

Probing heavy neutral leptons in the ν MSM

Shintaro Eijima (KEK)

Based on:

- JHEP07(2019)077 [SE, M. Shaposhnikov, I. Timiryasov]
- ArXiv:1902.04535 [I. Boiarska, K. Bondarenko, A. Boyarsky, SE, M. Ovchynnikov, O. Ruchayskiy, I. Timiryasov]

22nd New Physics Forum, Dec. 13, 2019
@ Kavli IPMU, University of Tokyo

Physics of right-handed neutrinos

Right-handed neutrinos can explain phenomena beyond the Standard Model (SM).

$$\mathcal{L} = \mathcal{L}_{SM} + i\bar{\nu}_{RI}\gamma^\mu\partial_\mu\nu_{RI} - F_{\alpha I}\bar{L}_\alpha\tilde{\Phi}\nu_{RI} - \frac{[M_M]_I}{2}\bar{\nu}_{RI}^c\nu_{RI} + h.c.$$

1. Seesaw mechanism
→ Neutrino oscillations
2. Leptogenesis
→ Baryon Asymmetry
of the Universe (BAU)
3. Dark Matter (DM)
→ Sterile neutrino
4. ...

Neutrino Minimal Standard Model (ν MSM)

[Asaka, Shaposhnikov ('05)] [Asaka, Blanchet, Shaposhnikov ('05)]

Right-handed neutrinos **with masses below the electroweak scale, ~ 100 GeV**, can explain phenomena beyond the Standard Model (SM) and be probed experimentally.

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- | | |
|--|---|
| 1. Seesaw mechanism
→ Neutrino oscillations | Heavy Neutral Leptons (HNLs)
with $M = \mathcal{O}(1\text{-}10)$ GeV |
| 2. Leptogenesis
→ Baryon Asymmetry
of the Universe (BAU) | Search for long-lived particles
$N_2 \ N_3$ |
| 3. Dark Matter (DM)
→ Sterile neutrino | with $M = \mathcal{O}(10)$ keV
X-ray obsearvations
N_1 |

Neutrino Minimal Standard Model (ν MSM)

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Goal of this work

We can probe origin of the puzzle of early Universe in laboratories!

Q1. Where should we explore for the leptogenesis?

1. Seesaw mechanism
→ Neutrino oscillations

Heavy Neutral Leptons (HNLs)
with $M = \mathcal{O}(1\text{-}10)$ GeV

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Q2. How can we probe the HNLs experimentally?

Contents

In this talk I show a parameter space of HNLs for the successful BAU and how it will be tested in experiments.

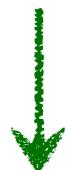
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Seesaw mechanism for HNLs

[Minkowski ('77)][Yanagida ('79)][Gell-Mann, Ramond, Slansky ('79)][Glashow ('79)][Mohapatra, Senjanovic ('79)]

Seesaw mechanism suggests couplings of HNLs are suppressed.

$$\mathcal{L}_M = [M_D]_{\alpha I} \bar{\nu}_{L\alpha} \nu_{R I} + \frac{[M_M]_I}{2} \bar{\nu}_{R I}^c \nu_{R I} + h.c. \quad [M_D]_{\alpha I} \equiv \langle \Phi \rangle F_{\alpha I}$$



To mass basis under $|M_D| \ll M_M$

$$\mathcal{L}_M \simeq \frac{[m_\nu]_i}{2} \bar{\nu}_i \nu_i^c + \frac{[M_N]_I}{2} \bar{N}_I^c N_I + h.c. \quad M_N \simeq M_M$$

$$[m_\nu]_i = - U_{PMNS}^\dagger [M_D M_M^{-1} M_D^T] U_{PMNS}^* = - \langle \Phi \rangle^2 U_{PMNS}^\dagger [F M_M^{-1} F^T] U_{PMNS}^*$$

$$\Delta m_{atm}^2 \simeq 2.5 \times 10^{-3} \text{ eV}^2 \rightarrow m_\nu \sim 0.05 \text{ eV}$$

$$\longrightarrow \boxed{F \sim \sqrt{\frac{m_\nu M_N}{\langle \Phi \rangle^2}} \simeq 4 \times 10^{-8} \left(\frac{M_N}{\text{GeV}} \right)^{\frac{1}{2}}}$$

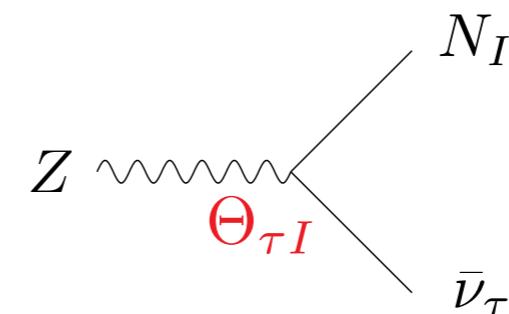
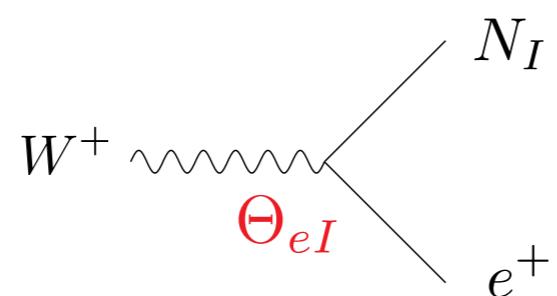
Interaction of HNLs

HNLs interact with SM particles as ordinary neutrinos through active-sterile mixing.

$$\rightarrow \nu_{L\alpha} = [U_{PMNS}]_{\alpha i} \nu_i + \Theta_{\alpha I} N_I^c$$

$$\Theta_{\alpha I} \equiv \frac{[M_D]_{\alpha I}}{M_N} = \frac{\langle \Phi \rangle F_{\alpha I}}{M_N} \sim 7 \times 10^{-6} \left(\frac{\text{GeV}}{M_N} \right)^{\frac{1}{2}}$$

Weak interaction with $\Theta_{\alpha I}$



Long-lived particle

$$\Gamma(N \rightarrow 3\nu) = \frac{G_F^2 M_N^5}{192\pi^3} \sum_{\alpha} |\Theta_{\alpha}|^2$$

$$\rightarrow \tau_N \sim 1 \text{ sec} \left(\frac{\text{GeV}}{M_N} \right)^4$$

$$\Gamma(N \rightarrow \pi^+ e^-) \simeq \frac{G_F^2}{16\pi} |\Theta_e|^2 |V_{ud}|^2 f_\pi^2 M_N^3$$

$$\rightarrow \tau_N \sim 0.1 \text{ sec} \left(\frac{\text{GeV}}{M_N} \right)^2$$

Yukawa couplings for ν oscillation measurements

Neutrino oscillation measurements determine structure of the Yukawa couplings.

$$\Delta m_{atm}^2 \simeq 2.5 \times 10^{-3} \text{ eV}^2 \text{ and } \Delta m_{sol}^2 \simeq 7.4 \times 10^{-5} \text{ eV}^2 \longrightarrow \mathbf{N}_{\nu_R} \geq 2$$

$$[m_\nu]_i = - \langle \Phi \rangle^2 U_{PMNS}^\dagger [F M_M^{-1} F^T] U_{PMNS}^*$$

$$\rightarrow F = \frac{i}{\langle \Phi \rangle} U_{PMNS} m_\nu^{\frac{1}{2}} \Omega M_N^{\frac{1}{2}} \quad (\text{3x2 matrix})$$

[Casas, Ibarra ('01)]

$$\Delta m^2, \theta_{ij}, \delta, \eta$$

Flavor structure;

$$|F_e| : |F_\mu| : |F_\tau|$$

$$\Omega = \begin{pmatrix} 0 & 0 \\ \cos \omega & \sin \omega \\ -\sin \omega & \cos \omega \end{pmatrix} \quad (\Omega \Omega^T = 1) \quad \text{Enhancement; } F \propto e^{i \text{Im} \omega} \text{ or } e^{-i \text{Im} \omega}$$
$$\cos(i \text{Im} \omega) = (e^{i \text{Im} \omega} + e^{-i \text{Im} \omega})/2 \quad \sin(i \text{Im} \omega) = i(e^{i \text{Im} \omega} - e^{-i \text{Im} \omega})/2$$

- Flavor components of F_α (and Θ_α) are not independent.
- Seesaw puts only the lower boundary on $|F_\alpha|$ (and $|\Theta_\alpha|$)

Yukawa couplings for ν oscillation measurements

Neutrino oscillation measurements determine structure of the Yukawa couplings.

$$\Delta m^2 \sim 2.5 \times 10^{-3} \text{ eV}^2 \text{ and } \Delta m^2 \sim 7.4 \times 10^{-5} \text{ eV}^2 \rightarrow N_\nu > 2$$

The upper boundary on $|\Theta_\alpha|$ ($\propto |F_\alpha|$) is a necessary criterion for experimental searches.

Q1. Where should we explore for the leptogenesis?

→ How large is the upper boundary from the leptogenesis?

$$(\text{NH}) \begin{pmatrix} \cos \omega & \sin \omega \\ -\sin \omega & \cos \omega \end{pmatrix} (\Omega \Omega^T = 1) \text{ Enhancement; } F \propto e^{i \text{Im} \omega} \text{ or } e^{-i \text{Im} \omega}$$

- Flavor components of F_α (and Θ_α) are not independent.
- Seesaw puts only the lower boundary on $|F_\alpha|$ (and $|\Theta_\alpha|$)

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Baryogenesis with HNLs

Deviation from equilibrium can be satisfied due to the smallness of Yukawa interaction.

Observed BAU

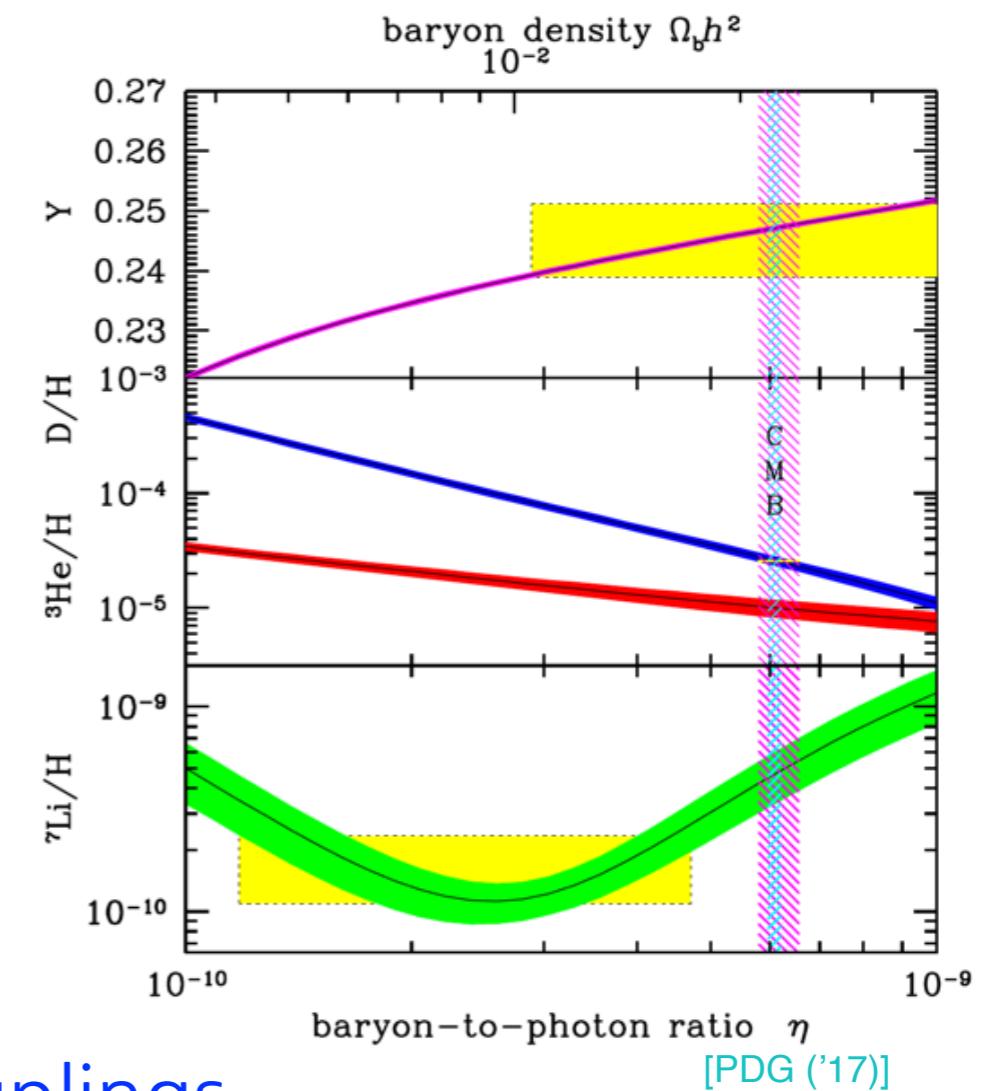
$$Y_B^{obs} = (0.872 \pm 0.004) \times 10^{-10}$$

[Planck collaboration ('18)]

$$Y_B \equiv \frac{n_b - n_{\bar{b}}}{s}$$

Sakharov conditions

1. B violation
Anomalous violation (Sphaleron)
2. C and CP violation
 CP violation in neutrino Yukawa couplings
3. Deviation from equilibrium
Decoupled due to the feeble Yukawa interaction



[PDG ('17)]

Leptogenesis with HNLs

Baryon asymmetry is generated by conversion from lepton asymmetry through sphaleron process.

Sphaleron process ; anomalous B violating process at high T

$$B(T_{sph}) \simeq \frac{28}{79} [B - L](T_{sph})$$

[Khlebnikov, Shaposhnikov('88)]



From BSM ($RH\nu$)

Lepton asymmetry production

$$T_{sph} \approx 130 \text{ GeV} \longrightarrow M_N \ll T \longrightarrow$$

[D'Onofrio, Rummukainen, Tranberg ('14)]

- Decay is irrelevant
- Lepton number is preserved effectively

→ Key dynamics

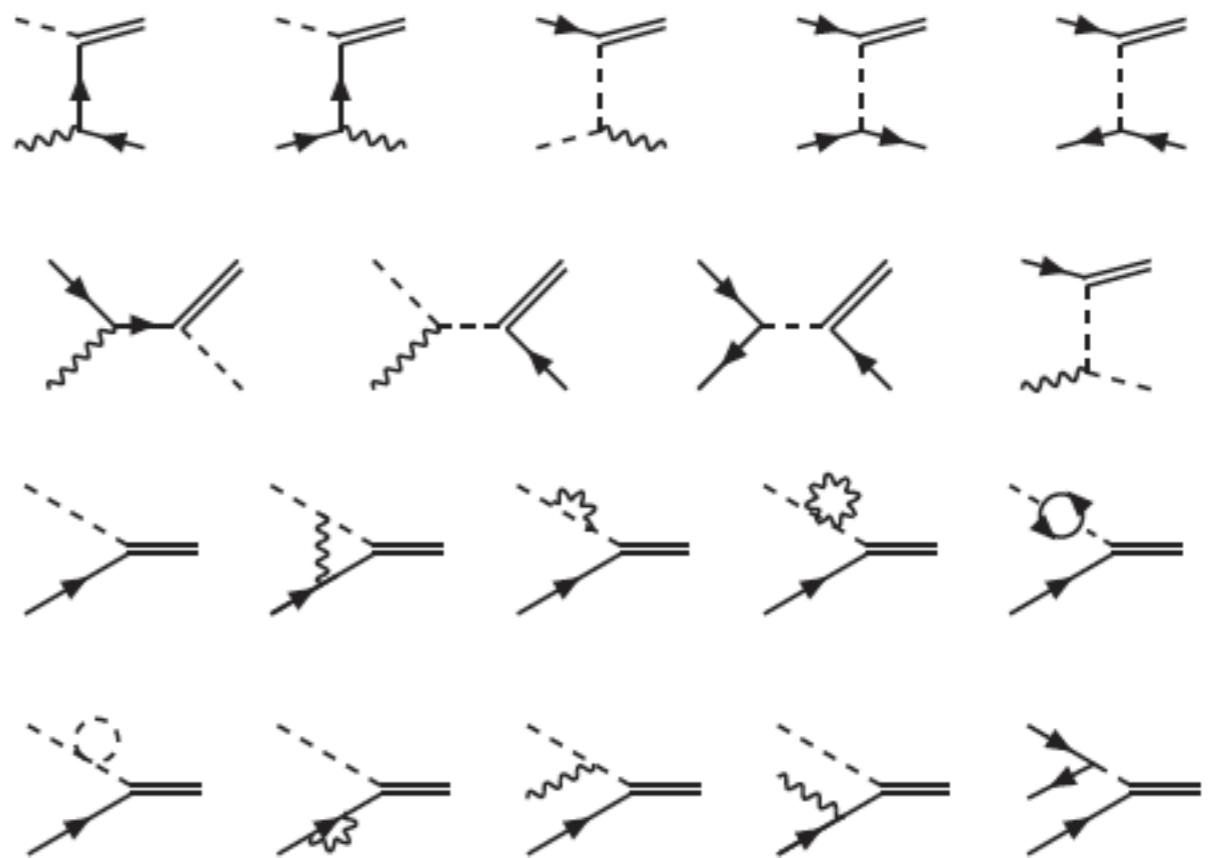
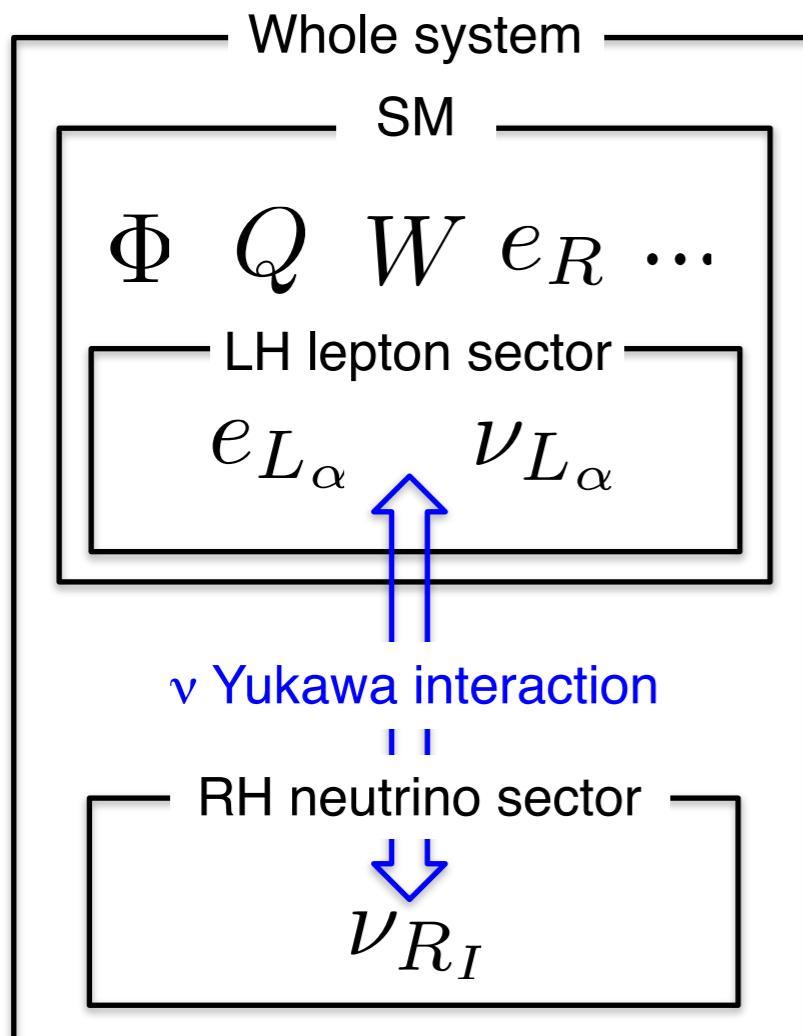
- Right-handed neutrino oscillation
- Separation of lepton asymmetry

Baryogenesis via $RH\nu$ oscillation [1]

[Akhmedov, Rubakov, Smirnov ('98)] [Asaka, Shaposhnikov ('05)]

$RH\nu$ (anti- $RH\nu$) are produced through the Yukawa interaction

$RH\nu$ production



[Ghisoiu, Laine ('14)]

$$\Gamma_N \simeq 0.01[F^\dagger F]T \quad \text{for } T > T_{EW}$$

[Ghilieri, Laine ('17)]

