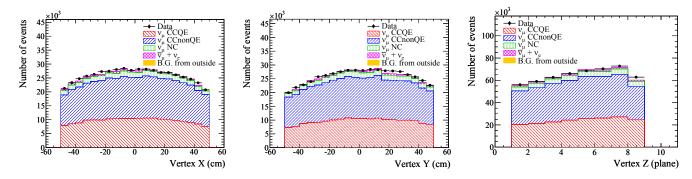


FIG. 19. Vertex X, Y and Z distributions for the standard module following event selection.

tainties and operational variations in the beamline conditions. They include uncertainties in the proton beam position, the off-axis angle, the absolute horn current, the horn angular alignment, the horn field asymmetry, the target alignment, and the proton beam intensity. The method of estimating these flux uncertainties is described in Ref [22]. To evaluate the systematic error from the flux uncertainties, the flux is fluctuated using a covariance matrix produced based on the flux uncertainty. This is repeated for many toy data sets, and the $\pm 1\sigma$ of the change in the cross section result is taken as the systematic error associated with the neutrino flux.

B. Neutrino interaction uncertainties

We use a data-driven method to calculate the neutrino interaction uncertainties, where the NEUT predictions are compared to available external neutrino-nucleus data in the energy region relevant for T2K. We fit some parameters of the models implemented in NEUT, and introduce ad hoc parameters, often with large uncertainties, to take into account remaining discrepancies between NEUT and the external data like [12, 44–55]. The model parameters include axial mass values for quasi-elastic scattering and meson production via baryon resonances, the Fermi momentum, the binding energy, a spectral function parameter, and a π -less Δ decay parameter. NEUT uses the relativistic Fermi gas model as a nuclear model. The spectral function model is more sophisticated, and is known to be a better representation of the nuclear model. A spectral function parameter is introduced to take into account the difference between the two nuclear models. In the resonant pion production process, baryon resonances, mainly Δ , can interact with other nucleons and disappear without pion emissions. The π -less Δ decay parameter is introduced to take into account uncertainties on this process. The implemented ad hoc parameters include cross section normalizations. In addition, uncertainties on the secondary interactions of the pions with the nuclear medium are included. Table VI shows the nominal values and uncertainties on these parameters. The method used to estimate these uncertainties is described in Ref [13]. Systematic errors due to these parameters are estimated from variations of the cross section results when these parameters are varied within their uncertainties. For the measurement of the CC-inclusive cross section ratio on Fe to CH, we assume that the uncertainties of $M_A^{\rm RES},$ CC1 π normalizations, NC normalizations, Fermi gas parameters and pion secondary interactions are fully correlated between the Fe target and the CH target cases because these uncertainties are understood as independent of the target nucleus. By contrast, the uncertainties of $M_A^{\rm QE}$, CCQE normalizations, CC coherent pion normalization and spectral function parameter are assumed to be uncorrelated because nuclear dependences of these uncertainties are not well understood. In addition, the uncertainty of CC other shape is left out of the cross section ratio measurement because there is no evidence for a large nuclear modification in the deep inelastic scattering regime.

C. Detector response uncertainties

The uncertainty of the target mass measurement, 0.13% for the standard module and 0.25% for Proton Module, is taken as the systematic error on the target mass. Variation of the measured MPPC dark rate during data acquisition, 5.84 hits/cycle for the standard module and 11.52 hits/cycle for the Proton Module, is taken as the uncertainty on the MPPC dark rate, where the cycle denotes the integration cycle synchronized with the neutrino beam pulse structure. The discrepancy between the hit detection efficiency measured with beam induced muon backgrounds and that of the MC simulation, 0.17% for the standard module and 0.21% for the Proton Module, is assigned as the uncertainty in the hit detection efficiency. The relation between these quantities and the cross section results are estimated by MC simulation, and variations on the calculated cross section results due to these uncertainties are assigned as systematic errors. The event pileup correction factor has uncertainties which come from the statistics of the beam data and the MPPC dark count in the estimation of the correction factor. The systematic error from these uncertainties is

TABLE VI. The nominal values of and the uncertainties on the neutrino interaction model parameters. First, second, and third groups represent the model parameters, the ad hoc parameters, and the pion secondary interaction parameters. Nominal values of 0 or 1 mean that the effect or the normalization is not implemented or is implemented by default, respectively.

