

# Colliding frontiers: the search for new physics at the LHC



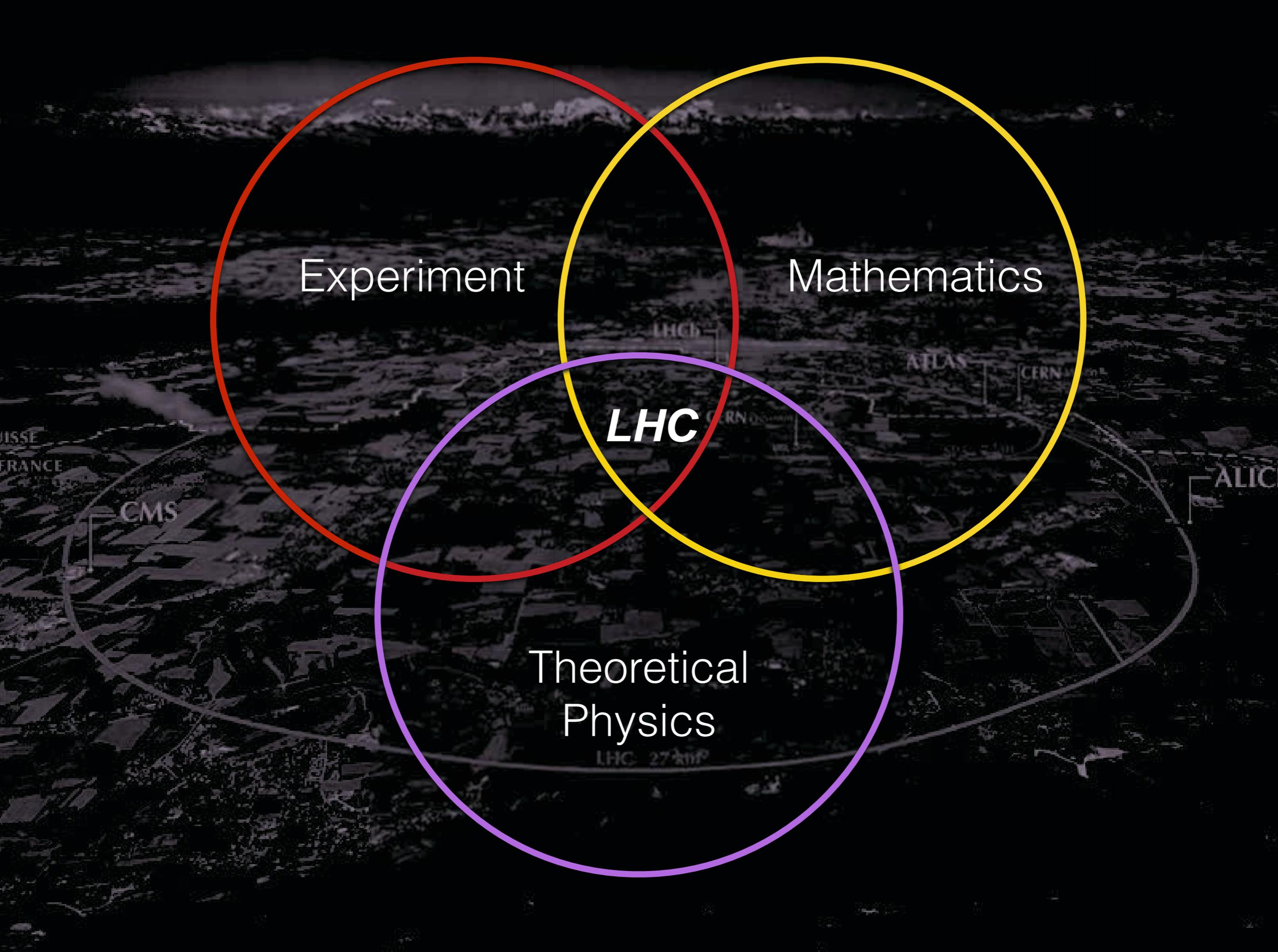
Tom Melia  
Berkeley Theoretical Physics

Experiment

Mathematics

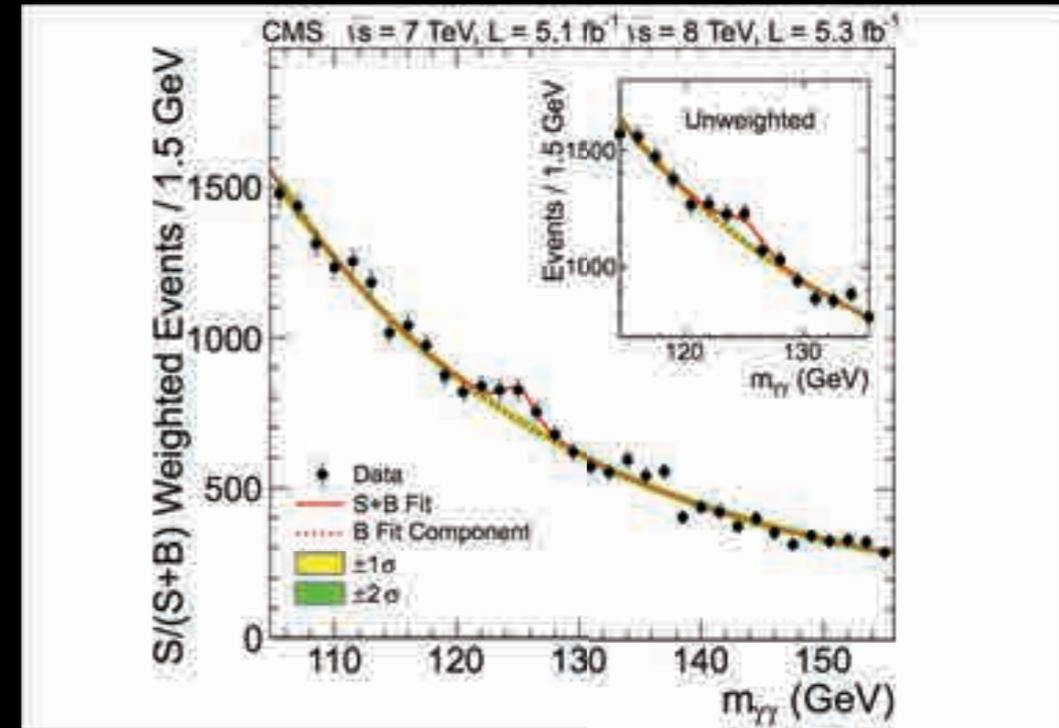
**LHC**

Theoretical  
Physics



# The Large Hadron Collider

Run 1 discovered the Higgs boson and completed the standard model



But there remain unresolved puzzles in our understanding

The origin of the electroweak scale

Three generations

Fermion masses

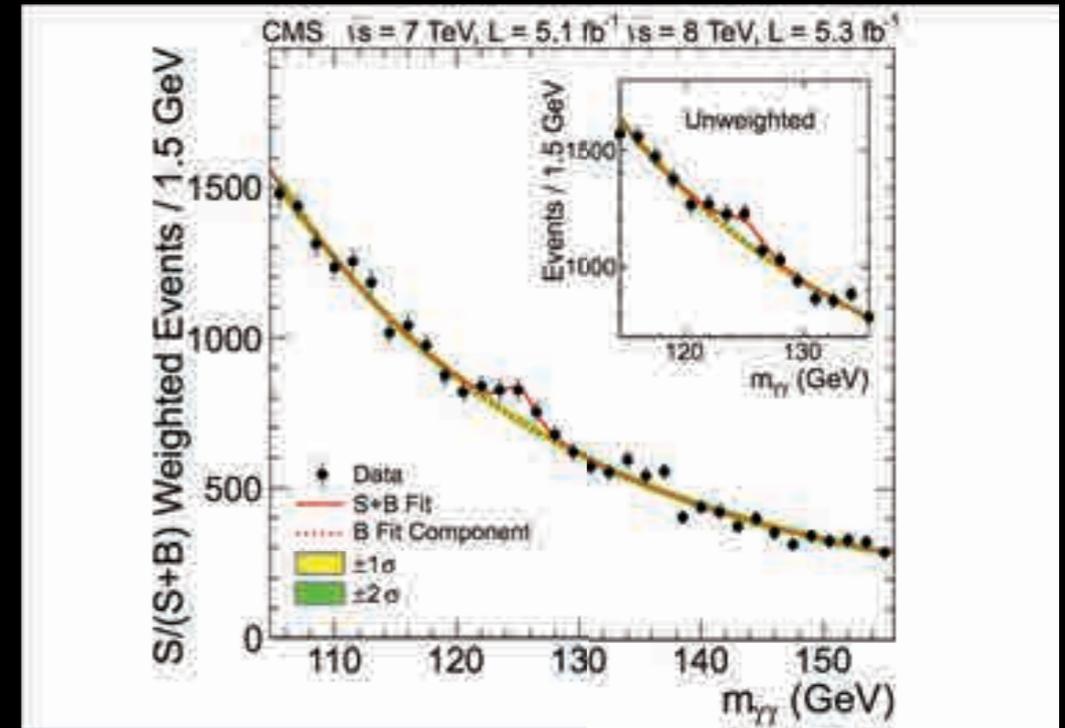
Gauge groups and charges

QCD theta angle

...

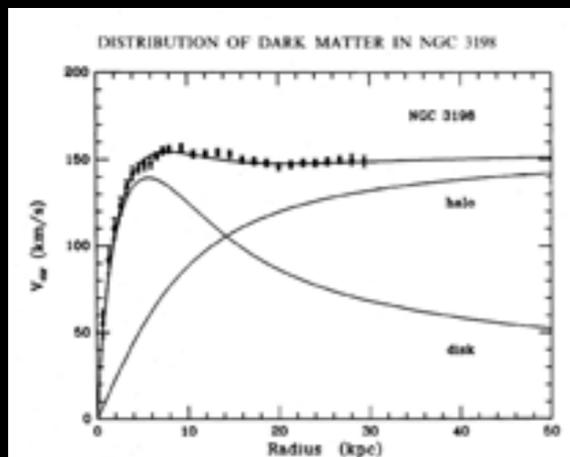
# The Large Hadron Collider

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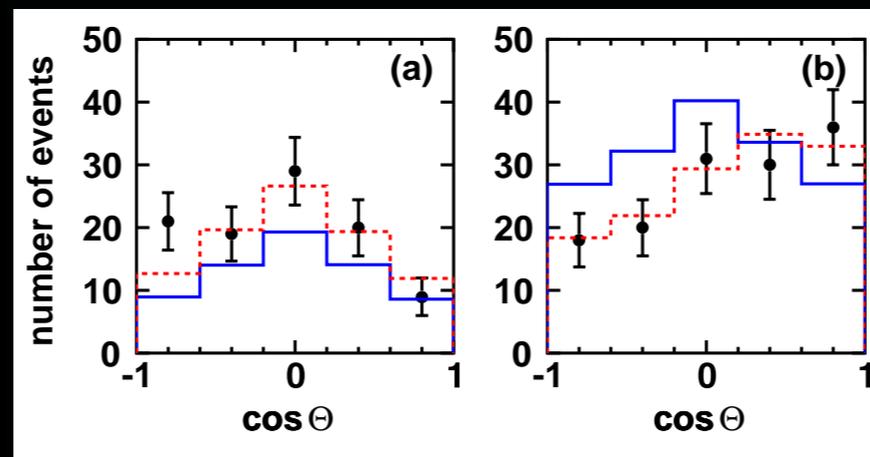


But there remain unresolved puzzles in our understanding

Dark matter



Neutrino masses



Gravity

...

# The Large Hadron Collider

Run 2 and beyond at the LHC will be a driving force in the search for new physics

What we discover will shape our ideas about nature and the future of our field

# An LHC path to new physics

New particle produced  
at the LHC?

yes

no

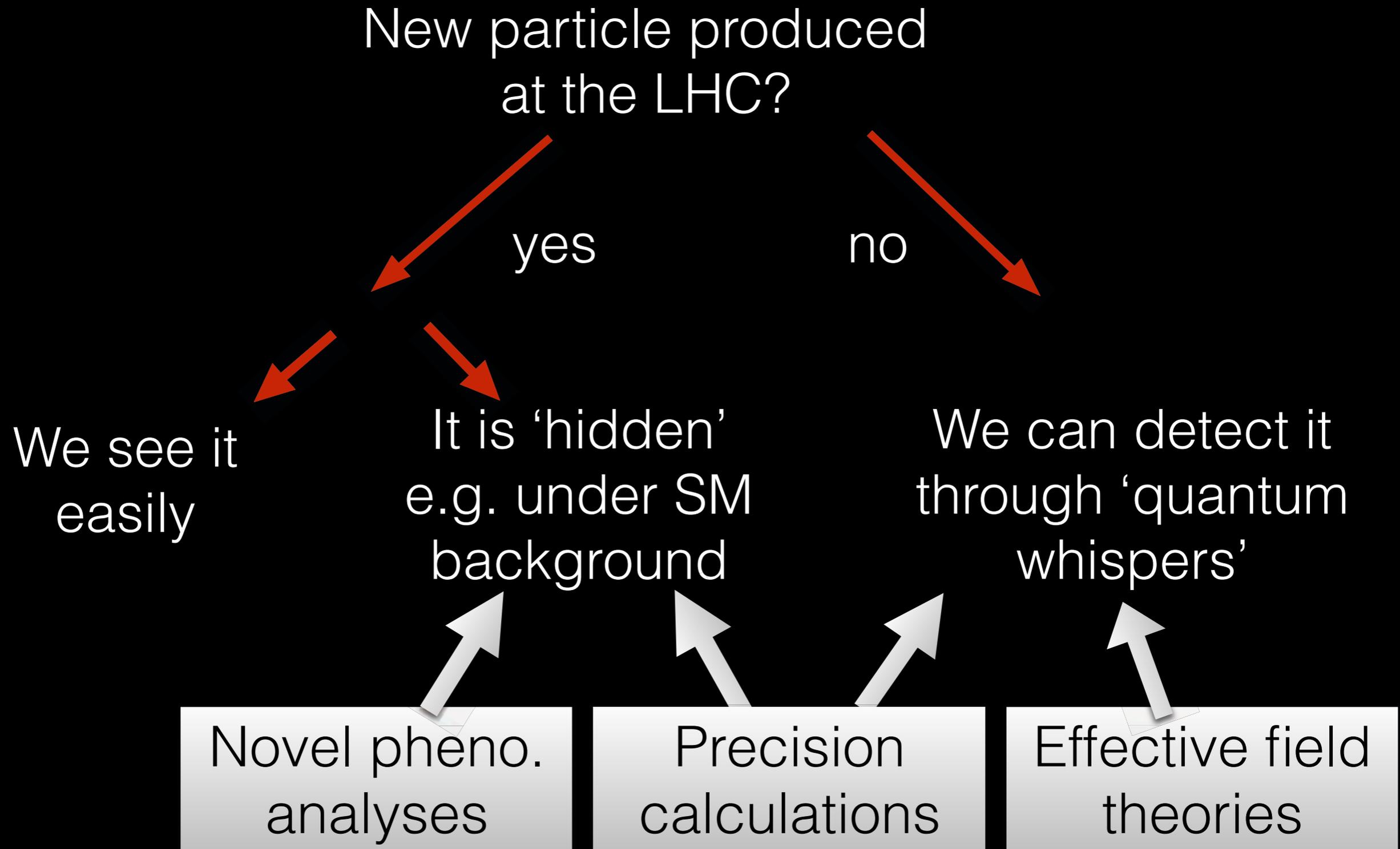
We see it  
easily

It is 'hidden'  
e.g. under SM  
background

We can detect it  
through 'quantum  
whispers'



# An LHC path to new physics



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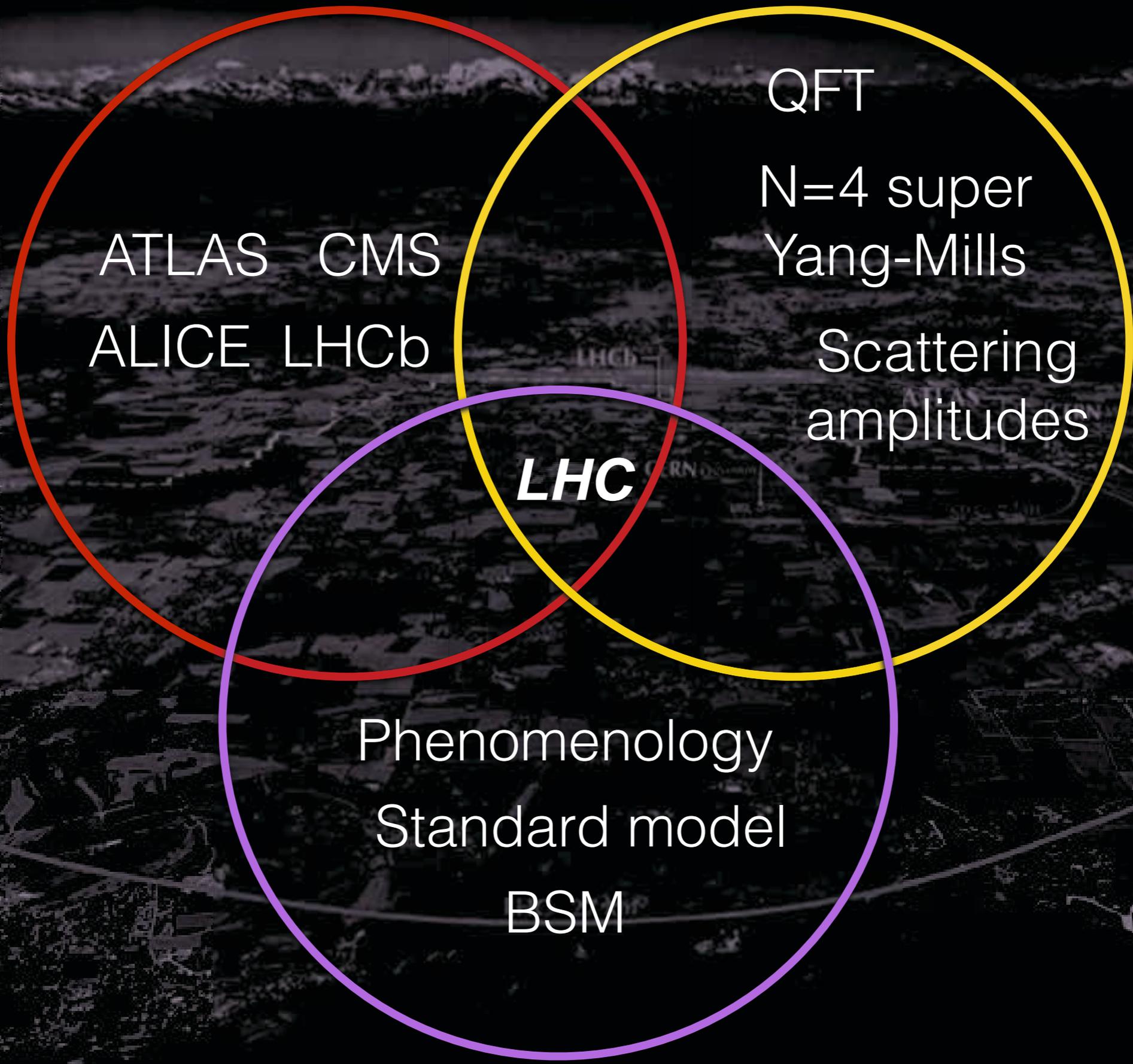
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All of  
these!

Novel pheno.  
analyses

Precision  
calculations

Effective field  
theories



ATLAS CMS  
ALICE LHCb

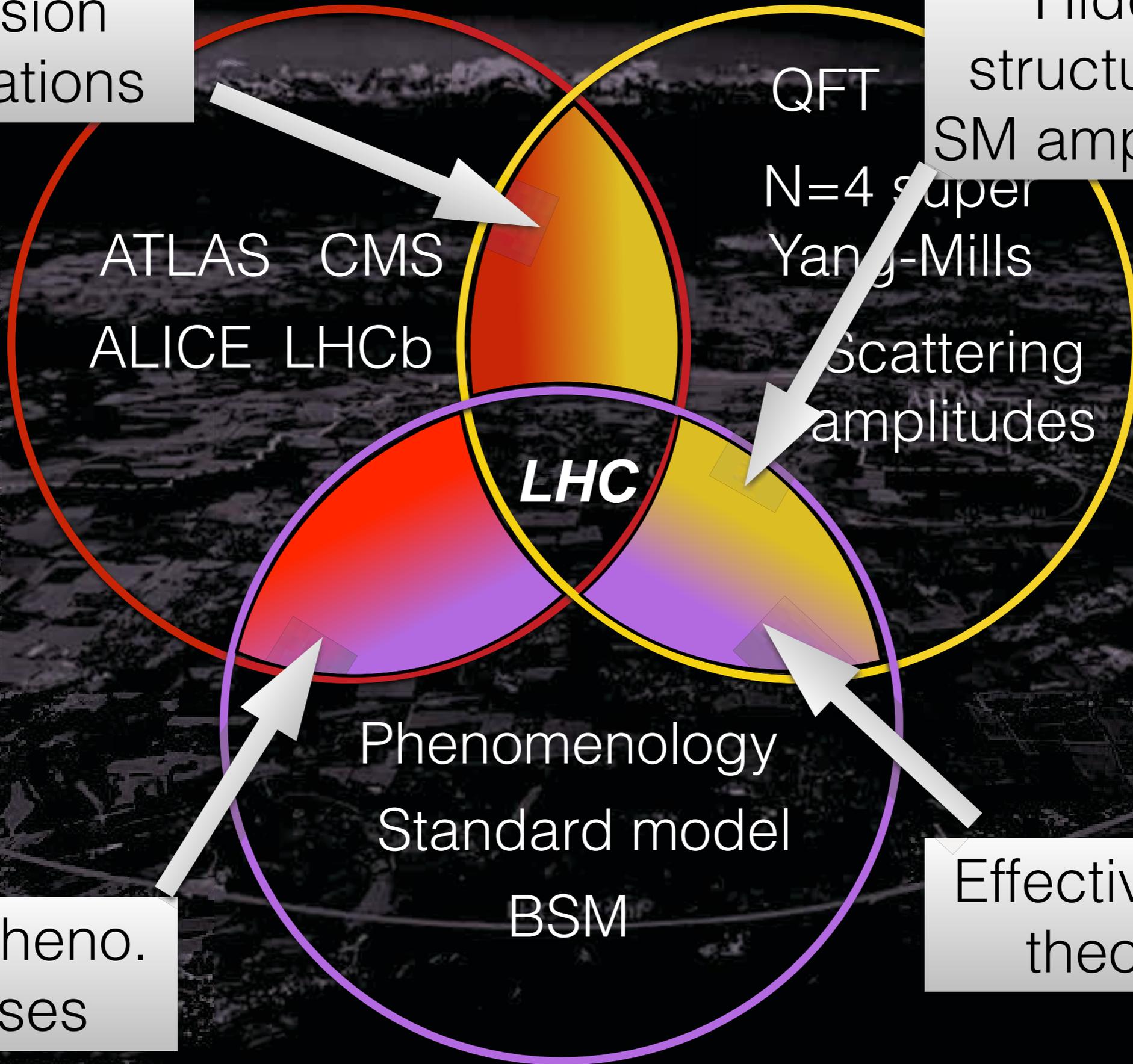
QFT  
N=4 super  
Yang-Mills  
Scattering  
amplitudes

**LHC**

Phenomenology  
Standard model  
BSM

Precision calculations

Hidden structures in SM amplitudes



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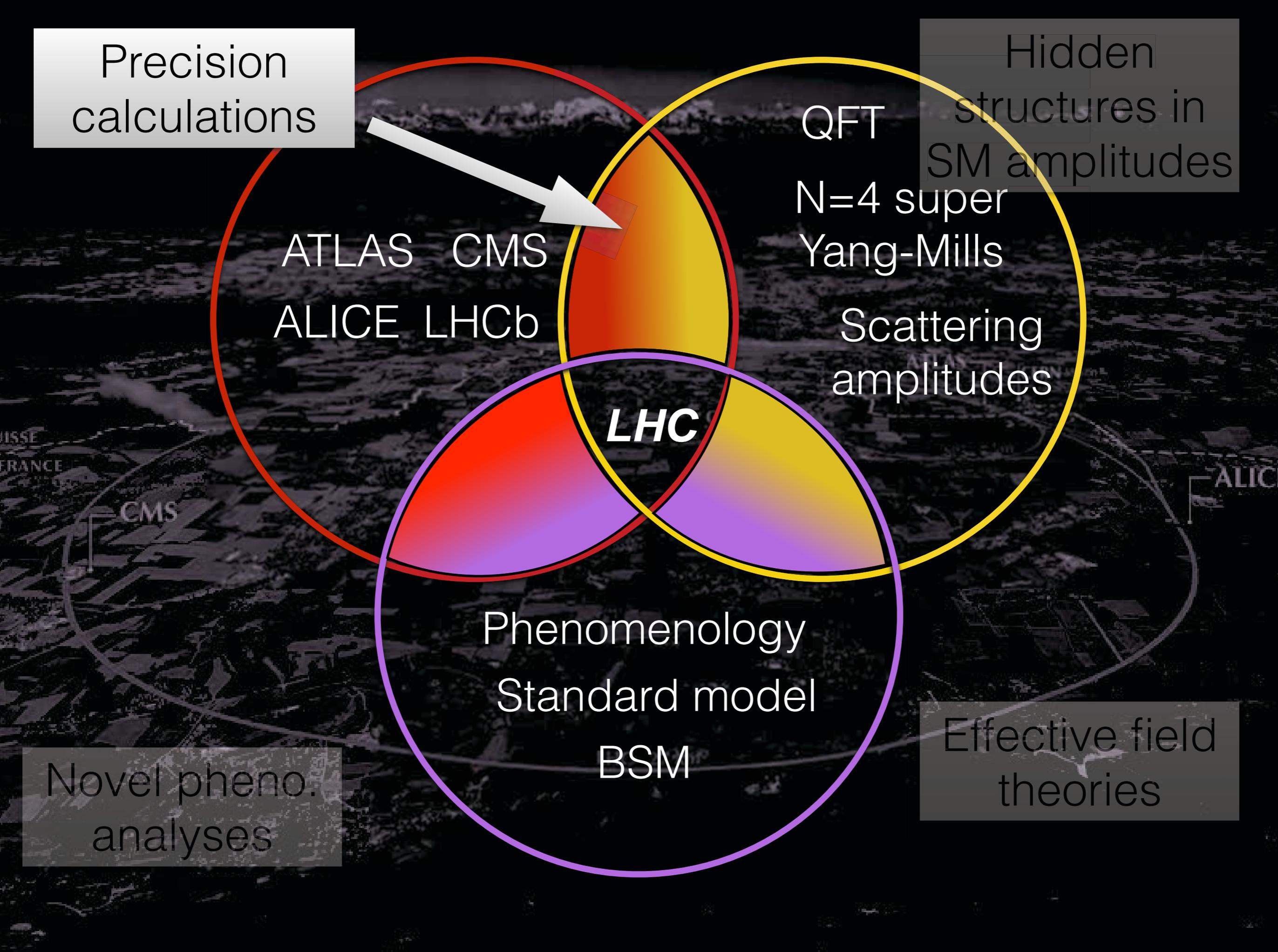
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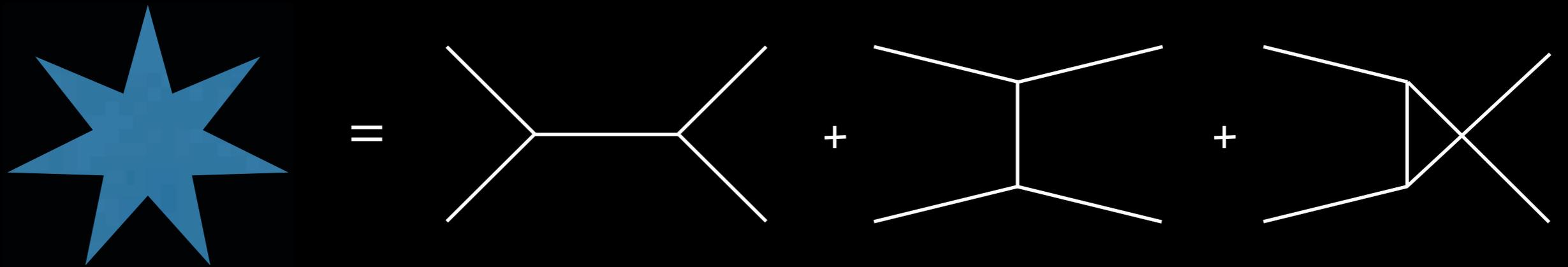
Effective field  
theories