Baryogenesis via RH ν oscillation [2]

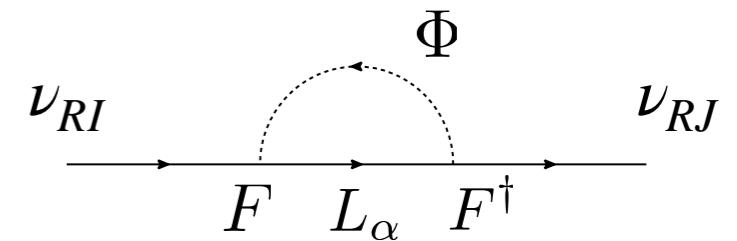
[Akhmedov, Rubakov, Smirnov ('98)] [Asaka, Shaposhnikov ('05)]

RH ν s start to oscillate at “oscillation temperature”, T_{osc} .

$$H_N = H_0 + H_I$$

$$H_0 \simeq \text{diag} \left(\frac{M_1^2}{2p}, \frac{M_2^2}{2p} \right)$$

$$H_I = [F^\dagger F] \frac{T^2}{8p}$$



$$\nu_{RI} \quad \text{Oscillations of } \nu_R \quad \nu_{RJ}$$

$$e^{-i \left(\frac{M_I^2 - M_J^2}{2p} \right) dt}$$

$$\text{Hubble param.: } H = \frac{T^2}{M_0} \quad (M_0 = 7 \times 10^{17} \text{ GeV})$$

$\frac{M_I^2 - M_J^2}{2p} = H$ gives a temperature where the oscillation gets active.

$$\rightarrow T_{osc} \simeq (\Delta M M M_0)^{\frac{1}{3}} \simeq 10^3 \text{ GeV} \left(\frac{\Delta M}{10^{-8} \text{ GeV}} \right)^{\frac{1}{3}} \left(\frac{M}{1 \text{ GeV}} \right)^{\frac{1}{33}}$$

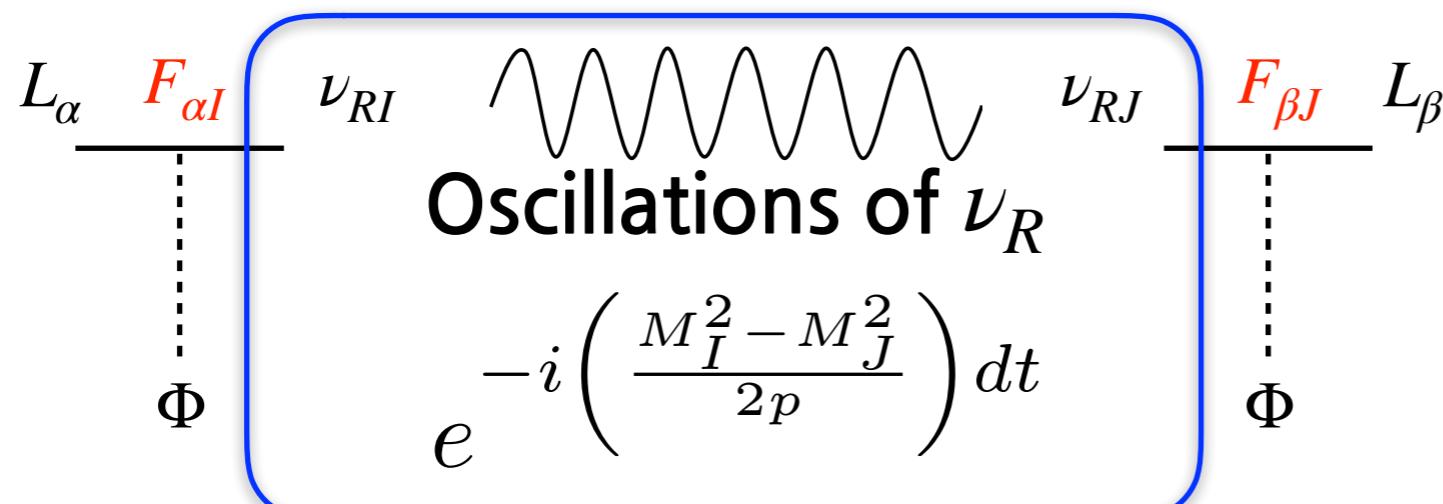
$$M = \frac{M_2 + M_1}{2} \quad \Delta M = \frac{M_2 - M_1}{2}$$

Baryogenesis via RH ν oscillation [3]

[Akhmedov, Rubakov, Smirnov ('98)] [Asaka, Shaposhnikov ('05)]

The oscillation of RH ν s affects flavor transition of active neutrinos,
 $L_\alpha \rightarrow L_\beta$.

CP violating flavor transition of active neutrinos



$$\begin{aligned}\Gamma(L_\alpha \rightarrow L_\beta) &\neq \Gamma(\bar{L}_\alpha \rightarrow \bar{L}_\beta) \\ \rightarrow n_{L_e} &\neq 0, n_{L_\mu} \neq 0, n_{L_\tau} \neq 0 \\ n_{L_e} + n_{L_\mu} + n_{L_\tau} &= 0\end{aligned}$$

Asymmetric param.:

$$\begin{aligned}A^a &= \text{Im}[F_{\alpha 2}[F^\dagger F]_{23} F_{\alpha 3}^\dagger] \\ &\neq 0\end{aligned}$$

$$n_{L_\alpha} \propto A^\alpha$$

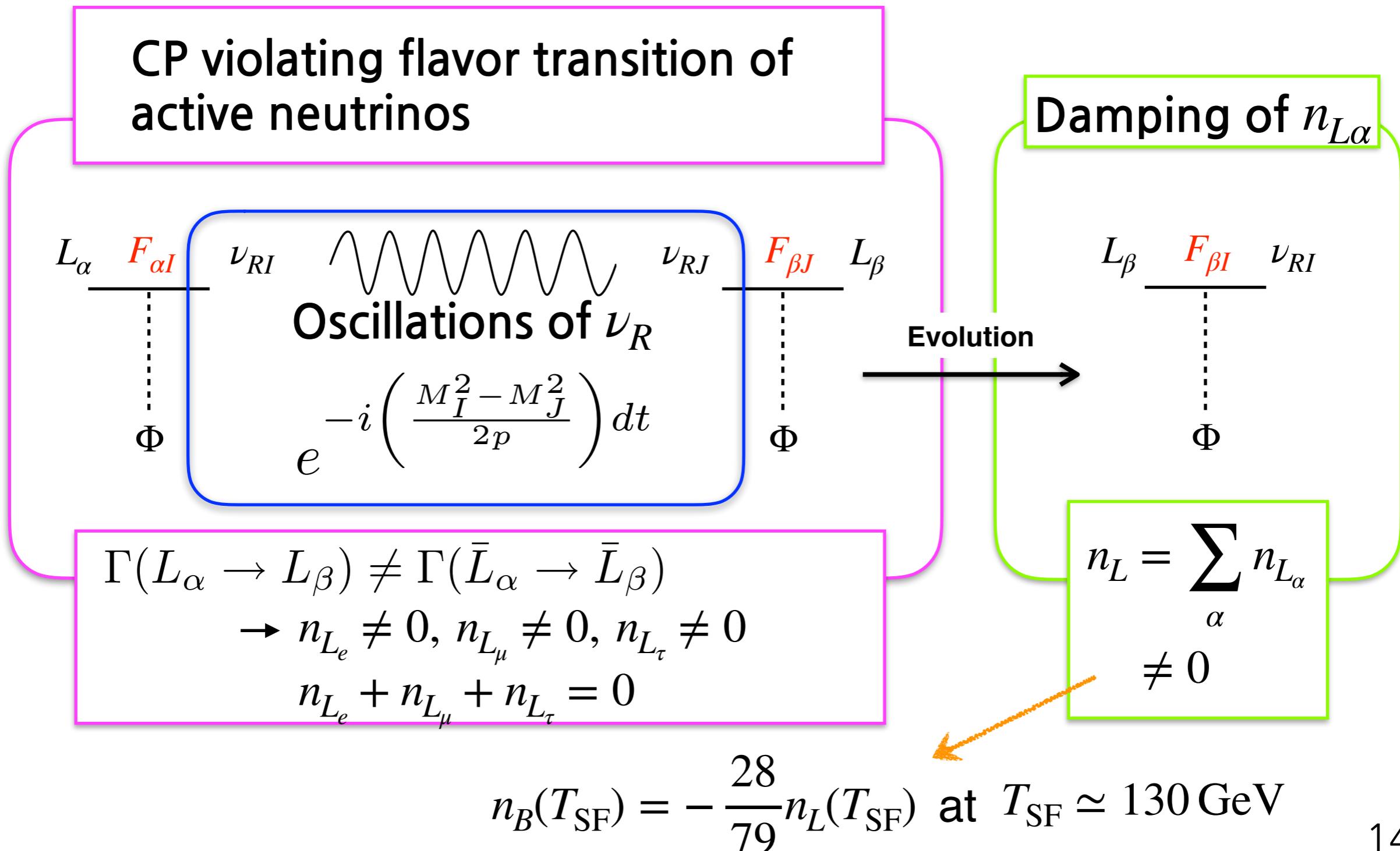
$$\sum_\alpha A^\alpha = 0$$

cf. CP violating ν oscillations; $P_{\nu_i \rightarrow \nu_j} - P_{\bar{\nu}_i \rightarrow \bar{\nu}_j} = \sum_{I>J} 4\Im[U_{iI}U_{jI}^*U_{iJ}^*U_{jJ}] \sin\left(\frac{\Delta m_{IJ}^2}{2E}L\right)$

Baryogenesis via RH ν oscillation [4]

[Akhmedov, Rubakov, Smirnov ('98)] [Asaka, Shaposhnikov ('05)]

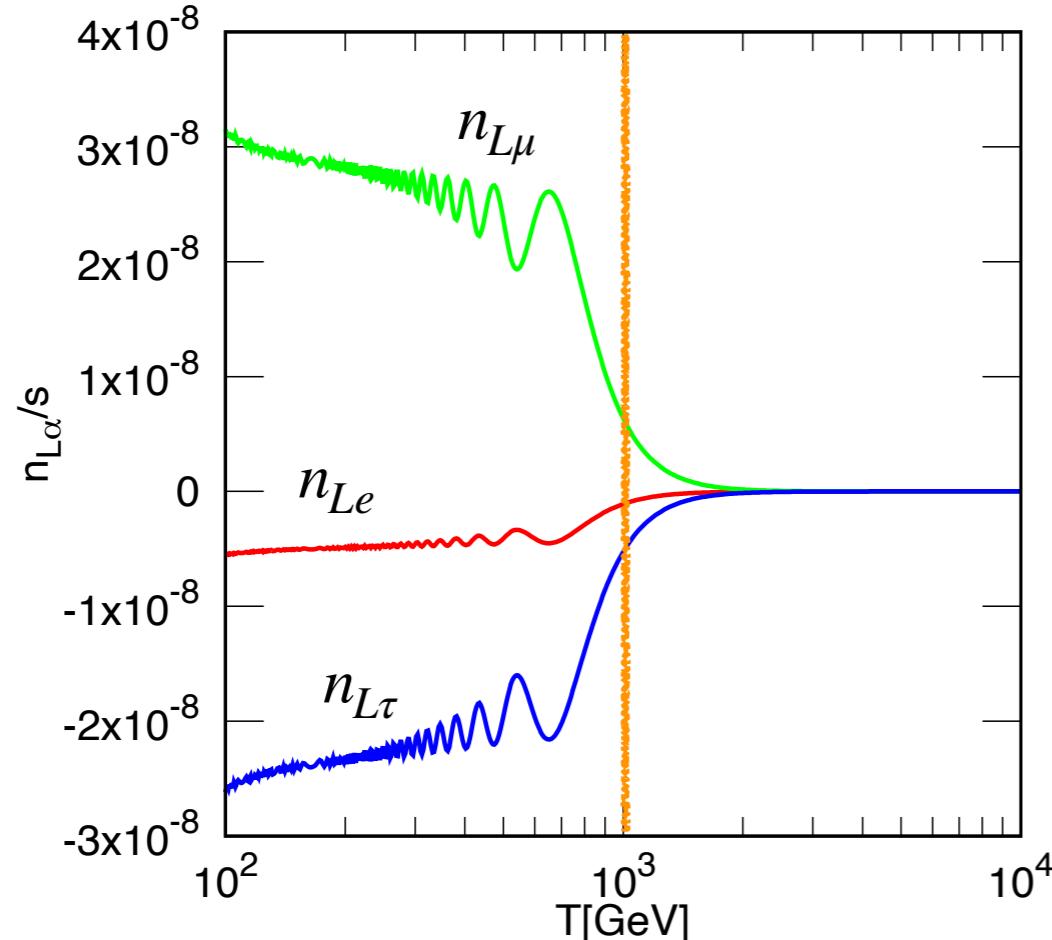
Net lepton asymmetry is produced in evolution with flavor difference in Yukawa couplings.



Evolution of asymmetries

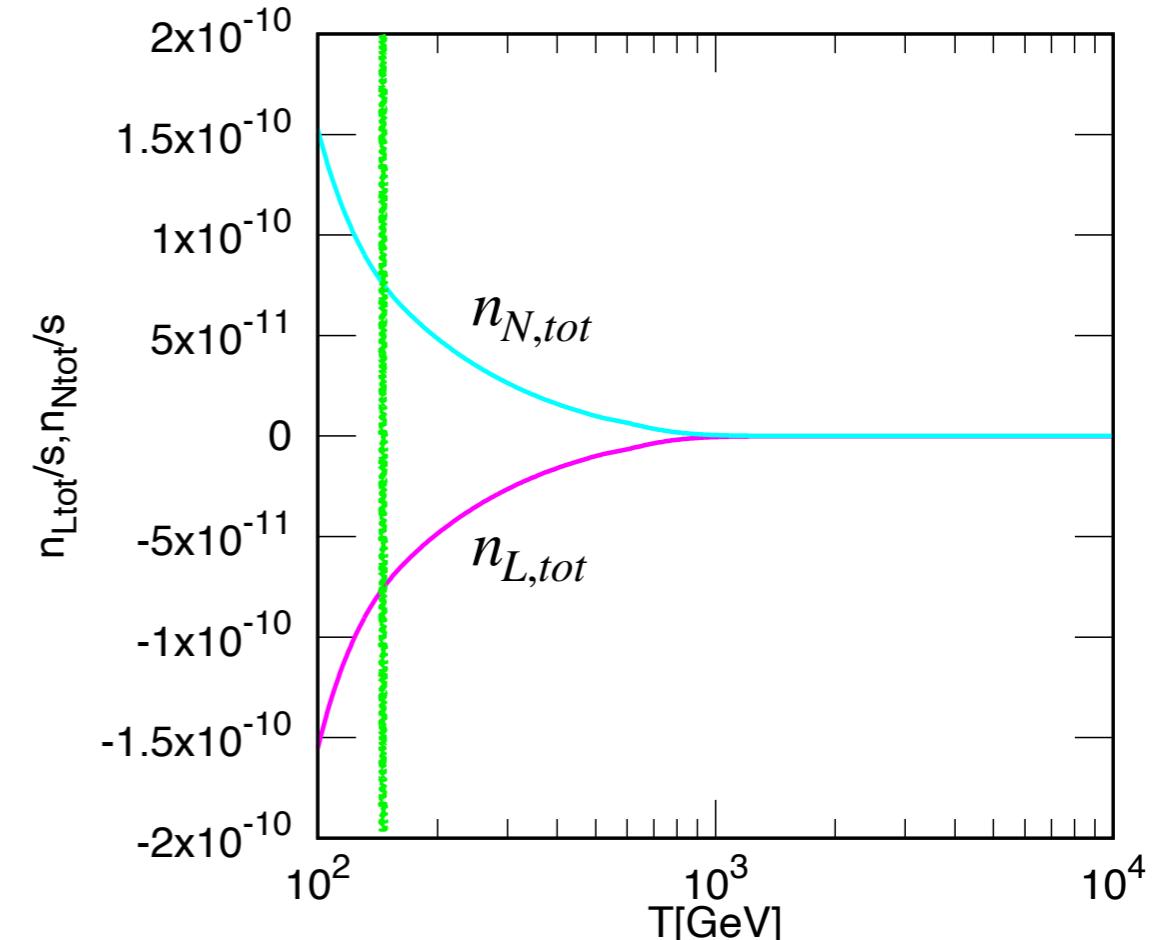
The evolution shows the feature clearly.

Flavor asymmetries



$T_{osc} \approx 10^3$ GeV
($M = 1$ GeV and $\Delta M = 5 \cdot 10^{-9}$ GeV)

Total asymmetry



- Lepton asymmetry separation
- Only $n_{L,tot}$ converts into n_B

Improvements of the leptogenesis

The leptogenesis has been studied actively in recent years and the upper boundaries on HNL mixing angles have been updated.

[Asaka, SE, Ishida ('12)] [Ghiglieri, Laine ('16,'17,'18)] [Hernandez, Kekic, Lopez-Pavon, Racker, Salvado ('16)] [Drewes, Garbrecht, Gueter, Klaric ('16)]
[Hambye, Teresi ('17)] [Asaka, SE, Ishida, Minogawa, Yoshii ('17)] [Antusch, Cazzato, Drewes, Fischer, Garbrecht, Gueter, Klaric ('17)]
[SE, Shaposhnikov ('17)] [SE, Shaposhnikov, Timiryasov ('17)]

Improvements of theoretical indication

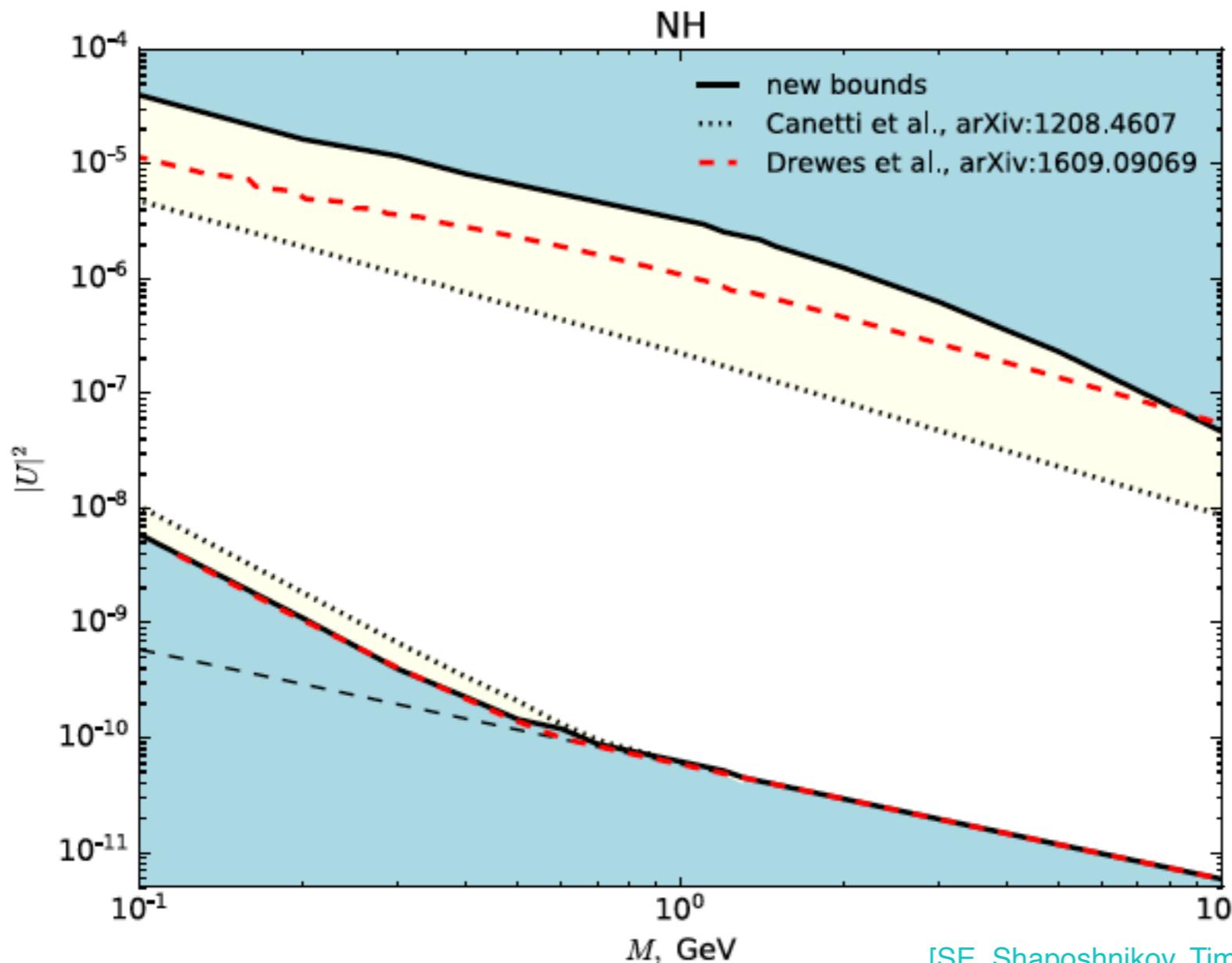
$$U^2 \equiv \sum_{\alpha, I} |\Theta_{\alpha I}|$$

2012 → 2016

$$\Gamma_N \approx 0.006 F^2 T \rightarrow \approx 0.01 F^2 T$$

2016 → 2018

- Lepton number violating effect
- Processes in the Higgs phase
- Plasma neutrality
- Exact treatment of sphaleron process
- ...



