

Modelling Polarized Foregrounds

Andrei Frolov

Kavli Institute for the Physics and Mathematics of the Universe

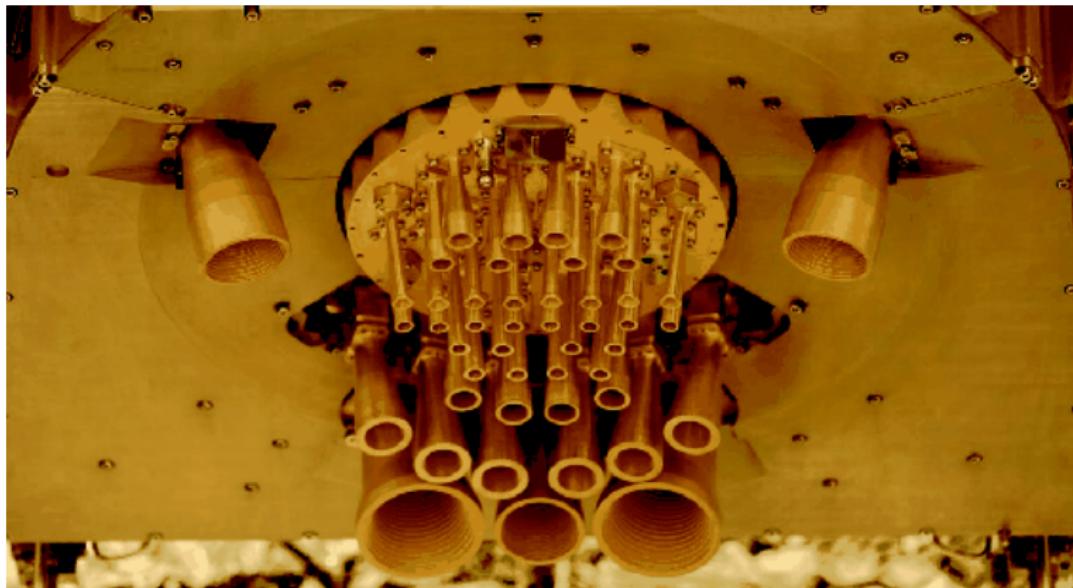
Kashiwanoha, Japan

14 November 2019

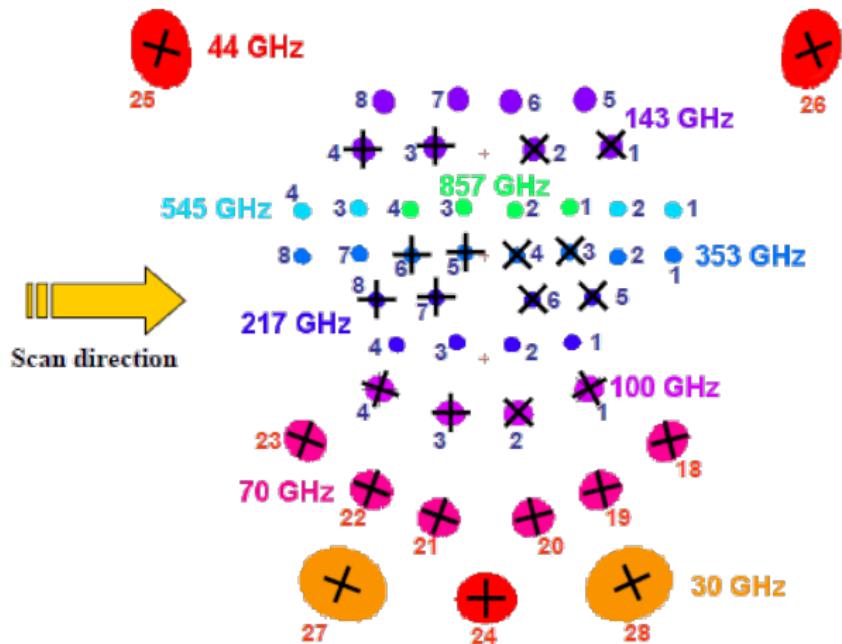
Planck before Launch



Planck Focal Plane

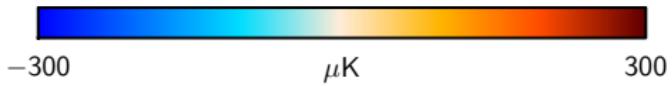
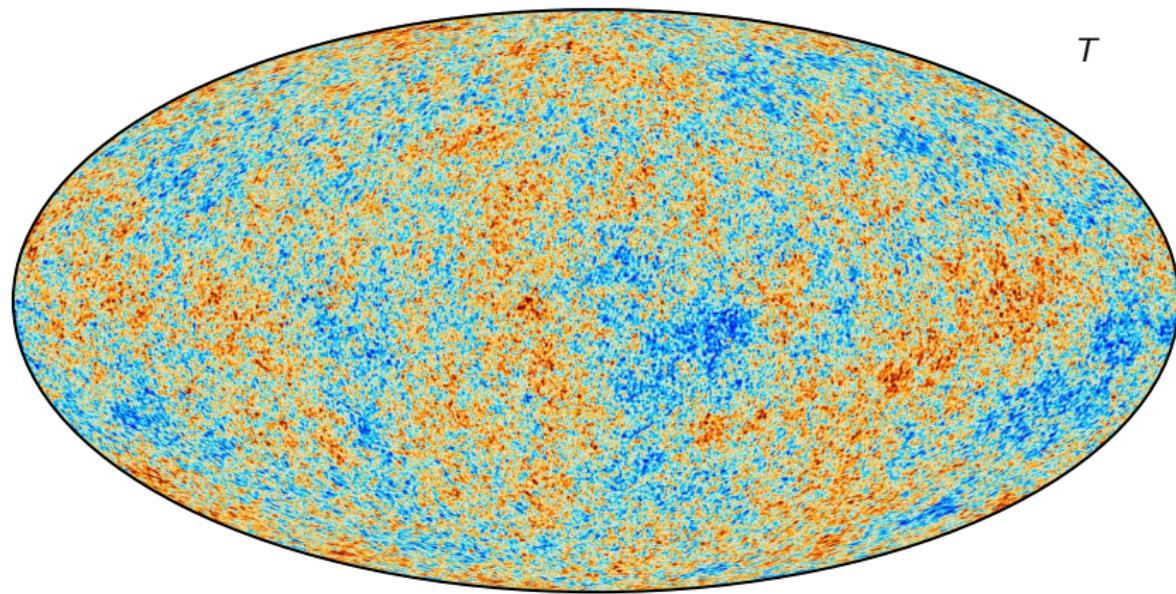


Planck Focal Plane Schematics



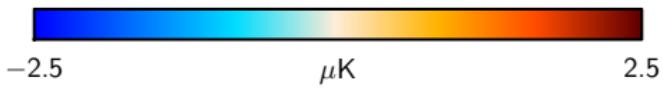
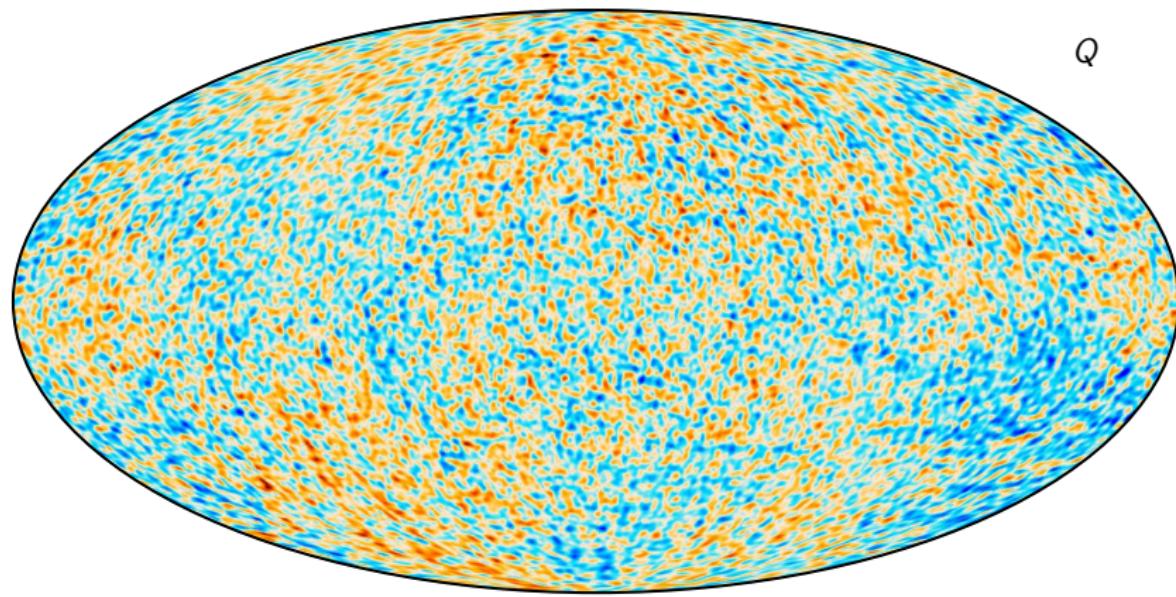
Planck 2018 CMB Maps

- Intensity T
- Polarization Q
- Polarization U



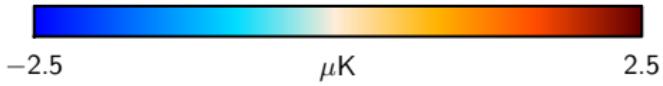
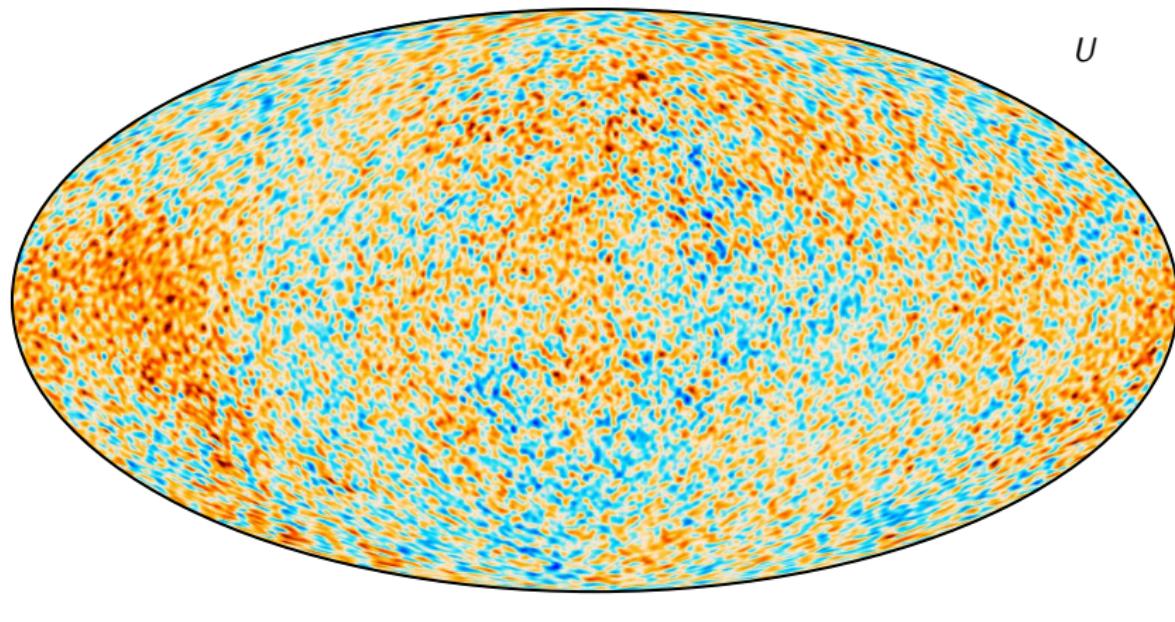
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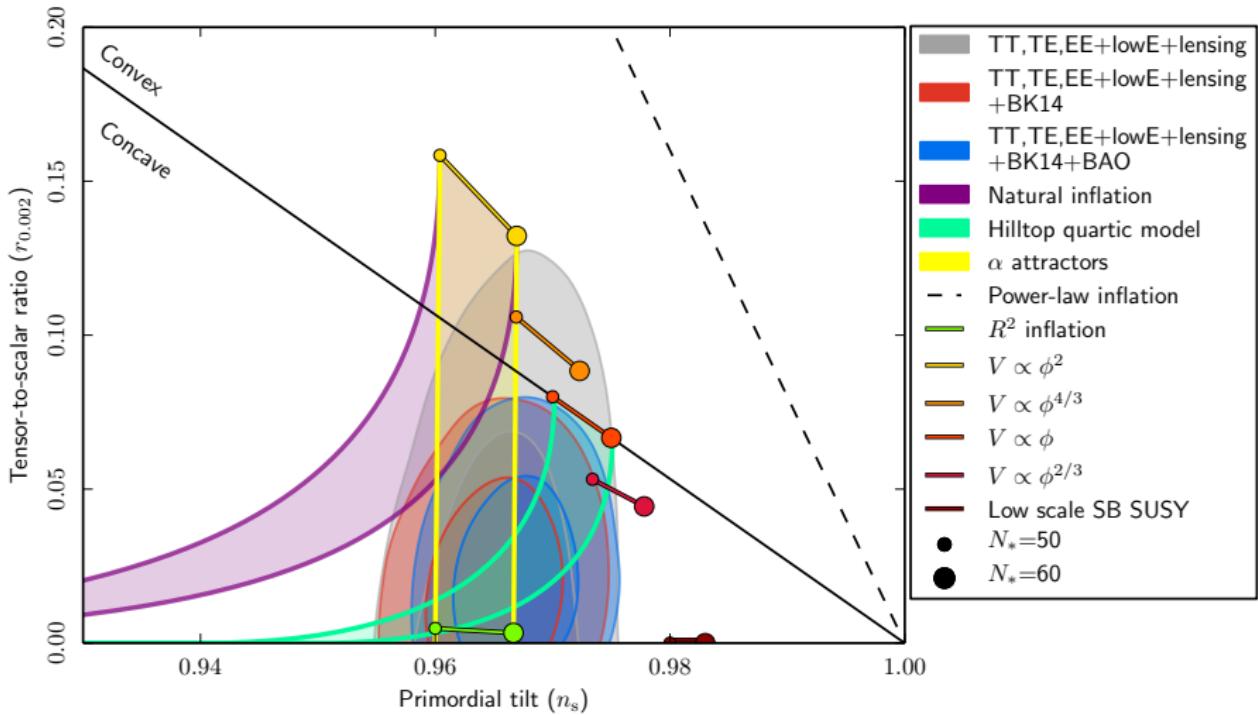


Planck 2018 CMB Maps

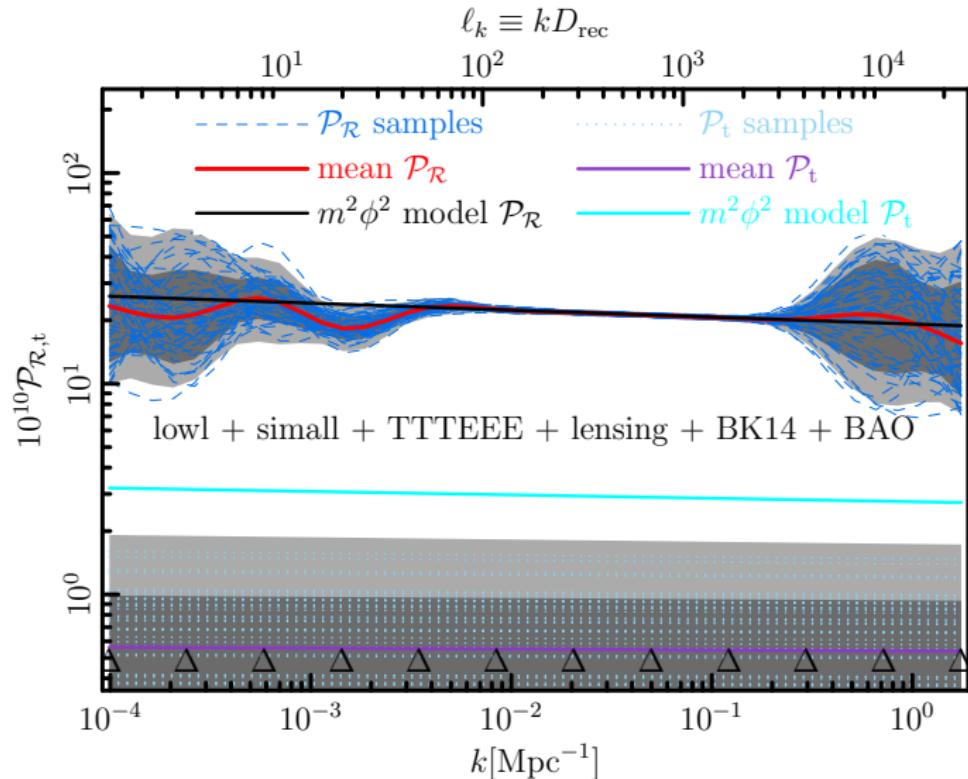
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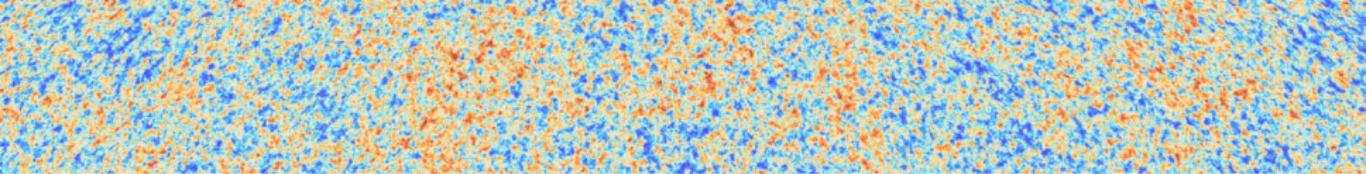