Novel pheno.  
analyses



# The connection between theory and experiment

Scattering amplitudes

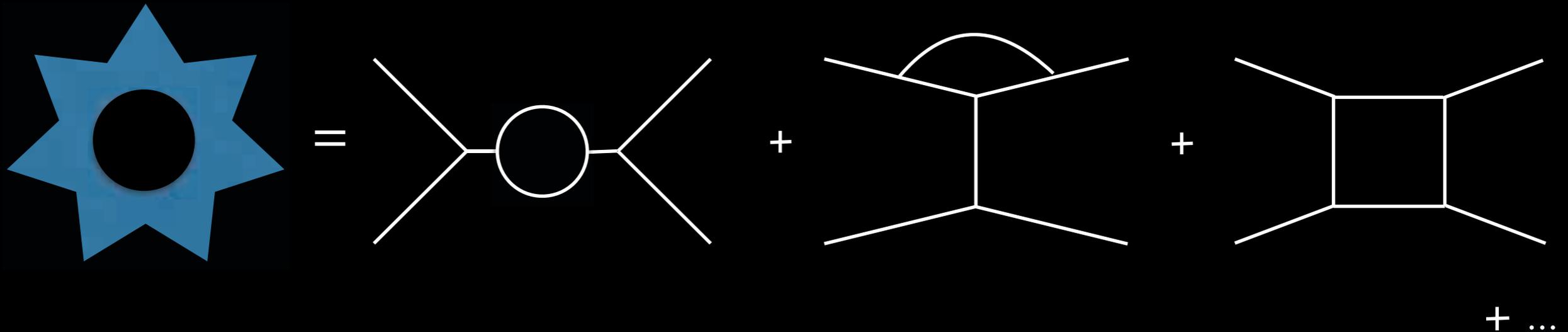


Feynman rules evaluate to give function of momenta of the particles

Tree amplitude is a rational function of Lorentz invariants  $p_1 \cdot p_2$ ,  $p_1 \cdot p_3$ ,  $p_1 \cdot p_4$ .

# The connection between theory and experiment

Scattering amplitudes

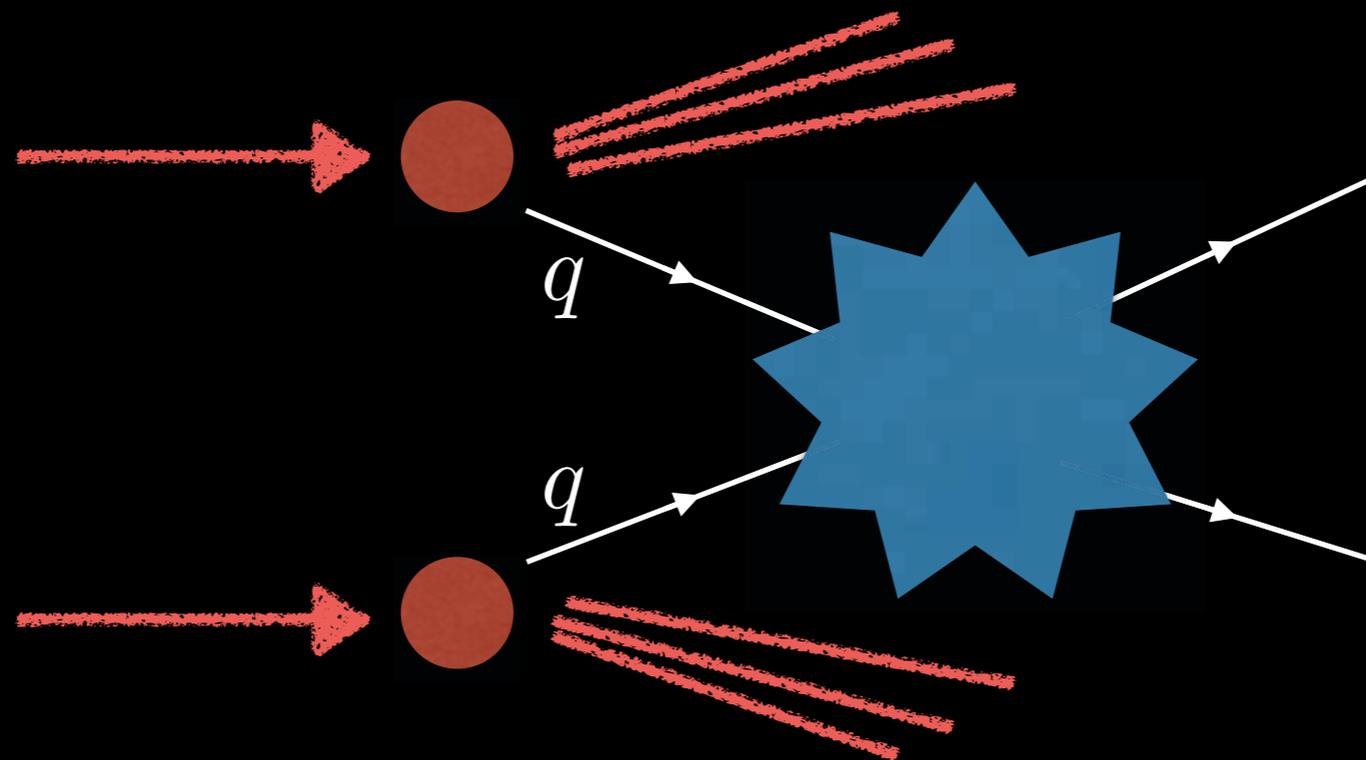


Quantum corrections ordered in perturbative expansion

Precision calculations

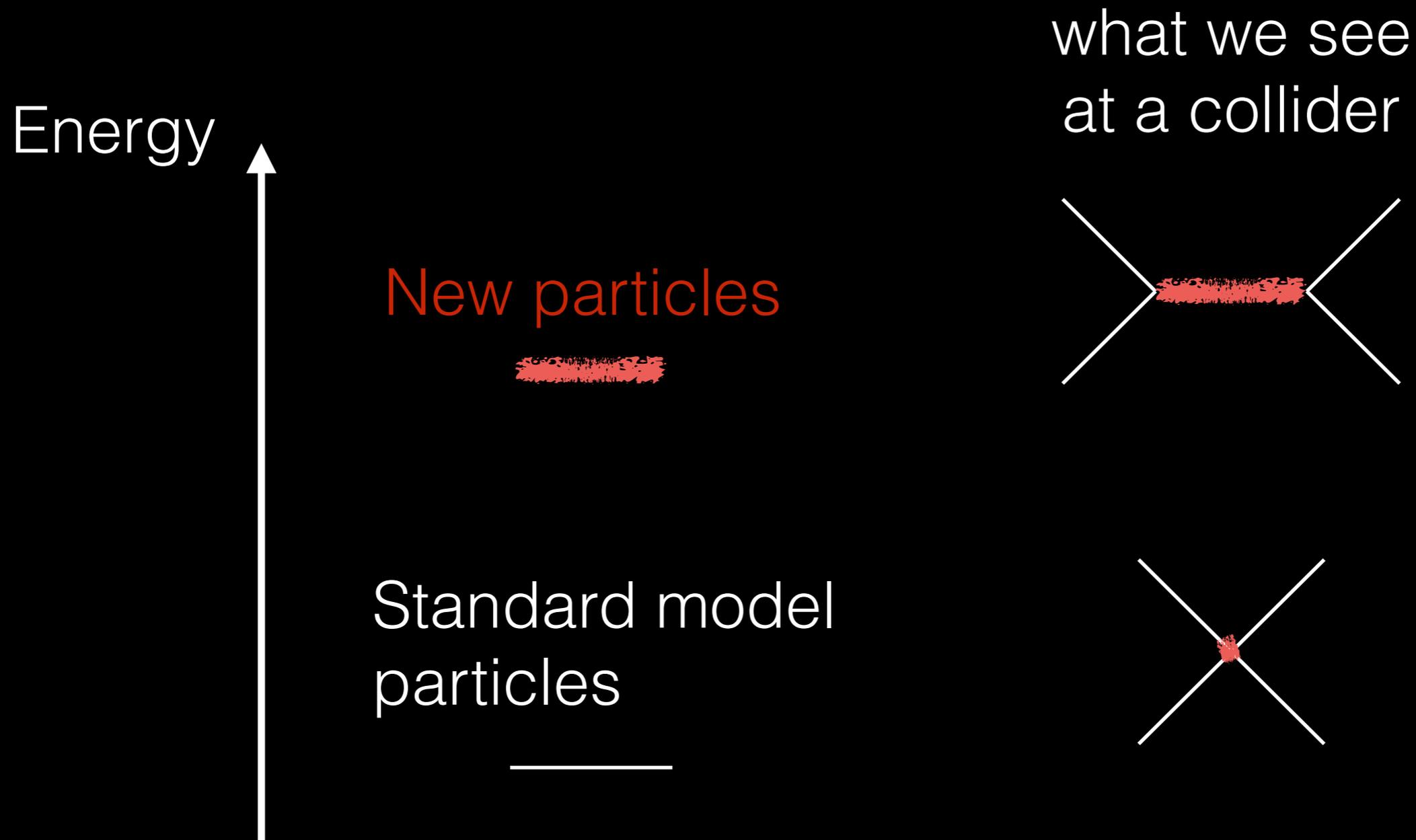
# Why precision?

LHC processes necessarily involve quarks and gluons



Strong coupling  $\sim 0.1$  (vs  $\sim 1/137$  for electroweak processes) means higher perturbative orders more important

# 'Quantum whispers' — indirect hints of new physics



# ‘Quantum whispers’ — indirect hints of new physics

Quantum effects are detectable...

...and they tend to be democratic (if they aren't, some high energy symmetry is at play)

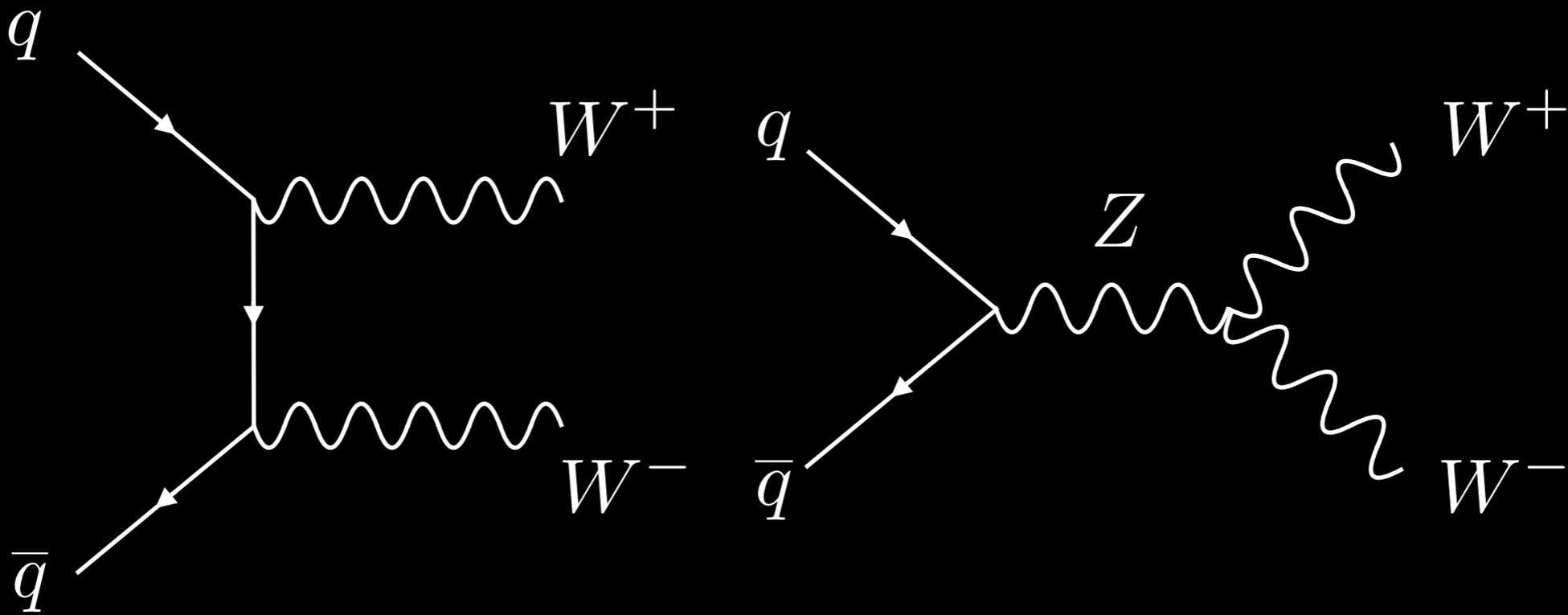
$$\mathcal{L} = \sum_i c_i \mathcal{O}_i$$

so write down everything allowed by the low energy symmetries

Effective field theories

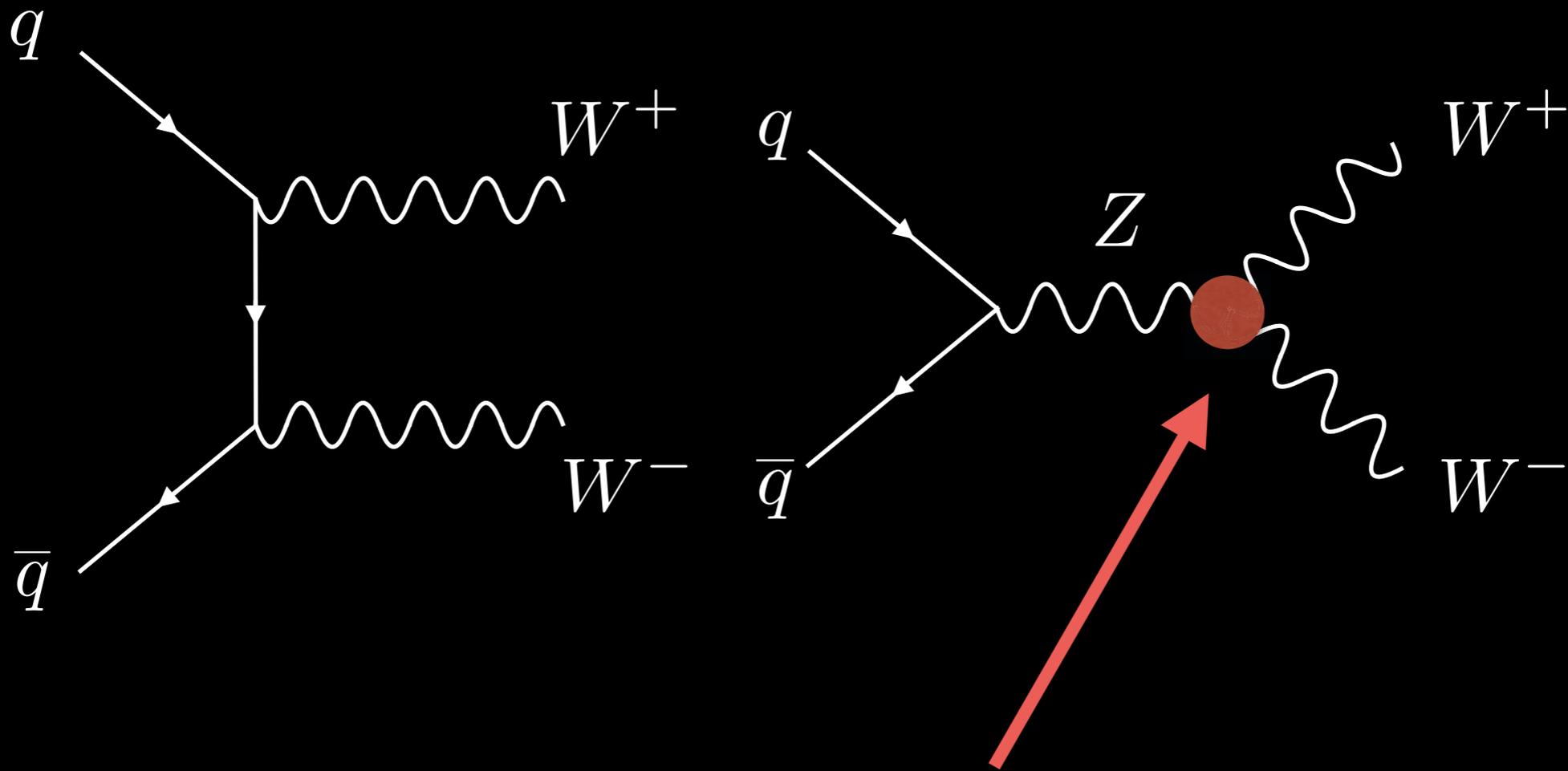
# EW boson pair production

Production of  $WW$ ,  $WZ$ ,  $ZZ$



# EW boson pair production

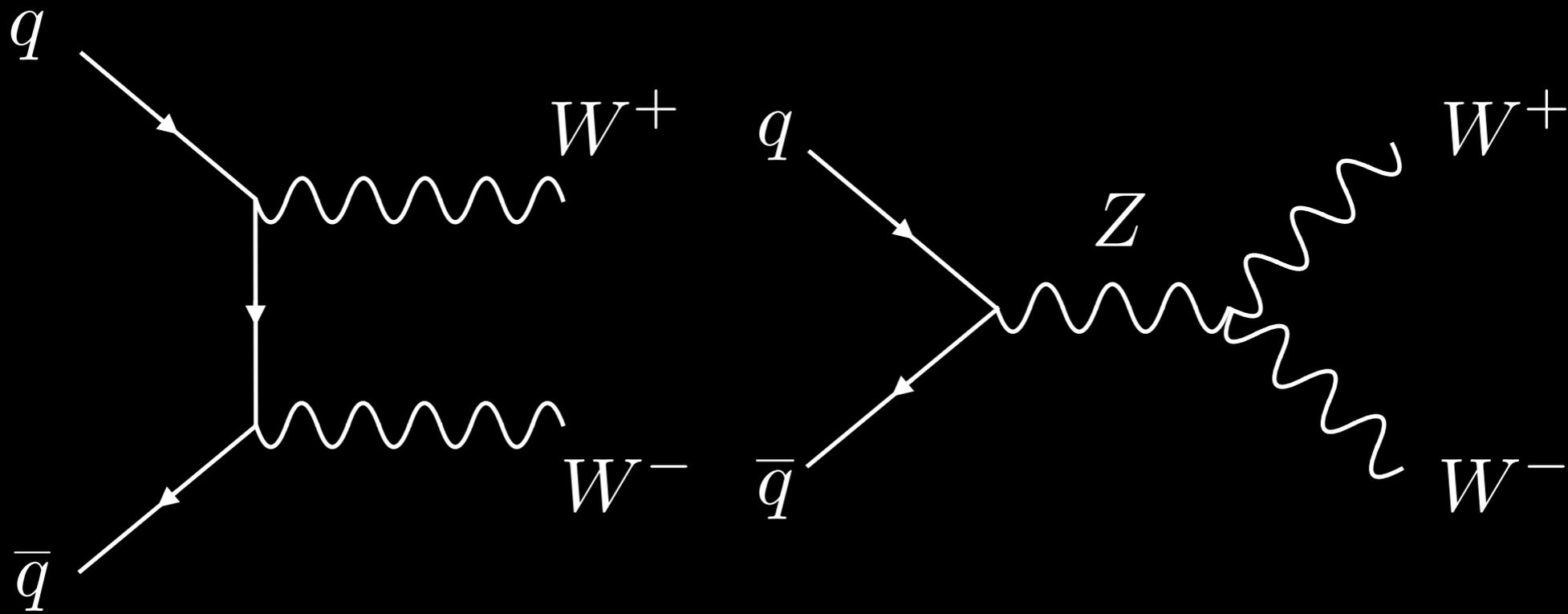
Production of  $WW$ ,  $WZ$ ,  $ZZ$



Probe 'quantum whispers' = 'anomalous tri-linear couplings'

# EW boson pair production

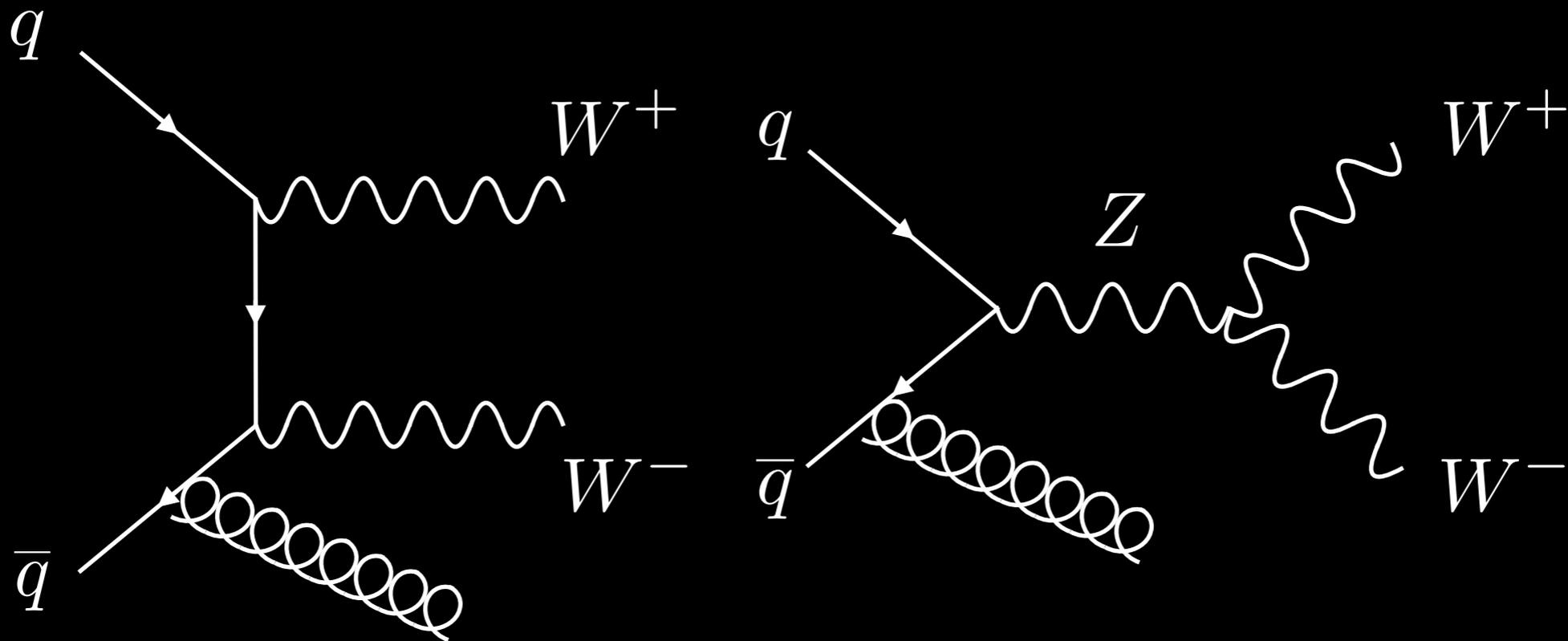
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Background to Higgs, new particle production