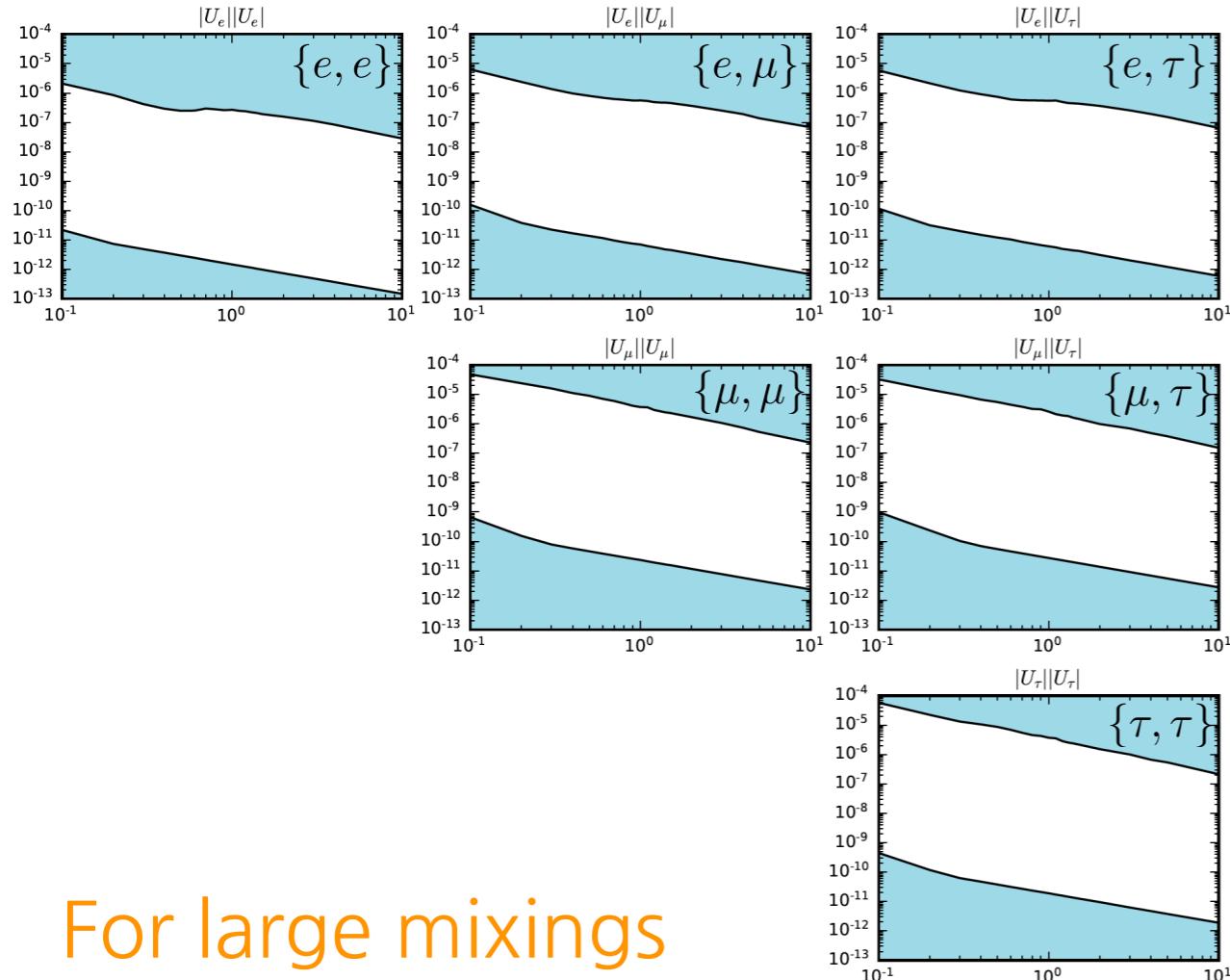
[SE, Shaposhnikov, Timiryasov ('18)]

Indication to experiments

Upper boundaries on individual mixings are evaluated from full parameter scanning.

Individual mixings

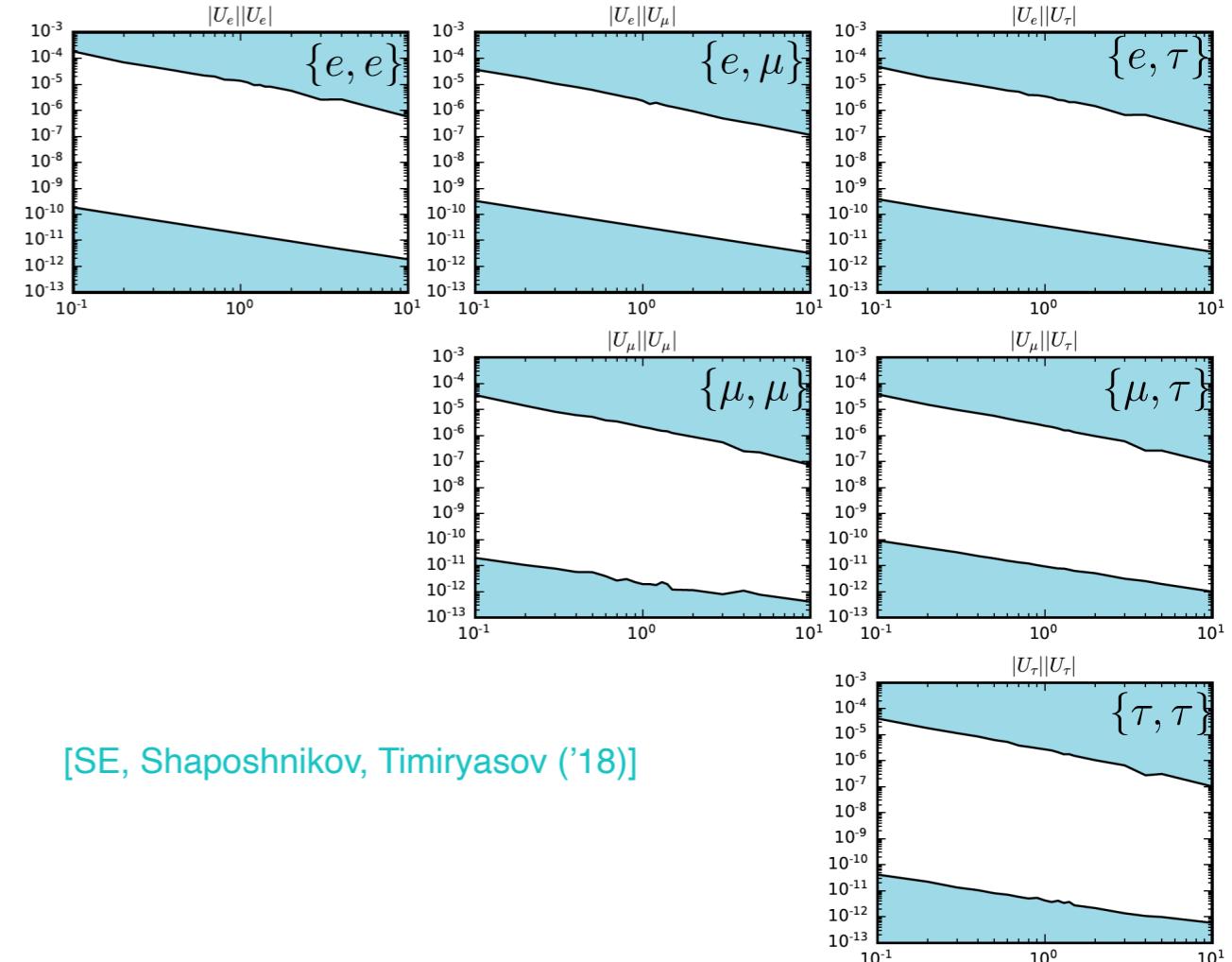
NH



$|U_\alpha| |U_\beta|$ with M_N

$$\sum_{I,J=1,2} |\Theta_{\alpha I}|^2 |\Theta_{\beta J}|^2 = |U_\alpha|^2 |U_\beta|^2$$

IH



[SE, Shaposhnikov, Timiryasov ('18)]

For large mixings

$$|\Theta_e|^2 \ll |\Theta_\mu|^2 \simeq |\Theta_\tau|^2 \quad \text{and} \quad \delta \sim \pi, \eta \sim 3\pi/2, \operatorname{Re}\omega \sim \pi/4 \quad (\text{NH})$$

$$|\Theta_e|^2 \gg |\Theta_\mu|^2 \simeq |\Theta_\tau|^2 \quad \text{and} \quad \delta \sim 0, \eta \sim \pi/2, \operatorname{Re}\omega \sim \pi/4 \quad (\text{IH})$$

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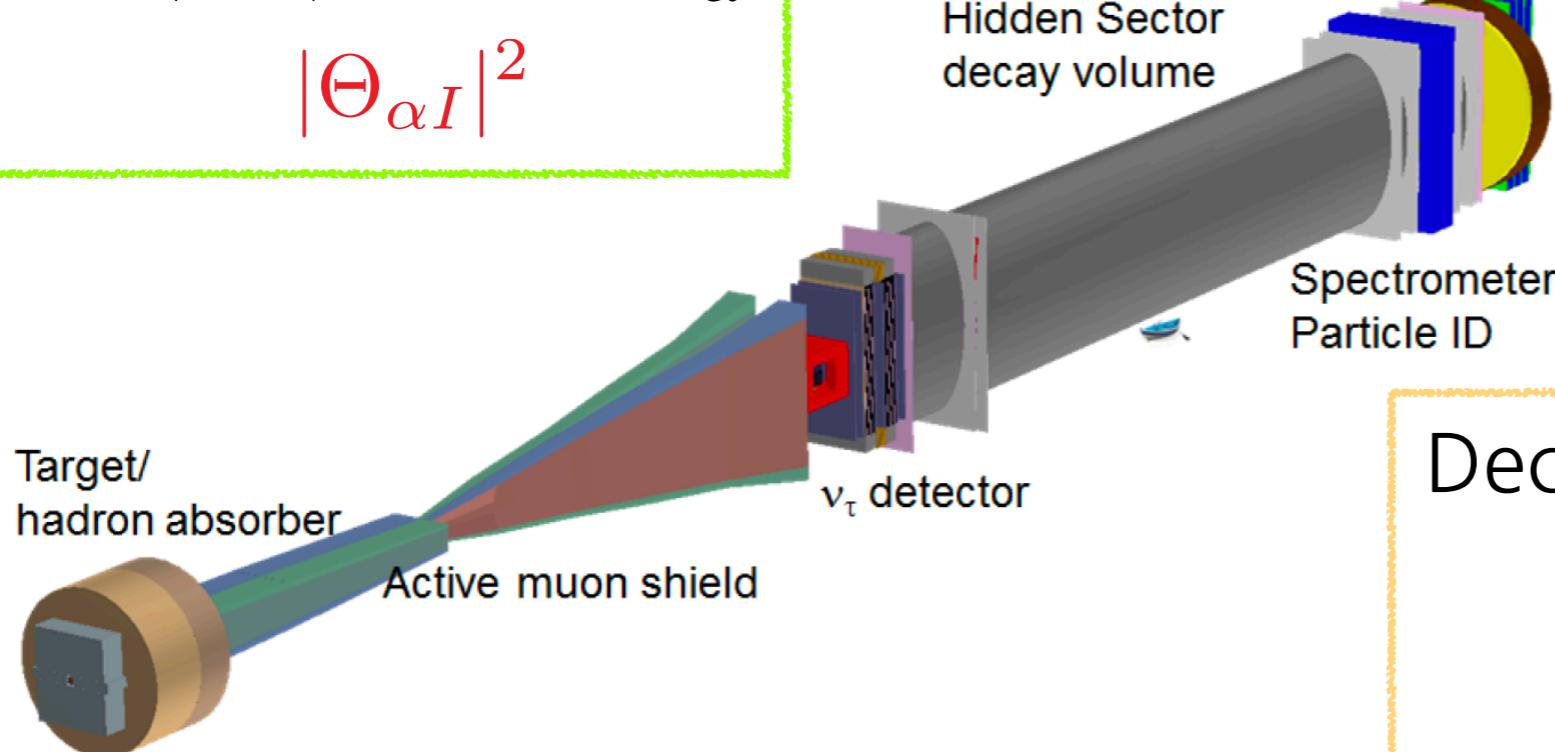
Q2. How can we probe the HNLs experimentally?

Intensity frontier experiments

There are some intensity frontier experiments in near-future, FASER, MATHUSLA, SHiP and so on.

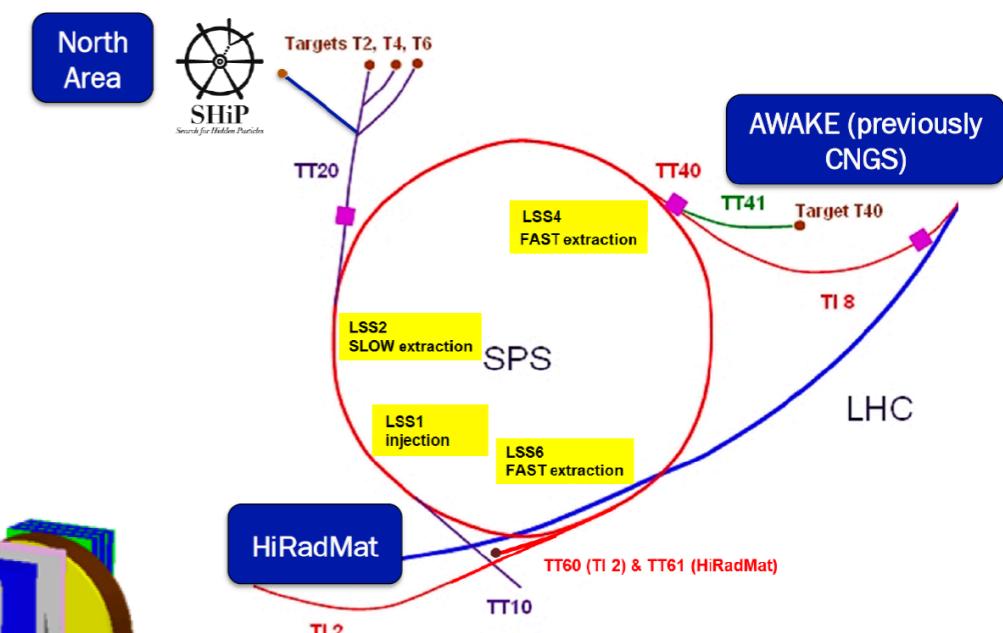
Search for Hidden Particle (SHiP)

Production of HNLs

$$B^+(D^+) \rightarrow N_I + l_\alpha^+$$
$$|\Theta_{\alpha I}|^2$$


[The SHiP collaboration ('15)]

2027?~



Decay of HNLs

$$N_I \rightarrow \nu_\gamma l_\beta^- l_\gamma^+$$

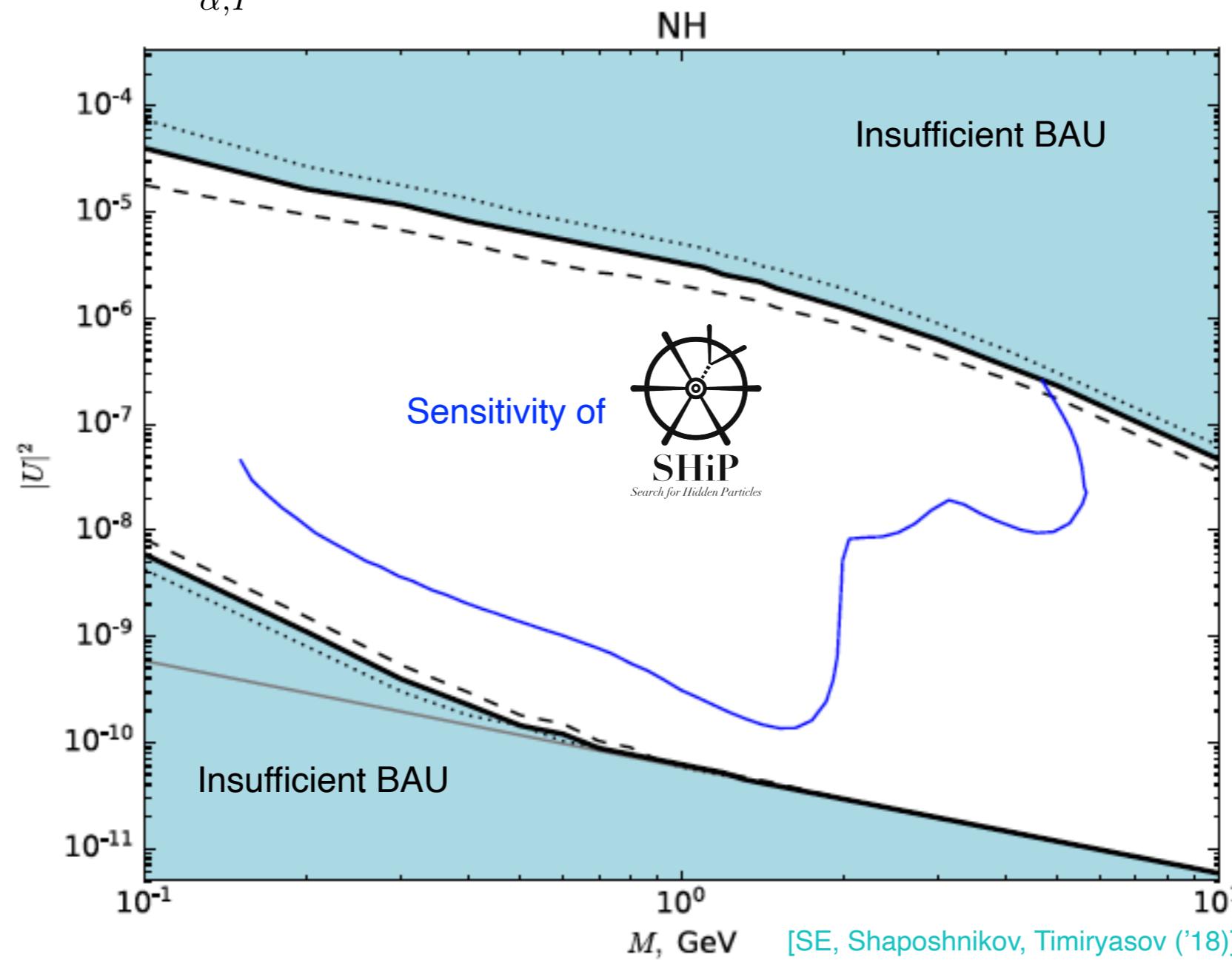
$$N_I \rightarrow l_\beta^- M^+$$

$$|\Theta_{\beta I}|^2$$

SHiP experiments

SHiP experiment tests the wide region of parameter space for Leptogenesis for $M_N \lesssim m_B$.

$$U^2 \equiv \sum_{\alpha, I} |\Theta_{\alpha I}|^2 \simeq \frac{\sum_i m_i}{2M} (X_\omega^2 + X_\omega^{-2}) \quad X_\omega = \exp(\text{Im } \omega)$$