Planck 2018 Constraints on Inflation



Primordial Scalar Fluctuations are now Nailed

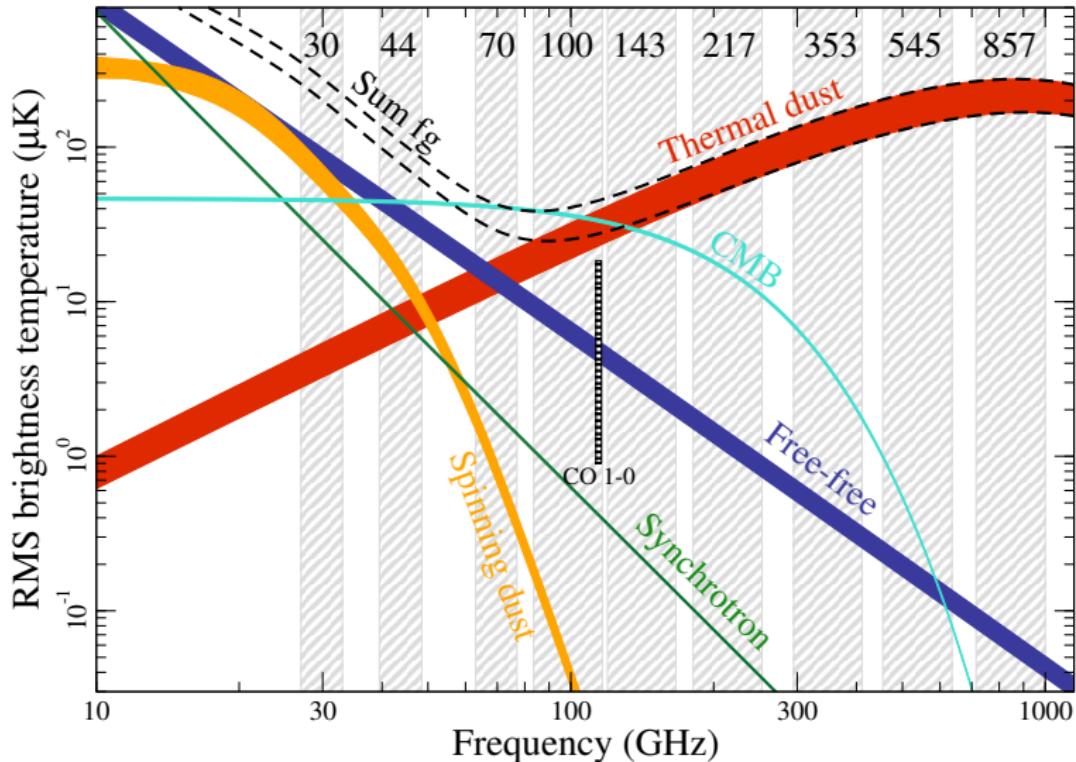




The target now is B-modes!

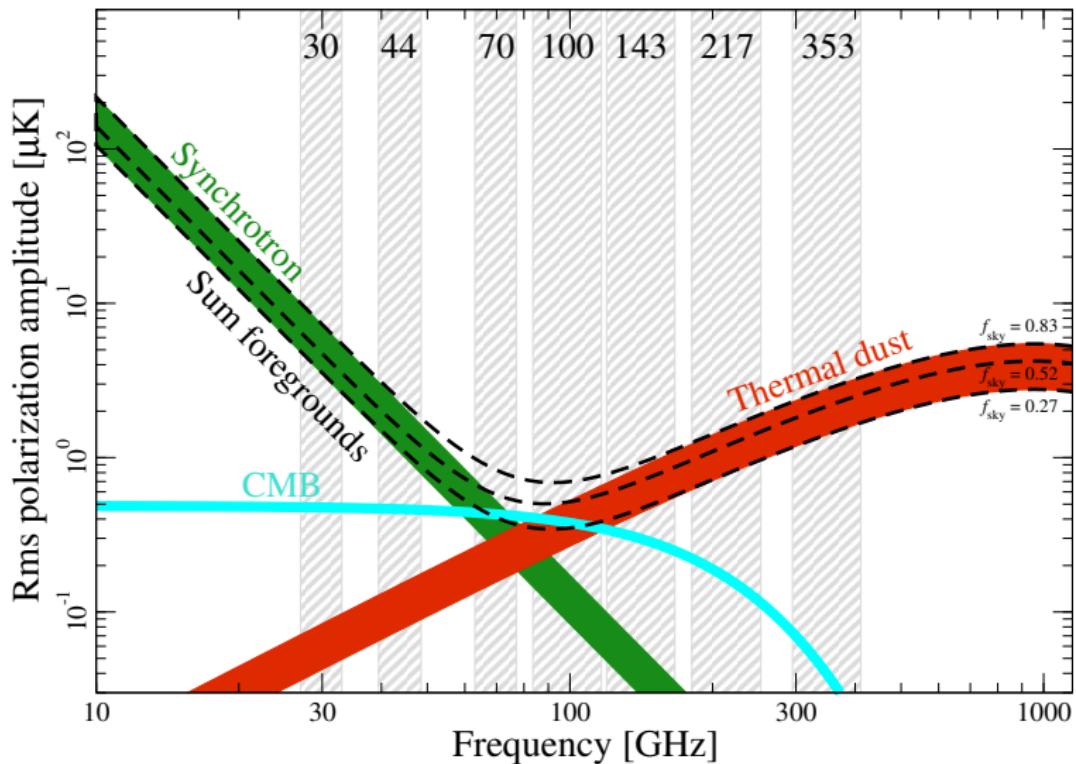
CMB vs. Astrophysical Foregrounds

- Intensity
- Polarization
- Atmospheric Transmission



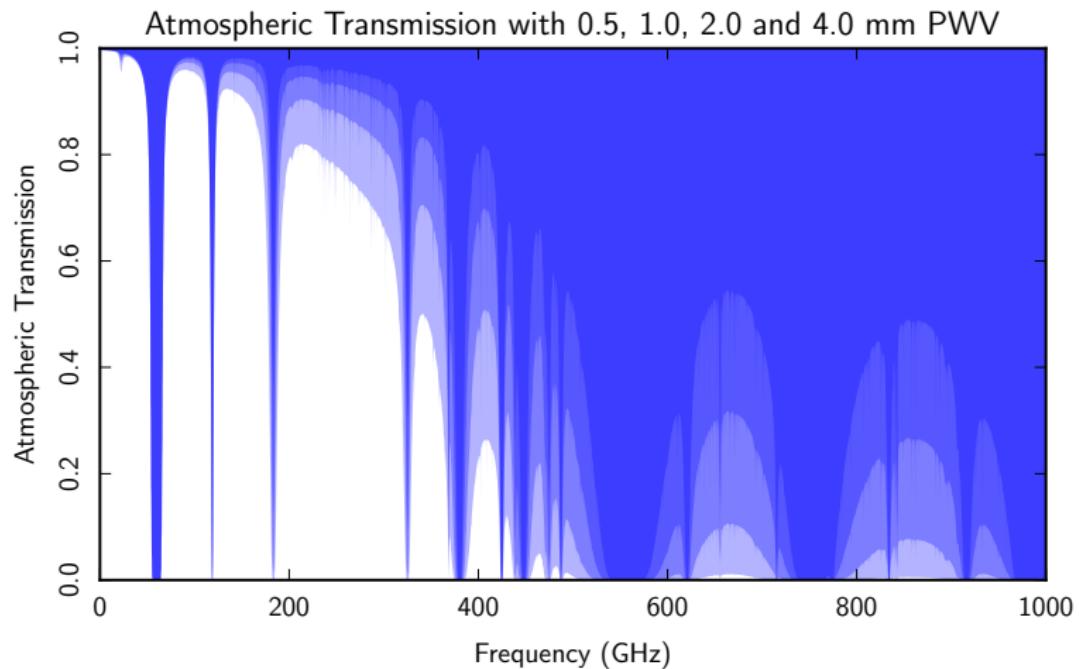
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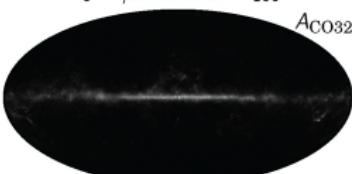
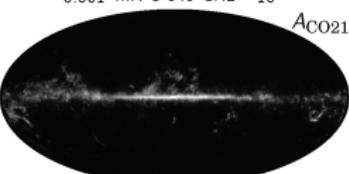
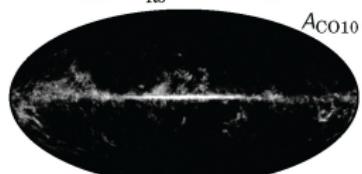
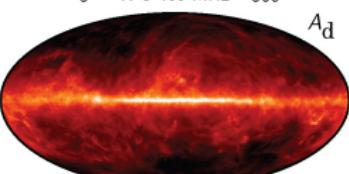
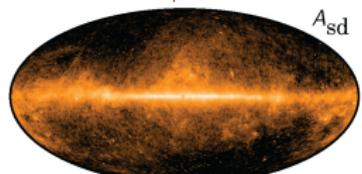
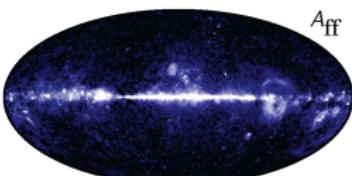
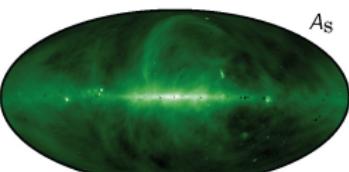
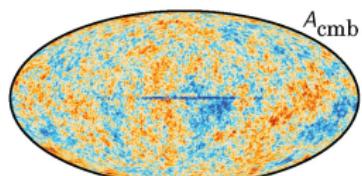


CMB vs. Astrophysical Foregrounds

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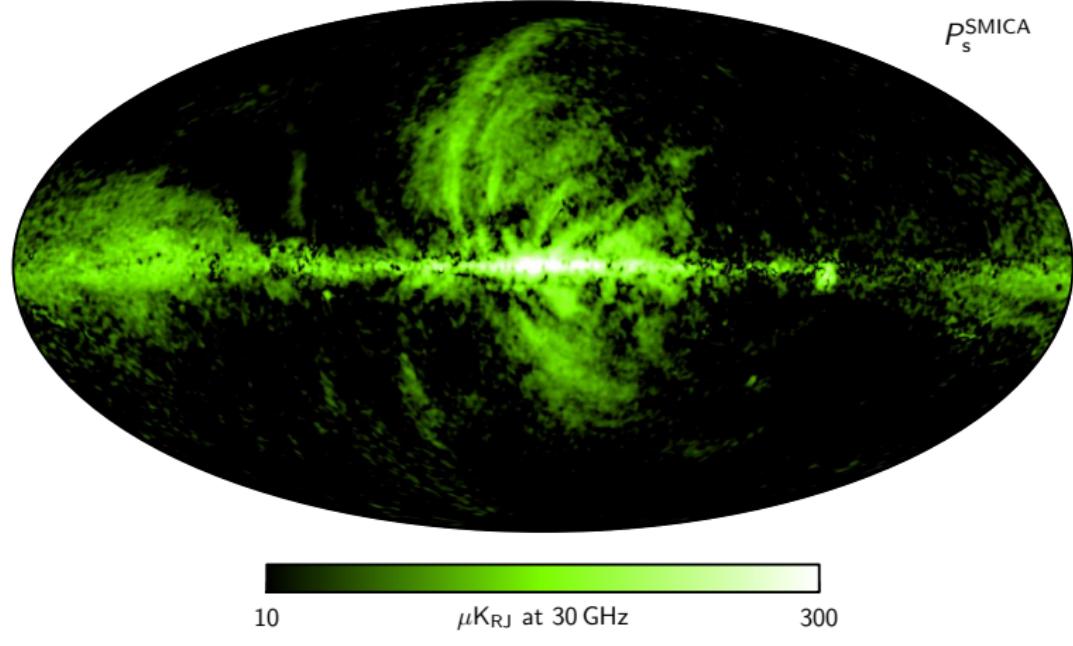
Temperature Component Maps



Polarization Component Maps

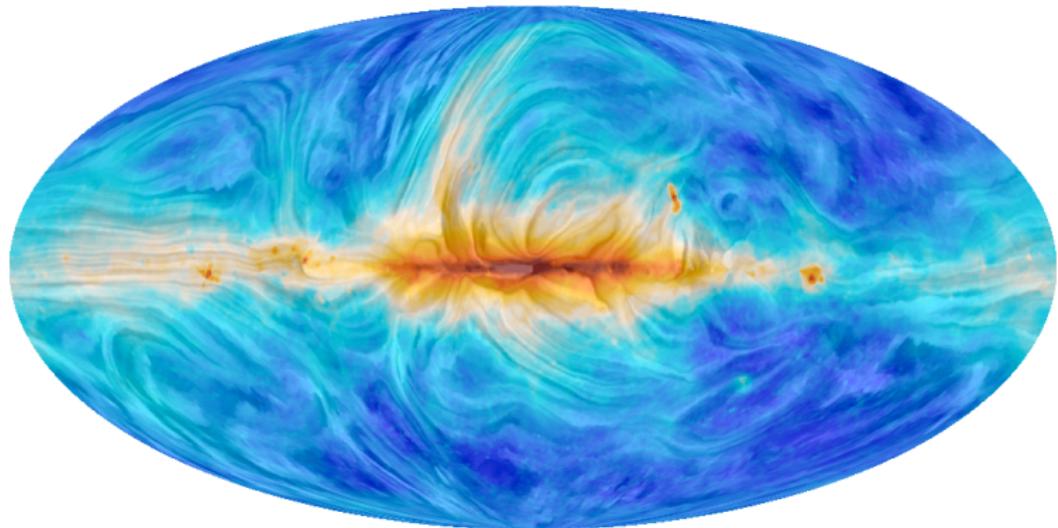
- Two main foregrounds, synchrotron emission and thermal dust
- Amplitude of CMB polarization **is less** than foregrounds
- Dust emission is highly polarized (polarization fraction is up to 20%)

