

# Dial M for Muons

Gordan Krnjaic



+Gustavo Marques-Tavares, Diego Redigolo, Kohsaku Tobioka  
1902.07715 *Phys.Rev.Lett.* (2020)

+Yonatan Kahn, Nhan Tran, Andrew Whitbeck  
1804.03144 *JHEP* (2018)

+Rodolfo Capdevilla, David Curtin, Yonatan Kahn  
2101.10334, 2006.16277 *Phys.Rev.D* (2021)

APEC Seminar June, 9 2021

# Overview

Current Status of  $g-2$

Singlet Models

Electroweak Models



# Overview

**Current Status of  $g-2$**

**Singlet Models**

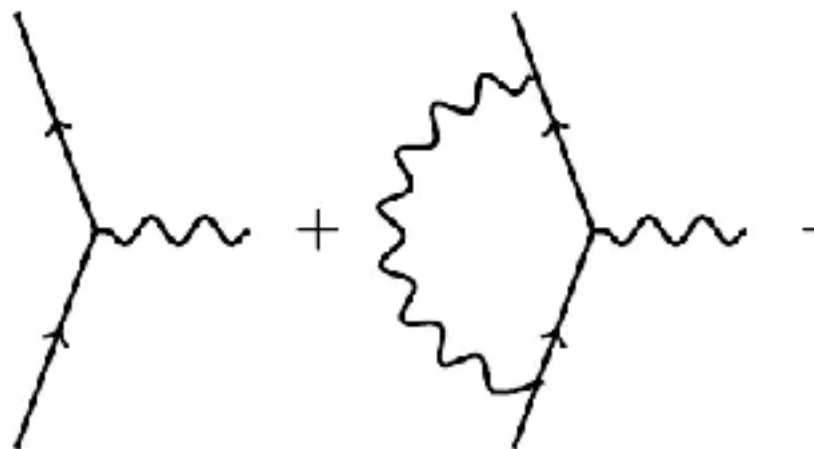
**Electroweak Models**

# Muon Anomalous Magnetic Moment

Lepton dipole moment  $\vec{\mu}_\ell = \pm g_\ell \frac{e}{2m_\ell} \vec{S}$   $a \equiv \frac{g - 2}{2}$

Tree level QED prediction:  $a = 0$

Quantum loop corrections:  $a \neq 0$



The image shows two Feynman diagrams representing the calculation of the lepton magnetic moment. The first diagram is a tree-level vertex where a lepton line splits and recombines with a photon line. The second diagram is a one-loop correction where a lepton line forms a loop with a photon line, and a photon line connects the loop to an external photon line. These diagrams are separated by a plus sign and followed by an ellipsis, indicating a series of higher-order corrections.