Parameter	Nominal value	Error
$M_A^{ m QE}$	$1.21 \mathrm{GeV}$	16.53%
$M_A^{ m \hat{RES}}$	$1.21 { m GeV}$	16.53%
π less Δ decay	0.2	20%
Spectral function	0	100%
Fermi momentum for Fe	250 MeV/c	12%
Fermi momentum for CH	217 MeV/c	13.83%
Binding energy for Fe	$33 \mathrm{MeV}$	27.27%
Binding energy for CH	$25 \mathrm{MeV}$	36%
CCQE norm. $(E_{\nu} < 1.5 \text{GeV})$	1	11%
CCQE norm. $(1.5 < E_{\nu} < 3.5 \text{GeV})$	1	10%
CCQE norm. $(E_{\nu} > 3.5 \text{GeV})$	1	10%
$CC1\pi$ norm. $(E_{\nu} < 2.5 \text{GeV})$	1	21%
$CC1\pi$ norm. $(E_{\nu} > 2.5 \text{GeV})$	1	21%
CC coherent π norm.	1	100%
CC other shape	0	40%
$NC1\pi^0$ norm.	1	31%
NC coherent π norm.	1	30%
$NC1\pi^{\pm}$ norm.	1	30%
NC other norm.	1	30%
Pion absorption	1	50%
Pion charge exchange (low energy)	1	50%
Pion charge exchange (high energy)	1	30%
Pion QE scattering (low energy)	1	50%
Pion QE scattering (high energy)	1	30%
Pion inelastic scattering	1	50%

estimated assuming the highest beam intensity achieved in beam operation so far. There is about a 35% discrepancy between the beam induced muon background rate estimated by the MC simulation and that measured from the data. The change in the background contamination fraction from this discrepancy is taken as the systematic error for the beam-related background. The cosmic-ray background was found to be very small from the out-ofbeam timing data. The systematic error on the track reconstruction efficiency is estimated by comparing the efficiency for several sub-samples between the data and the MC simulation. The standard deviation of the data - MC of the track reconstruction efficiency for the subsamples is taken as the systematic error. The systematic errors from all event selections are evaluated by varying each selection threshold. The maximum difference between the data and MC for each selection threshold is taken as the value of each systematic error.

D. Summary of the systematic errors

Table VII summarizes the systematic errors on each measurement. The total systematic error on the measurements of the CC inclusive cross section on Fe, that on CH, and their ratio are $^{+13.11\%}_{-10.84\%}, ^{+12.91\%}_{-10.69\%},$ and $^{+3.32\%}_{-3.33\%},$ respectively. The neutrino flux error is the dominant systematic error for the measurement of the CC inclusive cross section on Fe and CH. However, it is small for the measurement of the cross section ratio on Fe to CH, since this error mostly cancels between two detectors, as expected.

VII. RESULTS

The measured flux-averaged CC inclusive cross sections on Fe and CH and their ratio are

$$\begin{split} \sigma_{\mathrm{CC}}^{\mathrm{Fe}} &= (1.444 \pm 0.002(stat.)^{+0.189}_{-0.157}(syst.)) \\ &\quad \times 10^{-38} \mathrm{cm}^2/\mathrm{nucleon}, \\ \sigma_{\mathrm{CC}}^{\mathrm{CH}} &= (1.379 \pm 0.009(stat.)^{+0.178}_{-0.147}(syst.)) \\ &\quad \times 10^{-38} \mathrm{cm}^2/\mathrm{nucleon}, \text{ and} \end{split} \tag{2}$$

$$\frac{\sigma_{\text{CC}}^{\text{Fe}}}{\sigma_{\text{CC}}^{\text{CH}}} = 1.047 \pm 0.007(stat.) \pm 0.035(syst.),$$
 (4)

at a mean neutrino energy of 1.51 GeV. These are pure cross sections per nucleon for each atom, and isoscalar corrections are not applied. They agree well with the predicted values from NEUT and GENIE shown in Table VIII. The cross-section results are shown in Fig. 20 and 21 together with the predictions and measurements from other experiments. Our result of the cross section ratio on Fe to CH is very precise in 3% level. Hence, its consistency with the neutrino interaction models demonstrates that the target dependence of the nuclear effect is well understood and correctly treated in the models in 3% level.