Synchrotron Polarization Amplitude



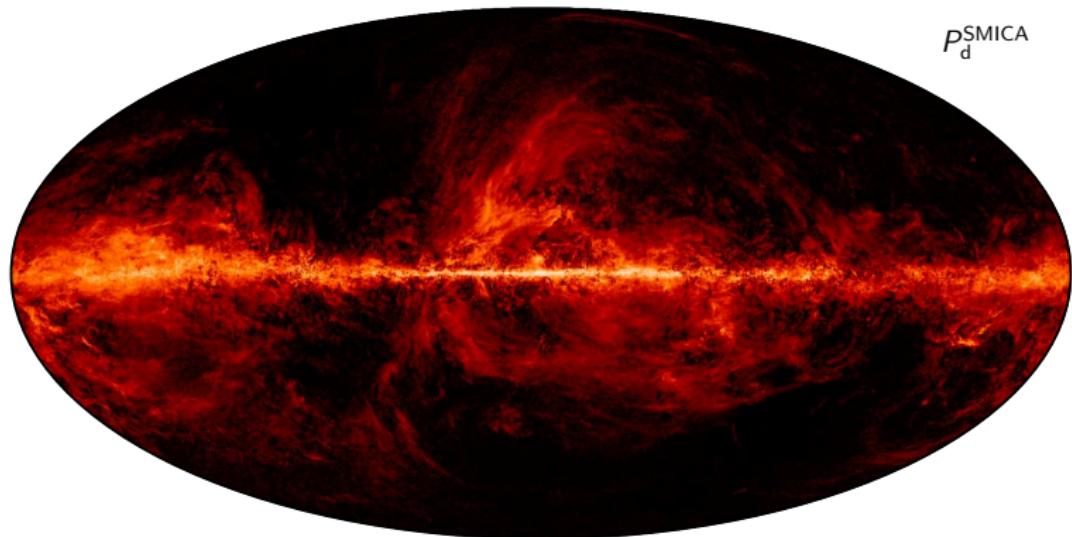
$P = \sqrt{Q^2 + U^2}$, SMICA component at 30GHz, smoothed to 40'

Polarization Direction and Total Intensity



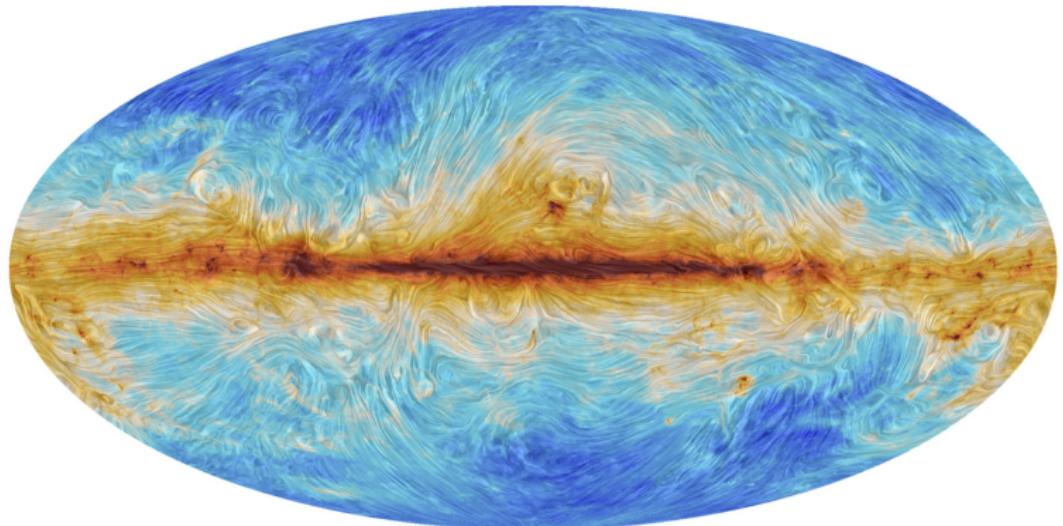
The colours represent intensity. The “drapery” pattern indicates the orientation of magnetic field projected on the plane of the sky, orthogonal to the observed polarization.

Dust Polarization Amplitude



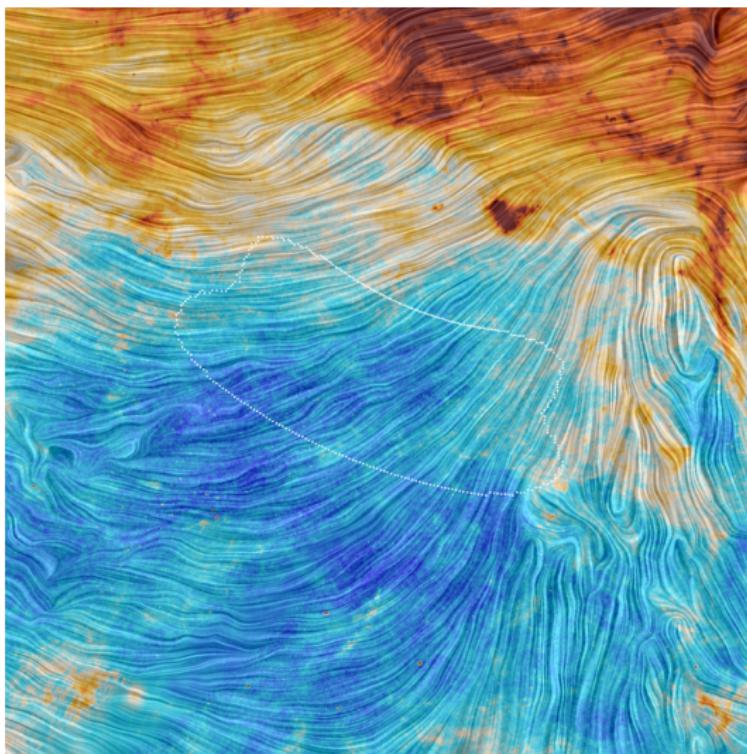
$P = \sqrt{Q^2 + U^2}$, SMICA component at 353GHz, smoothed to 12'

Polarization Direction and Total Intensity

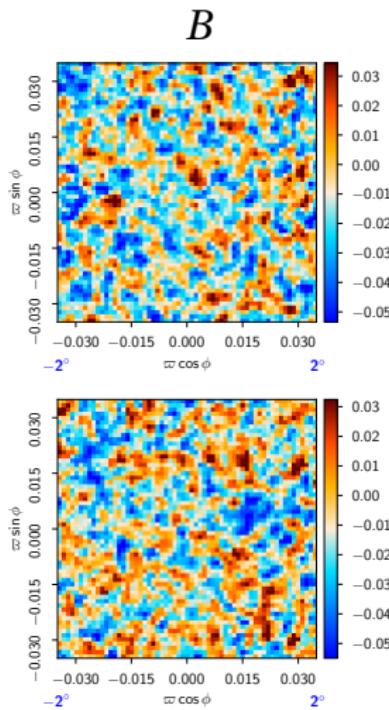
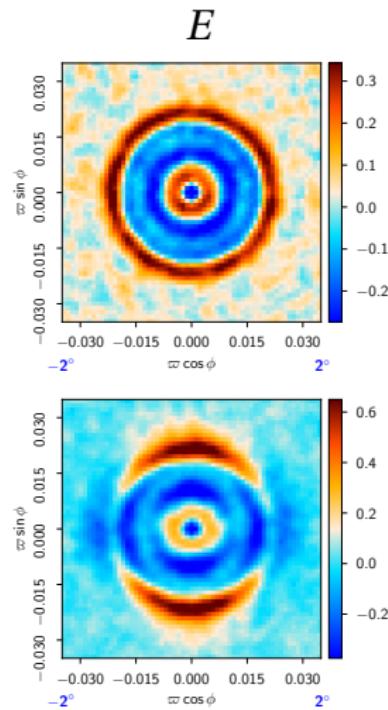
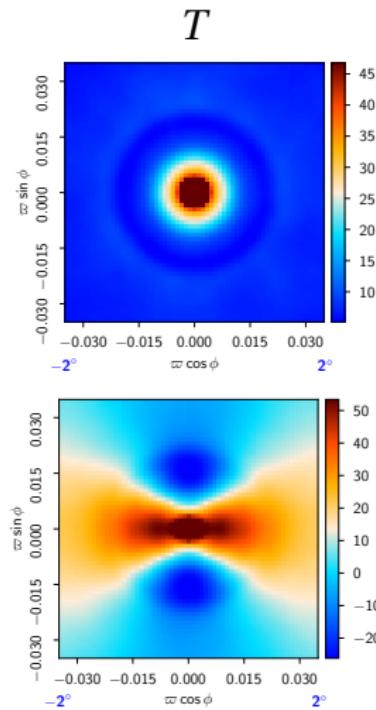


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Planck View of BICEP2 Field

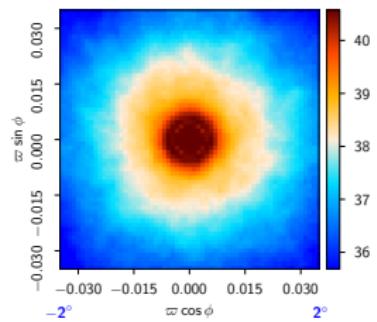


CMB Emission Stacks

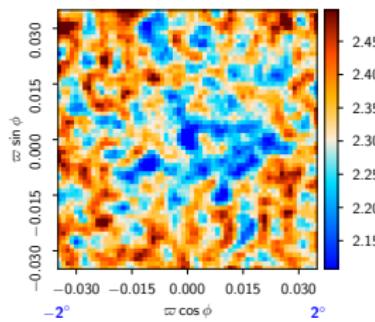


30GHz Emission Stacks

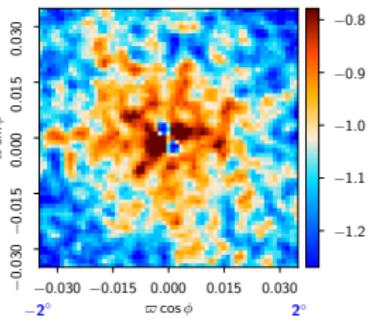
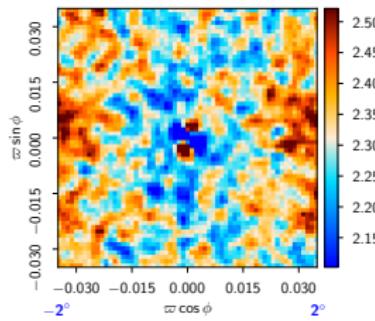
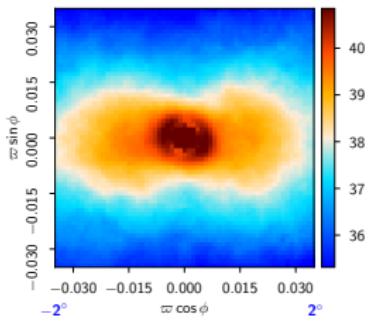
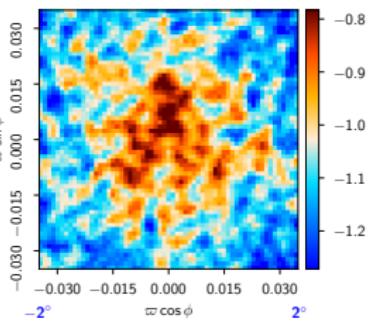
T



E

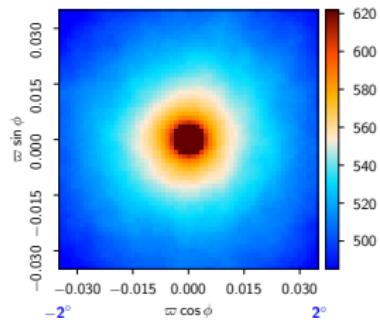


B

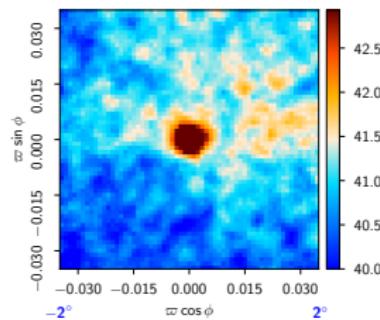


353GHz Emission Stacks

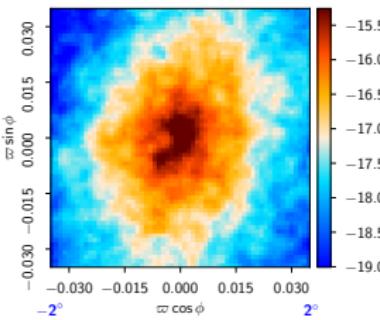
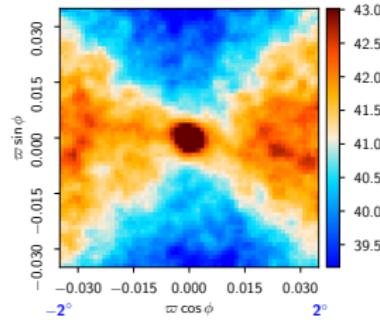
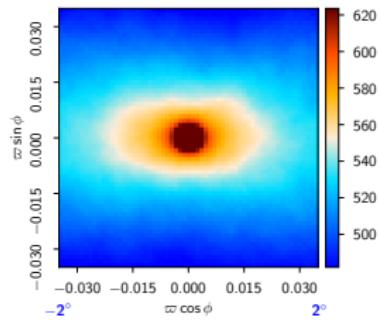
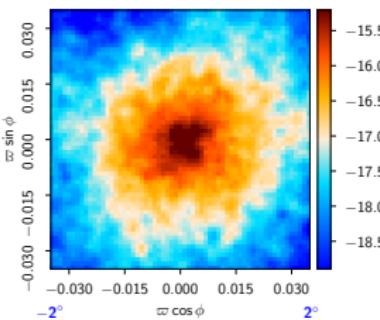
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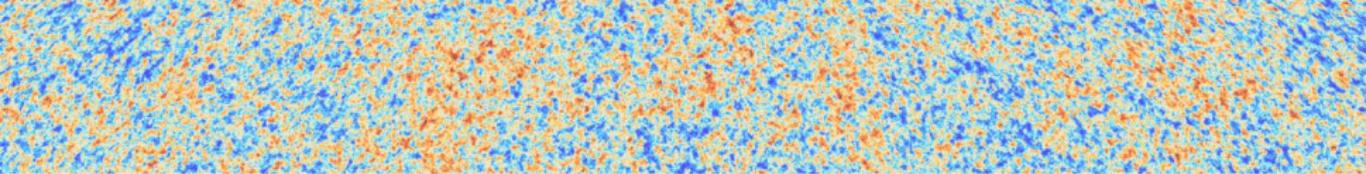


E



B





Modelling Polarized Dust Emission

Polarized Dust Emission

Polarization is caused by magnetic field alignment:

$$\begin{aligned} I &= \int S_\nu e^{-\tau_\nu} d\tau_\nu \left[1 - p_0 \left(\cos^2 \gamma - \frac{2}{3} \right) \right] \\ \begin{Bmatrix} Q \\ U \end{Bmatrix} &= \int S_\nu e^{-\tau_\nu} d\tau_\nu \begin{Bmatrix} \cos 2\psi \\ \sin 2\psi \end{Bmatrix} p_0 \cos^2 \gamma \end{aligned}$$

(p_0 is intrinsic polarization fraction ~ 0.21)

For a single layer, P/I determines magnetic field orientation:

$$\frac{I-P}{I+P} = 1 - \frac{6p_0}{2p_0+3} \cos^2 \gamma$$

Polarization Fraction Tensor

Transform polarization tensor into polarization fraction tensor:

$$\begin{bmatrix} i+q & u \\ u & i-q \end{bmatrix} = \ln \begin{bmatrix} I+Q & U \\ U & I-Q \end{bmatrix}$$

This is an invertible transformation on IQU maps:

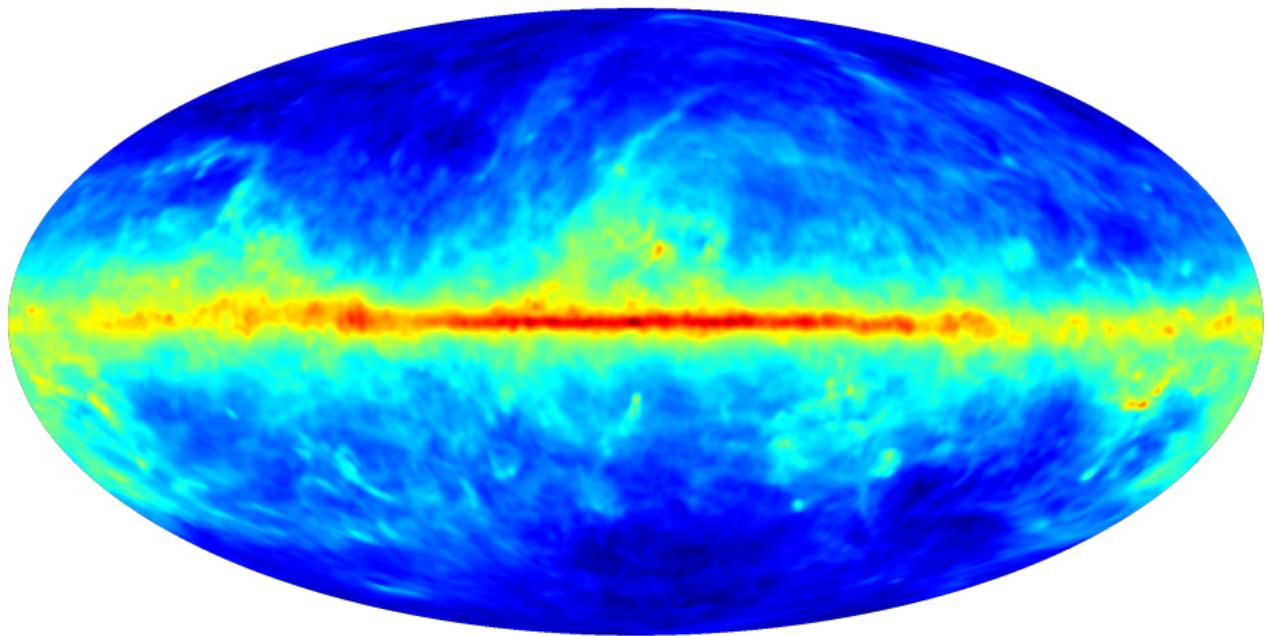
$$i = \frac{1}{2} \ln(I^2 - P^2), \quad q = \frac{1}{2} \frac{Q}{P} \ln \frac{I+P}{I-P}, \quad u = \frac{1}{2} \frac{U}{P} \ln \frac{I+P}{I-P}$$

$$I = e^i \cosh p, \quad Q = \frac{q}{p} e^i \sinh p, \quad U = \frac{u}{p} e^i \sinh p$$