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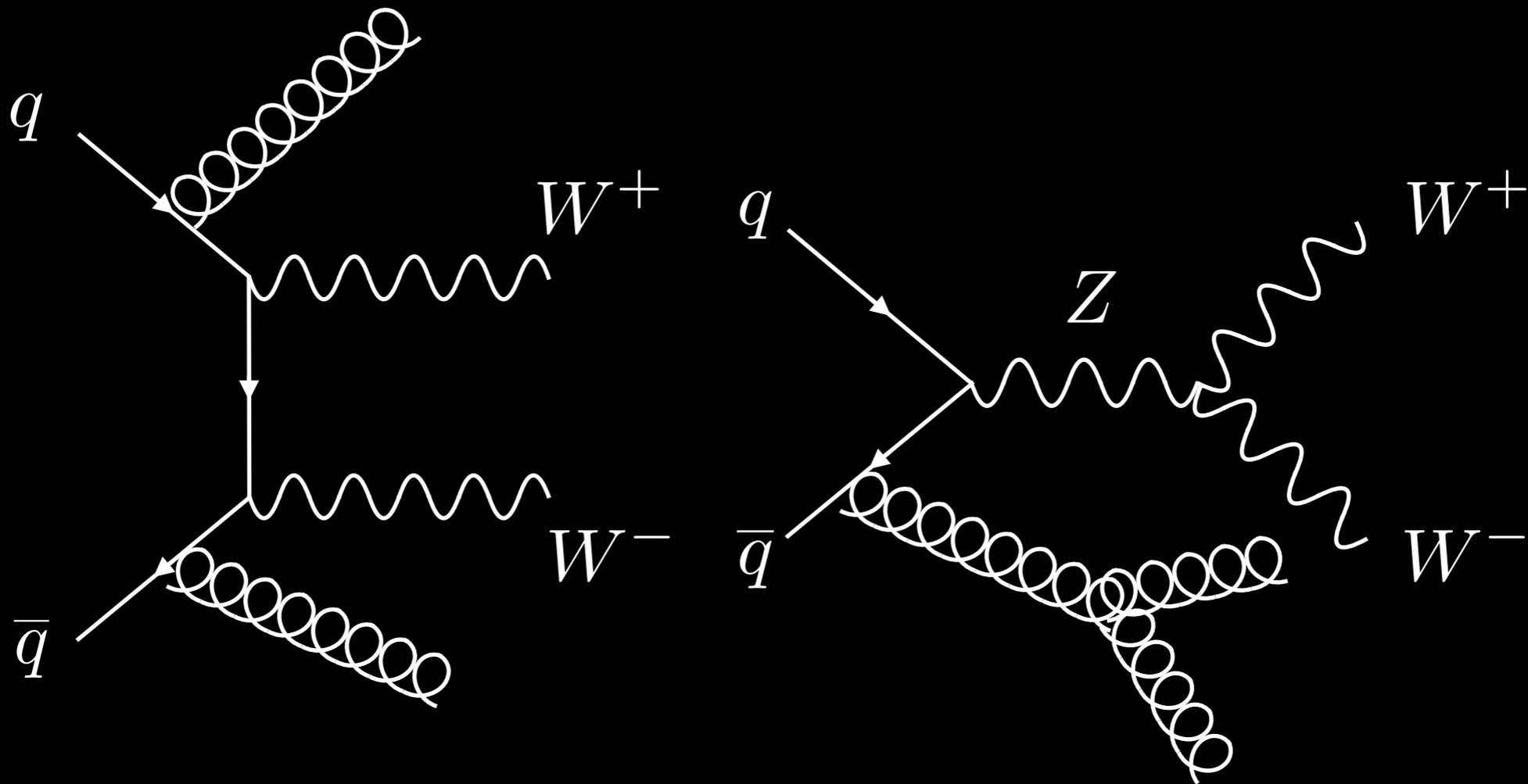
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Background to Higgs, new particle production

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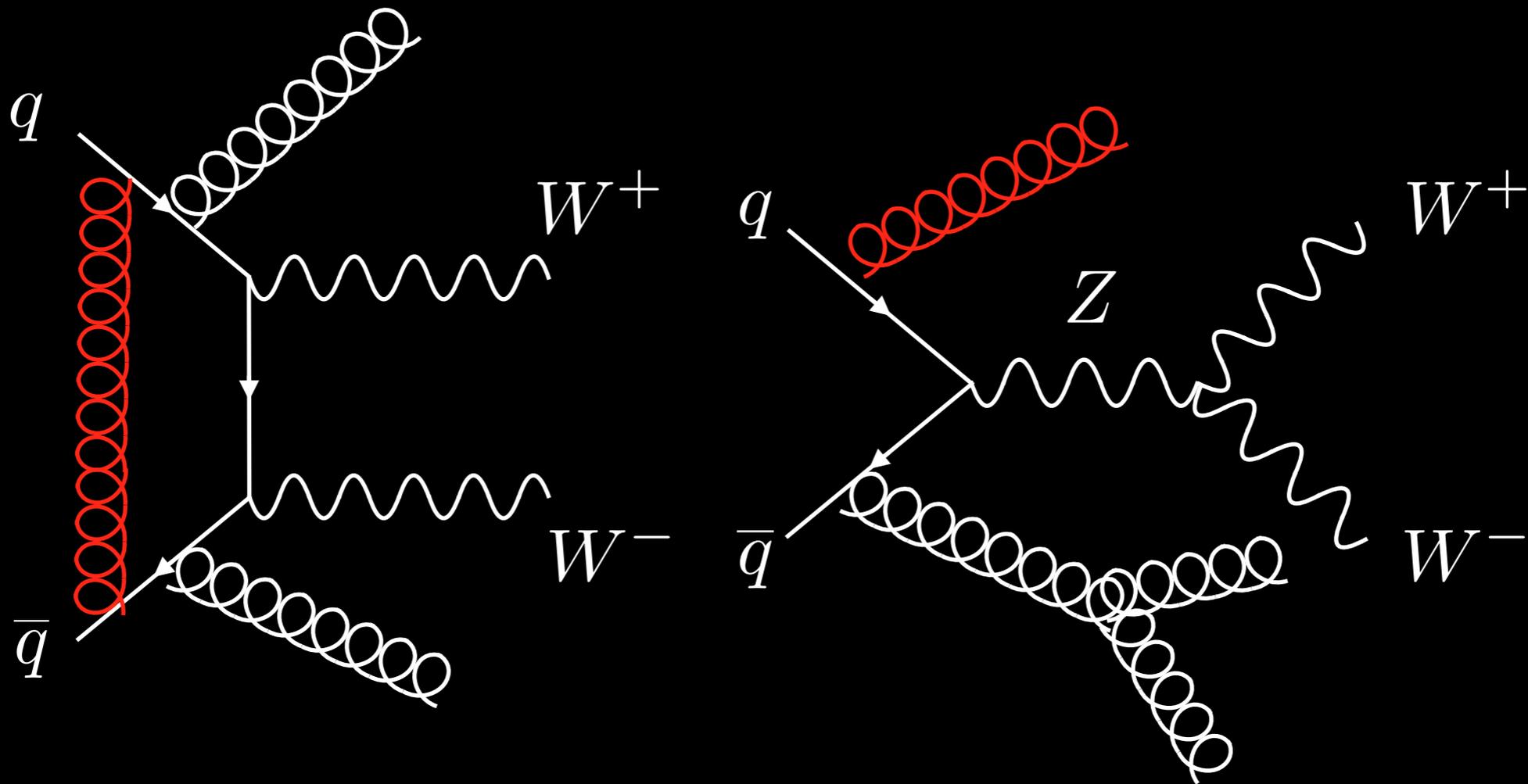
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Background to Higgs, new particle production

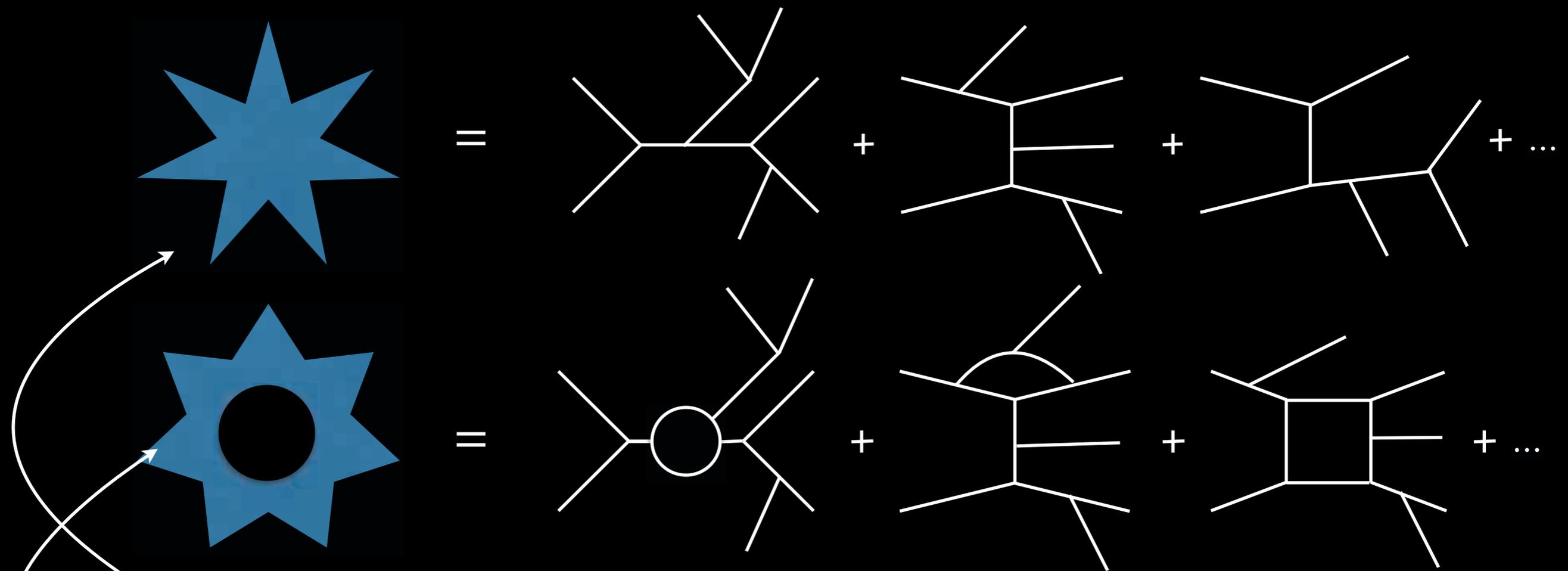
# EW boson pair production

Production of  $WW$ ,  $WZ$ ,  $ZZ$



Next-to-leading order (NLO) in QCD coupling

# Where does N=4 SYM come in?



7 gluons = ~2500 diagrams

even worse for one-loop amplitude...

# Where does N=4 SYM come in?

Two crucial ideas imported from N=4 SYM

Recursion — work directly with the amplitudes

Britto, Cachazo, Feng 2005

Britto, Cachazo, Feng, Witten 2005

(Berends, Giele 1988)

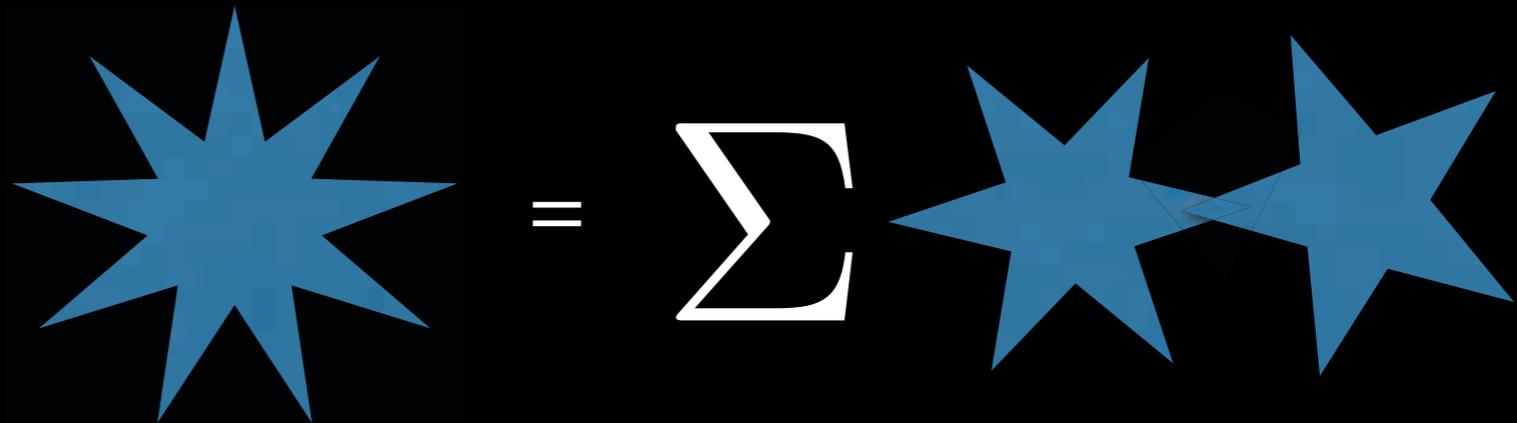
Unitarity — glue tree *amplitudes* to form loop  
*amplitudes*

Britto, Cachazo, Feng 2005

# Where does N=4 SYM come in?

Two crucial ideas imported from N=4 SYM

Recursion



Unitarity



# Where does N=4 SYM come in?

These techniques apply to colour-ordered amplitudes...

Mangano, Parke, Xu 1986

...an idea borrowed from string theory

$$\mathcal{A}_{n \text{ gluons}} = \sum_{\mathcal{P}(2, \dots, n)} \text{Tr}(T^{a_1}, T^{a_2}, \dots, T^{a_n}) A(1, 2, \dots, n)$$

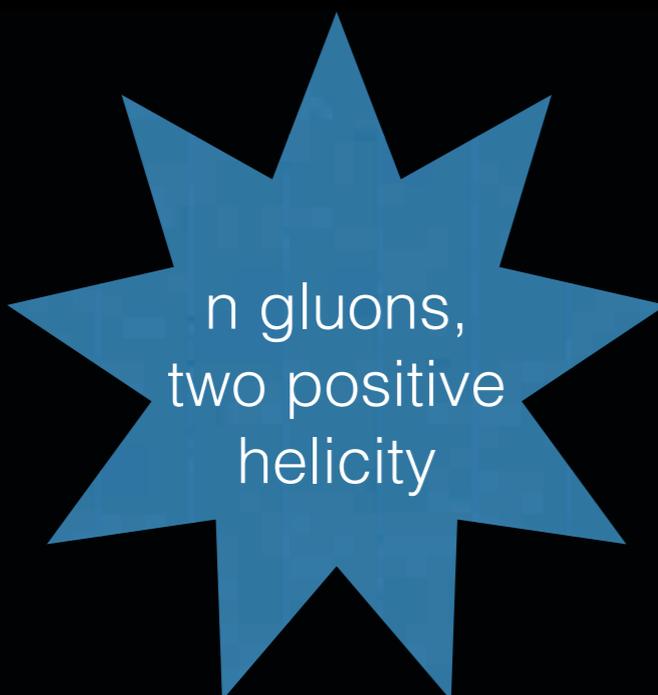
↑  
'Chan-Paton'  
factors



# Where does N=4 SYM come in?

Dramatic example: the Parke-Taylor formula

Parke, Taylor 1986



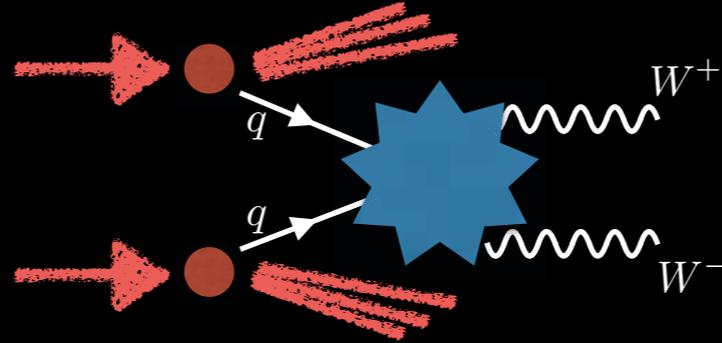
n gluons,  
two positive  
helicity

$$= ig^{n-2} \frac{\langle 12 \rangle^4}{\langle 12 \rangle \langle 23 \rangle \dots \langle n1 \rangle}$$

$$\langle ij \rangle = \sqrt{2p_i \cdot p_j} e^{i\phi}$$

this shift in philosophy has had a large impact on  
LHC precision

# 'N=4 feedback'



$$pp \rightarrow W^+W^+jj$$

TM, Melnikov, Rontsch, Zanderighi 10

NLO

POWHEG

TM, Nason, Rontsch,  
Zanderighi 11

$$pp \rightarrow W^+W^-jj$$

TM, Melnikov, Rontsch, Zanderighi 11

NLO

$$pp \rightarrow W^+W^-j$$

TM, Melnikov, Rontsch, Zanderighi 12

NLO

$$gg \rightarrow W^+W^-g$$

TM, Melnikov, Rontsch, Zanderighi 12

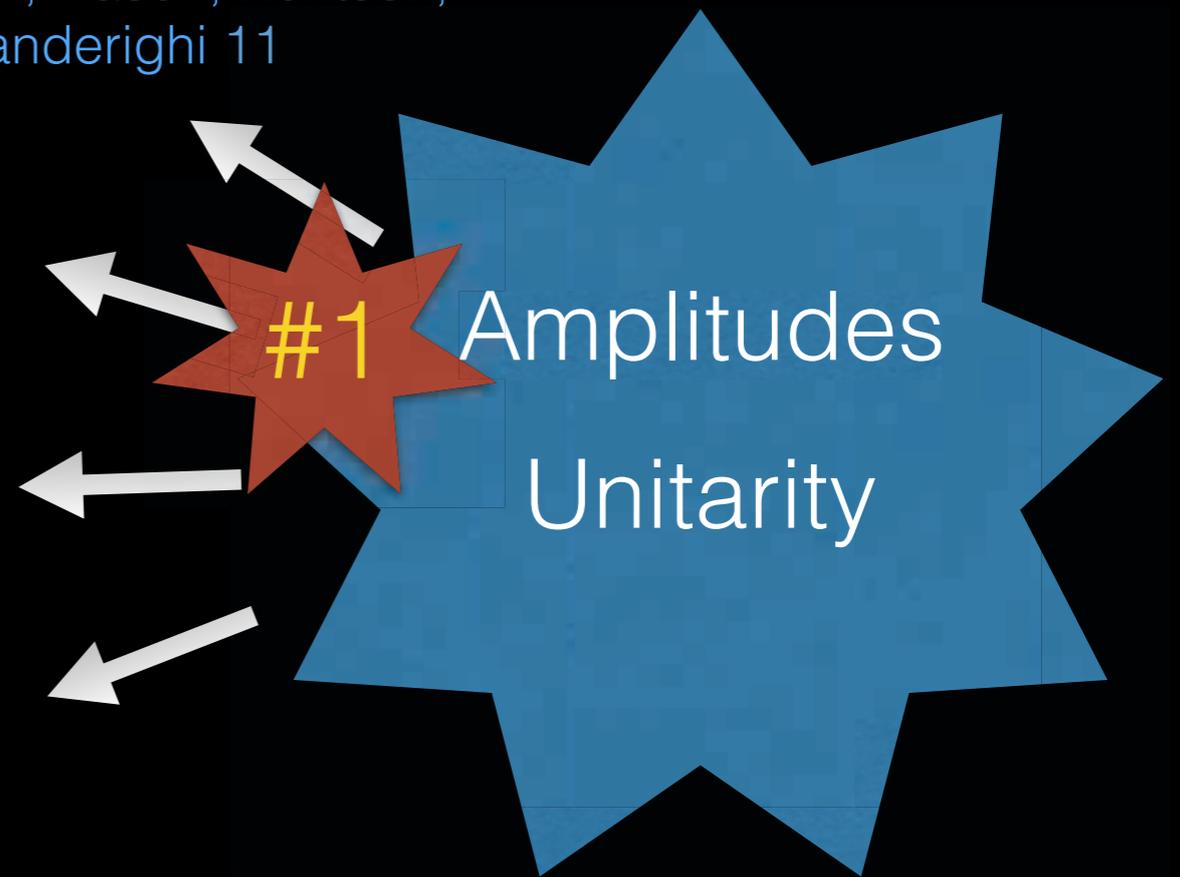
(N)NLO

$$pp \rightarrow WW, WZ, ZZ$$

TM, Nason, Rontsch, Zanderighi 11

Hamilton, TM, Monni, Re, Zanderighi 16

POWHEG



# Experimental analyses

>70 published ATLAS and CMS papers

POWHEG Codes  
TM, Nason, Rontsch, Zanderighi

Fiducial cross sections and anomalous couplings

**Measurements of  $W^\pm Z$  production cross sections in  $pp$  collisions at  $\sqrt{s} = 8$  TeV with the ATLAS detector and limits on anomalous gauge boson self-couplings**

**Measurement of the  $ZZ$  Production Cross Section in  $pp$  Collisions at  $\sqrt{s} = 13$  TeV with the ATLAS Detector**

**Measurement of  $ZZ$  production in  $pp$  collisions at  $\sqrt{s} = 7$  TeV and limits on anomalous  $ZZZ$  and  $ZZ\gamma$  couplings with the ATLAS detector**

**Measurement of the  $W^+ W^-$  cross section in  $pp$  collisions at  $\sqrt{s} = 8$  TeV and limits on anomalous gauge couplings**