In Table IX, the measured CC inclusive cross section on CH and the ratios to the predictions by NEUT and GE-NIE are compared to those for the T2K off-axis neutrinos measured by the ND280 detector. Here, it requires attention that the fluxes for these two detectors are highly correlated. Both the ND280 and INGRID data are in good agreement with both the NEUT and GENIE models.

VIII. CONCLUSIONS

We have reported the first neutrino cross section measurement with the T2K on-axis near neutrino detector, INGRID. We have selected a sample of inclusive ν_{μ} CC interactions in an INGRID standard module and the Proton Module. From the number of selected events, the flux-averaged CC inclusive cross sections on Fe and CH and their ratio at a mean neutrino energy of 1.51 GeV

TABLE VII. Summary of the systematic errors.

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Item	$\sigma_{ m CC}^{ m Fe}$	$\sigma_{ m CC}^{ m CH}$	$\sigma_{ m CC}^{ m Fe}/\sigma_{ m CC}^{ m CH}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		-10.34% + 12.74%		
CCQE normalization ($E_{\nu} < 1.5 \text{GeV}$) -0.82%+0.79% -0.52%+0.50% -0.95%+0.94% CCQE normalization ($E_{\nu} > 3.5 \text{GeV}$) -0.45%+0.50% -0.67%+0.76% -0.88%+0.83% CCQE normalization ($E_{\nu} > 3.5 \text{GeV}$) -0.11%+0.11% -0.10%+0.11% -0.18%+0.15% CCIπ normalization ($E_{\nu} > 2.5 \text{GeV}$) -0.50%+0.52% -0.54%+0.56% -0.04%+0.04% CC coherent π normalization -0.48%+0.49% -1.03%+1.10% -1.20%+1.14% CC other shape -0.82%+0.77% -1.07%+1.02% -0.13%+0.13% NC1π ⁰ normalization -0.02%+0.02% -0.018%+0.18% -0.13%+0.13% NC other normalization -0.02%+0.02% -0.01%+0.01% -0.01%+0.01% NC other normalization -0.31%+0.31% -0.23%+0.23% -0.07%+0.07% NC other normalization -0.12%+1.23% -0.71%+0.72% -0.51%+0.51% π less Δ decay -0.50%+0.54% -0.35%+0.39% -0.15%+0.15% Spectral function -0.76%+0.00% -0.98%+0.00% -0.76%+0.98% Fermi momentum -0.43%+0.49% -0.39%+0.41% -0.04%+0.08% Pion absorption	$M_{\cdot}^{ m QE}$			
CCQE normalization ($E_{\nu} < 1.5 \text{GeV}$) -0.82%+0.79% -0.52%+0.50% -0.95%+0.94% CCQE normalization ($E_{\nu} > 3.5 \text{GeV}$) -0.45%+0.50% -0.67%+0.76% -0.88%+0.83% CCQE normalization ($E_{\nu} > 3.5 \text{GeV}$) -0.11%+0.11% -0.10%+0.11% -0.18%+0.15% CCIπ normalization ($E_{\nu} > 2.5 \text{GeV}$) -0.50%+0.52% -0.54%+0.56% -0.04%+0.04% CC coherent π normalization -0.48%+0.49% -1.03%+1.10% -1.20%+1.14% CC other shape -0.82%+0.77% -1.07%+1.02% -0.13%+0.13% NC1π ⁰ normalization -0.02%+0.02% -0.018%+0.18% -0.13%+0.13% NC other normalization -0.02%+0.02% -0.01%+0.01% -0.01%+0.01% NC other normalization -0.31%+0.31% -0.23%+0.23% -0.07%+0.07% NC other normalization -0.12%+1.23% -0.71%+0.72% -0.51%+0.51% π less Δ decay -0.50%+0.54% -0.35%+0.39% -0.15%+0.15% Spectral function -0.76%+0.00% -0.98%+0.00% -0.76%+0.98% Fermi momentum -0.43%+0.49% -0.39%+0.41% -0.04%+0.08% Pion absorption	$M^{ m RES}$			
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Total $-10.84\% + 13.11\% - 10.69\% + 12.91\% - 3.33\% + 3.32\%$	Total		$-10.69\%{+}12.91\%$	

TABLE VIII. CC-inclusive cross sections on Fe and CH and their ratio predicted by NEUT and GENIE.