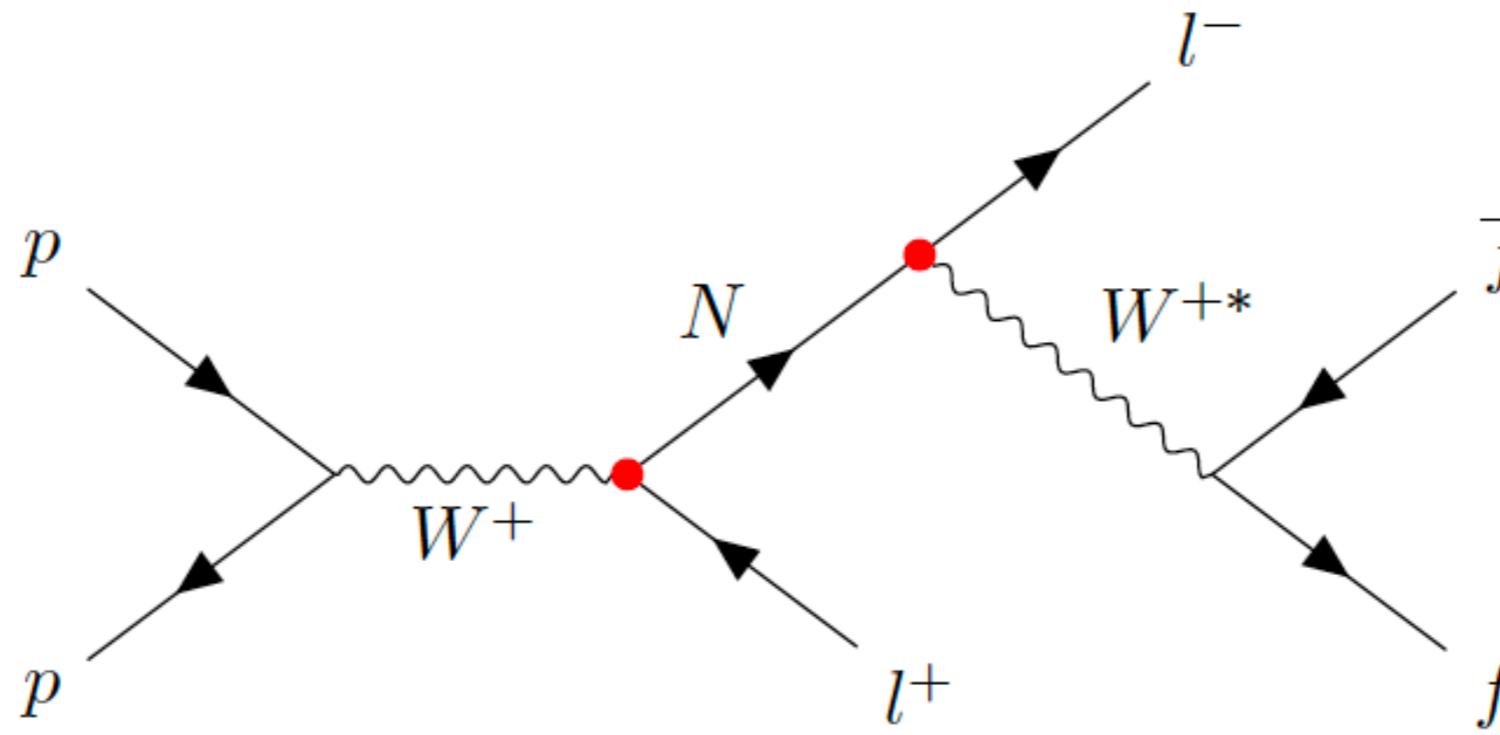
$$m_{D^\pm} = 1869 \text{ MeV}$$

$$m_{B_0} = 5279 \text{ MeV}$$

$$m_{B_c^+} = 6274 \text{ MeV}$$

Displaced vertex search

Displaced vertex technique in colliders is to look for geometrical gaps of vertexes in trackers.



[Drewes, Hager ('19)]

It has potential to address remaining parameter regions, $M_N \gtrsim m_B$.

Displaced vertex search at LHC

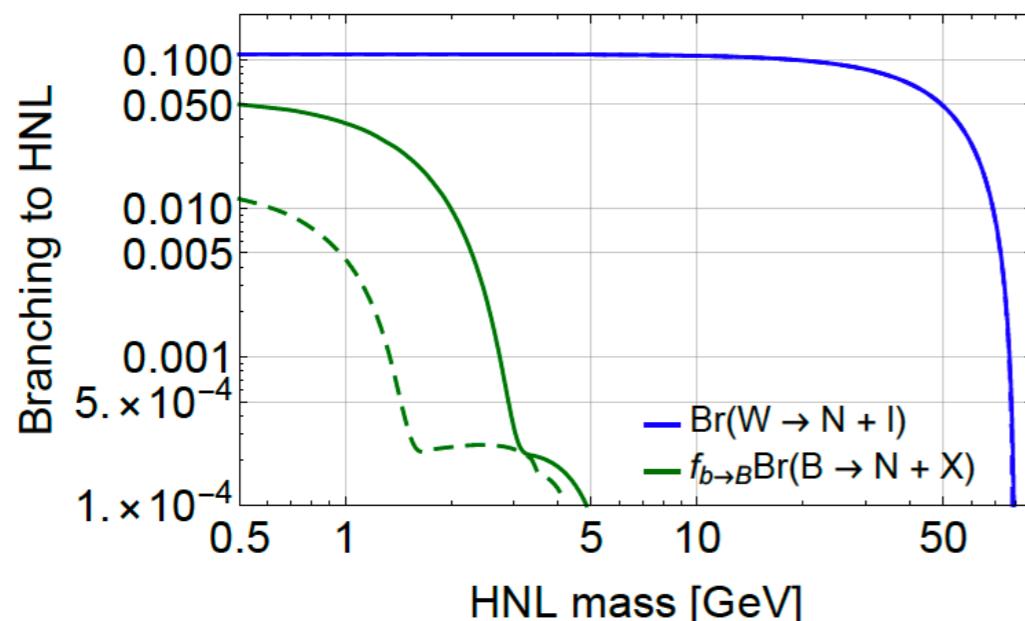
Displaced vertex search can be performed at LHC.

Sensitivity estimation

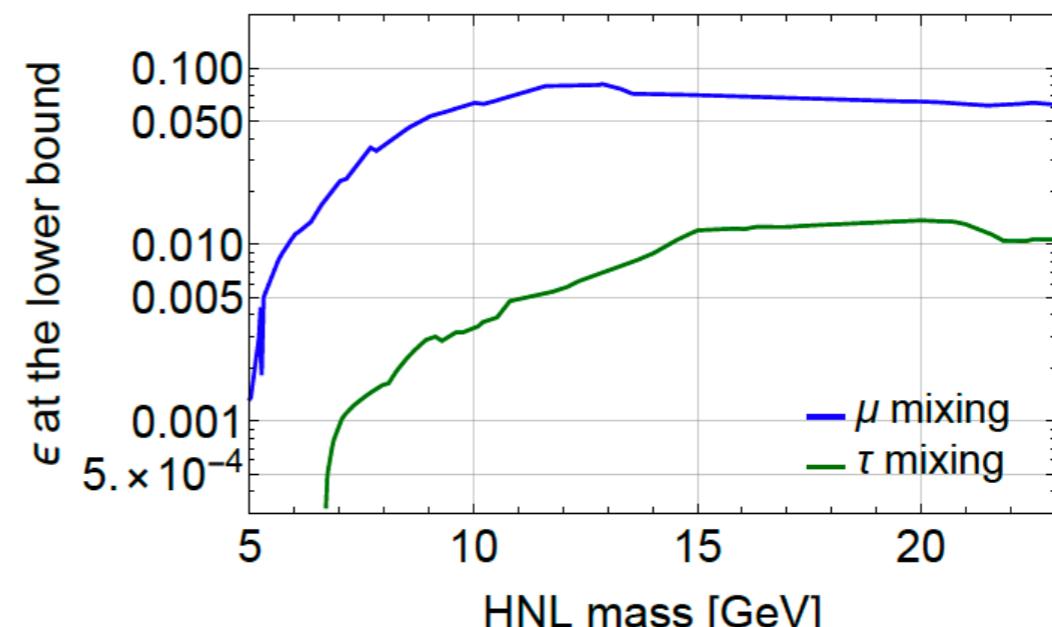
$$N_{\text{events}} = N_{\text{parent}} \cdot \text{Br} \cdot P_{\text{dec}} \cdot \epsilon$$

$$P_{\text{dec}} = e^{-l_{\min}/c\tau\langle\gamma_N\rangle} - e^{-l_{\max}/c\tau\langle\gamma_N\rangle}$$

Parent/Experiment	l_{\min}, l_{\max}	Cross-section	Number	$\langle E \rangle$
W @ ATLAS/CMS, Short DV	0.4 cm, 30 cm [72]	$\sigma_W \simeq 193 \text{ nb}$ [87]	5×10^{11}	–
W @ CMS, Long DV	2 cm, 300 cm	$\sigma_W \simeq 193 \text{ nb}$ [87]	5×10^{11}	–
B @ LHCb	2 cm, 60 cm [66]	$\sigma_{b\bar{b}} \simeq 1.3 \times 10^8 \text{ pb}$ [88]	$4.9 \cdot 10^{13}$	84 GeV [89]



[Kling, Trojanowski ('18)] [Aaij et al. LHCb Collaboration ('11, '17)]

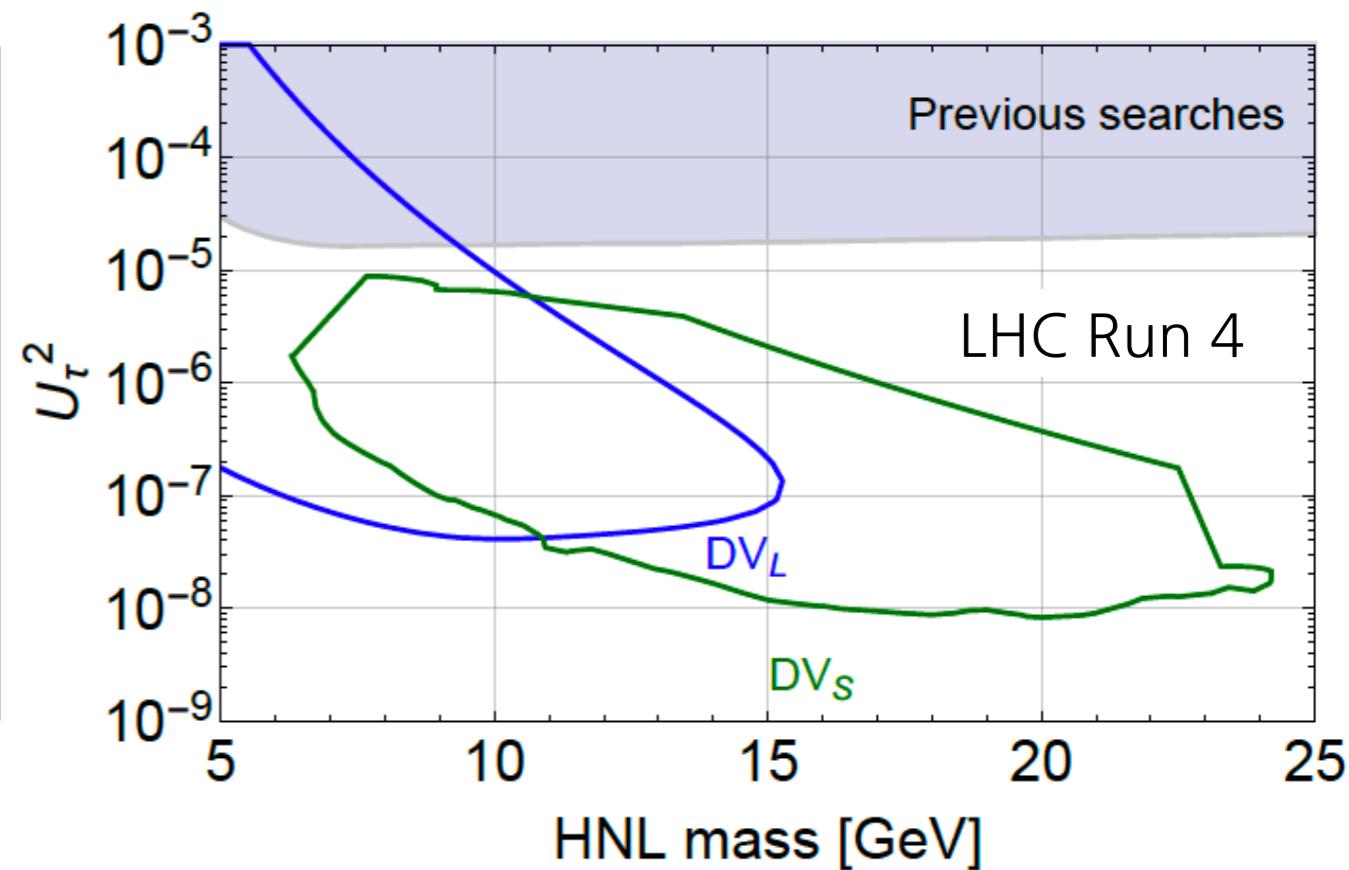
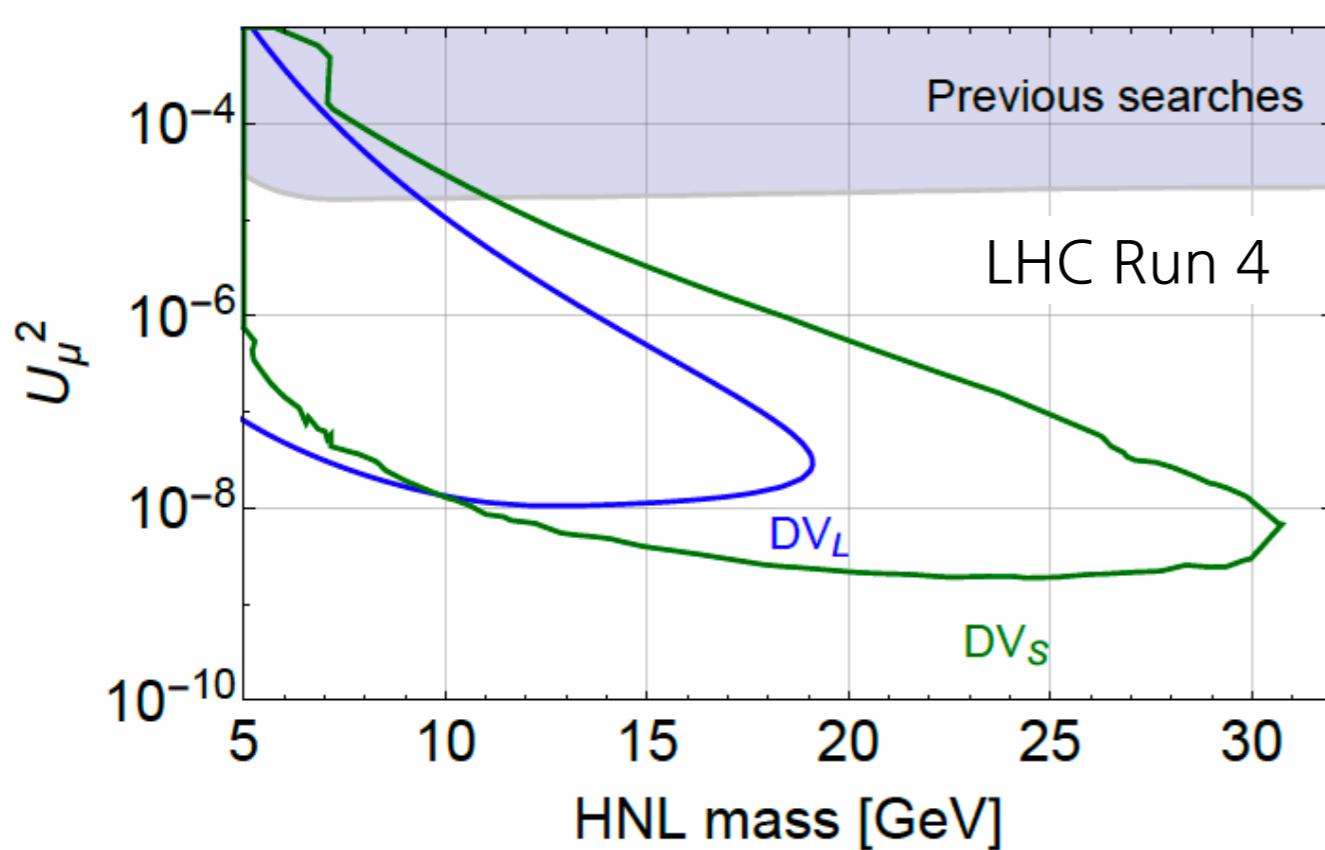


[Cottin, Helo, Hirsch ('18)]

Displaced vertex search at ATLAS and CMS

ATLAS/CMS can extend experimental reach of the mass.

Parent/Experiment	l_{\min}, l_{\max}	Cross-section	Number	$\langle E \rangle$
W @ ATLAS/CMS, Short DV	0.4 cm, 30 cm [72]	$\sigma_W \simeq 193 \text{ nb}$ [87]	5×10^{11}	—
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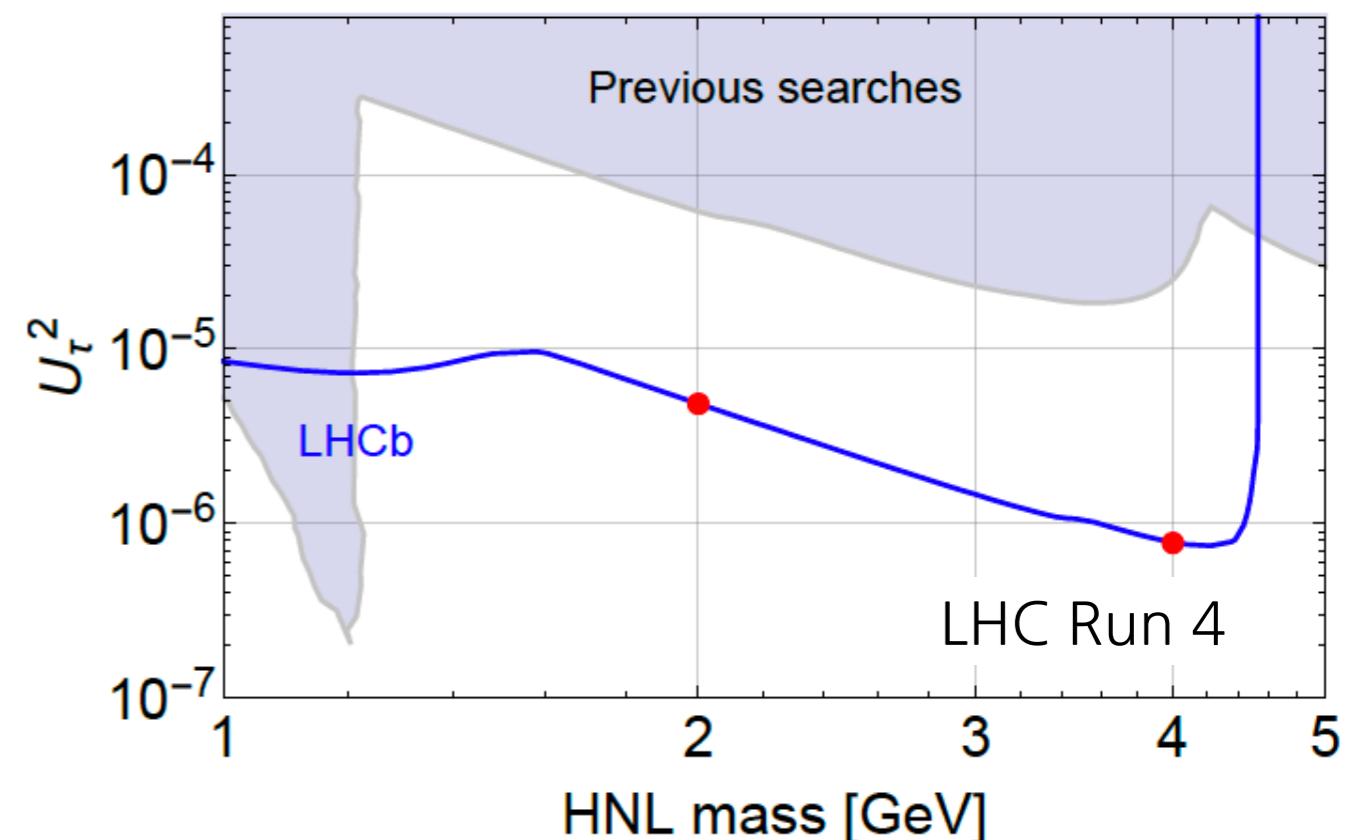
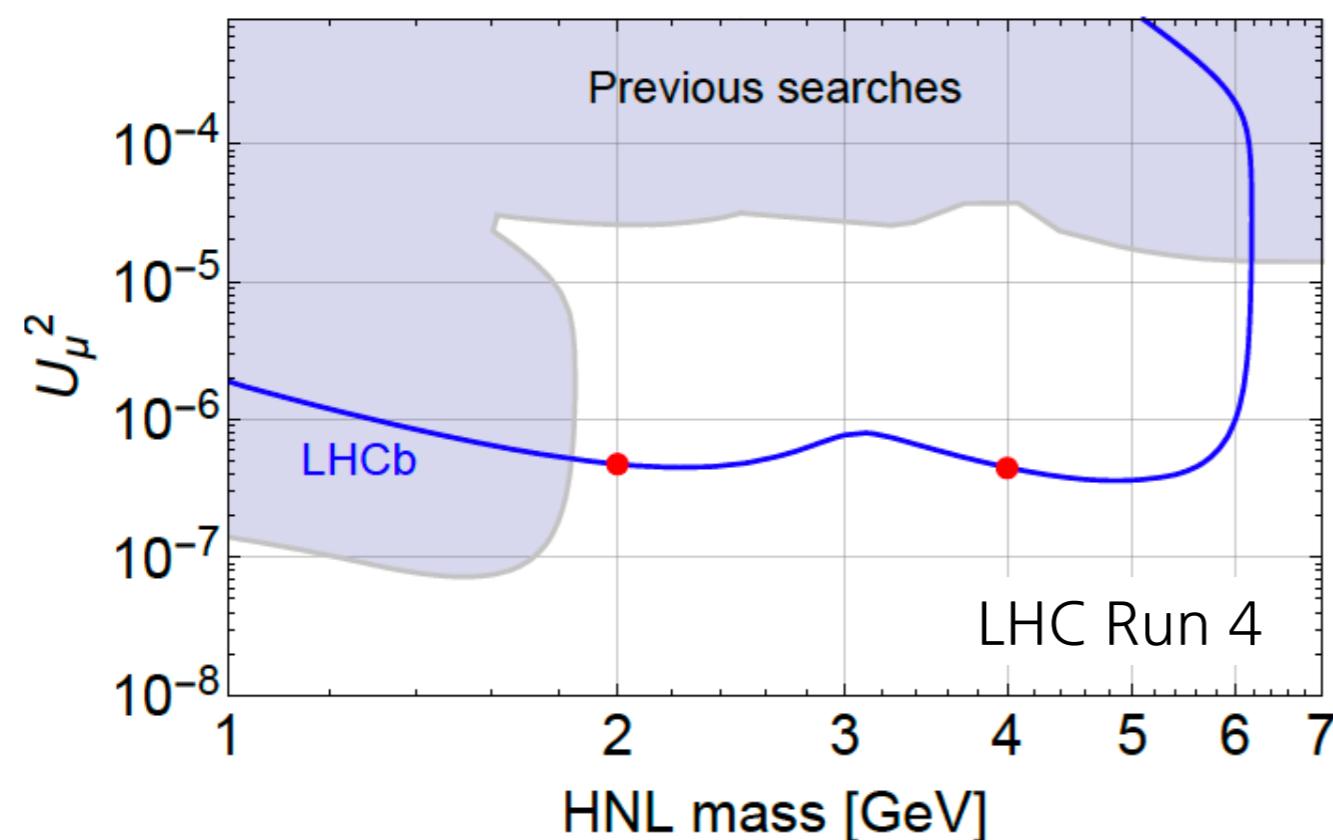