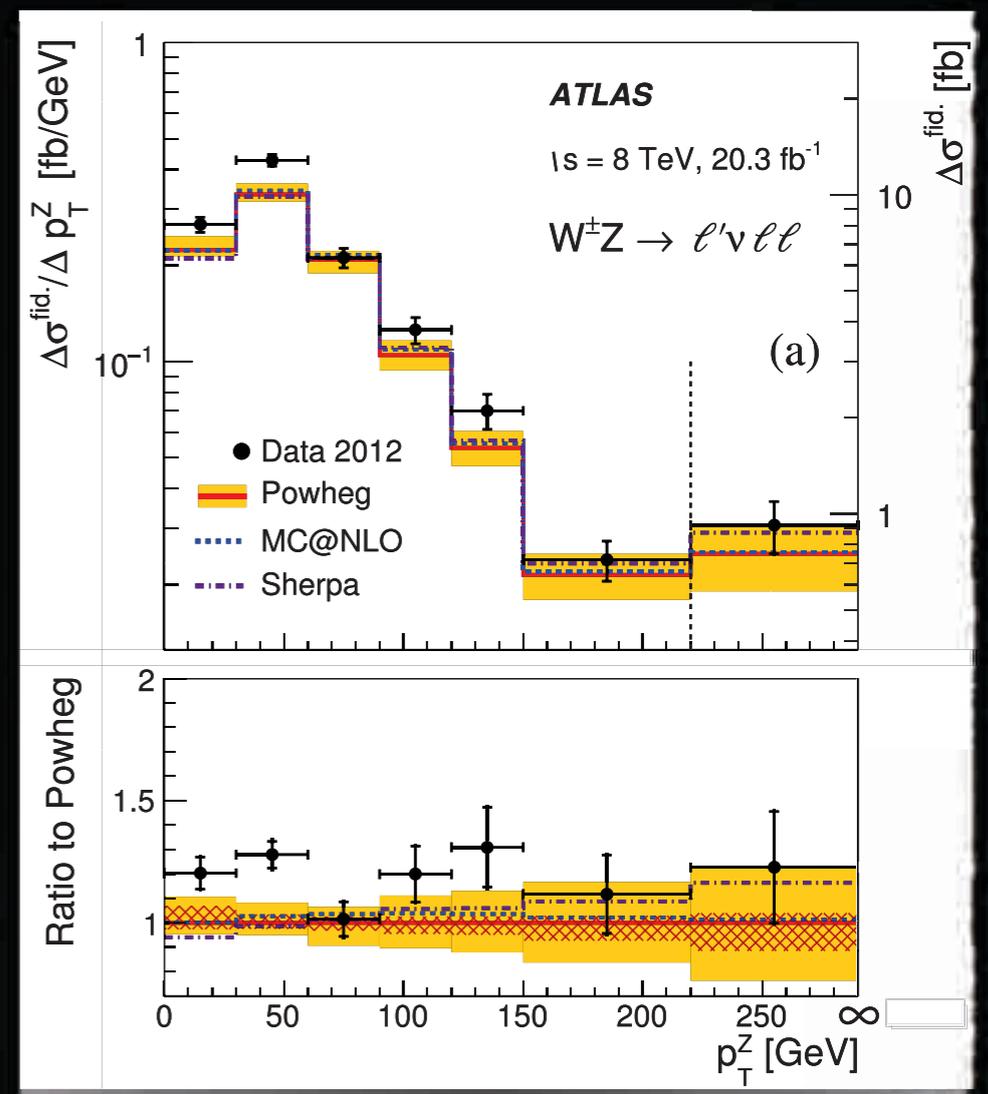
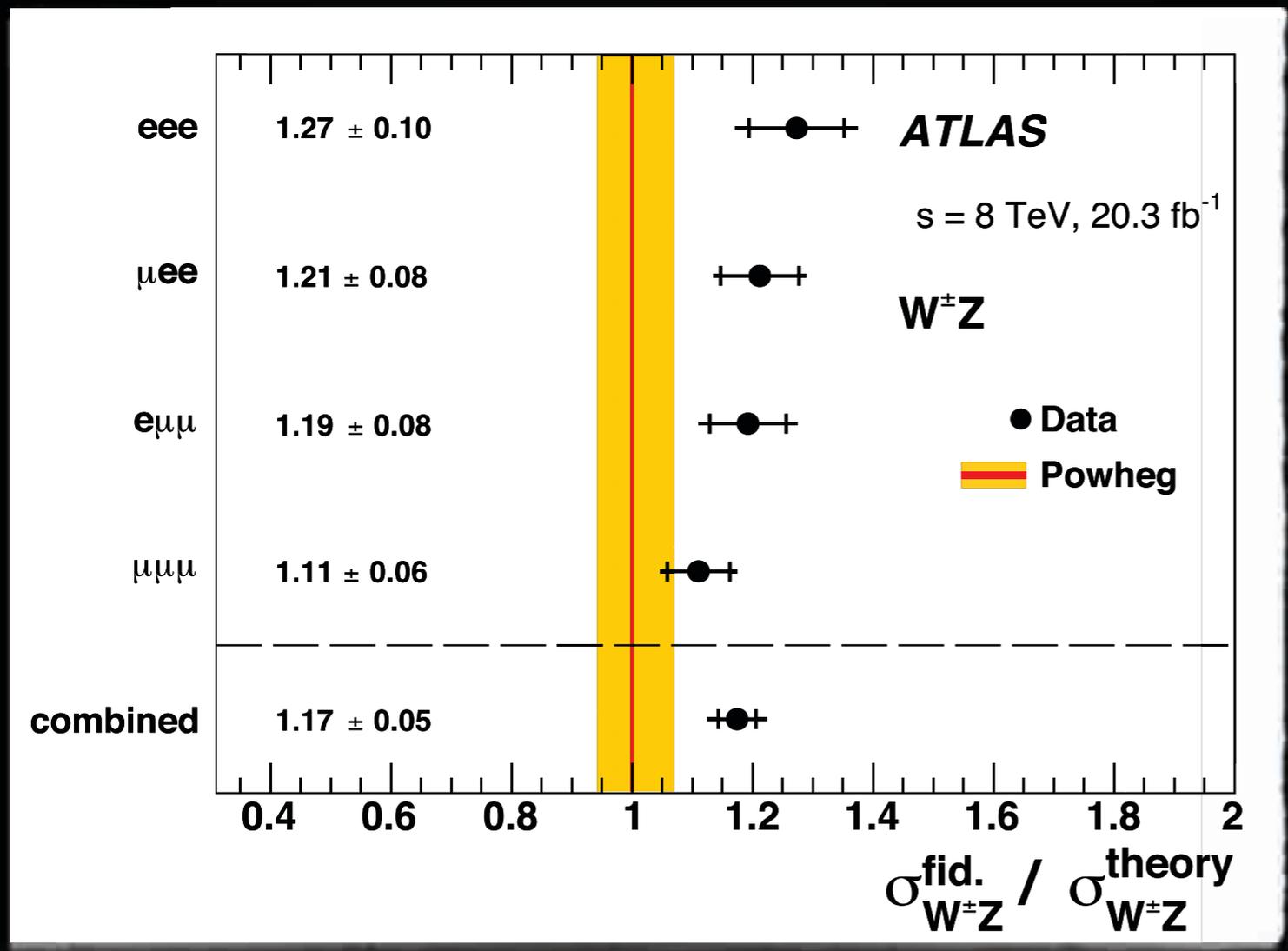
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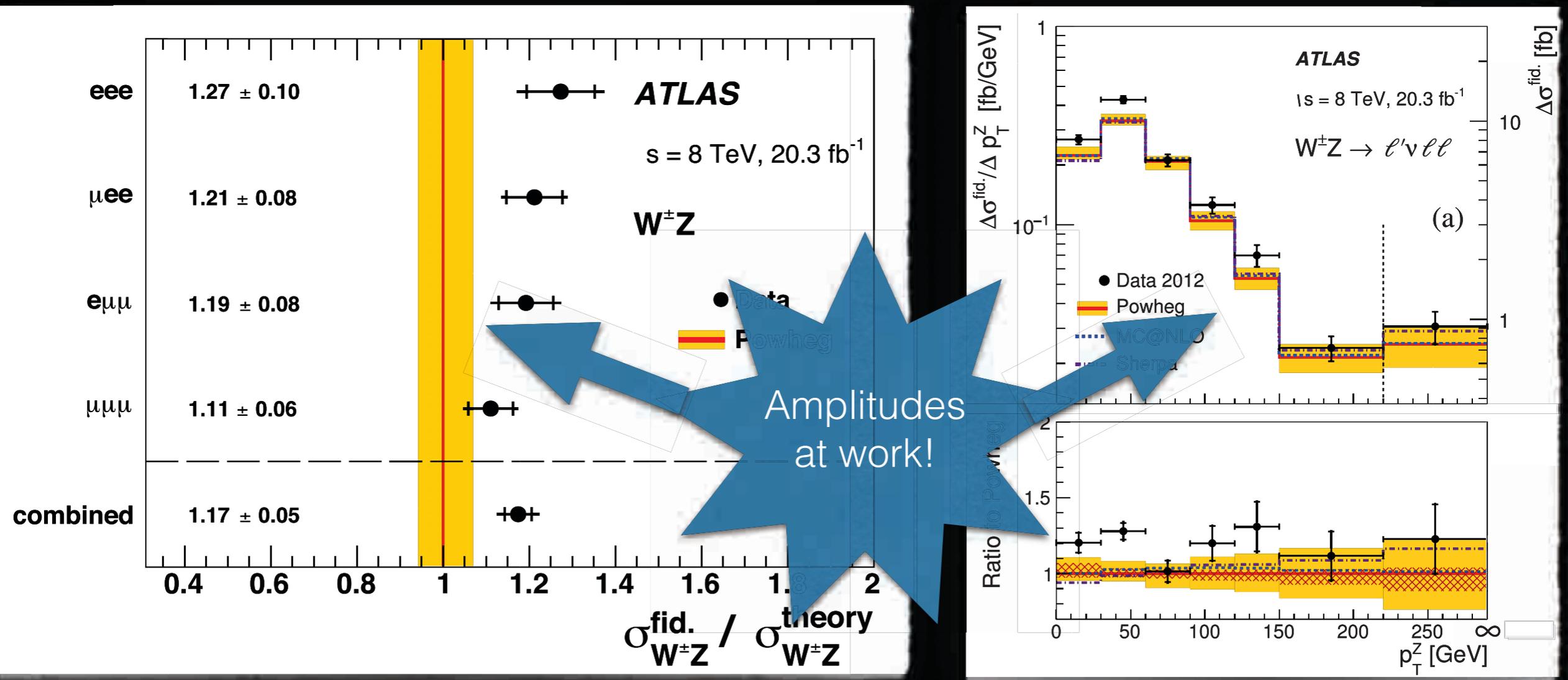
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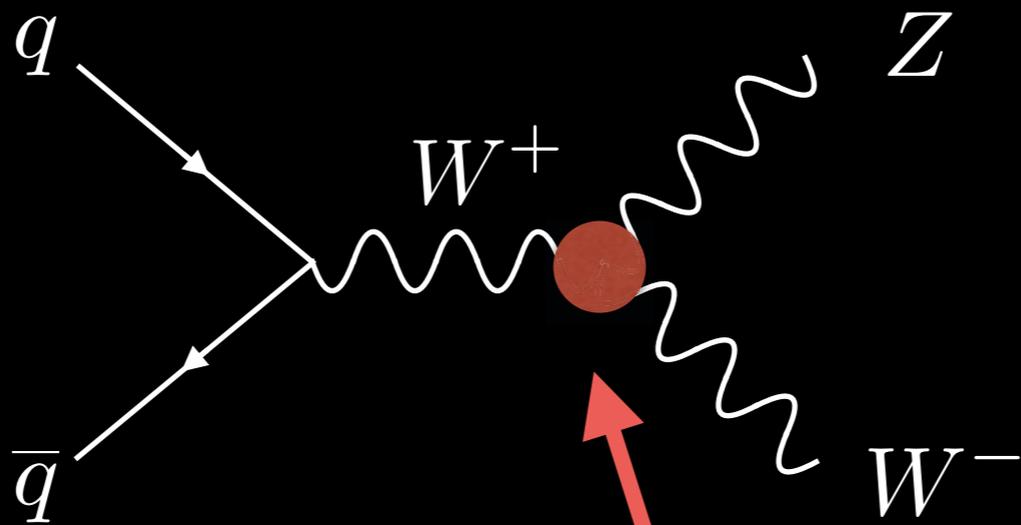
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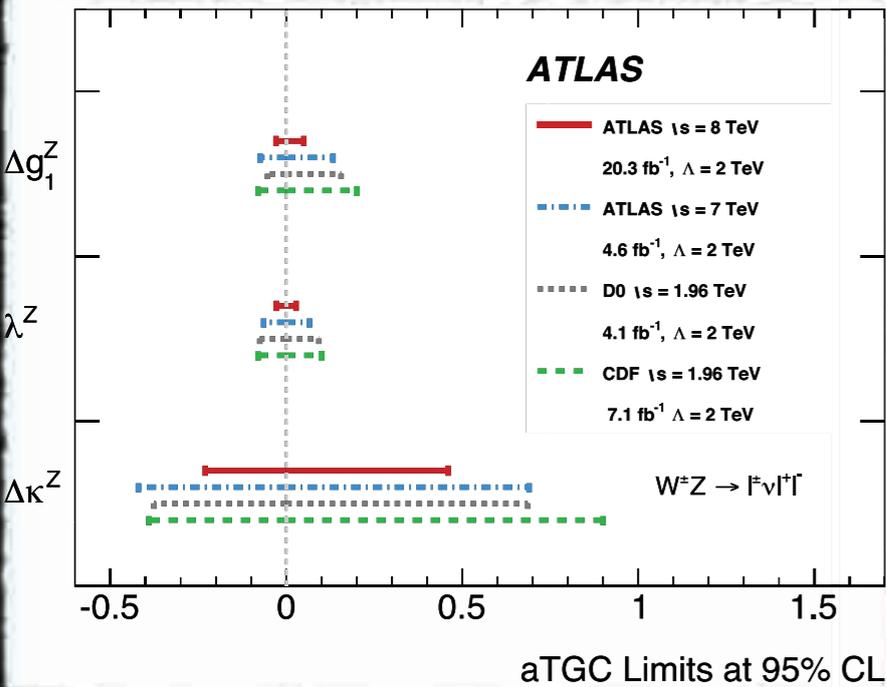


$$\mathcal{L} = \sum_i c_i \mathcal{O}_i$$

$$\frac{c_{WWW}}{\Lambda^2} \text{Tr}(W_{\mu\nu} W_{\nu\rho} W_{\rho\mu})$$

$$\frac{c_W}{\Lambda^2} (D_\mu H)^\dagger W_{\mu\nu} D_\nu H$$

$$\frac{c_B}{\Lambda^2} (D_\mu H)^\dagger B_{\mu\nu} D_\nu H$$



EFT coupling

Expected [TeV<sup>-2</sup>]

Observed [TeV<sup>-2</sup>]

$$c_W/\Lambda^2$$

[-3.7 ; 7.6]

[-4.3 ; 6.8]

$$c_B/\Lambda^2$$

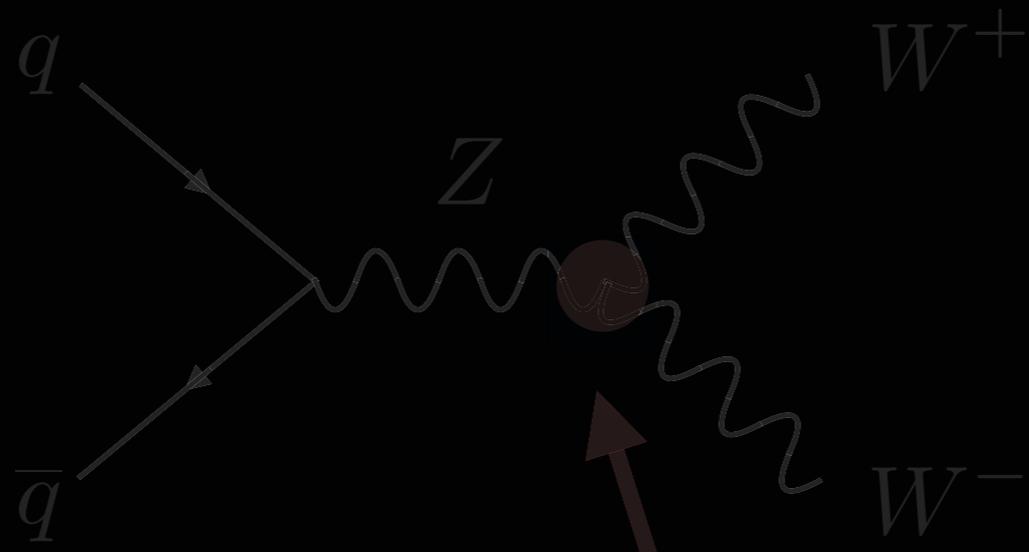
[-270 ; 180]

[-320 ; 210]

$$c_{WWW}/\Lambda^2$$

[-3.9 ; 3.8]

[-3.9 ; 4.0]

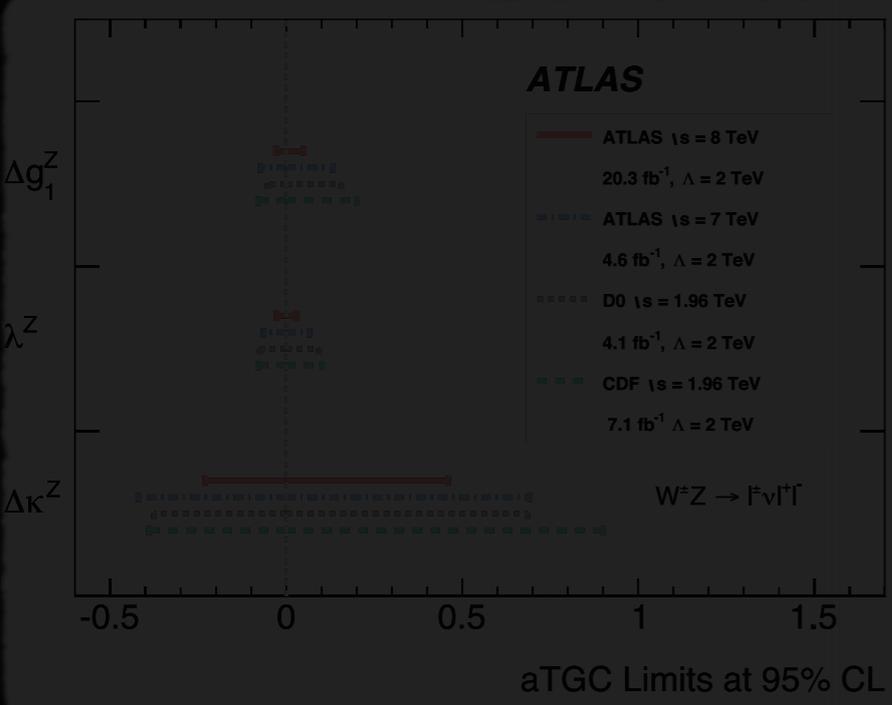


# Setting strongest limits on new physics...

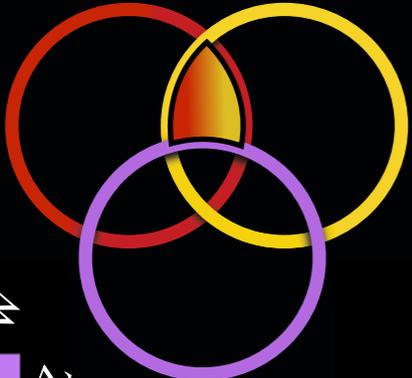
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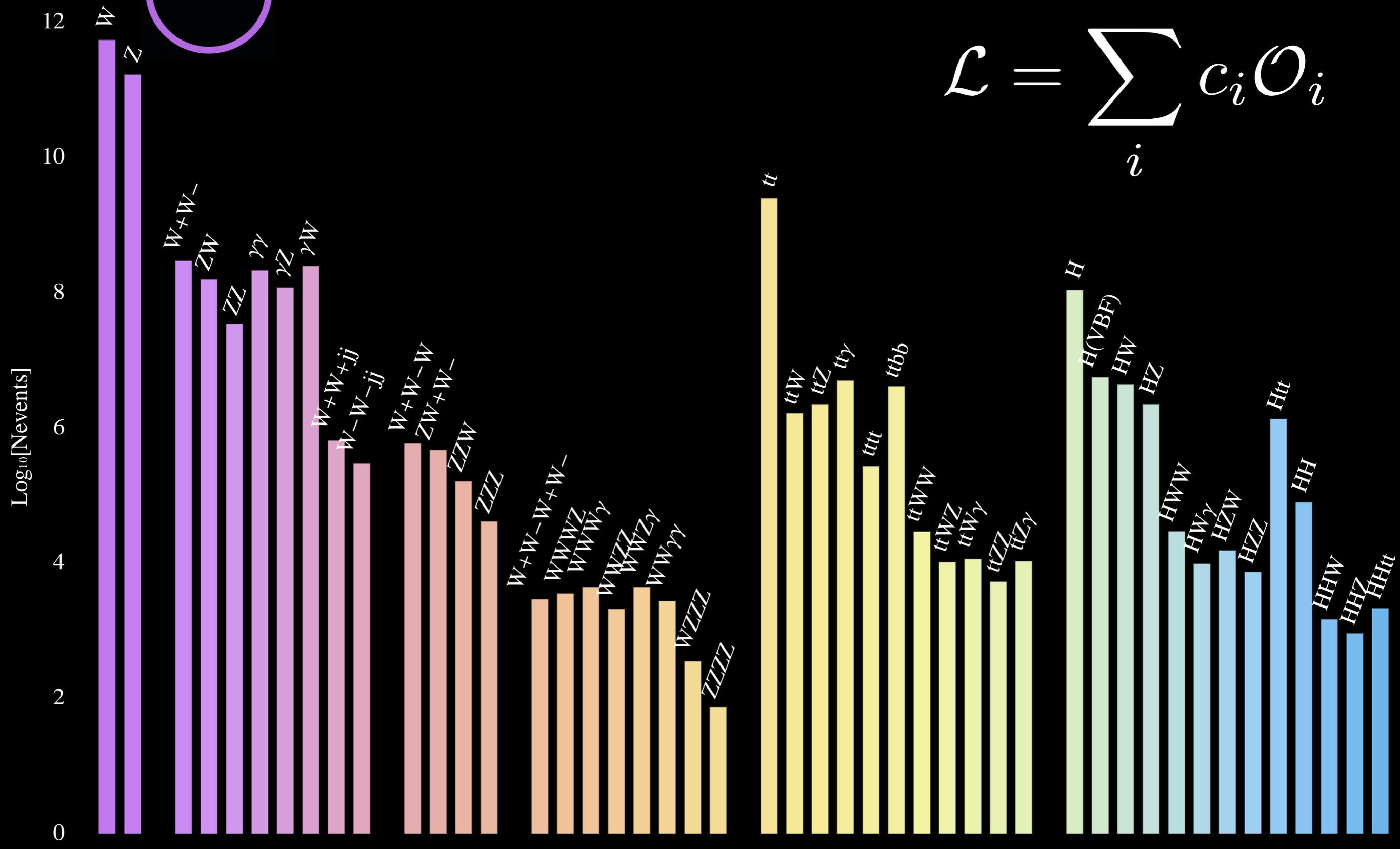


EFT coupling	Expected [TeV <sup>-2</sup> ]	Observed [TeV <sup>-2</sup> ]
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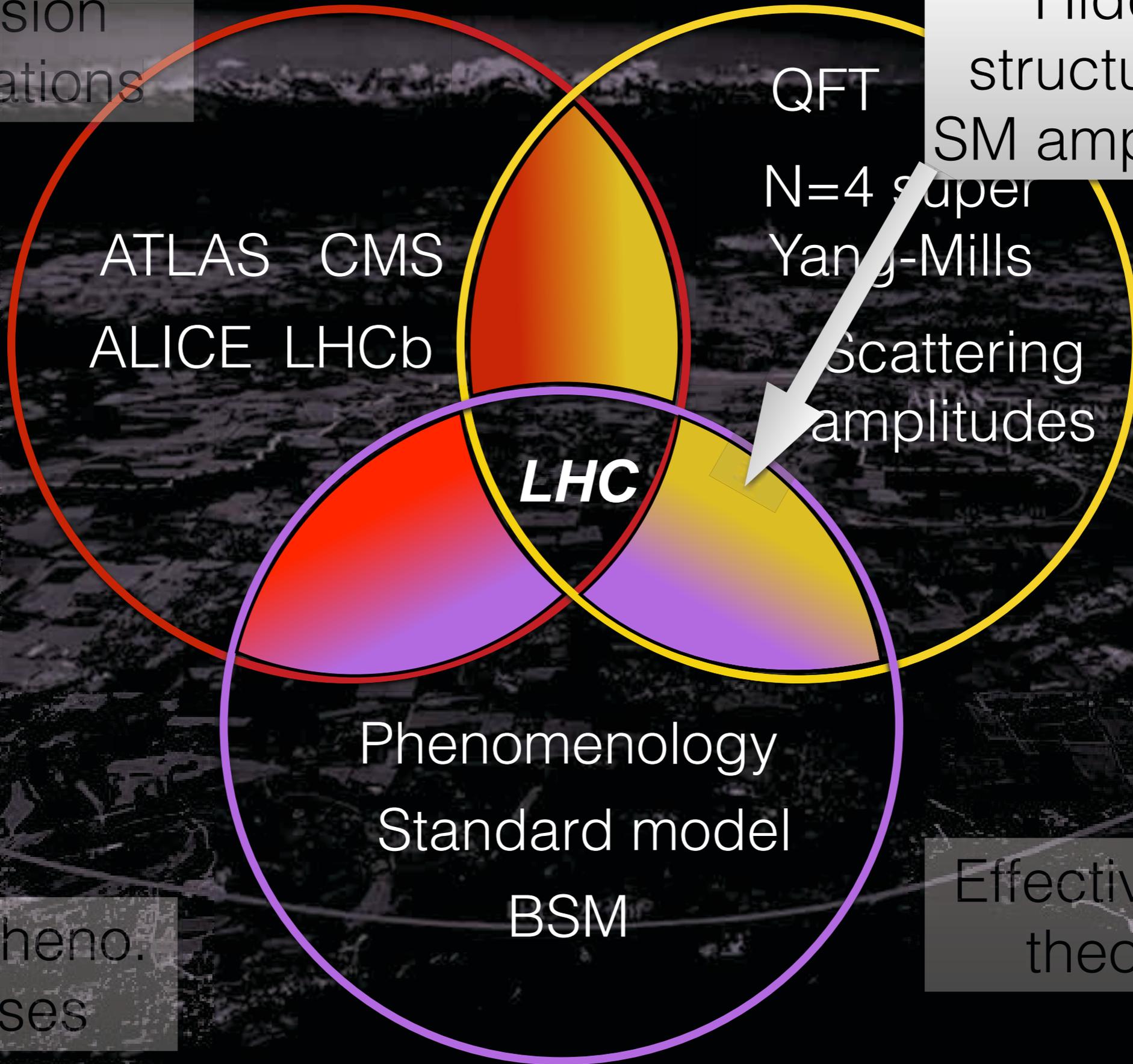
# Zoo of opportunities...

$$\mathcal{L} = \sum_i c_i \mathcal{O}_i$$



Precision calculations

Hidden structures in SM amplitudes



QFT

N=4 super  
Yang-Mills

Scattering  
amplitudes

**LHC**

Phenomenology  
Standard model  
BSM

Effective field theories

Novel pheno.  
analyses

Searching for **secrets** in the  
standard model

# Searching for **secrets** in the standard model



Amplitudes  
at play!

# Hidden structure in SM amplitudes

Long understood that SM tree amplitudes with gluons and one flavour of quark are 'effectively supersymmetric'

Parke, Taylor 1985 Kunszt 1986

$(g^a, \lambda^a)$  N=1 super-multiplet

Apart from the colour (adjoint gluino) these have identical interactions as a massless quark with a gluon

# Hidden structure in SM amplitudes

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$(g^a, \lambda^a)$  N=1 super-multiplet

$$\mathcal{A} = \sum_{\mathcal{P}(2, \dots, n)} \text{Tr}(T^{a_1}, T^{a_2}, \dots, T^{a_n}) A(1, 2, \dots, n)$$

goes beyond just  
using the techniques...



