

Inflation, Primordial Black holes and Gravitational Waves

-- Dawn of Gravitational Wave Astronomy --

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IPMU colloquium
24 January, 2018

Inflation

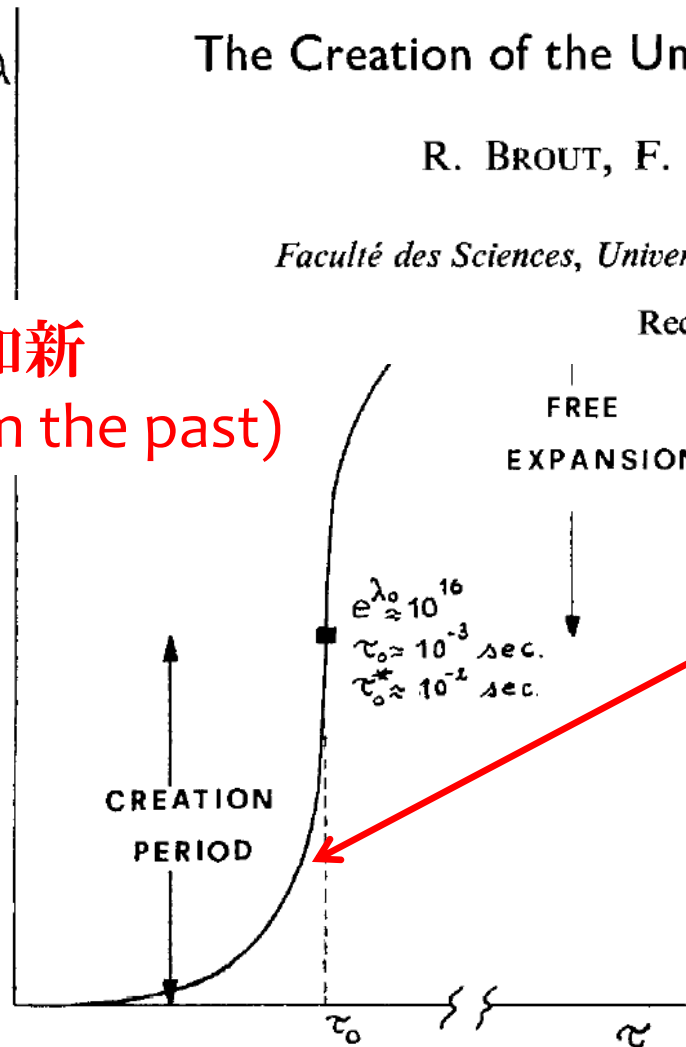
What is Inflation?

Brout, Englert & Gunzig '77, Starobinsky '79, Guth '81, Sato '81, Linde '81,...

- Inflation is a **quasi-exponential expansion** of the Universe at its very early stage; perhaps at $t \sim 10^{-36}$ sec.
- It was meant to solve **the initial condition (singularity, horizon & flatness, etc.) problems** in Big-Bang Cosmology:
 - if any of them can be said to be solved depends on precise definitions of the problems.
- **Quantum vacuum fluctuations** during inflation turn out to play the most important role. They give the initial condition for **all the structures in the Universe**.
- **Cosmic gravitational wave background** is also generated.

In summary, the picture that emerges is in complete accord with the kinematic generalities of causal cosmology presented in Section 2. For $y < y_0$, one has $p < 0$ ($p \simeq -\sigma$). For $y > y_0$, p becomes positive and λ undergoes an inflection. The situation is summarized in Figs. 1 and 2.

温故知新
(learning from the past)



The Creation of the Universe as a Quantum Phenomenon

R. BROUT, F. ENGLERT, AND E. GUNZIG

Faculté des Sciences, Université Libre de Bruxelles, Bruxelles, Belgium

Received July 7, 1977

$$ds^2 = -dt^2 + a^2(t)dH_{(3)}^2;$$

$$a(t) \simeq H^{-1} \sinh Ht$$

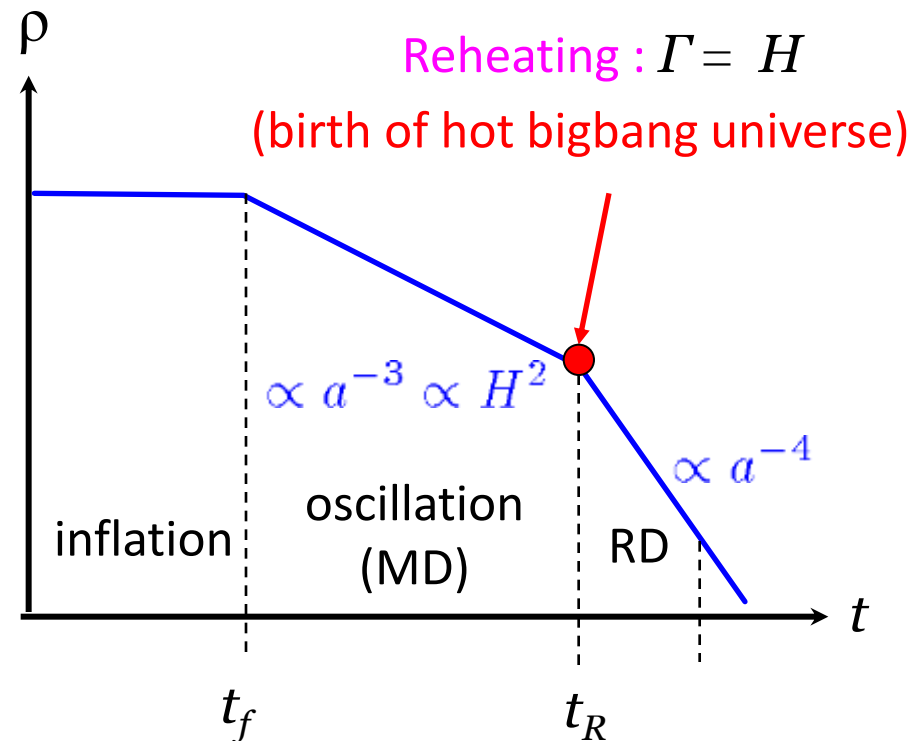
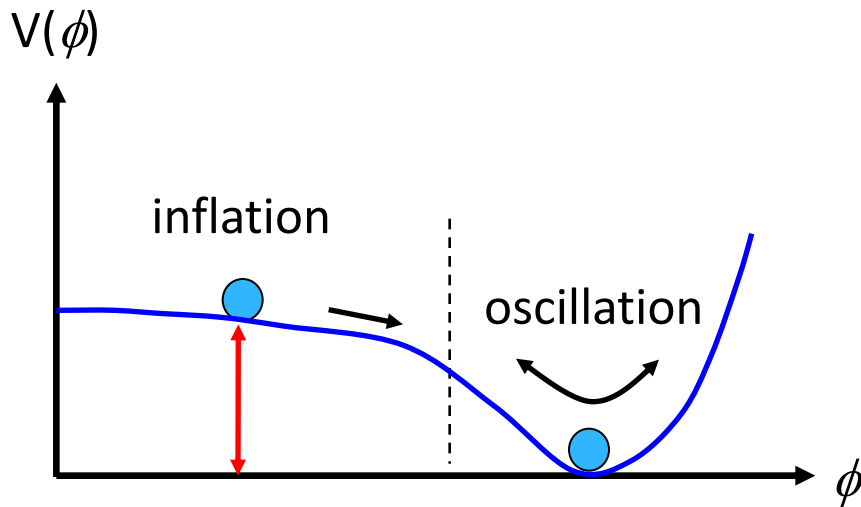
Creation of
Open Universe!

Now in the context of
String Landscape

FIG. 1. λ as a function of kinematical time τ for $\delta = 0$. Time scales are calculated for $m = 1$ GeV.

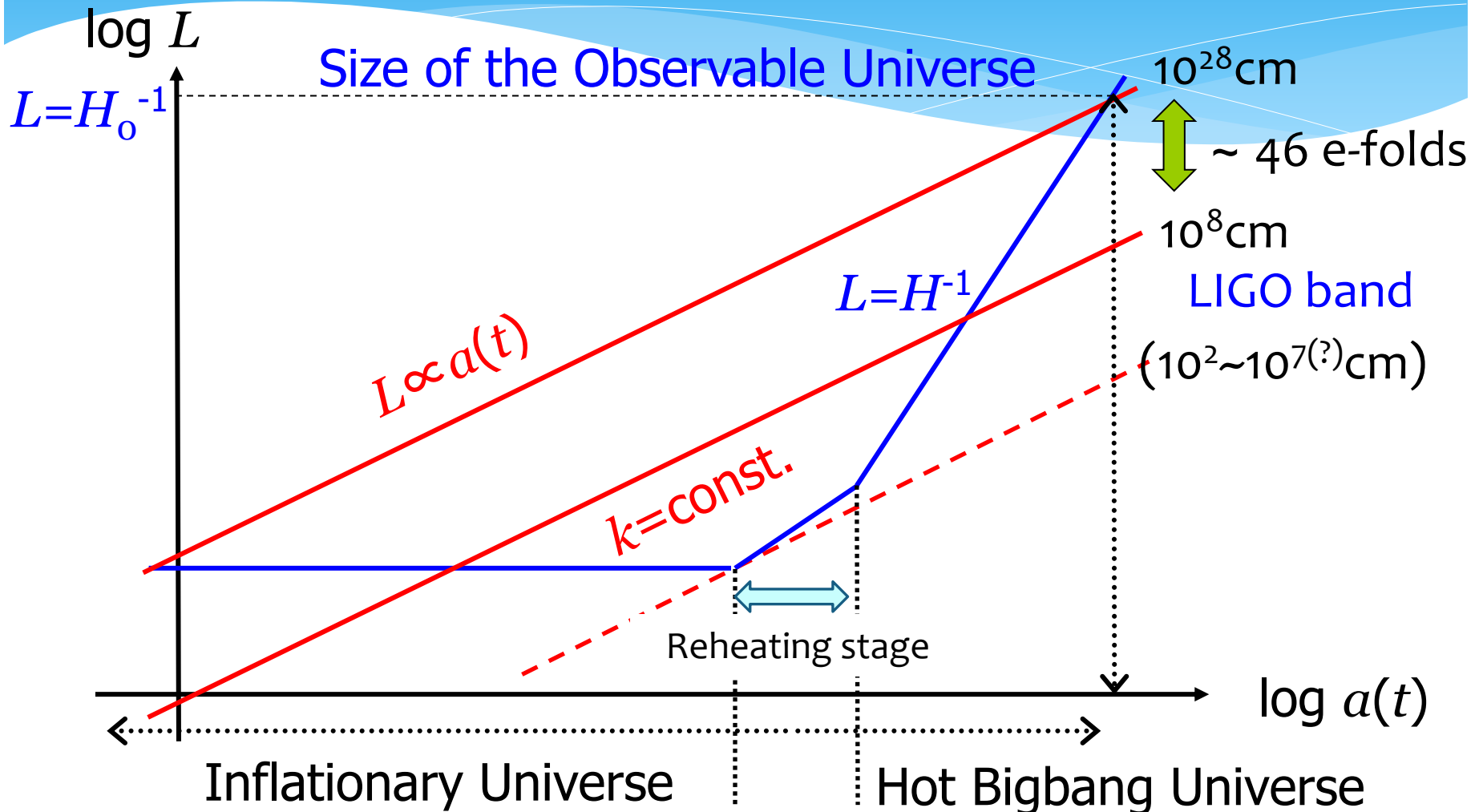
From inflation to bigbang

After inflation, vacuum energy is converted to **thermal energy** (called “**re**”heating) and **hot Bigbang Universe** is realized.



length scales of the inflationary universe

↔ targets for multi-frequency GW astronomy



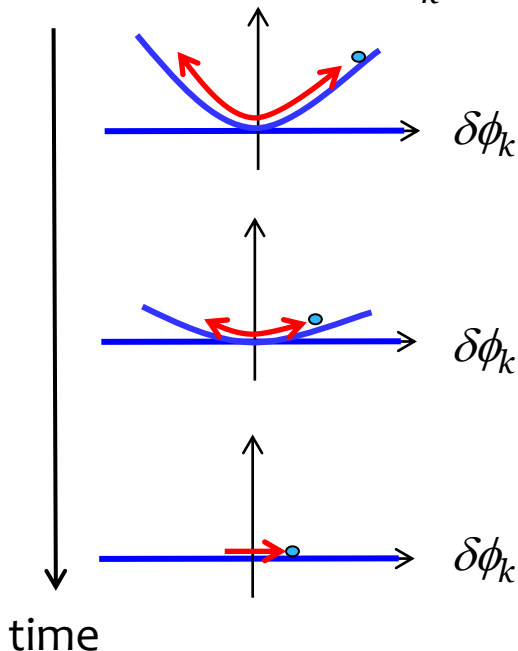
Quantum fluctuations during inflation

Mukhanov & Chibisov '81, ...

