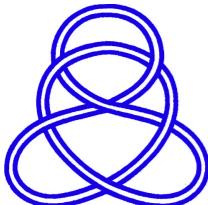
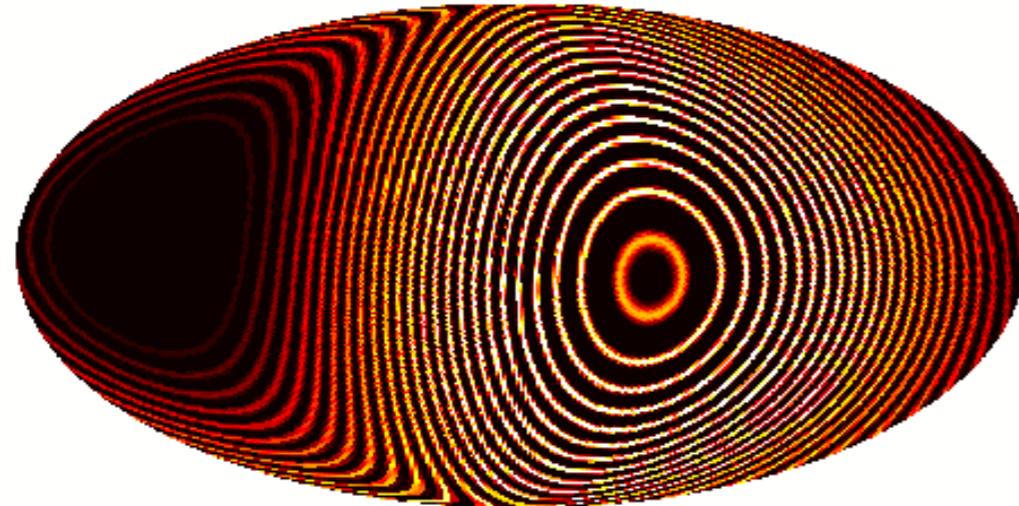


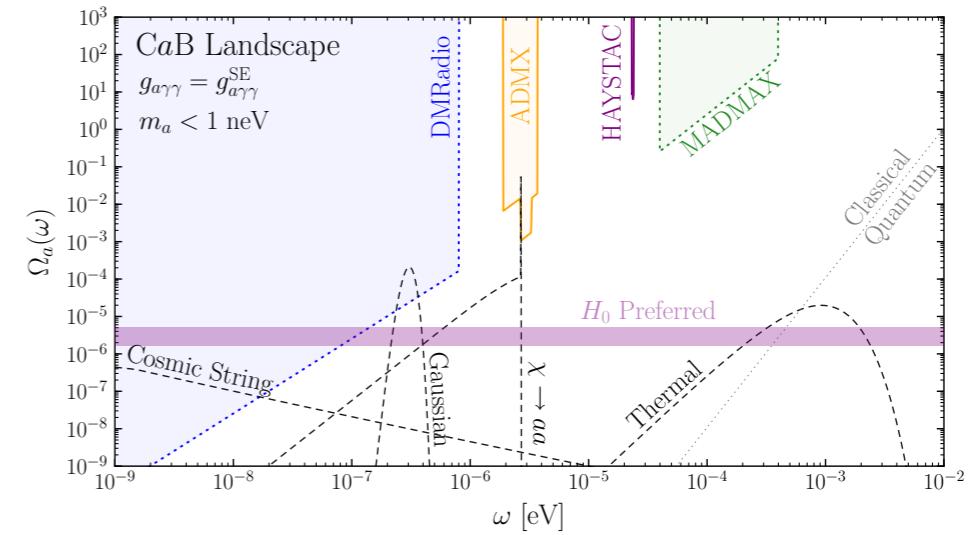
New Ideas for the Axion Dark Matter Program

NICK RODD | KAVLI IPMU | 12 MAY 2021

Dark Matter Interferometry 2009.14201 w/ Foster, Kahn, Nguyen, Safdi



The Cosmic Axion Background 2101.09287 w/ Dror, Murayama



Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$



Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

Introduces corrections to Maxwell's equations

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma} \mathbf{B} \cdot \nabla a$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\partial_t \mathbf{B}$$

$$\nabla \times \mathbf{B} = \partial_t \mathbf{E} + \mathbf{J} - g_{a\gamma\gamma} (\mathbf{E} \times \nabla a - \mathbf{B} \partial_t a)$$



Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a (\tilde{F} \tilde{F})$$

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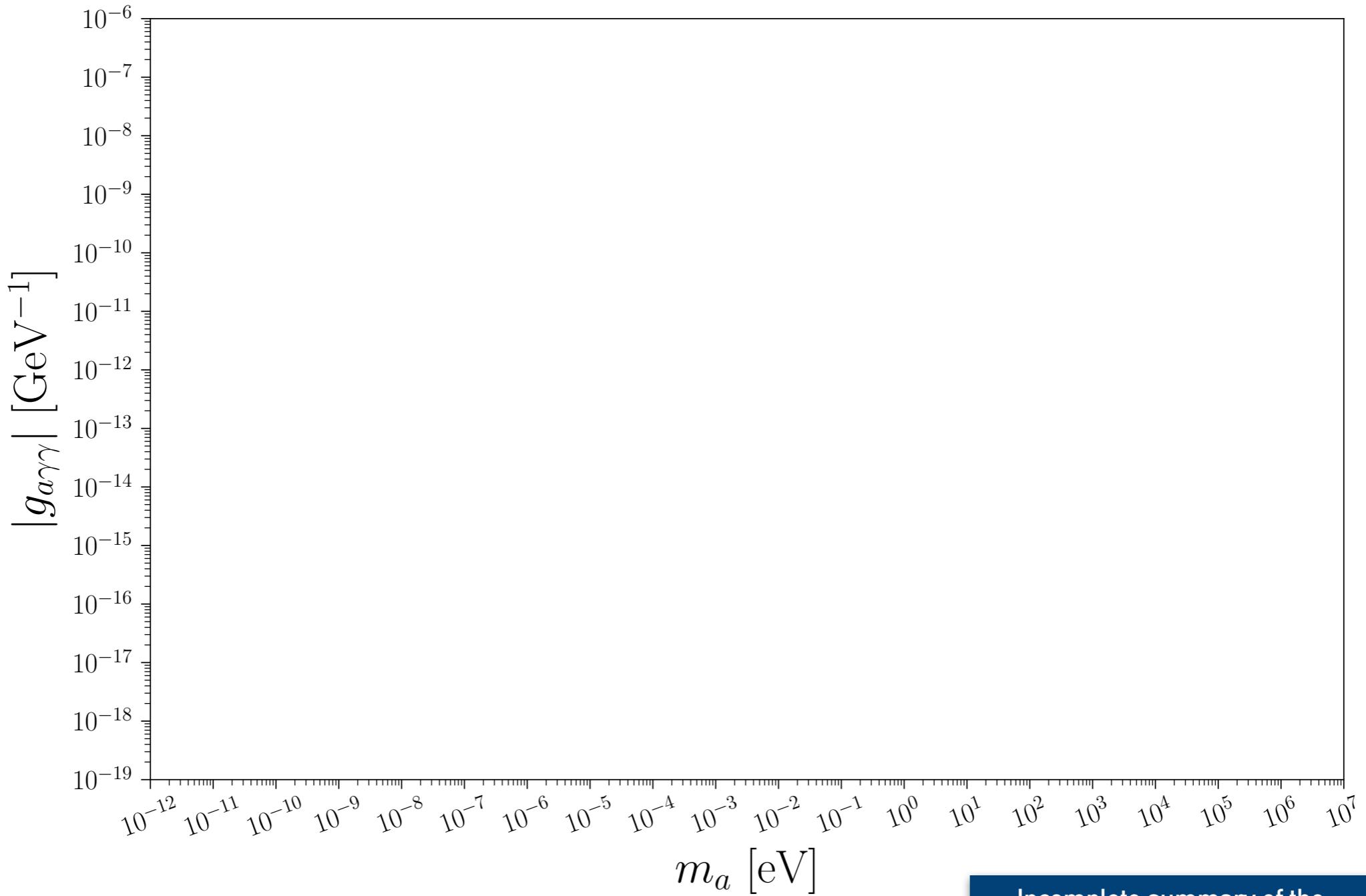
Suppressed for non-relativistic DM axions

Focus of axion DM searches



Motivation

$$\mathcal{L} \supset -\frac{1}{4} g_{a\gamma\gamma} a(F\tilde{F})$$

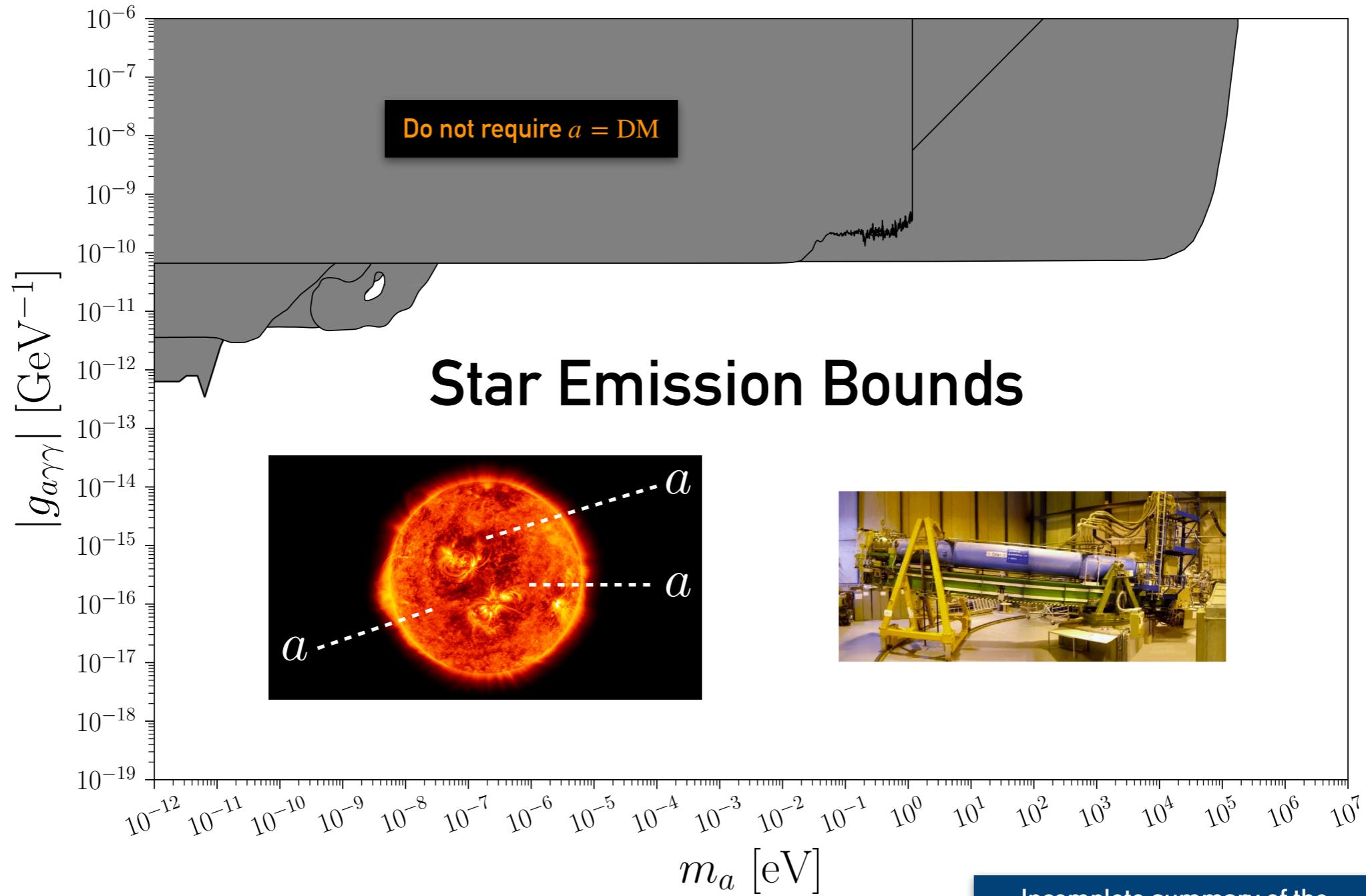


Incomplete summary of the
landscape, partially based on
github.com/cajohare/AxionLimits



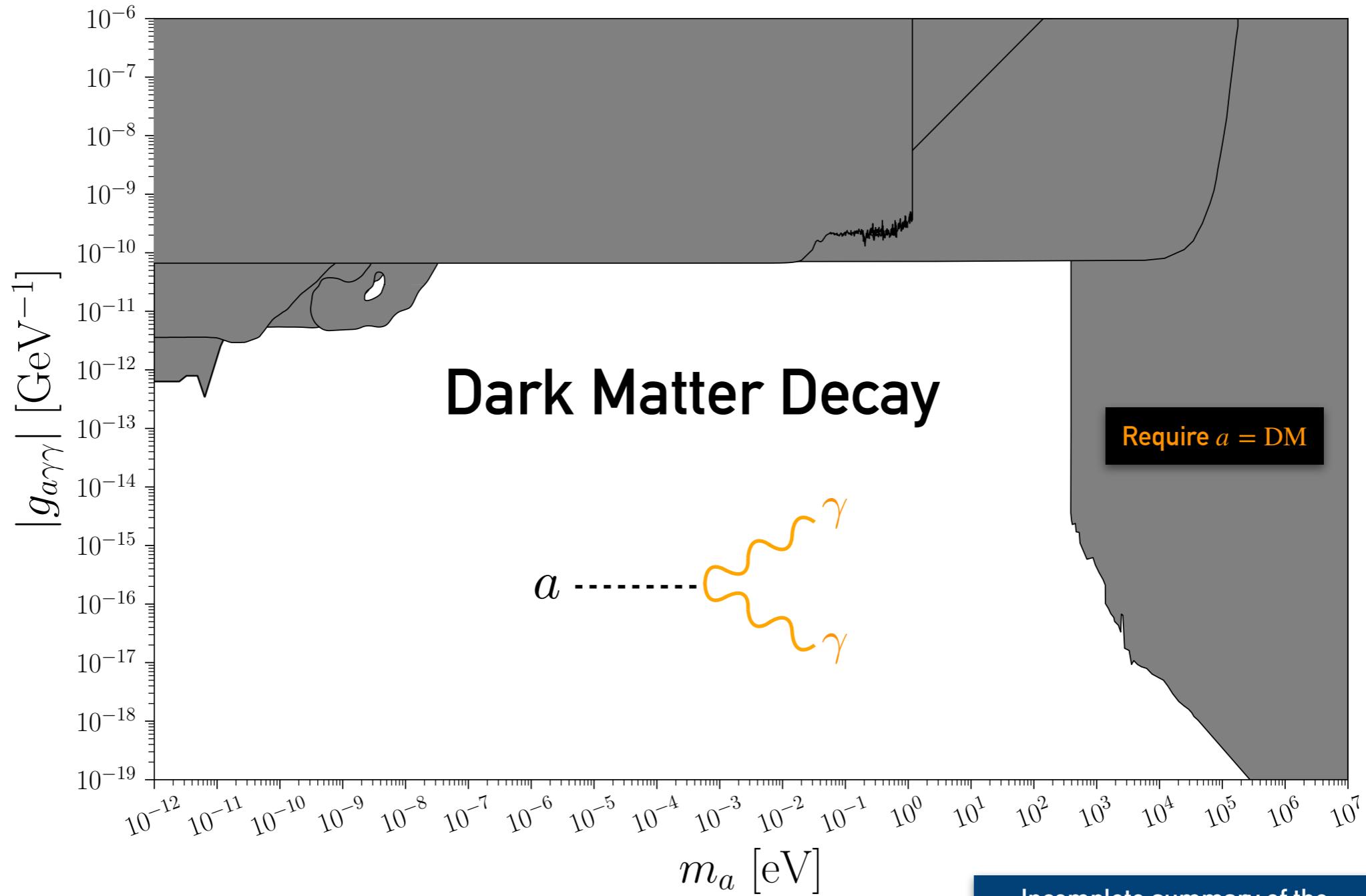
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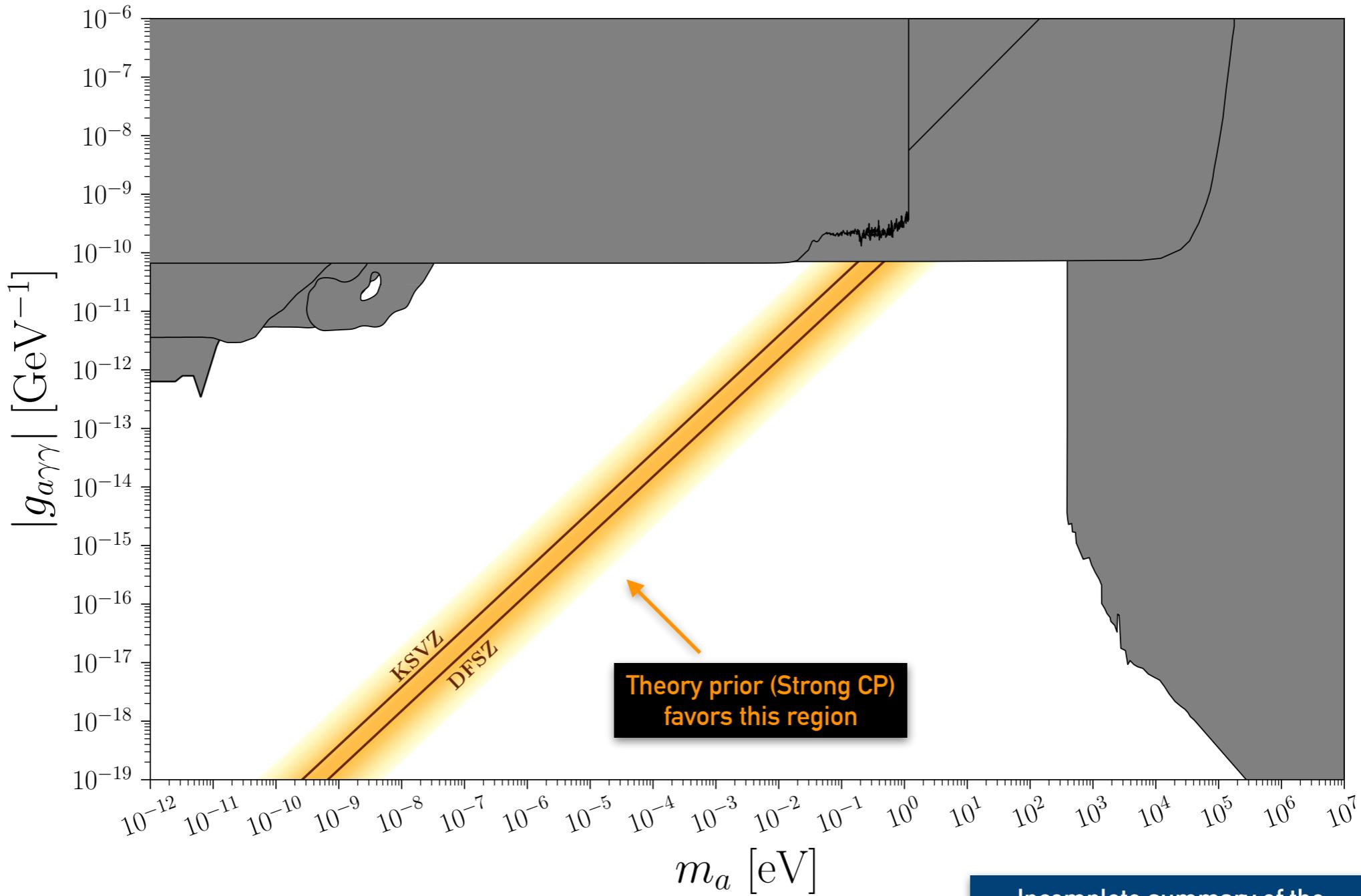
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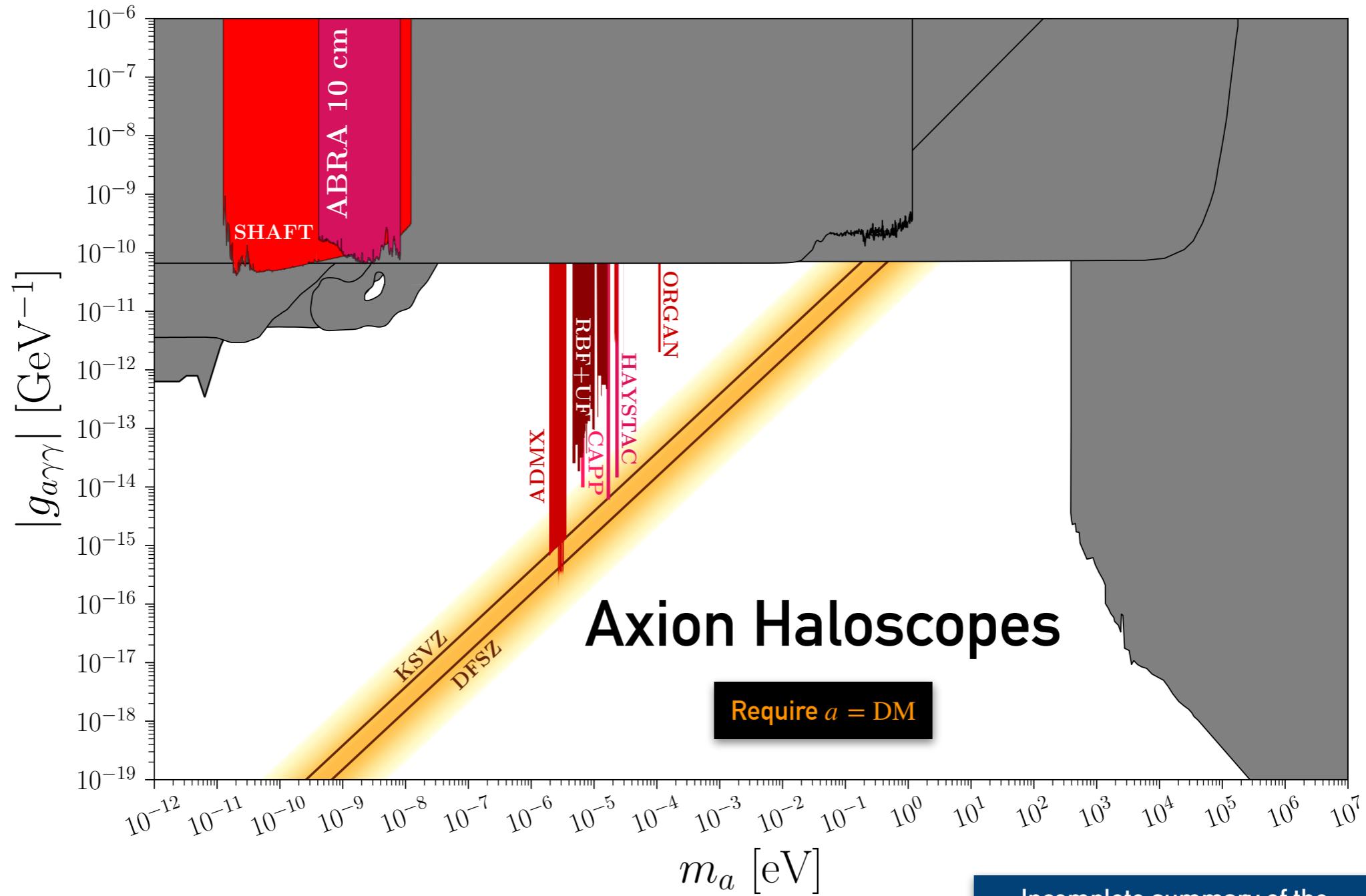