$\sigma_{ m CC}^{ m Fe}$	$\sigma_{\mathrm{CC}}^{\mathrm{CH}}$	$\sigma_{ m CC}^{ m Fe}/\sigma_{ m CC}^{ m CH}$
NEUT $1.3977 \times 10^{-38} \text{cm}^2$		
GENIE $1.2407 \times 10^{-38} \text{cm}^2$	$1.1883 \times 10^{-38} \text{cm}^2$	1.04407

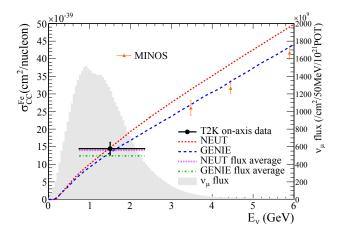
TABLE IX. The CC-inclusive cross section on CH measured with the T2K on-axis and off-axis fluxes and the ratios to the predictions by NEUT and GENIE. The errors represent the total (statistical and systematic) uncertainties.

	On-axis	Off-axis
Average energy	$1.51 \mathrm{GeV}$	$0.85 { m GeV}$
$Data (\times 10^{-38} cm^2)$	$1.379^{+0.178}_{-0.147}$	0.691 ± 0.085
Data/NEUT	$1.023^{+0.132}_{-0.109}$	0.950 ± 0.117
$\begin{array}{c} {\rm Data} \; (\times 10^{-38} {\rm cm}^2) \\ {\rm Data/NEUT} \\ {\rm Data/GENIE} \end{array}$	$1.160^{+0.150}_{-0.124}$	1.057 ± 0.130

ACKNOWLEDGEMENTS

have been measured. These results agree well with the model predictions.

It is a pleasure to thank Mr. Taino from Mechanical Support Co. for helping with the construction of



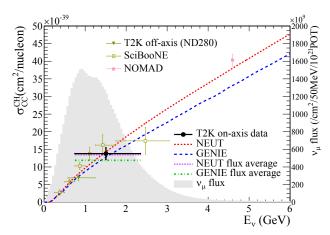


FIG. 20. The inclusive ν_{μ} charged current cross section on Fe (left) and that on CH (right) with predictions by NEUT and GENIE. The isoscalar corrections are not applied to our data or predictions. Our data point is placed at the flux mean energy. The vertical error bar represents the total (statistical and systematic) uncertainty, and the horizontal bar represents 68% of the flux at each side of the mean energy. The MINOS, T2K ND280, SciBooNE and NOMAD results are also plotted[12–15]. Because the isoscalar correction is applied to the MINOS data, it is expected to be shifted by about -2%.

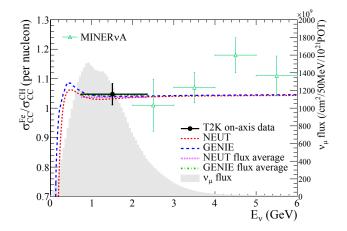


FIG. 21. The inclusive ν_{μ} charged current cross section ratio on Fe to CH with predictions by NEUT and GENIE. The isoscalar corrections are not applied to our data or predictions. Our data point is placed at the flux mean energy. The vertical error bar represents the total (statistical and systematic) uncertainty, and the horizontal bar represents 68% of the flux at each side of the mean energy. The MINER ν A result is also plotted[16].

INGRID. We thank the J-PARC staff for superb accelerator performance and the CERN NA61 collaboration for providing valuable particle production data. We acknowledge the support of MEXT, Japan; NSERC, NRC and CFI, Canada; CEA and CNRS/IN2P3, France; DFG, Germany; INFN, Italy; Ministry of Science and Higher Education, Poland; RAS, RFBR and MES, Russia; MICINN and CPAN, Spain; SNSF and SER, Switzerland; STFC, U.K.; and DOE, U.S.A. We also thank CERN for the UA1/NOMAD magnet, DESY for the HERA-B magnet mover system, and NII for SINET4. In addition participation of individual researchers and institutions has been further supported by funds from: ERC (FP7), EU; JSPS, Japan; Royal Society, UK; DOE Early Career program, U.S.A.

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