Zero-point (vacuum) fluctuations of ϕ :

$$\delta\phi = \sum_k \delta\phi_k(t) e^{ik \cdot x}$$

$$\delta\ddot{\phi}_k + 3H\delta\dot{\phi}_k + \omega^2(t)\delta\phi_k = 0 ; \quad \omega^2(t) = \frac{k^2}{a^2(t)}$$



harmonic oscillator with

friction term and **time-dependent** ω

$$\delta\phi_k \rightarrow \text{const.}$$

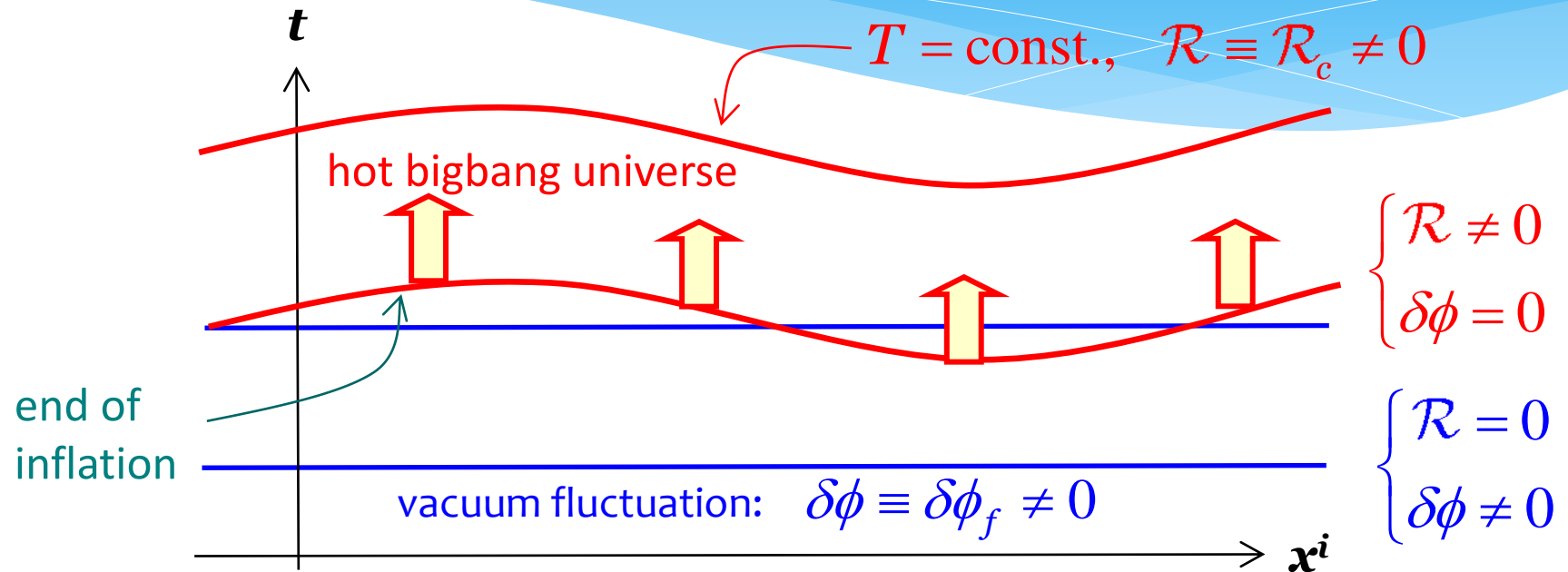
... frozen when $\omega < H$

(on superhorizon scales)

tensor (gravitational wave) modes also satisfy the same eq.

from $\delta\phi$ to curvature perturbation

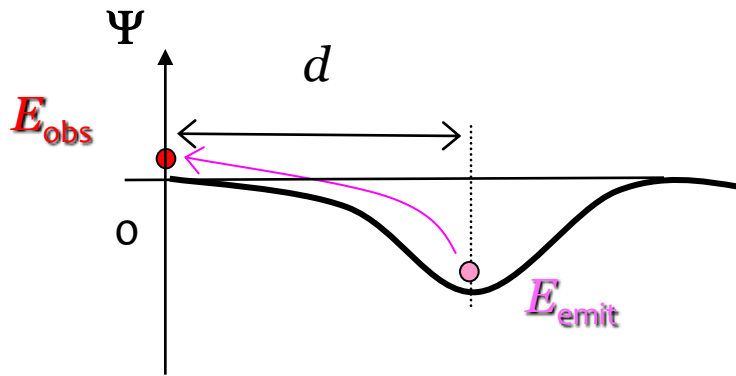
- Inflation ends/damped osc starts on “comoving” ($\phi = \text{const.}$) 3-surface.



- On $\phi = \text{const.}$ surface, curvature perturbation appears $\mathcal{R} \equiv \mathcal{R}_c = -\frac{H}{\dot{\phi}} \delta\phi_f$
- \mathcal{R}_c gives rise to gravitational potential perturbation Ψ : $\Psi = -\frac{3}{5} \mathcal{R}_c$

CMB temperature fluctuations

- Photons climbing up from gravitational potential well are redshifted.



For Planck distribution,

$$\frac{\Delta T}{T}(\vec{n}) \equiv \frac{T_{\text{obs}}}{T_{\text{emit}}} - 1 = \Psi(\vec{x}_{\text{emit}})$$

$$\vec{x}_{\text{emit}} = \vec{n}d ; \vec{n} = \text{line of sight}$$

$c=1$ units

- In an expanding universe, this is modified to be

$$\frac{\Delta T}{T}(\vec{n}) = \frac{1}{3} \Psi(\vec{x}_{\text{emit}})$$

Sachs-Wolfe effect

- There is also the standard Doppler effect:

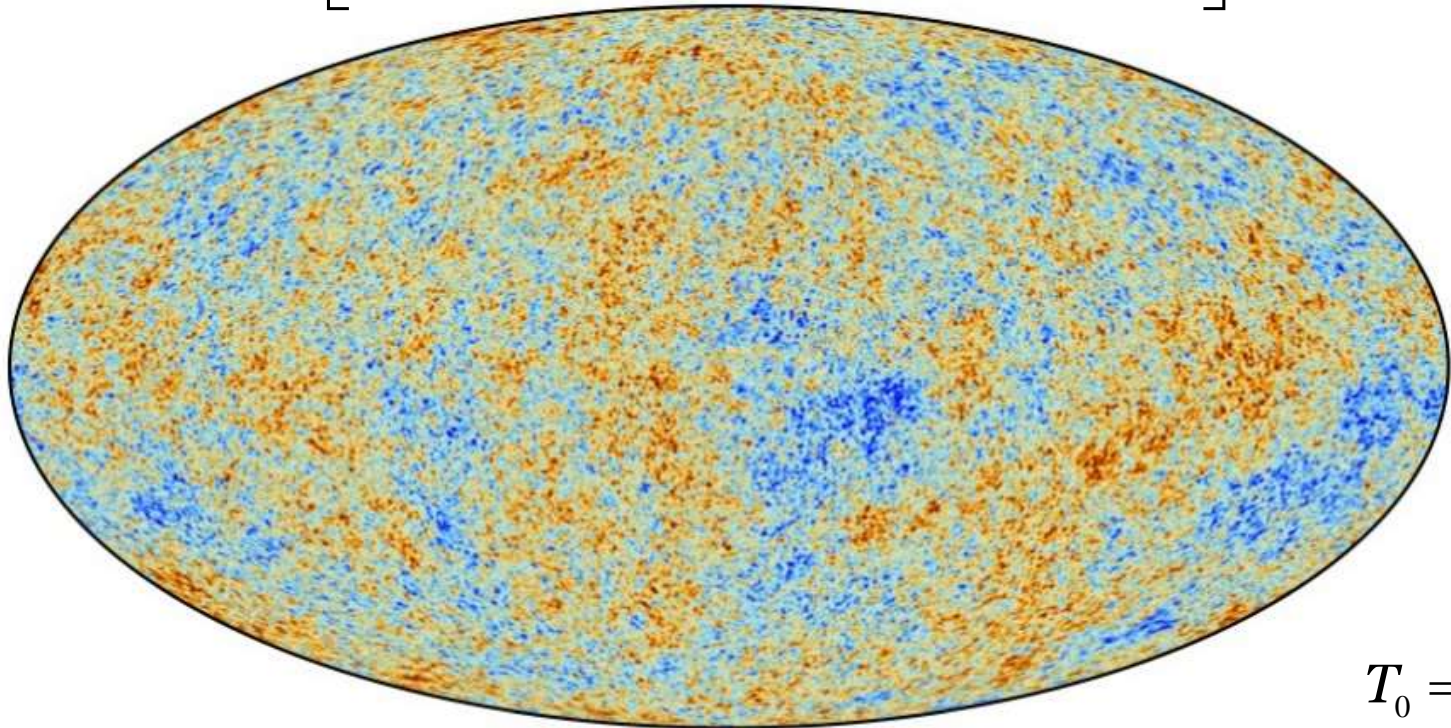
$$\frac{\Delta T}{T}(\vec{n}) = -\vec{n} \cdot \vec{v}(\vec{x}_{\text{emit}})$$

Planck CMB map

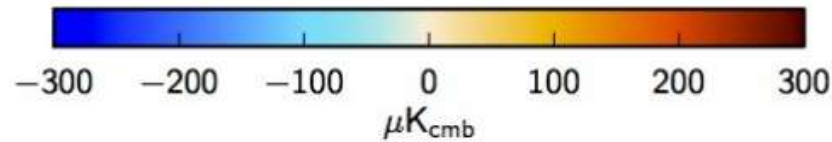
Planck 2013

$$\Delta T = \left[\frac{1}{3} \Psi - \vec{n} \cdot \vec{v} + \dots \text{(small corrections)} \right] T_0$$

but important!



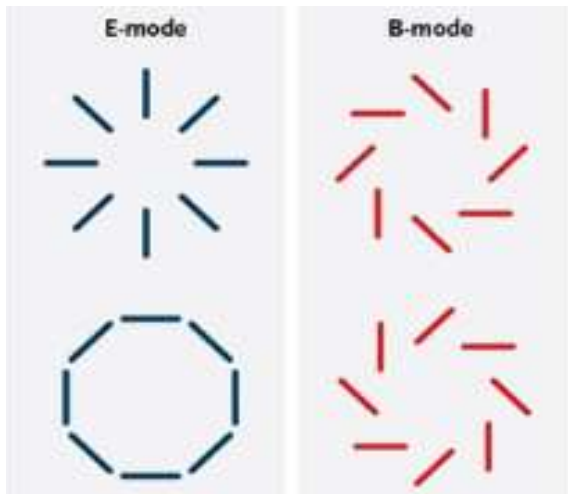
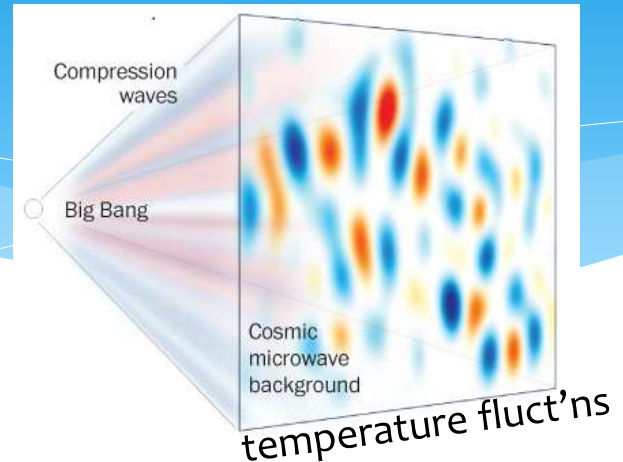
$$T_0 = 2.73K$$



