# **Axion Dark Matter coupled to**

# **Photons and Gravitons**

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Obata, TF & Michimura PRL**121**,161301(2018) TF, Tazaki & Toma PRL**122**,191101(2019) Nagano, TF, Obata & Michimura PRL**123**,111301(2019) TF, Tanaka, Obata & Yamada in prep.(2020)

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### Outline of Talk

- 1. Introduction
- 2. Protoplanetary Disk (Photon)
- 3. GW Interferometer (Photon)
- 4. GW Amplification (Graviton)
- 5. Summary

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### introduction



### PRESENTATION

# **Who is Dark Matter?**







PRESENTATION

### introduction



# **DM candidates**





### introduction



PRESENTATION

**DM candidates** 







# Scalar Dark Matter (∋Axion & ALPs)

Different from particle DMs: production & evolution

In this talk, we make no assumption on its production & evolution.

Oscillating Scalar Field:  $m \gg H$ 

 $\phi = (a/a_0)^{-\frac{3}{2}}\phi_0\cos(mt+\delta)$ 



 $\rho_{\phi} \propto a^{-3}, \ \delta_m \propto \text{amplitude pert. } \delta\phi(t, \mathbf{x})$ 



### introduction



# What characterizes ADM?

# • ADM can be very light. $(10^{-22} \text{eV} \leq m)$





### ADM may be coupled to gauge fields!





### introduction



# **Axion-Photon Coupling**

• Interaction term:  $\mathcal{L}_{\phi\gamma} = \frac{1}{4} g_{\phi\gamma} \phi F_{\mu\nu} \tilde{F}^{\mu\nu}$ 

# $\tilde{F}^{\mu\nu} \equiv \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} F_{\rho\sigma}$

# **Axion-Graviton Coupling**

• Interaction term:  $\mathcal{L}_{\phi g} = \frac{1}{4} g_{CS} \phi R_{\mu \nu \rho \sigma} \tilde{R}^{\mu \nu \rho \sigma}$ 

 $\tilde{R}^{\mu\nu\rho\sigma} \equiv \frac{1}{2} \epsilon^{\mu\nu\alpha\beta} R^{\mu\nu}_{\ \alpha\beta}$ 

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# **Axion-Photon Coupling**

Interaction term:  $\mathcal{L}_{\phi\gamma} = \frac{1}{4}g\phi F_{\mu\nu}\tilde{F}^{\mu\nu}$ 

 $\left[\partial_t^2 - \partial_i^2\right] \mathbf{A} = -g\dot{\phi}\nabla \times \mathbf{A}$ Photon:

Axion:  $\left[\partial_t^2 - \partial_i^2 + m^2\right]\phi = -g\dot{A}\cdot\nabla\times A$ 



### **Current constraint**







Assume background DM axion:  $\phi(t) = \phi_0 \cos(mt)$ 

 $-m\phi_0\sin(mt)$ 

# Photon EoM: $[\partial_t^2 - \partial_i^2] \mathbf{A} = -g \dot{\phi} \nabla \times \mathbf{A}$





Assume background DM axion:  $\phi(t) = \phi_0 \cos(mt)$ 

 $-m\phi_0\sin(mt)$ 

Photon EoM: 
$$[\partial_t^2 - \partial_i^2] \mathbf{A} = -g \dot{\phi} \nabla \times \mathbf{A}$$

 $i\widehat{\boldsymbol{k}} \times \boldsymbol{e}_{L,R} = \pm \boldsymbol{e}_{L,R}$ 

Dispersion relations of Left/Right Pol. are modified

$$\omega_{L,R}^2 = k^2 \left[ 1 \pm g \phi_0 \frac{m}{k} \sin(mt) \right] \qquad \bigoplus_{\text{left handed}} p_{\text{iff handed}}$$

Speed of light changes depending on polarization!





Another consequence: Rotation of liner pol. Plane

Linear pol. Photon can be  $\begin{pmatrix} 1\\ 0 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 1\\ i \end{pmatrix} + \frac{1}{2} \begin{pmatrix} 1\\ -i \end{pmatrix}$ , decomposed into circular pol.