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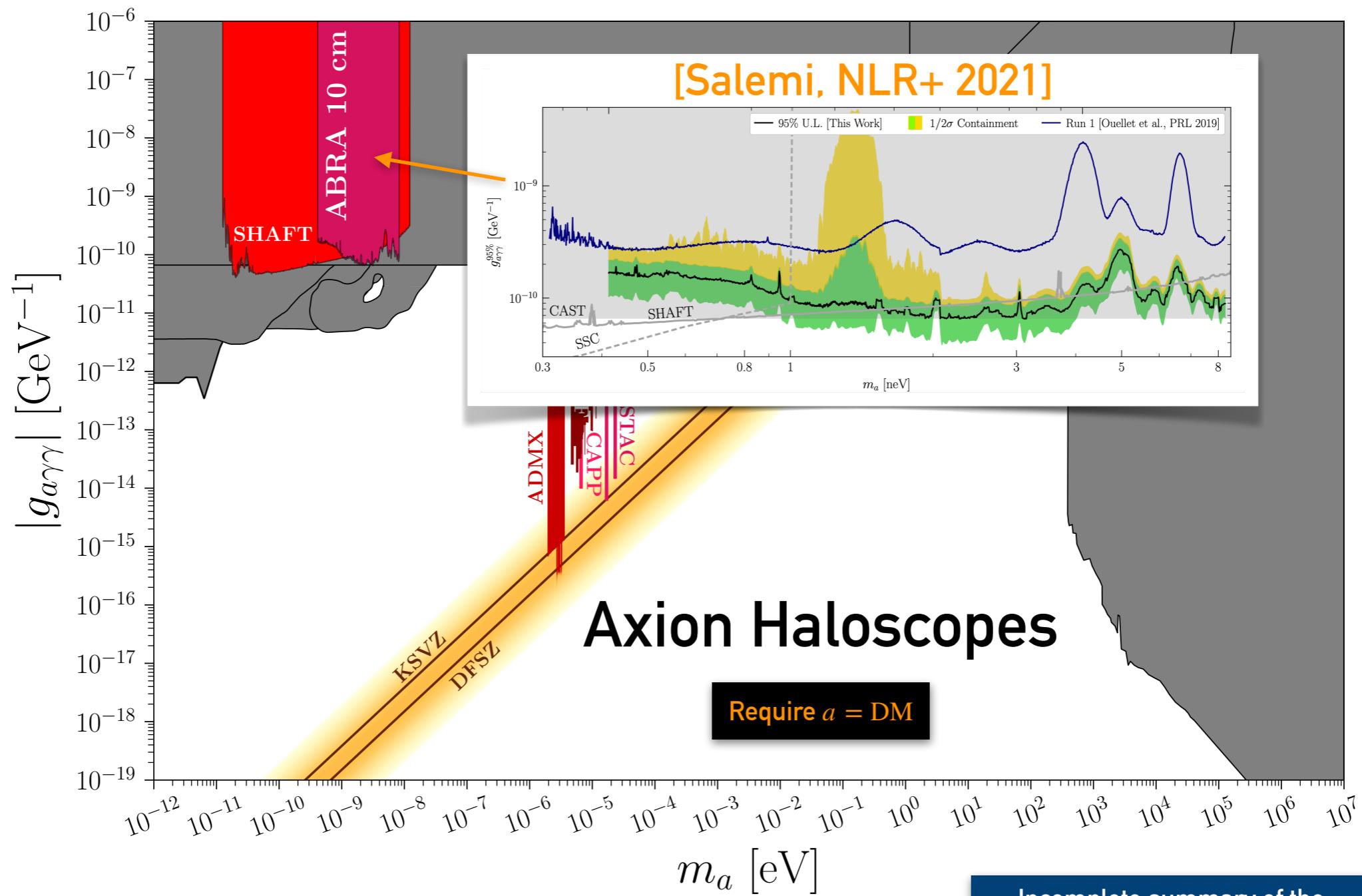
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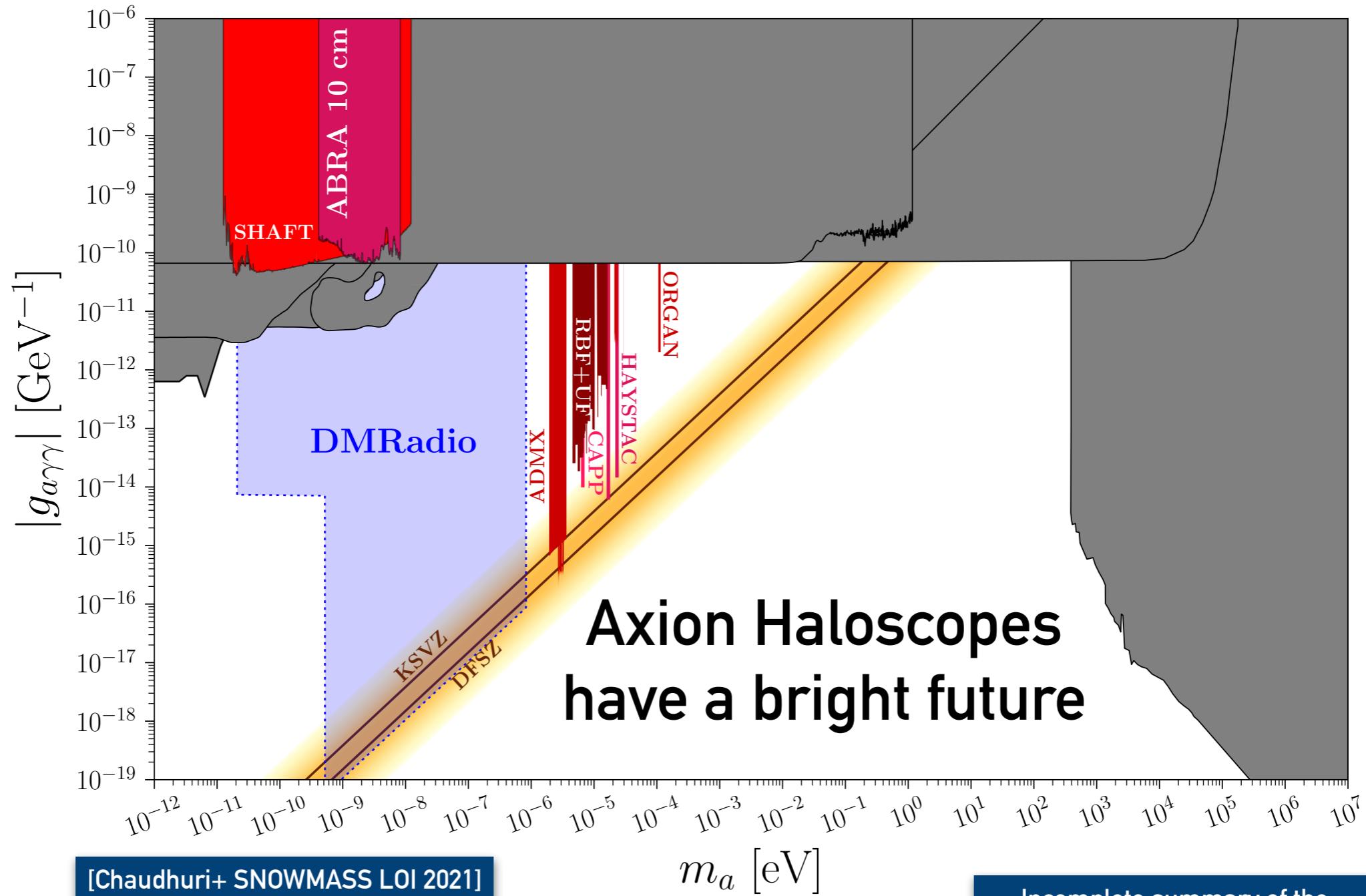
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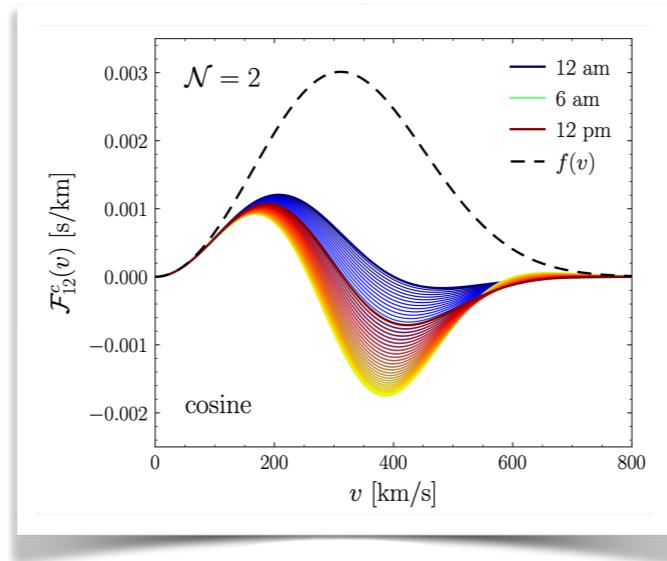
Outline

Two new ideas for exploiting this progress



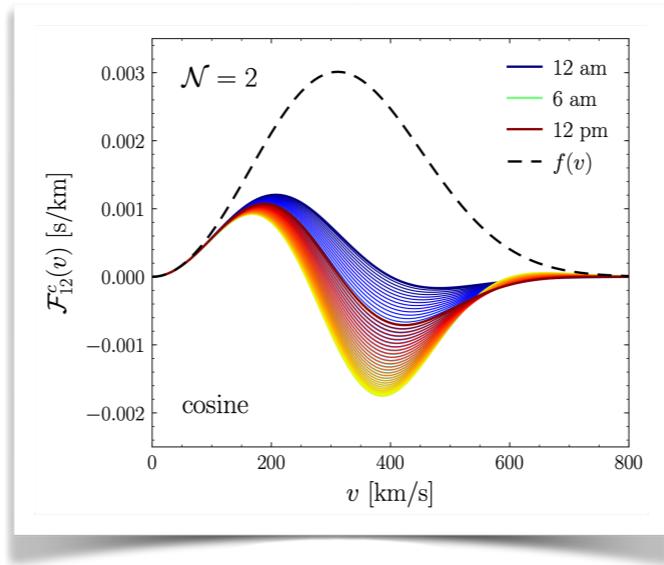
Outline

1. More information for DM searches? Dark Matter Interferometry

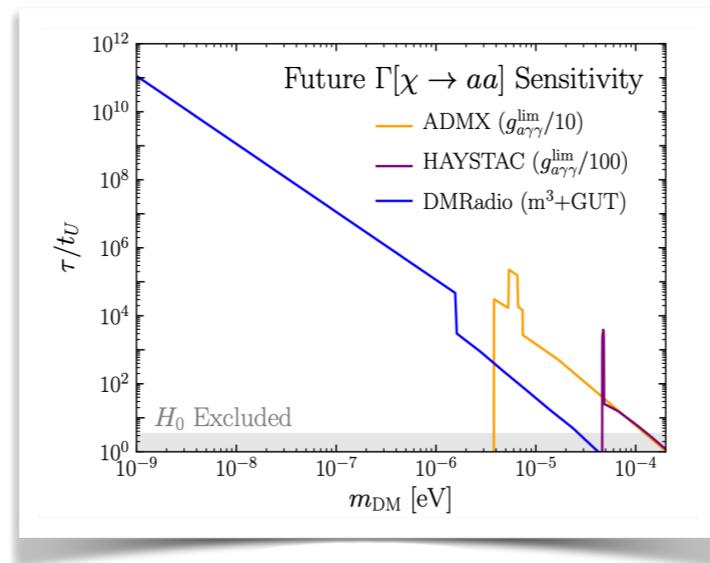


Outline

1. More information for DM searches? Dark Matter Interferometry



2. What else could these instruments see? The Cosmic Axion Background



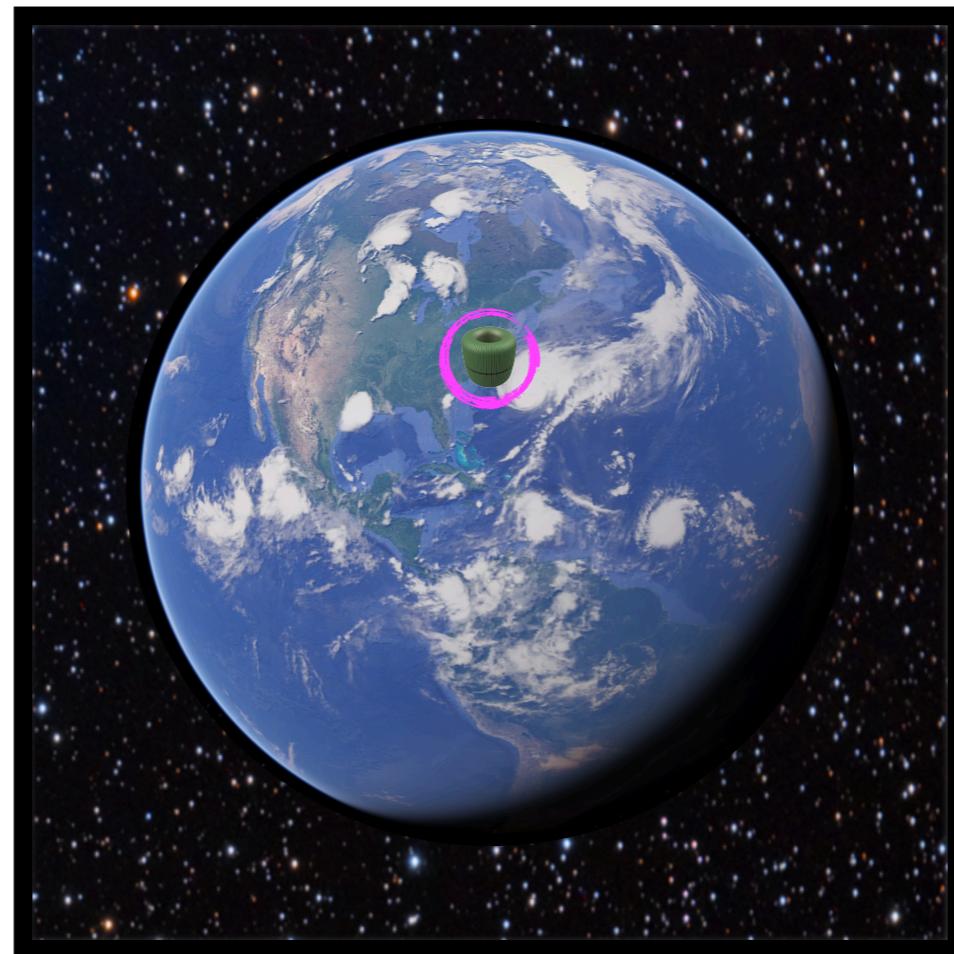
Dark Matter Interferometry

2009.14201

w/ Josh Foster, Yoni Kahn,
Rachel Nguyen, Ben Safdi

Basic Idea

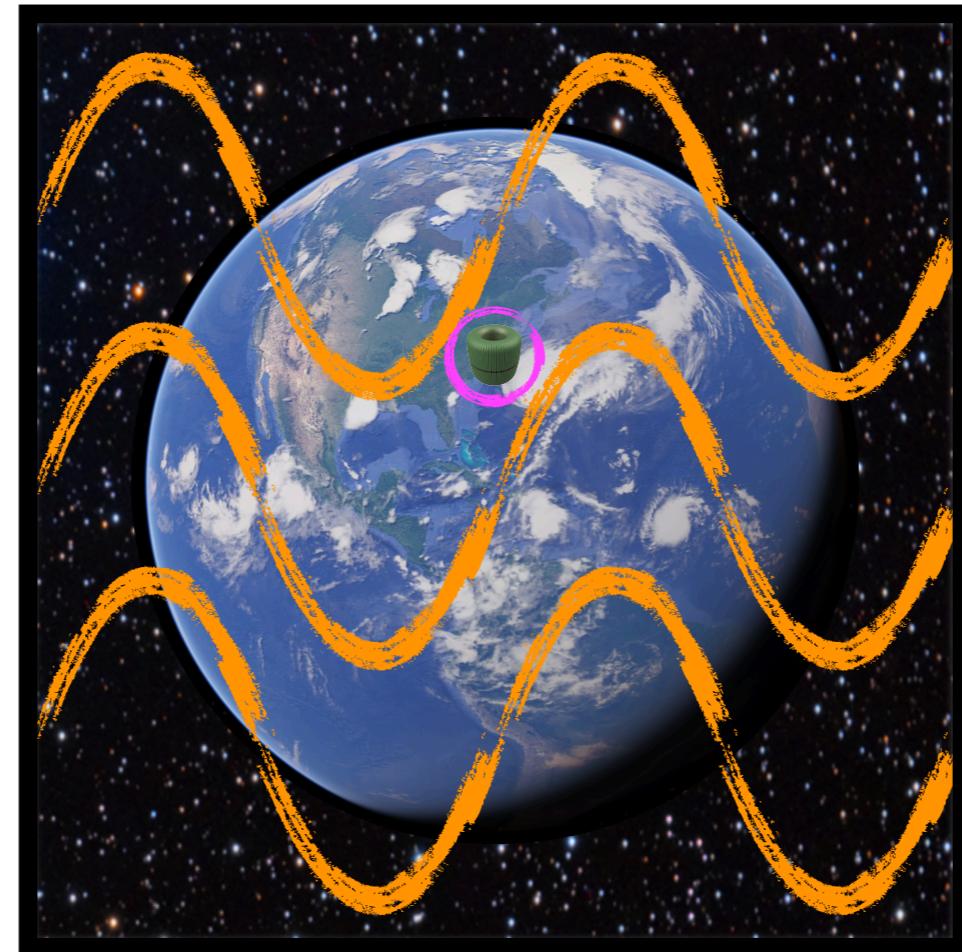
Wave-like Dark Matter



Basic Idea

Wave-like Dark Matter

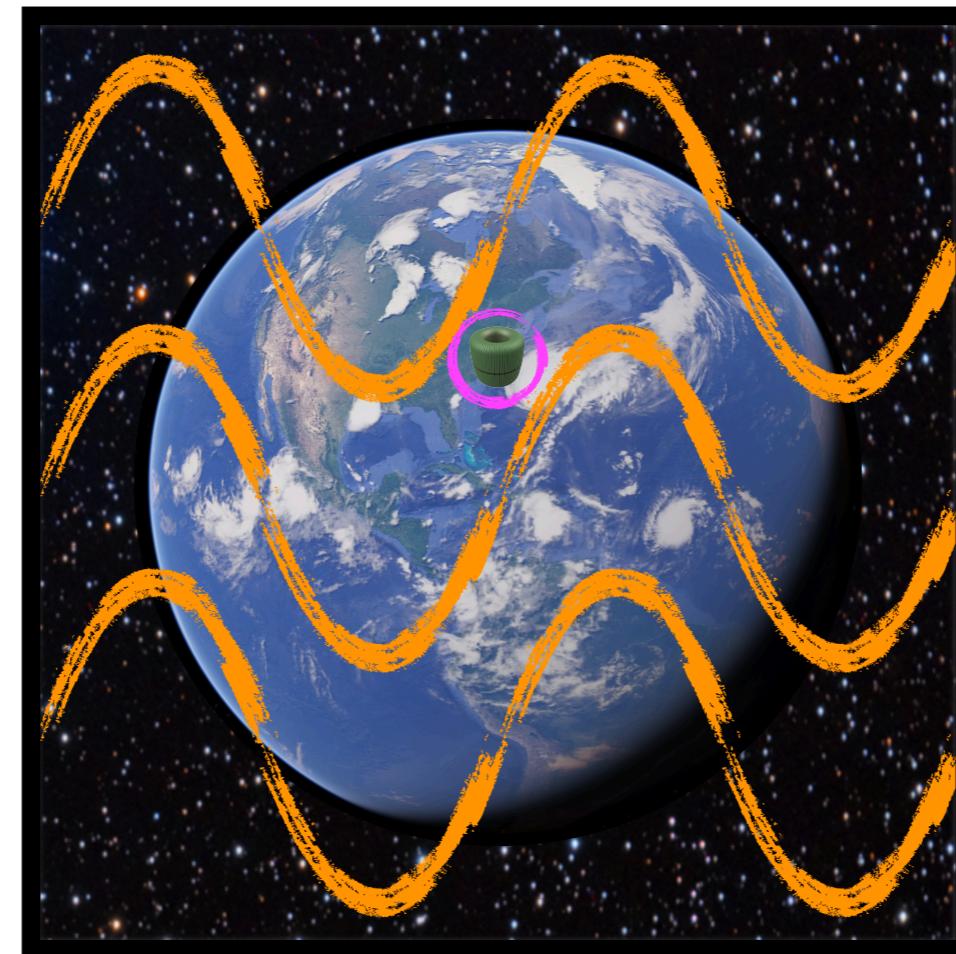
$$a \sim \cos(m_a t)$$



Basic Idea

Wave-like Dark Matter

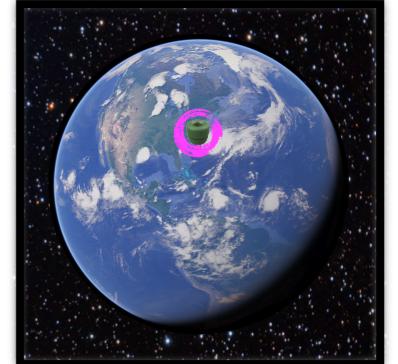
$$a \sim \cos(\omega t - \mathbf{k} \cdot \mathbf{x})$$



Basic Idea

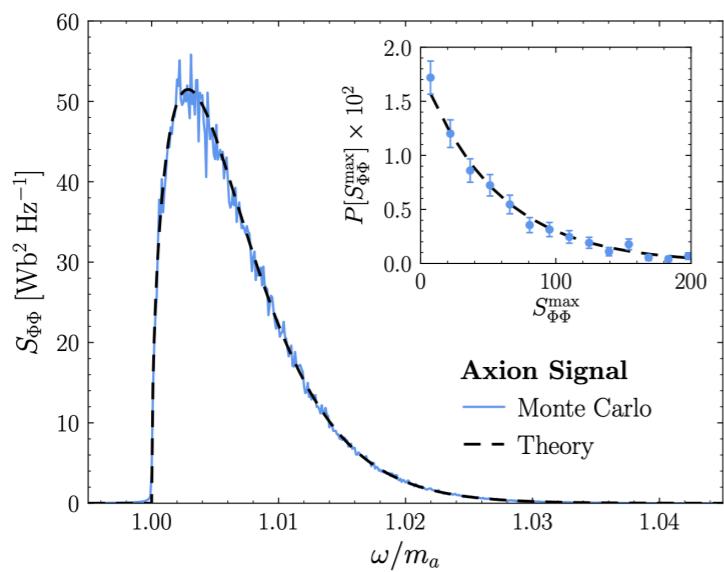
Wave-like Dark Matter

$$a \sim \cos(\omega t - \mathbf{k} \cdot \mathbf{x})$$



Speed $\omega \approx m_a(1 + |\mathbf{v}|^2/2)$

Determined by $f(v)$

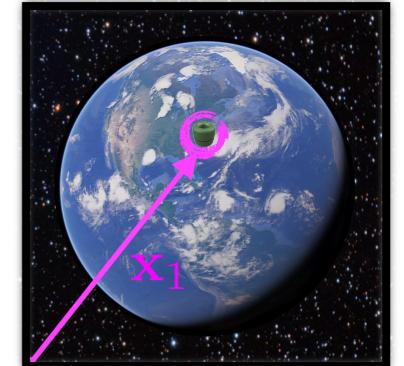


[Foster, NLR, Safdi 17]

Basic Idea

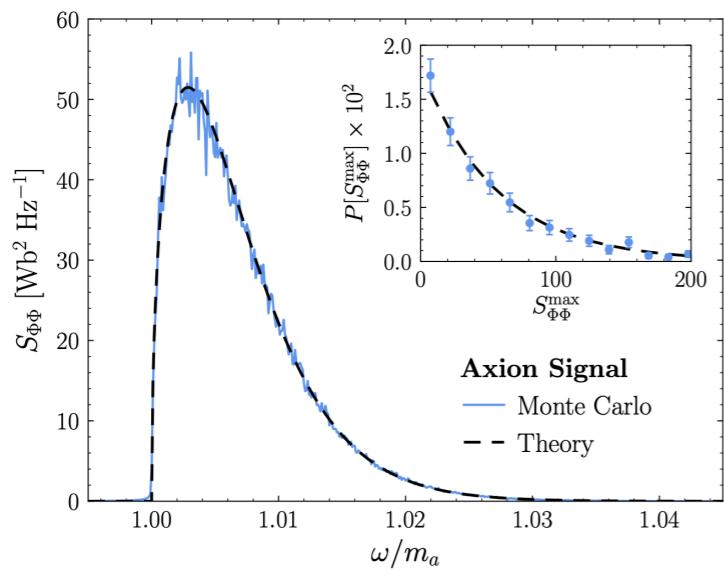
Wave-like Dark Matter

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Speed $\omega \approx m_a(1 + |\mathbf{v}|^2/2)$

Determined by $f(v)$



[Foster, NLR, Safdi 17]

Velocity $\mathbf{k} = m_a \mathbf{v}$

Determined by $f(\mathbf{v})$

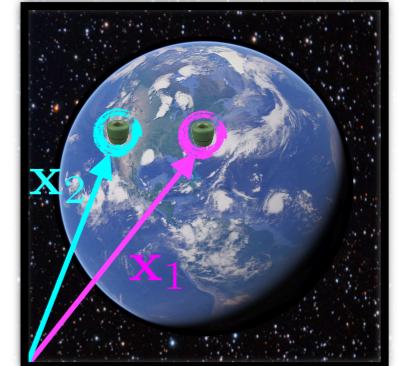
Invisible to a single detector

1. $\nabla a \sim \mathbf{k} \ll \omega \sim \partial_t a$
2. For 1 experiment, can choose $\mathbf{x} = 0$

Basic Idea

Wave-like Dark Matter

$$a \sim \cos(\omega t - \mathbf{k} \cdot \mathbf{x})$$



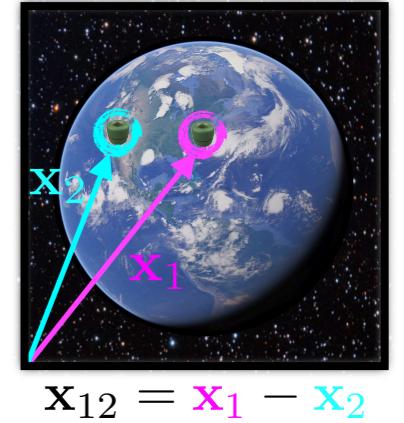
Key insight: two detectors will reveal the dependence on \mathbf{k}

Interferometry

$$f(v) \rightarrow \mathcal{F}_{12}^c(v) = \int d^3\mathbf{v} f(\mathbf{v}) \cos(m_a \mathbf{v} \cdot \mathbf{x}_{12}) \delta[|\mathbf{v}| - v]$$