$$+ \dots \rightarrow g = 2 + \frac{\alpha}{2\pi} + \dots$$

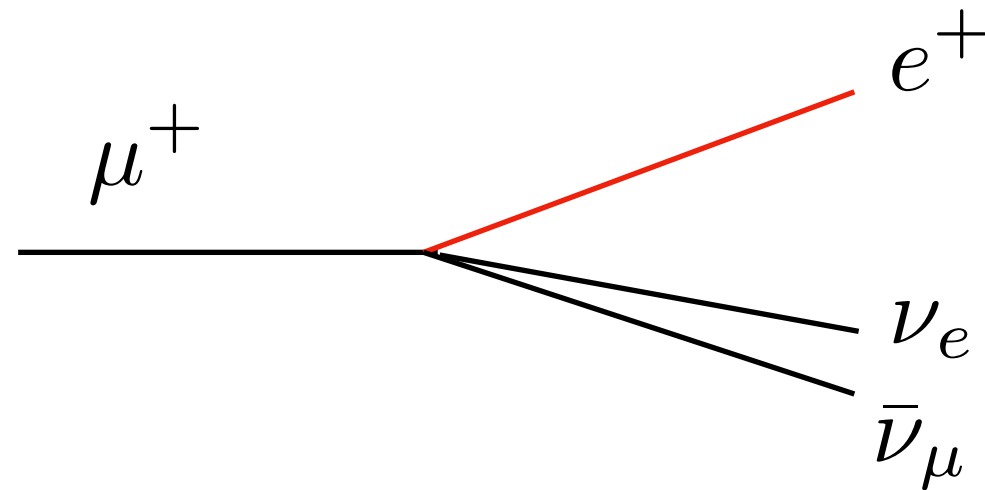
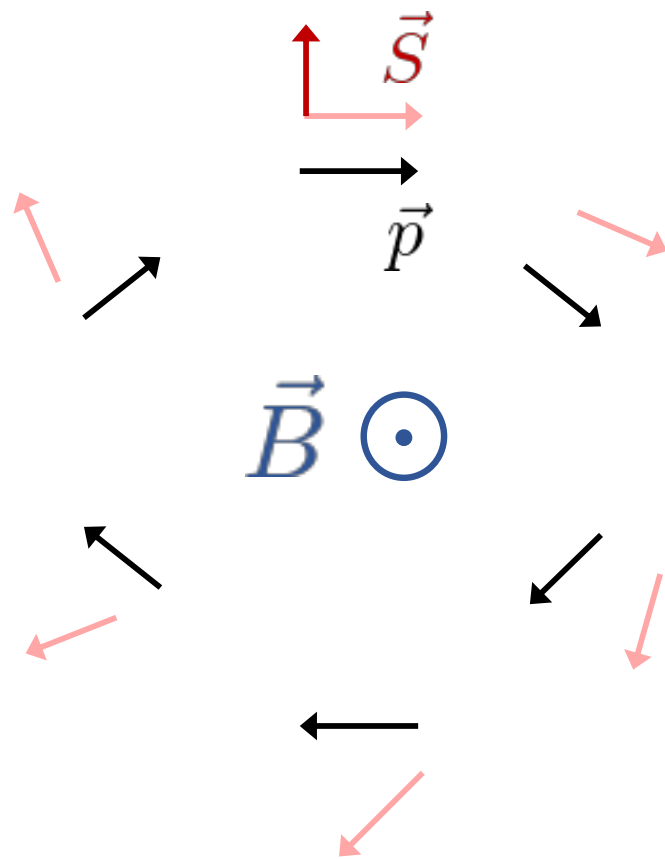
Sensitive to all known *and unknown* particles coupled to leptons