With ADM BG<br/>phase velocity<br/>are different, $\frac{e^{ikT}}{2} \left[ e^{i\int_t^{t+T}\delta\omega dt} \begin{pmatrix} 1\\i \end{pmatrix} + e^{-i\int_t^{t+T}\delta\omega dt} \begin{pmatrix} 1\\-i \end{pmatrix} \right]$  $\Rightarrow$  polarization<br/>plane rotates $= e^{ikT} \left( \frac{\cos(\int_t^{t+T}\delta\omega dt)}{-\sin(\int_t^{t+T}\delta\omega dt)} \right).$ 

# Birefringence



Rotation angle synchronizes with Axion

$$\theta(t,T) = \int_t^{t+T} \delta\omega(t) \,\mathrm{d}t = -\frac{g_{a\gamma}}{2} \left[\phi(t+T) - \phi(t)\right],$$

Motion of the linear polarization plane



# Birefringence



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# Birefringence



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Motion of the linear polarization plane





Rotation angle is  $\sim 10^{-2}$  for largest coupling g

 $\rho_{\rm DM} = m^2 \phi_0^2 / 2 \approx 0.3 \ {\rm GeV/cm^3}$ 

 $g_{12} \equiv g_{a\gamma}/(10^{-12} \text{GeV}^{-1}),$ 

 $m_{22} \equiv m/(10^{-22} \text{eV})$ 

 $\theta(t,T) \approx 2 \times 10^{-2} \sin \Xi \sin(mt + \Xi + \delta) g_{12} m_{22}^{-1}$ 

 $\Xi \equiv mT/2 \approx 10^2 (T/10 \text{pc}) m_{22}$ 

How can we observe this?

In astro, we don't know the initial polarization plane. Can't measure  $\theta$  ...





# **ProtoPlanetary Disk**

Observations of PPD can be used!

PPD is a flattened gaseous object surrounding a young star.

PPDs are bright simply by scattering the central star's light.

Real data

Artist's image









# **Polarization of PPD**

Scattered light should be polarized perpendicular to the scattering plane (=this monitor).

Initial polarization Plane is known!!





**Obsevation of PPD** 

### [Hashimoto et al. APJL729:L17(2011)]

We expect a concentric pattern of linear polarization.

### Our Simulation without Axion DM











# Is this angle 90° or not?



# **Obsevation of PPD** [Hashimoto et al. APJL729:L17(2011)]

<sup>2</sup>olarized Intensity [mJy/(arcsec)<sup>2</sup>

We expect a concentric pattern of linear polarization.

### Our Simulation without Axion DM



### **Observation by SUBARU**



AB Aurigae (160pc away)



[Hashimoto et al. APJL729:L17(2011)]

# **Obsevation of PPD**

The observation data reveals



[TF. Tazaki & Toma (2018)] See also 1903.02666 for CMB

# **New constraint**

Compared to the prediction, we obtain the best constraint on g of ultralight ADM ( $m \sim 10^{-22}$  eV)



### Fedderke+ PRD100,015040(2019)







# Long-term Obs of PPD

If we observe a PPD for longer time than  $m^{-1}$ , the periodic shift of  $\theta$  should be detected.



### Chigusa, Moroi & Nakayama: 1911.09850



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# Can we use GW interferometers

# to search for Axion DM?





[DeRocco & Hook, PRD 98, 035021 (2018)]

# Yes!! Because GW interferometer is



Measure the other polarization component (horizontal) by filtering the original pol. component (vertical)





# **Coexist with GW observation**

Tiny signal compensated by long operation time



Additional instruments at the tail enable interferometers to probe ADM during the GW observation run without loosing any sensitivity to GWs Long Run!



# Sensitivity Curve for 1 year run





Sensitivity Curve for 1 year run





# **DANCE Act.1** has started!

### PRESENTATION

Prototype exp. (Act.1) is being constructed in U. Tokyo. (Ando lab.)

We got a grant (35kUSD/yr) and applied for another one to extend our experiment.

The first result (1m, 3months) will be obtained within a year

# Image: Fill AOM FOM FOM FOM FOM PRESERVE 周辺長1m 7/ネス3×10<sup>3</sup> Image: Fill AOM FOM FOM PRESERVE アクシオン信号 Collimator PRESERVE Image: Fill AOM FOM PRESERVE アクシオン信号 Collimator PRESERVE Image: Fill AOM FOM PRESERVE アクシオン信号 Collimator PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE Image: Fill AOM FOM PRESERVE Fill AOM FOM PRESERVE

DANCE Act 1の構成



### **Recent Proposals for ADM Search**



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### introduction



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### [Yoshida & Soda (2017)]

### **GW** amplification

### [arXiv:1708.09592v2]

### Exploring the string axiverse and parity violation in gravity with gravitational waves

Daiske Yoshida<sup>\*</sup> and Jiro Soda<sup>†</sup> Physics Department, Kobe University. (Dated: October 17, 2018)

We study gravitational waves in the presence of the string axion dark matter and the gravitational Chern-Simons coupling. We show that the parametric resonance of gravitational waves occurs due to the axion coherent oscillation and the circular polarization of gravitational waves is induced by the Chern-Simons coupling. For example, the gravitational waves should be enhanced ten times every  $10^{-8}$  pc in the presence of the axion dark metter with were  $10^{-10}$  eV provided the employee enstant  $\ell = 10^8$  km. After 10 kpc propagation, the amplitude of GWs are enhanced by  $10^{10^{12}}$  and the polarization of GWs becomes completely circular. However, we have never observed these signatures. This indicates that the Chern-Simons coupling constant and/or the abundance of the light string axion should be strongly constrained than the current limits  $\ell \leq 10^8$  km and  $\rho \leq 0.3$  GeV/cm<sup>3</sup>.