- DV_S : $W^+ \rightarrow l_\alpha^+ N \rightarrow l_\alpha^+ (l_\beta^- \bar{f} f')$ in inner tracker of ATLAS/CMS
- DV_L : $W^+ \rightarrow l_\alpha^+ N \rightarrow l_\alpha^+ (\mu^- \mu^+ \nu_\mu)$ in muon tracker of CMS

Displaced vertex search at LHCb

Decays of HNLs in LHCb can be identified as a DV event.

Parent/Experiment	l_{\min}, l_{\max}	Cross-section	Number	$\langle E \rangle$
W @ ATLAS/CMS, Short DV	0.4 cm, 30 cm [72]	$\sigma_W \simeq 193 \text{ nb}$ [87]	5×10^{11}	—
W @ CMS, Long DV	2 cm, 300 cm	$\sigma_W \simeq 193 \text{ nb}$ [87]	5×10^{11}	—
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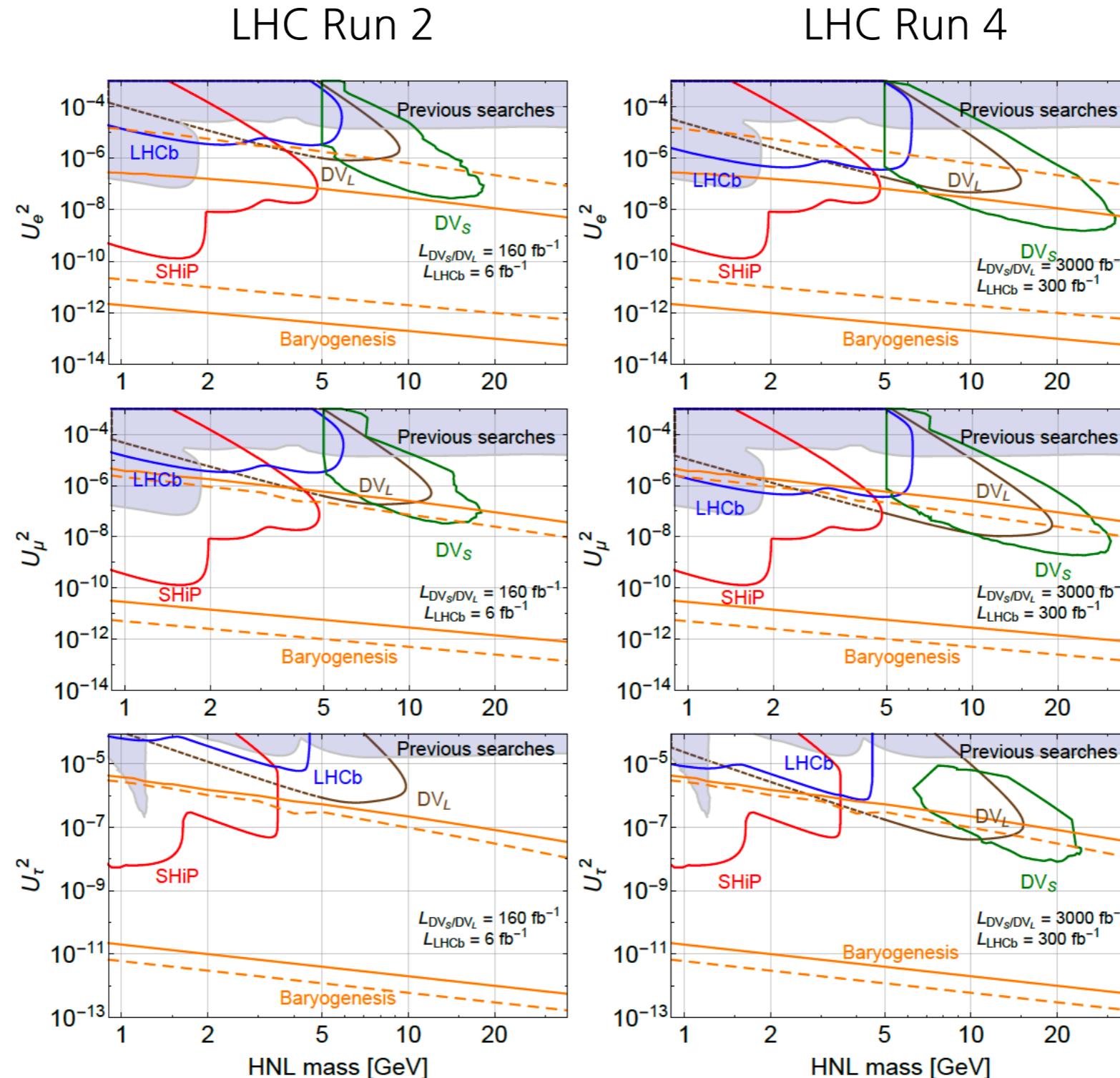
$$M^+ \rightarrow l_\alpha^+ N \rightarrow l_\alpha^+ (l_\beta^- + \dots)$$

$$\epsilon \sim 10^{-2}$$

[Aaij et al. LHCb Collaboration ('14)]

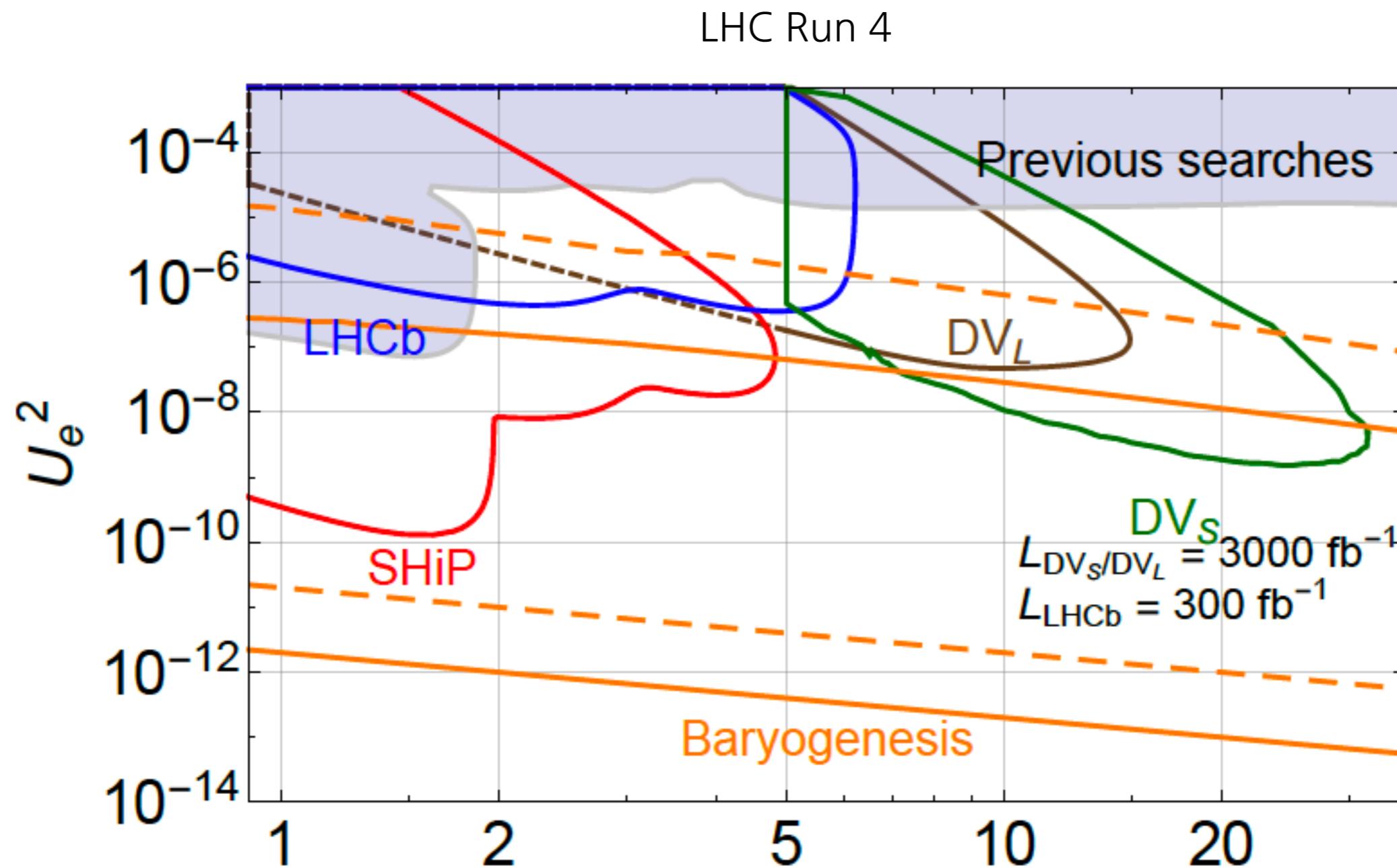
Summary plots

DV searches at LHC and SHiP complete each other.



Summary plots

DV searches at LHC and SHiP complete each other.



Summary

We have a chance to prove the matter-antimatter asymmetry of the Universe through exploring heavy neutral leptons.

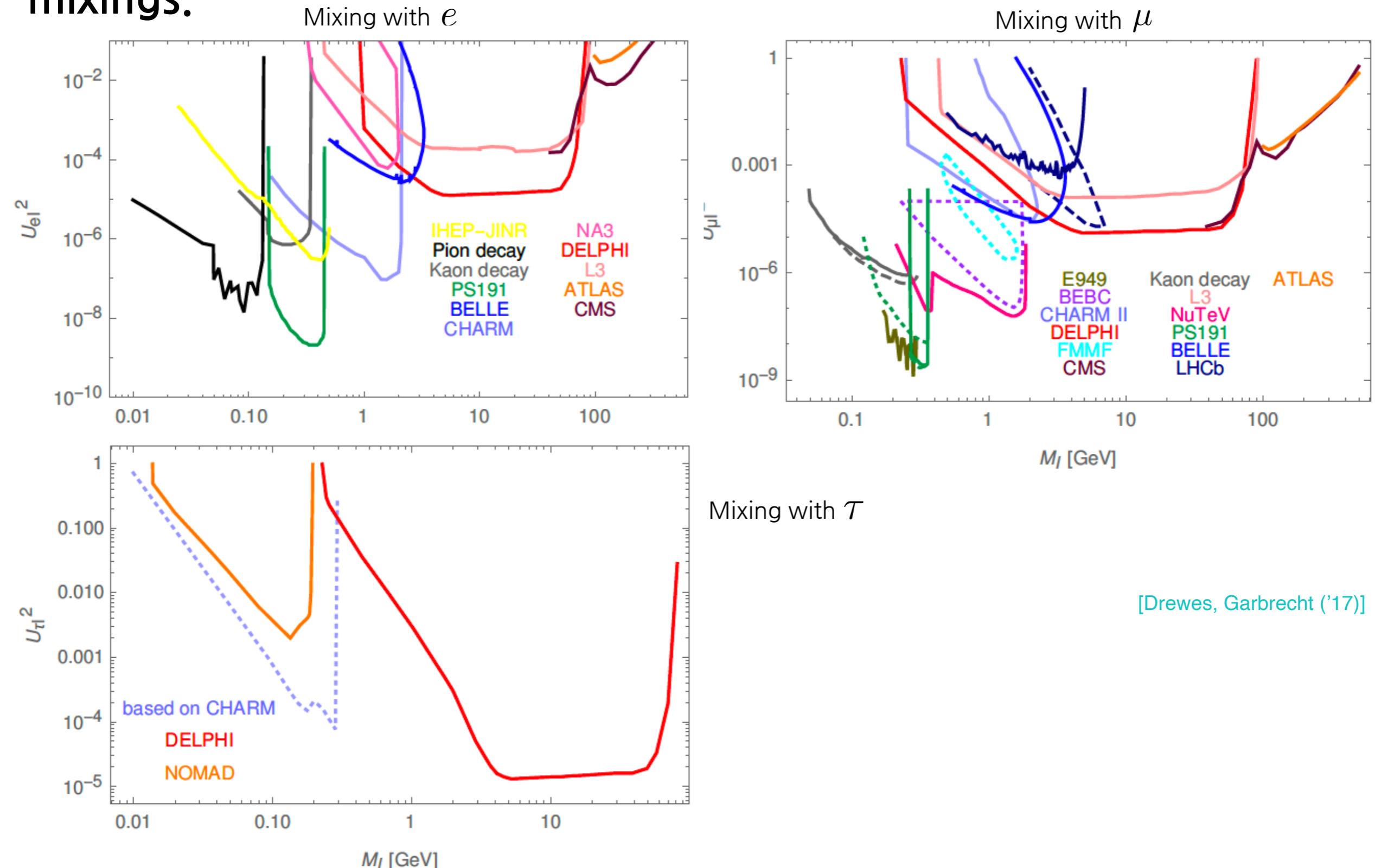
Baryogenesis via right-handed neutrino oscillations has been studied actively and the theoretical prediction to parameter space has been updated.

In the test displaced vertex searches at LHC and intensity frontier experiments in near future complete each other.

Backup

Experimental bounds

Negative results in past experiments have put upper bounds on the mixings.

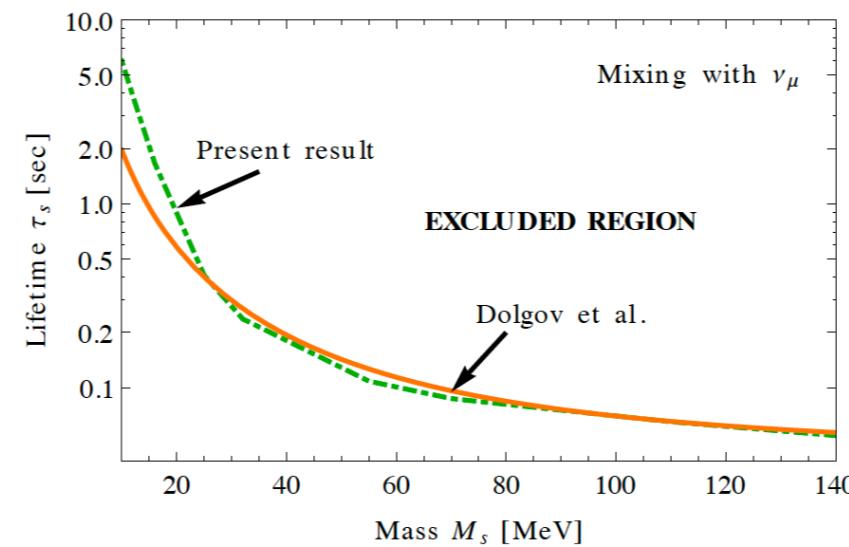
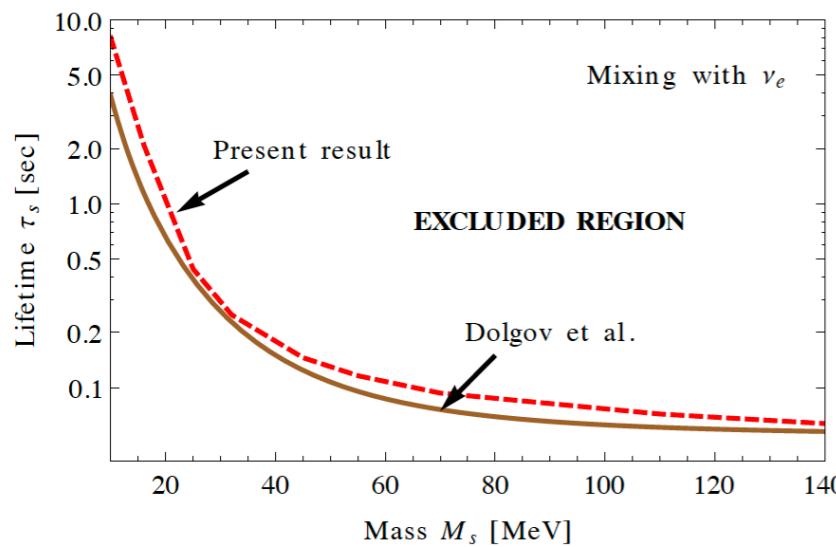


Cosmological bounds

Long-live HNLs may spoil the success of Big-Bang Nucleosynthesis.