Gravitational Waves from Inflation

Cosmological GWs

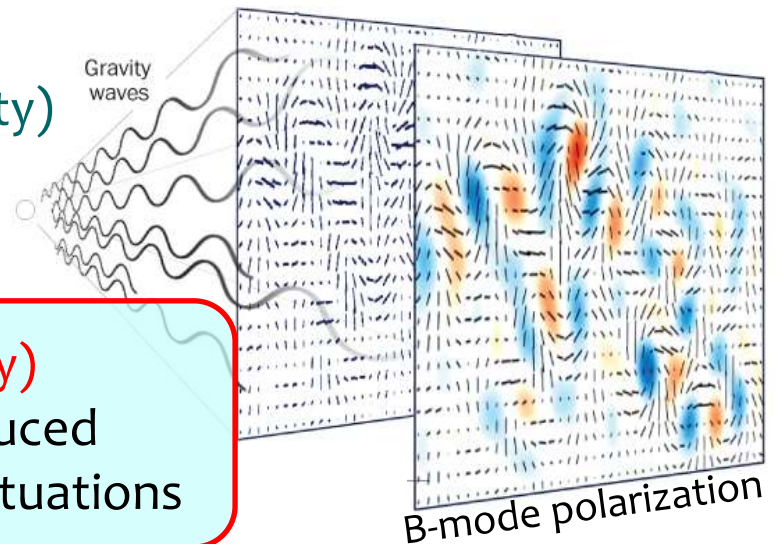
- scalar field(s) produce density fluctuations
-> CMB temp+E-mode fluctuations
- tensor (GW) fluctuations
-> CMB temp+E-mode+B-mode fluct'ns



E-mode (even parity)



B-mode (odd parity)
= cannot be produced
from density fluctuations



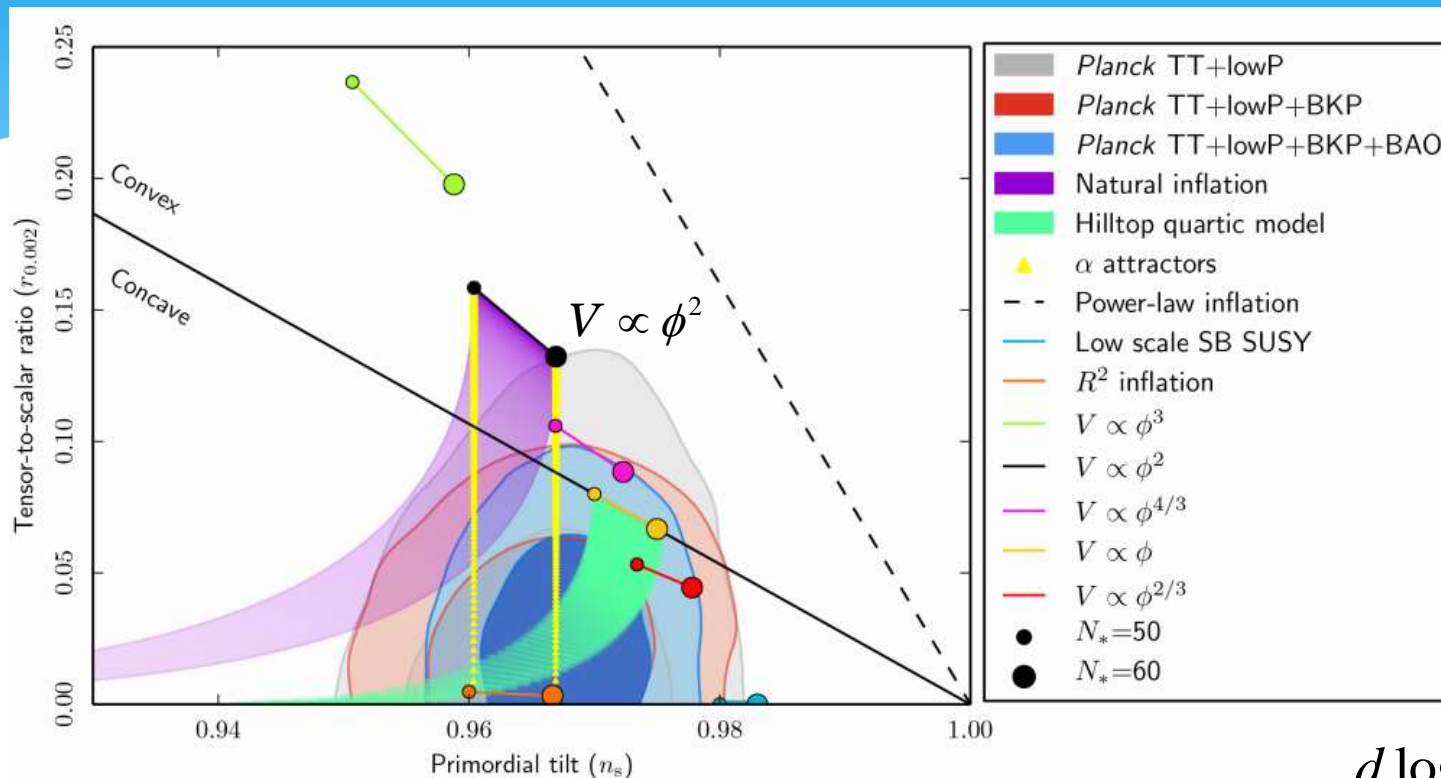
<http://www.skyandtelescope.com/>

Source: Harvard-Smithsonian Center for Astrophysics

CMB B-mode=cosmological GW detector

Planck constraints on inflation

Planck 2015 XX



- scalar spectral index: $n_s \sim 0.96$
- tensor-to-scalar ratio: $r < 0.1$
- simplest $V \propto \phi^2$ model is almost excluded

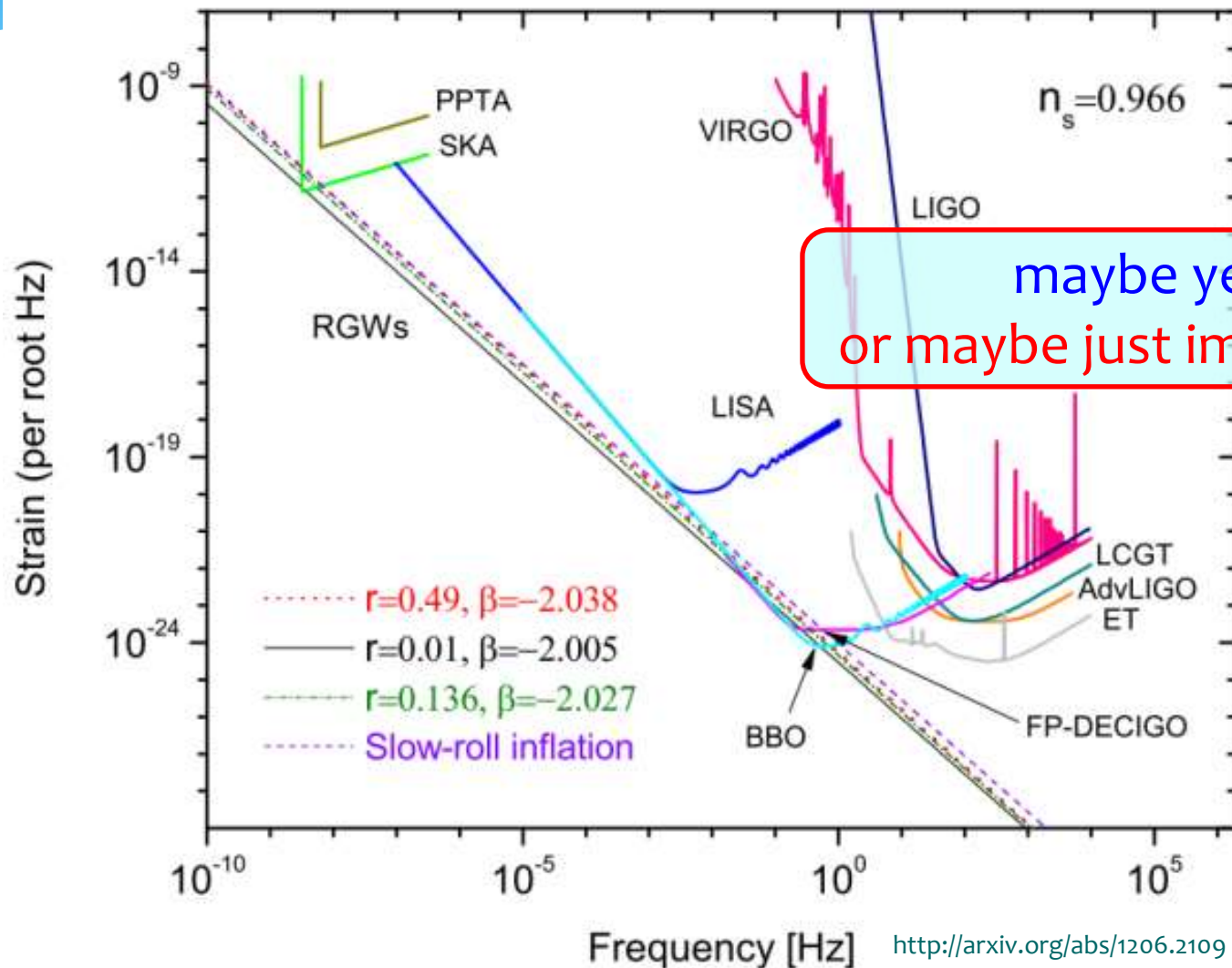
$$n_s - 1 \equiv \frac{d \log[k^3 P_s(k)]}{d \log k}$$

$$r \equiv \frac{P_T(k)}{P_S(k)}$$

some element of non-canonicity needed

GWs from “Standard” Inflation

could direct detection by GW observatories possible?



maybe yes...
or maybe just impossible...

blue-tilted GW spectrum?

possible e.g. in massive gravity inflation model Lin & MS (2015)

tensor (=GW)
spectral index:

$$n_T \approx \frac{2m_g^2}{3H^2}$$

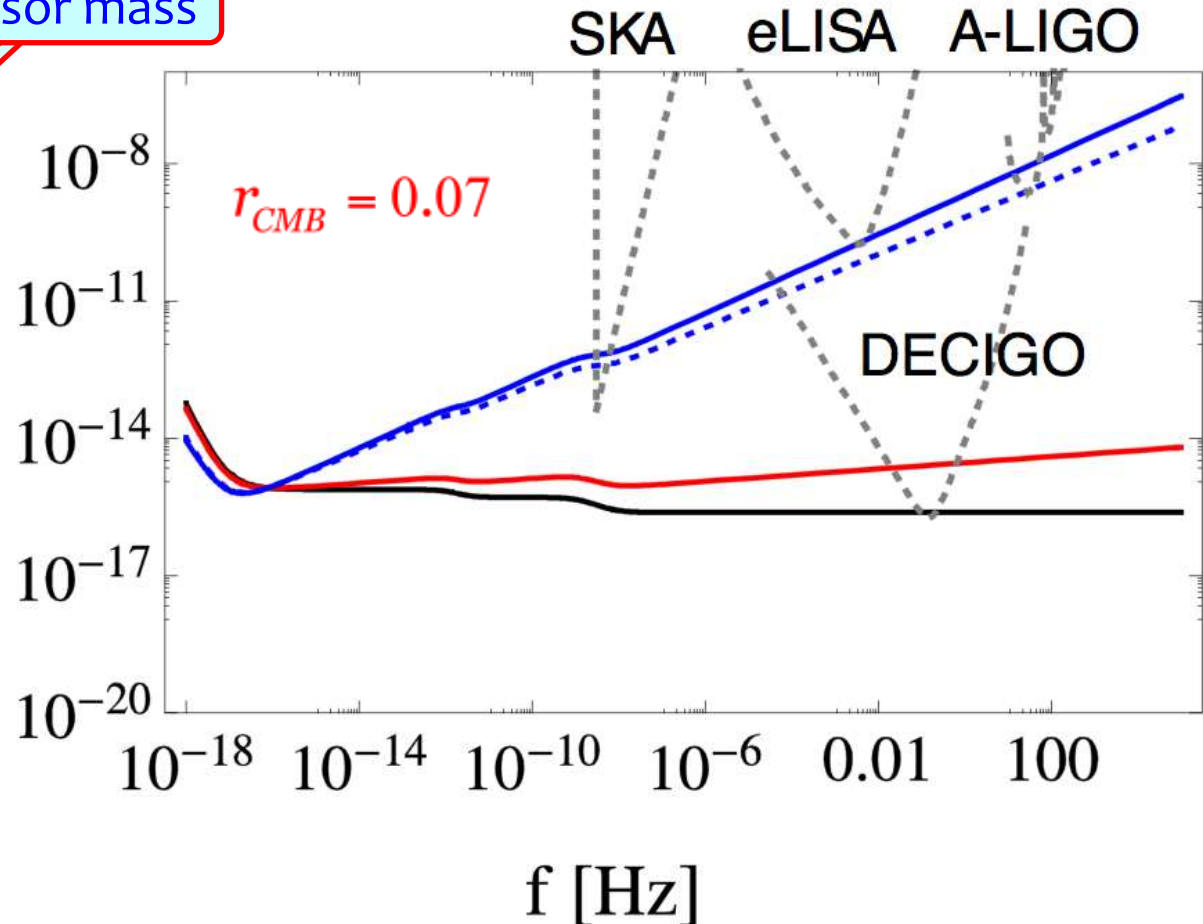
tensor mass

Ω_{GW}

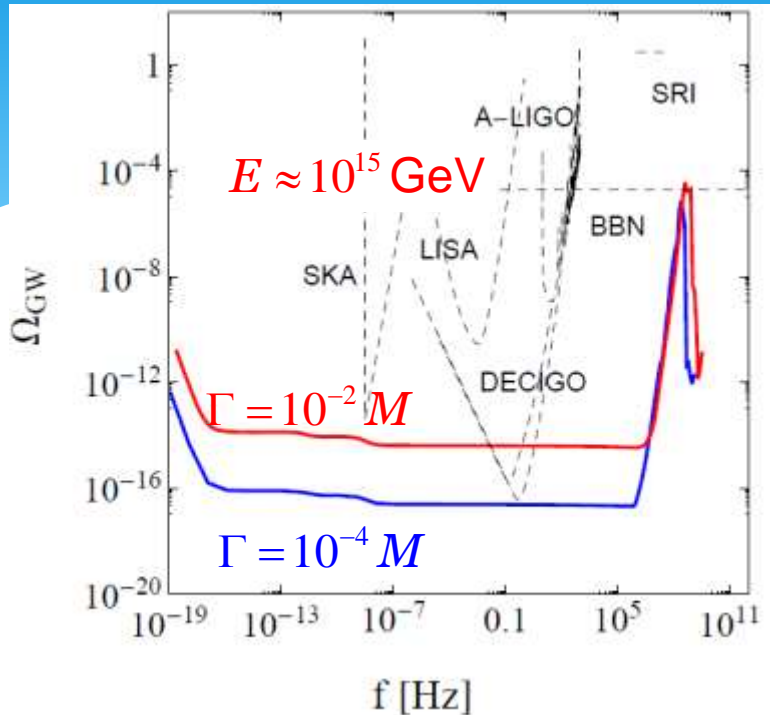
- : $m_g^2 / H^2 = 0.6$

- : $m_g^2 / H^2 = 0.1$

- : $n_T = 0$



quantitative examples



$E \approx 10^{15} \text{ GeV}$

$\Gamma = 10^{-2} M$

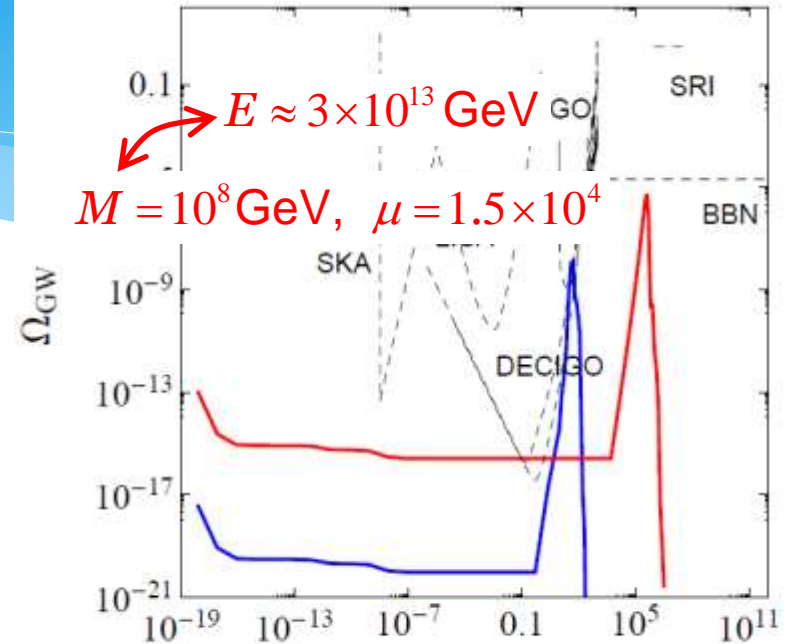
$\Gamma = 10^{-4} M$

Starobinsky model $\left(\varepsilon_{\text{inf}} = -\frac{H}{H^2} \simeq 2.5 \times 10^{-4} \right)$

$$V = \frac{3}{4} M^2 M_{pl}^2 \left[1 - \exp\left(-\frac{\sqrt{6}\phi}{3M_{pl}}\right) \right]^2$$

with $m_g^2 = \lambda \phi^2 \exp[-2(\phi / M_{pl})^2]$
 $\lambda = 4.8 \times 10^{-7}$

Kuroyanagi, Lin, MS & Tsujikawa '17



$E \approx 3 \times 10^{13} \text{ GeV}$

$M = 10^8 \text{ GeV}, \mu = 1.5 \times 10^4$

$M = 1 \text{ GeV}, \mu = 4.8 \times 10^4 \rightarrow E \approx 3 \times 10^9 \text{ GeV}$

low-scale model $(\varepsilon_{\text{inf}} \ll 10^{-4})$

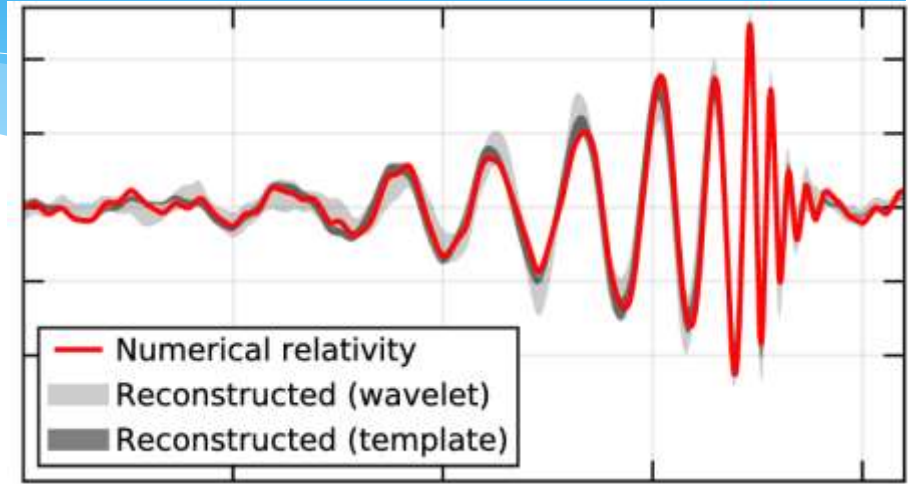
$$V = \frac{1}{2} M^2 \phi^2, \quad H_{\text{end}} = \frac{2}{3} M, \quad \Gamma = 10^{-3} M$$

with $m_g^2 = \mu \frac{\dot{\phi}^2}{M_{pl}^2}$

Big-Bang Nucleosynthesis (BBN) gives stringent constraints

Gravitational Wave Physics/Astronomy

The Dawn has arrived!



LIGO

- GWs from binary BH merger were detected for the first time on Sep14, 2015 (GW150914).

2017 Nobel Prize!

BBH masses: $36 M_{\odot} + 29 M_{\odot}$

Source redshift: 0.09 (~ 1.2 Glyr)

Event rate: 0.6-12 /Gpc³ /yr

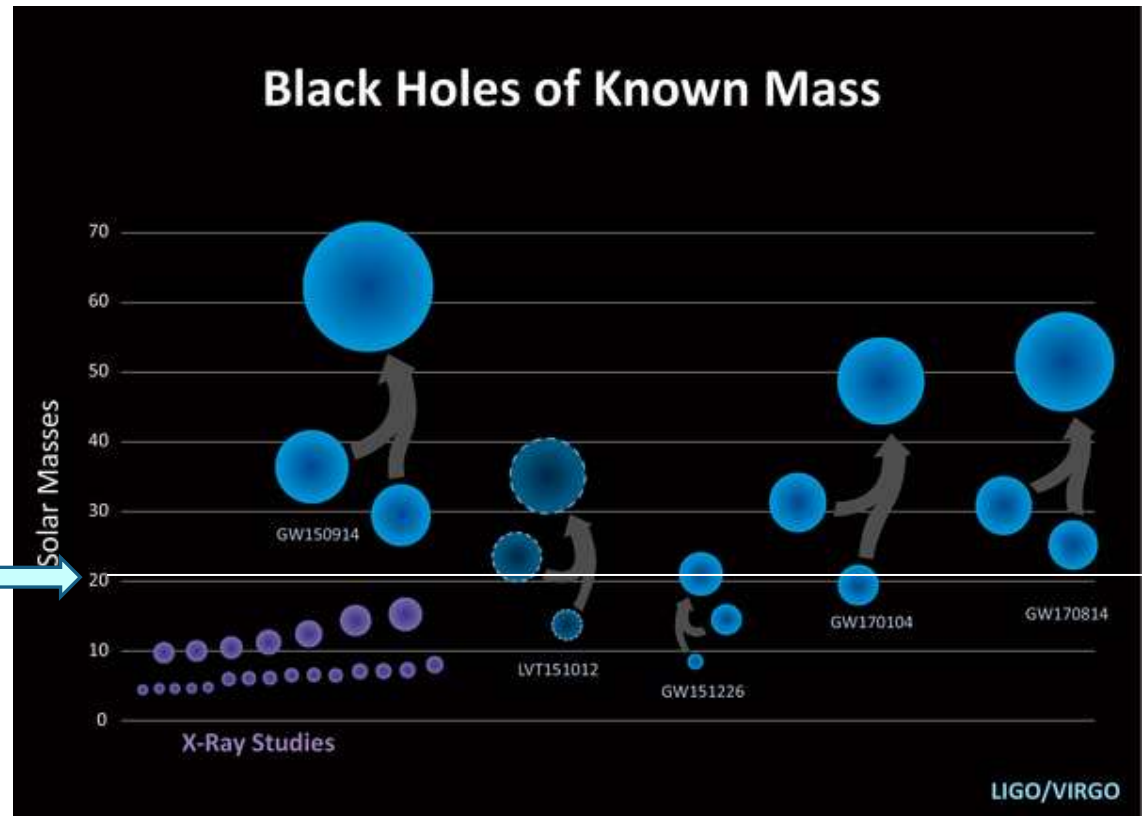
Unusual properties of LIGO BHs

LIGO has detected 4BBH mergers (+1 candidate) so far.

Any implications ?

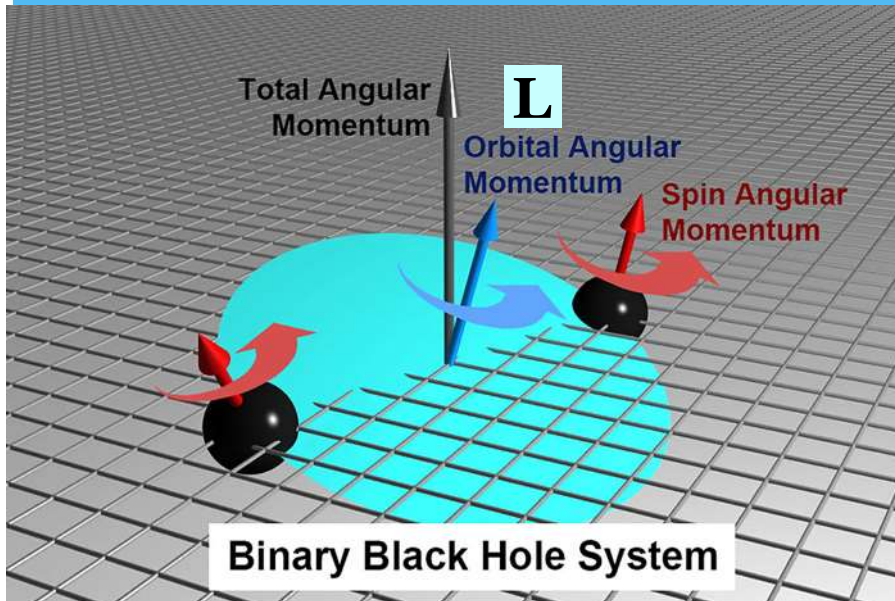
- They seem to be **unusually heavy!**
(exc. GW151226)
- Their **spins** seem to be **unusually small!**

$20 M_{\odot}$ →



LIGO BH spins

$$\chi_{\text{eff}} = (m_1 \mathbf{s}_1 + m_2 \mathbf{s}_2) \cdot \mathbf{n}_L / (m_1 + m_2): \quad \mathbf{n}_L = \mathbf{L} / L$$