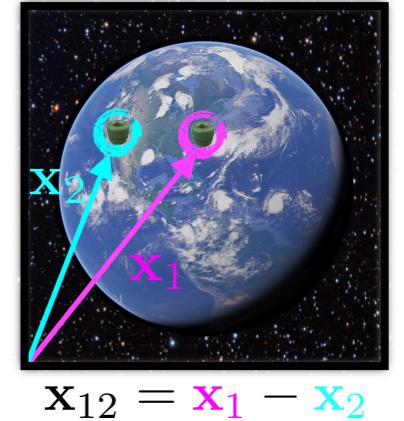


Derived in the context of a
full likelihood description
in our paper



Interferometry

$$f(v) \rightarrow \mathcal{F}_{12}^c(v) = \int d^3\mathbf{v} f(\mathbf{v}) \cos(m_a \mathbf{v} \cdot \mathbf{x}_{12}) \delta[|\mathbf{v}| - v]$$



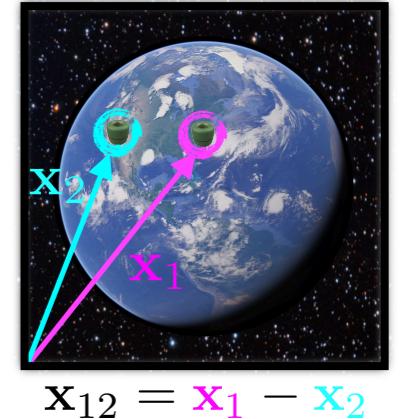
$$\mathbf{x}_{12} = \mathbf{x}_1 - \mathbf{x}_2$$

Nearby detectors $\mathbf{x}_{12} \rightarrow 0$

$$\mathcal{F}_{12}^c(v) \rightarrow \int d^3\mathbf{v} f(\mathbf{v}) \delta[|\mathbf{v}| - v] = f(v)$$

Interferometry

$$f(v) \rightarrow \mathcal{F}_{12}^c(v) = \int d^3\mathbf{v} f(\mathbf{v}) \cos(m_a \mathbf{v} \cdot \mathbf{x}_{12}) \delta[|\mathbf{v}| - v]$$



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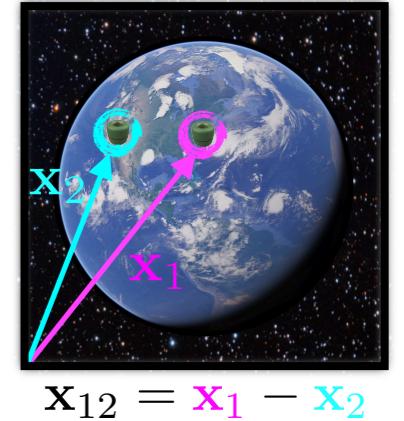
$$\mathcal{F}_{12}^c(v) \rightarrow \int d^3\mathbf{v} f(\mathbf{v}) \delta[|\mathbf{v}| - v] = f(v)$$

Far apart detectors $\mathbf{x}_{12} \rightarrow \infty$

$$\langle \mathcal{F}_{12}^c(v) \rangle \rightarrow 0$$

Interferometry

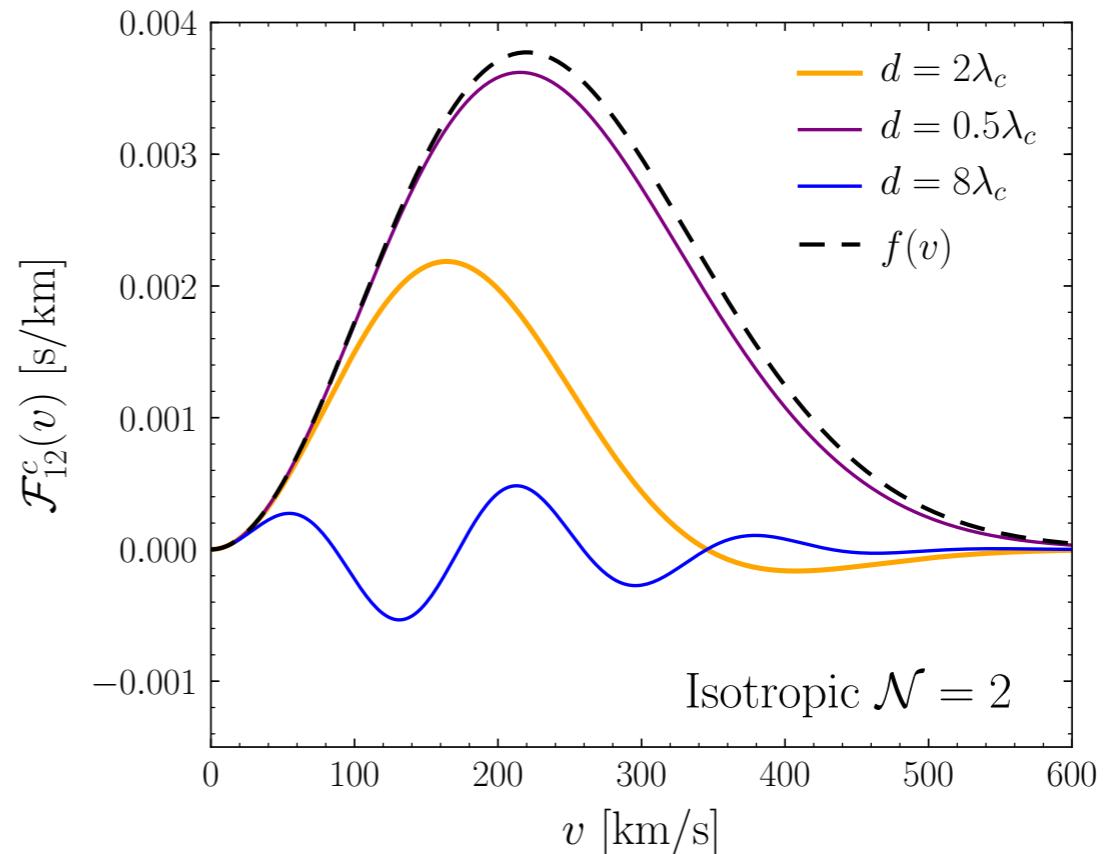
$$f(v) \rightarrow \mathcal{F}_{12}^c(v) = \int d^3\mathbf{v} f(\mathbf{v}) \cos(m_a \mathbf{v} \cdot \mathbf{x}_{12}) \delta[|\mathbf{v}| - v]$$



Depends on Coherence Length

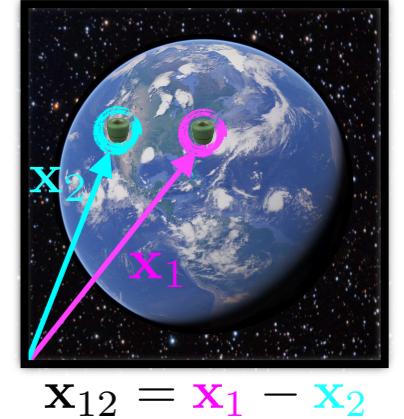
$$d = |\mathbf{x}_{12}| \quad \lambda_c \sim \frac{1}{m_a v_0}$$

- $m_a = 25 \text{ } \mu\text{eV} \Rightarrow \lambda_c \approx 10 \text{ m}$
- $m_a = 1 \text{ neV} \Rightarrow \lambda_c \approx 300 \text{ km}$



Interferometry

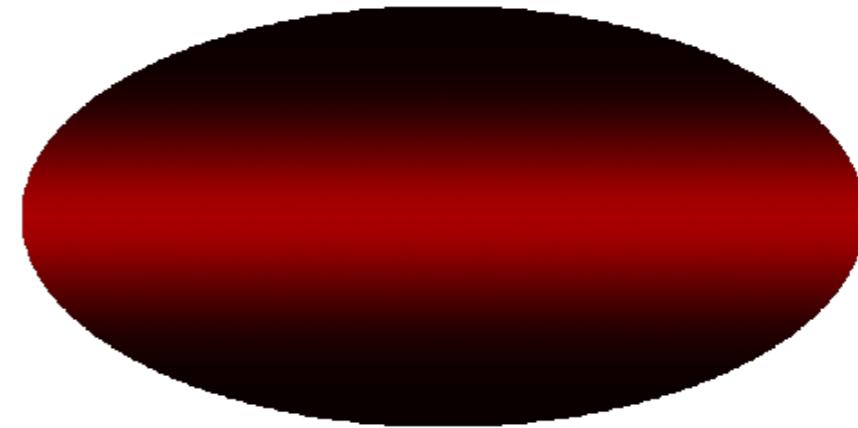
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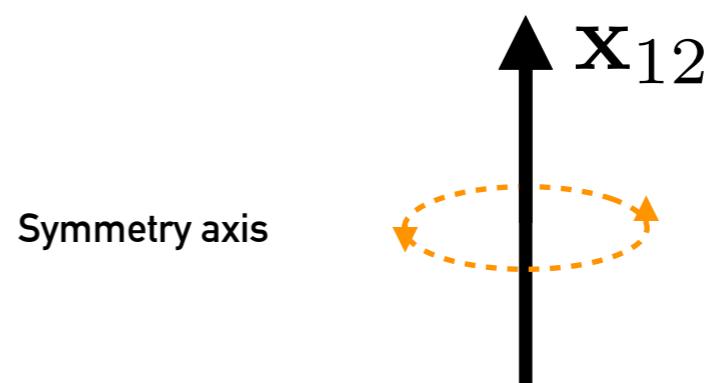
$$\theta_{\odot}^t = \pi/2$$

Inherent Degeneracy in Problem

- Rotations around \mathbf{x}_{12} leave $\mathbf{v} \cdot \mathbf{x}_{12}$ unchanged
- Need multiple \mathbf{x}_{12} to break
- Obstructs localization

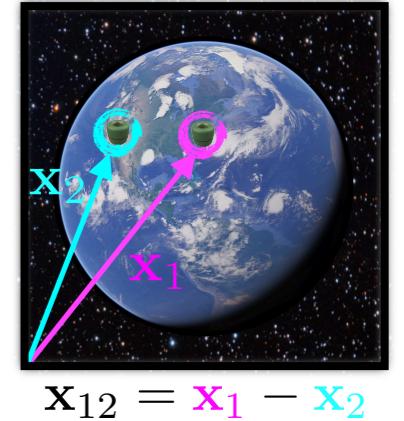


True location: image center

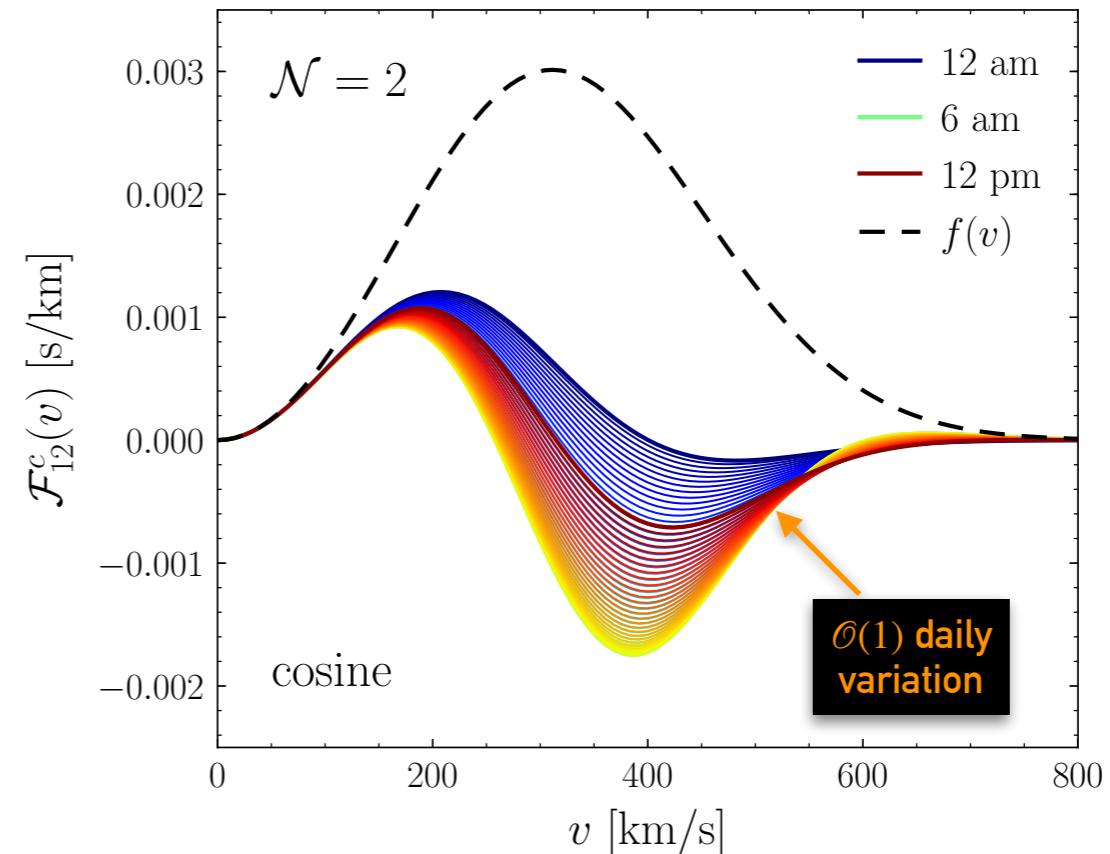


Interferometry

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Broken by Daily Modulation!



Standard Halo Model

Can we determine the direction of the DM wind?

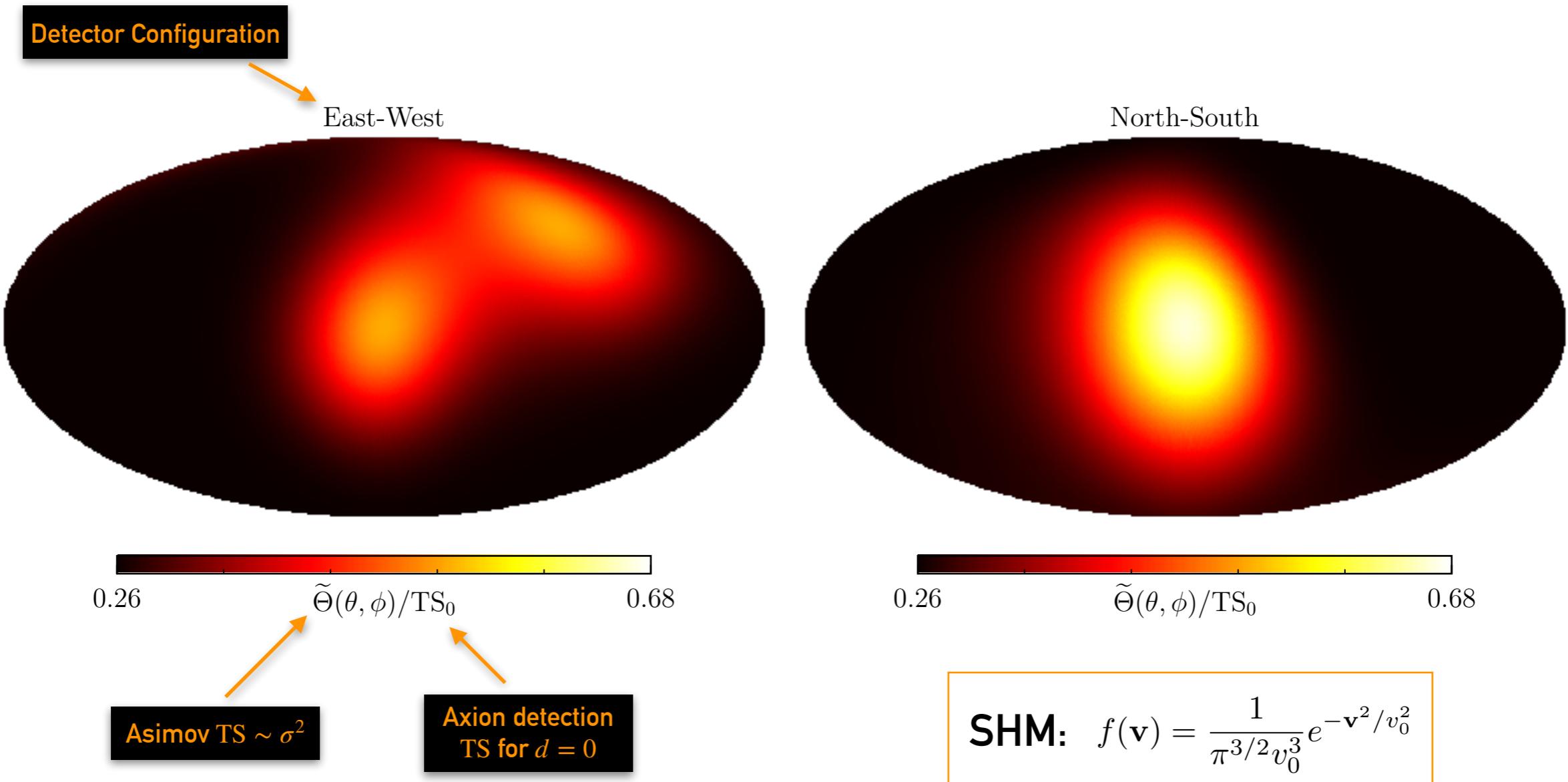
$$\text{SHM: } f(\mathbf{v}) = \frac{1}{\pi^{3/2} v_0^3} e^{-\mathbf{v}^2/v_0^2}$$



DARK MATTER INTERFEROMETRY

Standard Halo Model

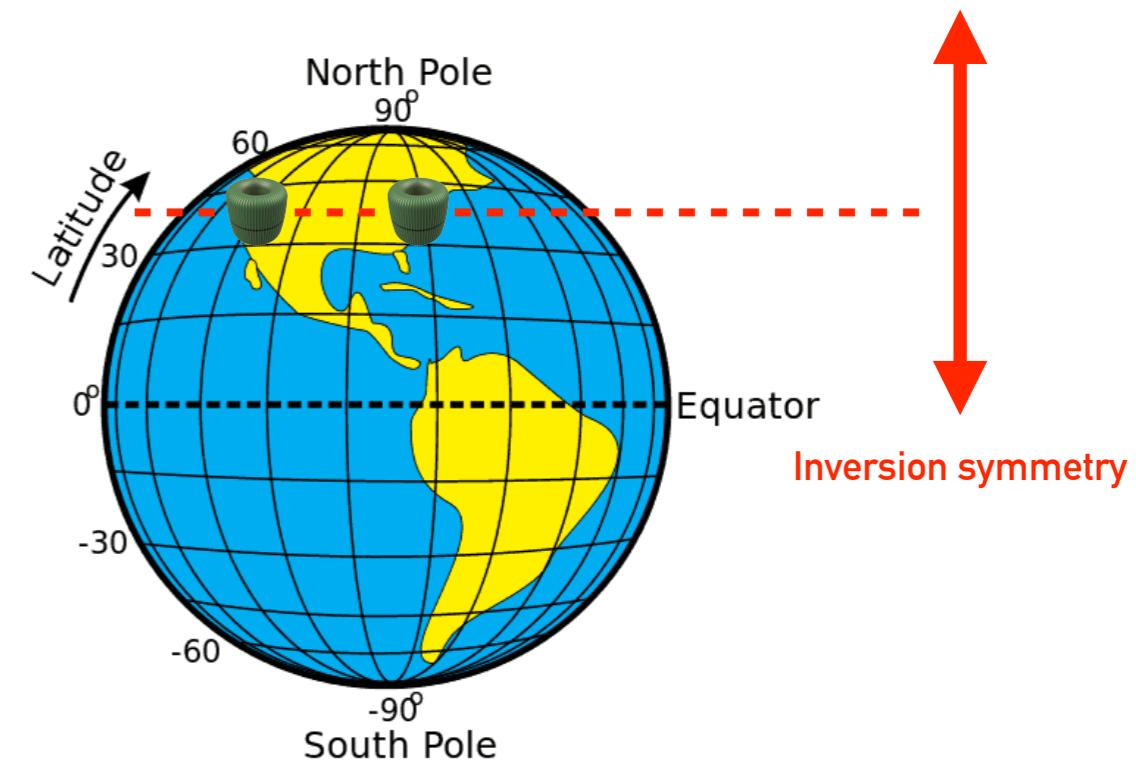
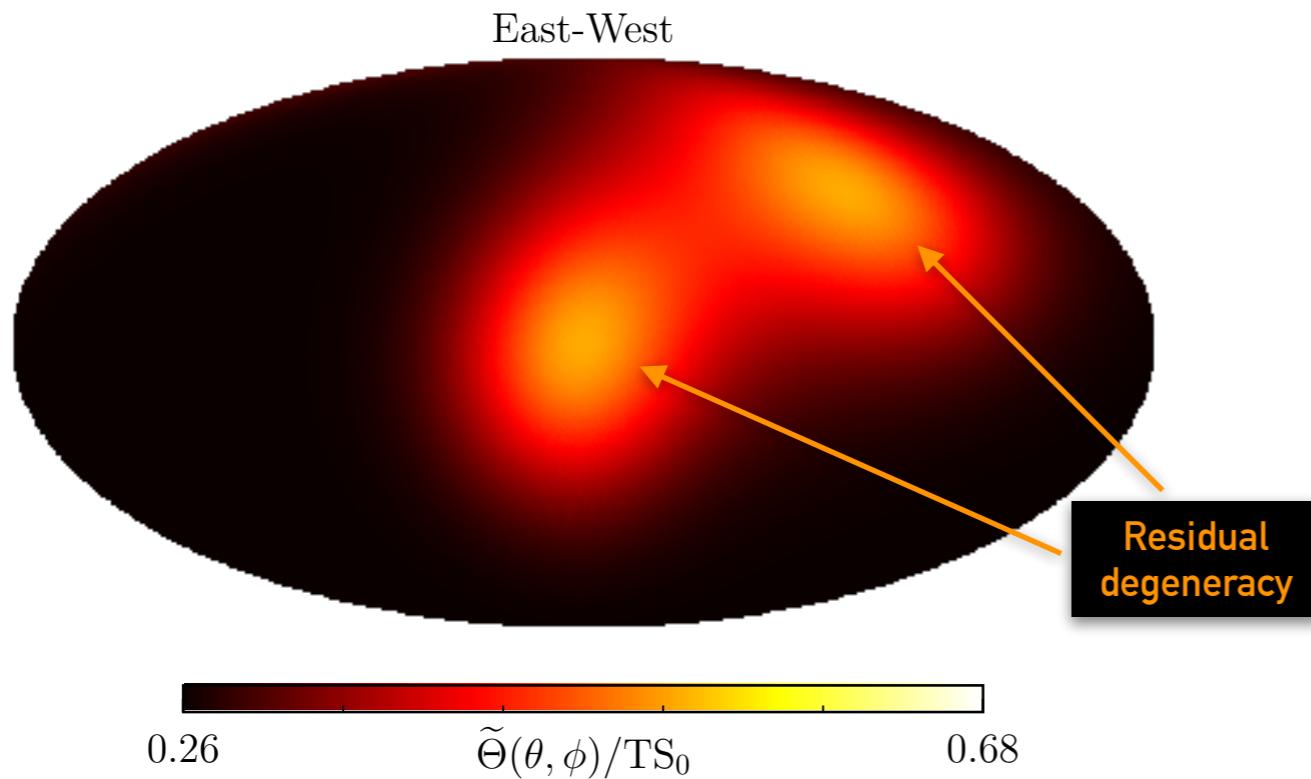
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DARK MATTER INTERFEROMETRY

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Can we determine the direction of the DM wind?