Polarization Fraction Tensor

[Dust]

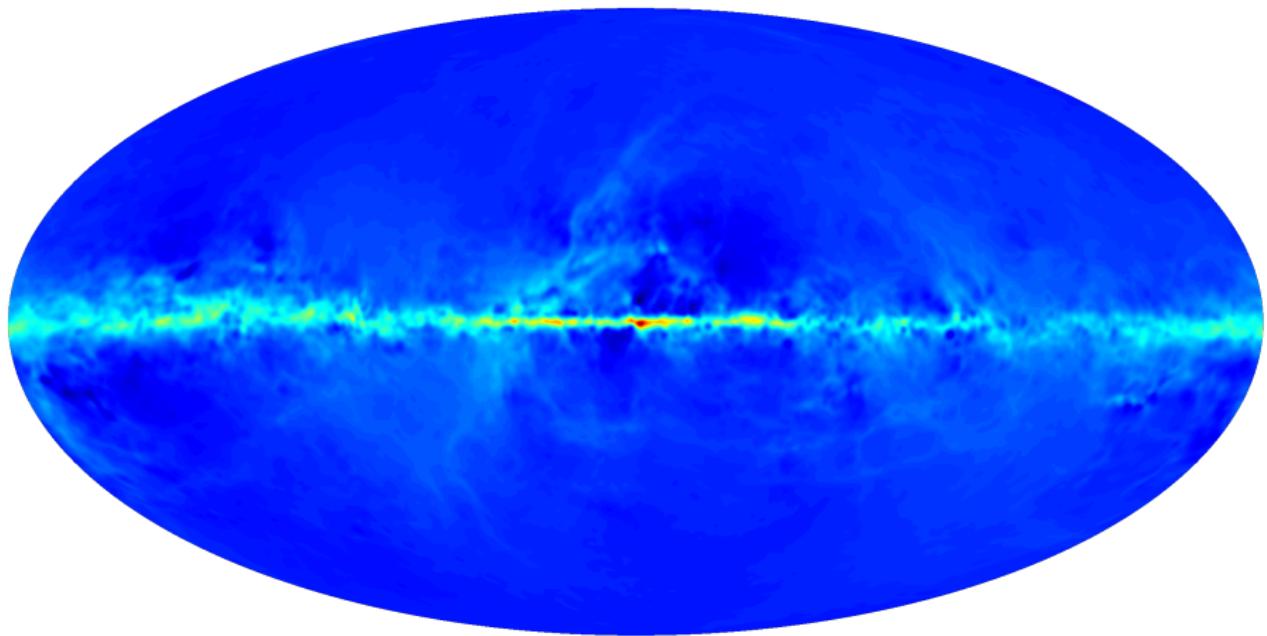
- I ◦ E ◦ B ◦ i ◦ e ◦ b ◦



Polarization Fraction Tensor

[Dust]

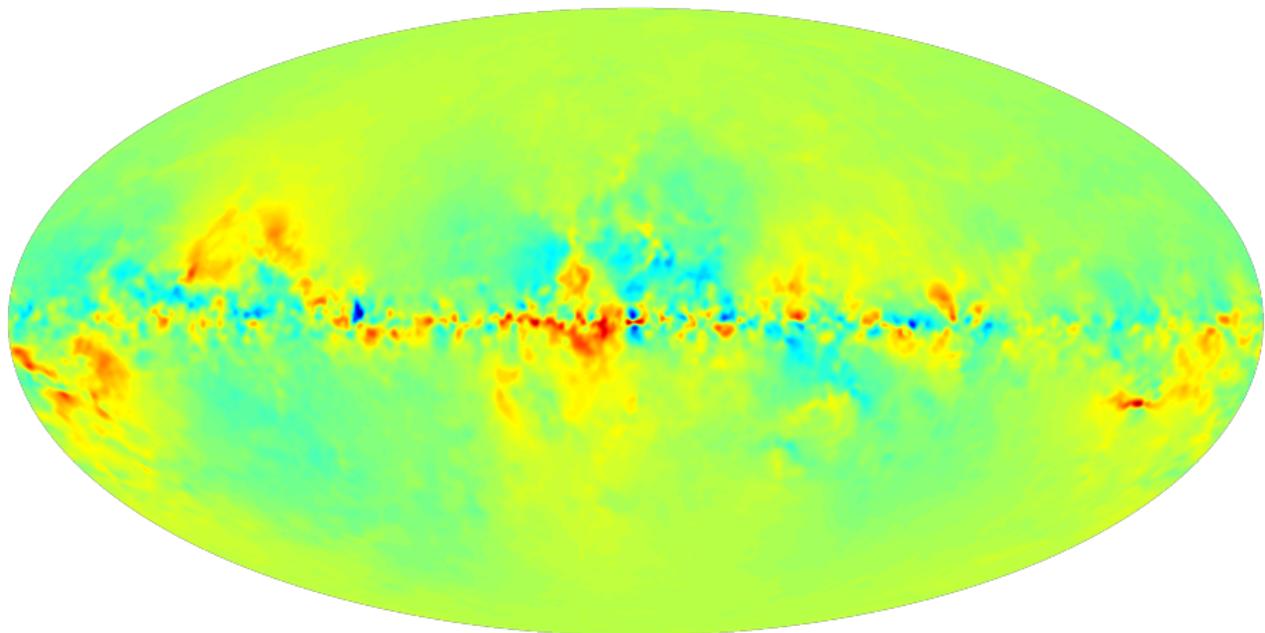
• In I \circ E \circ B \circ i \circ e \circ b \circ



Polarization Fraction Tensor

[Dust]

• In I \circ E \circ B \circ i \circ e \circ b \circ

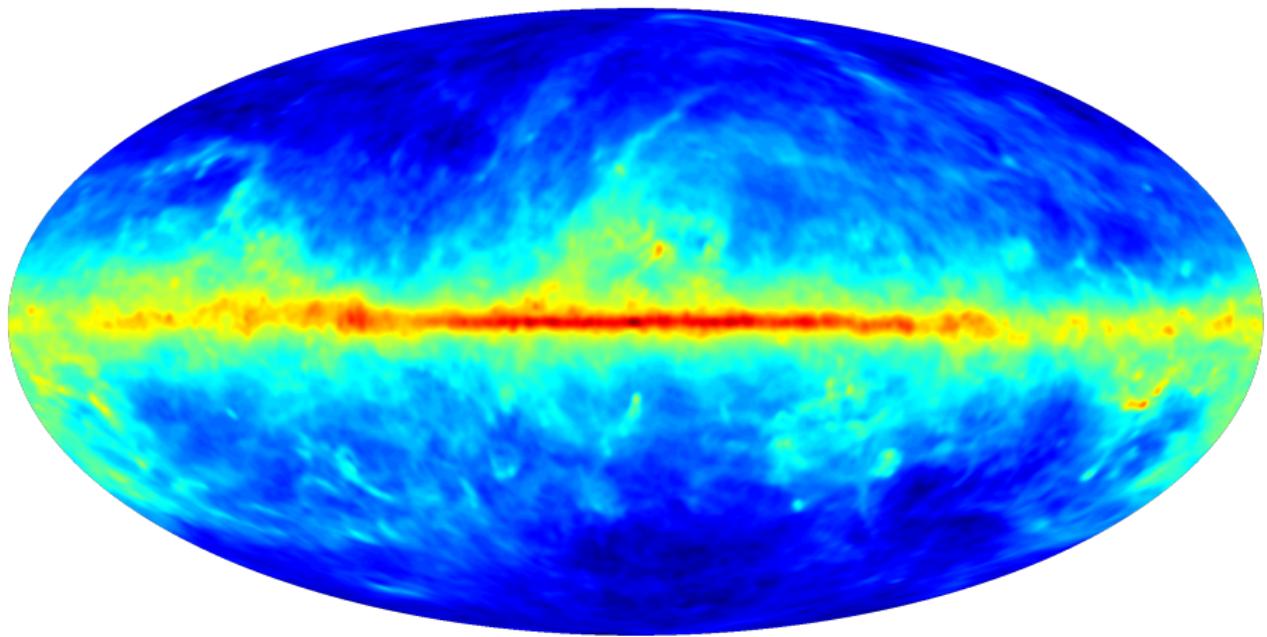


-1.29E-03 0 +1.01E-03

Polarization Fraction Tensor

[Dust]

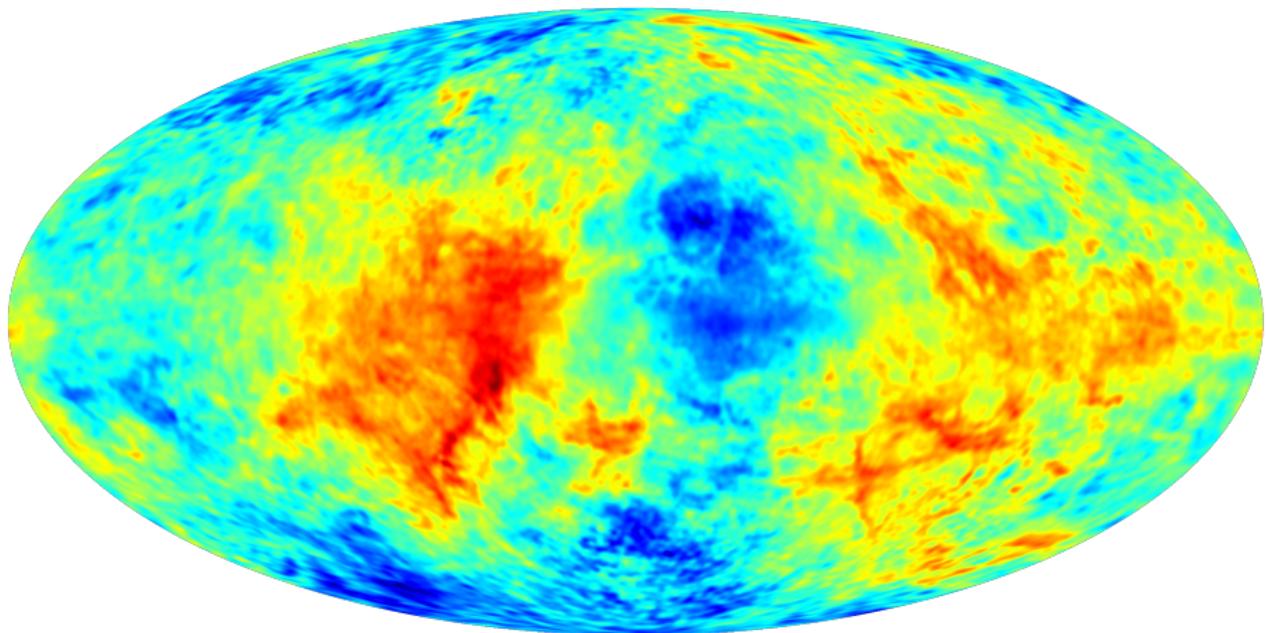
• In I • E • B • i • e • b •



Polarization Fraction Tensor

[Dust]

• In I • E • B • i • e • b •

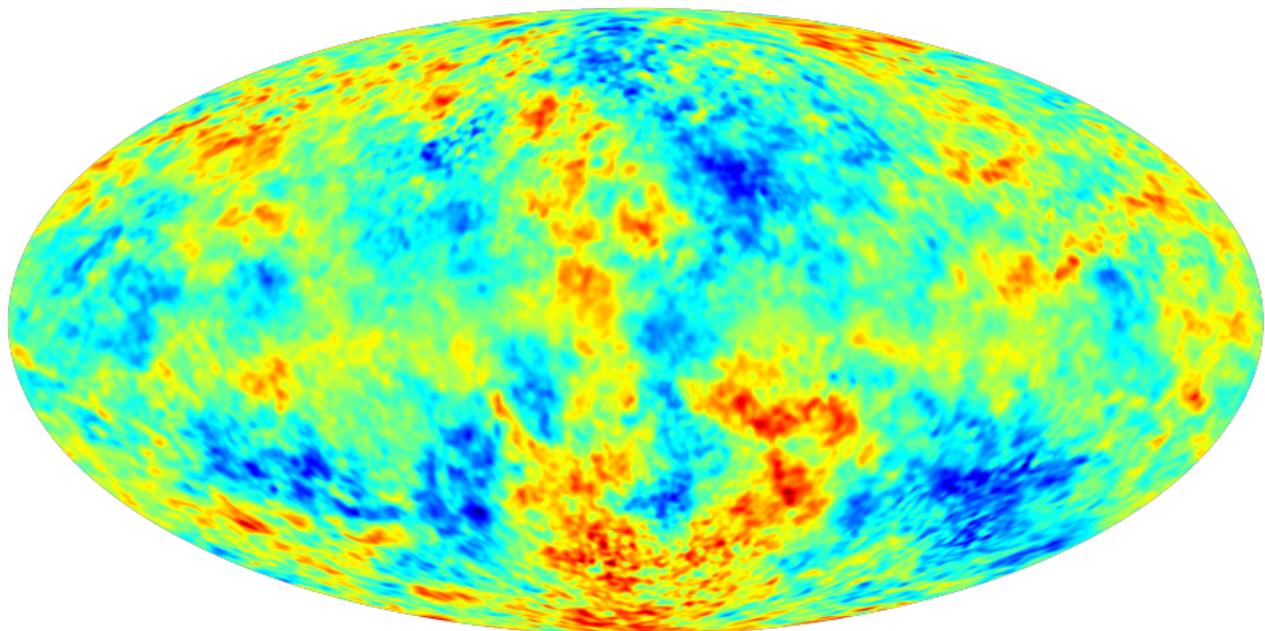


-0.274 +0.254

Polarization Fraction Tensor

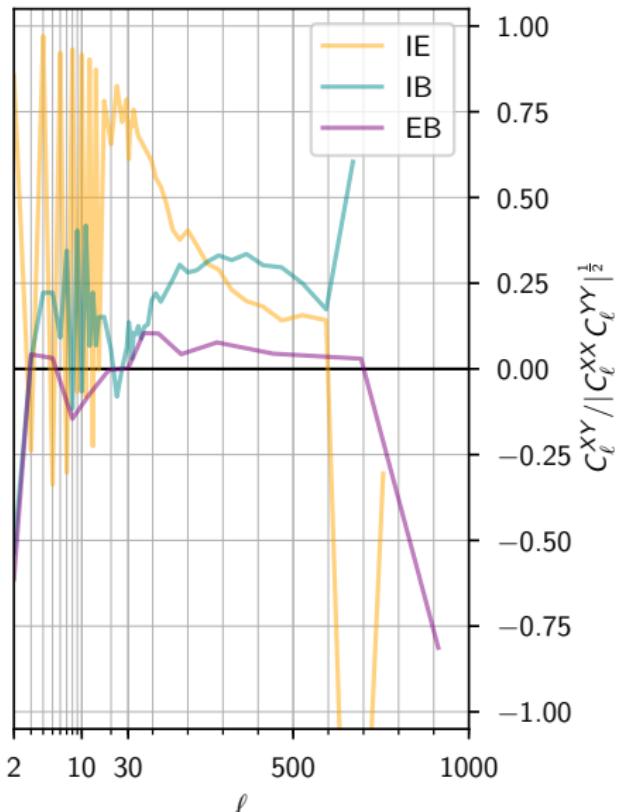
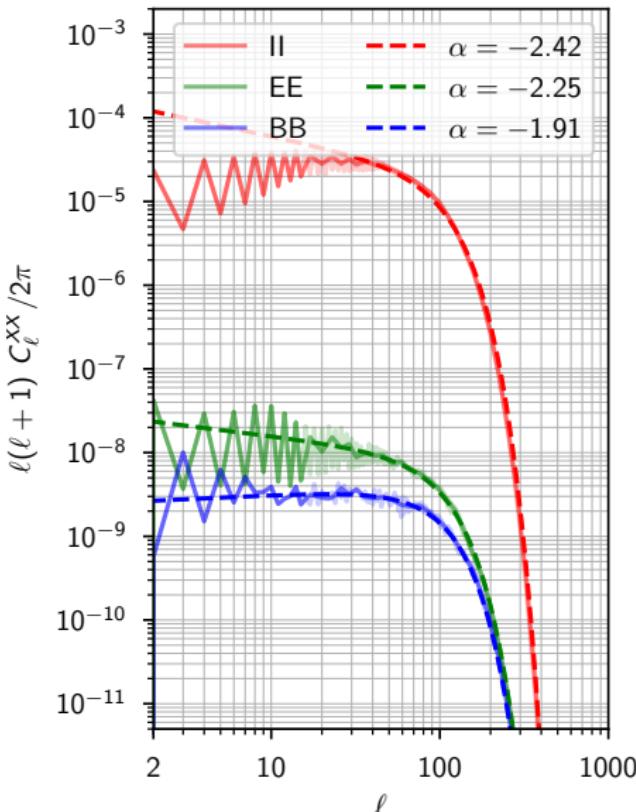
[Dust]