Upper bound on lifetime

For $M_N < m_\pi$



[Ruchayskiy, Ivashko ('12)]

For $M_N \geq m_\pi$

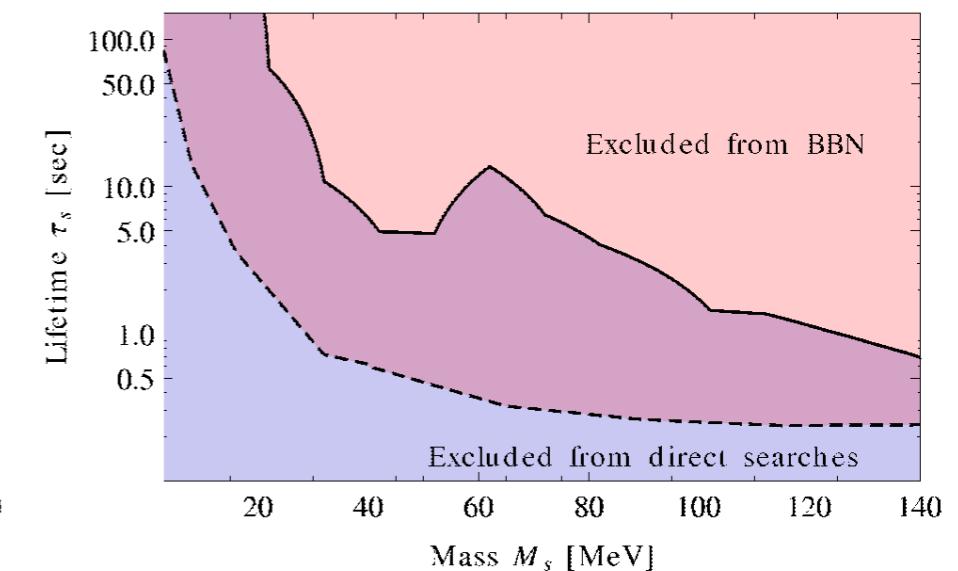
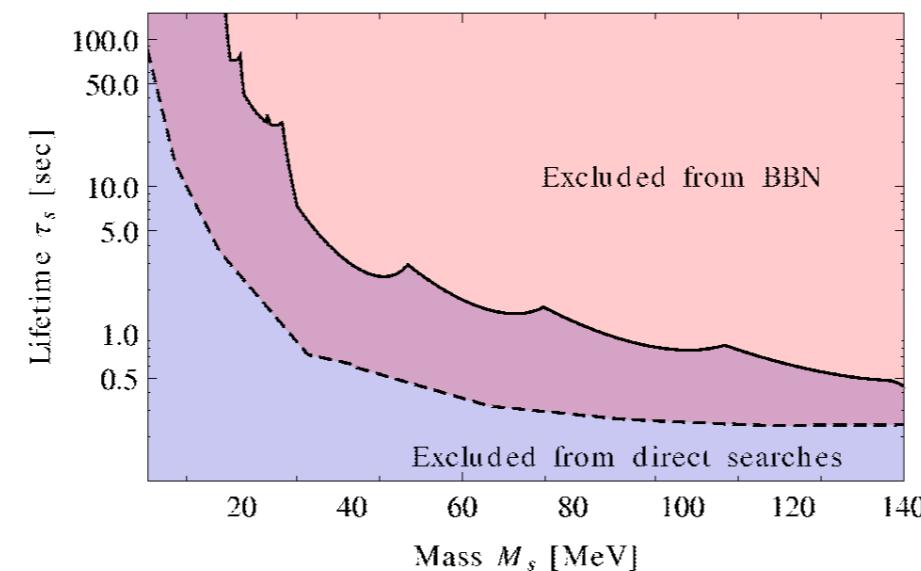
$$\tau_N \leq 0.1 \text{ sec}$$

[Dolgov, Hansen, Raffelt, Semikoz ('00)]

Lower bound of mixings

$$\tau_N = \Gamma_N^{-1} \propto (\Theta^2)^{-1}$$

$M_N \lesssim m_\pi$ is excluded.



Kinetic equations

The mechanism is described by kinetic equations of density matrix.

Density matrix: $\rho = \begin{pmatrix} \rho_{11} & \rho_{12} \\ \rho_{21} & \rho_{22} \end{pmatrix}$

ρ_{II} : occupation numbers
 ρ_{IJ} : correlations

For ν_R and anti- ν_R (2x2 matrix)

$$\frac{d\rho_N}{dt} = -i [H_N, \rho_N] - \frac{1}{2} \{\Gamma_N, \rho_N - \rho_N^{\text{eq}}\} - \frac{1}{2} \sum_{\alpha} [\tilde{\Gamma}_N^{\alpha} \Delta\rho_{\nu_{\alpha}}]$$

Oscillation Production and Destruction Communication (back-reaction)

$$\frac{d\rho_{\bar{N}}}{dt} = -i [H_N^*, \rho_{\bar{N}}] - \frac{1}{2} \{\Gamma_N^*, \rho_{\bar{N}} - \rho_N^{\text{eq}}\} + \frac{1}{2} \sum_{\alpha} [(\tilde{\Gamma}_N^{\alpha})^* \Delta\rho_{\nu_{\alpha}}]$$

For lepton asymmetries $\Delta\rho_{\nu_{\alpha}}$ ($\alpha = e, \nu, \tau$)

$$\frac{d\Delta\rho_{\nu_{\alpha}}}{dt} = -\Gamma_{\nu_{\alpha}} \Delta\rho_{\nu_{\alpha}} + \text{Tr}[\tilde{\Gamma}_{\nu_{\alpha}} \rho_{\bar{N}}] - \text{Tr}[\tilde{\Gamma}_{\nu_{\alpha}}^* \rho_N]$$

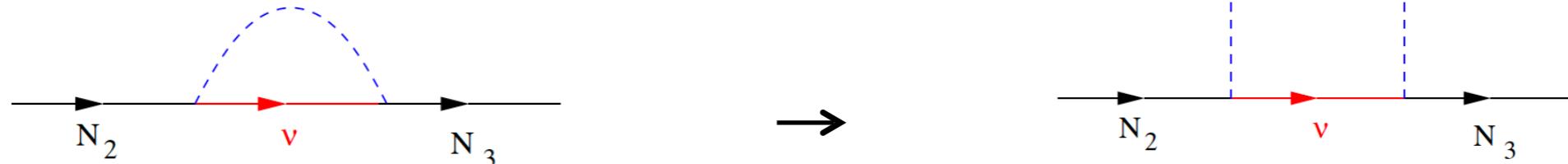
Damping

Communication (back-reaction)

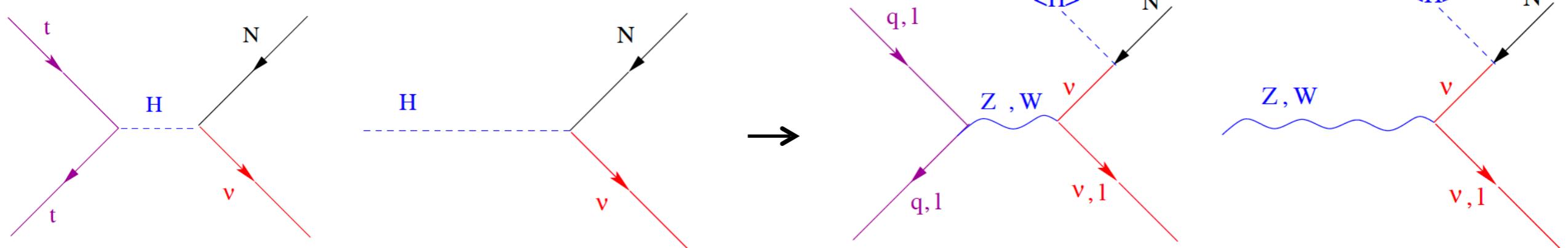
Kinetic equations in the Higgs phase

Gauge interaction with neutrino mixing gets dominant instead of Yukawa interaction.

For effective Hamiltonian of ν_R



For interactions of ν_R



Lepton number conserving and violating contributions

$$\Gamma = \Gamma_+ + \Gamma_-$$

$$\Gamma_+, H_+ \propto T$$

; Lepton # conserving

$$H = H_+ + H_-$$

$$\Gamma_-, H_- \propto (M/T)^2 T$$

; Lepton # violating

H and Γ in the Higgs phase

Effective Hamiltonian

$$H_N = H_0 + H_I,$$

$$H_0 = -\frac{\Delta M M}{E_N} \sigma_1$$

$$H_I = h_+ \left[\sum_{\alpha} Y_{+,\alpha}^N \right] + h_- \left[\sum_{\alpha} Y_{-,\alpha}^N \right],$$

Production and back-reaction rates

$$\Gamma_N = \gamma_+ \left[\sum_{\alpha} Y_{+,\alpha}^N \right] + \gamma_- \left[\sum_{\alpha} Y_{-,\alpha}^N \right]$$

$$\tilde{\Gamma}_N^{\alpha} = -\gamma_+ Y_{+,\alpha}^N + \gamma_- Y_{-,\alpha}^N$$

$$\Gamma_{\nu_{\alpha}} = (\gamma_+ + \gamma_-) \sum_I h_{\alpha I} h_{\alpha I}^*$$

$$\tilde{\Gamma}_{\nu_{\alpha}} = -\gamma_+ Y_{+,\alpha}^{\nu} + \gamma_- Y_{-,\alpha}^{\nu}$$

Coefficients

$$h_+ = \frac{2\langle\Phi\rangle^2 E_{\nu} (E_N + k)(E_N + E_{\nu})}{kE_N(4(E_N + E_{\nu})^2 + \gamma_{\nu}^2)},$$

$$h_- = \frac{2\langle\Phi\rangle^2 E_{\nu} (E_N - k)(E_N - E_{\nu})}{kE_N(4(E_N - E_{\nu})^2 + \gamma_{\nu}^2)},$$

$$\gamma_+ = \frac{2\langle\Phi\rangle^2 E_{\nu} (E_N + k)\gamma_{\nu}}{kE_N(4(E_N + E_{\nu})^2 + \gamma_{\nu}^2)},$$

$$\gamma_- = \frac{2\langle\Phi\rangle^2 E_{\nu} (E_N - k)\gamma_{\nu}}{kE_N(4(E_N - E_{\nu})^2 + \gamma_{\nu}^2)},$$

$$E_N = \sqrt{k^2 + M^2} \quad E_{\nu} = k - b_L$$

Yukawa couplings

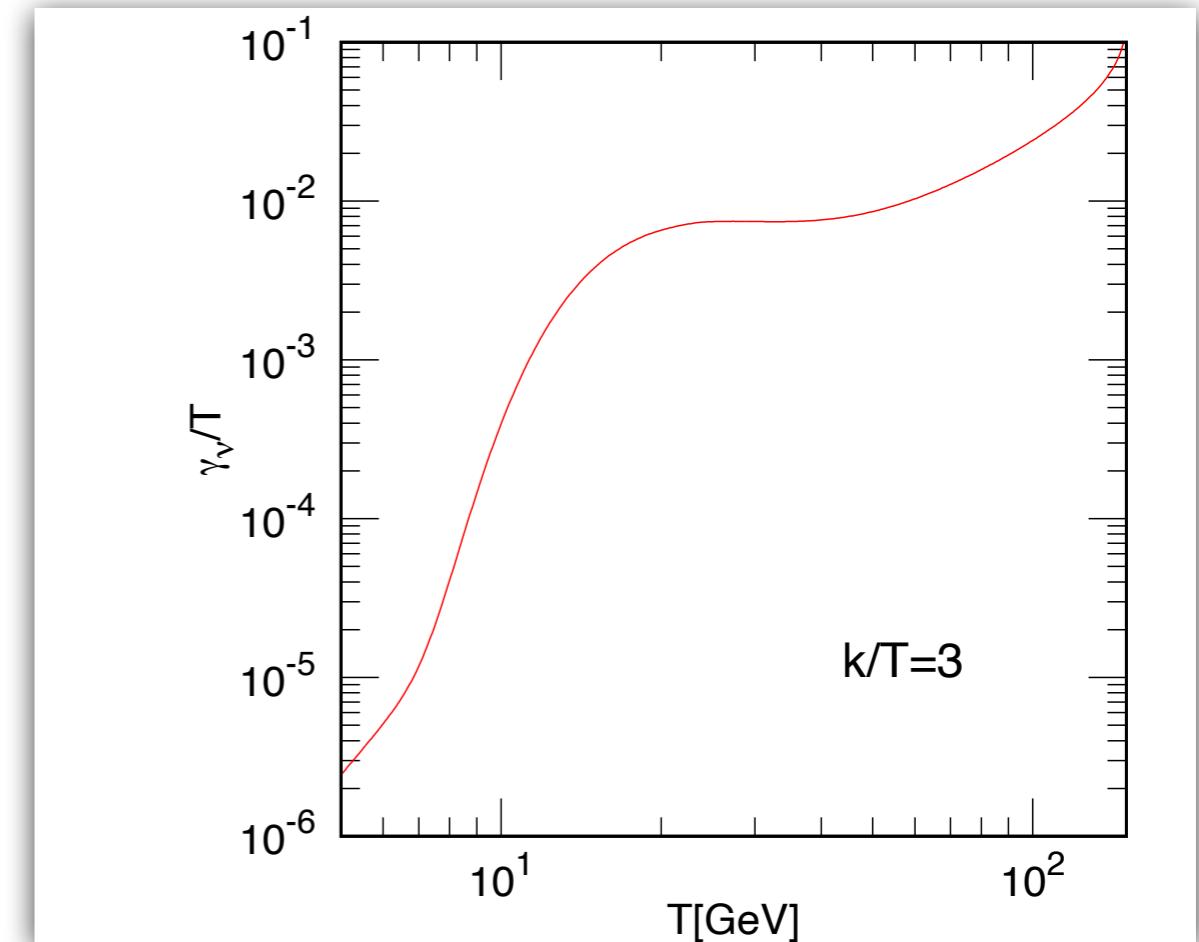
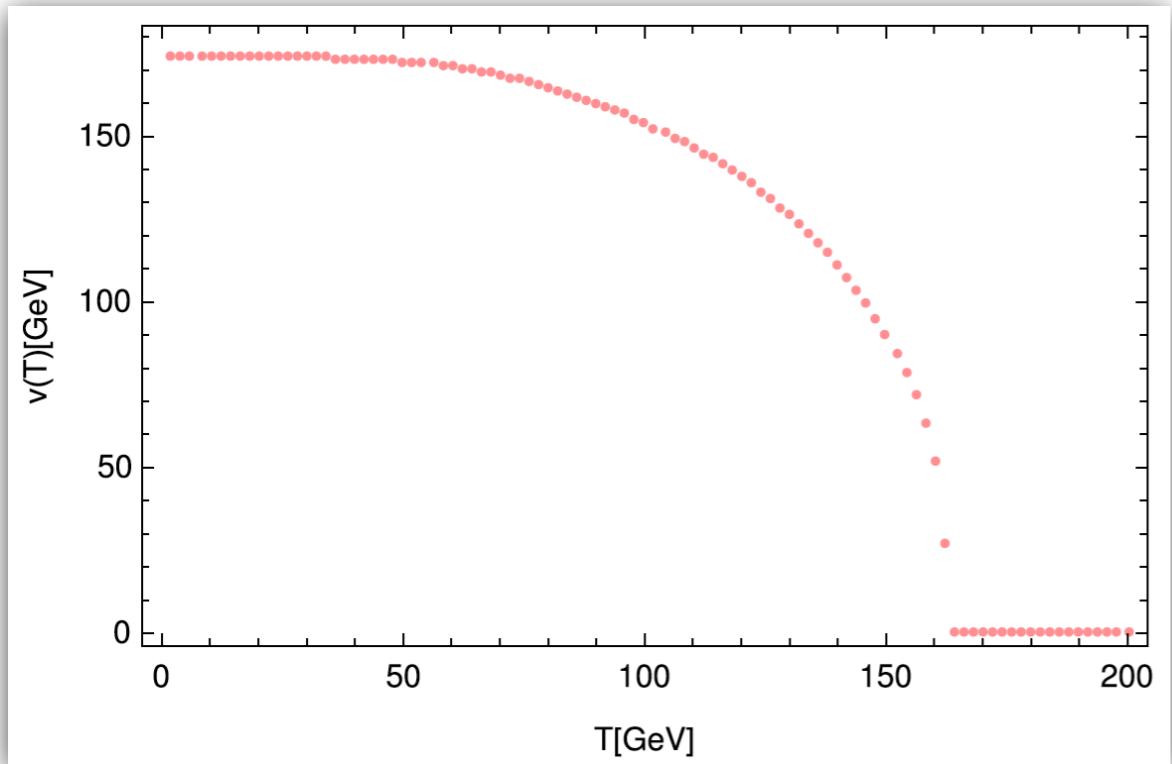
$$Y_{+,\alpha}^N = \begin{pmatrix} h_{\alpha 3} h_{\alpha 3}^* & -h_{\alpha 3} h_{\alpha 2}^* \\ -h_{\alpha 2} h_{\alpha 3}^* & h_{\alpha 2} h_{\alpha 2}^* \end{pmatrix},$$

$$Y_{-,\alpha}^N = \begin{pmatrix} h_{\alpha 2} h_{\alpha 2}^* & -h_{\alpha 3} h_{\alpha 2}^* \\ -h_{\alpha 2} h_{\alpha 3}^* & h_{\alpha 3} h_{\alpha 3}^* \end{pmatrix},$$

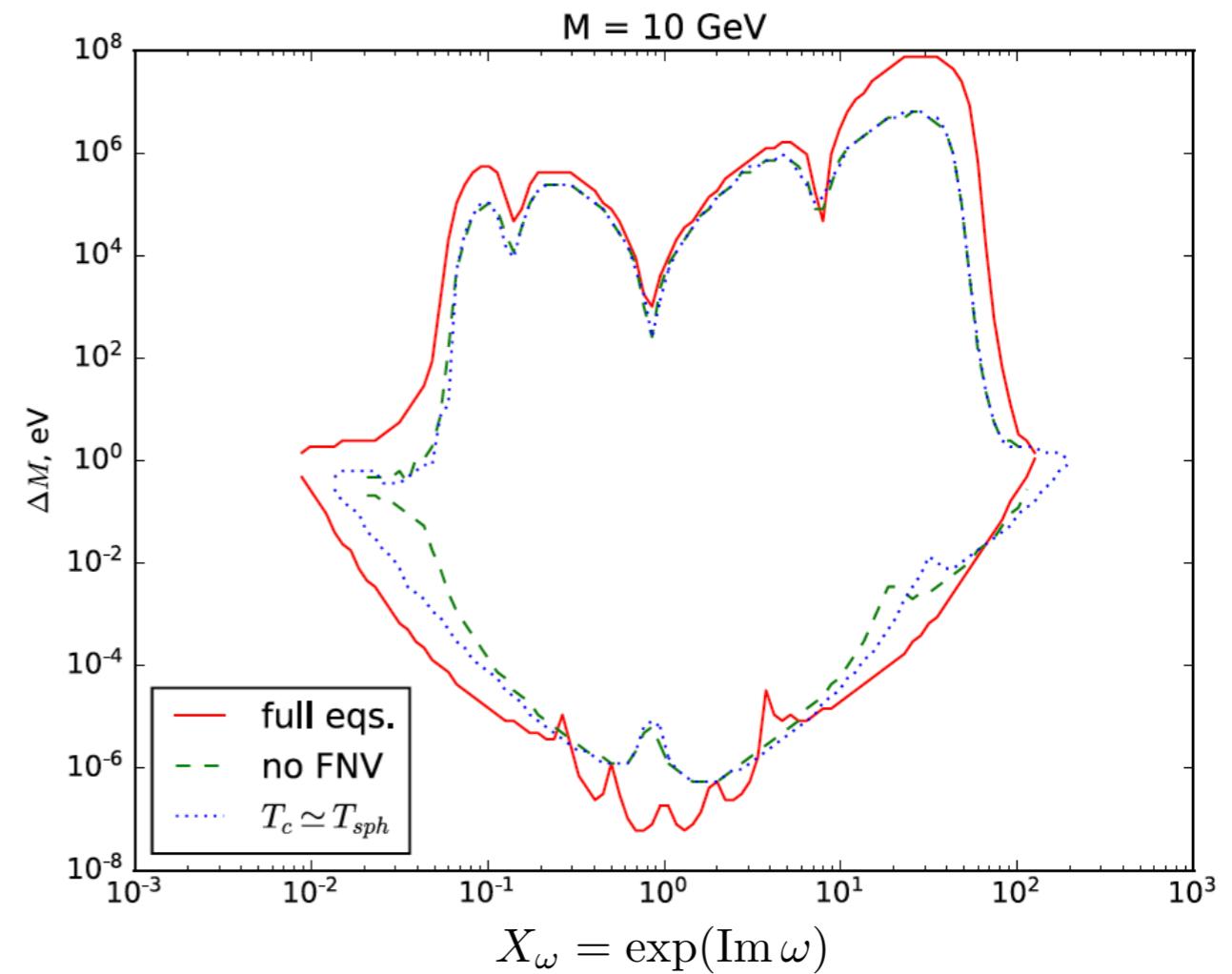
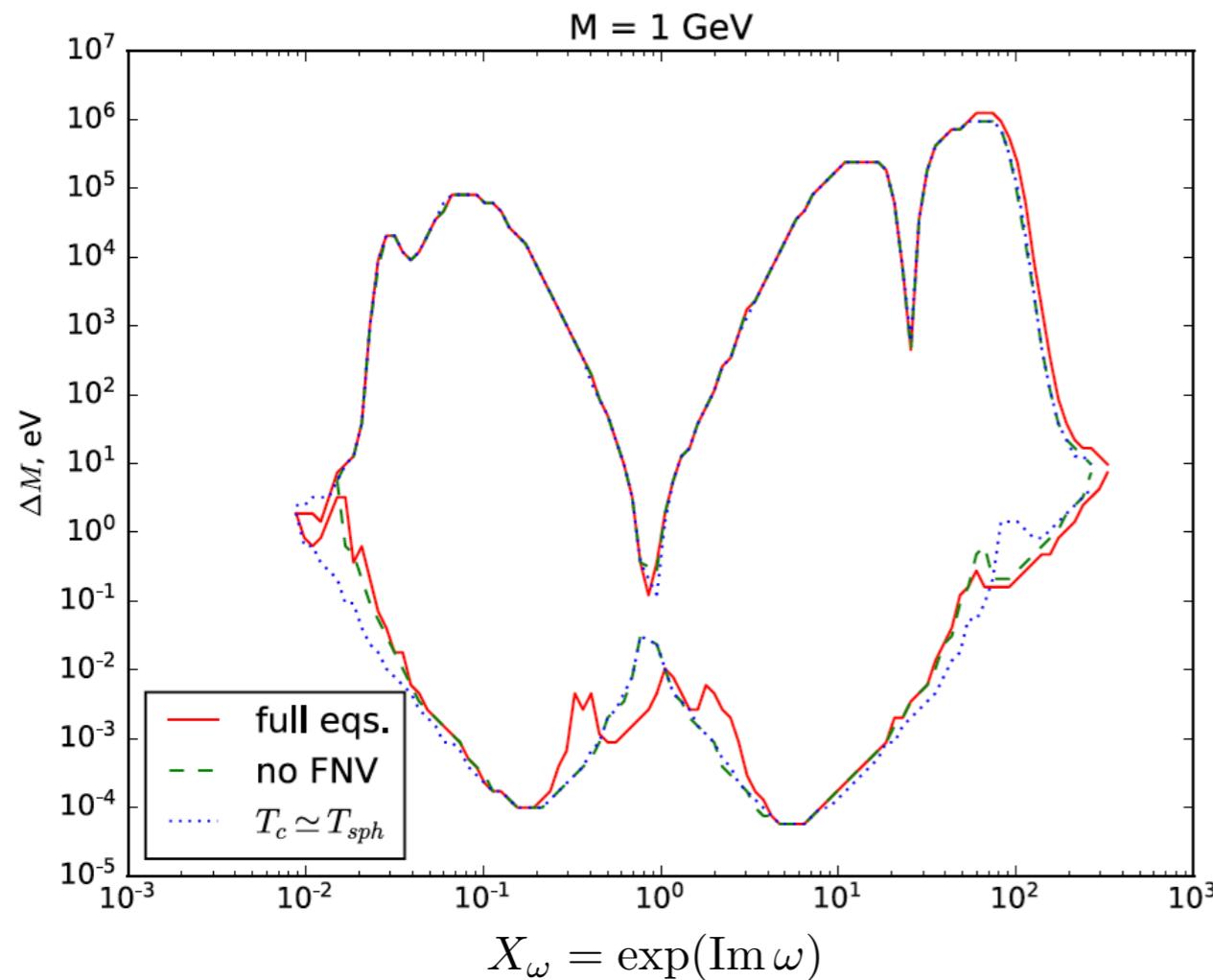
$$Y_{+,\alpha}^{\nu} = \begin{pmatrix} h_{\alpha 3} h_{\alpha 3}^* & -h_{\alpha 2} h_{\alpha 3}^* \\ -h_{\alpha 3} h_{\alpha 2}^* & h_{\alpha 2} h_{\alpha 2}^* \end{pmatrix},$$