Standard Halo Model

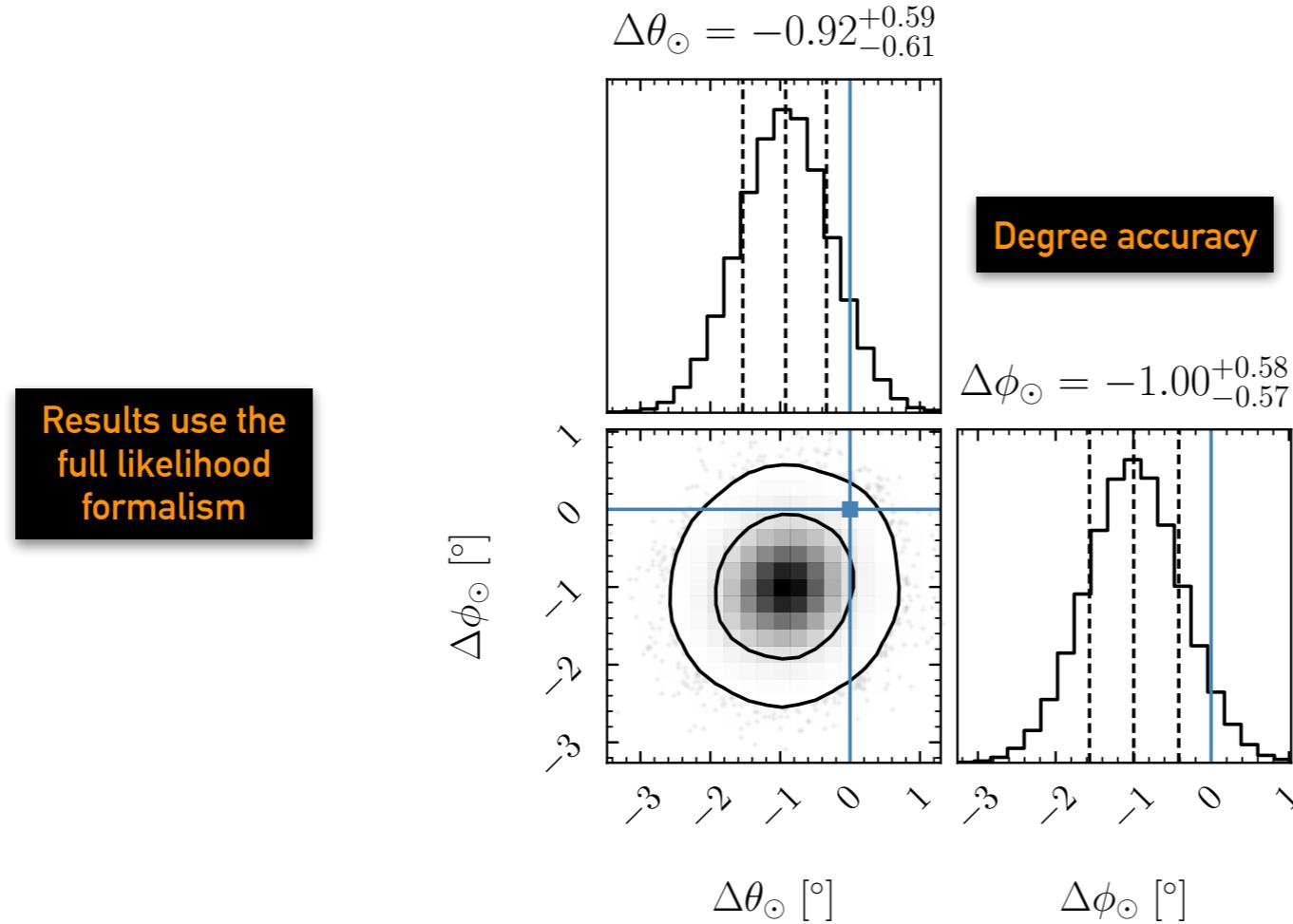
If HAYSTAC discovers DM, how well can they infer v_\odot with 2 detectors and 1 day of data?



DARK MATTER INTERFEROMETRY

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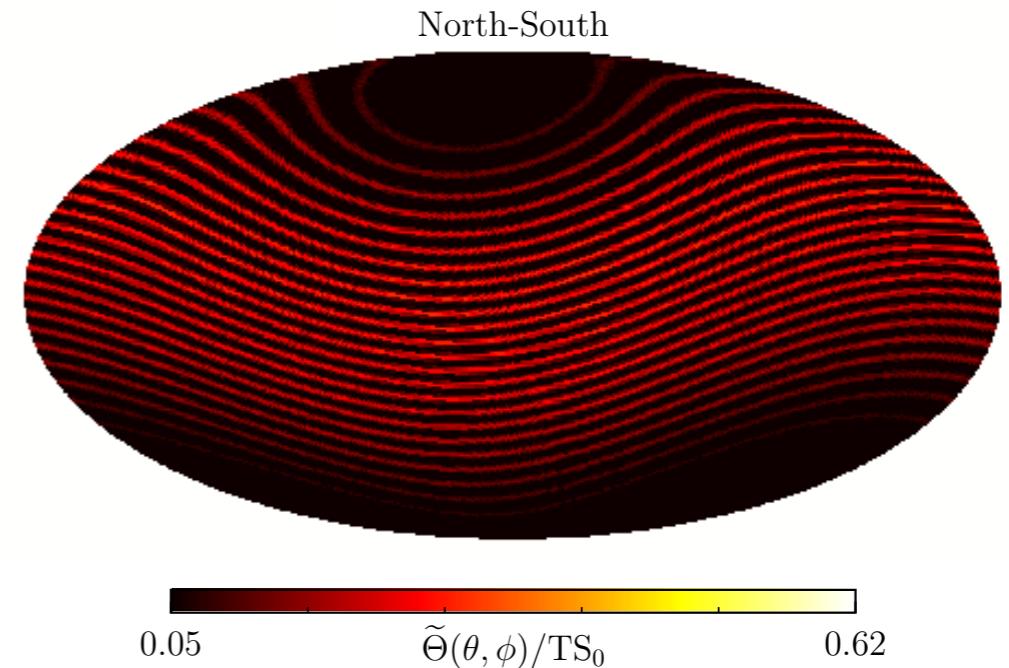
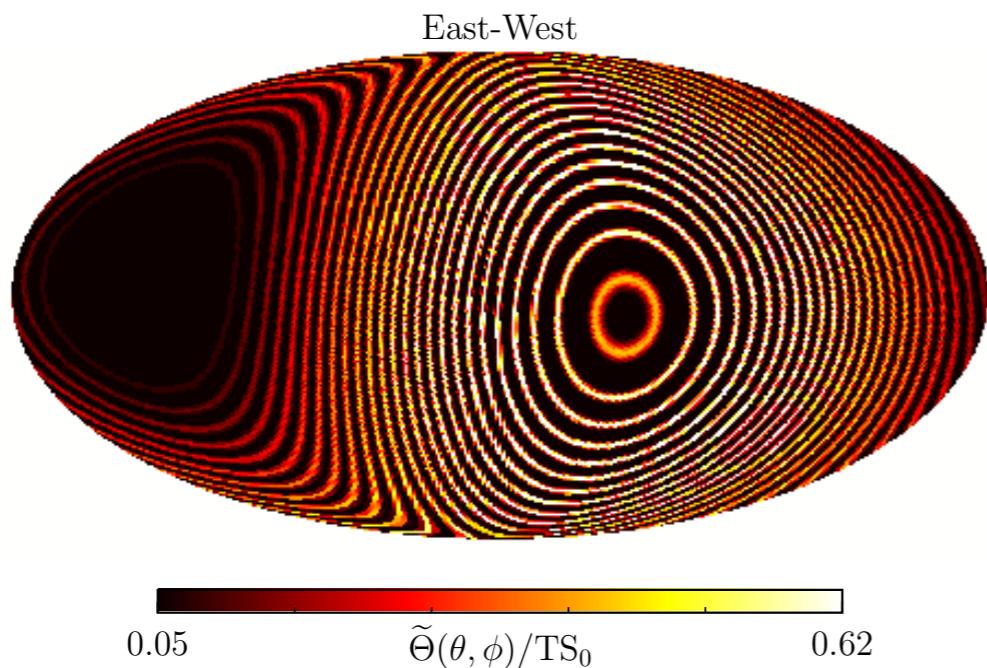
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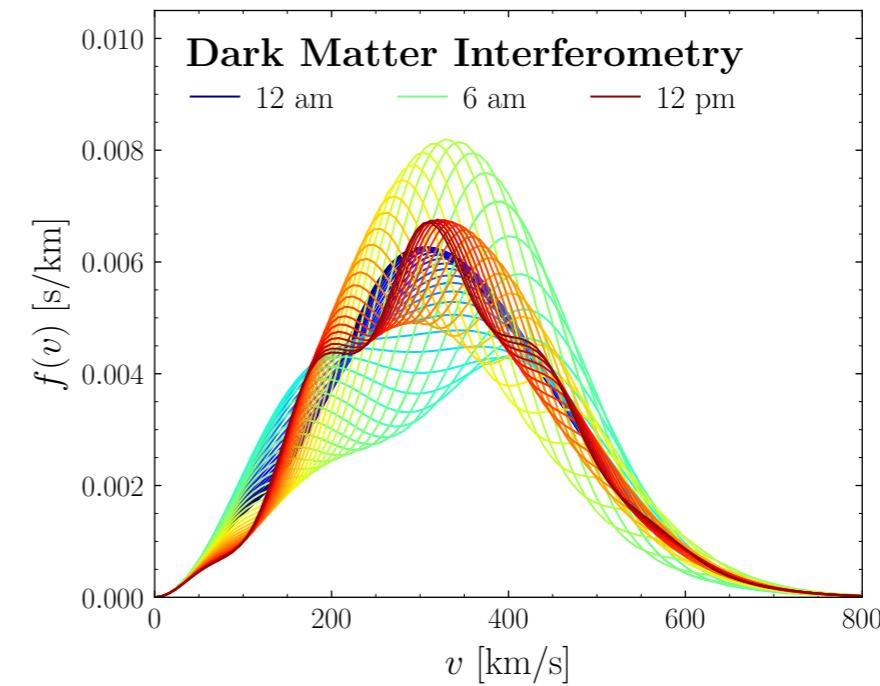
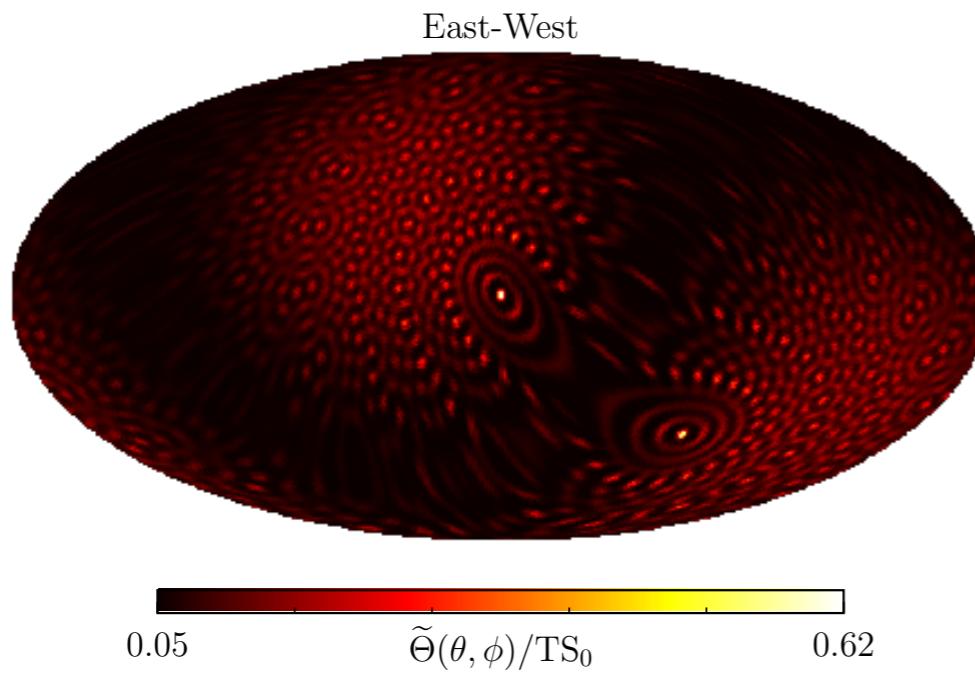
Stream Localization

Can we determine the direction
of an incident DM stream?



Summary

Interferometry performed directly on the axion wave reveals hidden DM structure



Cosmic Axion Background

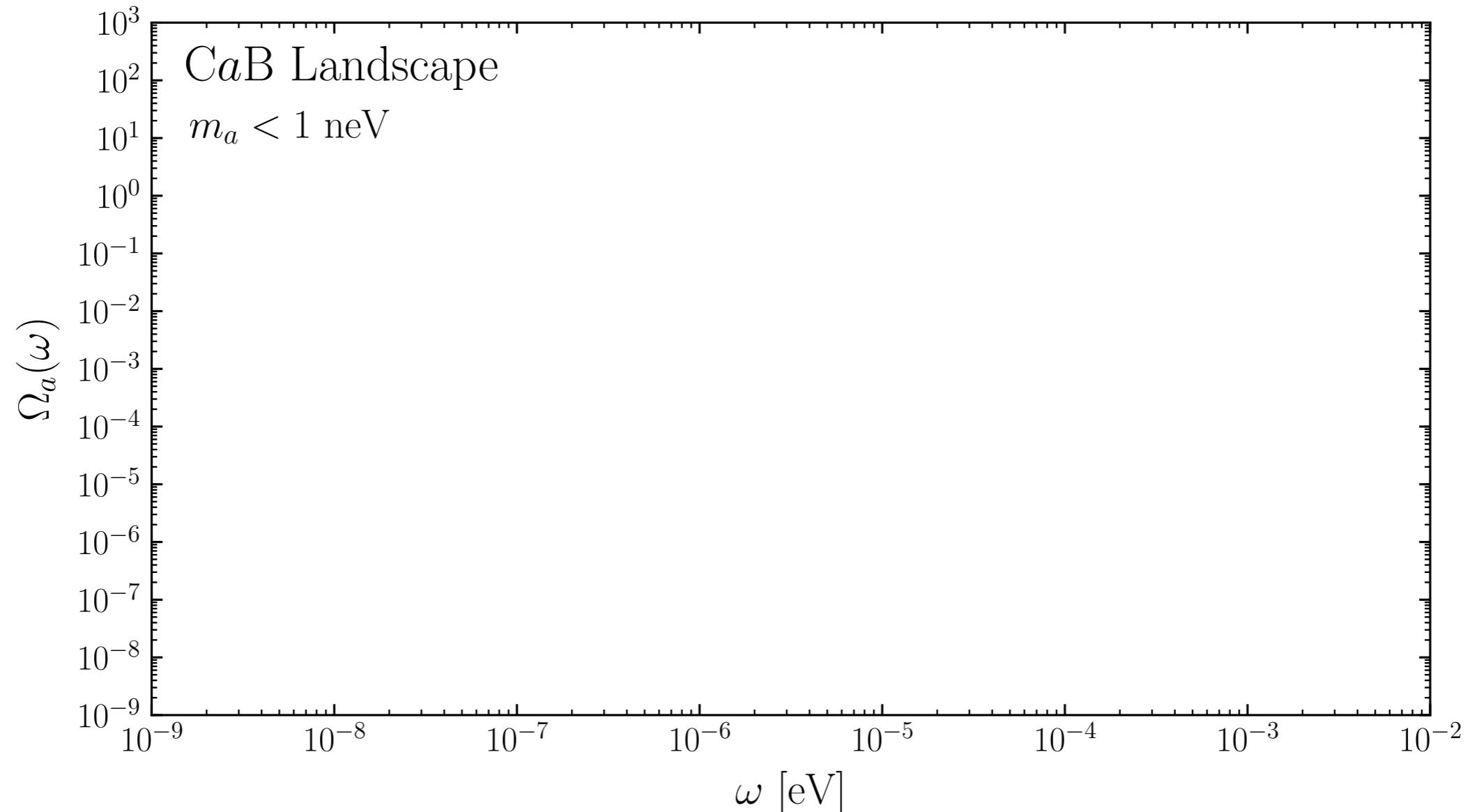
2101.09287
w/ Jeff Dror, Hitoshi Murayama

The Cosmic Axion Background

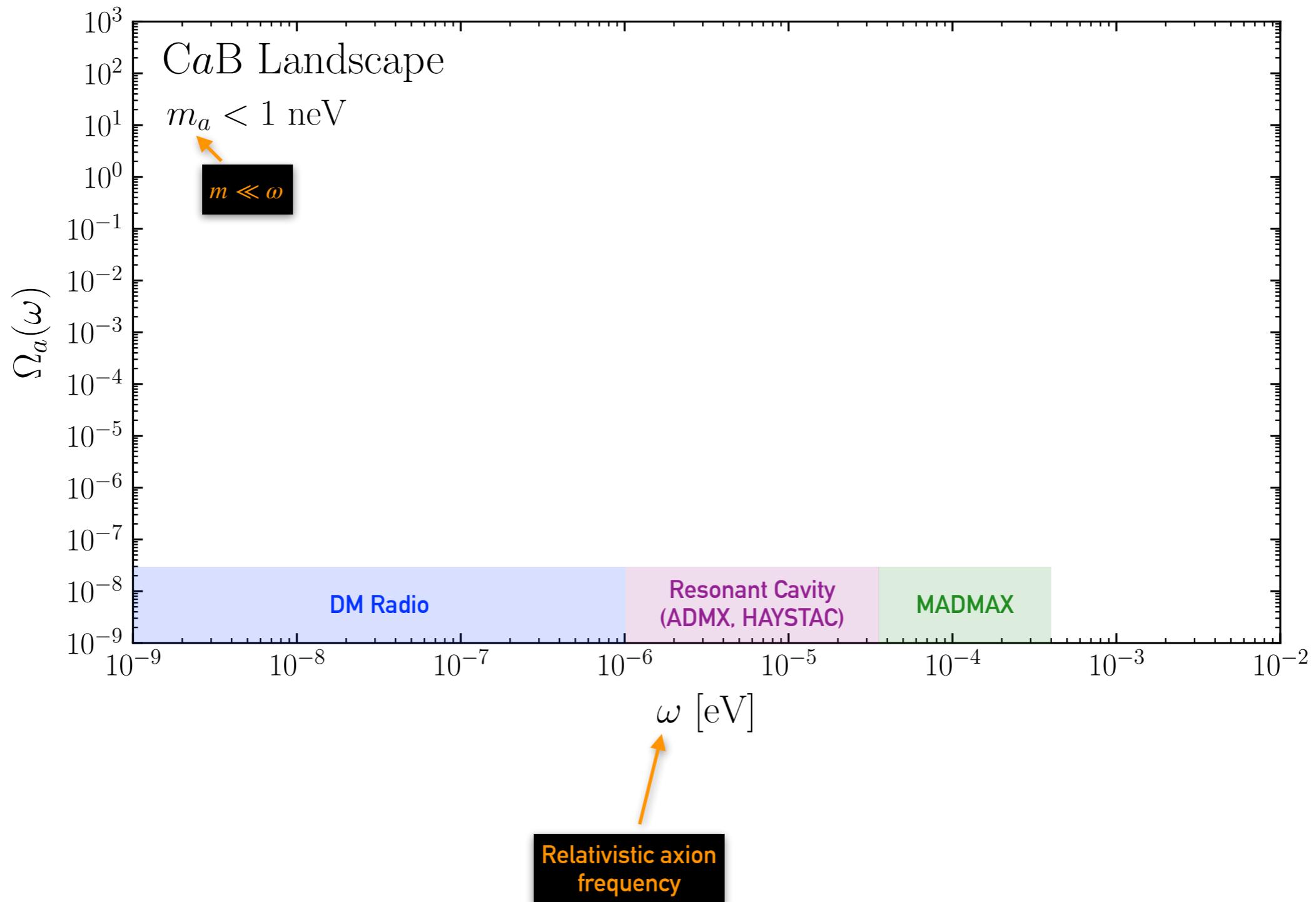
**Can we detect relativistic axions that
are a relic of the early universe?**