• In I o E o B o i o e o b o



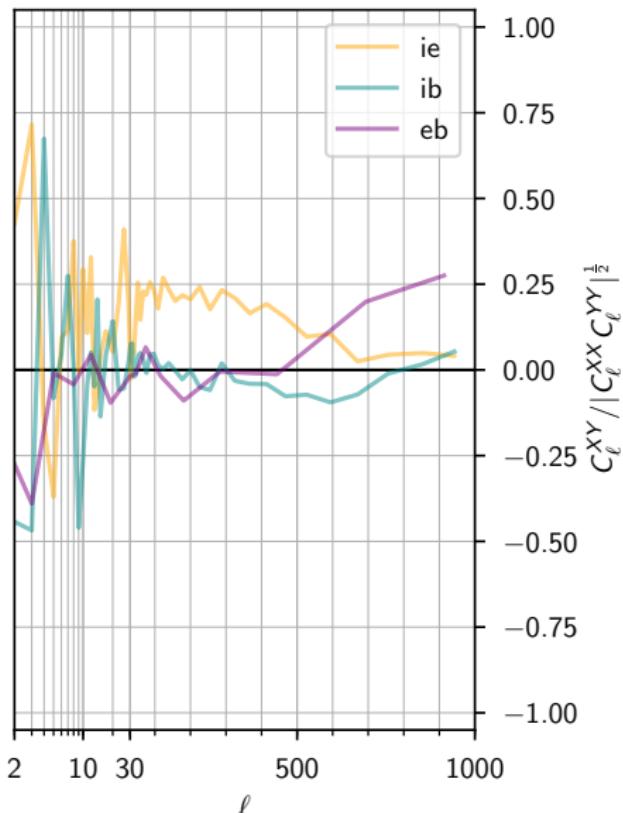
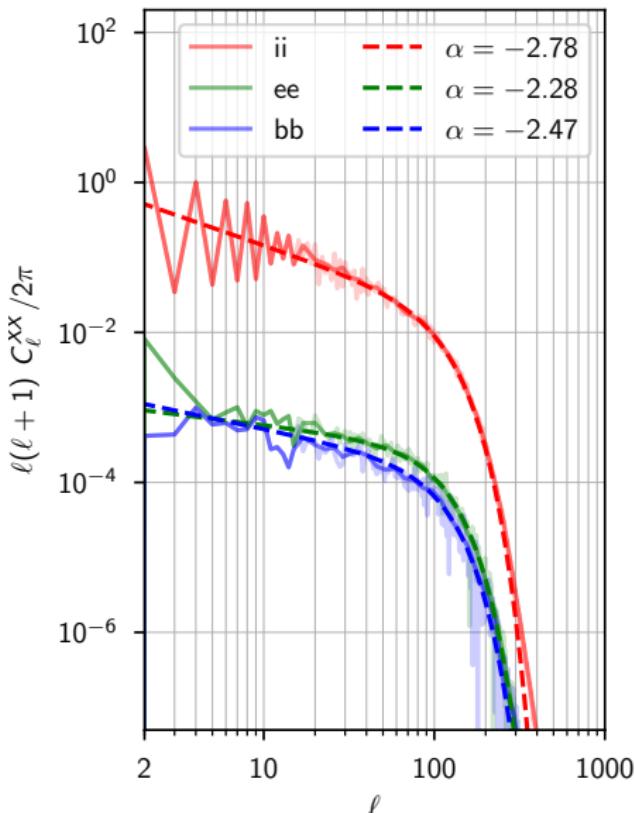
Parity-Violating Correlations Disappear!

- polarization
- polarization fraction



Parity-Violating Correlations Disappear!

- polarization
- polarization fraction



Geometric Factors in Emission Integral

$$p \equiv \frac{B_\phi^2 + B_\theta^2}{B^2} = \cos^2 \gamma$$

$$q \equiv \frac{B_\phi^2 - B_\theta^2}{B^2} = \cos^2 \gamma \cos 2\psi$$

$$u \equiv -\frac{2B_\phi B_\theta}{B^2} = \cos^2 \gamma \sin 2\psi$$

These get averaged along the line of sight with weighting:

$$\langle X \rangle = \frac{1}{s_\nu} \int S_\nu e^{-\tau_\nu} d\tau_\nu X, \quad s_\nu = \int S_\nu e^{-\tau_\nu} d\tau_\nu$$

Magnetic Field Model

Split magnetic field into large-scale and random components:

$$\mathbf{B} = \bar{\mathbf{B}} + \delta\mathbf{B}$$

To first order, intensity and polarizations components are:

$$I = s_\nu \left(1 + \frac{2}{3} p_0 \right) - s_\nu p_0 \left[\mathfrak{p}[\bar{\mathbf{B}}] + \left. \frac{\partial \mathfrak{p}}{\partial \mathbf{B}} \right|_{\bar{\mathbf{B}}} \langle \delta\mathbf{B} \rangle + \dots \right]$$

$$Q = s_\nu p_0 \left[\mathfrak{q}[\bar{\mathbf{B}}] + \left. \frac{\partial \mathfrak{q}}{\partial \mathbf{B}} \right|_{\bar{\mathbf{B}}} \langle \delta\mathbf{B} \rangle + \dots \right]$$

$$U = s_\nu p_0 \left[\mathfrak{u}[\bar{\mathbf{B}}] + \left. \frac{\partial \mathfrak{u}}{\partial \mathbf{B}} \right|_{\bar{\mathbf{B}}} \langle \delta\mathbf{B} \rangle + \dots \right]$$

They split into large-scale pattern and random component!

Reconstruct Large-Scale Magnetic Field

Estimator of dust column depth:

$$I + P = s_\nu \left(1 + \frac{2}{3} p_0 \right) + O(\delta B^2),$$

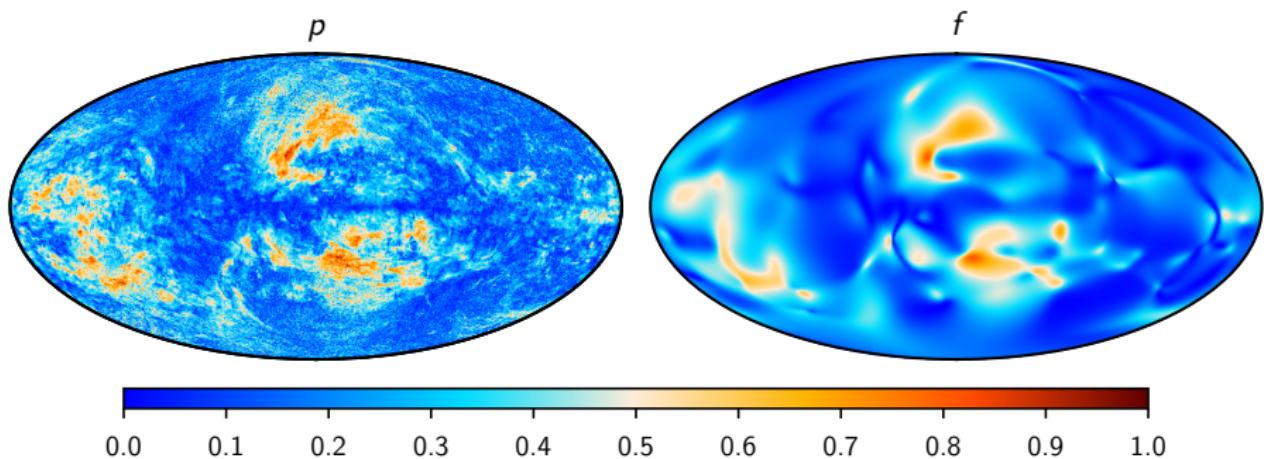
Estimators of magnetic field geometry:

$$\begin{aligned}\tilde{q} \equiv \frac{Q}{I+P} &= \frac{3p_0}{3+2p_0} \left[q[\bar{\mathbf{B}}] + \left. \frac{\partial q}{\partial \mathbf{B}} \right|_{\bar{\mathbf{B}}} \langle \delta \mathbf{B} \rangle + \dots \right], \\ \tilde{u} \equiv \frac{U}{I+P} &= \frac{3p_0}{3+2p_0} \left[u[\bar{\mathbf{B}}] + \left. \frac{\partial u}{\partial \mathbf{B}} \right|_{\bar{\mathbf{B}}} \langle \delta \mathbf{B} \rangle + \dots \right].\end{aligned}$$

Reconstruct large-scale magnetic field using least square fit:

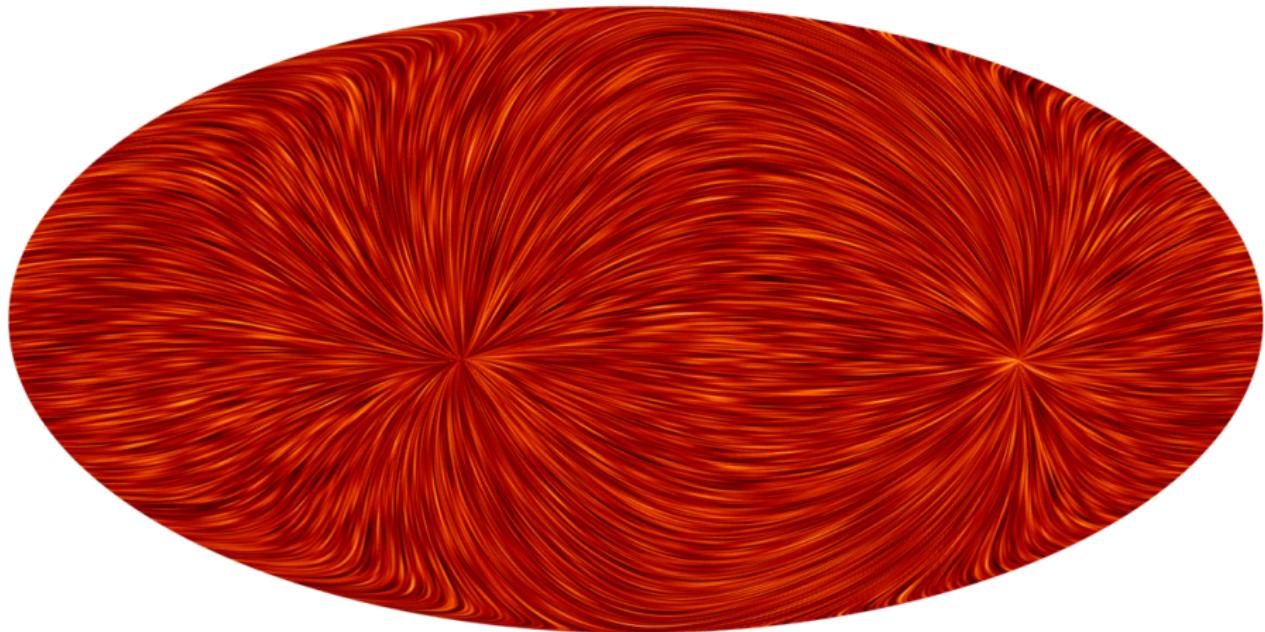
$$\chi_{\bar{\mathbf{B}}}^2 = (\tilde{q} - \varepsilon q[\bar{\mathbf{B}}])^2 + (\tilde{u} - \varepsilon u[\bar{\mathbf{B}}])^2, \quad \varepsilon = \frac{3p_0}{3+2p_0}.$$

Reconstructed Polarization Fraction



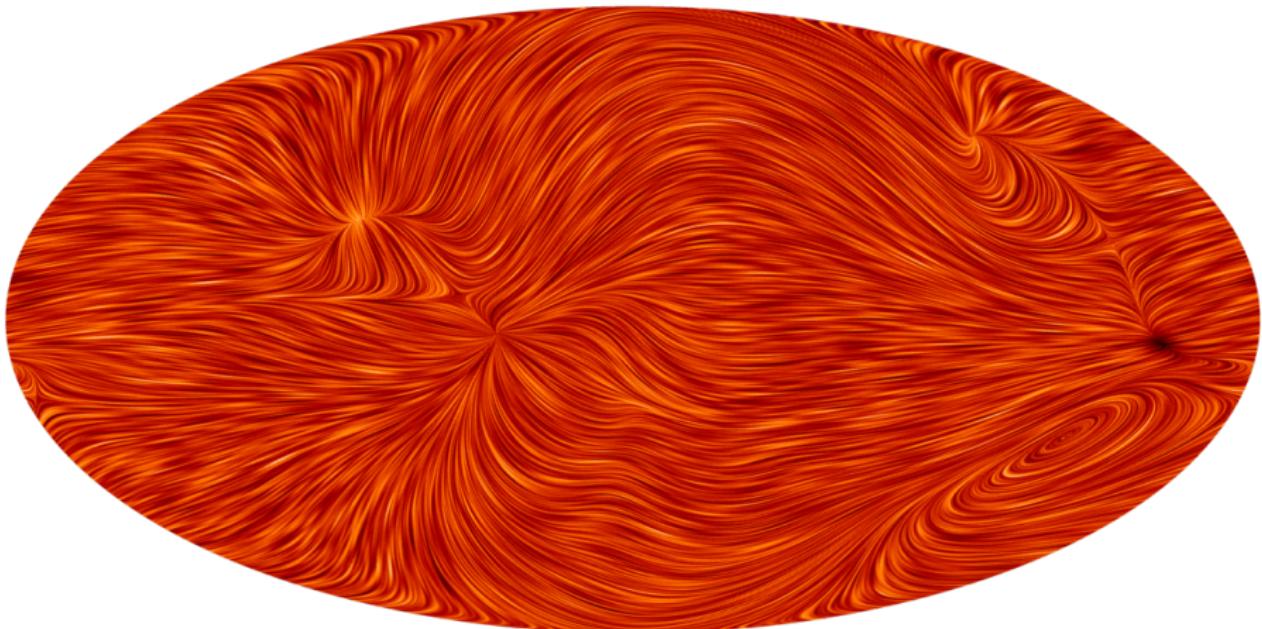
Magnetic Field Lines

• $\ell_{\max} = 1^\circ$ • $\ell_{\max} = 5^\circ$ • $\ell_{\max} = 10^\circ$ • $\ell_{\max} = 20^\circ$