# Hidden structure in SM amplitudes

All N=4 super Yang-Mills tree amplitudes are known in closed (and concise) form

Drummond, Henn 2009

$(g^+, \lambda_A, \phi_{AB}, \bar{\lambda}_A, g^-)$  N=4 super-multiplet

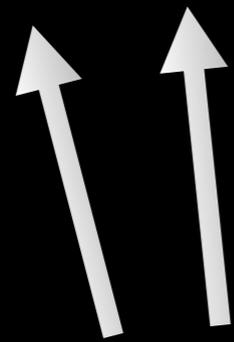
$A = 1, 2, 3, 4$

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$A = 1, 2, 3, 4$

gluons and four flavours of massless 'quarks'

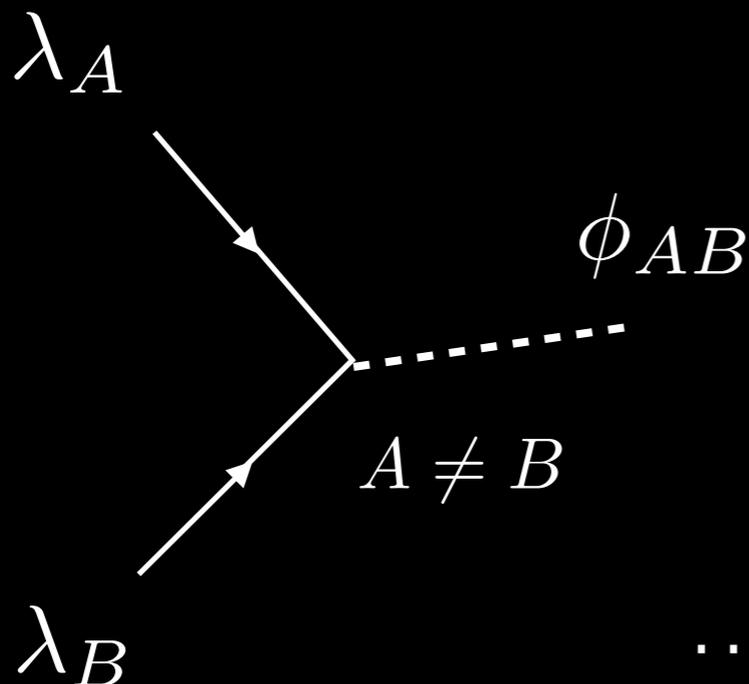
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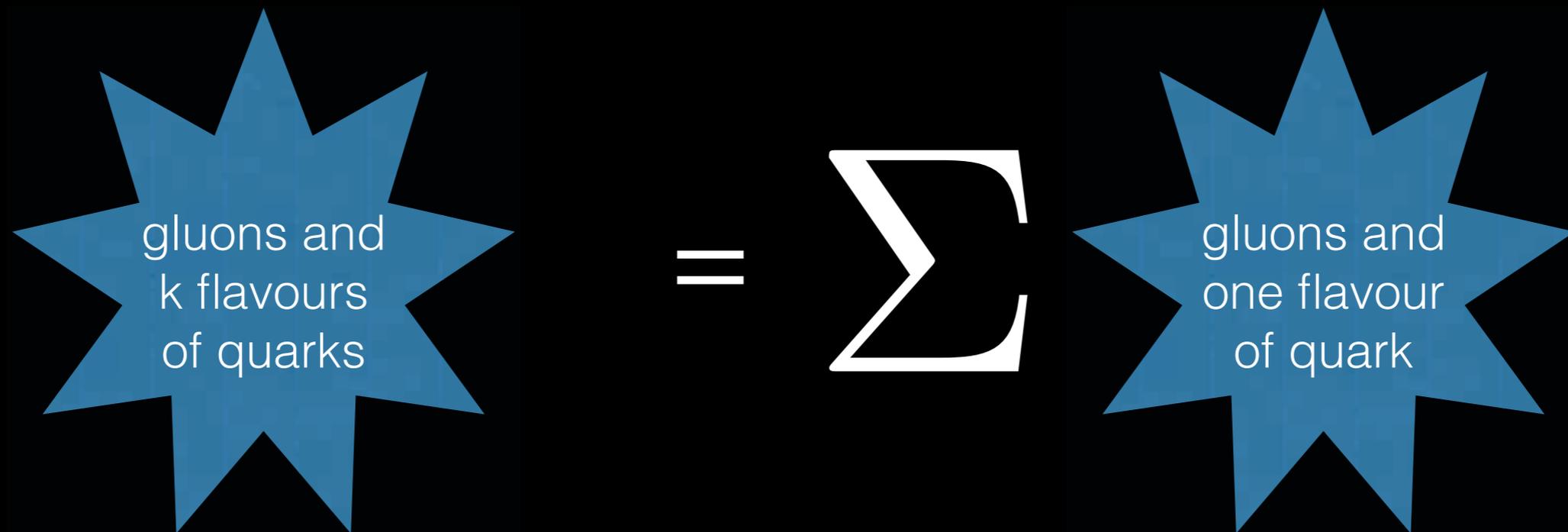
...scalars contaminate the amplitudes

Dixon, Henn, Plefka, Schuster 2011

# 'Emergent flavour'

It turns out that it is possible to express any k-flavour QCD tree amplitude in terms of one-flavour amplitudes

TM 2014



All massless QCD from N=4 SYM

# Dyck word structure



Understanding a basis for these amplitudes is crucial for this

Structure based around 'Dyck words'

TM 2013

# Dyck word structure

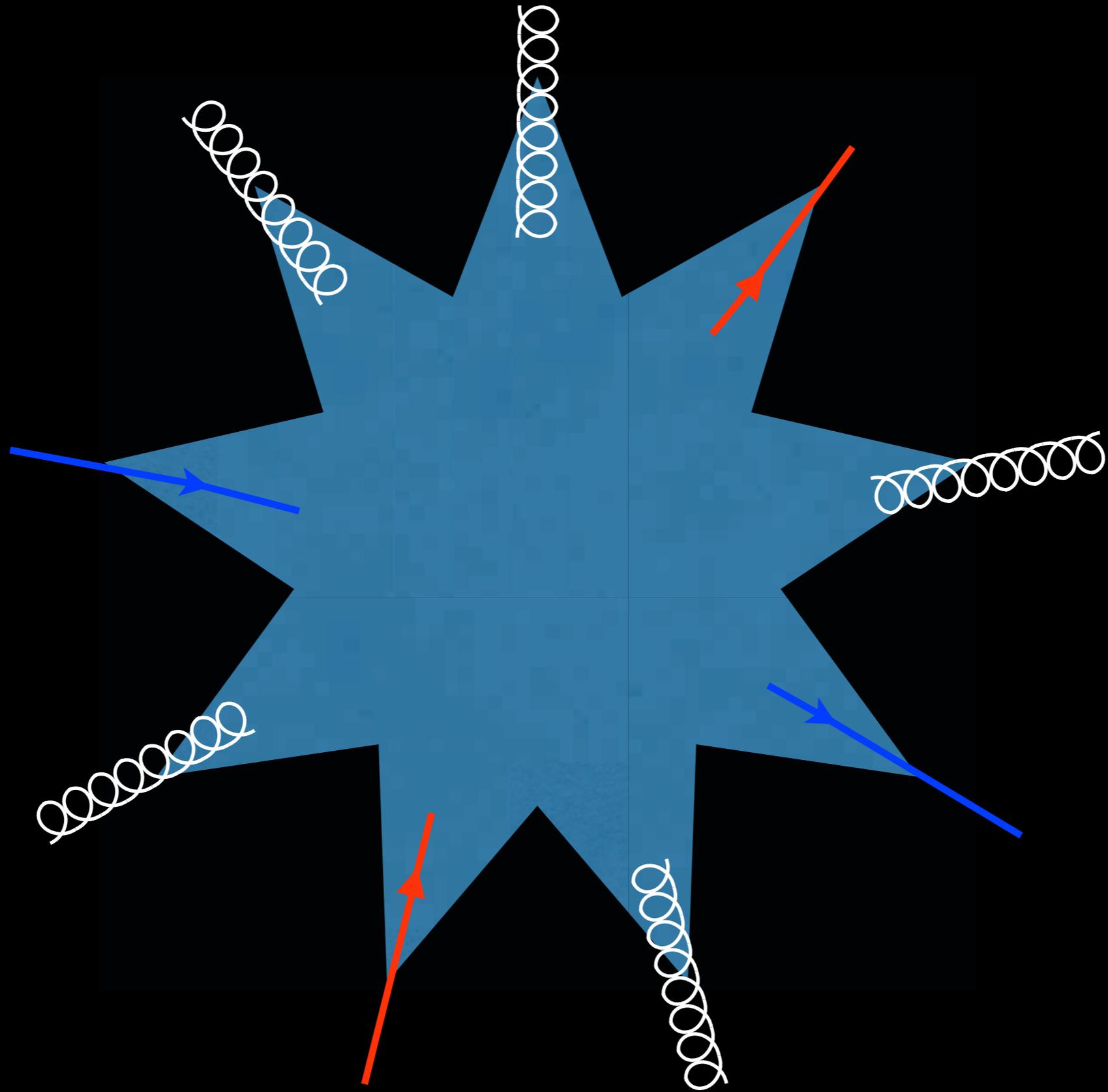
String of  $r$  Xs and  $r$  Ys such that the number of Xs is always greater than or equal to the number of Ys in any initial segment of the string.

$r=1$       XY

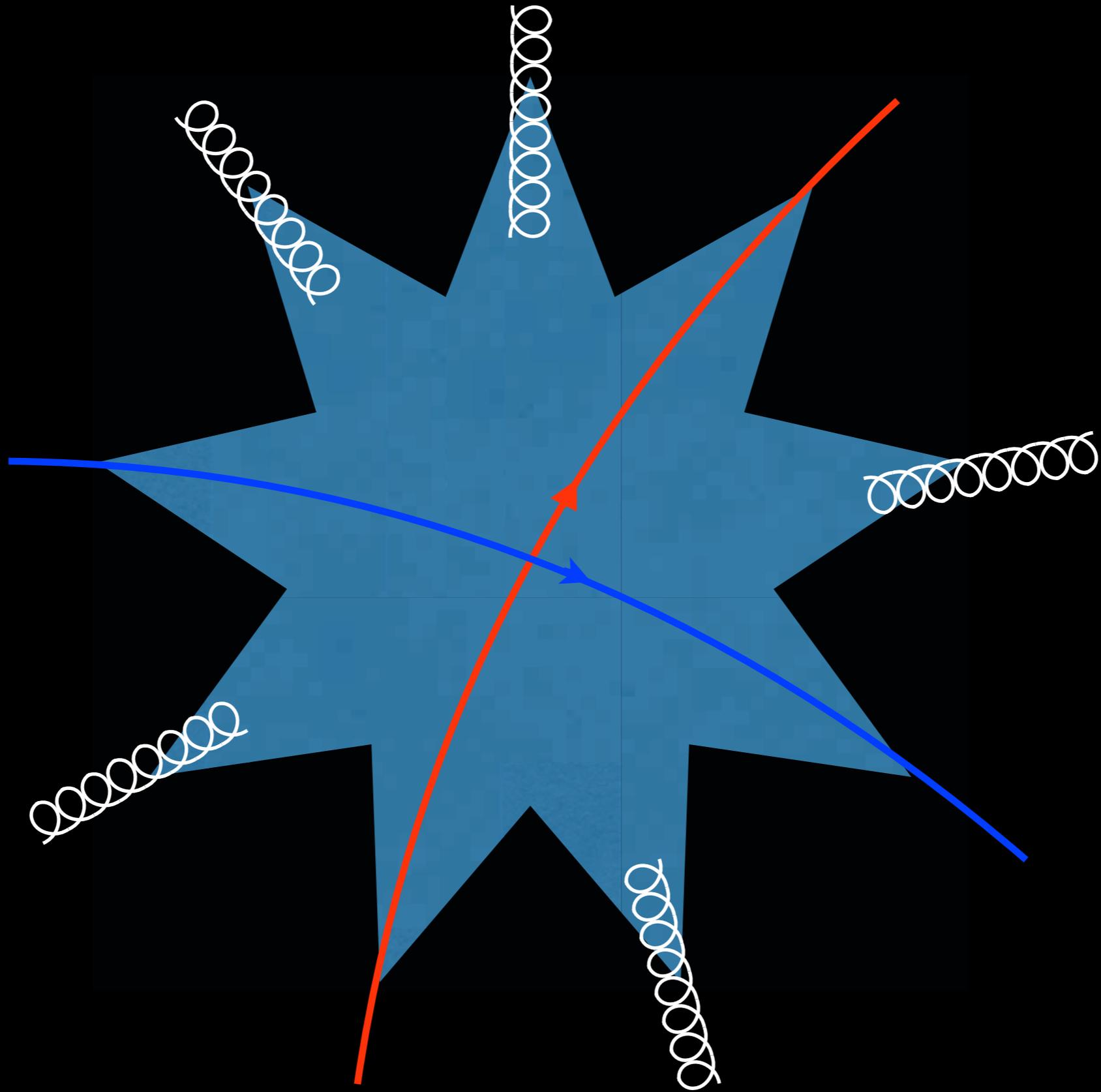
$r=2$       XXYY      XYXY

$r=3$       XXXYYY      XXYXY      XXYYXY      XYXXYY      XYXYXY

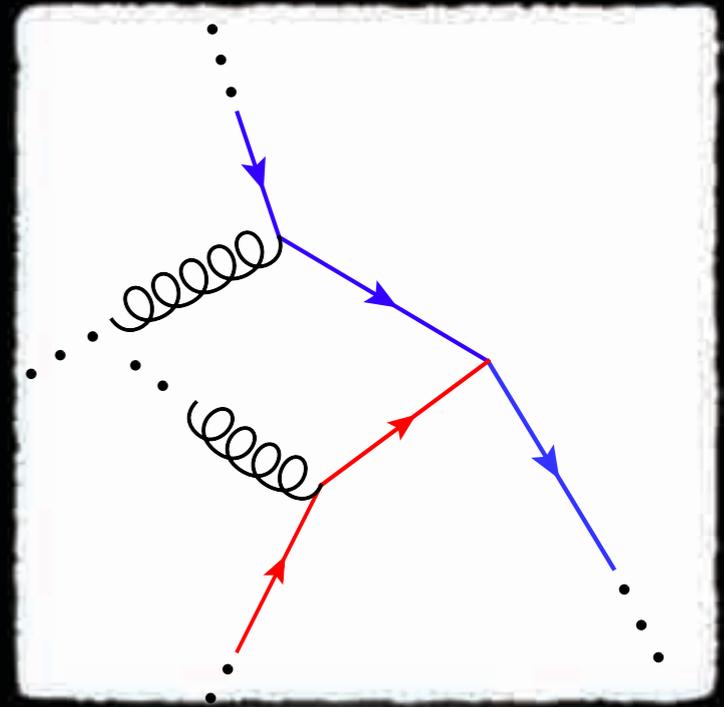
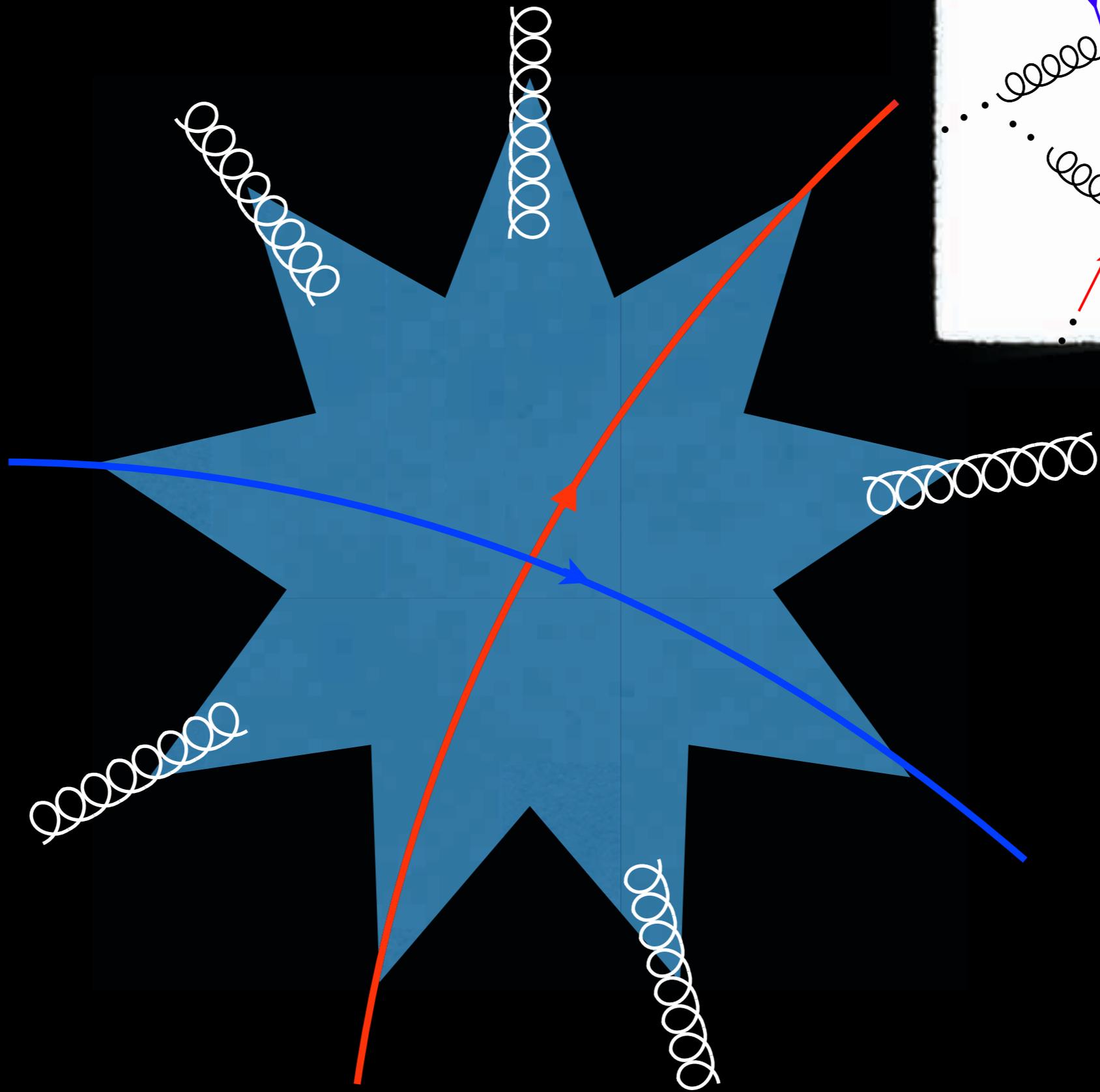
# Planarity



# Planarity



# Planarity



# Dyck word structure

$r=3$

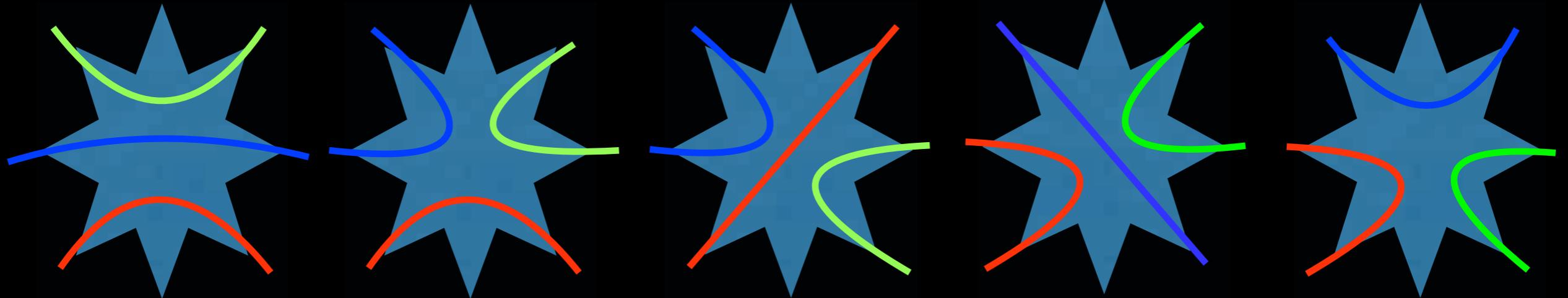
XXXYYY

XXYXYY

XXYYXY

XYXXYY

XYXYXY



determines # independent  
amplitudes

# One flavour recursion

$r=3$

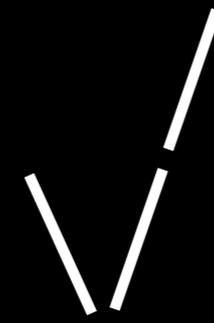
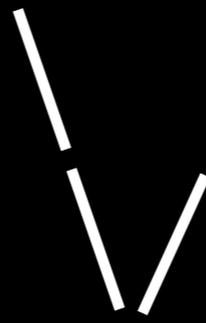
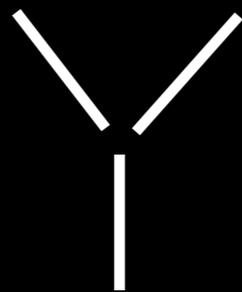
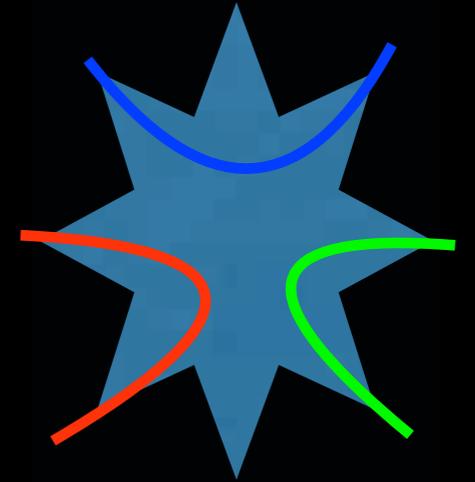
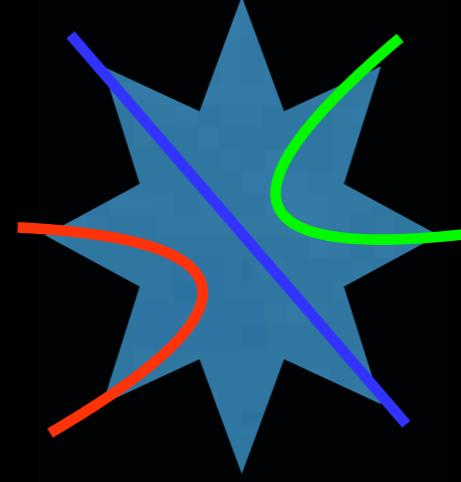
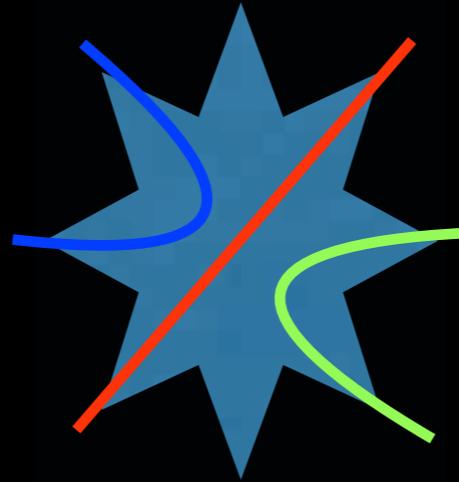
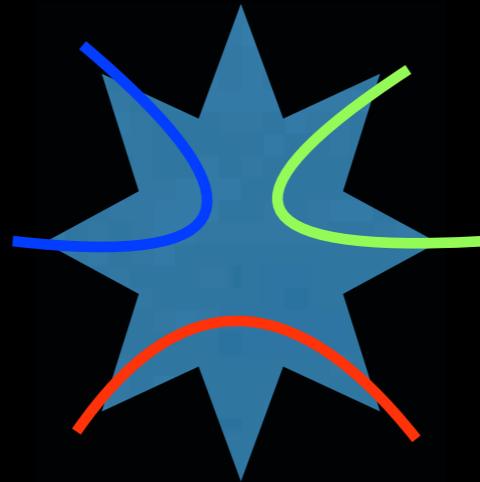
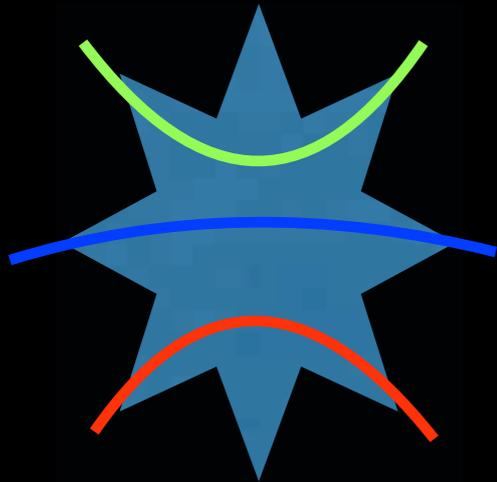
XXXYYY