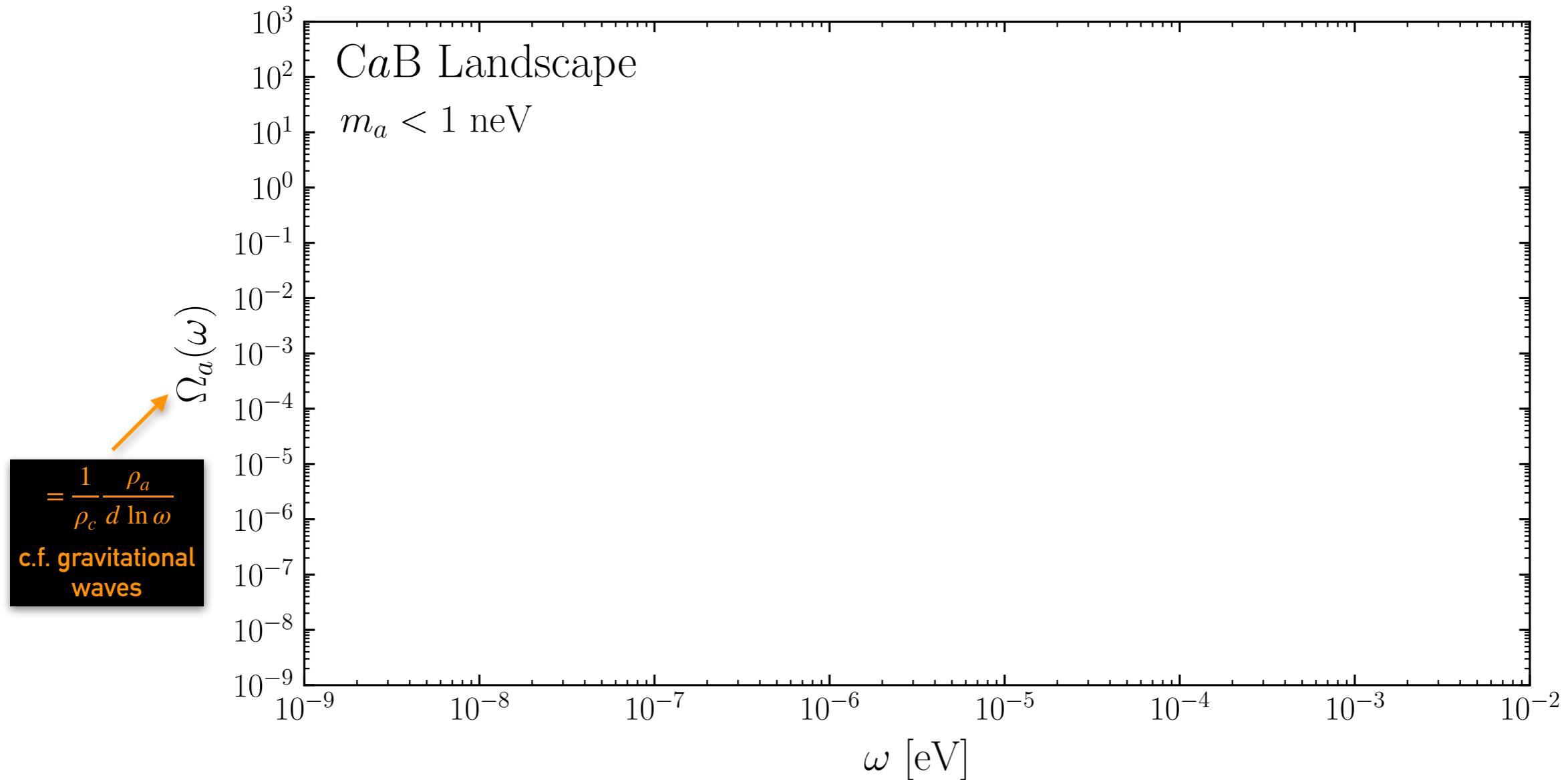
Landscape



Landscape

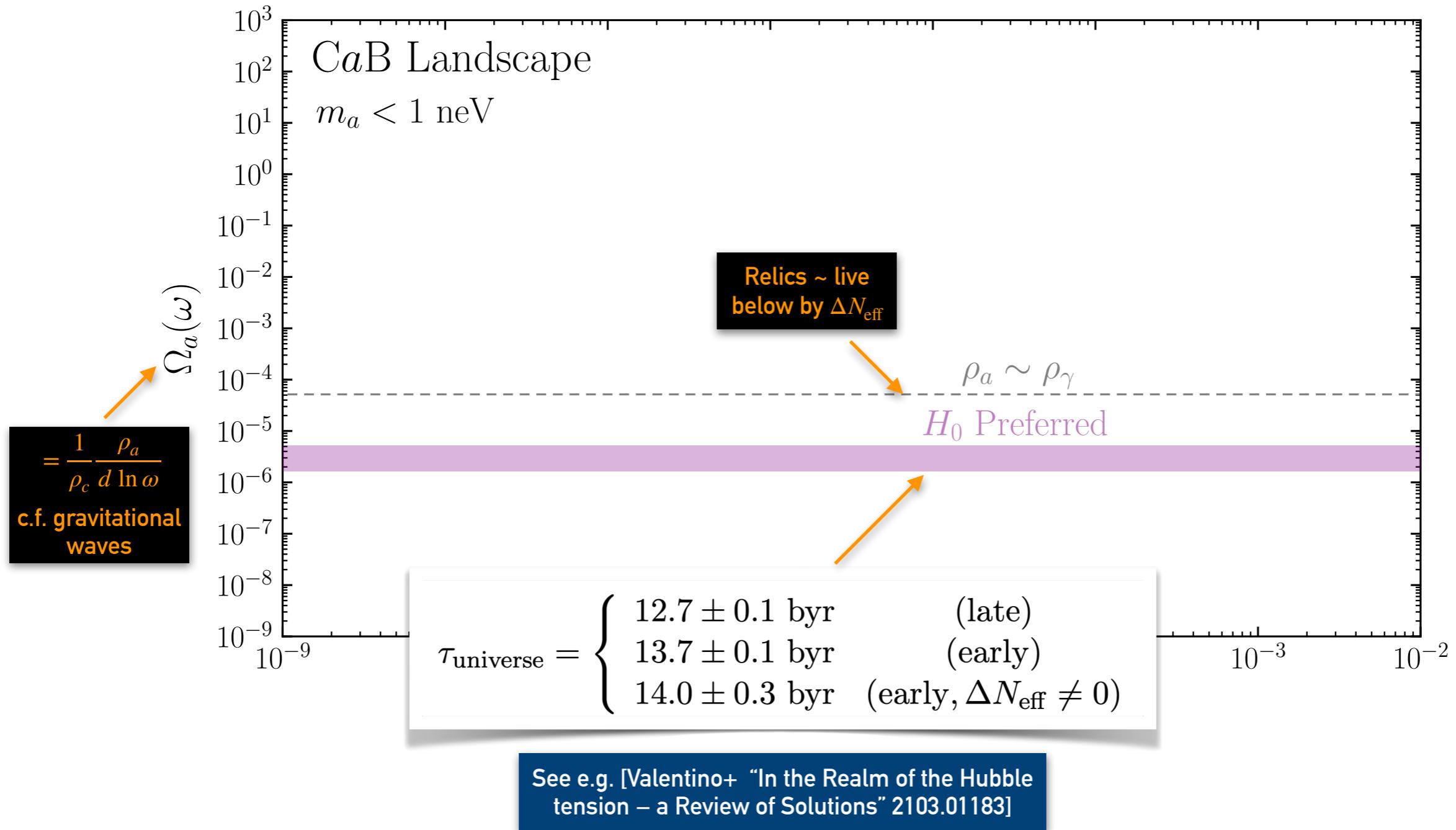


Landscape

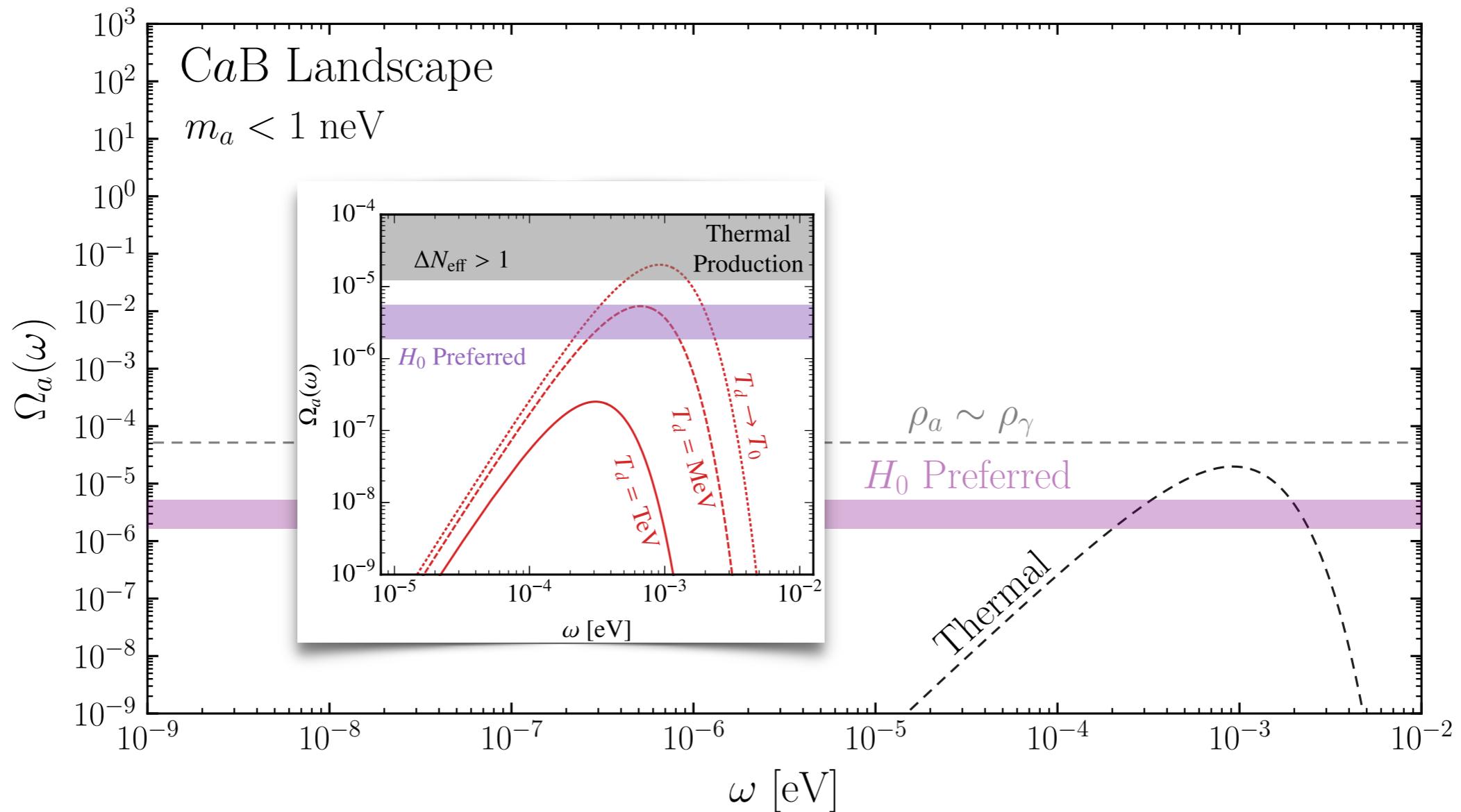


THE COSMIC AXION BACKGROUND

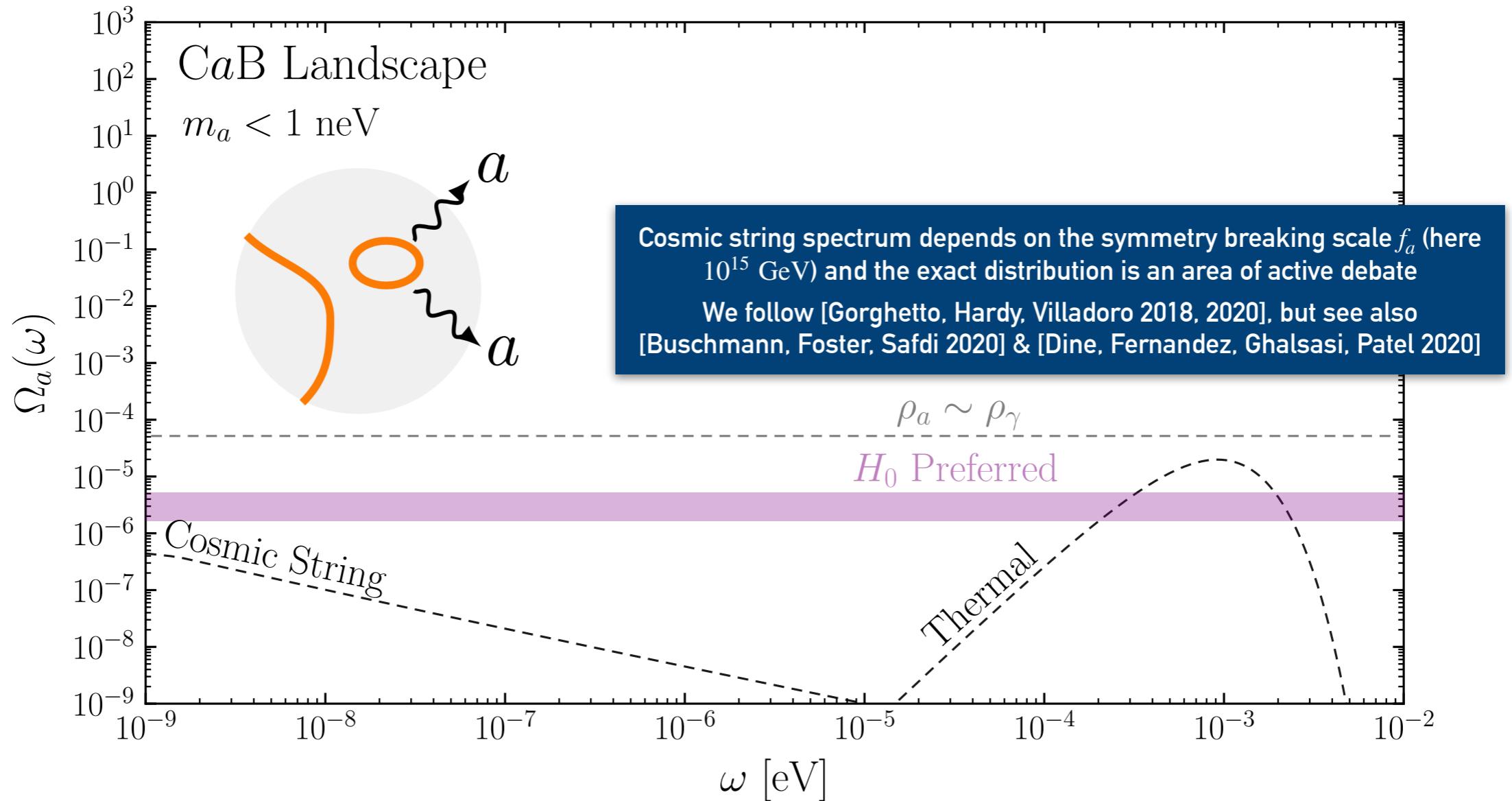
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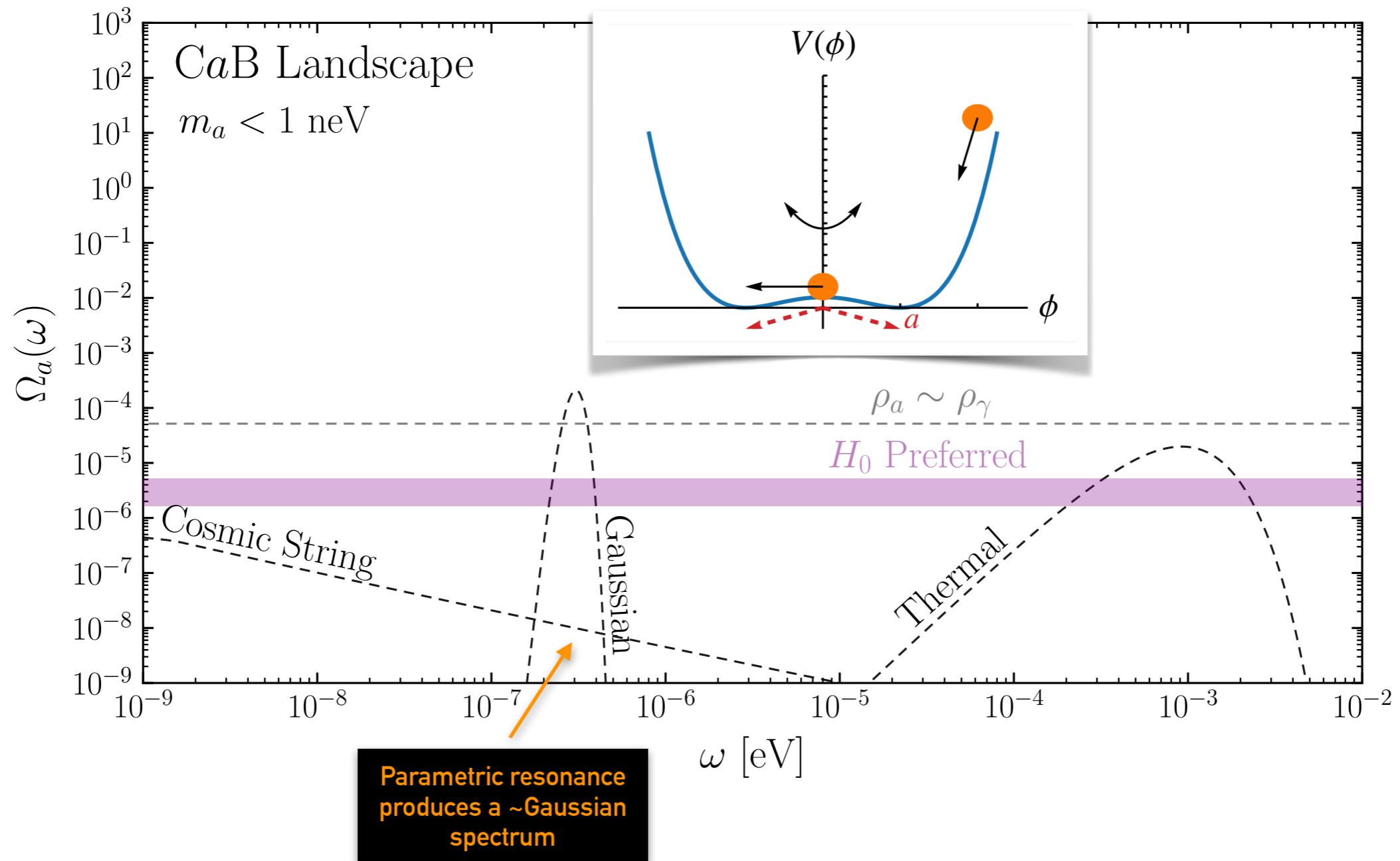
Landscape



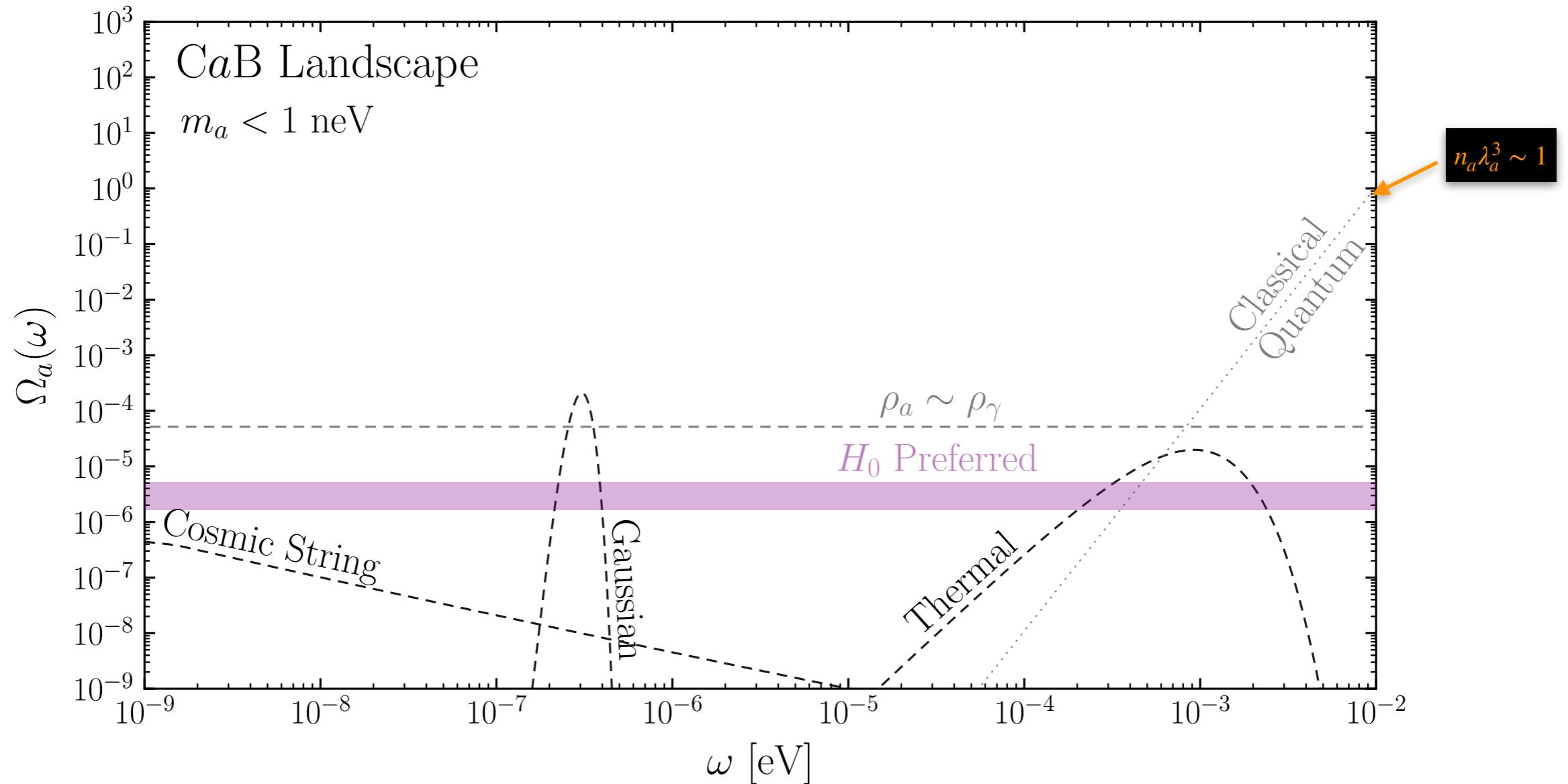
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Landscape

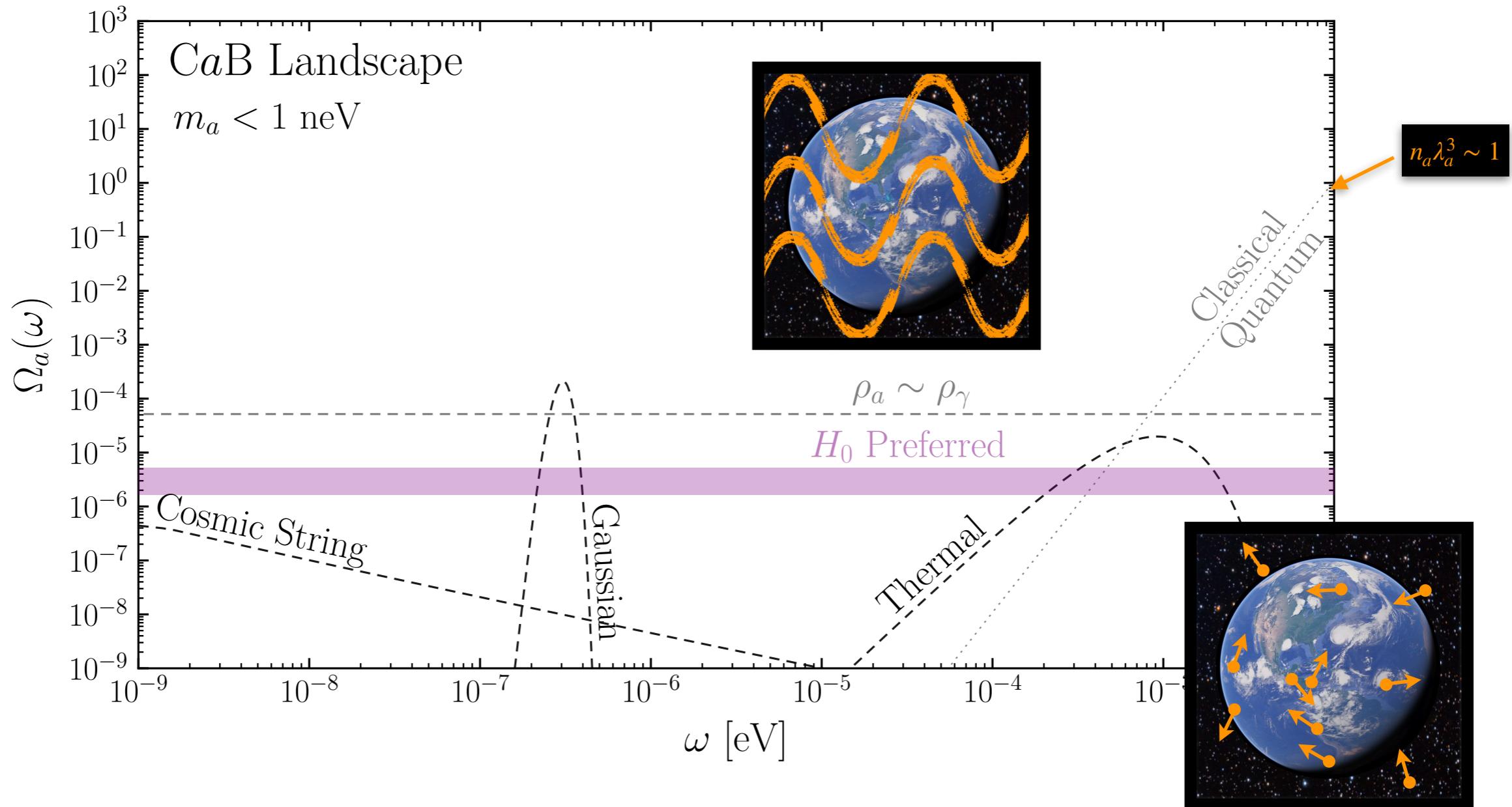


Landscape



Landscape

Classical wave description applies



Rough Sensitivity

$$a(t) \sim \sum_i \cos(\omega_i t + \phi_i)$$

Sampled from $p(\omega)$

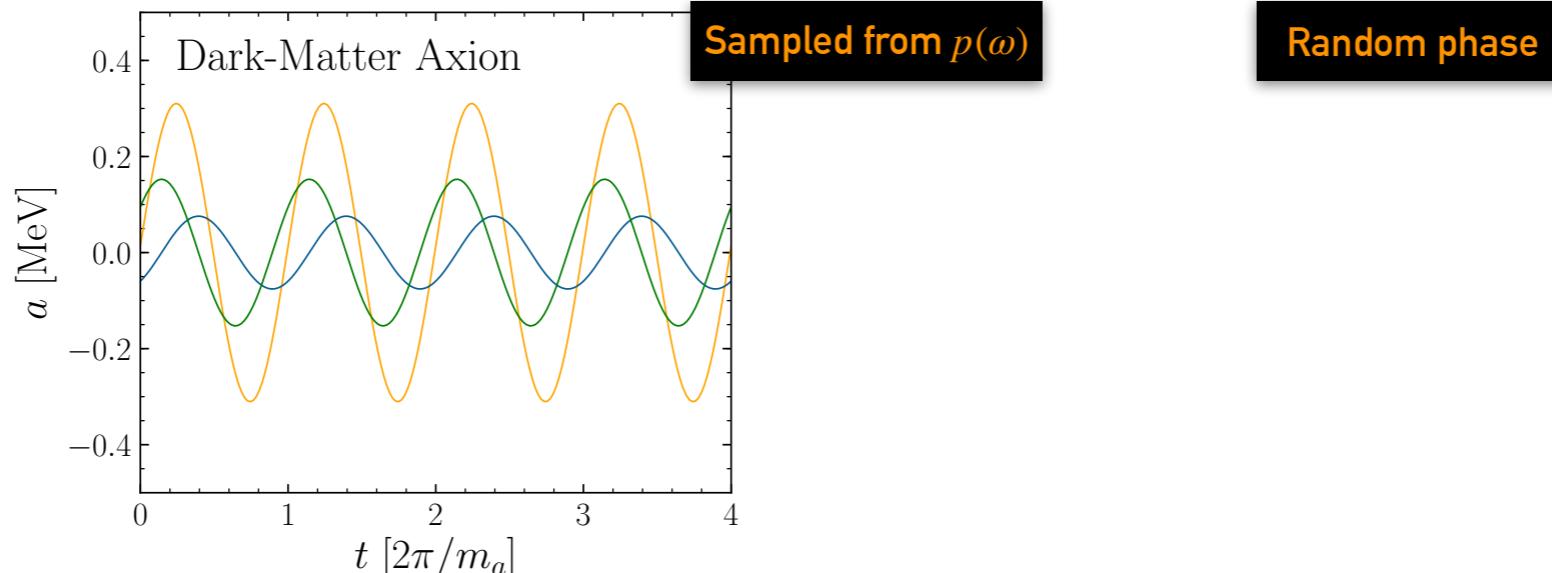
Random phase



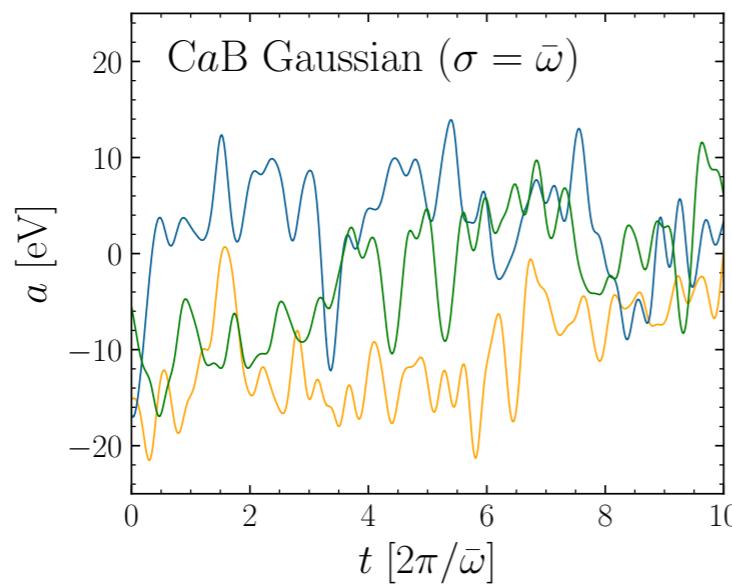
Rough Sensitivity

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**Dark
Matter**



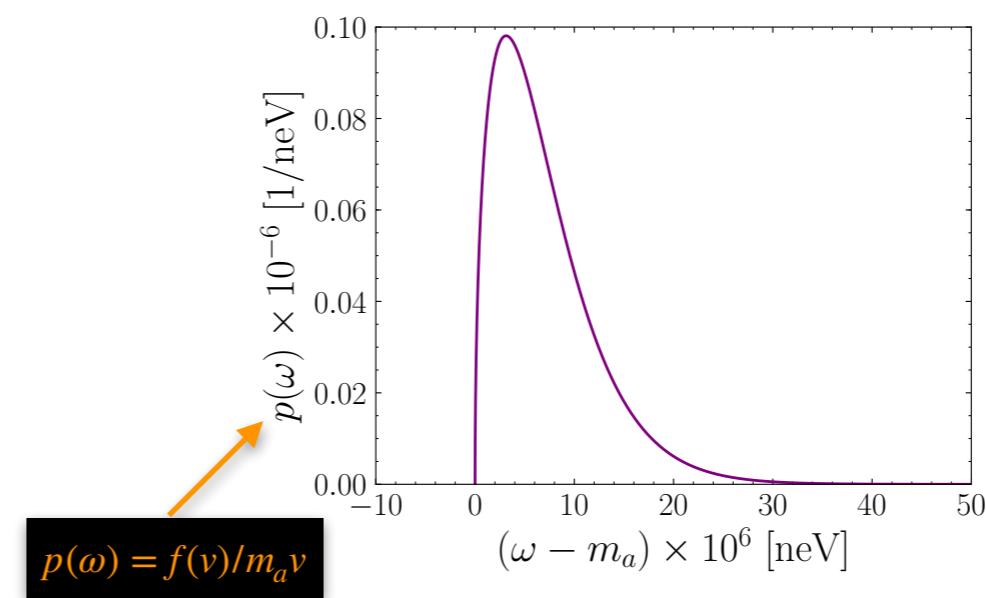
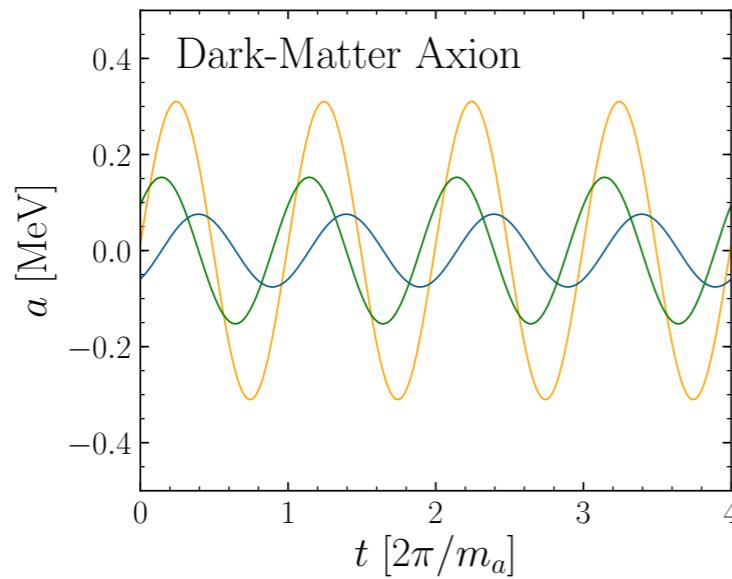
CaB