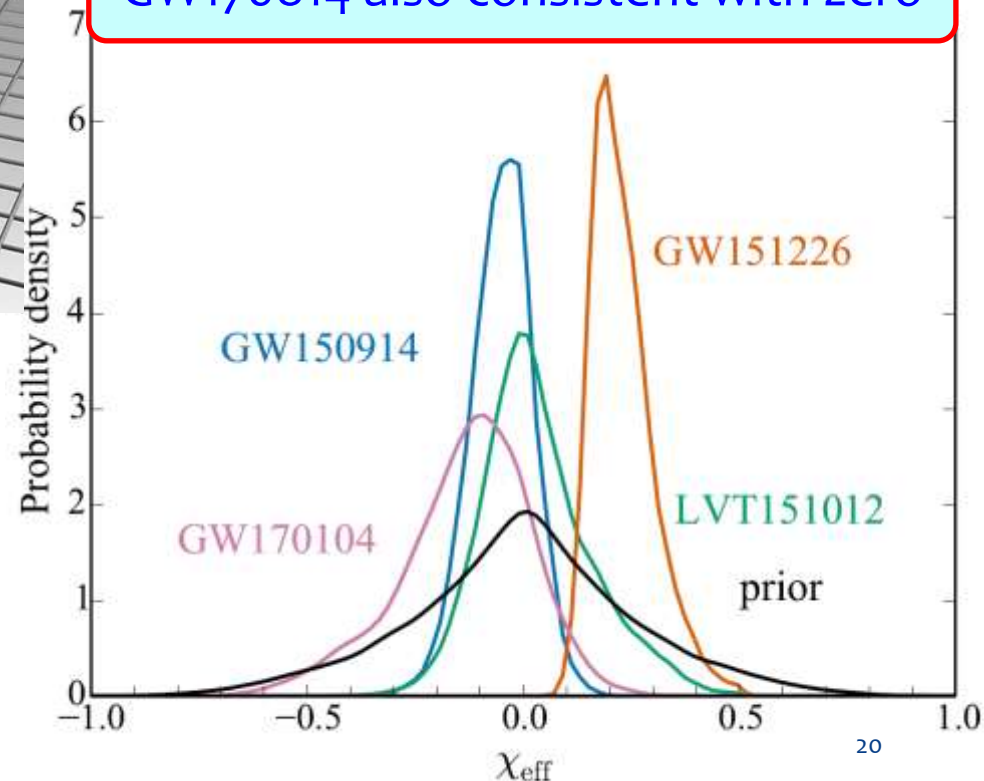


<http://www.ctc.cam.ac.uk/>

χ_{eff} would be larger if astrophysical origin

$\chi_{\text{eff}} = 0$ is consistent (exc. GW151226)

GW170814 also consistent with zero

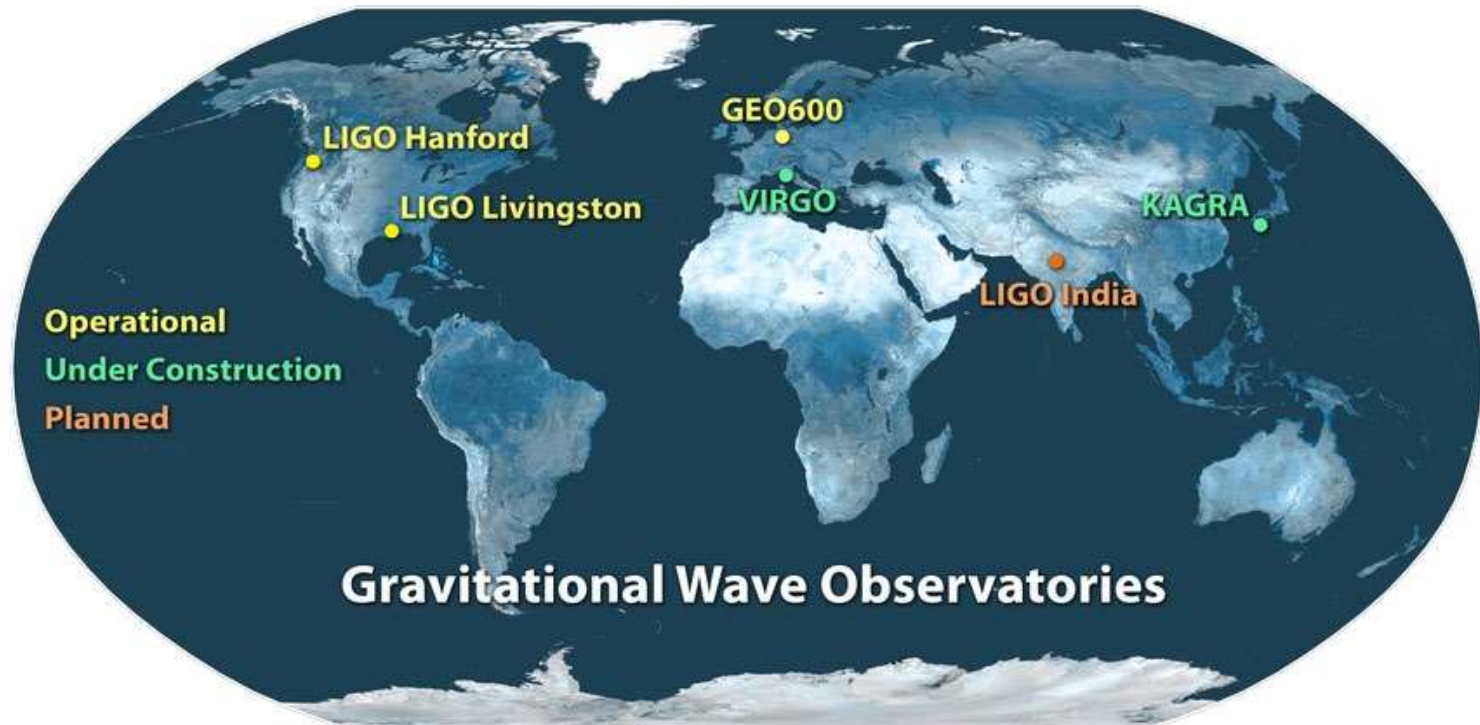


Future Network of GW Observatories

VIRGO started to operate on 1st Aug. 2017

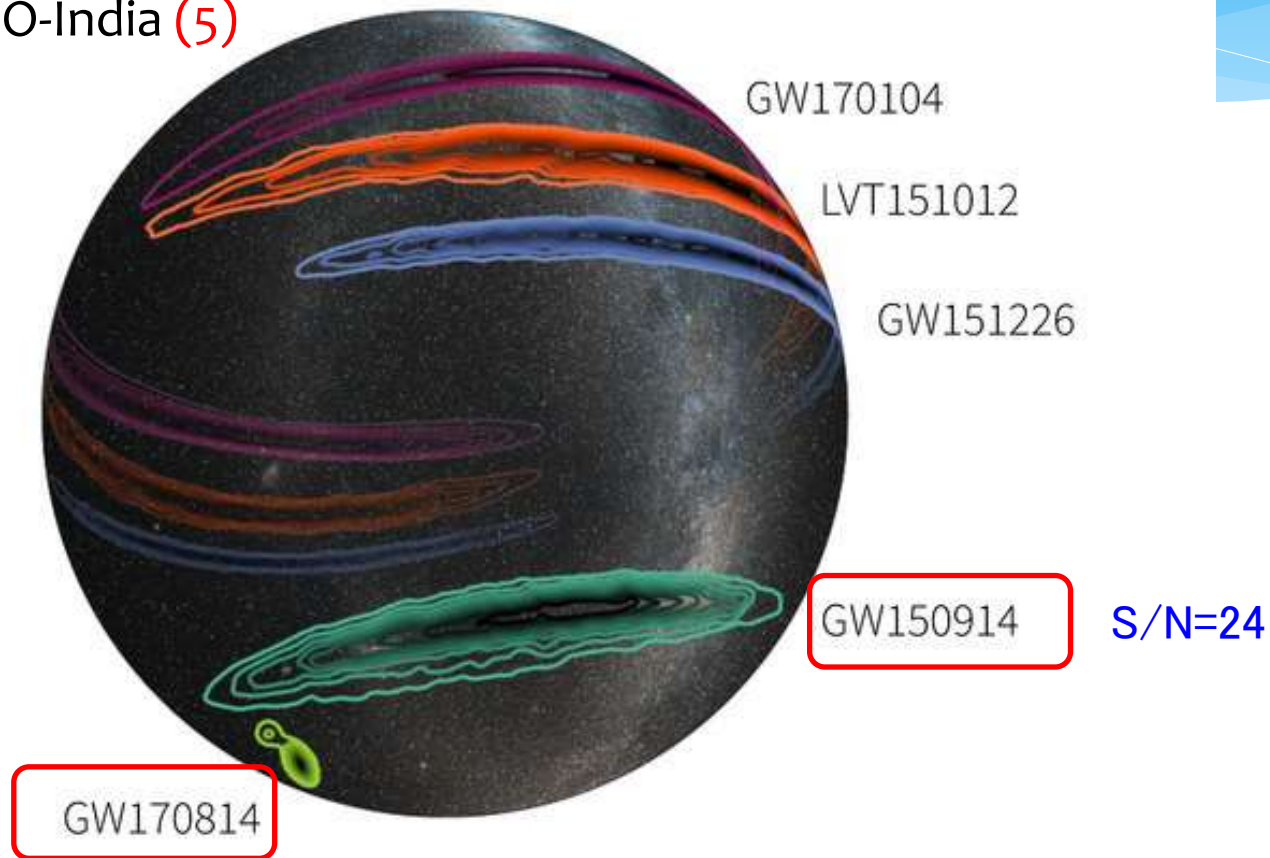
KAGRA will start operation by 2020-2021 (iKAGRA has started!)

LIGO-India has been recently approved by Indian gov.



Huge advantage in angular resolution

- Impressive increase from LIGO alone (2) to LIGO+VIRGO (3)
- +KAGRA (4)
- +LIGO-India (5)



S/N=15 (LIGO), 4.4 (Virgo) \Rightarrow S/N=18.3 (LIGO+Virgo)

KAGRA

KAmioka GRAvitational wave detector

In Japanese it is pronounced as Kagura, which means “God Music” (神楽)

Previously called LCGT

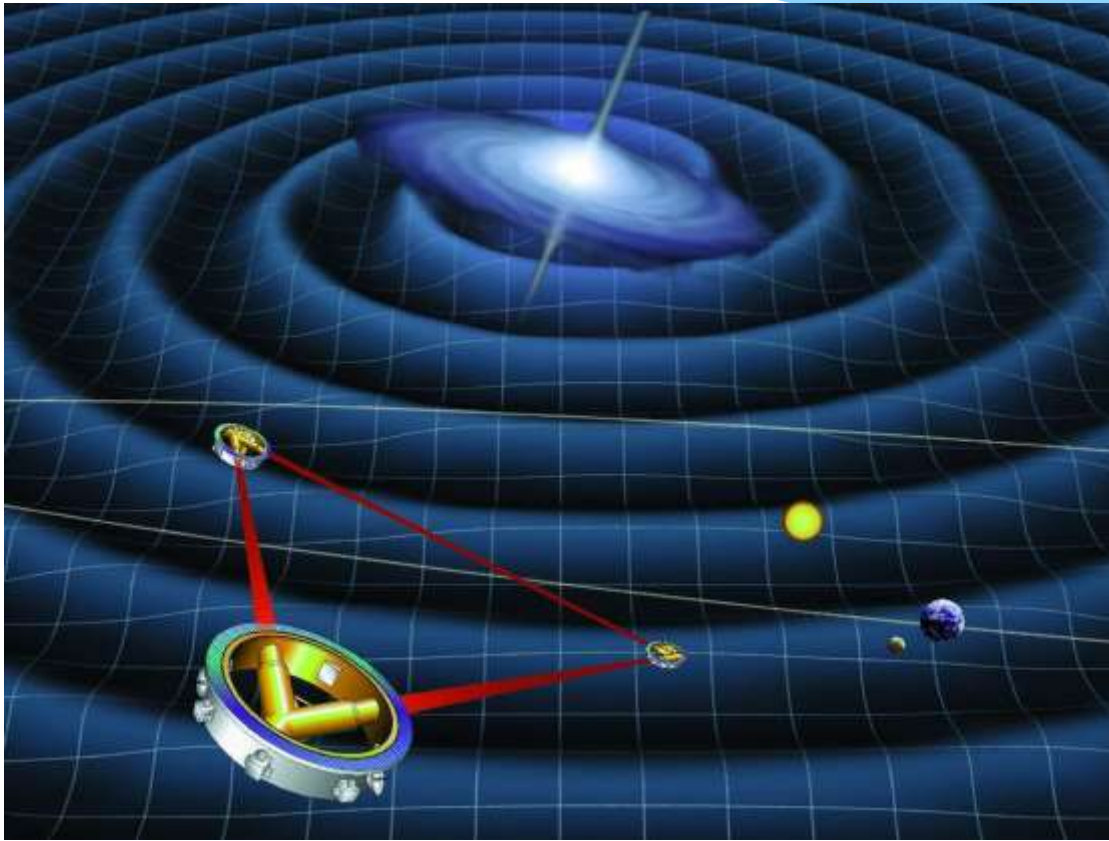
Large Cryogenic
Gravitational wave Telescope