$$Y_{-,\alpha}^{\nu} = \begin{pmatrix} h_{\alpha 2} h_{\alpha 2}^* & -h_{\alpha 2} h_{\alpha 3}^* \\ -h_{\alpha 3} h_{\alpha 2}^* & h_{\alpha 3} h_{\alpha 3}^* \end{pmatrix},$$

T-depending parameters



Effects of LNV and in the Higgs phase



Plasma neutrality

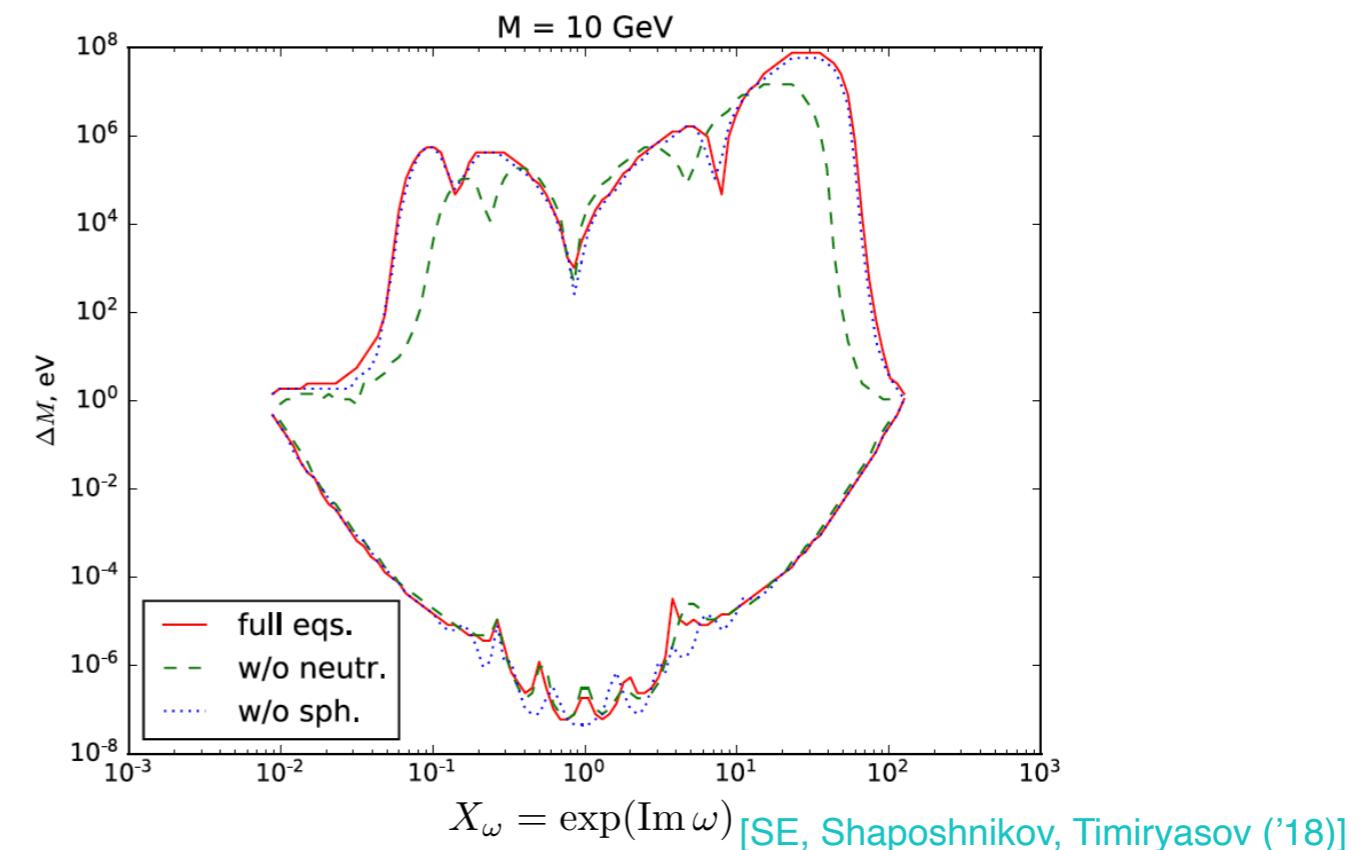
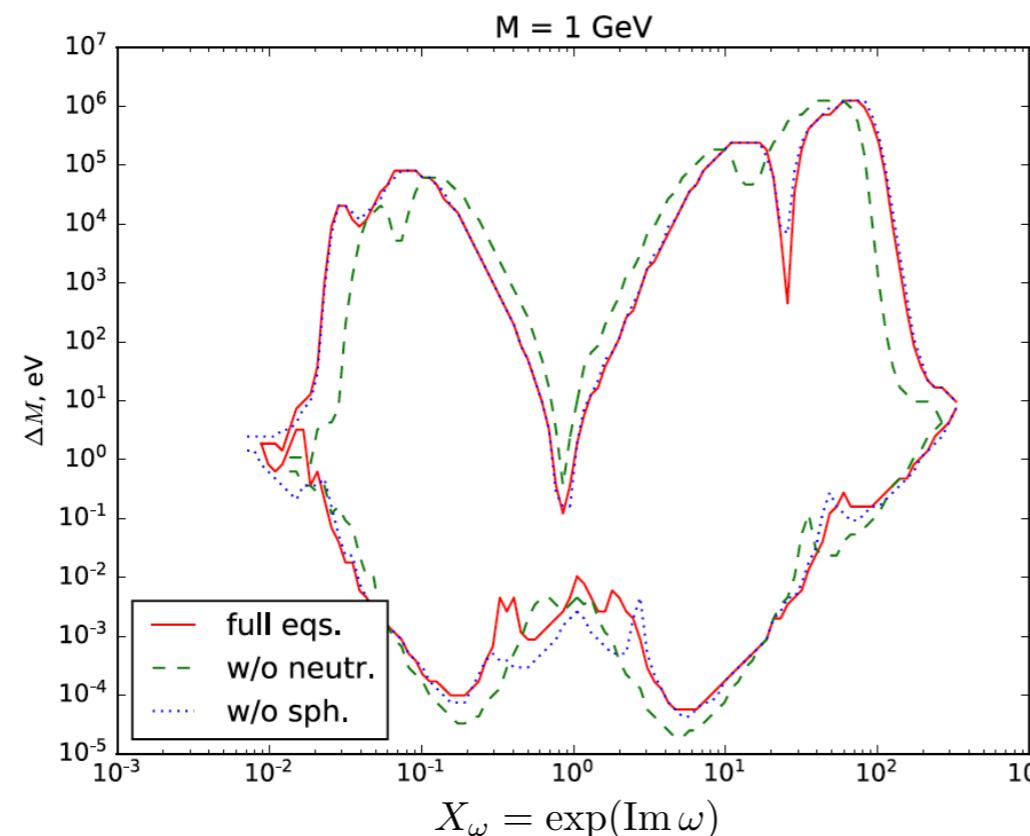
Generated lepton asymmetries have to be distributed into other SM particles in plasma immediately.

Replacing as follows in the right-handed side of kinetic equations.

$$\mu_\alpha = \omega_{\alpha\beta}(T)n_{\Delta_\beta} + \omega_B(T)n_B,$$

$$\omega(T) = \frac{1}{T^2} \begin{pmatrix} a & b & b \\ b & a & b \\ b & b & a \end{pmatrix}, \quad a = \frac{22(15x^2 + 44)}{9(17x^2 + 44)}, \quad b = \frac{8(3x^2 + 22)}{9(17x^2 + 44)},$$

$$\omega_B(T) = \frac{1}{T^2} \frac{4(27x^2 + 77)}{9(17x^2 + 44)} \quad x = \langle \Phi(T) \rangle / T$$



Exact treatment of sphaleron process

Usual approach is instant freeze-out of sphaleron process.

Kinetic equation of baryon asymmetry

$$\dot{n}_B = -\Gamma_B(n_B - n_{B^{\text{eq}}}),$$

$$\Gamma_B = 3^2 \cdot \frac{869 + 333(\langle \Phi \rangle / T)^2}{792 + 306(\langle \Phi \rangle / T)^2} \cdot \frac{\Gamma_{\text{diff}}(T)}{T^3},$$

$$n_{B^{\text{eq}}} = -\chi(T) \sum_{\alpha} n_{\Delta_{\alpha}}, \quad \chi(T) = \frac{4(27(\langle \Phi \rangle / T)^2 + 77)}{333(\langle \Phi \rangle / T)^2 + 869}$$

$$\Gamma_{\text{diff}} \simeq \begin{cases} T^4 \cdot \exp(-147.7 + 0.83T/\text{GeV}), & \text{in the Higgs phase,} \\ T^4 \cdot 18 \alpha_W^5, & \text{in the symmetric phase.} \end{cases}$$

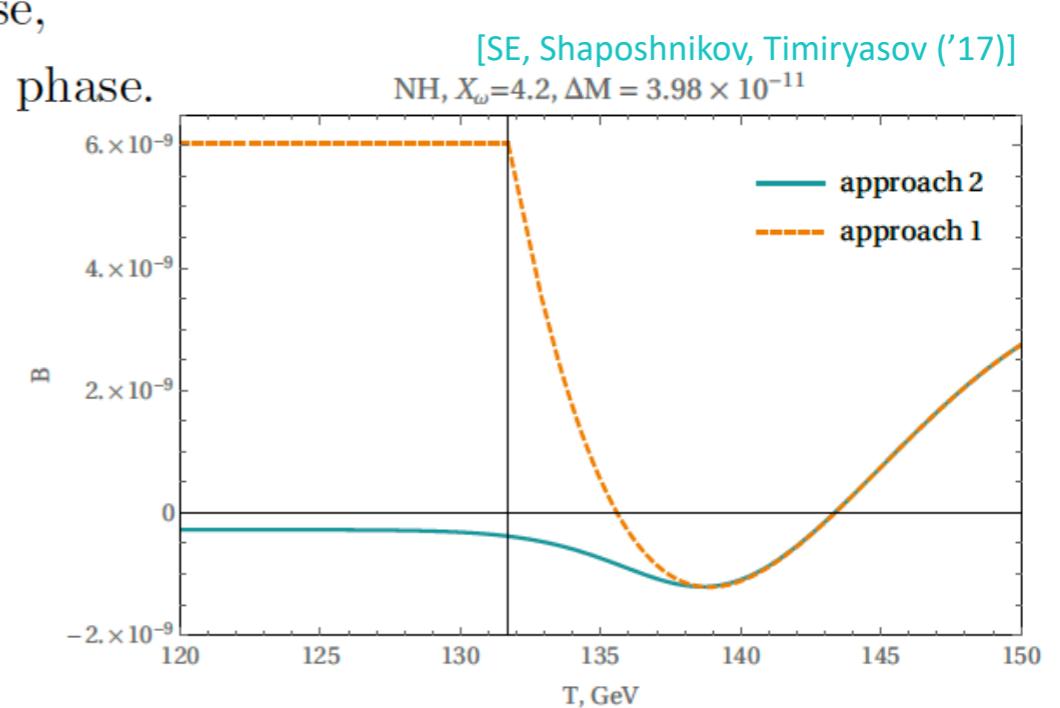
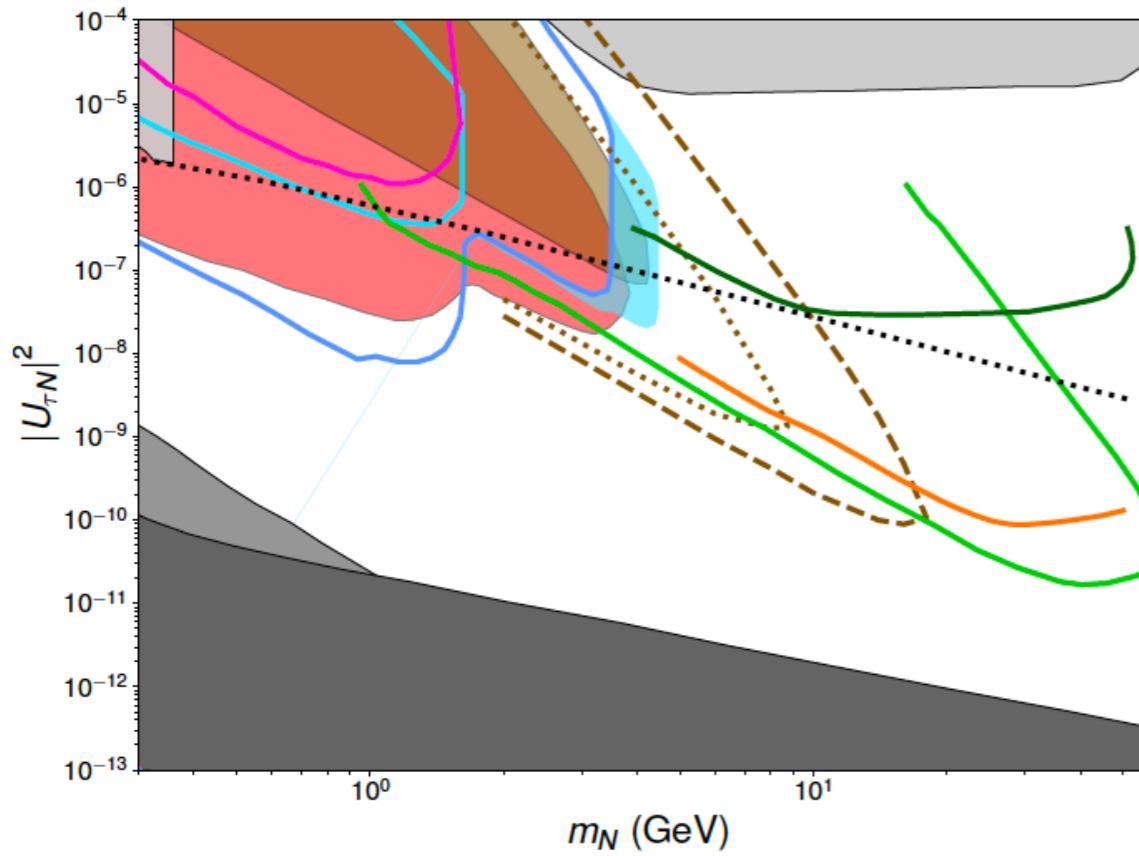
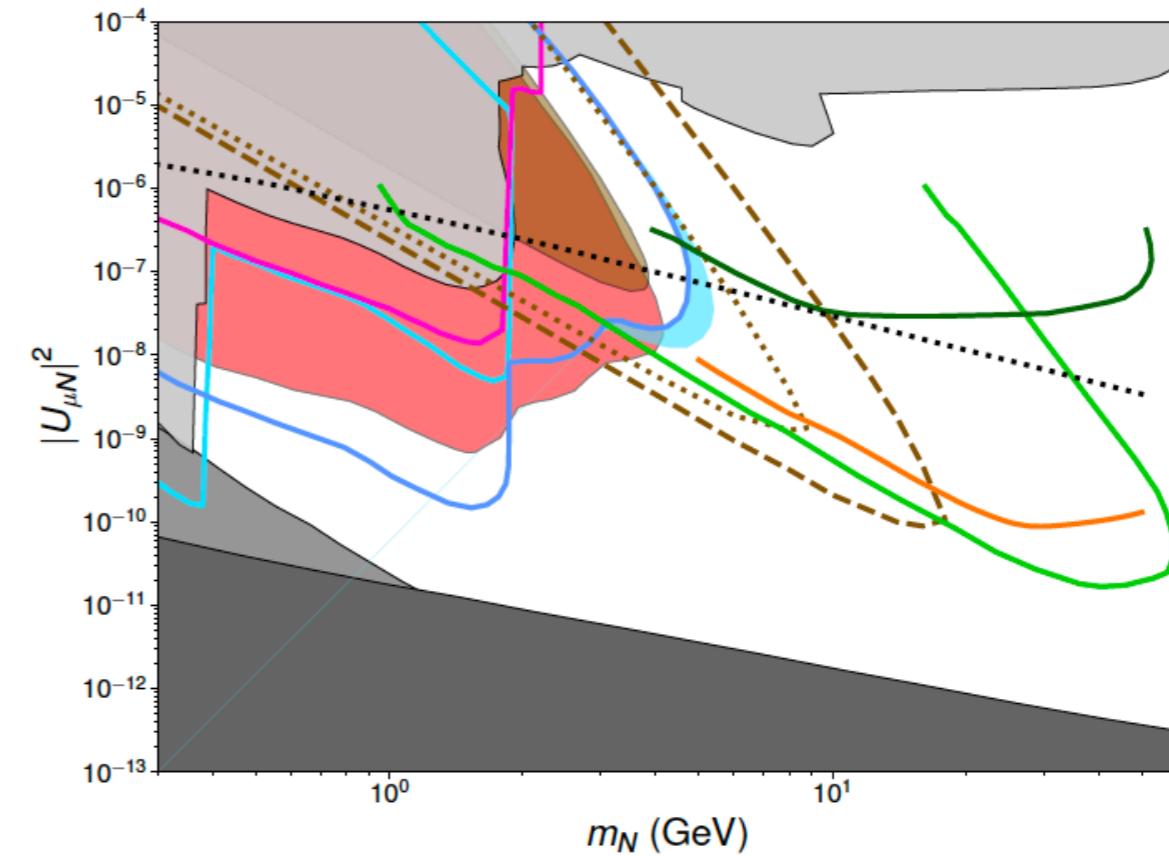
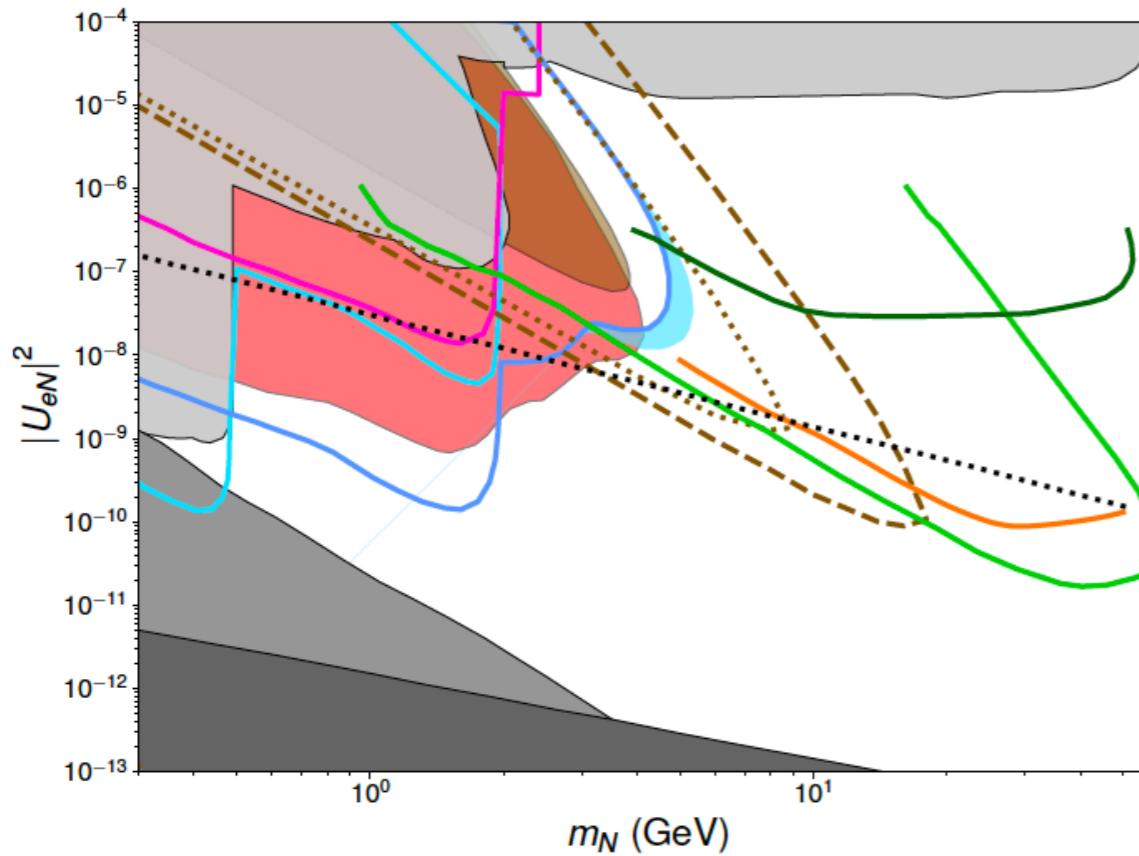