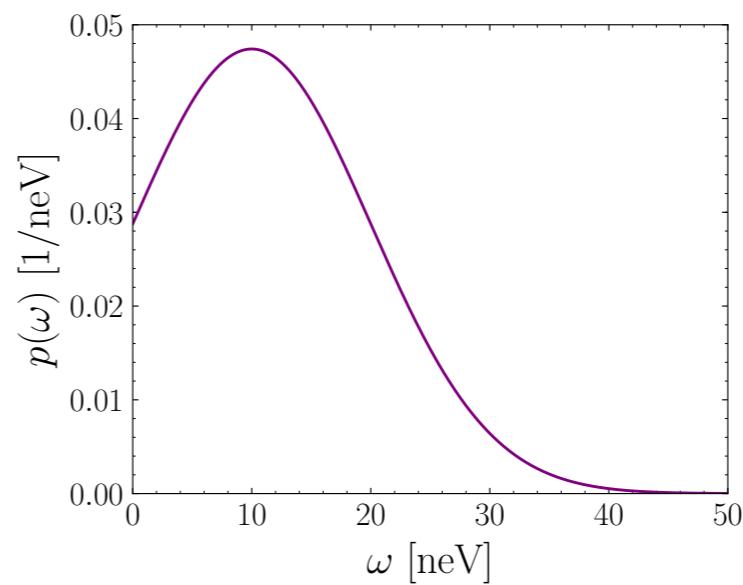
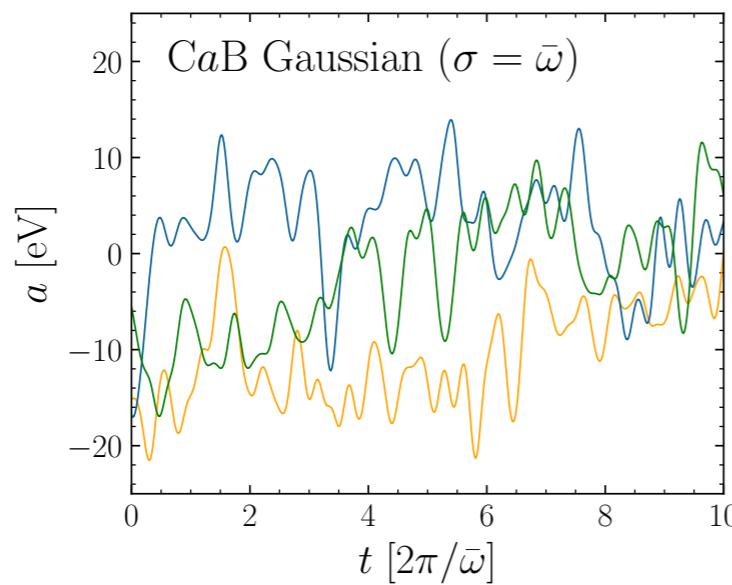
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Dark Matter



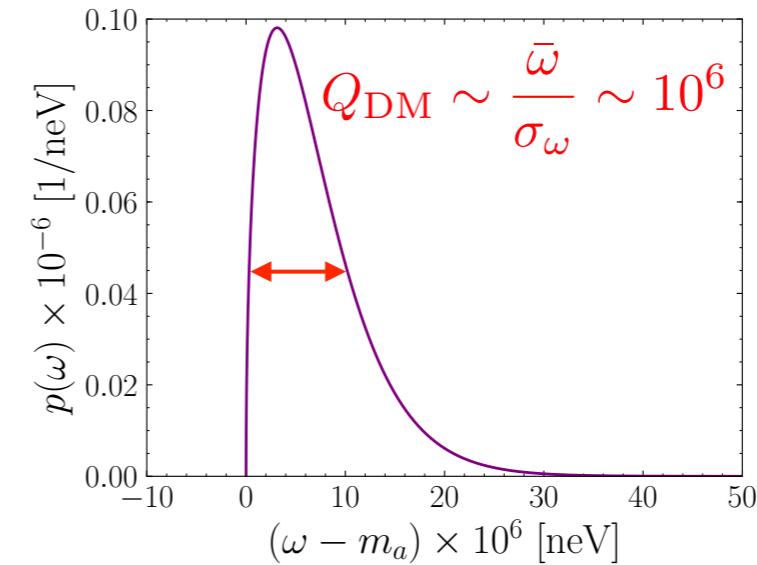
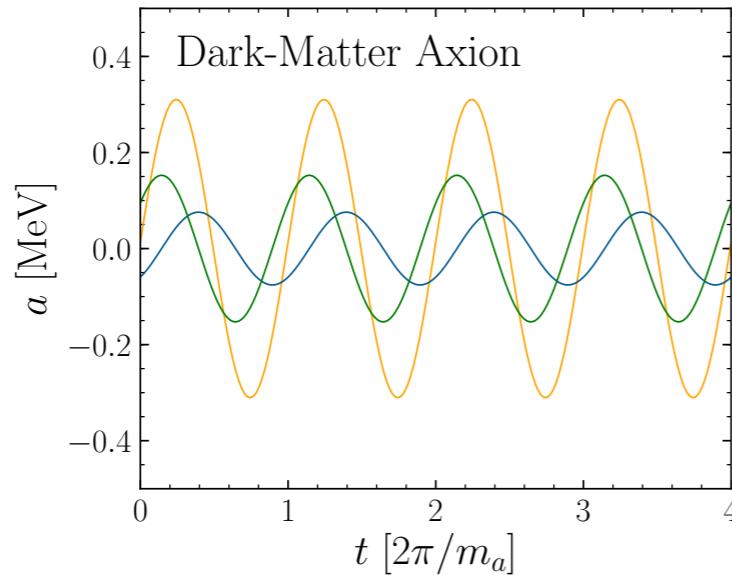
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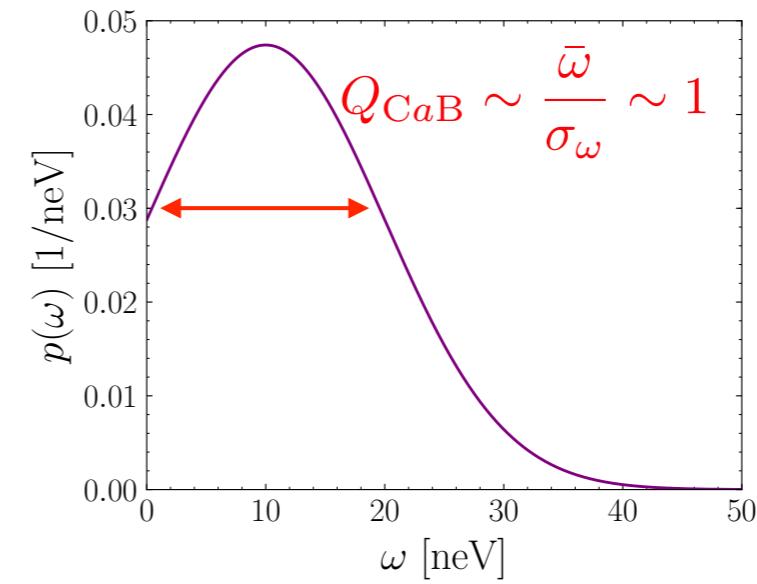
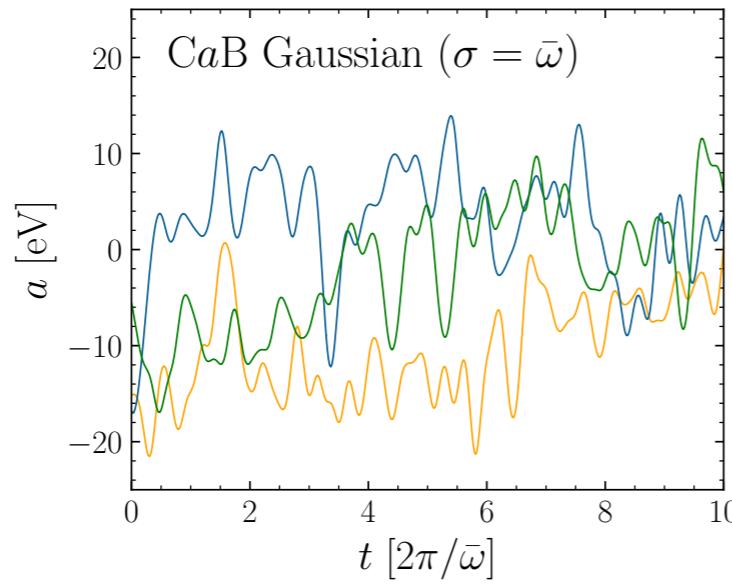
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Dark Matter



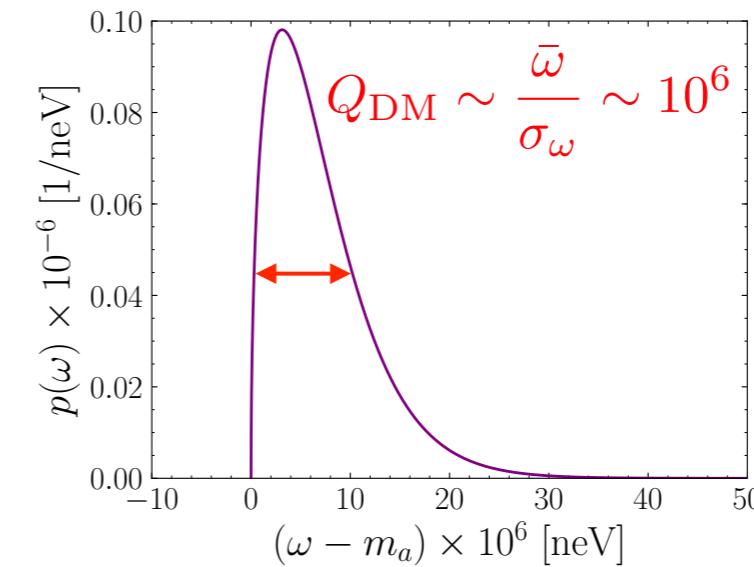
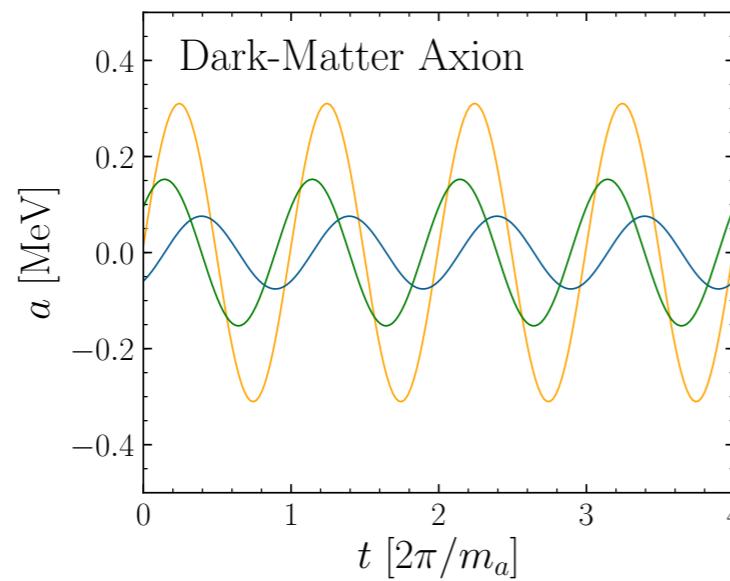
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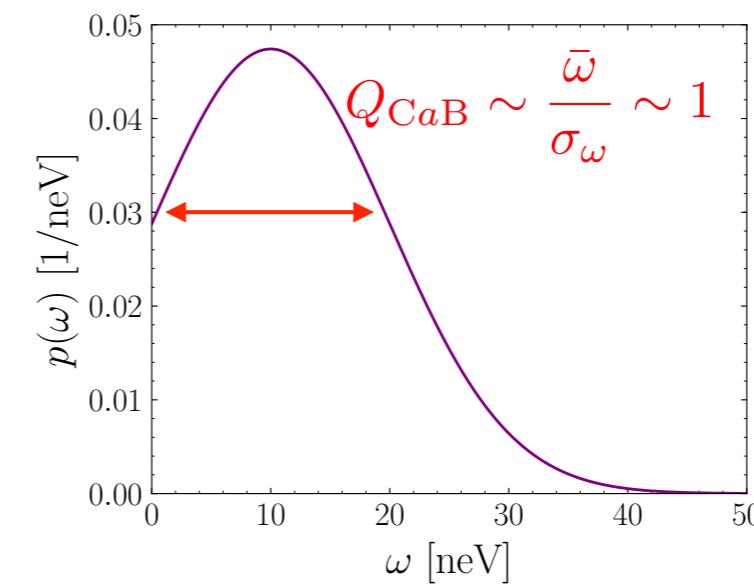
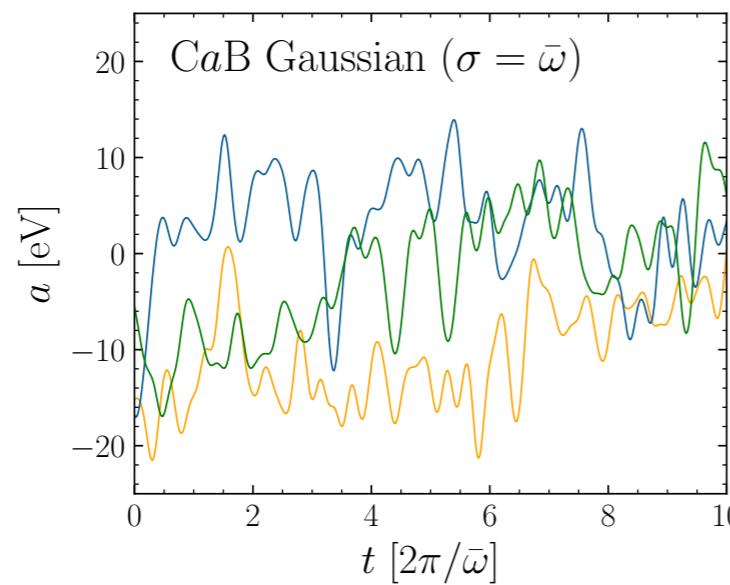
Rough Sensitivity

$$a(t) \sim \sum_i \cos(\omega_i t + \phi_i)$$

Dark Matter



CaB



Much broader signal -
existing searches would
throw out as background

Rough Sensitivity

$$a(t) \sim \sum_i \cos(\omega_i t + \phi_i)$$

Power in the axion field

Power spectral density -
measures power at a
given frequency

$$\langle S_a(\omega) \rangle = \frac{\pi \rho_a}{\bar{\omega}} \frac{p(\omega)}{\omega}$$



Rough Sensitivity

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Experimentally accessible power

$$\langle S_{g\partial a}(\omega) \rangle = \pi g_{a\gamma\gamma}^2 \rho_a \frac{\omega}{\bar{\omega}} p(\omega)$$



Rough Sensitivity

$$a(t) \sim \sum_i \cos(\omega_i t + \phi_i)$$

Power in the axion field

$$\langle S_a(\omega) \rangle = \frac{\pi \rho_a}{\bar{\omega}} \frac{p(\omega)}{\omega}$$

Experimentally accessible power

$$\langle S_{g\partial a}(\bar{\omega}) \rangle = \frac{\pi g_{a\gamma\gamma}^2 \rho_a Q_a}{\bar{\omega}}$$

Approximate $p(\omega) \sim Q_a/\bar{\omega}$



Rough Sensitivity

Estimate sensitivity by matching power $P_{\text{DM}} = P_{\text{CaB}}$

$$\langle S_{g\partial a}(\bar{\omega}) \rangle = \frac{\pi g_{a\gamma\gamma}^2 \rho_a Q_a}{\bar{\omega}}$$



Rough Sensitivity

Estimate sensitivity by matching power $P_{\text{DM}} = P_{\text{CaB}}$

$$\text{Single bin: } (g_{a\gamma\gamma}^{\lim})^2 \rho_{\text{DM}} Q_{\text{DM}} = (g_{a\gamma\gamma}^{\text{SE}})^2 \rho_a Q_{\text{CaB}}$$

$$\langle S_{g\partial a}(\bar{\omega}) \rangle = \frac{\pi g_{a\gamma\gamma}^2 \rho_a Q_a}{\bar{\omega}}$$

Rough Sensitivity

Estimate sensitivity by matching power $P_{\text{DM}} = P_{\text{CaB}}$

Single bin: $(g_{a\gamma\gamma}^{\lim})^2 \rho_{\text{DM}} Q_{\text{DM}} = (g_{a\gamma\gamma}^{\text{SE}})^2 \rho_a Q_{\text{CaB}}$

$$\text{All bins: } \rho_a = \rho_{\text{DM}} \left(\frac{g_{a\gamma\gamma}^{\lim}}{g_{a\gamma\gamma}^{\text{SE}}} \right)^2 \sqrt{\frac{Q_{\text{DM}}}{Q_{\text{CaB}}}}$$

Lose: $\rho_a \ll \rho_{\text{DM}}$ **Win:** $g_{a\gamma\gamma}^{\lim} \ll g_{a\gamma\gamma}^{\text{SE}}$ **Lose:** $Q_{\text{CaB}} \ll Q_{\text{DM}}$

$$\langle S_{g\partial a}(\bar{\omega}) \rangle = \frac{\pi g_{a\gamma\gamma}^2 \rho_a Q_a}{\bar{\omega}}$$

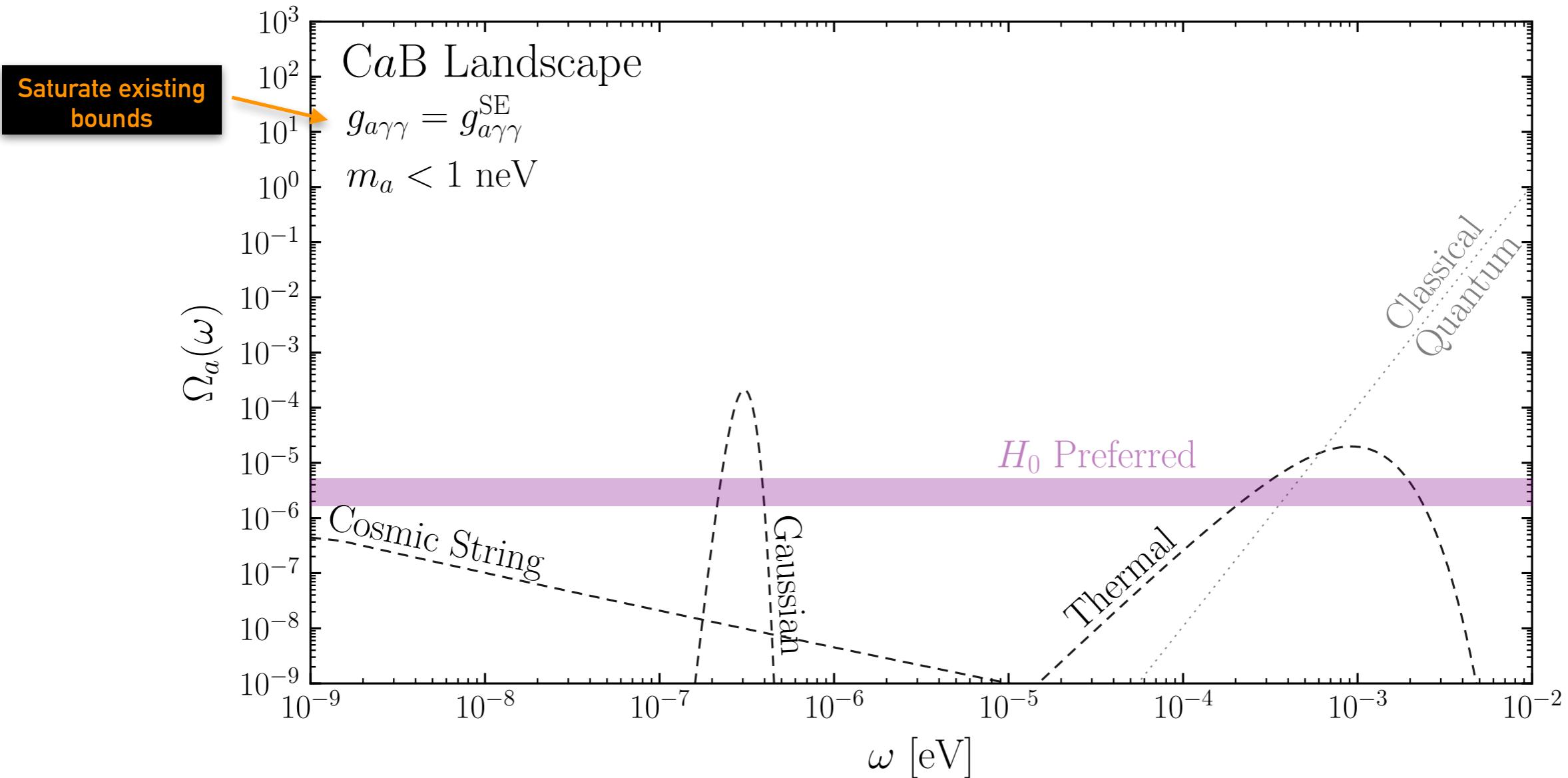
Rough Sensitivity

$$\rho_a = \rho_{\text{DM}} \left(\frac{g_{a\gamma\gamma}^{\lim}}{g_{a\gamma\gamma}^{\text{SE}}} \right)^2 \sqrt{\frac{Q_{\text{DM}}}{Q_{\text{CaB}}}}$$