For electrons agrees SM to  $\sim 12$  decimals, best prediction in history

# Spin precession in a uniform B field

$$\omega_a = a_\mu \frac{eB}{2m_\mu}$$

Lab Frame



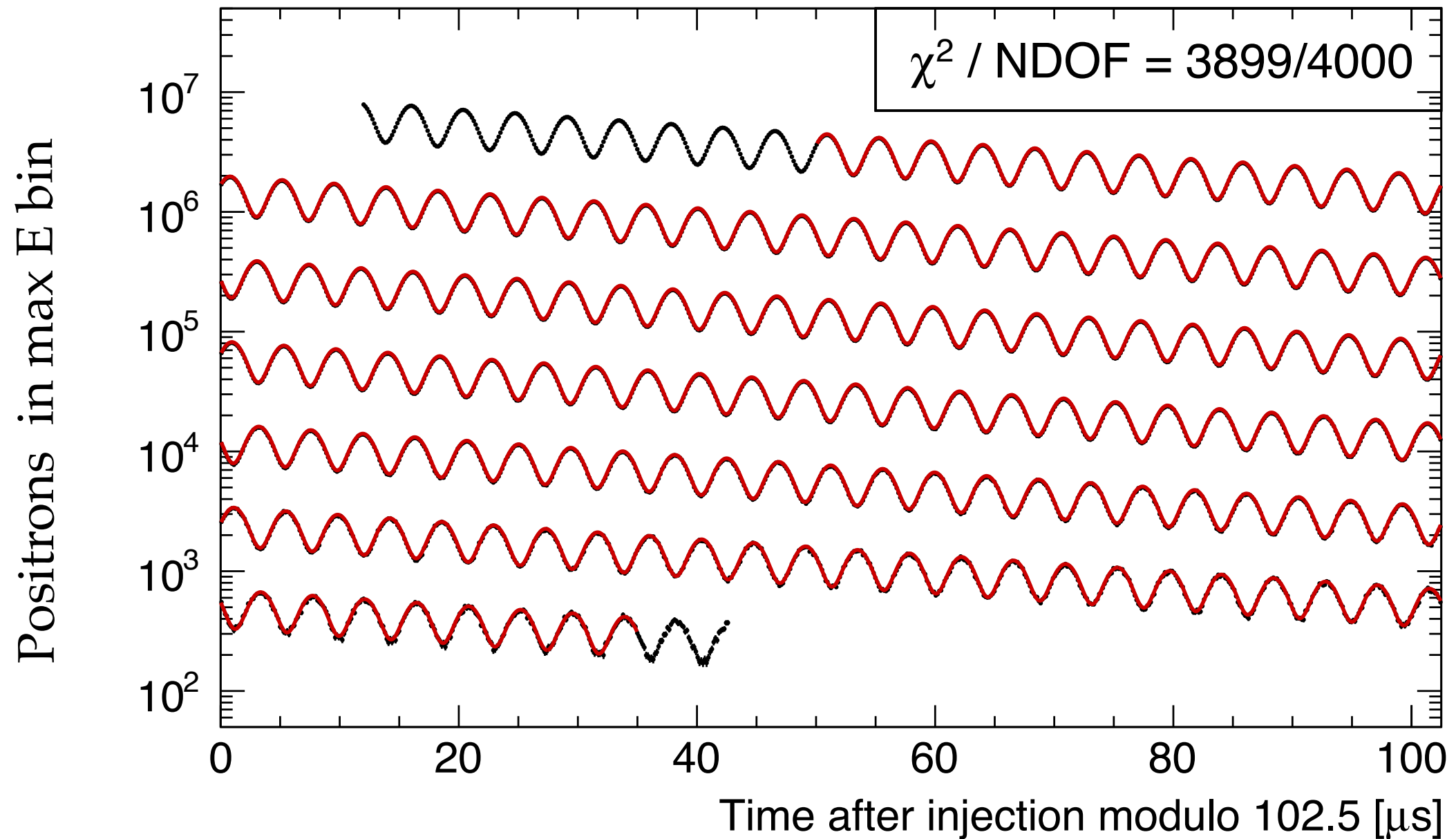
$$\frac{d\Gamma}{dE} = A [1 - B(\vec{s} \cdot \vec{p})]$$

$$\vec{s} \cdot \vec{p} \propto \cos \omega_a t$$

Upon  $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$  decay  $e^+$  emitted preferentially along  $\vec{S}$   
 Asymmetry in  $e^+$  energy distribution measures  $\omega_a$