Arm length 3km
Cooled to 20K



<http://gwcenter.icrr.u-tokyo.ac.jp/en/>

Space-based Future Projects



<http://lisa.nasa.gov/>

Arm Length



DECIGO: 1,000 km

launched by ~2030?
target freq: ~ 0.1 Hz

Deci-hertz Interferometer
Gravitational wave Observatory

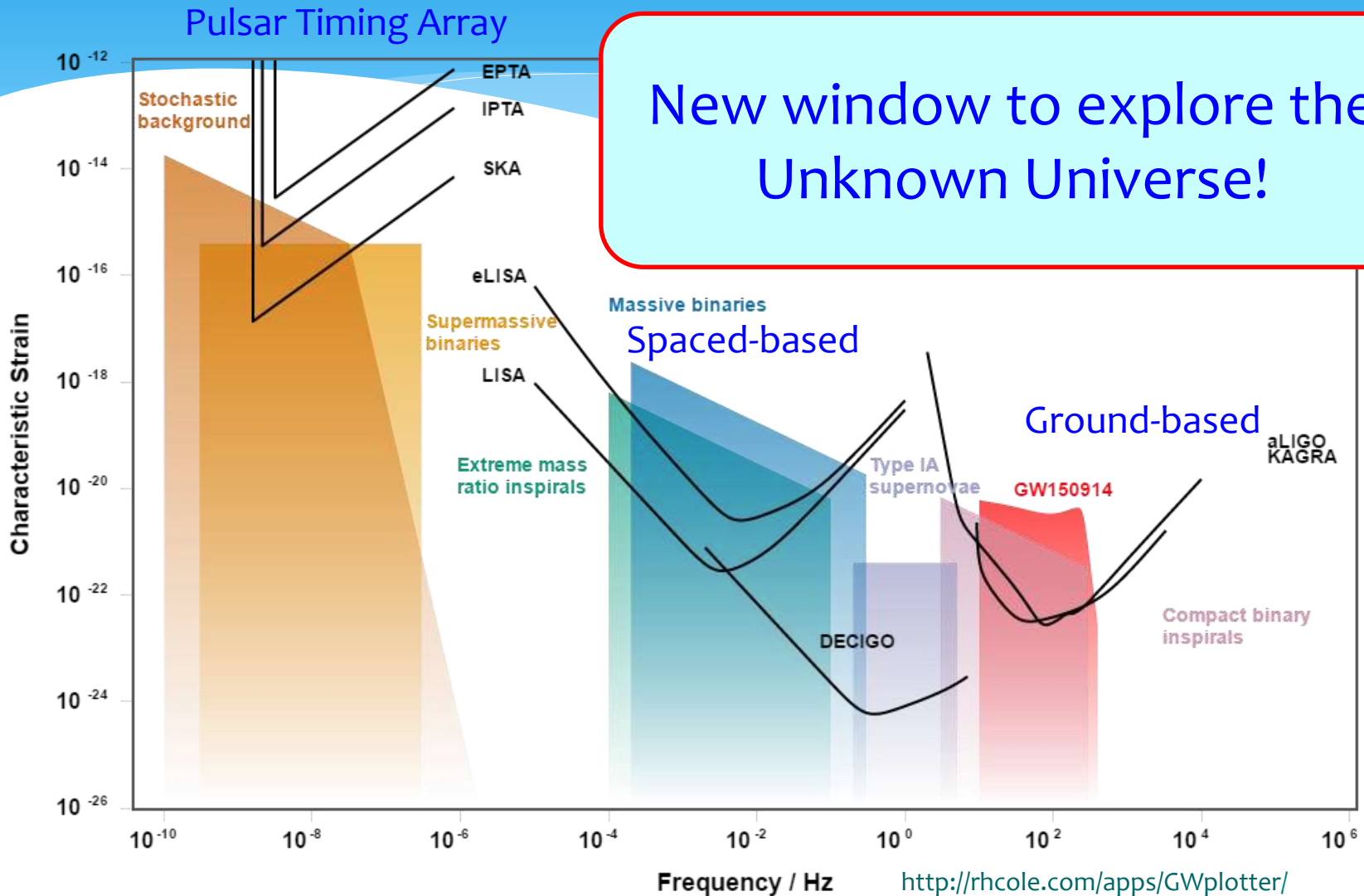
LISA: 5,000,000 km

launched by ~2034?
target freq: $\sim 10^{-3}$ Hz

Laser Interferometer Space Antenna

Multi-frequency GW Astronomy

New window to explore the Unknown Universe!



<http://rhcole.com/apps/GWplotter/>

Binary Neutron Star merger found!

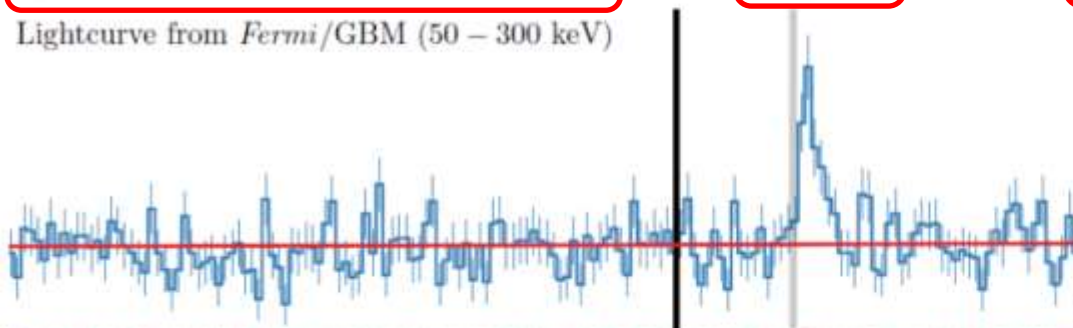


GW170817 / GRB170817A

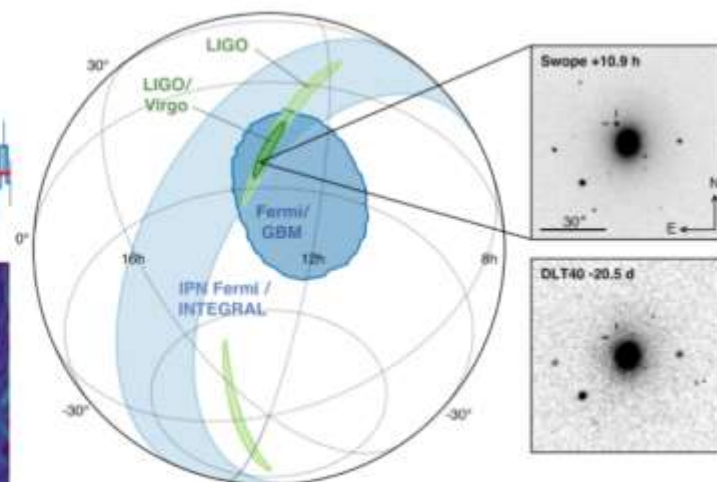
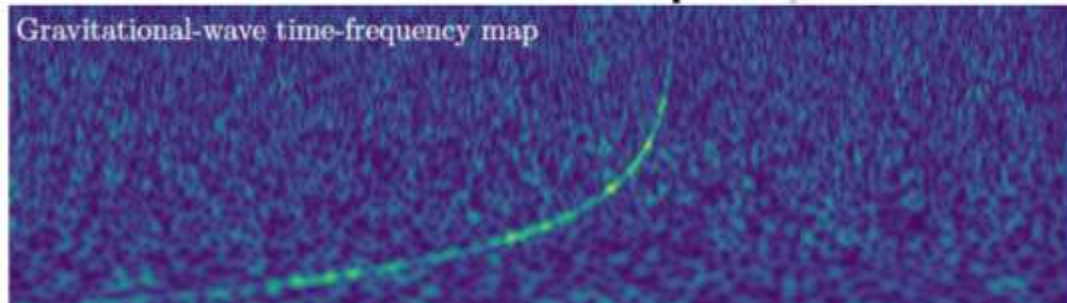
Detections News About LIGO science Educational resources Multimedia For researchers LIGO Lab site

LIGO, Virgo, and partners make first detection of gravitational waves and light from colliding neutron stars

Lightcurve from *Fermi*/GBM (50 – 300 keV)



Gravitational-wave time-frequency map



multi-messenger astronomy!

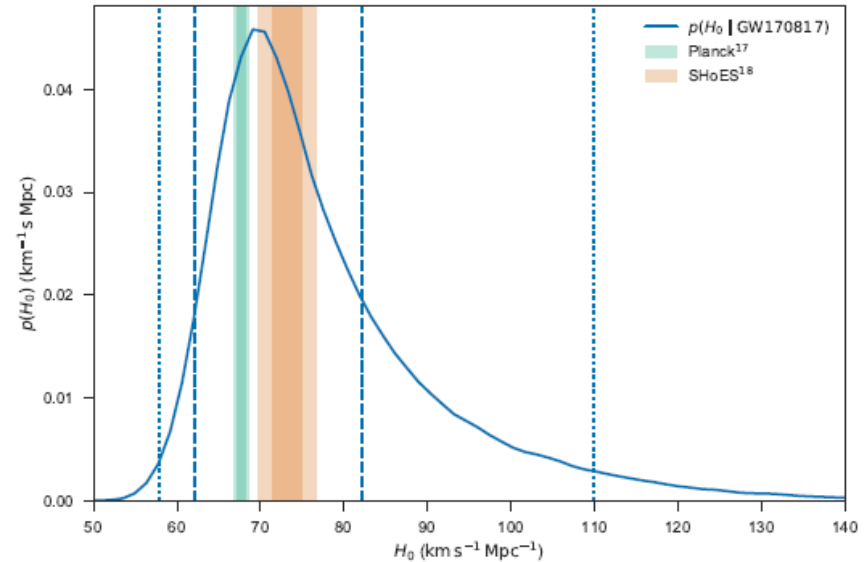
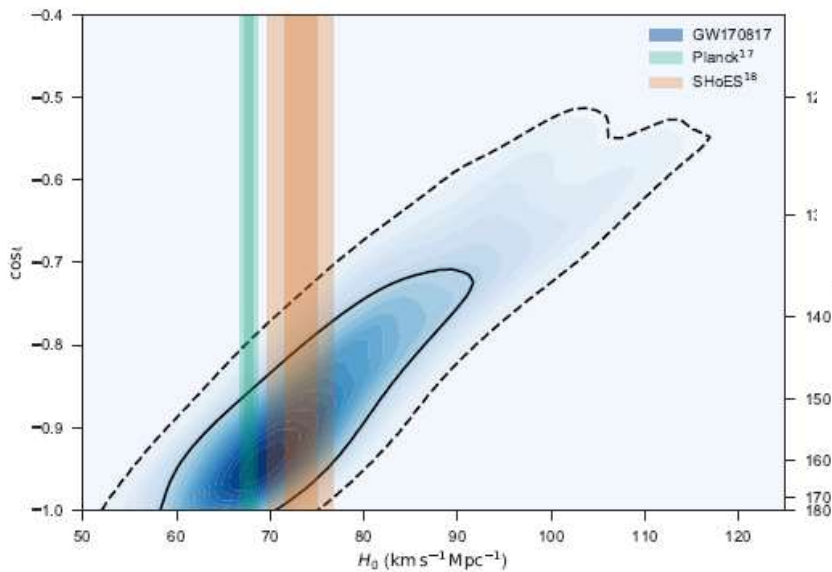
70 observatories include. 7 satellites



Cosmological Implication!

A GRAVITATIONAL-WAVE STANDARD SIREN MEASUREMENT OF THE HUBBLE CONSTANT

THE LIGO SCIENTIFIC COLLABORATION AND THE VIRGO COLLABORATION, THE IM2H COLLABORATION, THE DARK ENERGY CAMERA GW-EM COLLABORATION AND THE DES COLLABORATION, THE DLT40 COLLABORATION, THE LAS CUMBRES OBSERVATORY COLLABORATION, THE VINROUGE COLLABORATION, THE MASTER COLLABORATION, et al.



$$H_0 = 70.0^{+12.0}_{-8.0} \text{ km s}^{-1} \text{ Mpc}^{-1}.$$

from just a single event!

Primordial Black Holes

What are Primordial BHs?