Figure 3. An example of a large deviation. $B^{\text{appr.1}}/B^{\text{appr.2}} \simeq -21.9$. Upper panel, $\Delta(T)$ as function of temperature in the approach with instant freeze-out (dotted orange line) and in the approach with the separate equation for B (blue line). Lower panel, $B(T)$ as function of temperature. The black vertical line shows the sphaleron freeze out temperature $T_{\text{sph}} = 131.7 \text{ GeV}$. To illustrate a situation when lepton asymmetry is generated right before the sphaleron freeze-out we utilize the following values of the parameters: the common mass of HNLs is $M = 1 \text{ GeV}$, $\Delta M = 3.98 \cdot 10^{-11} \text{ GeV}$, $X_{\omega} = 4.2$, $\delta = 3\pi/2$, $\eta = 19\pi/16$, $\text{Re } \omega = \pi/4$. See also the discussion in the main text.

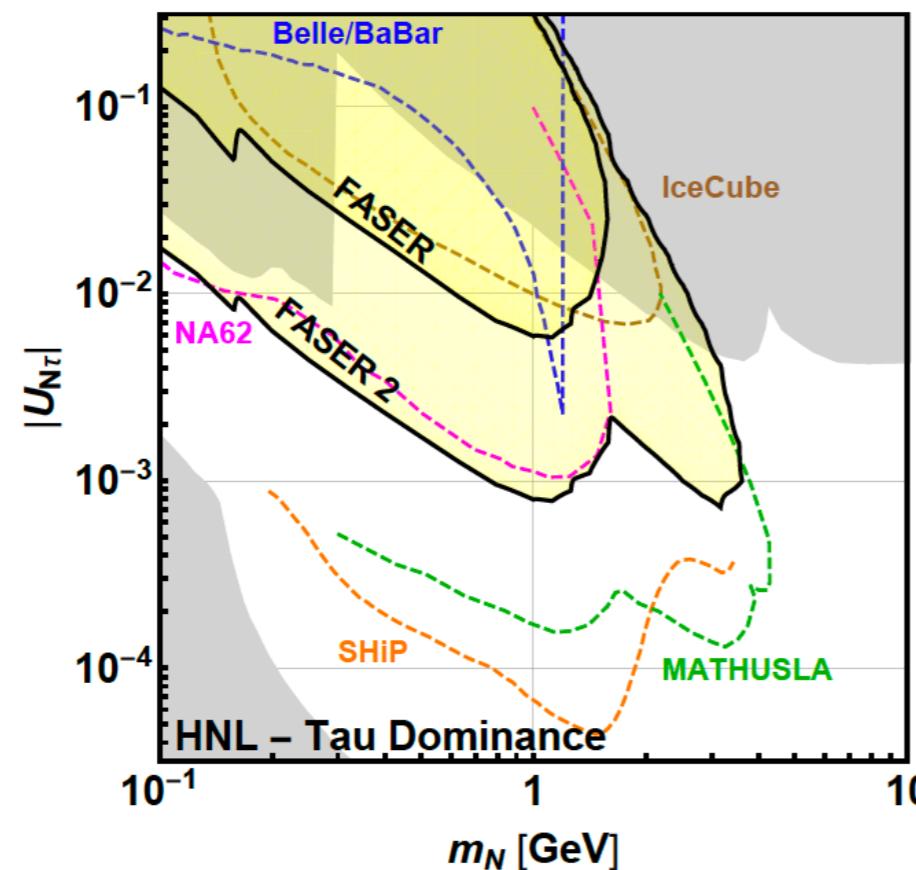
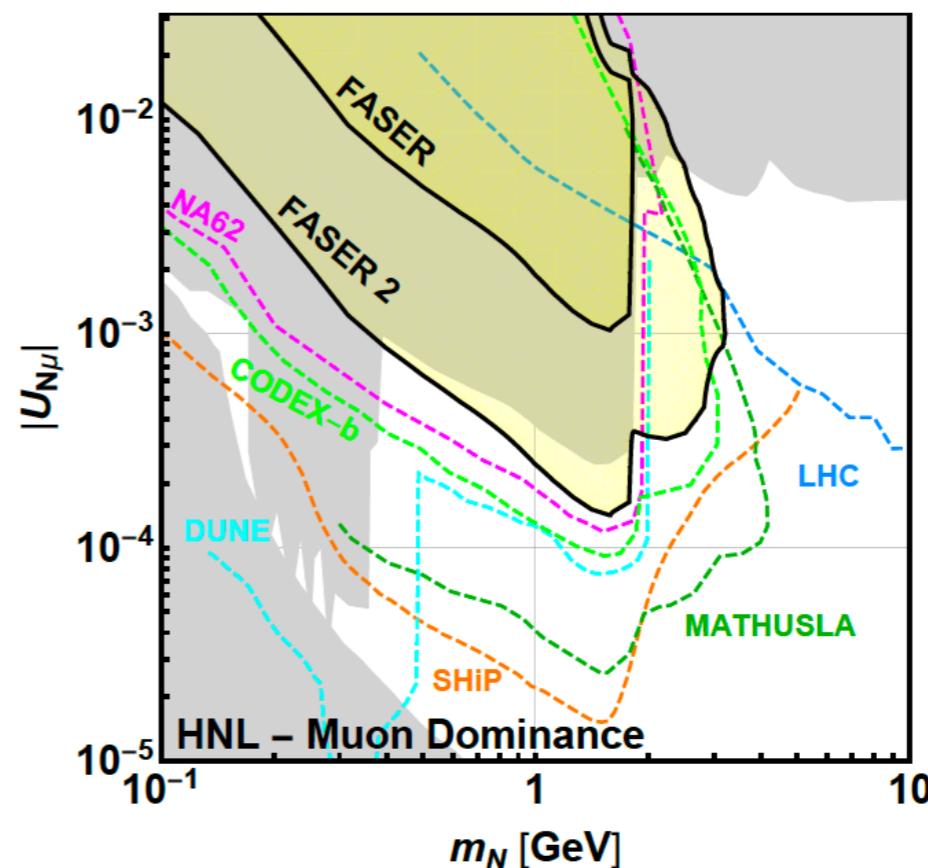
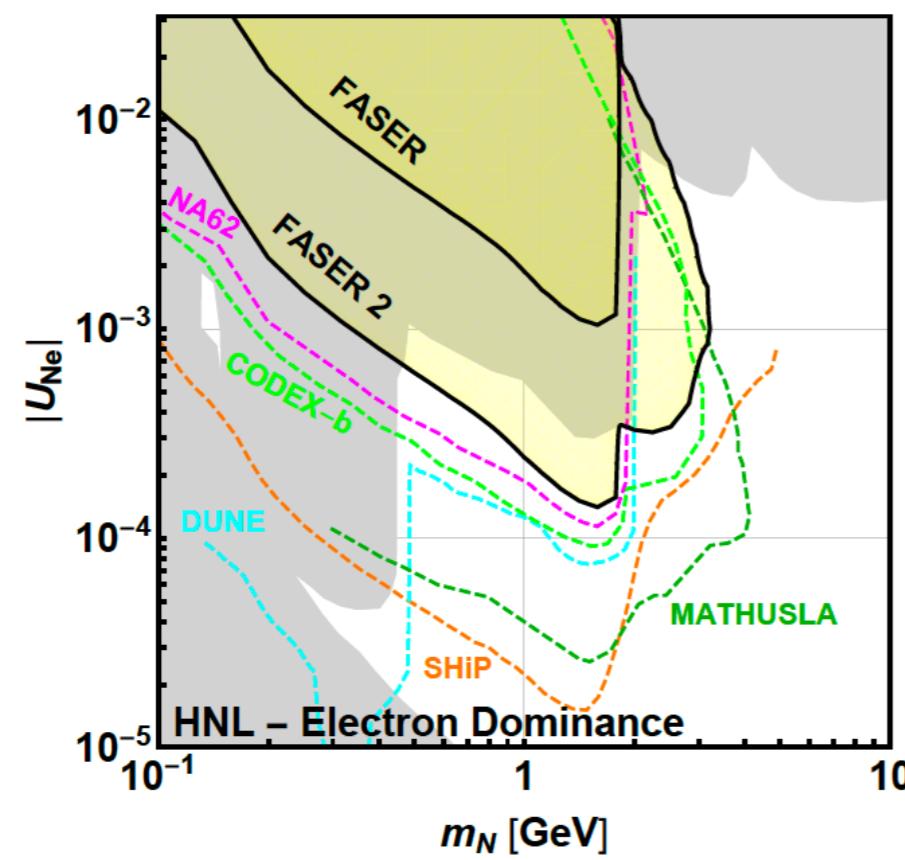
MATHUSLA



- CEPC
- ILC
- FCC-ee
- DUNE
- NA62
- SHiP
- (Possible reach if B_c contributions larger than perturbative prediction)
- SHiP
- MATHUSLA HL-LHC (W/Z)
- MATHUSLA HL-LHC (B/D-Meson)
- MATHUSLA FCC-hh (Forward) (W/Z)
- MATHUSLA FCC-hh (Standard) (W/Z)
- BBN
- Current Exp. Limits
- Neutrino Osc. ($n = 2$)
- Leptogenesis ($n = 2$)

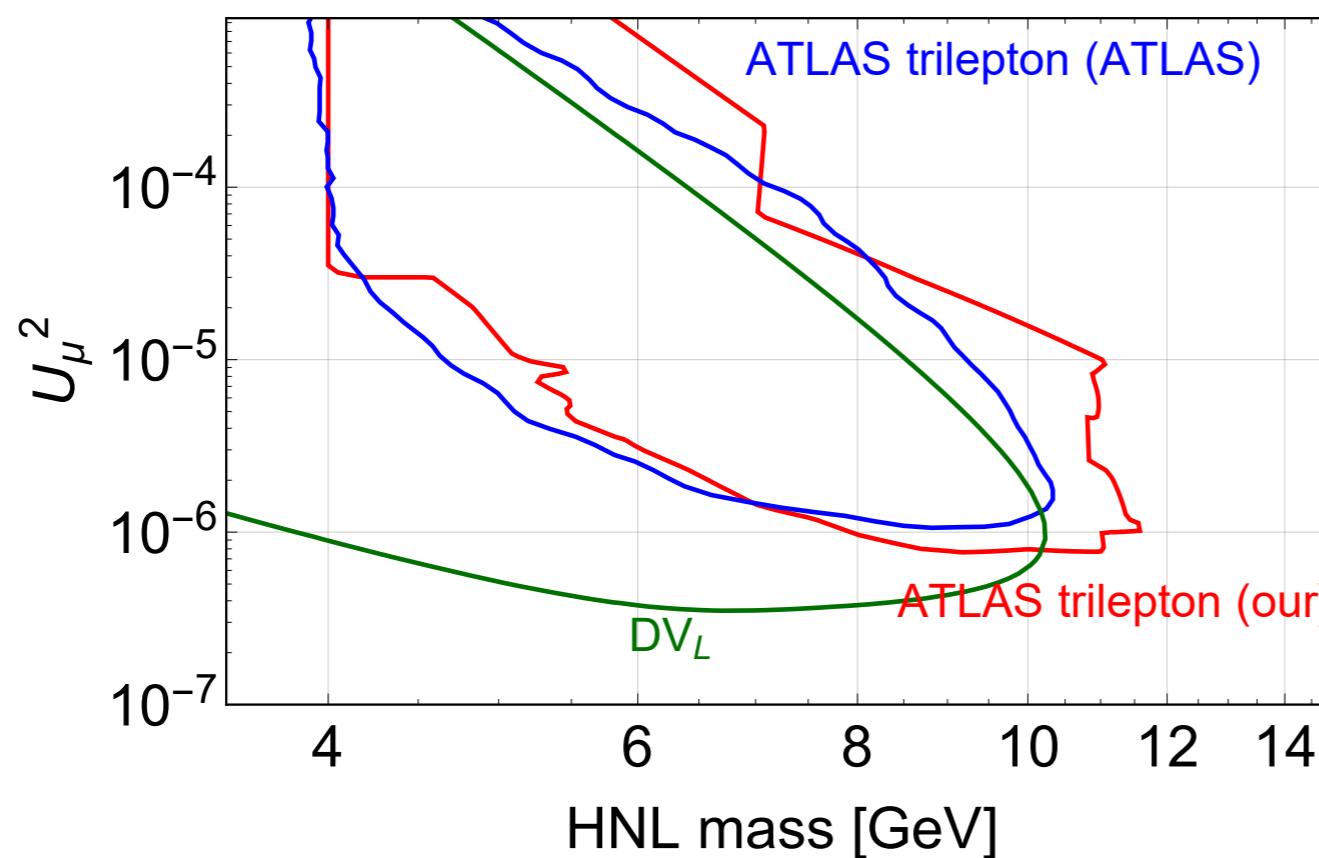
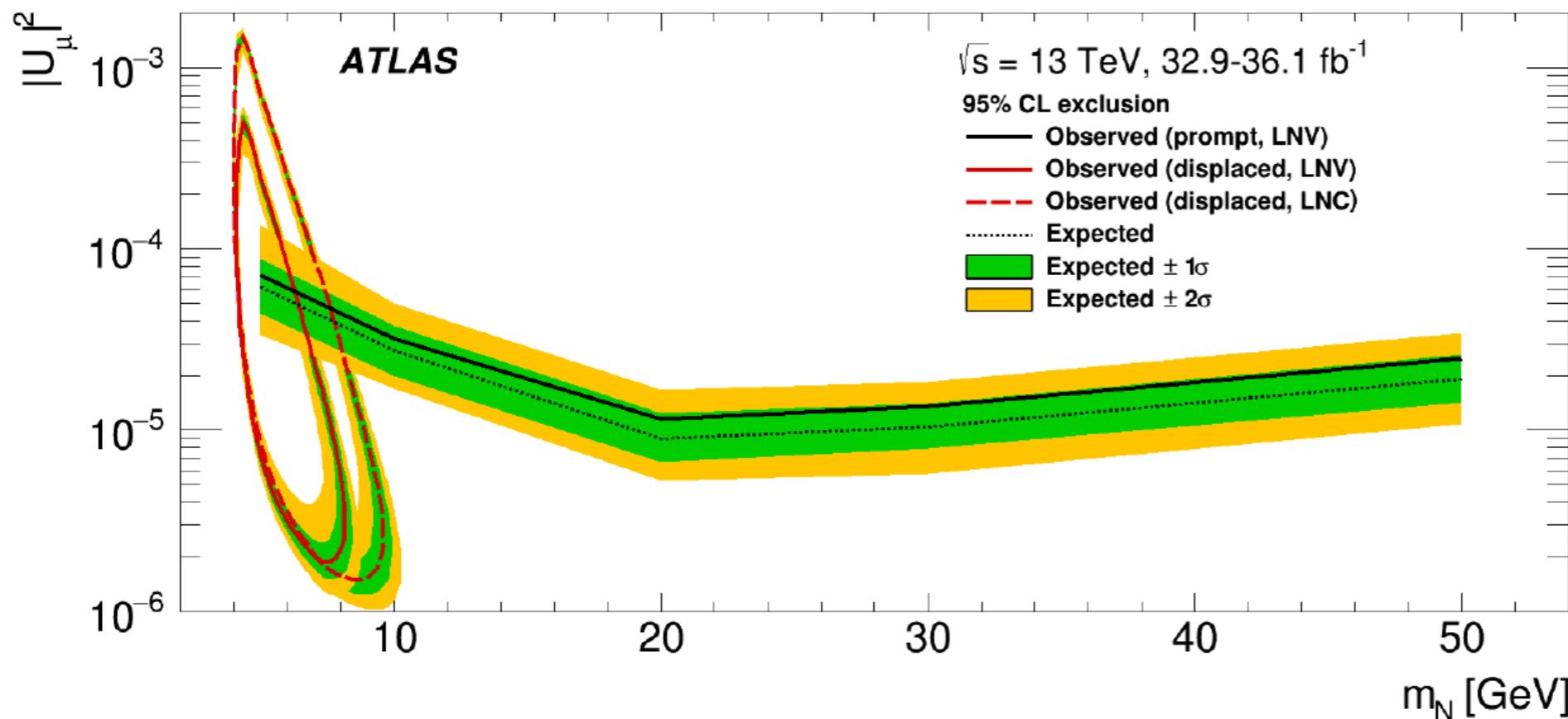
[Currin, Drewes, McCullough, Meade, Mohapatra, Sheldon, Shuve, et al. ('18)]

FASER



[FASER Collaboration ('18)]

Bounds from DV in ATLAS



$$W^+ \rightarrow \mu^+ N \\ \rightarrow \mu^+ (\mu^- \mu^+ / e^+ \nu_\mu / \nu_e)$$

[Boiarska, Bondarenko, Boyarsky, SE,
Ovchynnikov, Ruchayskiy, Timiryasov ('19)]