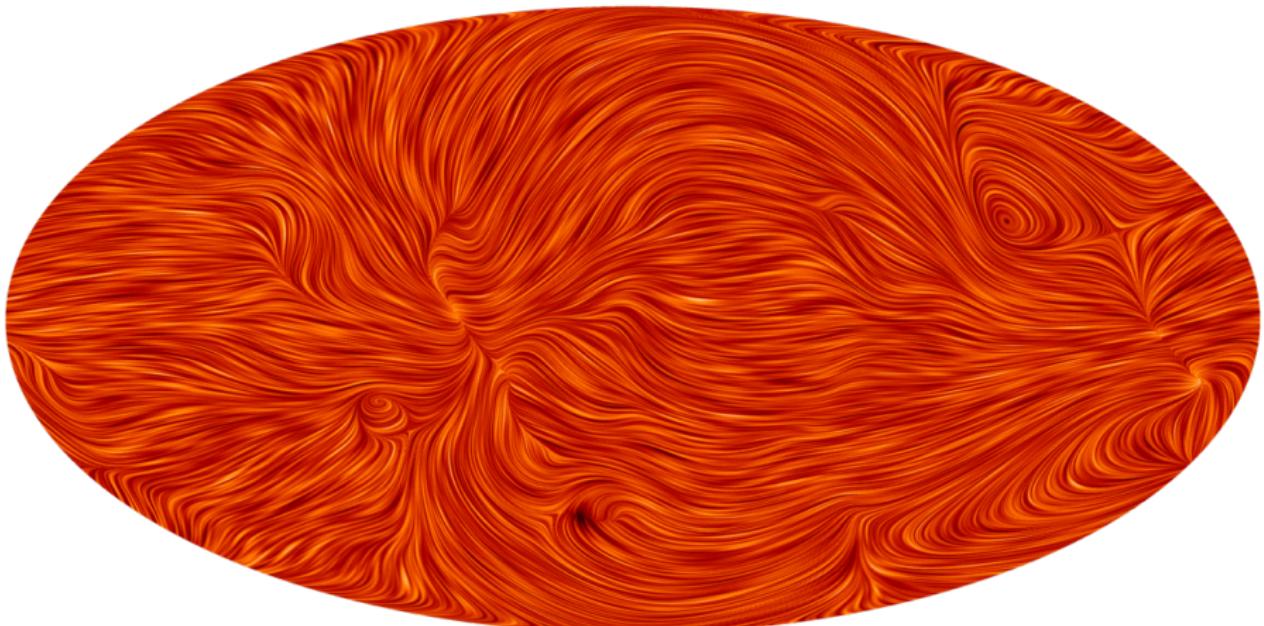
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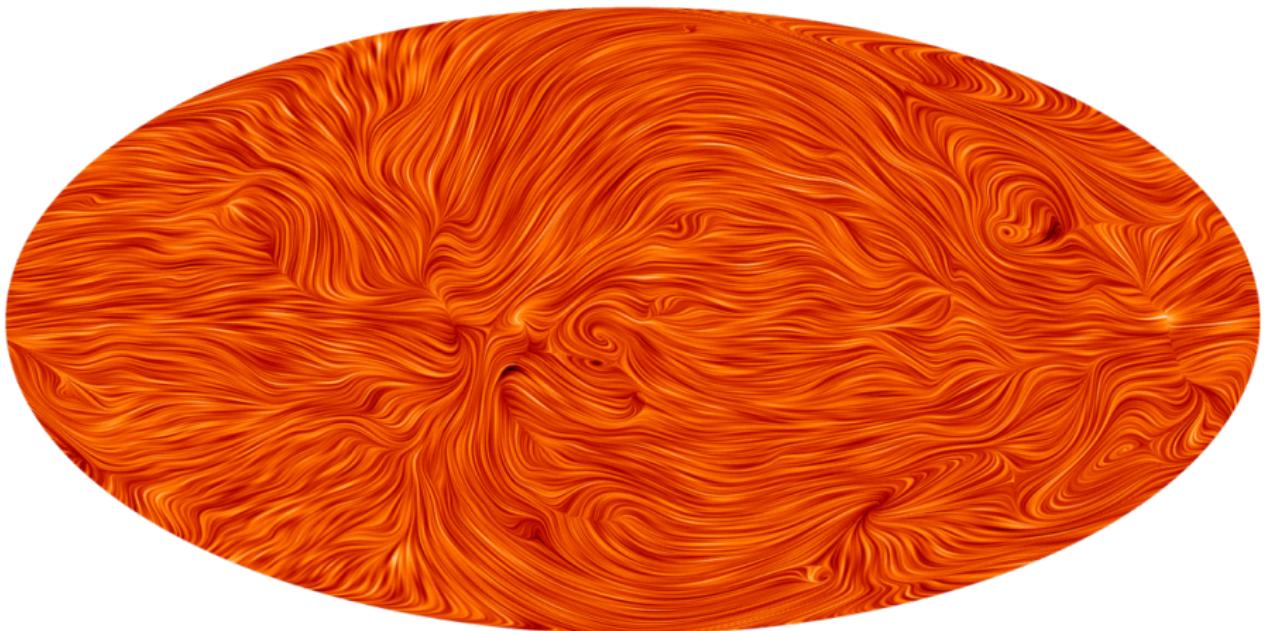
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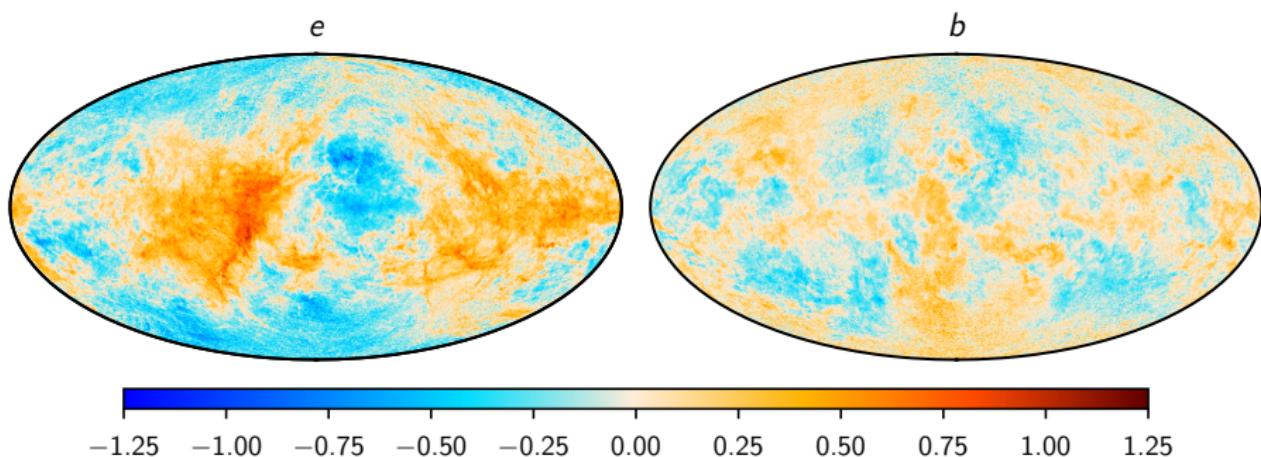
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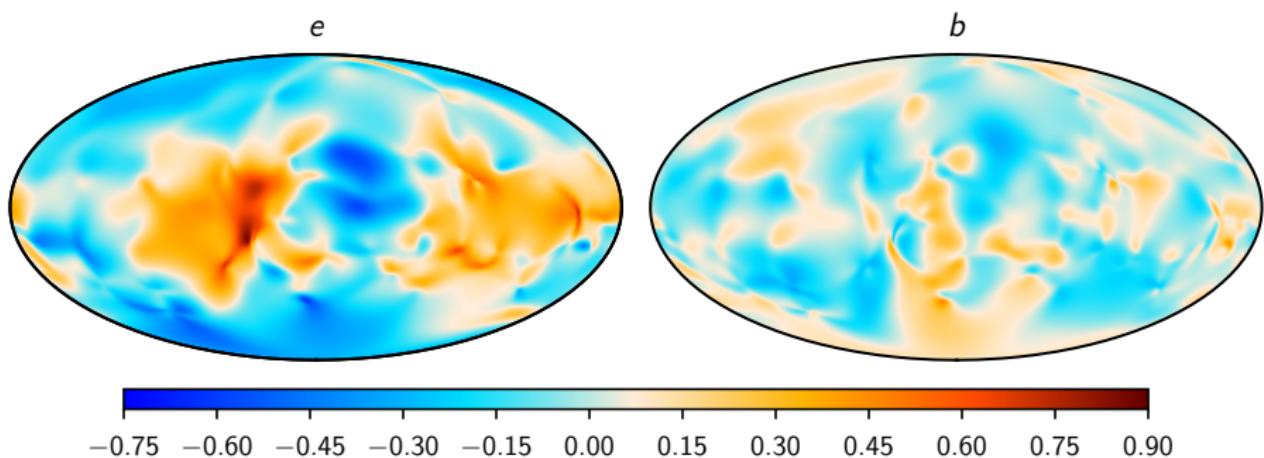
Reconstructed Polarization Fraction

- Sky
- Large Scale Component
- Random Component



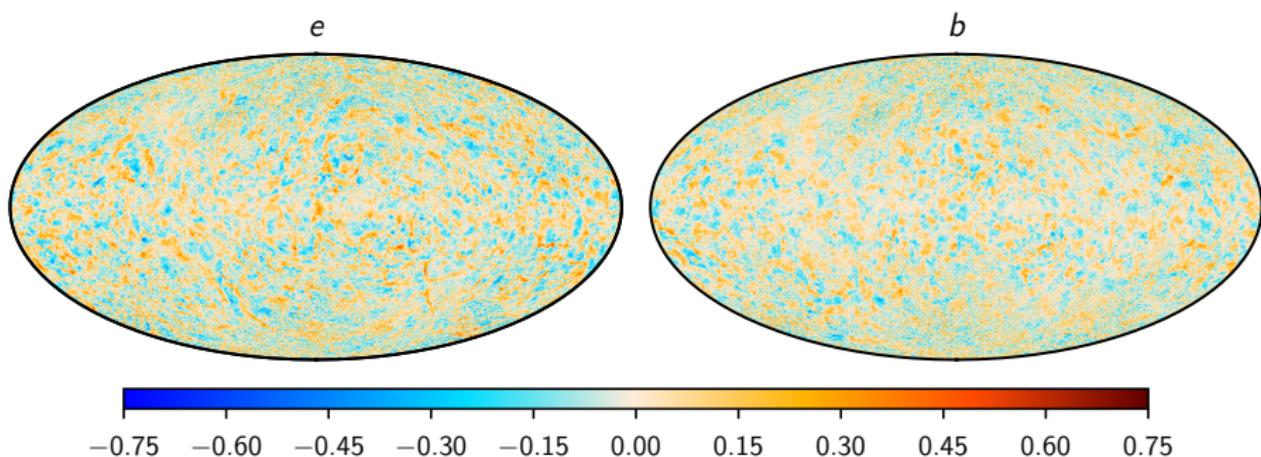
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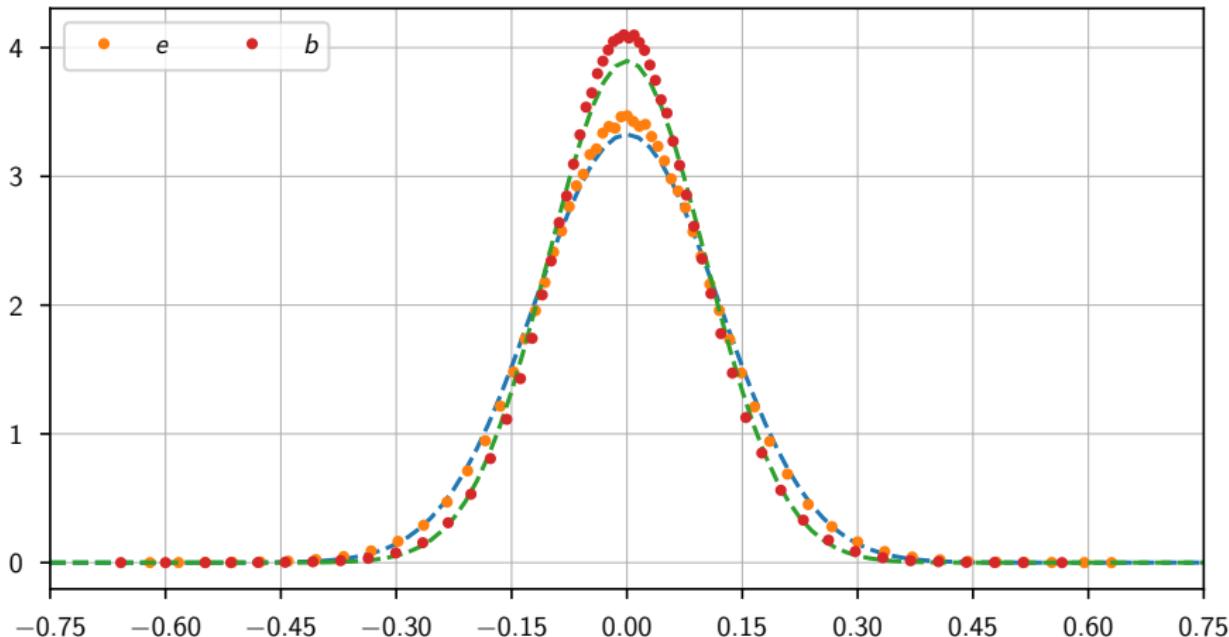
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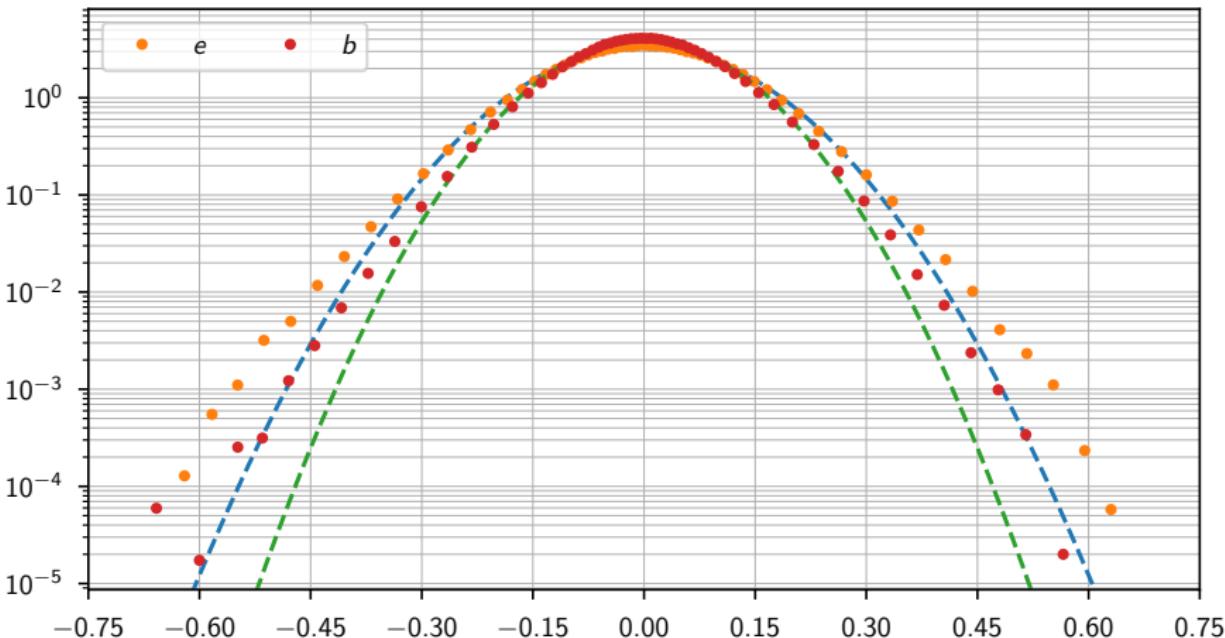
Random Residual is Quite Gaussian