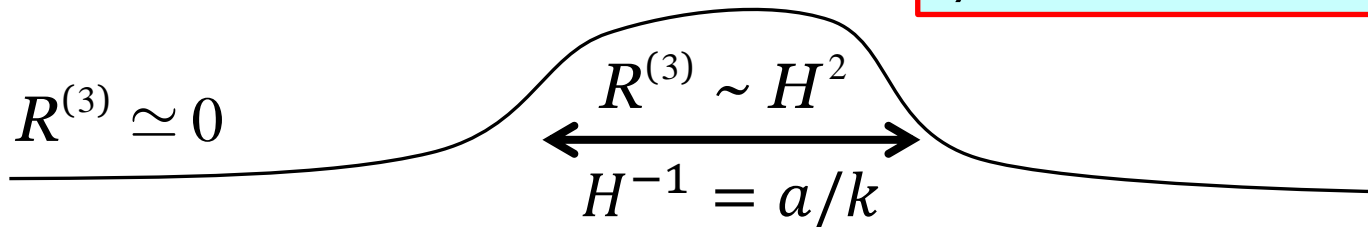
- PBH = BH formed before recombination epoch (ie at $z \gg 1000$)
conventionally during radiation-dominated era
- Hubble size region with $\delta\rho/\rho = O(1)$ collapses to form BH
Carr (1975), ...
- Such a large perturbation may be produced by inflation
Carr & Lidsey (1991), ...
- PBHs may dominate Dark Matter.
Ivanov, Naselsky & Novikov (1994), ...
- Origin of supermassive BHs ($M \gtrsim 10^6 M_\odot$) may be primordial.

Curvature perturbation to PBH

- gradient expansion/separate universe approach

$$6H^2(t, \mathbf{x}) + R^{(3)}(t, \mathbf{x}) = 16\pi G \rho(t, \mathbf{x}) + \dots \quad \text{Hamiltonian constraint (Friedmann eq.)}$$

$$\Rightarrow \boxed{R^{(3)} \approx -\frac{4}{a^2} \nabla^2 \mathcal{R}_c \approx \frac{8\pi G}{3} \delta\rho_c} \quad \Rightarrow \quad \boxed{\frac{\delta\rho_c}{\rho} \sim \mathcal{R}_c \text{ at } \frac{k^2}{a^2} = H^2}$$



- If $R^{(3)} \sim H^2$ ($\Leftrightarrow \delta\rho_c / \rho \sim 1$), it collapses to form BH

Young, Byrnes & MS '14

$$M_{\text{PBH}} \sim \rho H^{-3} \sim 10^5 M_{\odot} \left(\frac{t}{1\text{s}} \right) \sim 20 M_{\odot} \left(\frac{k}{1\text{pc}^{-1}} \right)^{-2}$$

- Spins of PBHs are expected to be **very small**

examples

hybrid-type inflation

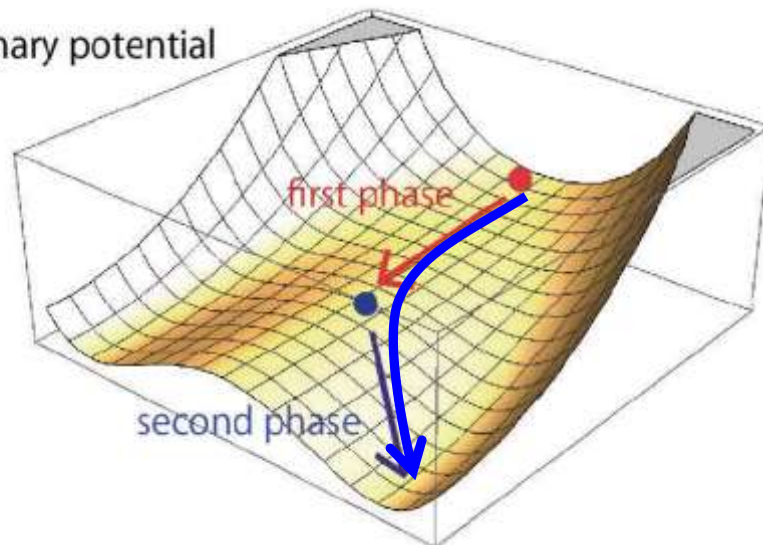
Garcia-Bellido, Linde & Wands '96, ...

\mathcal{R}_C grows near the saddle point
non-Gauss may become large

Abolhasani, Firouzjahi & MS '11,..

Pattison et al. 1707.00537

inflationary potential

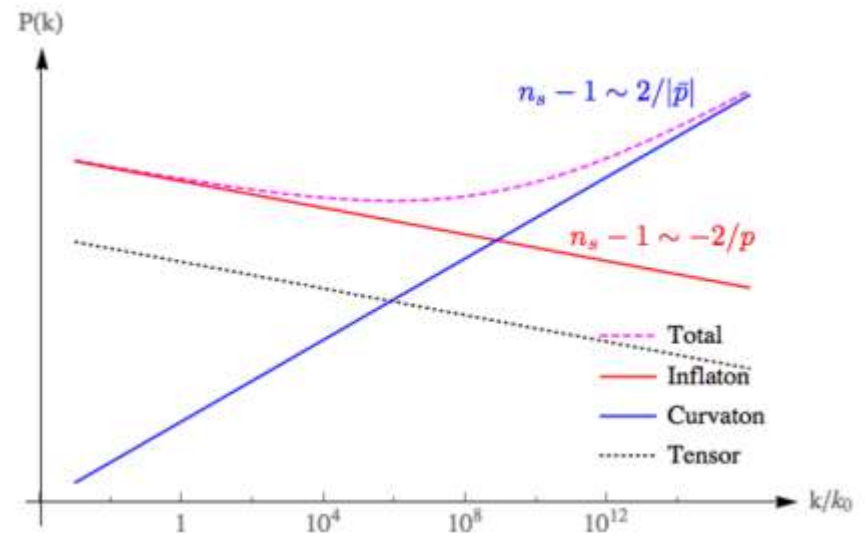


non-minimal curvature

Domenech & MS '16

$$L = -\frac{1}{2} f(\phi) g^{\mu\nu} \partial_\mu \chi \partial_\nu \chi$$

$$-\frac{1}{2} h(\phi) m^2 \chi^2$$




Accretion to PBH?

➤ Bondi accretion

$$\dot{M} = \lambda \cdot 4\pi r_B^2 \rho c_s : \quad c_s = \sqrt{P / \rho} (= 1 / \sqrt{3}), \quad r_B = \frac{GM}{c_s^2}, \quad \lambda \lesssim O(1)$$

- accretion rate/Hubble time

$$\Rightarrow \frac{\dot{M}}{HM} = \lambda \frac{3}{4} \frac{H}{H_M} : \quad M = \frac{4\pi\rho_M}{3} (c_s H_M^{-1})^3 = \frac{c_s^3}{2GH_M}, \quad \frac{H}{H_M} = \left(\frac{a_M}{a} \right)^2$$

 horizon size at the time of PBH formation

$$\Rightarrow \int_{a_M}^{\infty} \frac{\dot{M}}{H} \frac{da}{a} \simeq \lambda \frac{3}{8} M \quad \text{PBH mass can increase by a factor of 1.5 at most}$$

Mass increase can be ignored, given other ambiguities

Effect on CMB?

accretion can lead to radiative emission

- Eddington luminosity: max luminosity from accretion

$$L_{\text{edd}} = \frac{4\pi GMm_p c}{\sigma_T}; \quad m_p = \text{proton mass}$$

$\sigma_T = \text{Thomson cross section}$

$$L = \varepsilon L_{\text{edd}}; \quad \varepsilon \leq 1 \quad \dots \quad \text{luminosity from PBH}$$

- energy output/Hubble time

$$\frac{\dot{\rho}_R}{H\rho_R} = \varepsilon \frac{n_{\text{PBH}} L_{\text{edd}}}{H\rho_R} = \varepsilon \frac{\rho_{\text{PBH}}}{\rho_R} \frac{4\pi Gm_p}{\sigma_T H} = \varepsilon f_{\text{PBH}} \left(\frac{a}{a_{\text{eq}}} \right)^3 \frac{4\pi Gm_p}{\sigma_T H_{\text{eq}}}$$
$$\simeq 10^{-4} \varepsilon f_{\text{PBH}} \left(\frac{a}{a_{\text{eq}}} \right)^3; \quad f_{\text{PBH}} = \frac{\Omega_{\text{PBH}}}{\Omega_{\text{CDM}}}$$

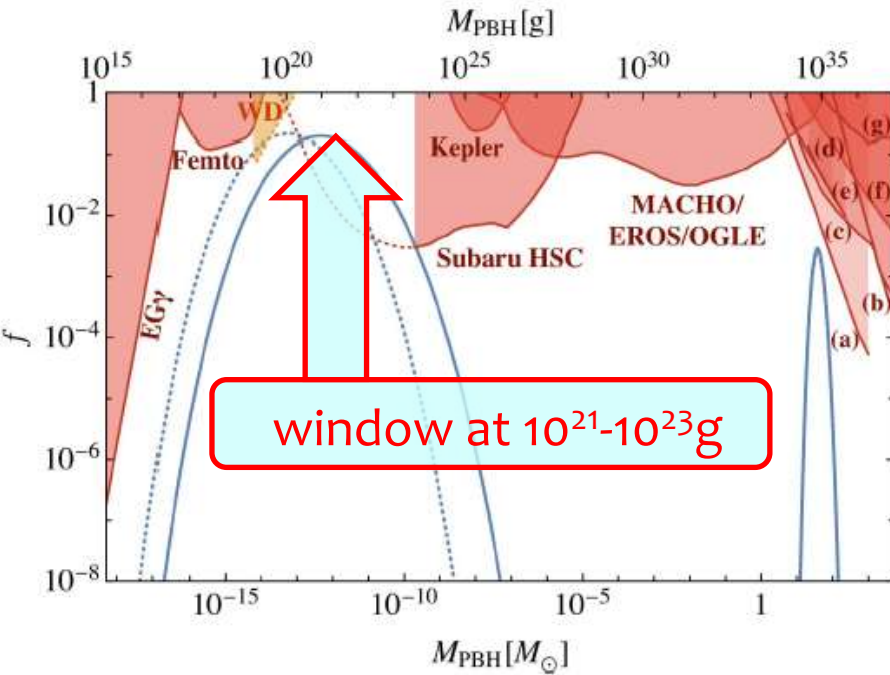
small, but may not be entirely negligible...

Constraints on PBHs

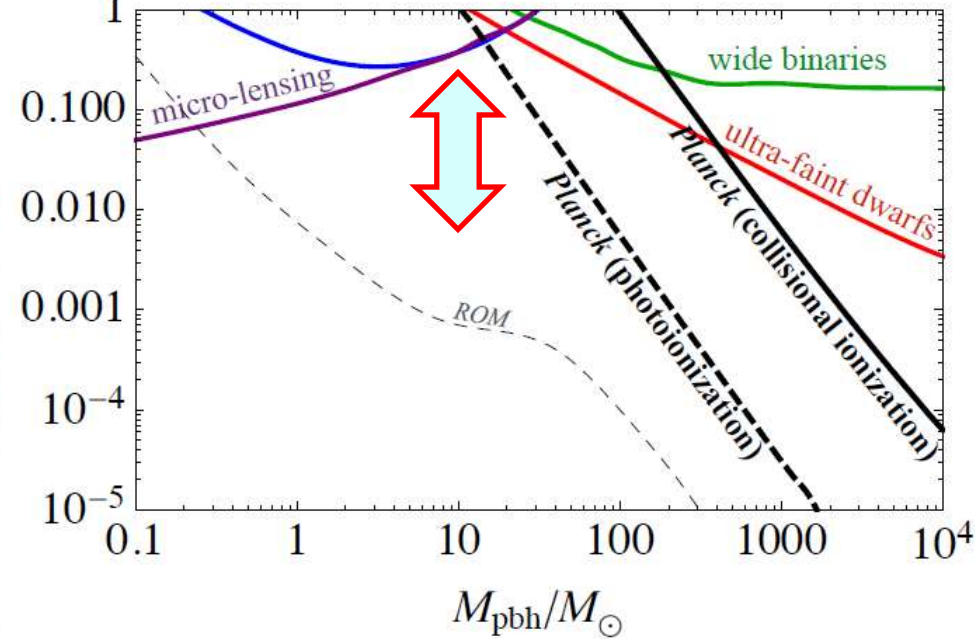
$$f_{\text{PBH}} = \frac{\Omega_{\text{PBH}}}{\Omega_{\text{DM}}}$$

LIGO BBHs may occupy ~10% of DM

Can DM be PBHs?