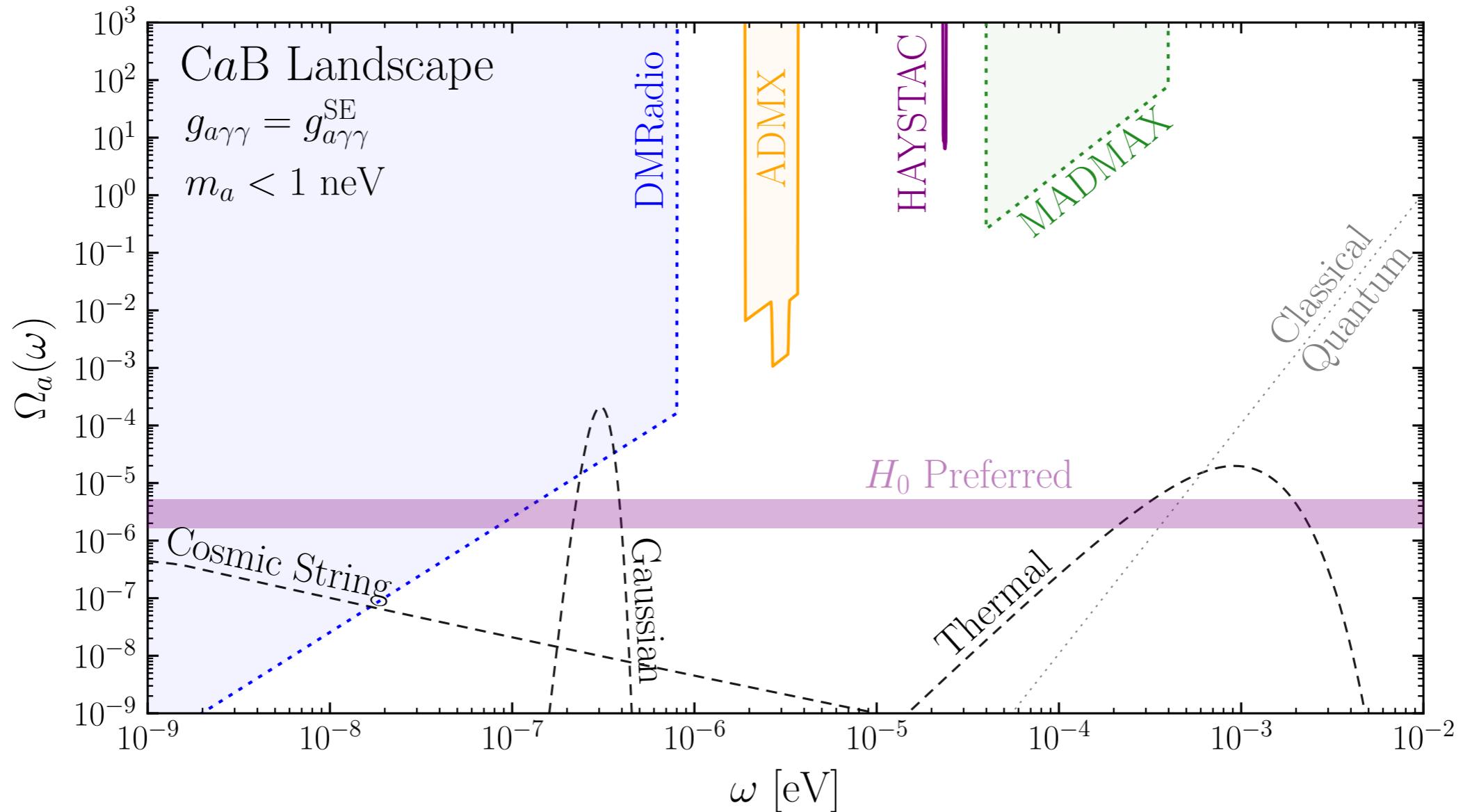
Parametric scaling confirmed by detailed calculations for both resonant and broadband instruments



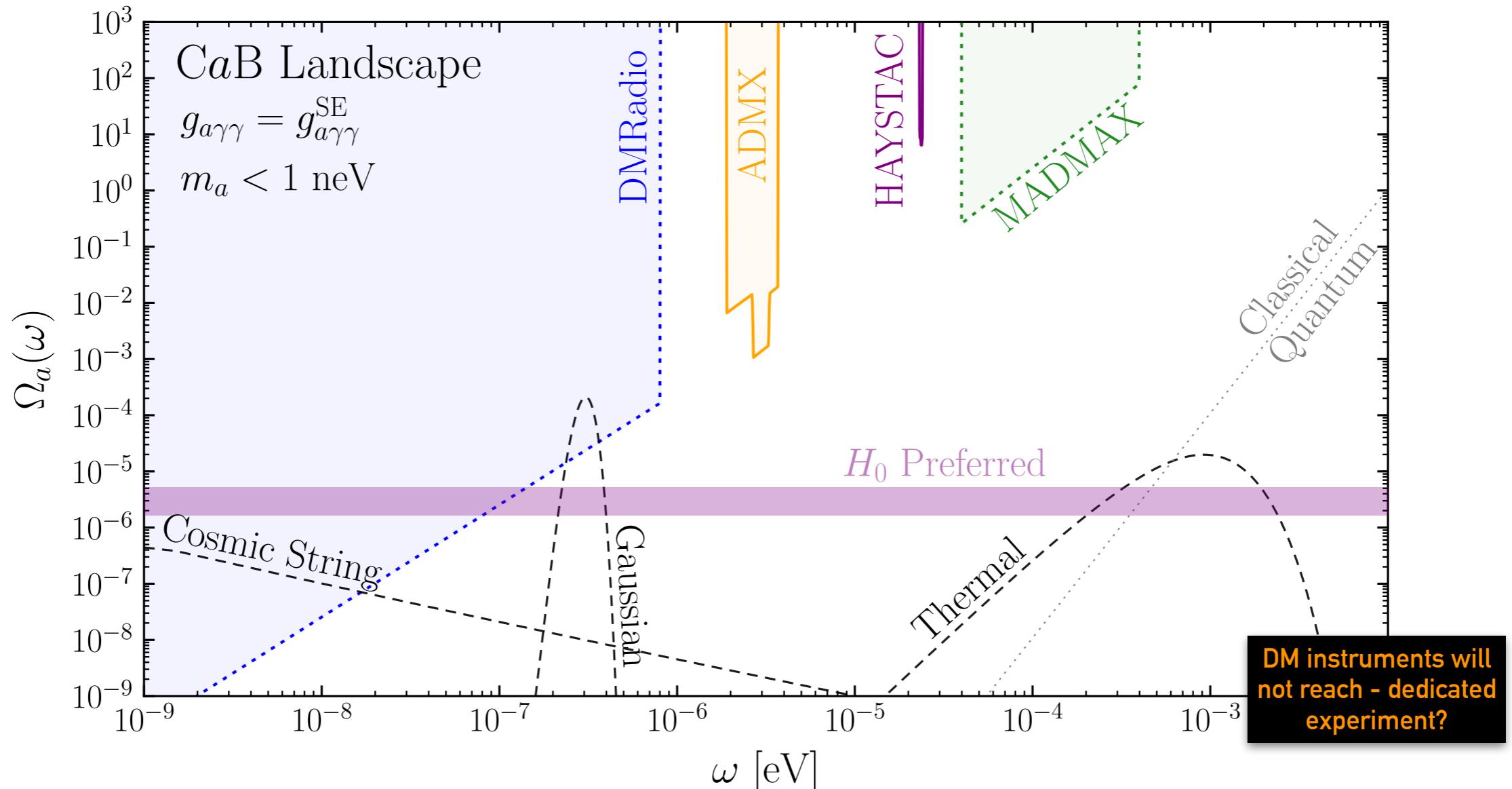
Experimental Landscape



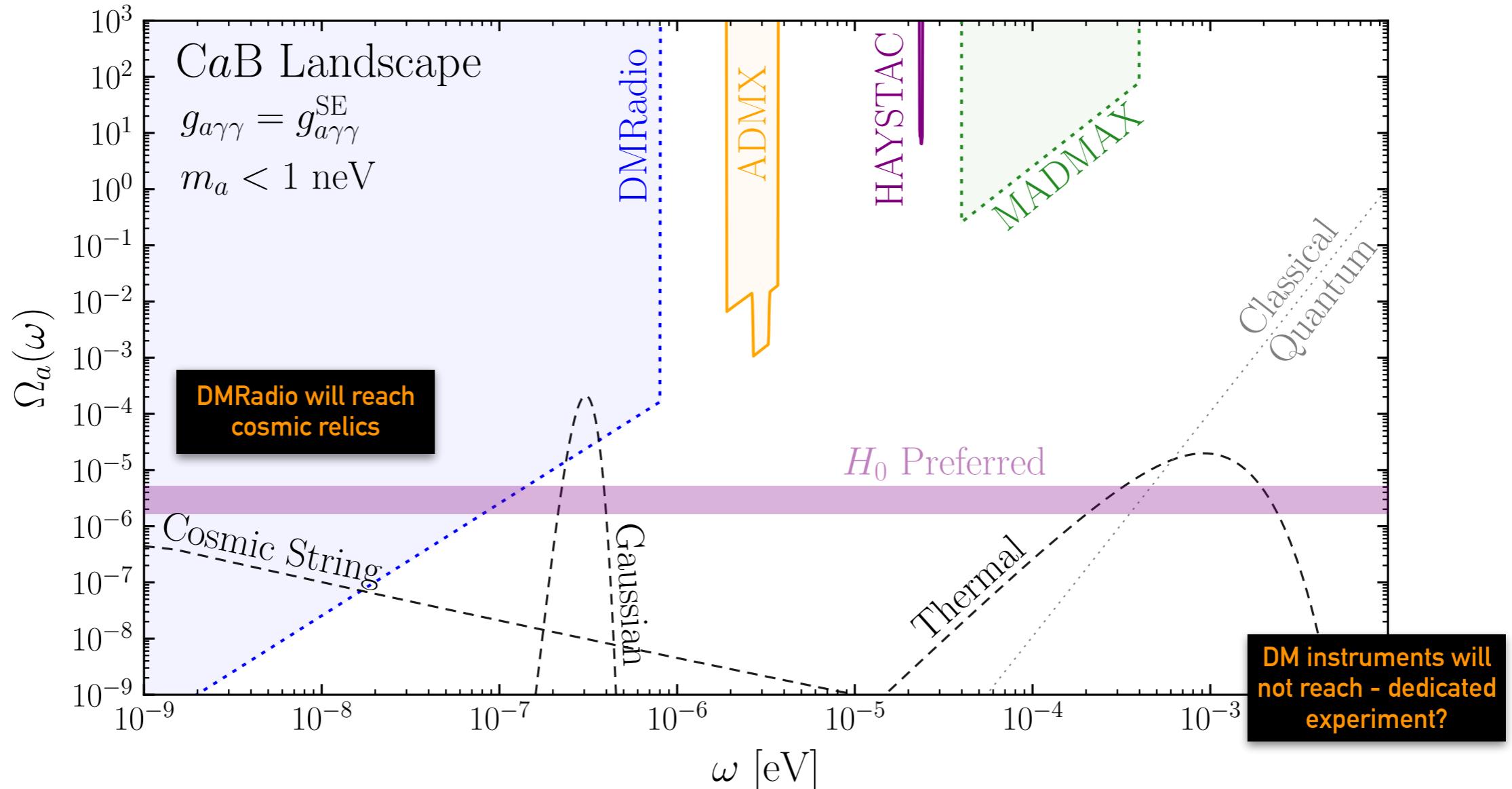
Experimental Landscape



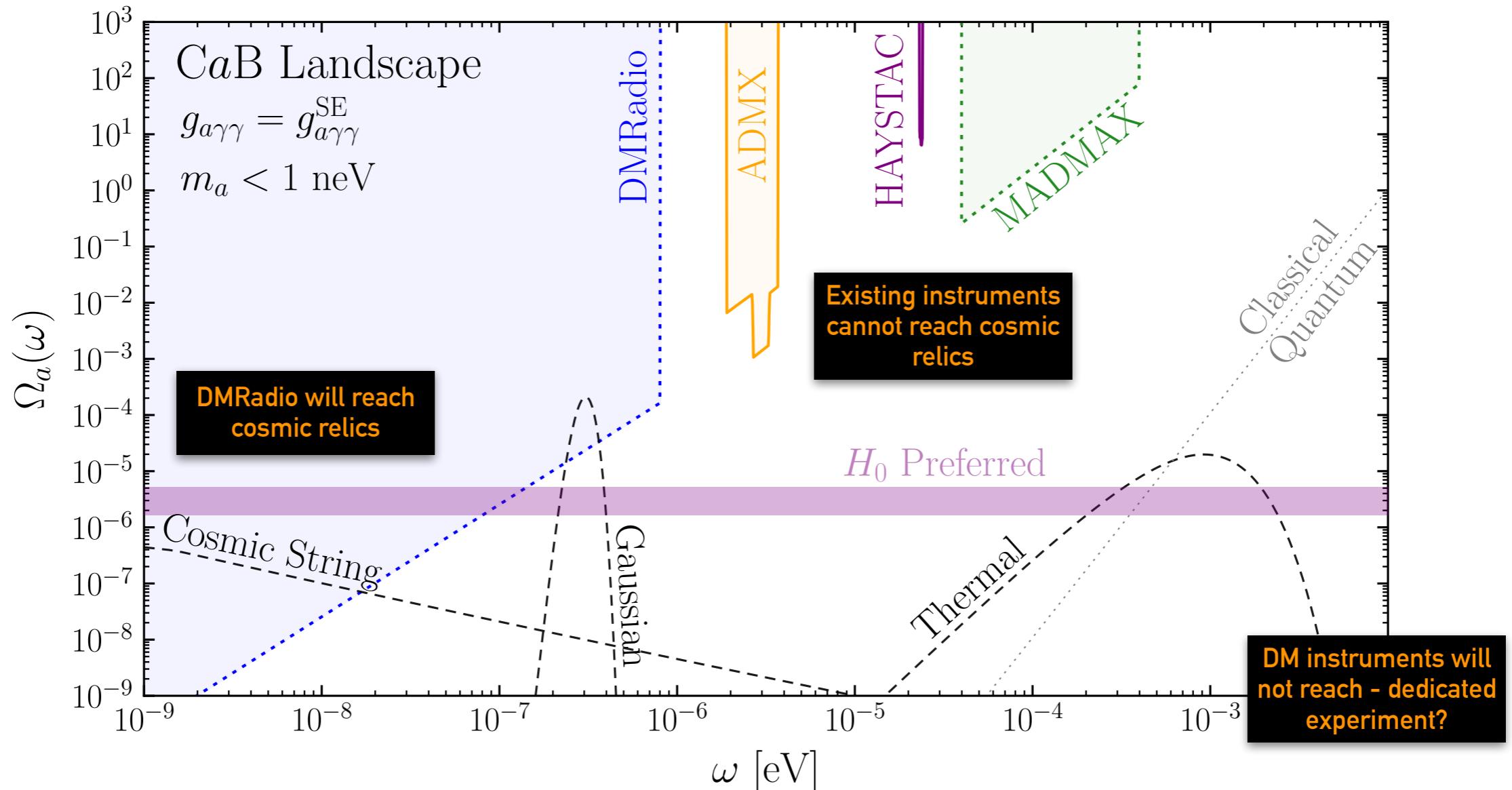
Experimental Landscape



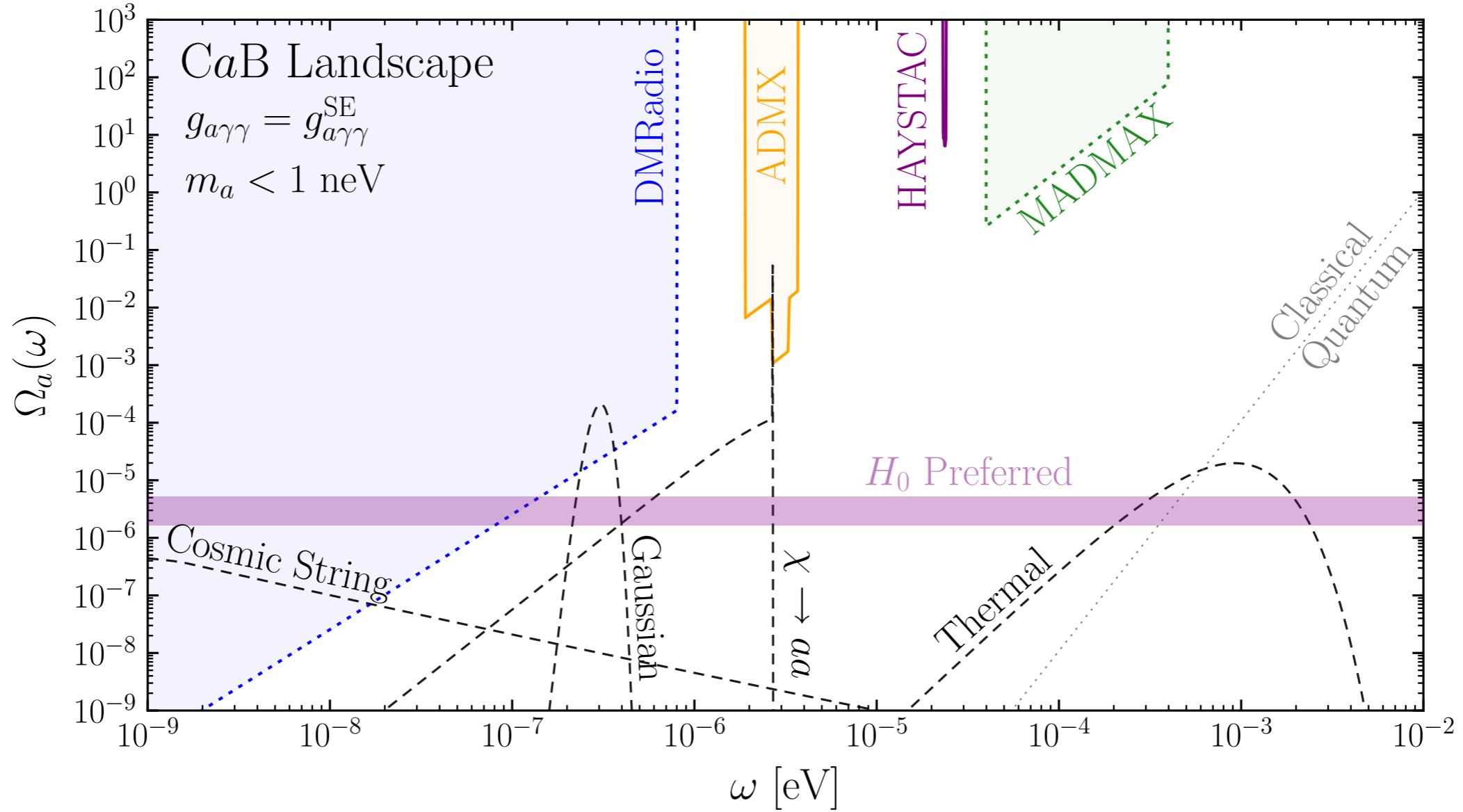
Experimental Landscape



Experimental Landscape

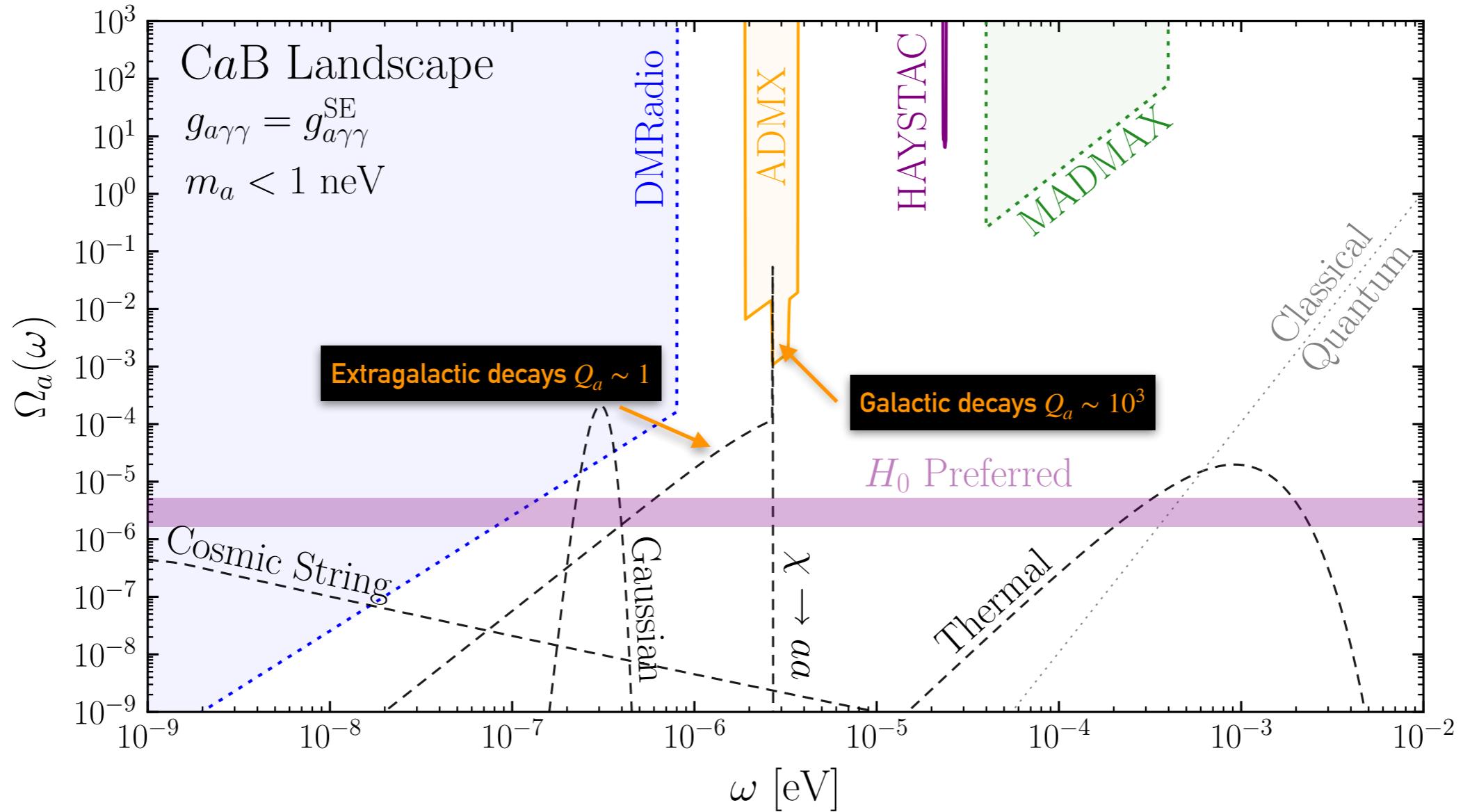


Experimental Landscape



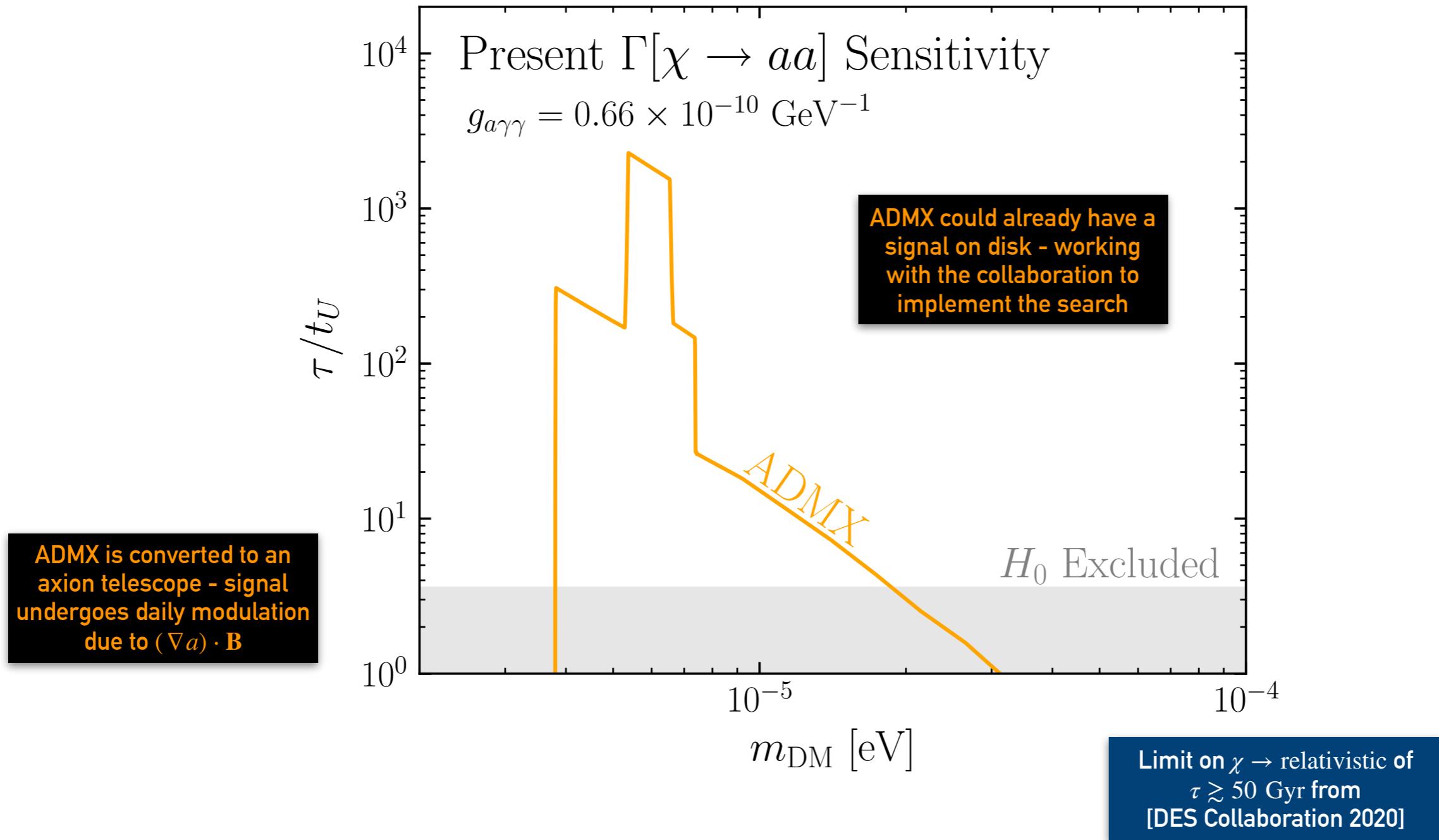
Late time production can generate $\rho_a > \rho_\gamma$
 Dark matter decay is one example