- 1-point PDF
- Tails
- Local non-Gaussianity corrected



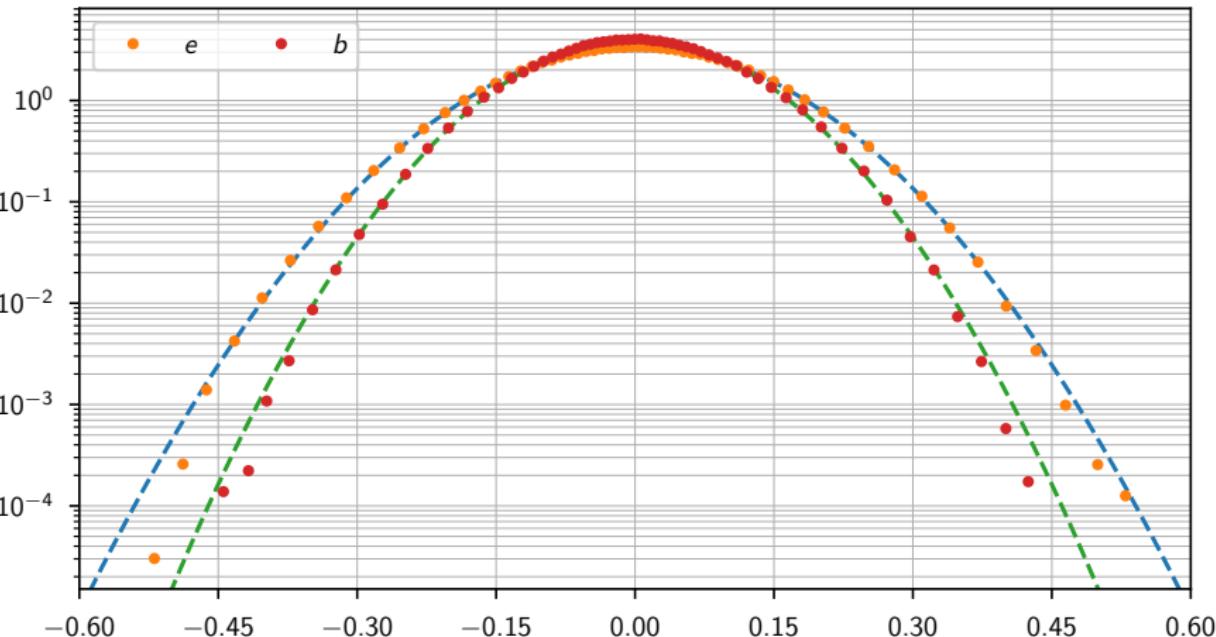
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- Tails
- Local non-Gaussianity corrected

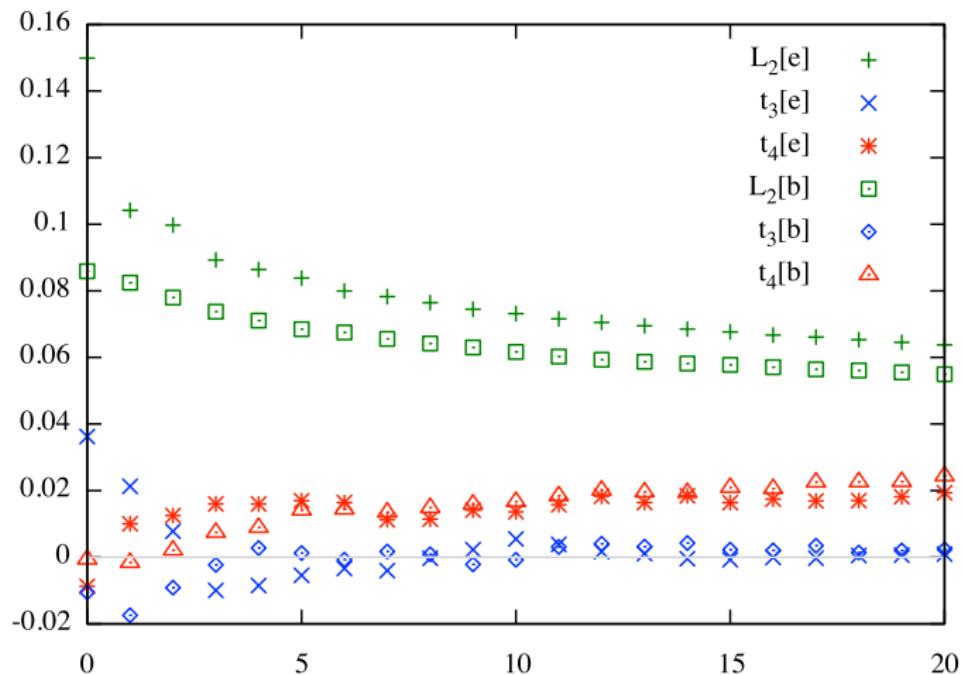


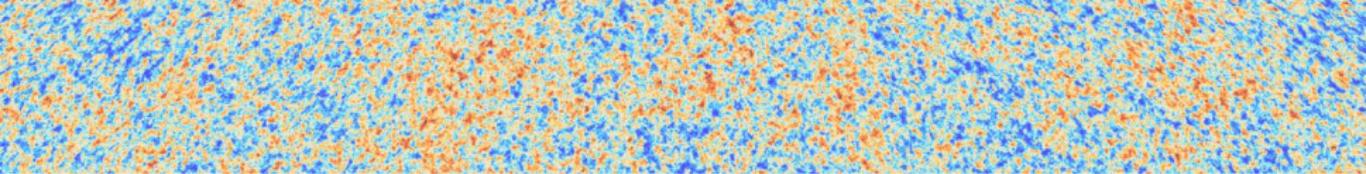
Random Residual is Quite Gaussian

- 1-point PDF ◦ Tails ◦ Local non-Gaussianity corrected ◦



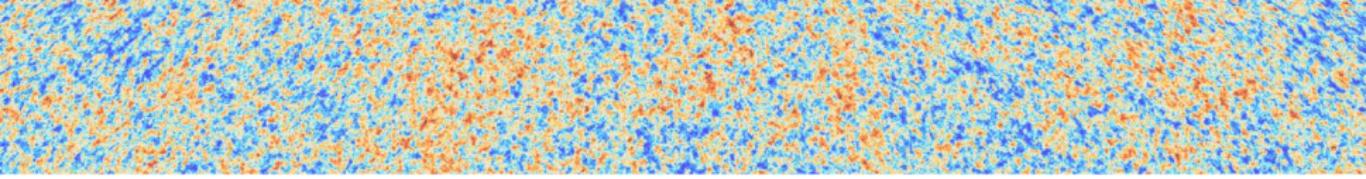
Where to Stop?





Polarized Dust Emission is Actually Very Simple!

Model It!

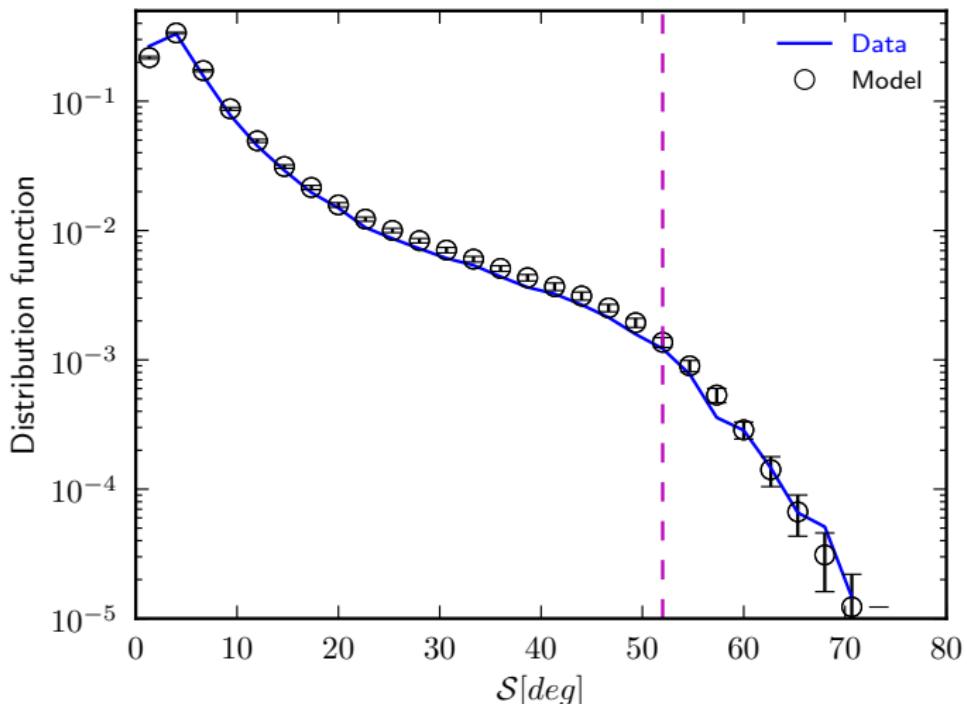


Polarized Dust Emission is
Actually Very Simple!

Model It!

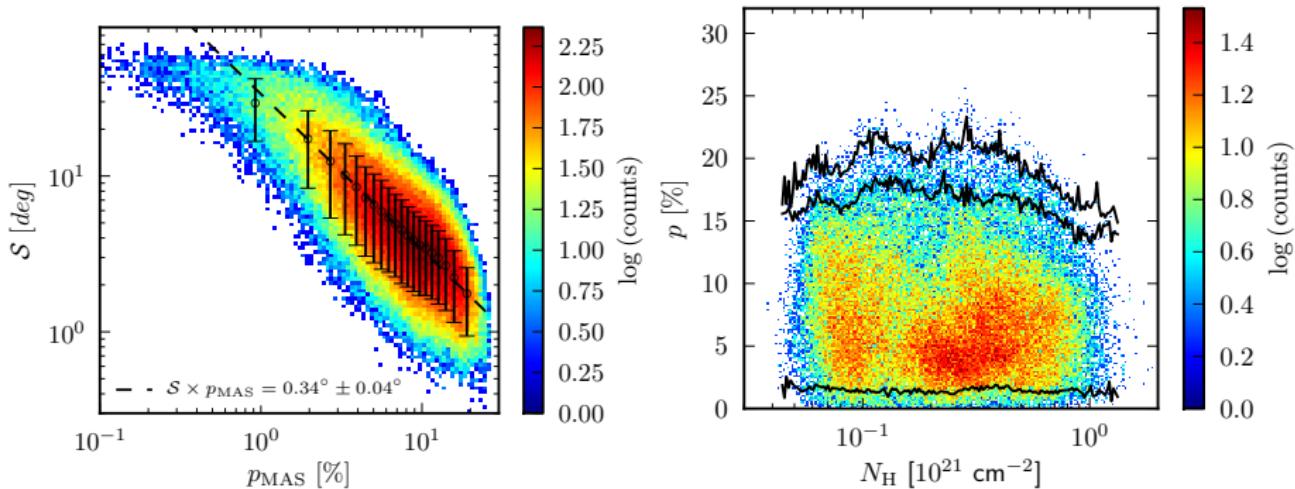
Random Realizations Reproduce Sky Statistics

- Polarization Angle Dispersion ◦ Sky Correlations ◦ Random Realization ◦



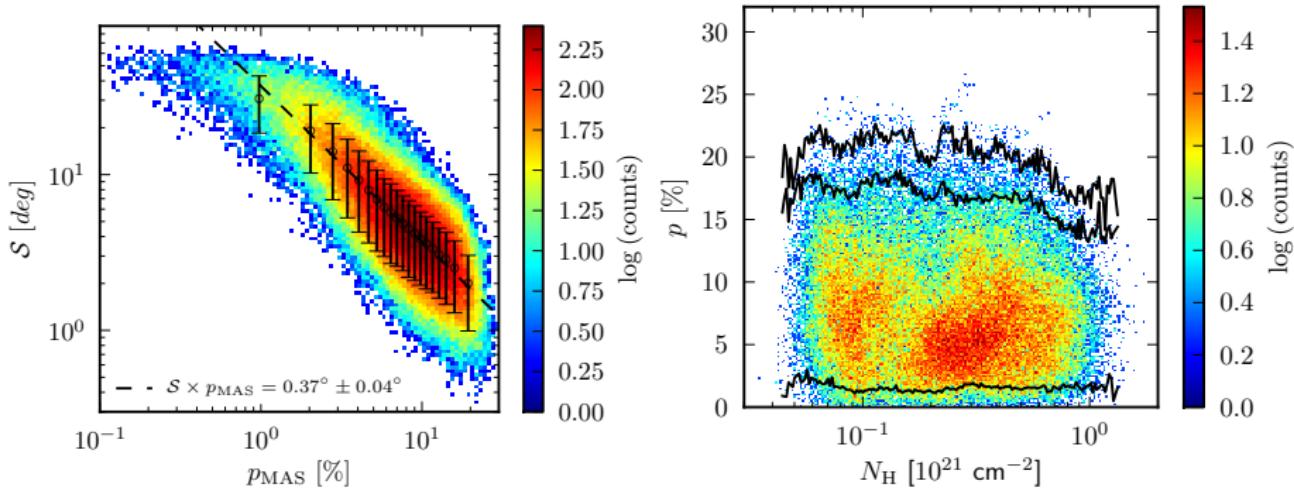
Random Realizations Reproduce Sky Statistics

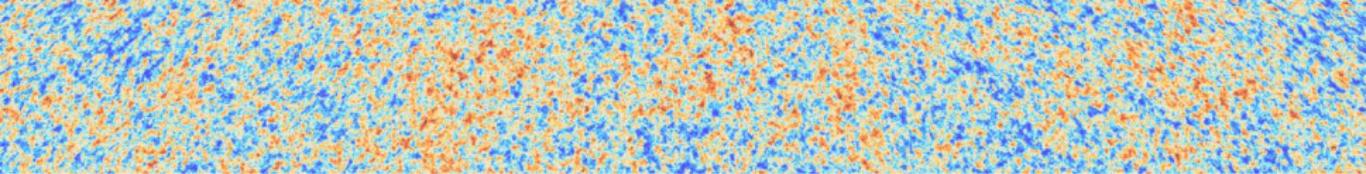
- Polarization Angle Dispersion ◦ Sky Correlations ◦ Random Realization ◦



Random Realizations Reproduce Sky Statistics

- Polarization Angle Dispersion ◦ Sky Correlations ◦ Random Realization ◦



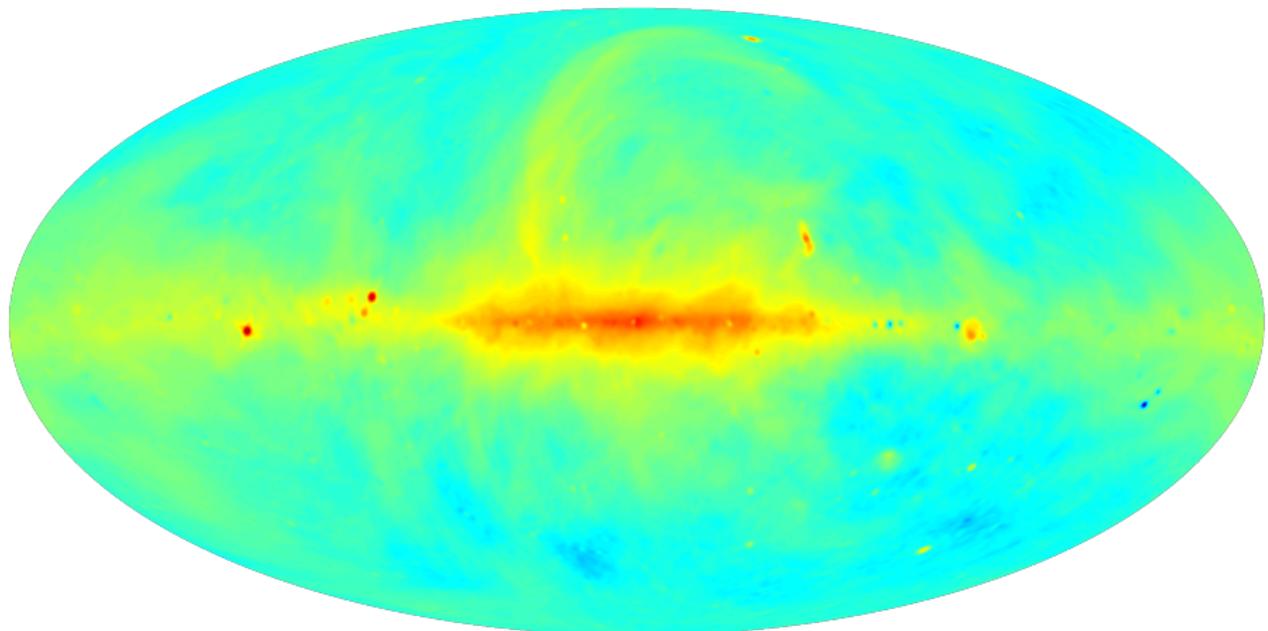


Modelling Synchrotron Emission

Polarization Fraction Tensor

[Synchrotron]