PACS numbers: 04.30.-w, 14.80.Va,95.35.+d

Keywords: string axiverse, parity violation in gravity, gravitational waves





# **GW** amplification

### Interaction term

$$S_{\rm CS} = \frac{1}{4} \alpha \, \int_{\mathcal{V}} dx^4 \sqrt{-g} \, \Phi \tilde{R} R$$

### Oscillating axion

$$\Phi = \Phi_0 \cos(m\eta) \; ,$$

### **EoM for GWs**

$$h_{\rm A}'' + \frac{\epsilon_{\rm A}\delta\,\cos(m\eta)}{1 + \epsilon_{\rm A}\frac{k}{m}\delta\,\sin(m\eta)}k\,h_{\rm A}' + k^2h_{\rm A} = 0$$

### Small parameter

$$\delta \equiv \frac{\alpha}{\kappa} m^2 \Phi_0$$

### [arXiv:1708.09592v2]

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[Jung, Kim, Soda and Urakawa (2020)]

# **GW** amplification





FIG. 2. The upper limit on the axion Chern-Simons coupling  $\ell$ , assuming the absence of a resonance peak in the 11 GW observations at LIGO O1+O2. The gray shaded re-

Taking into account the axion coherence, the amplification becomes mild.

But they still claim a sharp resonant peak in GW spectrum is produced.

### Our on-going work



# Setup

[TF, Obata, Tanaka & Yamada in prep]

### Action:

$$S \equiv \int d^4x \sqrt{-g} \left[ \frac{M_{\rm Pl}^2}{2} R + \frac{M_{\rm Pl}\ell_{\rm dCS}^2}{4\sqrt{2}} \phi^* RR - \frac{1}{2} \left( \nabla_\mu \phi \nabla^\mu \phi + 2V(\phi) \right) + \mathcal{L}_{\rm mat} \right]$$

# $\begin{array}{ll} \mbox{Oscillating axion} & \mbox{Axion amplitude} \\ \phi(t,x) = \frac{1}{2} \left( \phi_0(x) e^{-imt} + \phi_0^*(x) e^{imt} \right) & \ensuremath{\varepsilon}(x) \equiv \frac{\sqrt{2}\ell_{\rm dCS}^2}{M_{\rm Pl}} m^2 \phi_0(x) \\ \\ \mbox{EoM for GWs} \\ (\partial_t^2 - \partial_x^2) h_{\rm R/L} - \frac{1}{2} i \lambda_{\rm R/L} \left( \varepsilon(x) e^{-imt} + \varepsilon^*(x) e^{imt} \right) \partial_t \partial_x h_{\rm R/L} = 0, \end{array}$

So far, the same as Kobe group.



### **Analysis on resonance**

Landau says a resonance is caused by the interaction btw 2 opposite modes,  $\omega \approx m/2$  and  $\omega \approx -m/2$ .

Ansatz in the constant amplitude & phase case ( $\epsilon = const$ .)

$$h_{\rm R/L}(t,x) = A_0 e^{-i\omega t + ikx} + B_0 e^{-i(\omega - m)t + ikx} + c.c.$$

EoM yields the dispersion relation

$$\delta \omega^2 = \delta k^2 - \frac{m^2}{64} |\varepsilon|^2 \qquad \omega \approx k \approx m/2.$$

Resonant amplification within the band  $|\delta k| < \frac{m|\varepsilon|}{2}$ 

### Our on-going work



### Wave packet

We know how a plane wave behaves:

$$h_{\delta\omega} \propto \exp\left[-i\delta\omega\left(t-x\,\delta\hat{k}\right)\right], \quad \hat{\delta k} \equiv \sqrt{1+\frac{|\varepsilon|^2}{64}\frac{m^2}{\delta\omega^2}},$$

As more realistic GW signal, consider a Gaussian wave packet  $\propto \exp[-\delta\omega^2/2K^2]$ .

$$h_{\text{packet}} = \frac{1}{\sqrt{2\pi}K} e^{-im(t-x)/2} \int d\delta\omega \, e^{f(\delta\omega)} \qquad f(\delta\omega) = -i\delta\omega \left(t - x\sqrt{1 + \frac{|\varepsilon|^2}{64}\frac{m^2}{\delta\omega^2}}\right) - \frac{\delta\omega^2}{2K^2}$$

Saddle point integral gives analytic results which respect the causality

$$h_{\text{packet}}(t > x) \sim \exp\left[\frac{m|\varepsilon|}{8}\sqrt{t^2 - x^2}\right]$$
$$h_{\text{packet}}(t < x) \sim \exp\left[-\frac{1}{2}K^2(x - t)^2\right]$$

### Numerical results



### **Causal amplification**



**mx/2**π

GW packet itself is not amplified much, but it gets a long growing tail behind it.