# Spin precession in a uniform B field

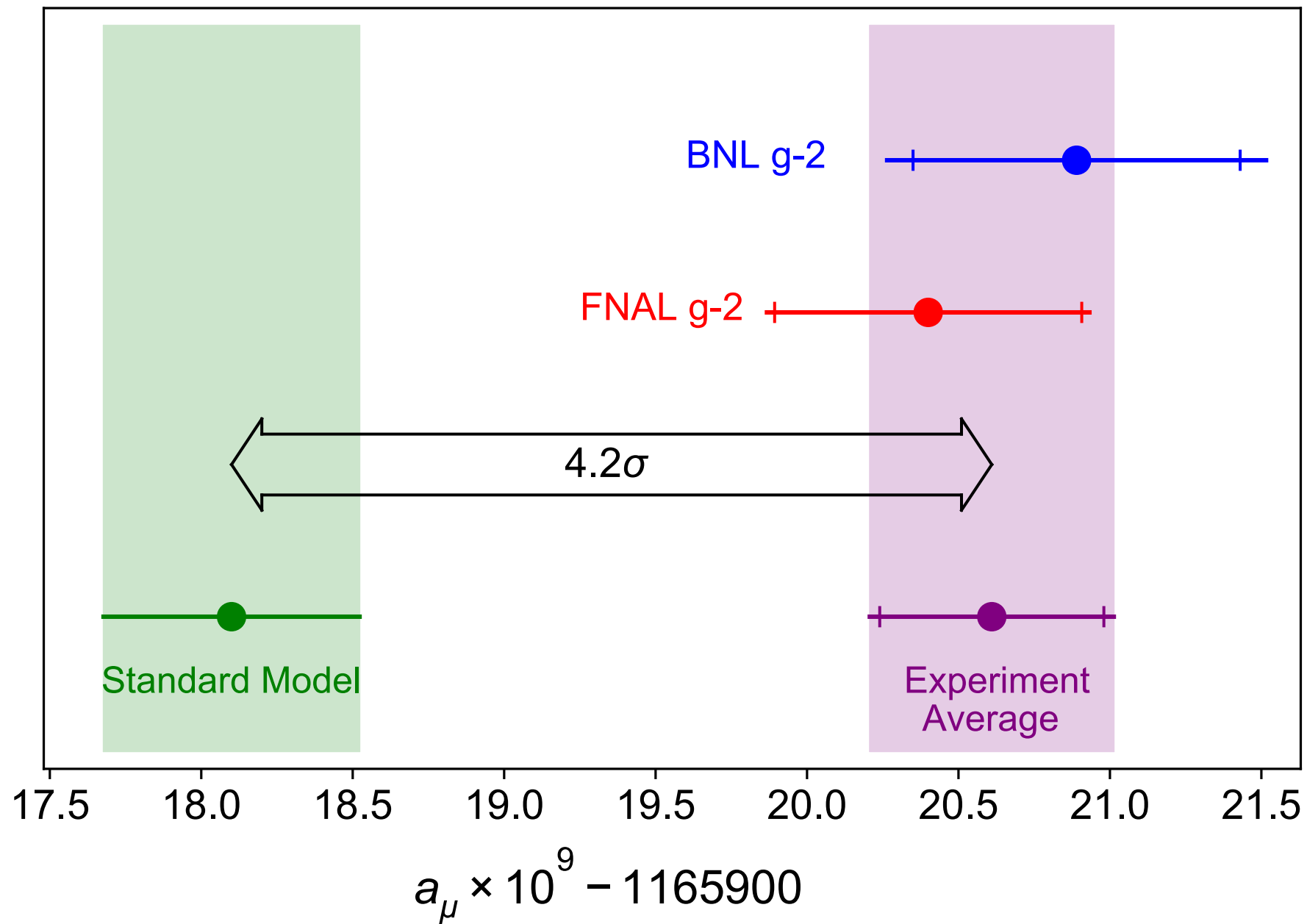
$$\omega_a = a_\mu \frac{eB}{2m_\mu}$$



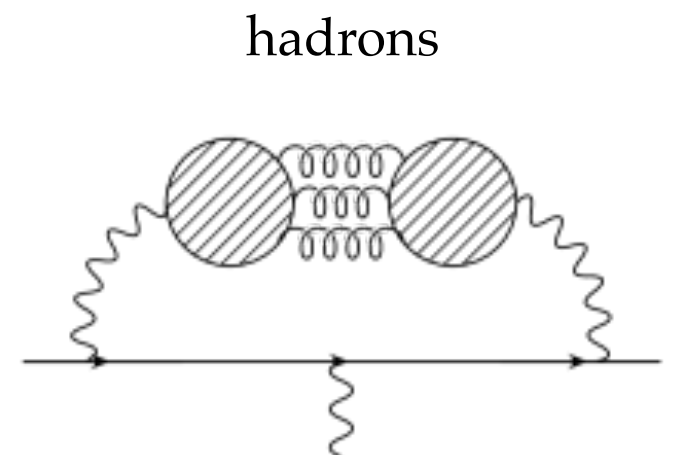
$$N_e(t) \propto e^{-t/\tau_\mu} (1 + B' \cos \omega_a t)$$