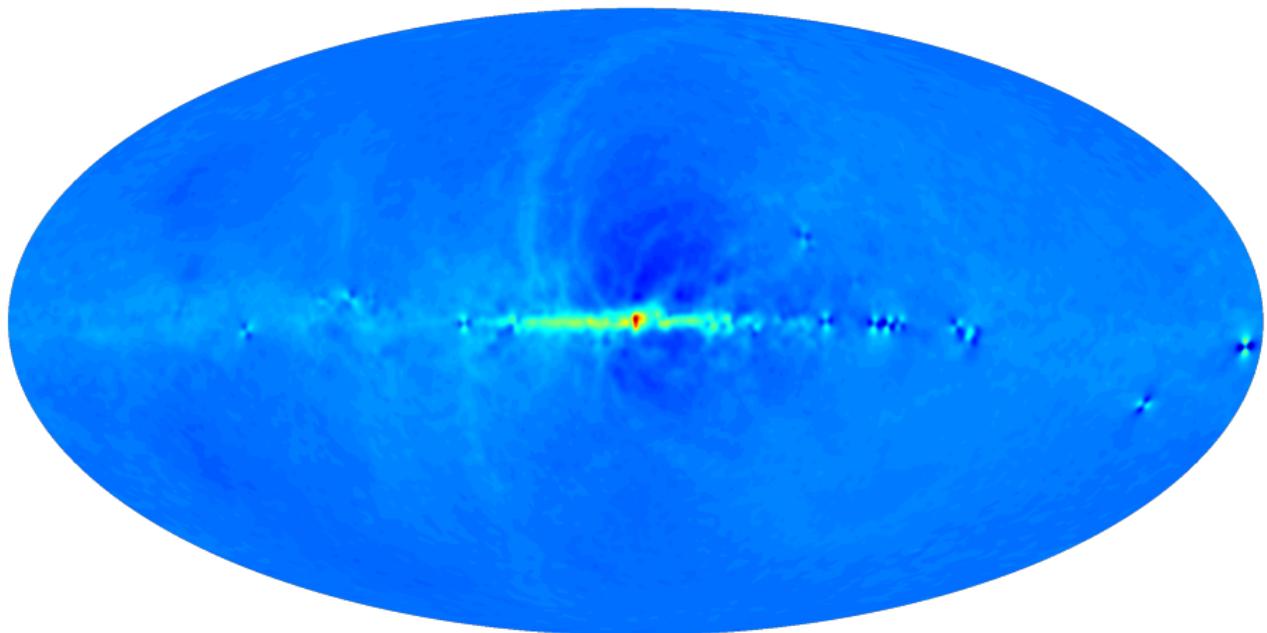
- In ◦ E ◦ B ◦ i ◦ e ◦ b ◦



Polarization Fraction Tensor

[Synchrotron]

◦ In I ◦ E ◦ B ◦ i ◦ e ◦ b ◦

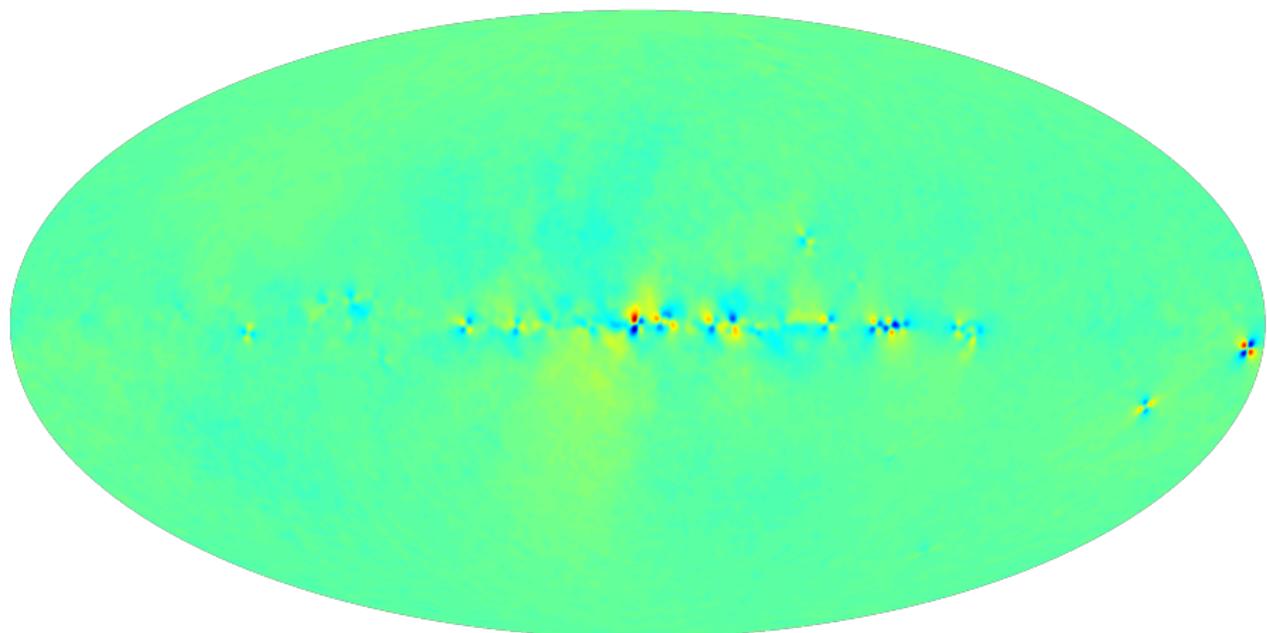


-20% +50%

Polarization Fraction Tensor

[Synchrotron]

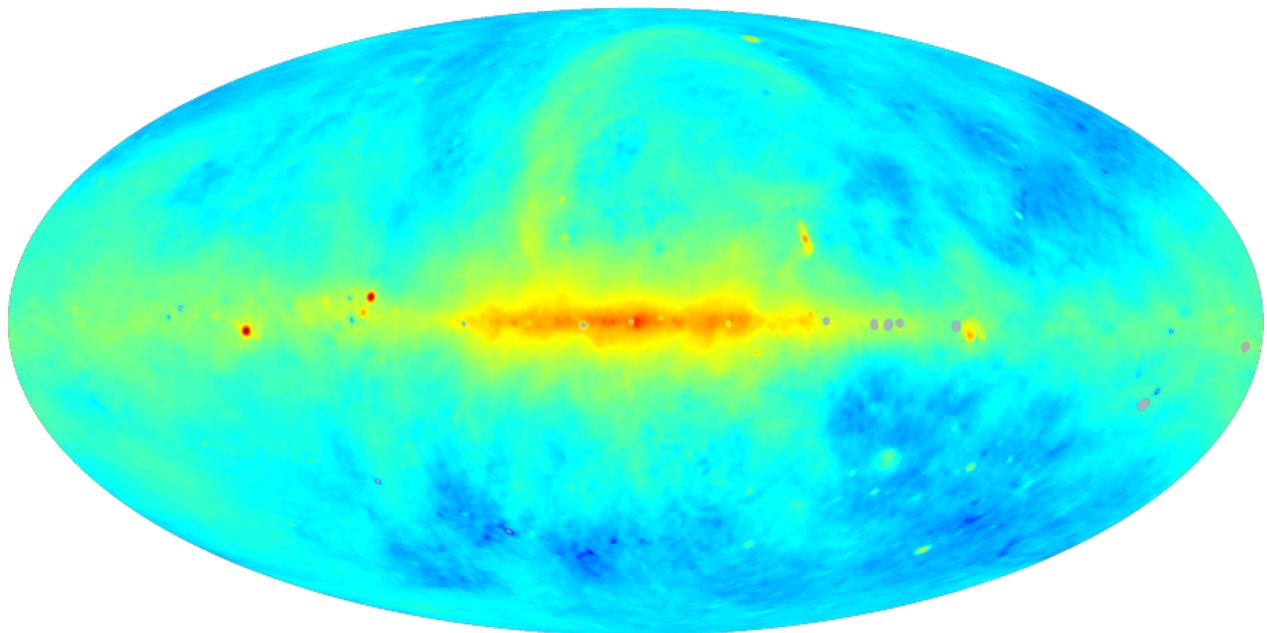
• In I • E • B • i • e • b •



Polarization Fraction Tensor

[Synchrotron]

- In I • E • B • i • e • b

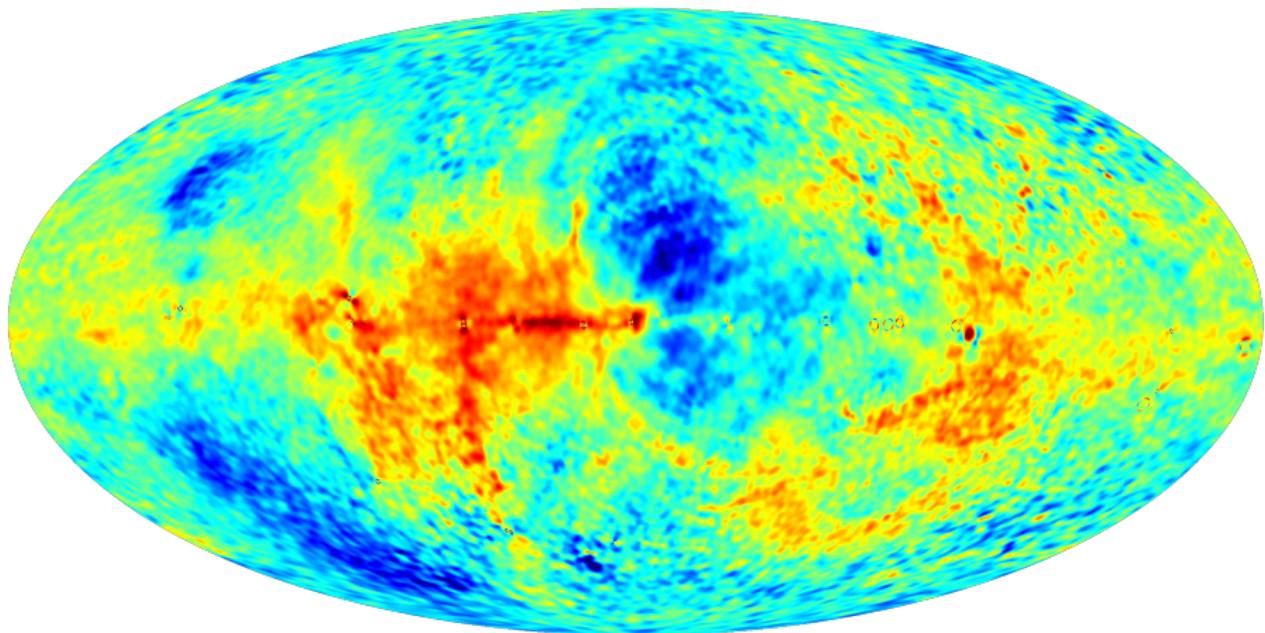


-0.104 +0.14

Polarization Fraction Tensor

[Synchrotron]

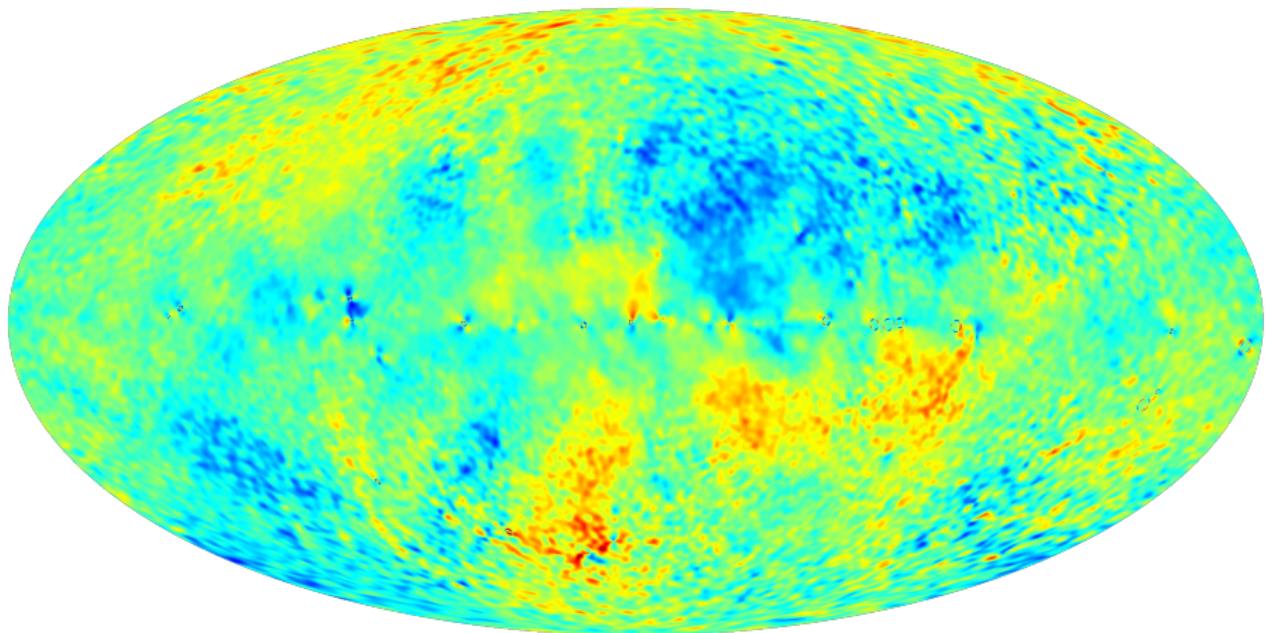
- In I • E • B • i • e • b



Polarization Fraction Tensor

[Synchrotron]

- In I • E • B • i • e • b



Synchrotron Polarization

Rybicki & Lightman (1979)

$$P_{\perp}(\omega) = \frac{\sqrt{3}}{4\pi} \frac{q^3 B_{\perp}}{mc^2} [F(x) + G(x)]$$

$$P_{\parallel}(\omega) = \frac{\sqrt{3}}{4\pi} \frac{q^3 B_{\perp}}{mc^2} [F(x) - G(x)]$$

$$F(x) = x \int_x^{\infty} K_{\frac{5}{3}}(\xi) d\xi, \quad G(x) = x K_{\frac{2}{3}}(x), \quad x = \frac{\omega}{\omega_c}$$

$$\omega_c = \frac{3}{2} \frac{q B_{\perp}}{m c} \gamma^2$$

Synchrotron Polarization

Rybicki & Lightman (1979)

$$N(\gamma)d\gamma \propto \gamma^{-p}d\gamma$$

$$P \propto \frac{q^3 B_\perp}{mc^2} \left(\frac{qB_\perp}{mc\omega} \right)^{\frac{1}{2}(p-1)}$$

$$\Pi(\omega) = \frac{P_\perp(\omega) - P_{\parallel}(\omega)}{P_\perp(\omega) + P_{\parallel}(\omega)} = \frac{G(x)}{F(x)} \quad \longrightarrow \quad \Pi = \frac{p+1}{p+\frac{7}{3}}$$

But polarization fraction varies on the sky!

Synchrotron Polarization

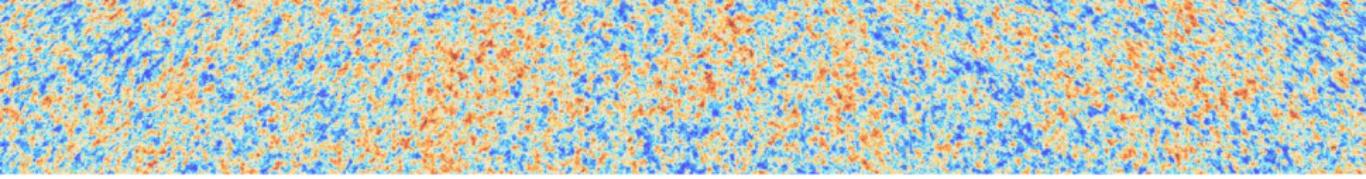
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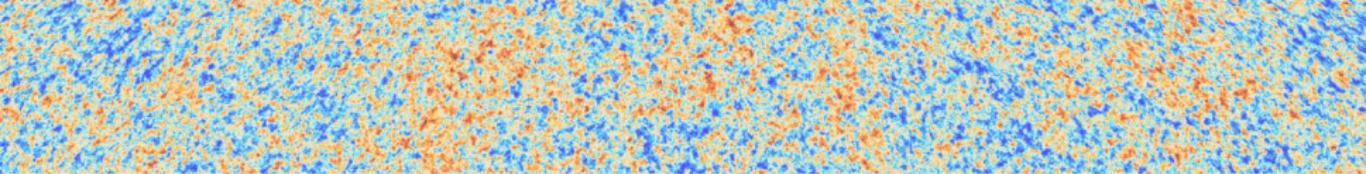
But polarization fraction varies on the sky!



What are we looking at here?

Spatial dependence of
spectral index?

And why is it correlated to
magnetic features?



– The End –