**mt/2***π* 

GW packet itself is not amplified much, but it gets a long growing tail behind it.





[TF, Obata, Tanaka & Yamada in prep]

# **Axion Coherence**

Axion oscillation is **NOT** coherent over a scale  $\lambda_c \approx (mv)^{-1}$ .

 $\phi(t, x) = \Phi(x) \cos(mt + \delta(x))$  and  $\delta(x)$  varies

In our formulation

A simple simulation inside Milky way galaxy ( $v \approx 10^{-3}$ )

 $\phi_{0}(x) = \Phi(x)e^{i\delta(x)}$ Phase  $\delta(x)$   $\varepsilon(x) \equiv \frac{\sqrt{2}\ell_{dCS}^{2}}{M_{Pl}}m^{2}\phi_{0}(x)$ Account for  $\epsilon(x)$  !



### Our on-going work



### **Re-analysis on resonance**

Ansatz in the varying amplitude & phase case ( $\epsilon \neq const$ .)

$$h_{\rm R/L}(t,x) = \left(A(x) e^{-imt/2} + B(x) e^{imt/2}\right) e^{-i\delta\omega(t-x) + im/2x}$$

EoM yields our master equation w.r.t.  $X \equiv A'/A$ 

$$X' + X^2 + \left(2i\delta\omega - \frac{\varepsilon'}{\varepsilon}\right)X + \frac{m^2}{64}|\varepsilon|^2 = 0$$

We found a consistent analytic solution for  $|\epsilon| \ll 1$ 

$$X(x) = \frac{m^2}{64} \int_x^{x_{\text{end}}} \mathrm{d}y \,\varepsilon(x) \varepsilon^*(y) e^{-2i\delta\omega(x-y)}$$

Evaluate it with a Gaussian  $\epsilon \qquad \langle \varepsilon(x)\varepsilon^*(y)\rangle = |\overline{\varepsilon}|^2 \exp\left[-\frac{(x-y)^2}{2\lambda_{\rm ob}^2}\right]$ 

### Our on-going work



### **Incoherent** amplification







### How large is C?

Axion DM starts oscillating at  $m = H(t_{osc})$  and then  $\phi$  is homogeneous.

After that, the amplitude decreases and the incoherence develops.

Amplification is most efficient at  $t_{osc}$  in the early universe!?

Require the backreaction not to alter the Axion DM dynamics.

GW Amplification  $h_{after} = e^{N_*} h_{before}$  is mild  $N_* < 10$  at  $H = H_*$ 

Then we can estimate the parameter  ${\mathcal C}$  at present

$$\mathcal{C} \approx 3 \times 10^{-2} \,\Omega_A^{-1}(t_{\rm eq}) \left(\frac{N_*}{10}\right) \left(\frac{L}{10 \,\rm kpc}\right) \left(\frac{\rho_{\rm DM}}{0.3 \,\rm GeV/\,cm^3}\right) \left(\frac{v}{7 \times 10^{-4}}\right)^{-1} \left(\frac{H_*}{H(t_{\rm eq})}\right)^{-1/2} \,\rm e^{-1/2}$$

No significant amplification by Axion DM....



### Our on-going work



# Way out??

If the axion is not DM, there may be a chance to have great amplifications.

### Conditions

- Axion has to start oscillating well after m = H
- Non-DM axion forms clouds

### **Preliminary estimate**

$$\mathcal{C} = \frac{1}{2} \left( \frac{3\sqrt{\pi^7/2} N_*^2 \left( m\ell_{\rm dCS} \right)^4}{\left( L_1 H_* \right)^4} \right)^{1/3} \approx 10 \left( \frac{N_*}{10} \right)^{2/3} \left( m\ell_{\rm dCS} \right)^{4/3} \left( L_1 H_* \right)^{-4/3}$$

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# Summary



### Axion DM may be coupled to photon & graviton

### Photon coupling causes **Birefringence**

Observations of protoplanetary disks are useful to search for ultralight ADM (m  $\sim 10^{-22}$ )

GW interferometer are sensitive to ADM with  $10^{-16}$ eV  $< m < 10^{-12}$ eV

# Graviton coupling causes GW amplification

GW packet itself is not enhanced but gets a amplified tail

Considering cosmology, ADM won't cause significant amplification.



# Thank you !