g-2 collaboration 2104.03247

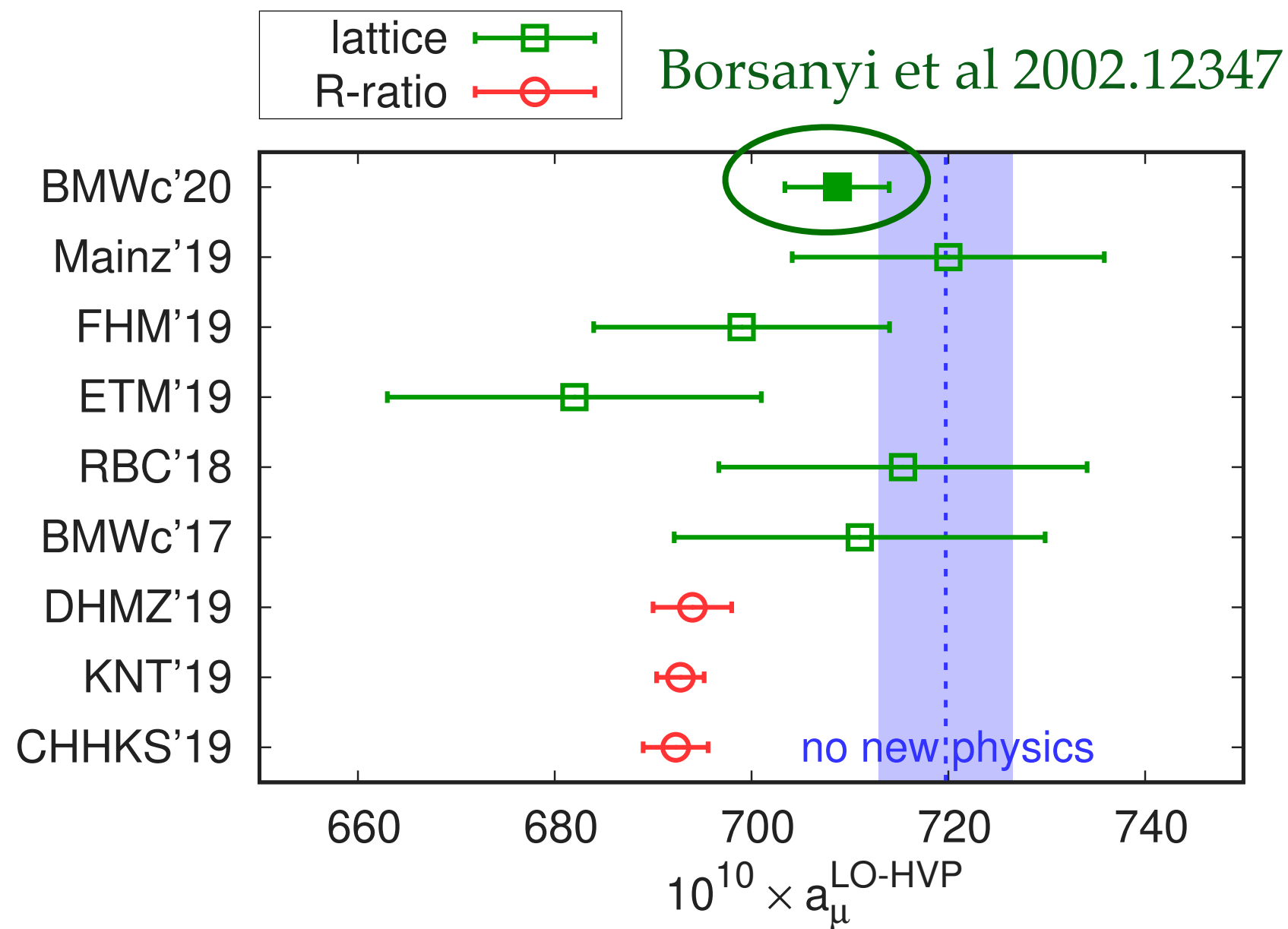
# Theory vs. Experiment



Theory uncertainty driven by  
non-perturbative QCD corrections



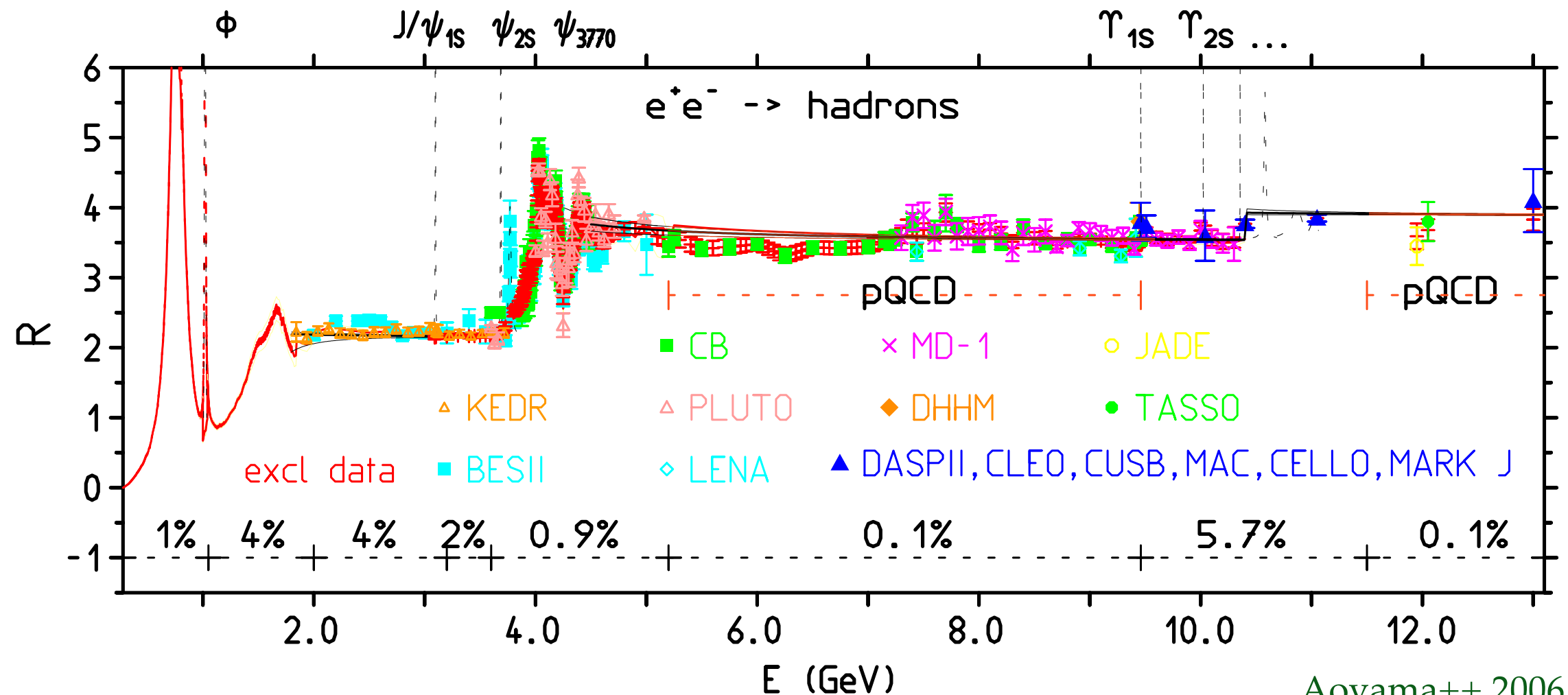
# Comparing SM Theory Calculations



Recent lattice BMWc result in tension with data driven R-ratio method  
... but it's closer to experiment

# R-Ratio Calculations

Hadronic contributions can be extracted from  $e^+e^- \rightarrow \text{hadrons}$  data