Inomata et al., 1711.06129



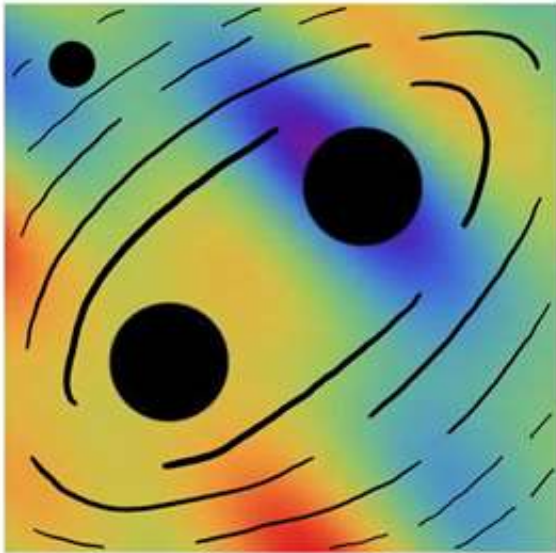
Ali-Haimoud & Kamionkowski, 1612.05644

Ricotti, Ostriker & Mack ('08)
overestimated the accretion effect

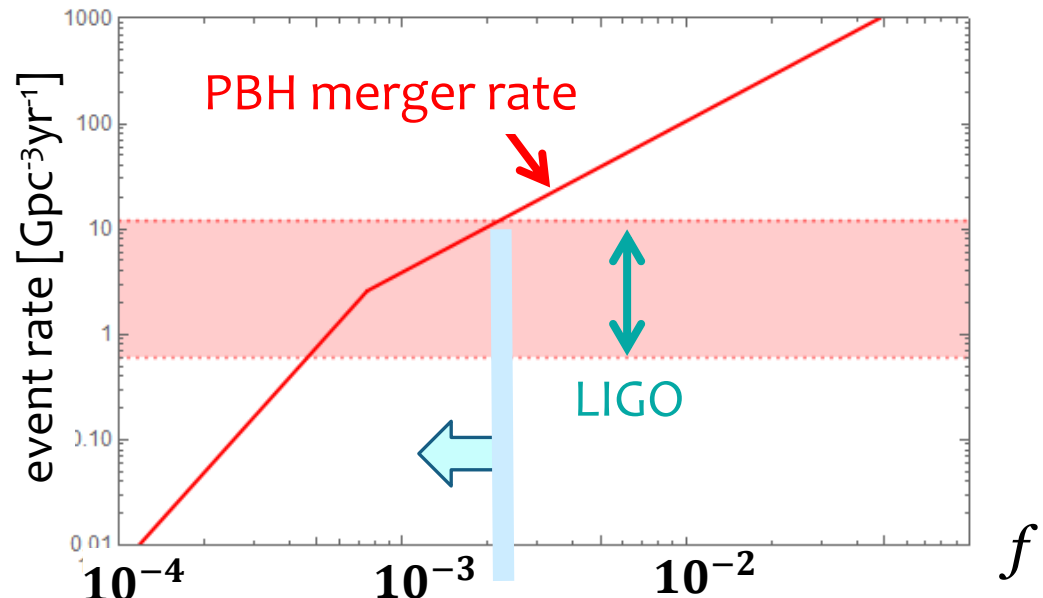
LIGO BHs = PBHs?

MS, Suyama, Tanaka & Yokoyama '16

$$M_{PBH} \simeq 20 \left(\frac{k}{\text{kpc}^{-1}} \right)^{-2} M_{\odot} \simeq 20 \left(\frac{100 \text{MeV}}{T} \right)^2 M_{\odot}$$



3-body interaction
leads to formation of
BH binaries

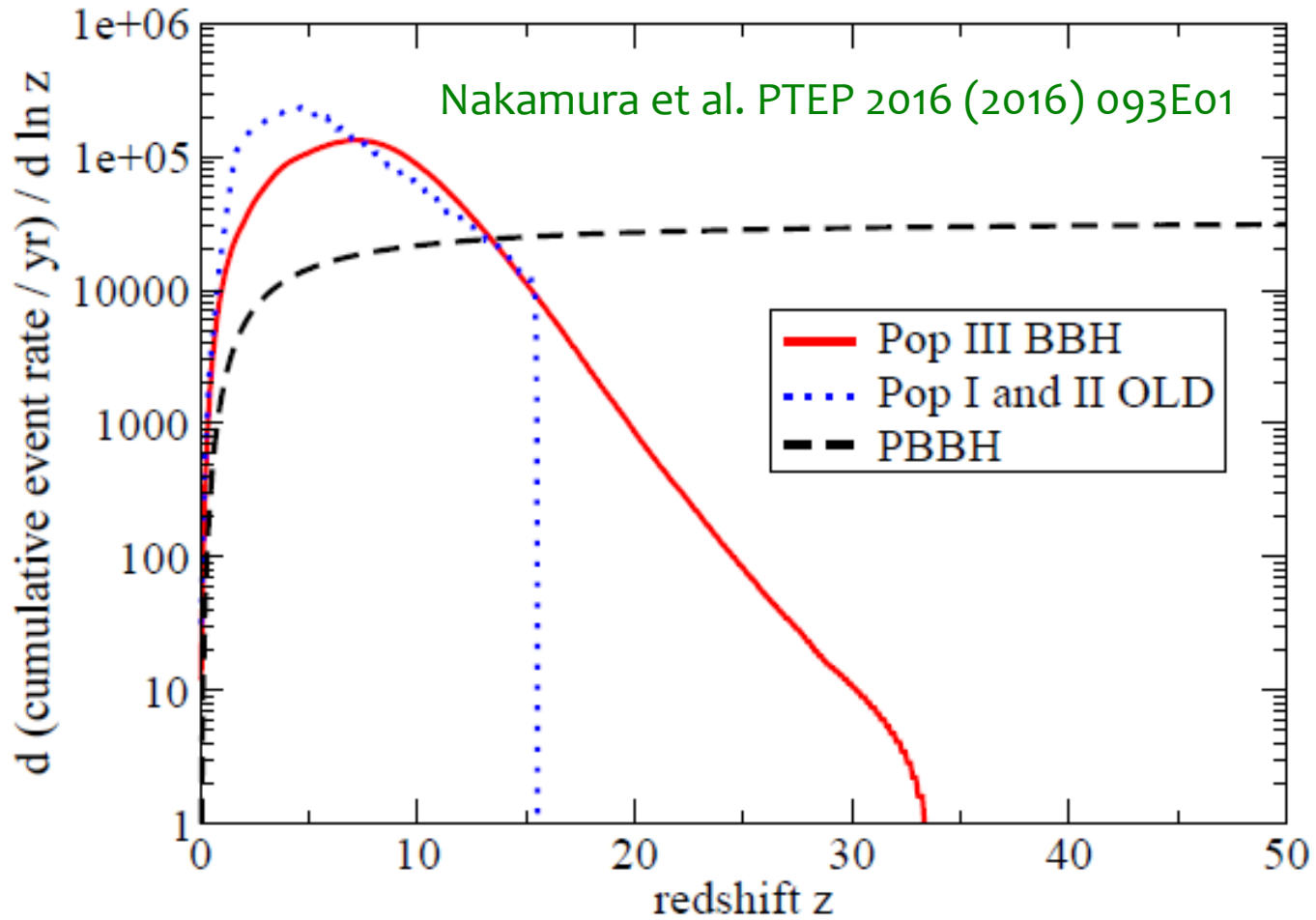


f = fraction of PBH in dark matter

tightest constraint at $M \sim 10M_{\odot}$

(cf. Ali-Haïmoud et al., 1709.06576)

testing PBH hypothesis



testing PBH hypothesis 2

Kocsis, Suyama, Tanaka, Yokoyama, arXiv:1709.09007

BBH Merger Rate at time t :

mass function

$$\mathcal{R}(m_1, m_2, t) = \frac{n_{\text{BH}}}{2} f(m_1) f(m_2) P_{\text{intr}}(m_1, m_2, t)$$

intrinsic probability

$$P_{\text{intr}}(m_1, m_2, t) \propto g(m_1) g(m_2) m_t^\alpha : m_t = m_1 + m_2$$

$$\Leftrightarrow \alpha(m_1, m_2, t) \equiv -m_t^2 \frac{\partial^2}{\partial m_1 \partial m_2} \ln \mathcal{R}(m_1, m_2, t)$$

- PBH binary scenario
- Dynamical formation in dense stellar systems

$$\frac{36}{37} < \alpha < \frac{22}{21}$$

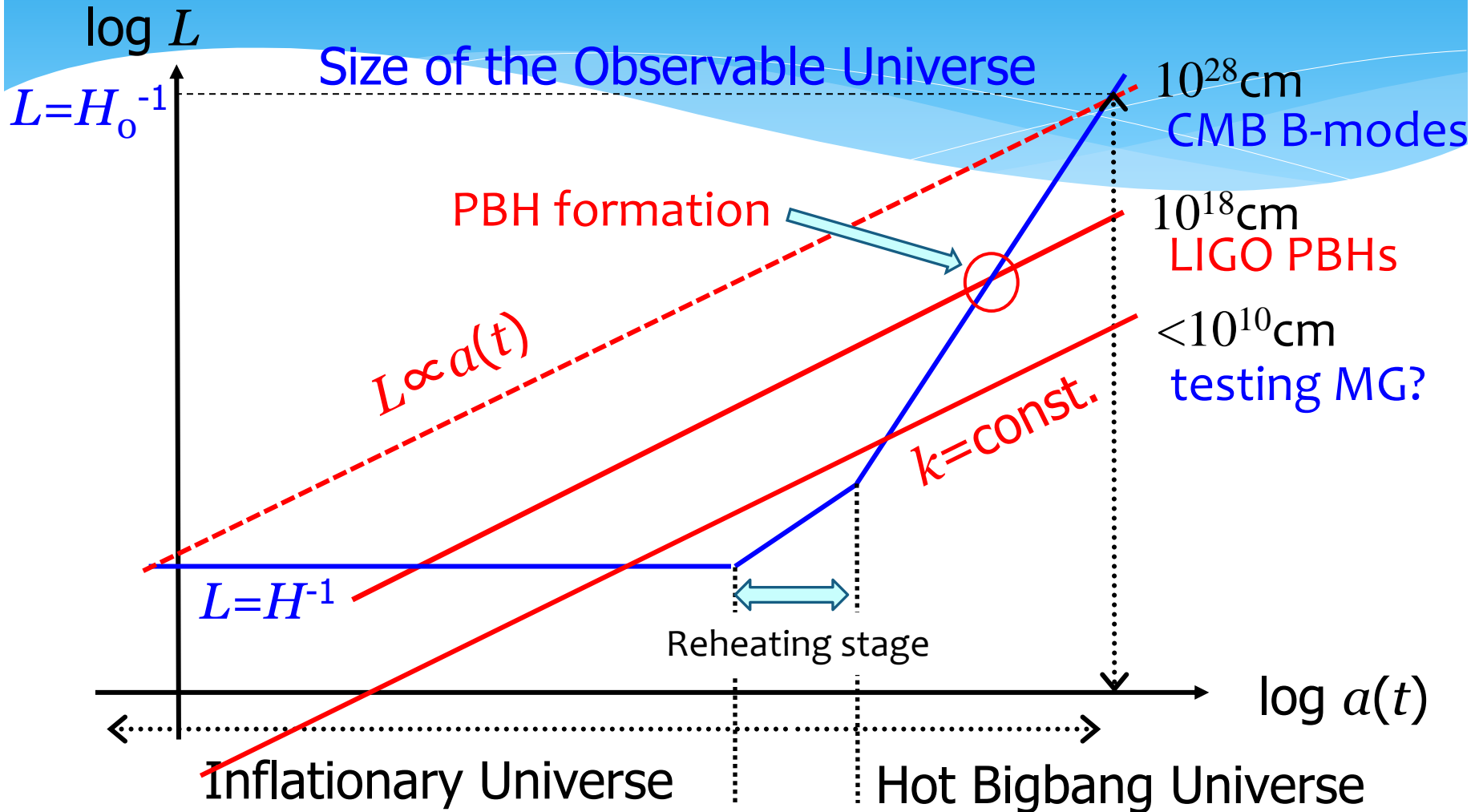


$$\alpha \approx 4$$

clearly distinguishable!

O'Leary et al (2016)

testing inflation by GW astronomy



Summary

* Inflation has become the **standard model** of the Universe.
further tests are needed to confirm inflation.

* **Cosmological GWs** are the key to understanding/confirmation of inflation.

* **LIGO detection of GWs** marked the **1st milestone** in GW physics/astronomy.
The Dawn has arrived!

* **LIGO BHs** may be **primordial**.

advanced GW detectors will prove/disprove the scenario.

* **Multi-frequency GW** astronomy/astrophysics has begun.

GWs will be **an essential tool** for exploring
the Physics of the Unknown Universe