XXYXYY

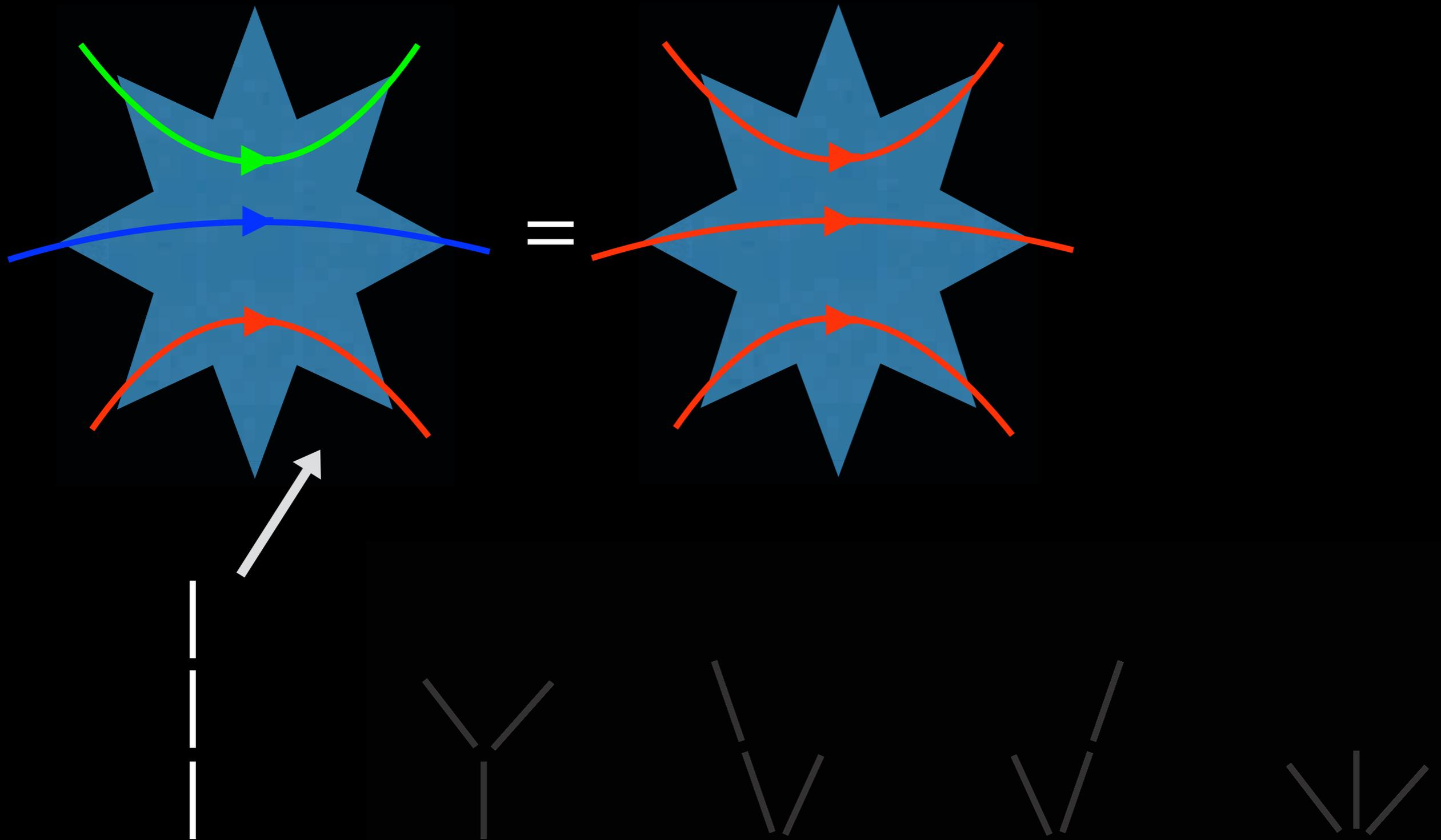
XXYYXY

XYXXYY

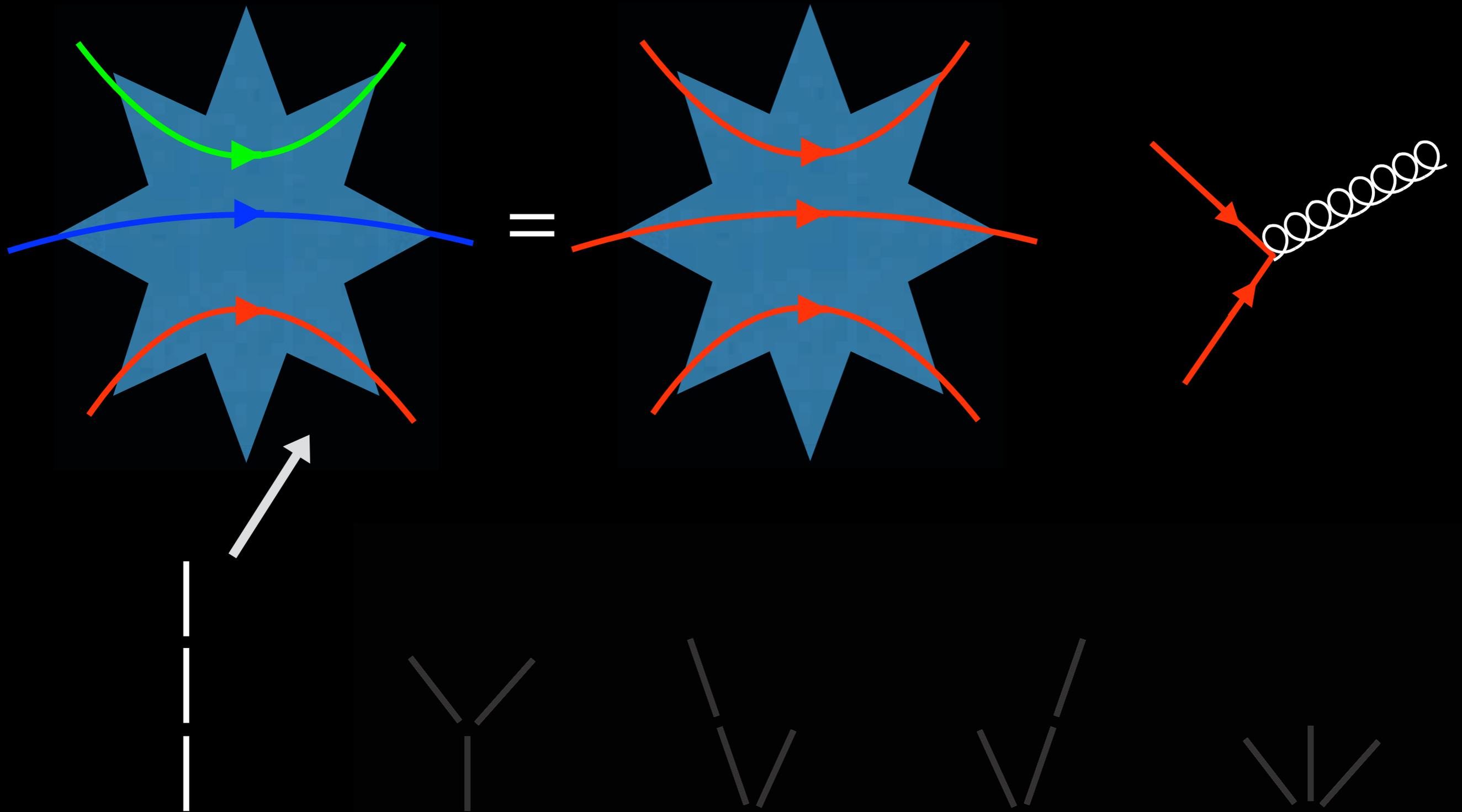
XYXYXY



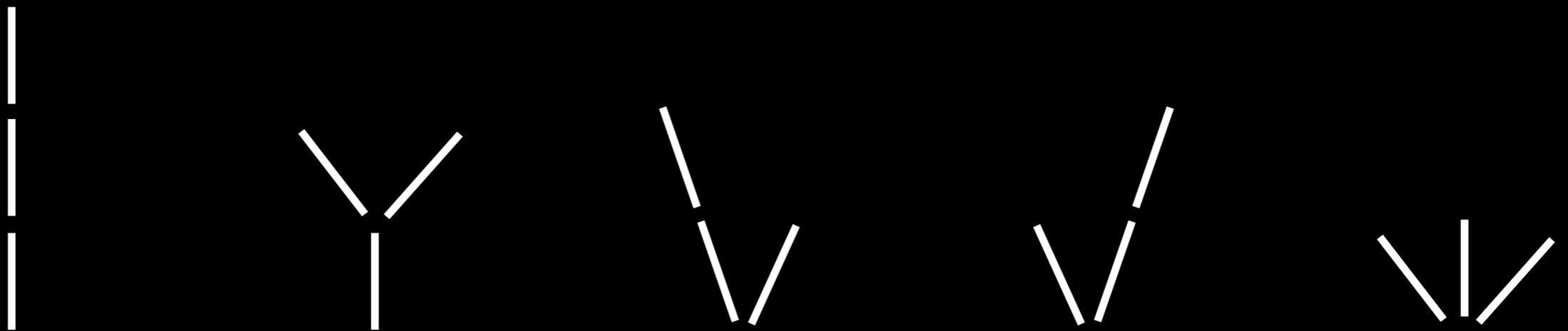
# One flavour recursion



# One flavour recursion



# One flavour recursion



# More feedback into QCD

This basis has provided a bridge for some of the most recent developments in the amplitudes field to be imported into QCD...

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BCJ relations

Bern, Carrasco, Johansson 2008



QCD trees

Johansson, Ochirov 2015  
de la Cruz, Kniss, Weinzierl 2015

CHY representation

Cachazo, He, Yuan 2014,15



QCD trees

de la Cruz, Kniss, Weinzierl 2015

# More feedback into QCD

JO conjecture on simple way  
to put colour back correctly...

$$A_{n,k}^{\text{tree}} = \sum_{\sigma \in \text{Melia basis}}^{z(n,k)} C(\underline{1}, \bar{2}, \sigma) A(\underline{1}, \bar{2}, \sigma),$$

Johansson, Ochirov 2015

c.f.

$$A = \sum_{\mathcal{P}(2,\dots,n)} \text{Tr}(T^{a_1}, T^{a_2}, \dots, T^{a_n}) A(1, 2, \dots, n)$$

# More feedback into QCD

JO conjecture on simple way to put colour back correctly...

$$\mathcal{A}_{n,k}^{\text{tree}} = \sum_{\sigma \in \text{Melia basis}}^{z(n,k)} C(\underline{1}, \bar{2}, \sigma) A(\underline{1}, \bar{2}, \sigma),$$

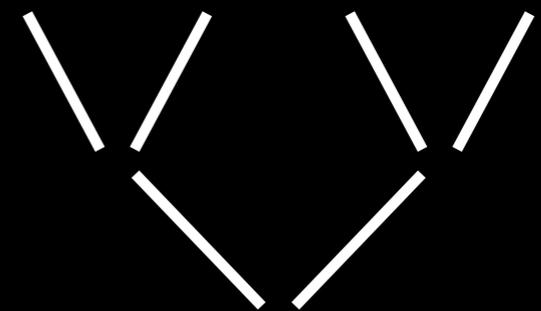
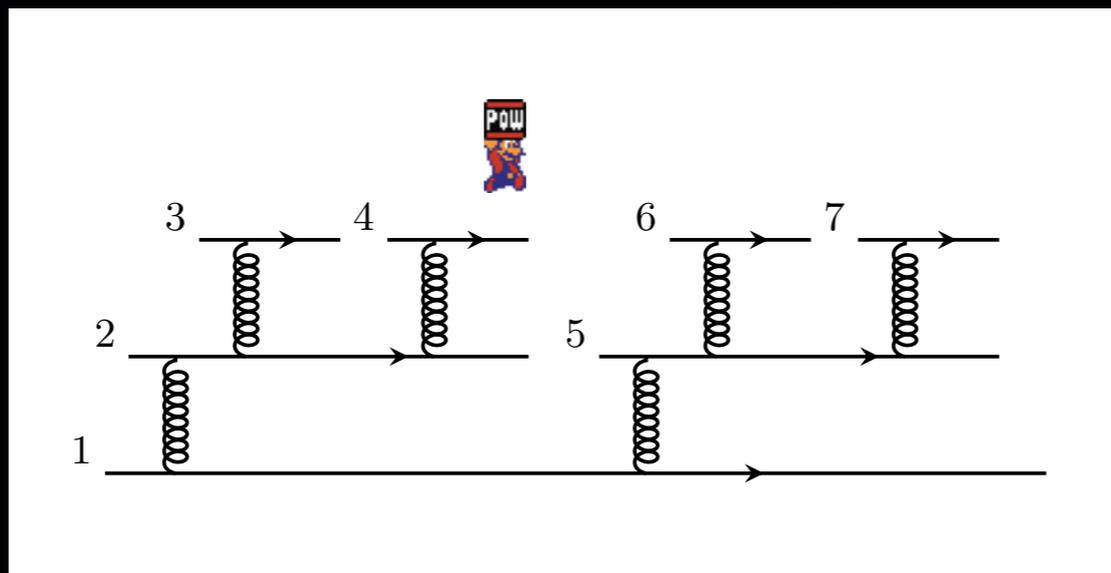
c.f.

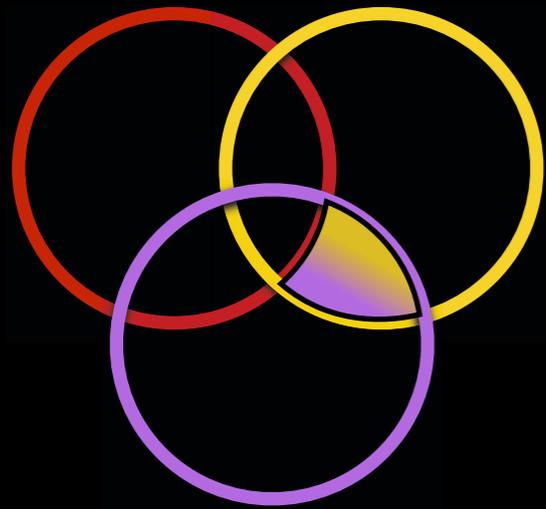
$$\mathcal{A} = \sum_{\mathcal{P}(2, \dots, n)} \text{Tr}(T^{a_1}, T^{a_2}, \dots, T^{a_n}) A(1, 2, \dots, n)$$

Johansson, Ochirov 2015

Proof using 'Mario World' Feynman diagrams

TM 2015





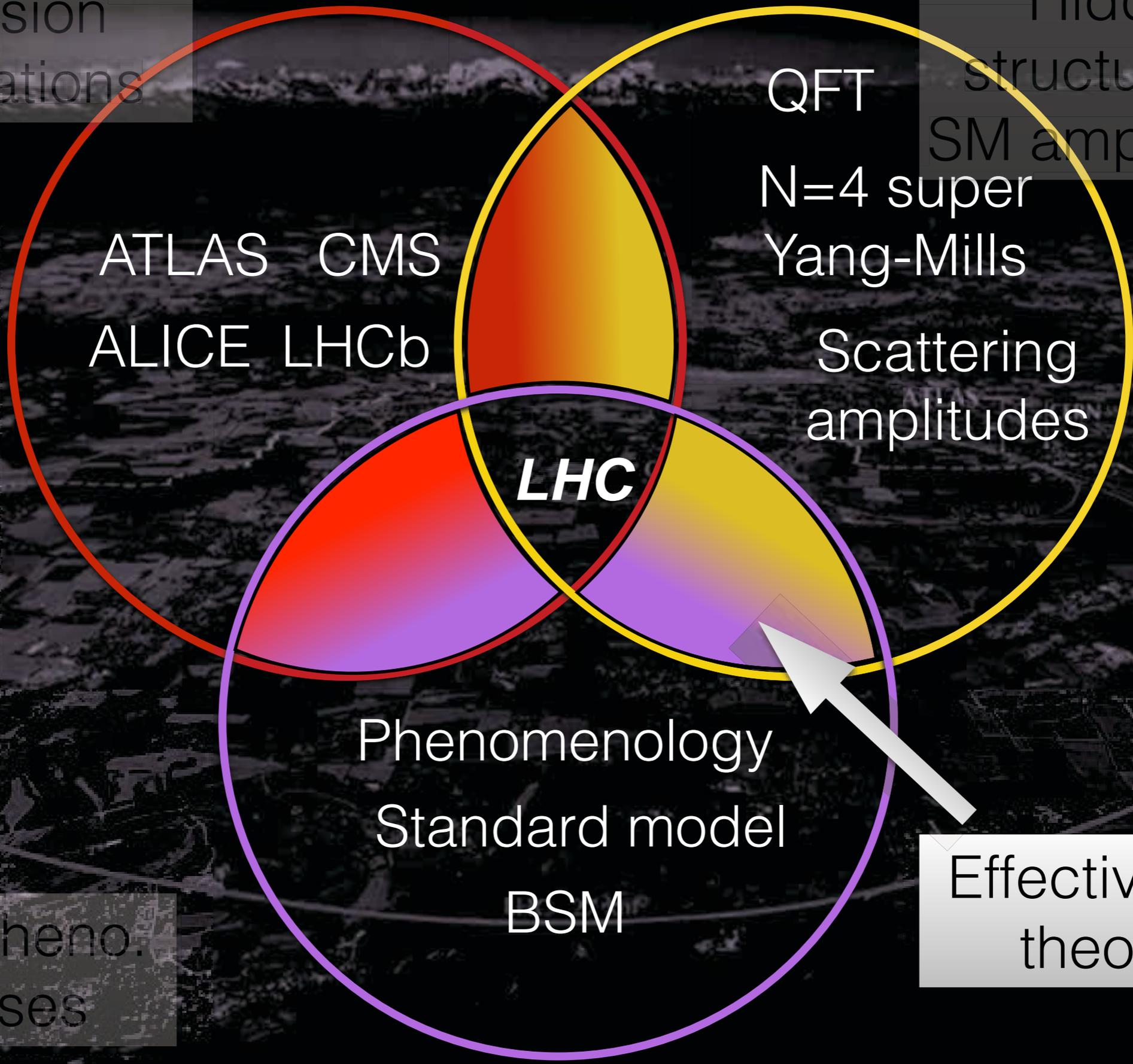
There are secrets in the  
standard model...

‘One flavour’ was pretty well hidden

What does it mean?

Precision calculations

Hidden structures in SM amplitudes



Novel pheno. analyses

UISSE  
FRANCE

CMS

ALICE

# Surprises in the structure of EFT

Ongoing work to understand mathematical structure of EFTs on general grounds

Henning, Lu, TM, Murayama 2015, 16...

The importance and ubiquity of EFTs has been understood for decades — remarkable that very basic questions about their structure are (were) unknown

# Lightening review...

$$\mathcal{L} = \sum_i c_i \mathcal{O}_i$$

It turns out the structure of an operator basis is controlled by the conformal algebra

Organize into irreps. of the conformal group — the basis is spanned by primary operators

# Application to the SM

On this operator basis we defined a generating function — Hilbert series

Evaluate to count the number of independent operators at a given mass dimension in the SM

Buchmuller, Wyler 1986



dim 6, 1 gen.

Grzadkowski et. al. 2010



dim 6, 1 gen, corrected

Manohar et. al. 2013



dim 6, Nf gen.

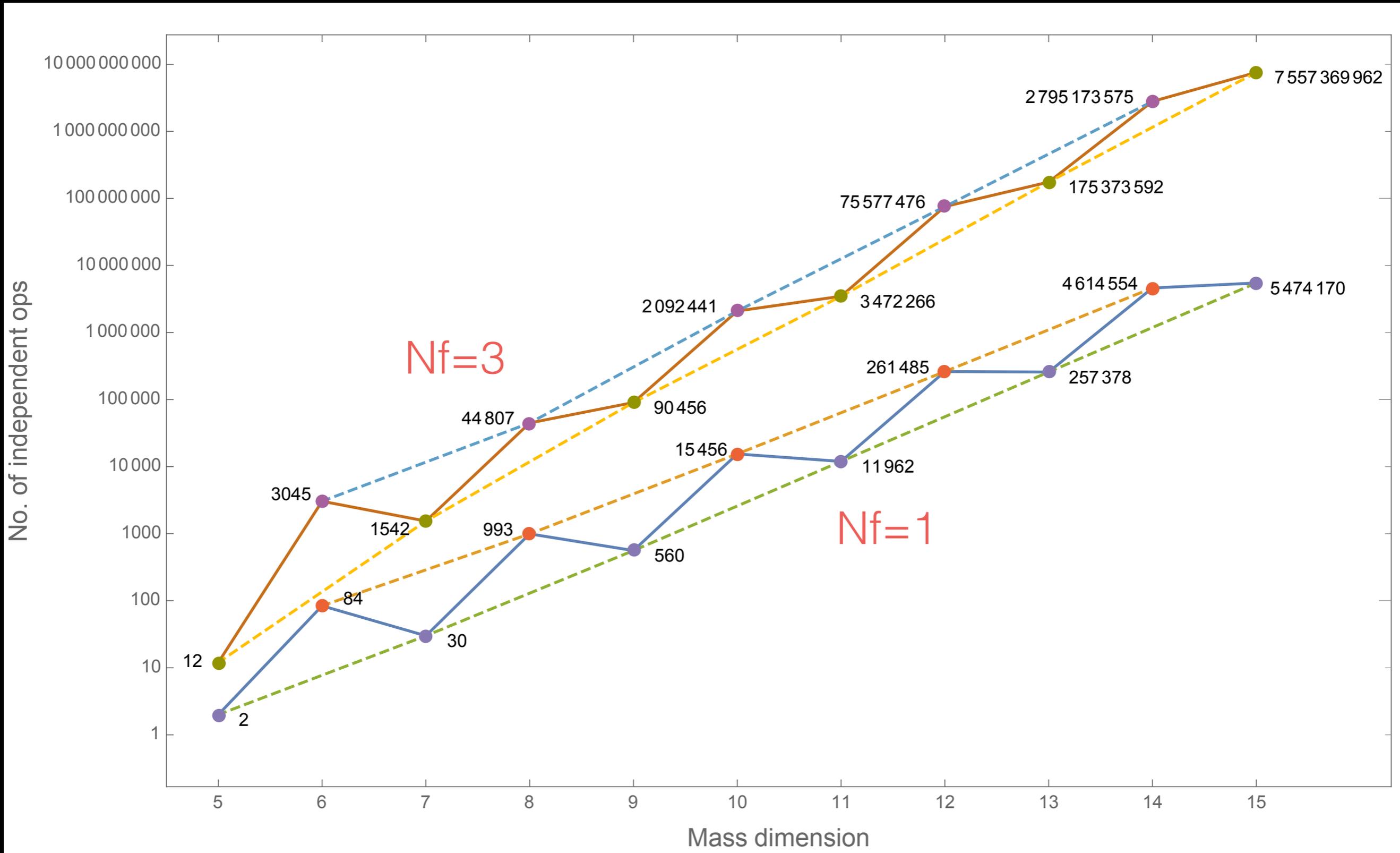
Lehman, Martin 2014



dim 7, Nf gen.

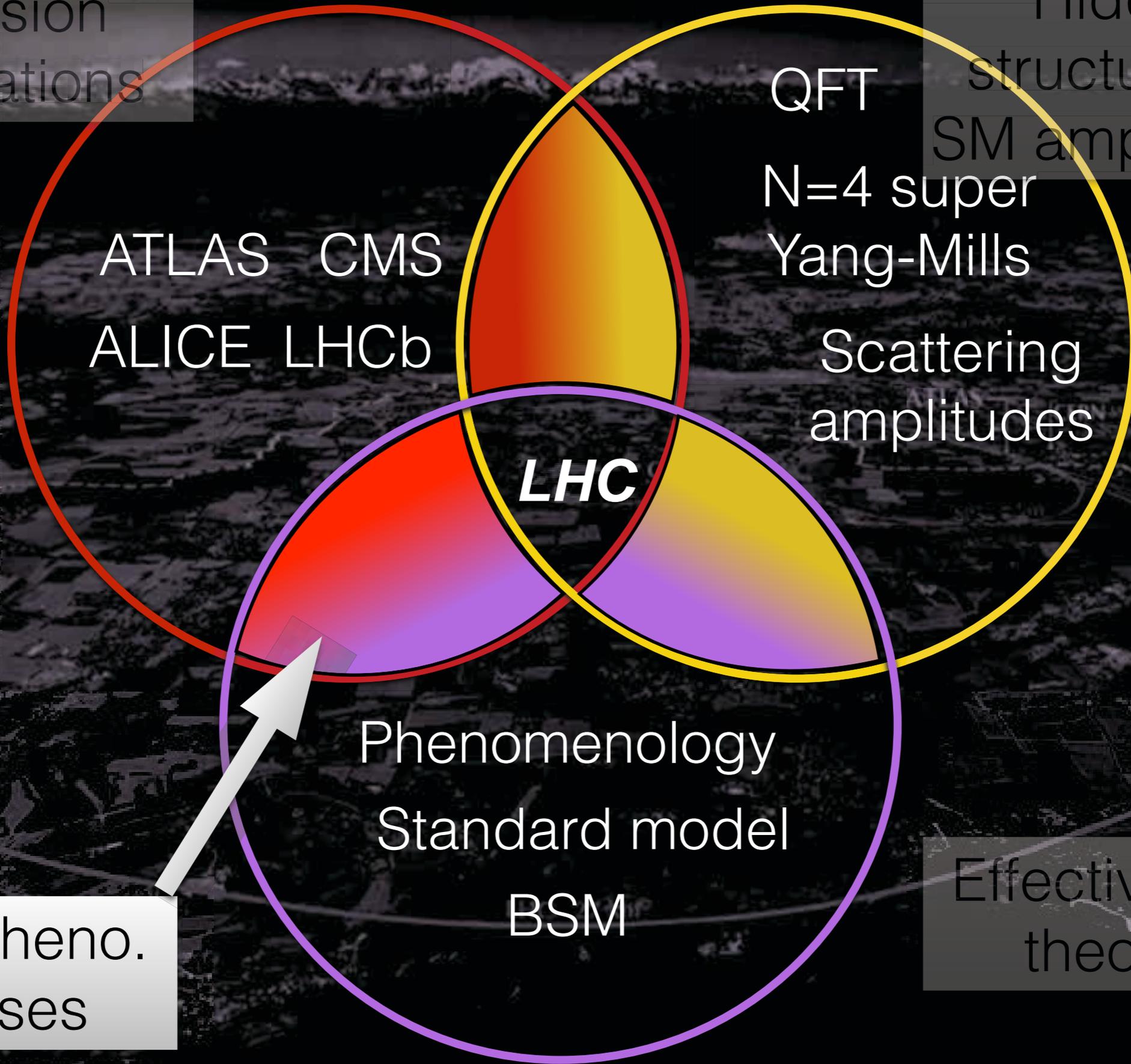
dim 8, 1 gen.

# Counting in the SM EFT



Precision  
calculations

Hidden  
structures in  
SM amplitudes



QFT  
N=4 super  
Yang-Mills  
Scattering  
amplitudes

ATLAS CMS  
ALICE LHCb

**LHC**

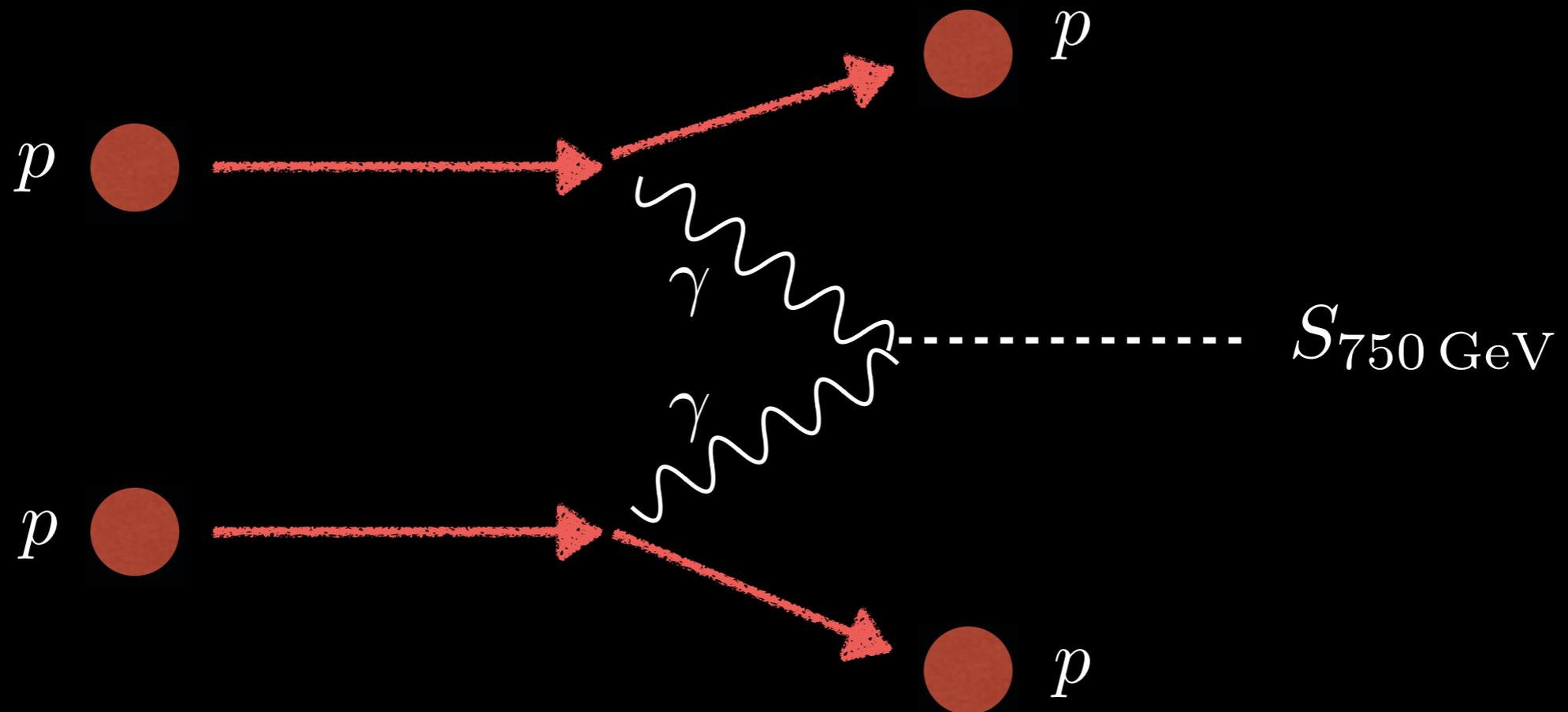
Phenomenology  
Standard model  
BSM

Effective field  
theories

Novel pheno.  
analyses



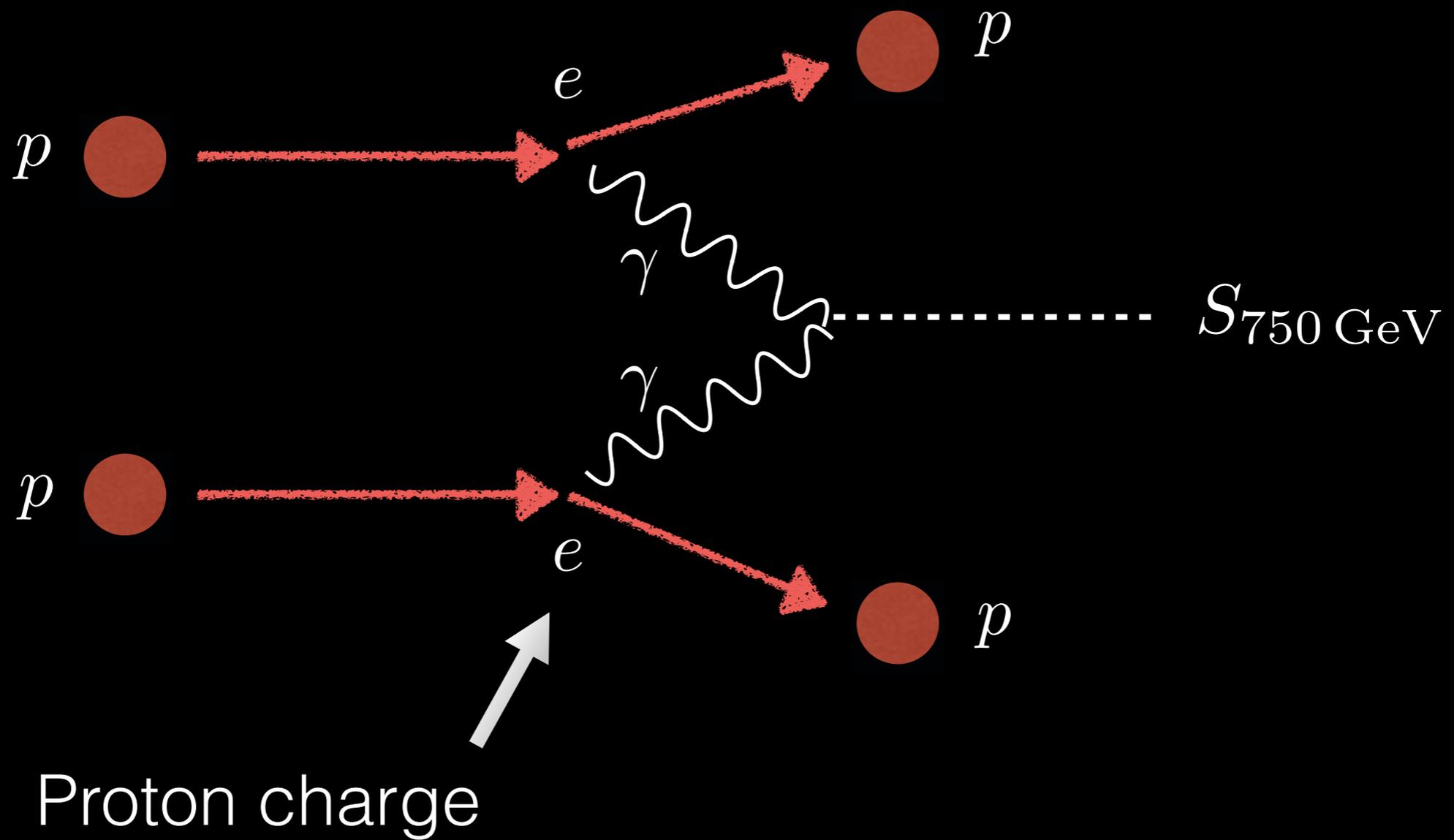
# Photon-photon fusion in elastic scattering