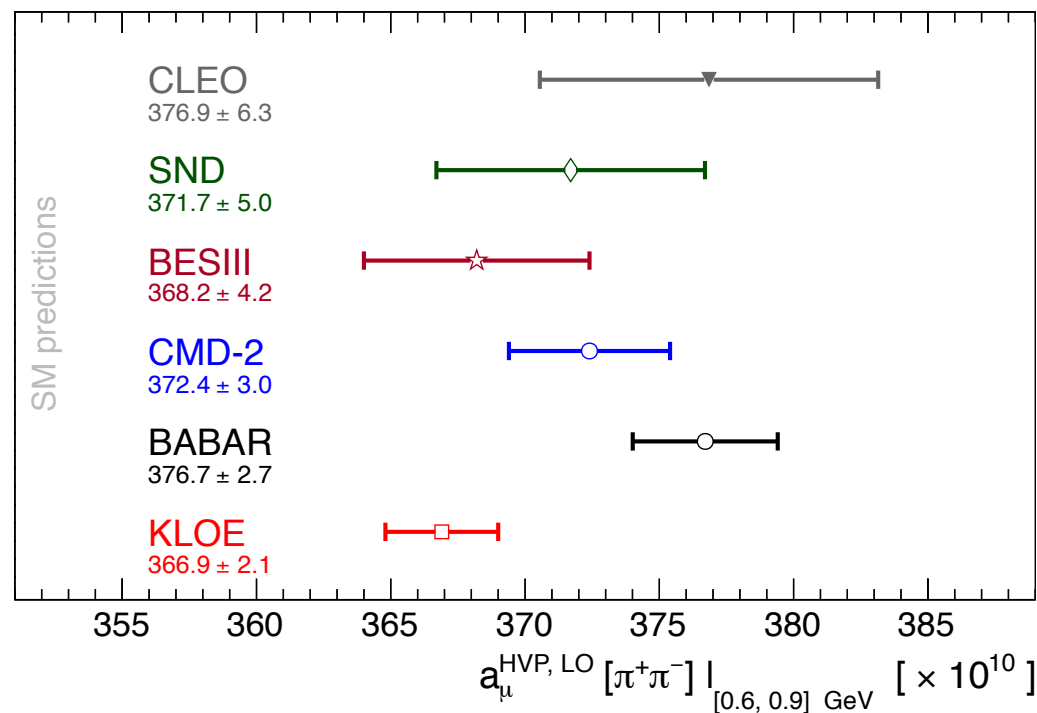


Aoyama++ 2006.04822

$$a_{\mu}^{\text{HVP, LO}} = \frac{\alpha^2}{3\pi^2} \int_{M_{\pi}^2}^{\infty} \frac{K(s)}{s} R(s) ds$$