Experimental Landscape

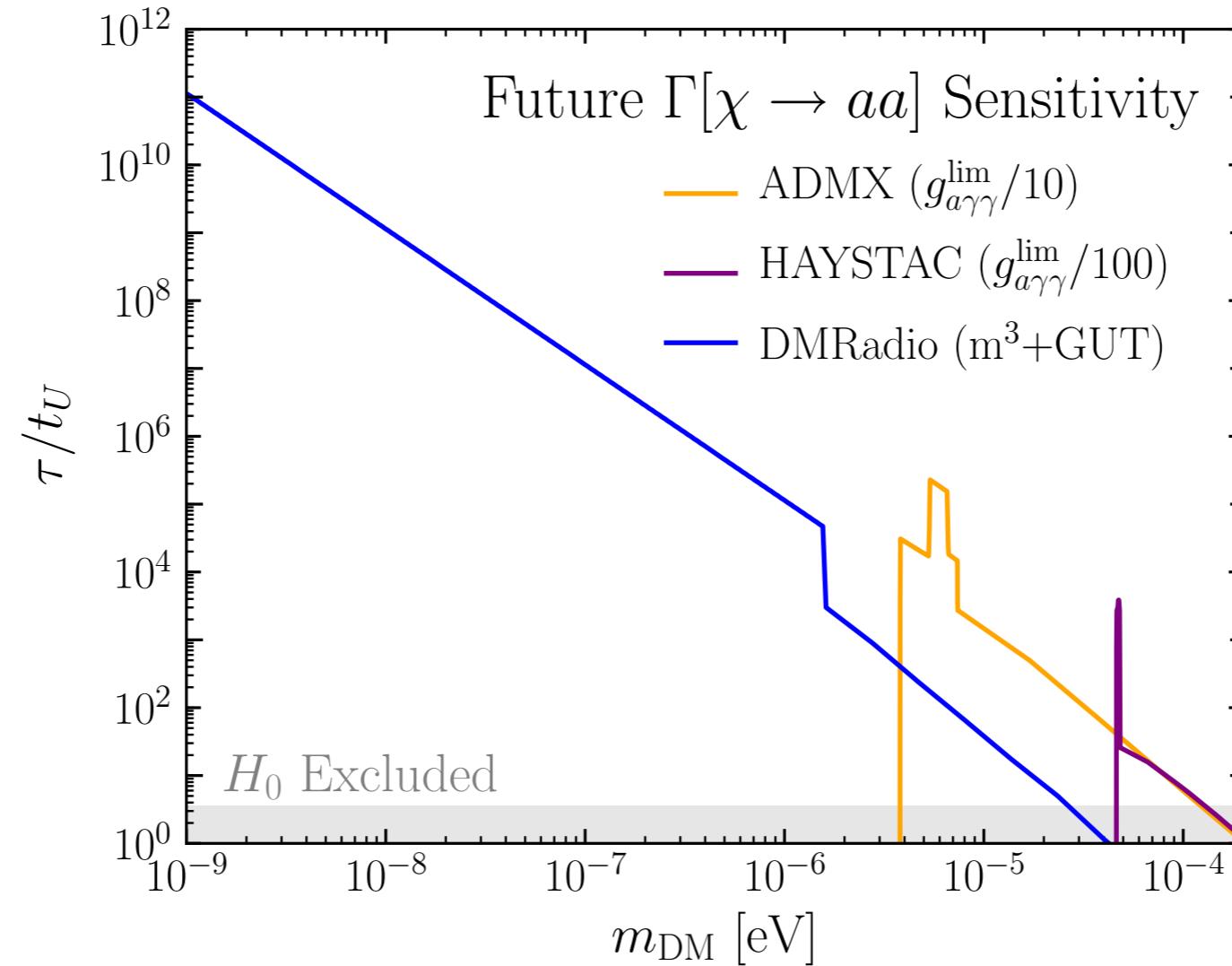


Late time production can generate $\rho_a > \rho_\gamma$
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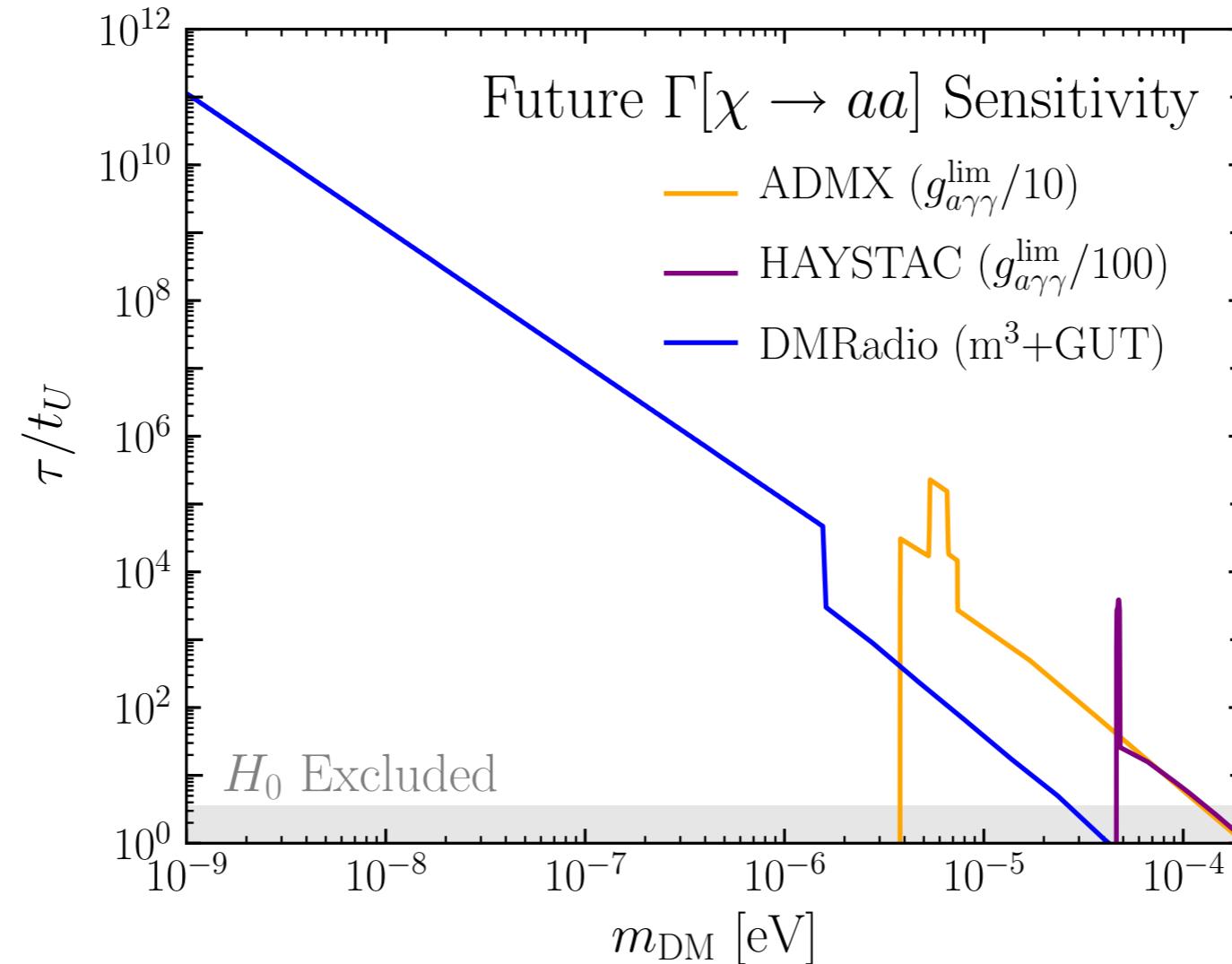
Dark Matter Decay Sensitivity



Dark Matter Decay Sensitivity



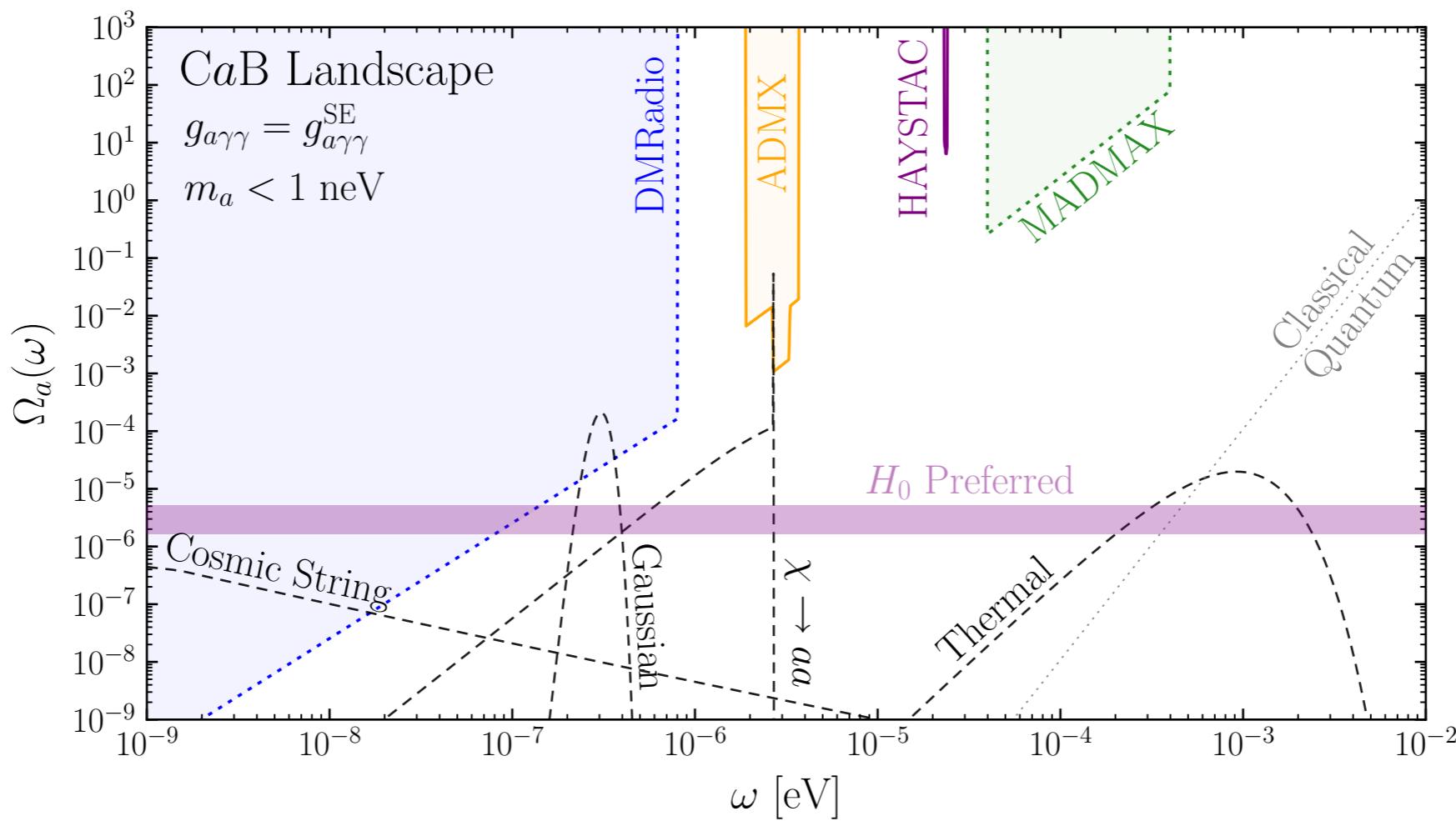
Dark Matter Decay Sensitivity



**Above neglects Bose enhancement - will be a huge effect
Working to include**

Summary

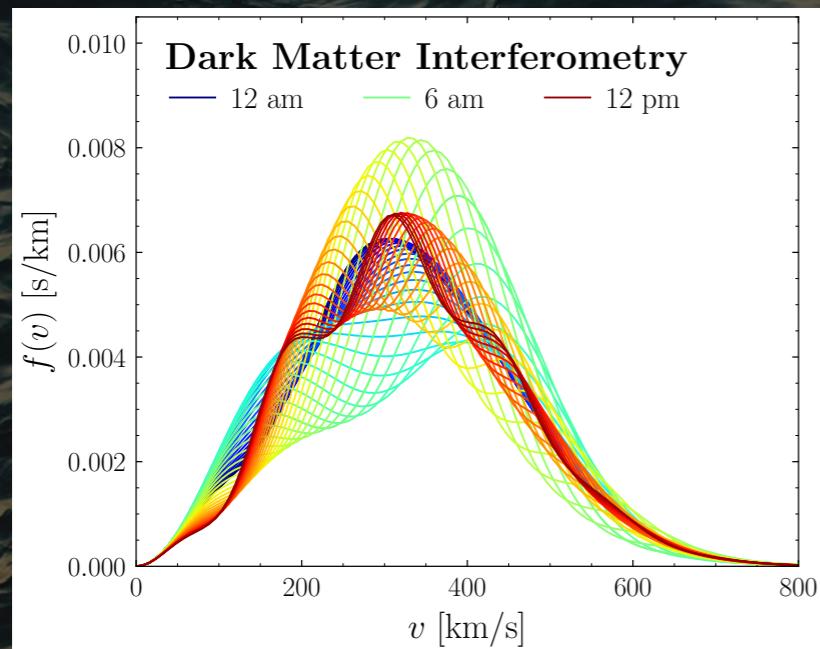
Data collected by axion DM instruments is sensitive to a cosmic axion background



Conclusion

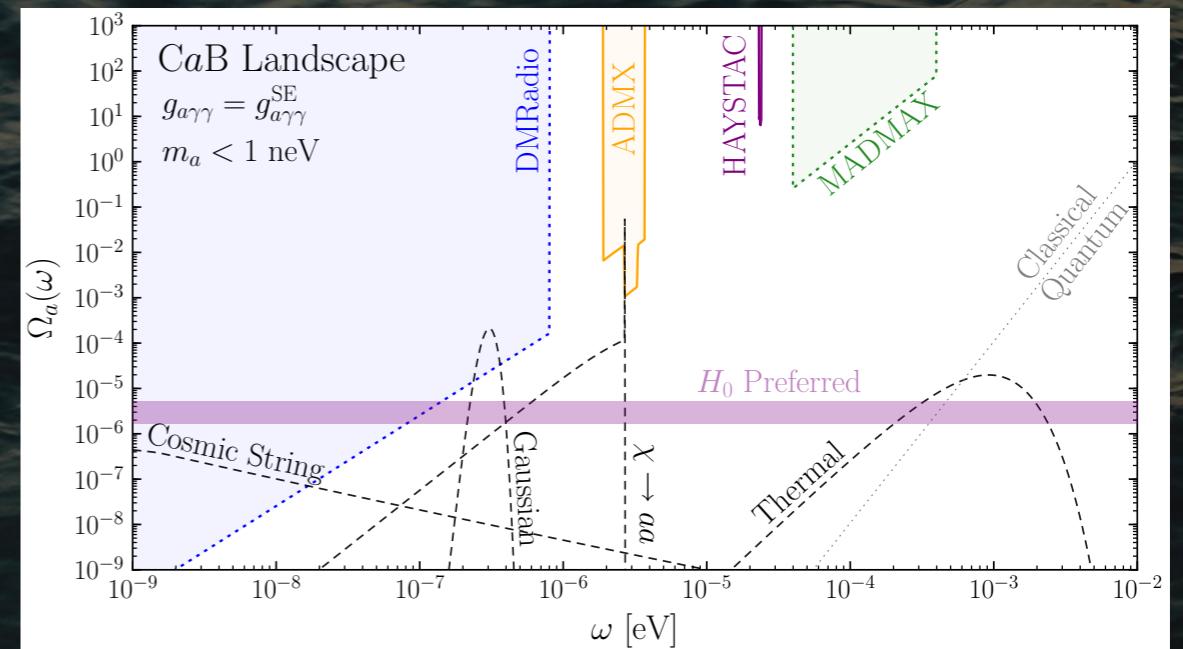
Dark Matter Interferometry

2009.14201 w/ Foster, Kahn, Nguyen, Safdi



The Cosmic Axion Background

2101.09287 w/ Dror, Murayama



Backup Slides



Stream Localization

$$\mathcal{F}_{12}^c(v) = \int d^3\mathbf{v} f(\mathbf{v}) \cos(m_a \mathbf{v} \cdot \mathbf{x}_{12}) \delta(|\mathbf{v}| - v)$$

- Velocity distribution support sets $|\mathbf{v}| \sim \bar{v}$

$$m_a \mathbf{v} \cdot \mathbf{x}_{12} \sim (m_a \bar{v} d) \hat{\mathbf{v}} \cdot \hat{\mathbf{x}}_{12}$$

- Recall, for maximum sensitivity we want $d \sim \lambda_c$

$$(m_a \bar{v} d) \hat{\mathbf{v}} \cdot \hat{\mathbf{x}}_{12} \rightarrow (m_a \bar{v} \lambda_c) \hat{\mathbf{v}} \cdot \hat{\mathbf{x}}_{12} \sim \frac{\bar{v}}{v_0} \hat{\mathbf{v}} \cdot \hat{\mathbf{x}}_{12}$$

- For bulk halo, expect $\bar{v} \sim v_0$, whereas for stream $\bar{v} \gg v_0$
- Small differences in $\hat{\mathbf{v}} \cdot \hat{\mathbf{x}}_{12}$ results in a large change in cos argument



THE COSMIC AXION BACKGROUND

Daily Modulation

Full Equations

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma} \mathbf{B} \cdot \nabla a$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\partial_t \mathbf{B}$$

$$\nabla \times \mathbf{B} = \partial_t \mathbf{E} + \mathbf{J} - g_{a\gamma\gamma} (\mathbf{E} \times \nabla a - \partial_t a \mathbf{B})$$



THE COSMIC AXION BACKGROUND

Daily Modulation

Assume only large static \mathbf{B} field

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma} \mathbf{B} \cdot \nabla a$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\partial_t \mathbf{B}$$

$$\nabla \times \mathbf{B} = \partial_t \mathbf{E} + \mathbf{J} + g_{a\gamma\gamma} \partial_t a \mathbf{B}$$



Daily Modulation

Assume only large static \mathbf{B} field

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma} \mathbf{B} \cdot \nabla a$$

$$\nabla \cdot \mathbf{B} = 0 \qquad \textit{Effective Charge}$$

$$\nabla \times \mathbf{E} = -\partial_t \mathbf{B}$$

$$\nabla \times \mathbf{B} = \partial_t \mathbf{E} + \mathbf{J} + g_{a\gamma\gamma} \partial_t a \mathbf{B}$$

Effective Current



THE COSMIC AXION BACKGROUND

Daily Modulation

Sensitive to the incident direction

$$\mathbf{B} \cdot \nabla a = a(t) \mathbf{k} \cdot \mathbf{B}$$



THE COSMIC AXION BACKGROUND

Daily Modulation

Power deposited sensitive to α

$$P_a^{\text{CaB}} = \frac{\pi}{8} \sin^4 \alpha g_{a\gamma\gamma}^2 Q_a B_0^2 V C \frac{\rho_a}{\bar{\omega}}$$

Daily modulation
in the signal!



Bose Enhancement

Relevant when $f_a \gg 1$

$$f_a = \frac{2\pi^2}{\omega^3} \frac{d\rho_a}{d\omega} \simeq 4 \times 10^{10} \left(\frac{Q_a}{1} \right) \left(\frac{\rho_a}{\rho_\gamma} \right) \left(\frac{\bar{\omega}}{1 \text{ }\mu\text{eV}} \right)^{-4}$$

Large over the entire range we consider

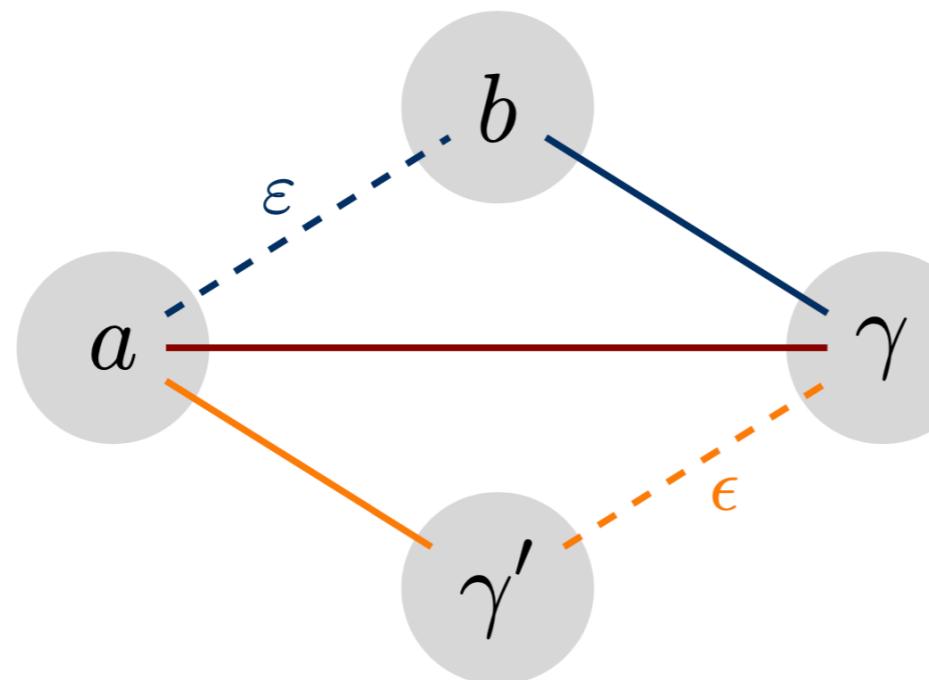


Dark Matter Decaying to Axions

example
model

$$V(\Phi) = \lambda^2 \left(|\Phi|^2 - f_a^2/2 \right)^2 \quad \Phi = (\chi + f_a) e^{ia/f_a}$$

$$\frac{\Gamma_{\varphi \rightarrow aa}}{H_0} \simeq \left(\frac{m_\varphi}{10 \text{ } \mu\text{eV}} \right)^3 \left(\frac{100 \text{ MeV}}{f_a} \right)^2 \rightarrow \text{smiley face emoji}$$



$$\frac{\varepsilon \alpha}{4\pi f_b}$$

$$\frac{\alpha}{4\pi f_a}$$

$$\frac{\epsilon^2 \alpha'}{4\pi f_a}$$

Slide courtesy of Jeff Dror

Parametric Resonance

$$V(\Phi) = \lambda^2 \left(|\Phi|^2 - f_a^2/2 \right)^2$$

Oscillations when
 $m_\chi^{\text{eff}}(\chi_i) \simeq \lambda \chi_i \sim H$

Typical energy:

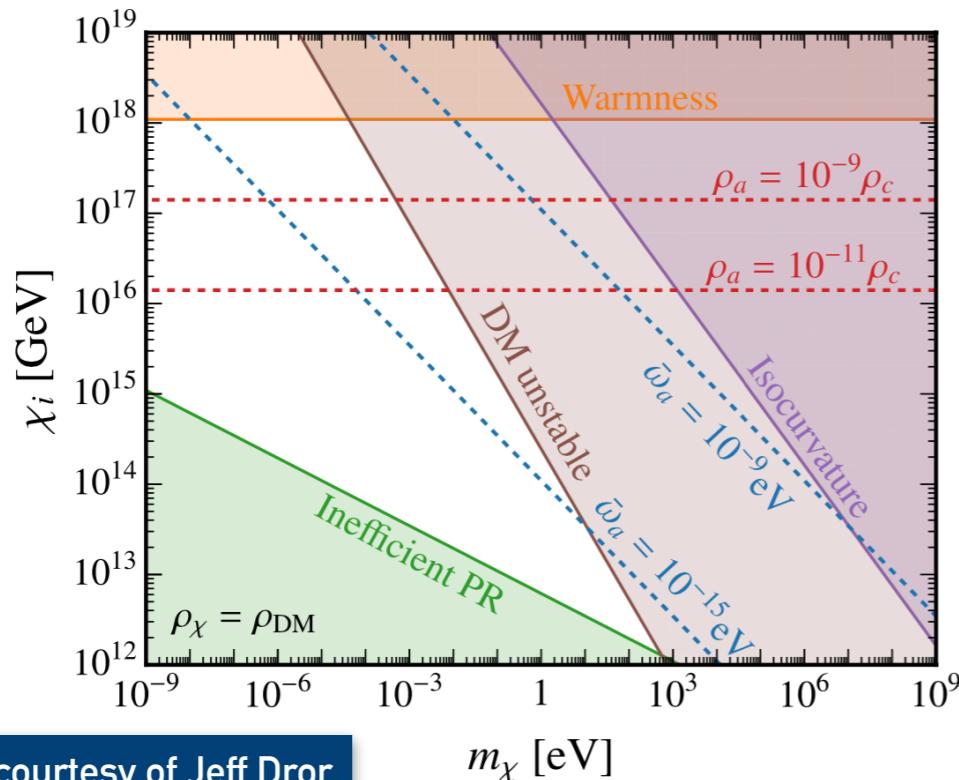
$$\bar{\omega}_a \sim m_\chi^{\text{eff}}(\chi_i) \left(\frac{s(T_0)}{s(T_{\text{osc}})} \right)^{1/3} \sim 10^{-15} \text{ eV} \left(\frac{m_\chi^{\text{eff}}(\chi_i)}{\text{MeV}} \right)^{1/2}$$

Energy density:

$$\Omega_a \sim 3 \times 10^{-7} \left(\frac{\chi_i}{M_{\text{Pl}}} \right)^2$$

detectable?

Assume χ dark matter



Slide courtesy of Jeff Dror