Csaki, Hubisz, Terning 15

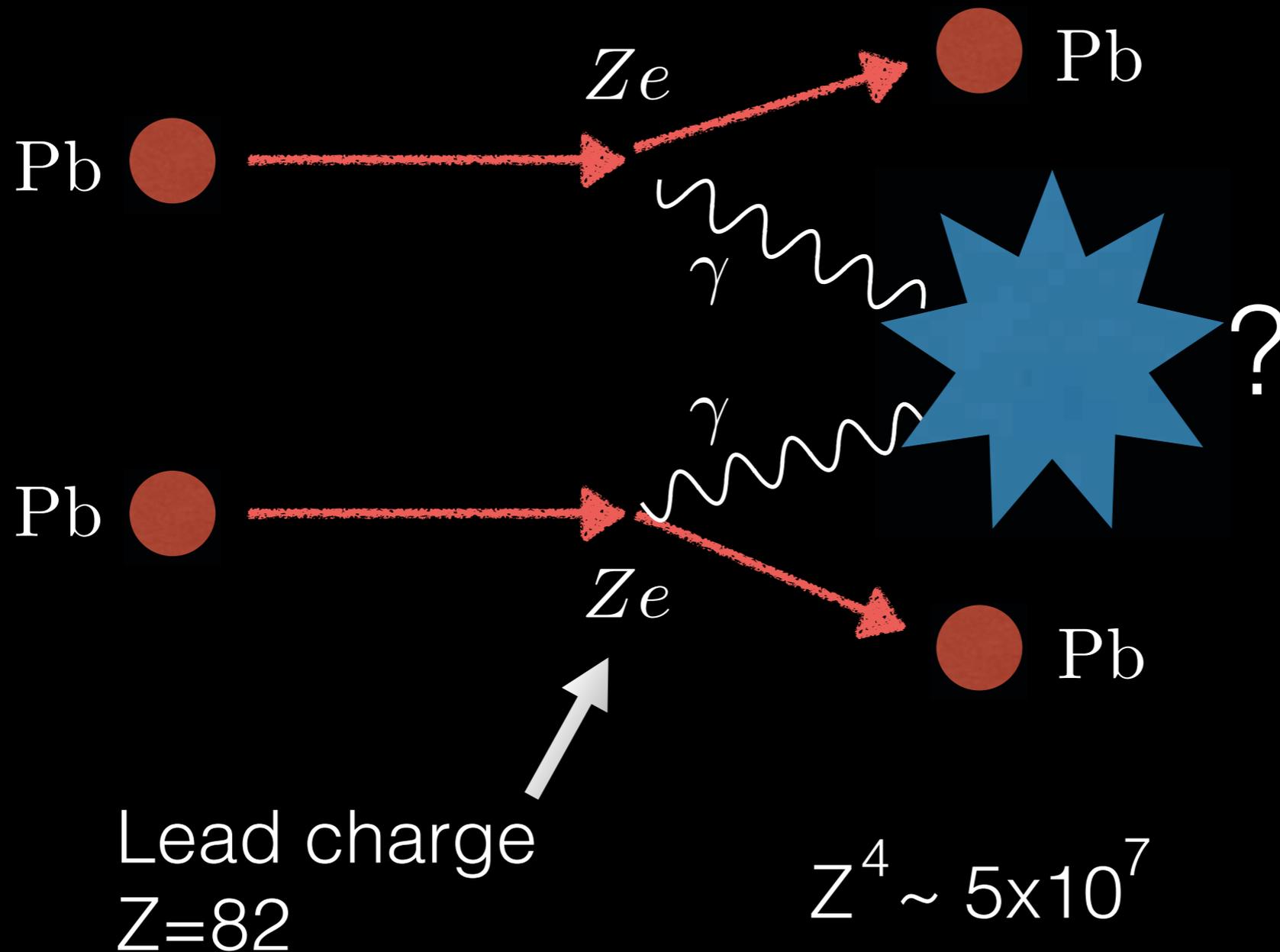
...

# Photon-photon fusion in elastic scattering

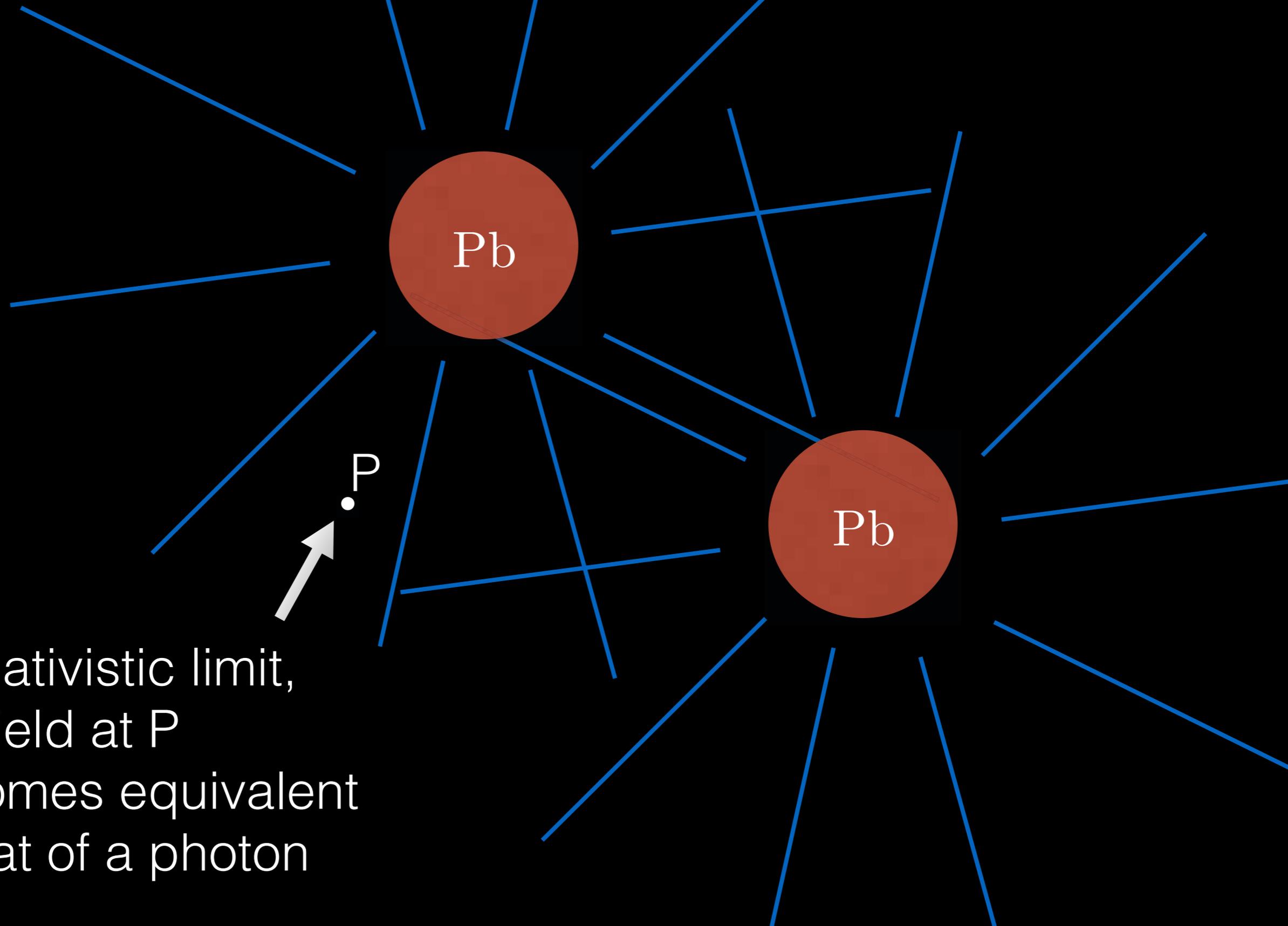


# Heavy ion 'photon collider'

(RHICs 'Gold Flashlight')

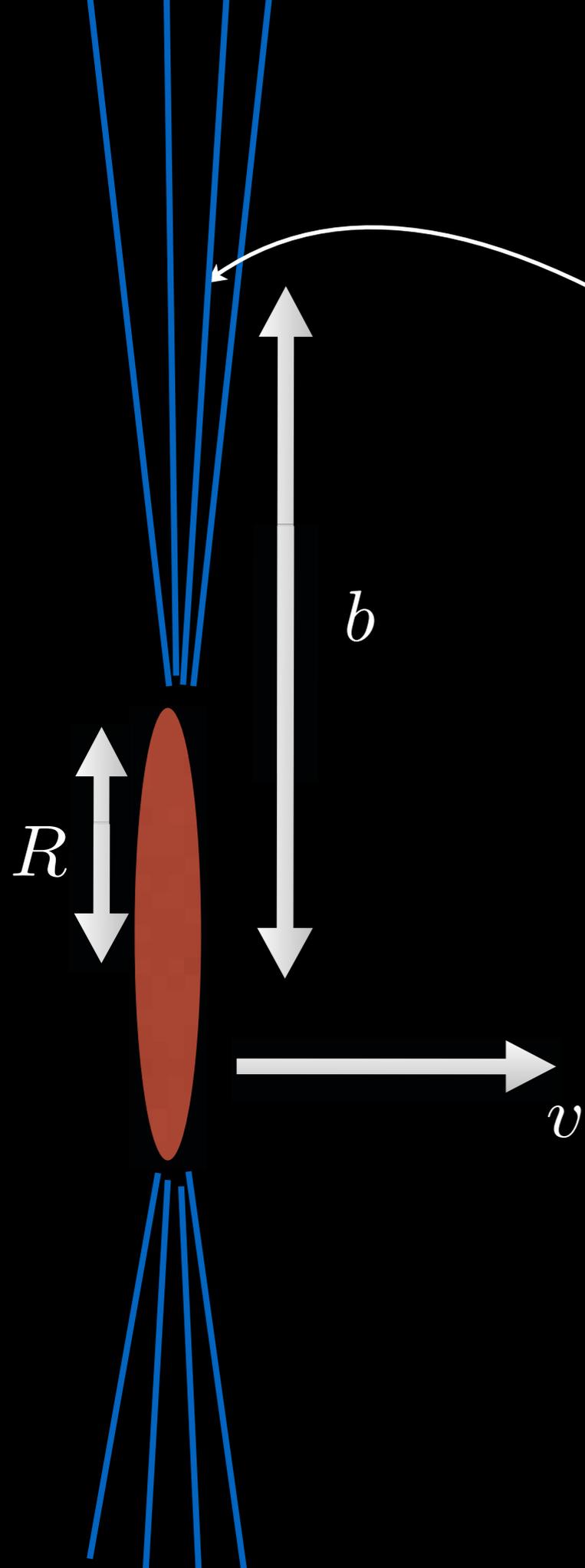


# Enrico Fermi's effective photons



In relativistic limit,  
EM field at P  
becomes equivalent  
to that of a photon

# Mass reach



$$\Delta t \sim \frac{b}{\gamma v} \implies \omega_{\max} \sim \frac{\gamma}{b}$$

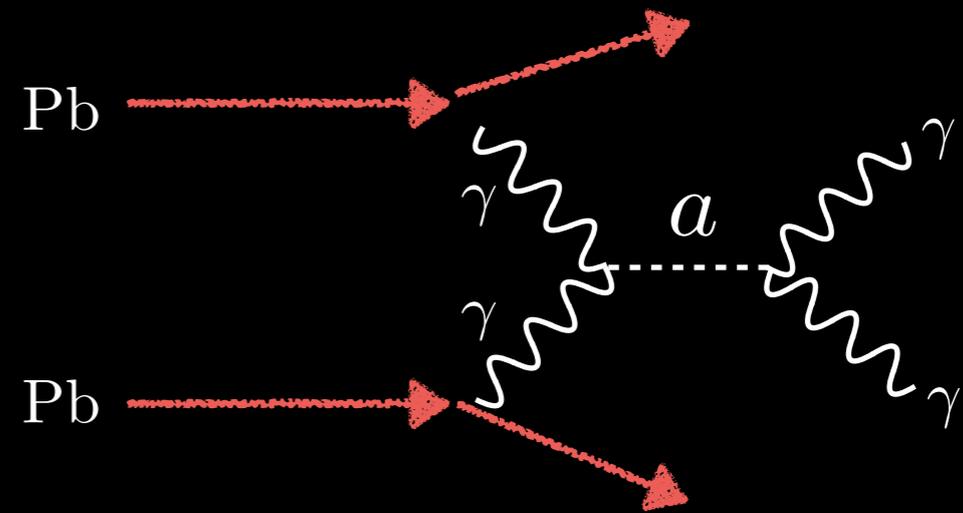
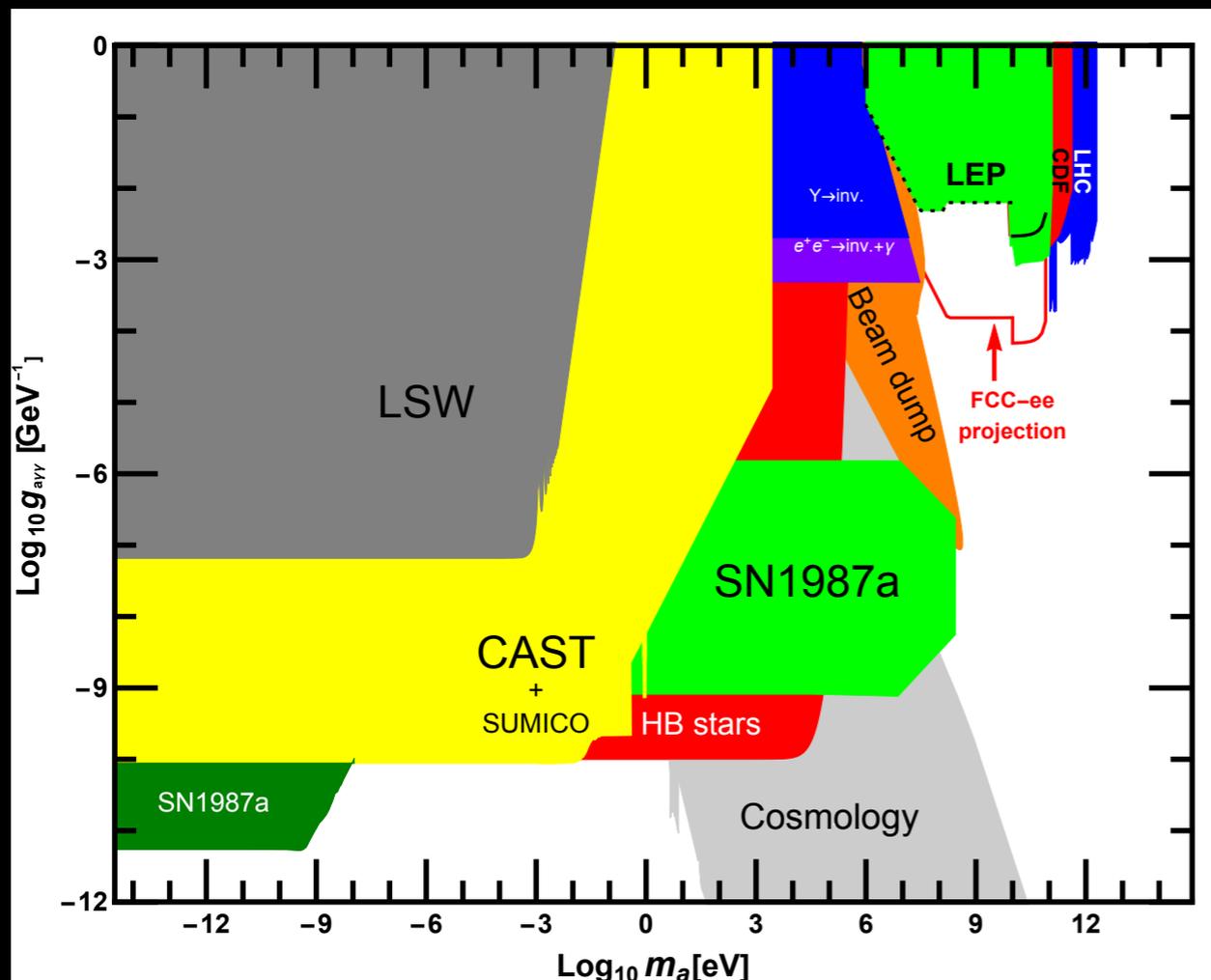
	$b_{\min} = 2R$	$E_{\text{nucleon}}$	$2\omega_{\max}$
$p$	1.6 fm	7.5 TeV	1500 GeV
Pb	14 fm	5.6 TeV	160 GeV

# Search for axion like particles

Knapen, Lin, Lou, TM 16

$$\mathcal{L} = \frac{1}{2}(\partial a)^2 - \frac{1}{2}M^2 a^2 - \frac{a}{\Lambda} F^{\mu\nu} \tilde{F}^{\mu\nu}$$

e.g. pseudo Nambu-Goldstone boson from some spontaneously broken symmetry



Sensitive to mass range  $M \sim \text{GeV}$

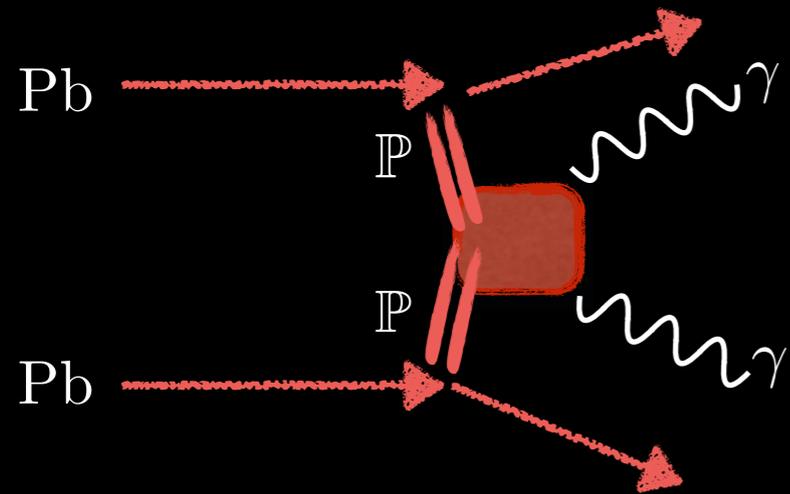
# How to trigger?

Two new triggers prepared (CMS Ultra-Peripheral Collisions working group analysis released soon)

Two photons with  $E > 2$  GeV and no hadronic activity in one of the forward calorimeters

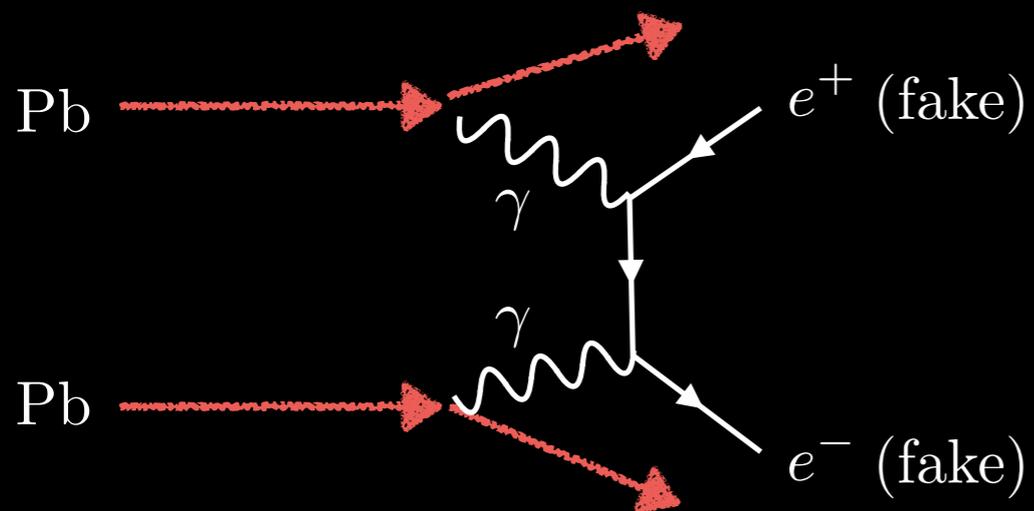
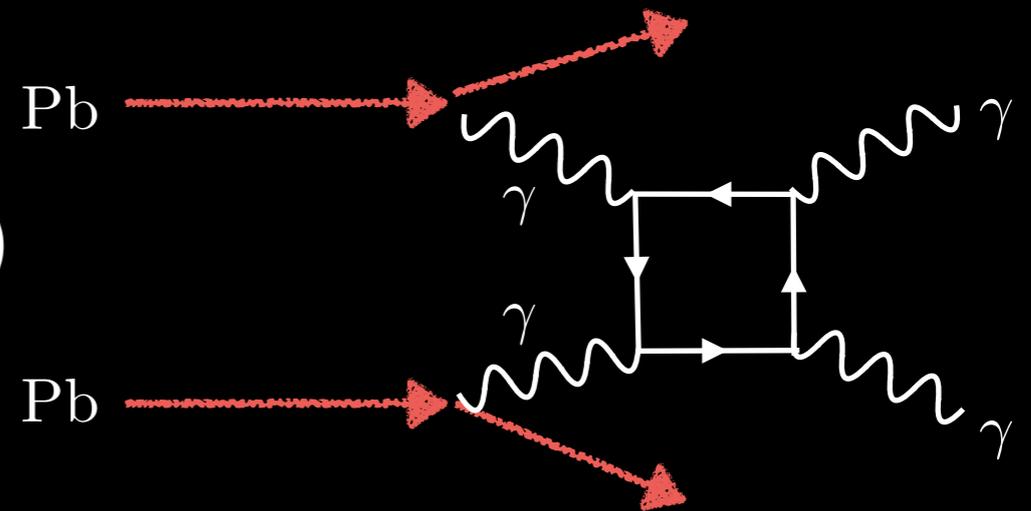
One photon  $E > 5$  GeV and no hadronic activity in one of the forward calorimeters

# Backgrounds



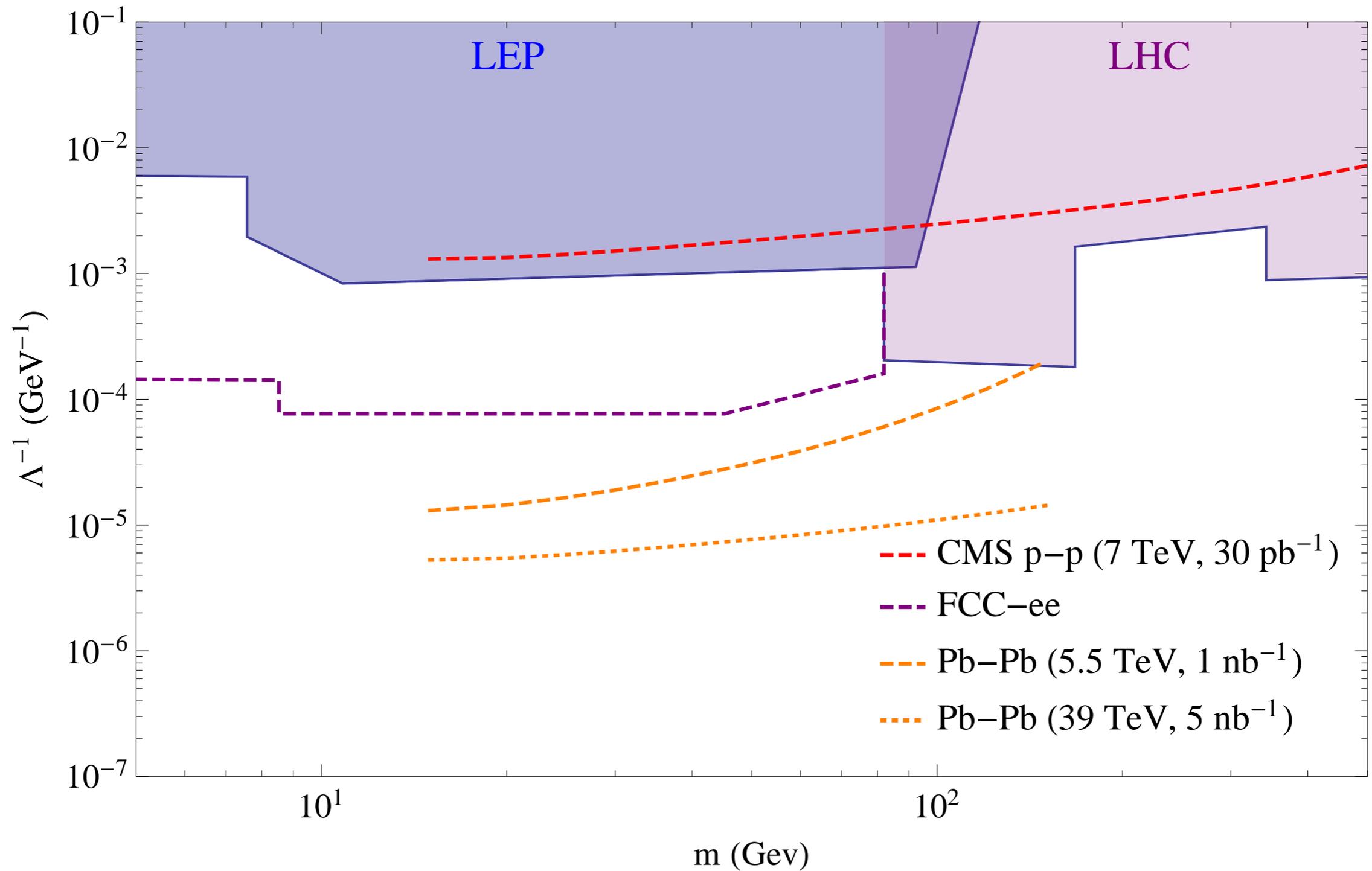
CEP (Central exclusive production)

LBL (Light by light)

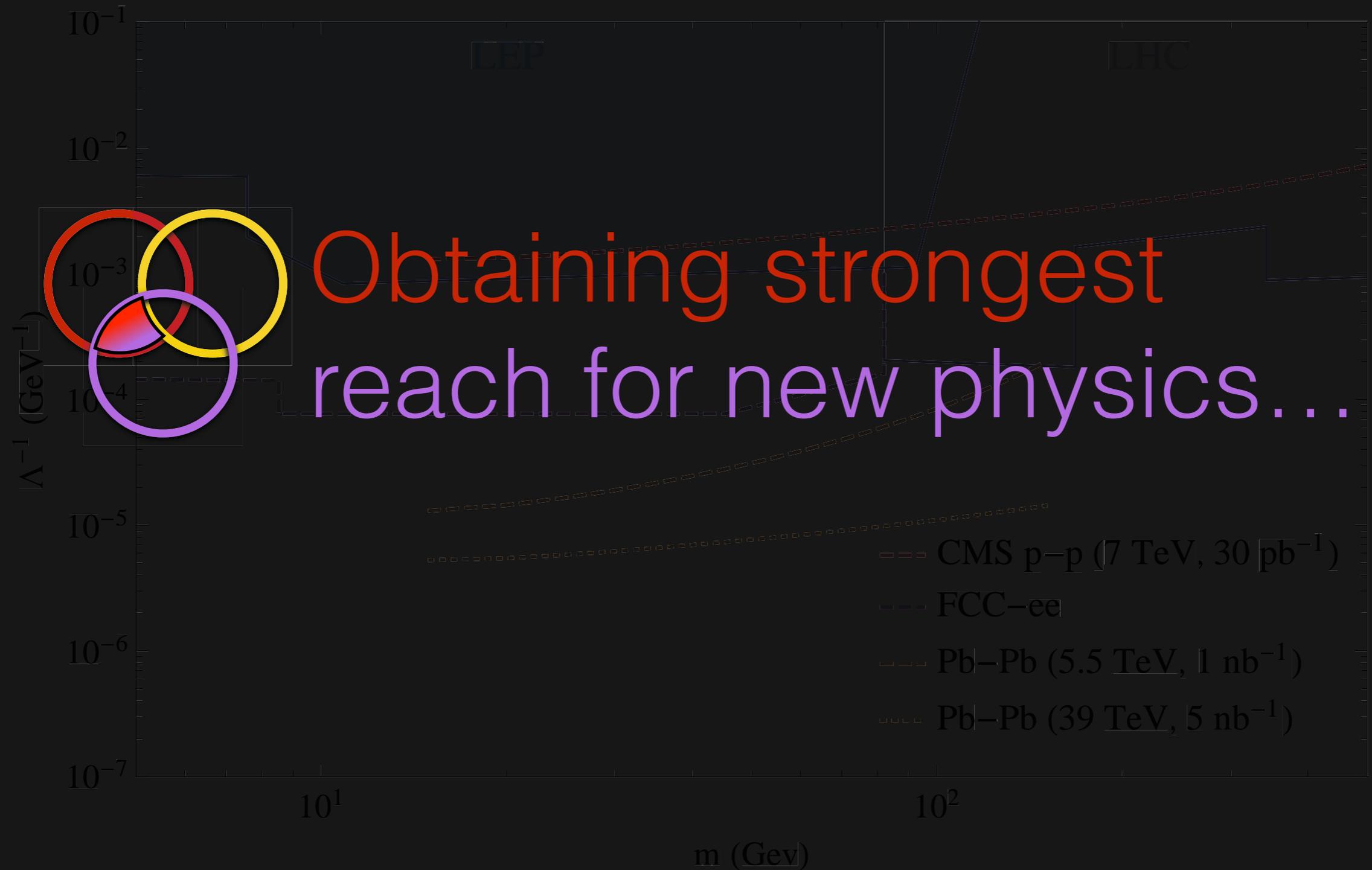


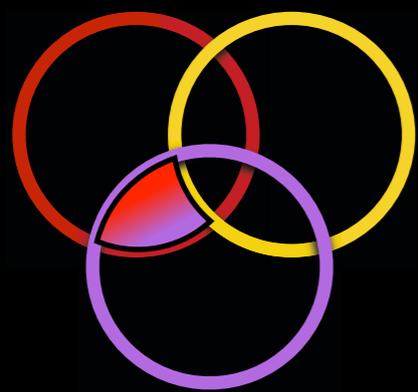
Fakes

# (Preliminary) limits...



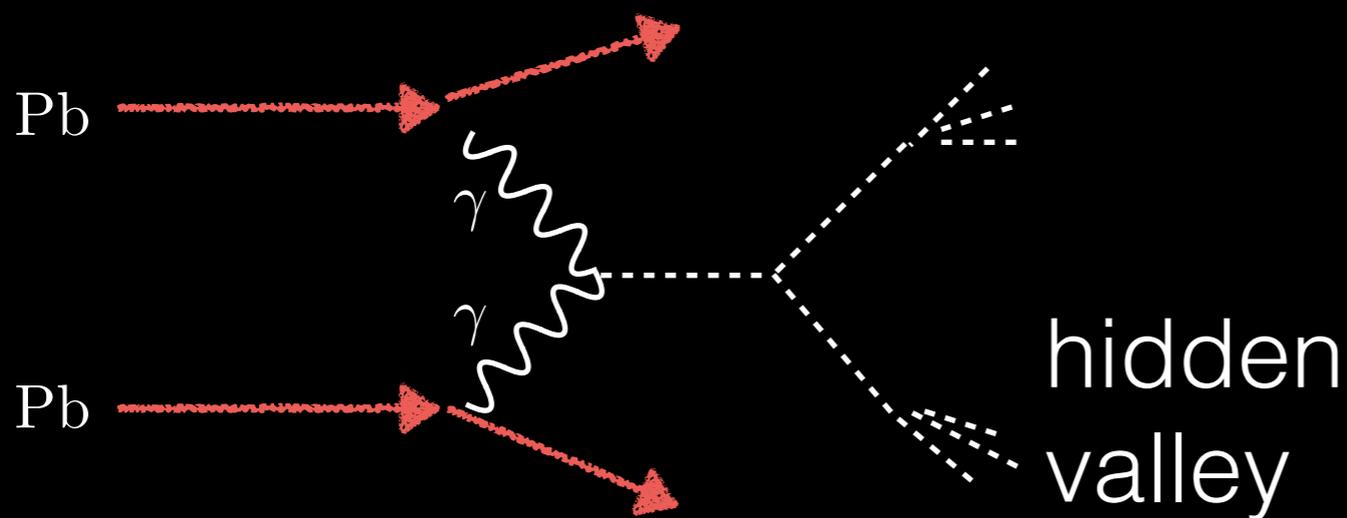
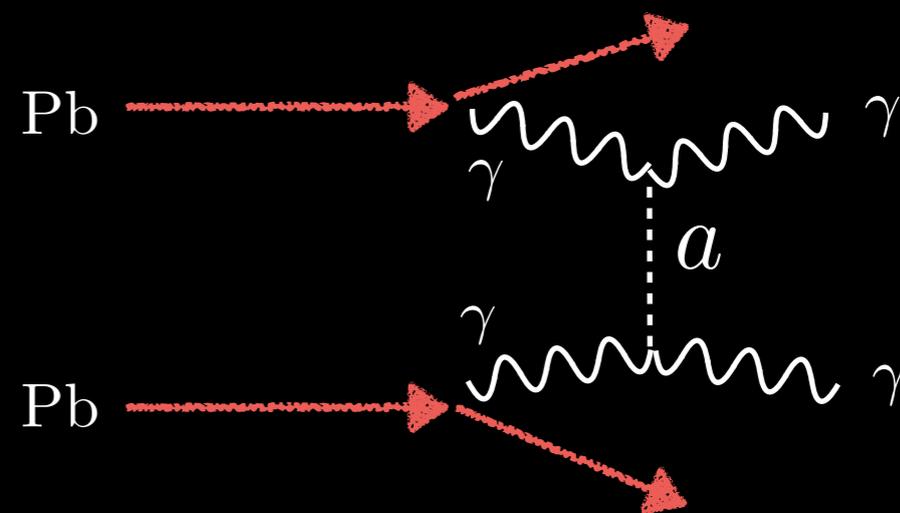
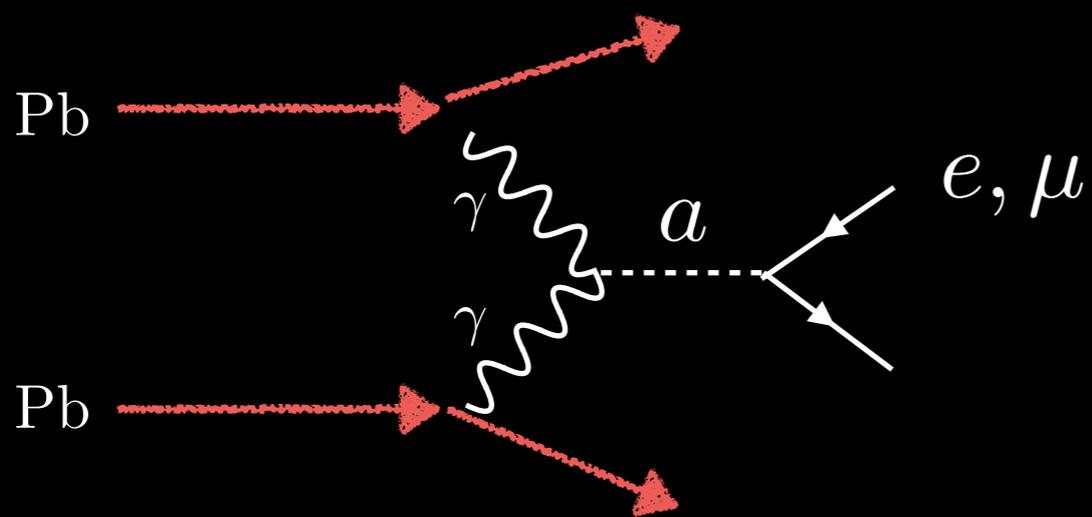
(Preliminary) limits...





# Gamma-gamma gateway...

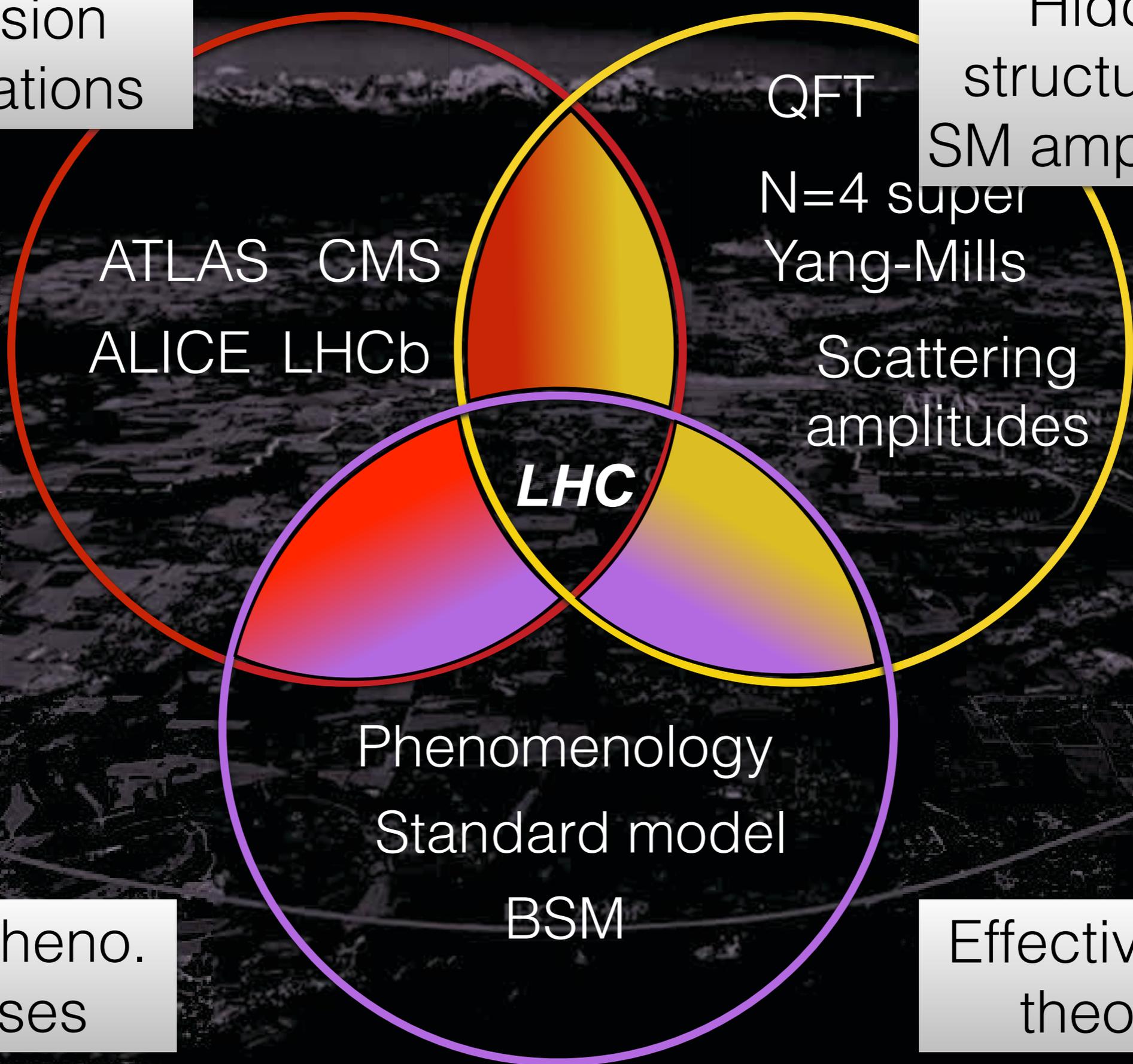
What else can you do with the worlds highest energy 'Lead flashlight'?



potential to exploit exquisite ALICE and LHCb tracking?

Precision  
calculations

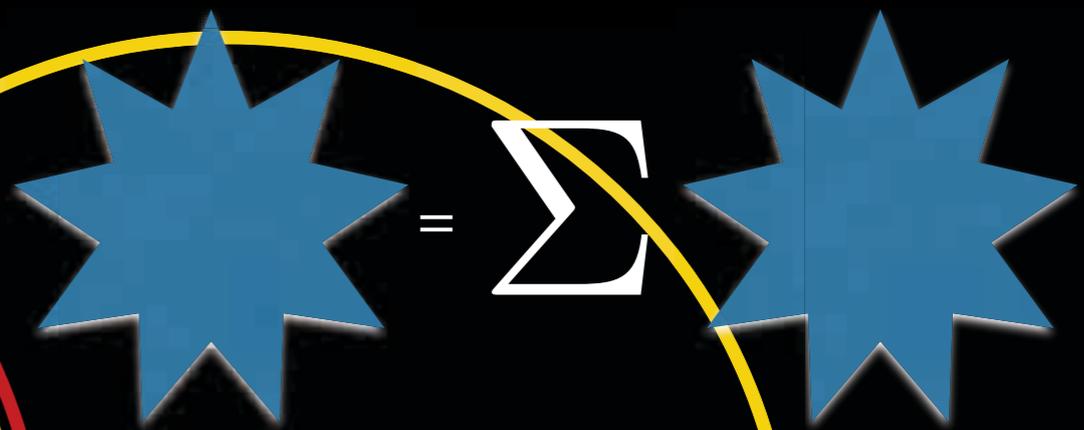
Hidden  
structures in  
SM amplitudes



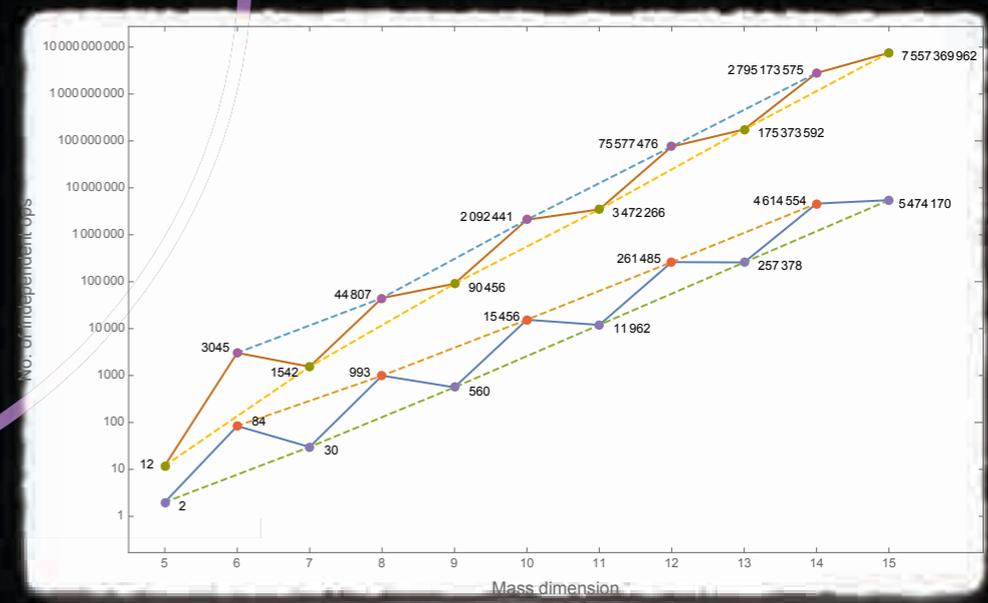
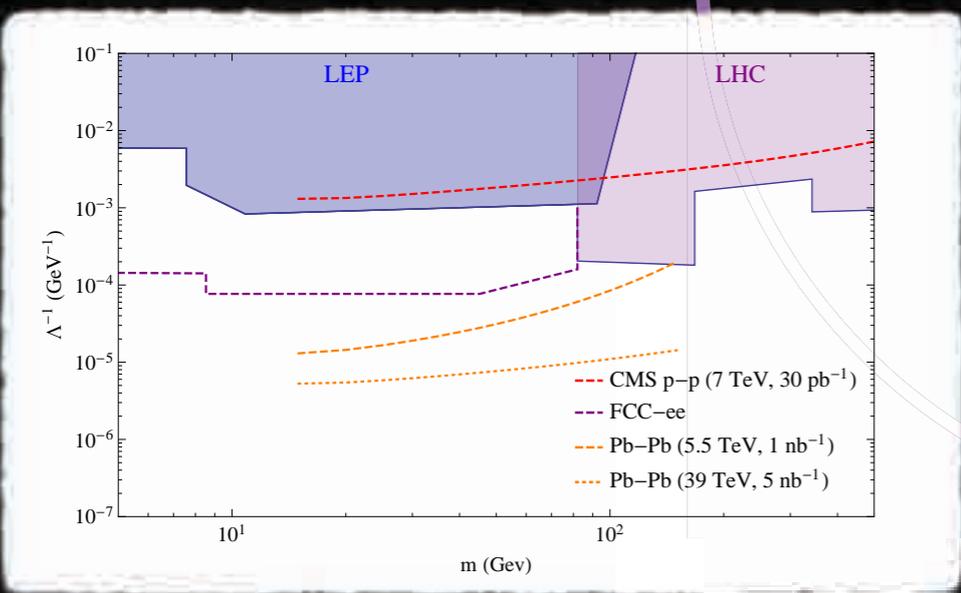
Novel pheno.  
analyses

Effective field  
theories

EFT coupling	Expected [TeV <sup>-2</sup> ]	Observed [TeV <sup>-2</sup> ]
$c_W/\Lambda^2$	[-3.7 ; 7.6]	[-4.3 ; 6.8]
$c_B/\Lambda^2$	[-270 ; 180]	[-320 ; 210]
$c_{WWW}/\Lambda^2$	[-3.9 ; 3.8]	[-3.9 ; 4.0]



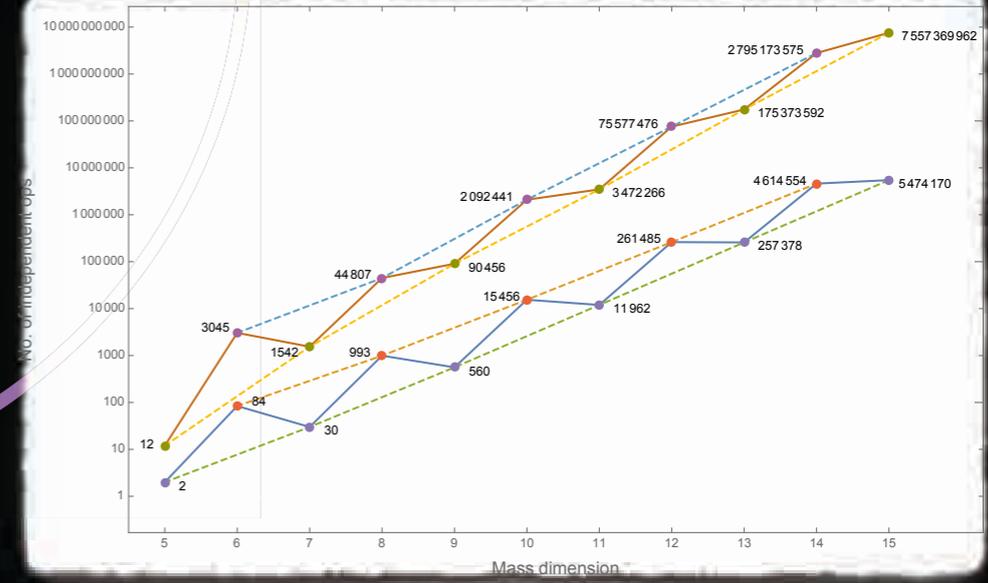
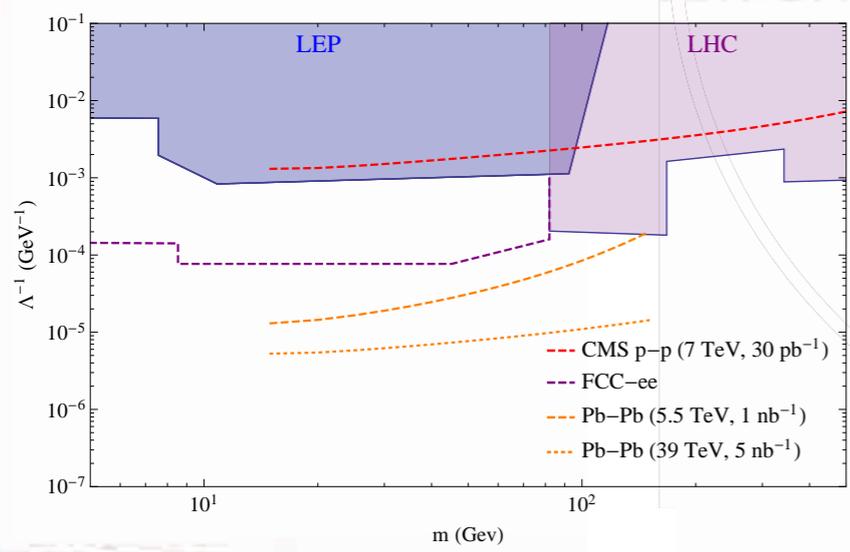
# The discovery potential of colliding frontiers...



EFT coupling	Expected [TeV <sup>-2</sup> ]	Observed [TeV <sup>-2</sup> ]
$c_W/\Lambda^2$	[-3.7 ; 7.6]	[-4.3 ; 6.8]
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LHC has run-time outlined -2035...

...more colliders on the way



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...colliding frontiers  
are an exciting  
place to be!