$$R(s) \propto \sigma(e^+e^- \rightarrow \text{hadrons})$$

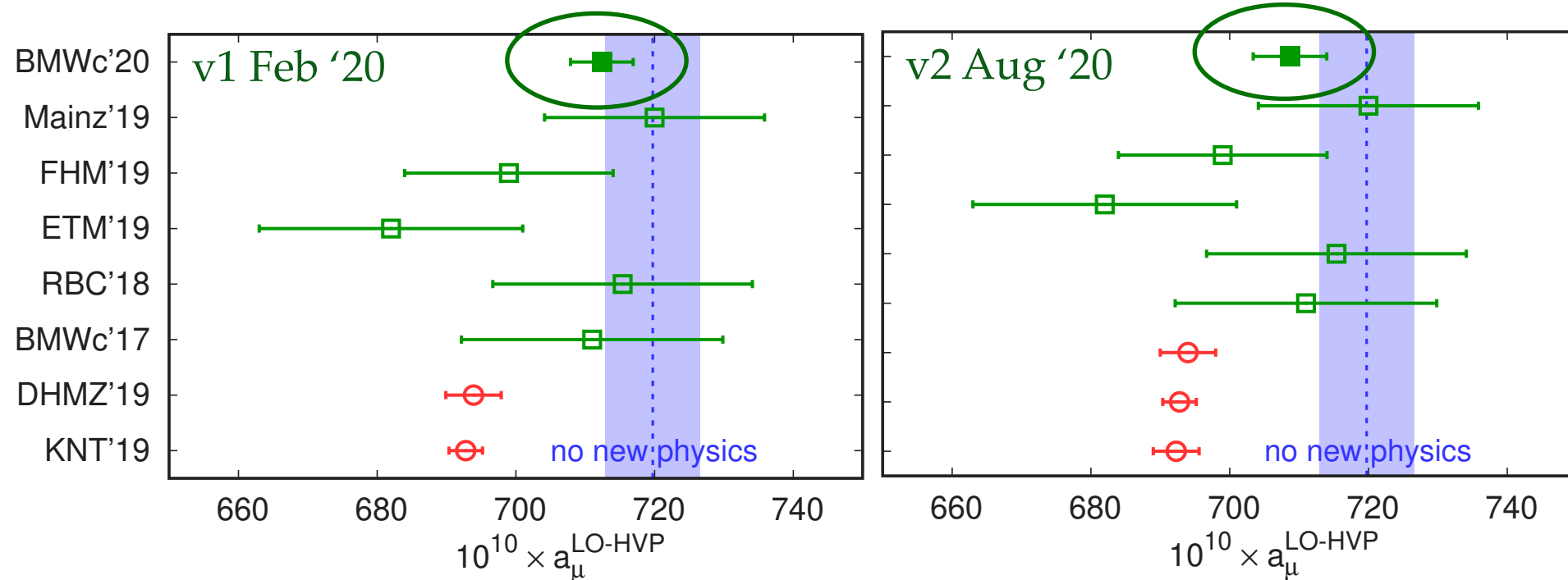
# R-Ratio Possible issue of internal consistency across full data set?



Aoyama++ 2006.04822

Borsanyi++ 2002.12347

## Lattice



Possible issue of extrapolating to continuum limit?

BMW also makes electroweak fit worse and in tension with  $e^+e^- \rightarrow \pi\pi$



# What should we believe?

## 1) Issue with with R-ratio calculations?

Possible, but nothing obvious (maybe tension in data?)

## 2) Issue with lattice calculations?

Also possible, need confirmation from other groups

## 3) R-ratio correct, but unknown experimental systematic?

After new data, this is extremely unlikely

This is the main new thing we have learned

## 4) New BSM particles contributing to loops?

# Overview

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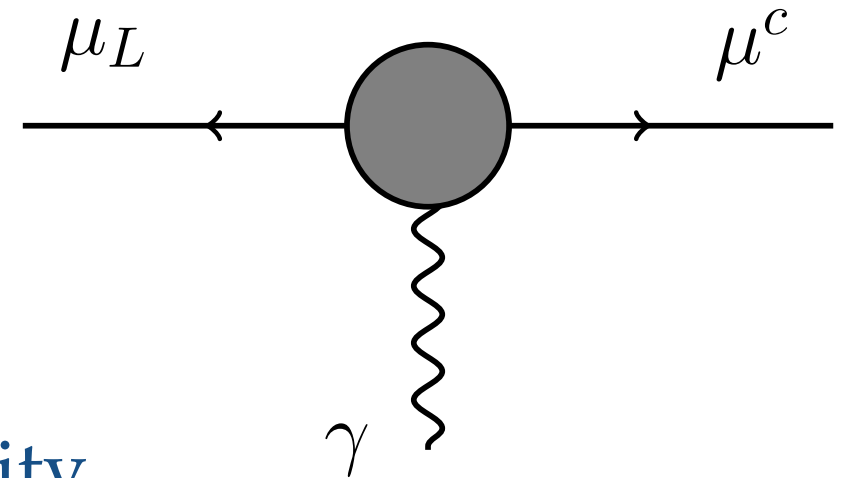
**Singlet Models**

Electroweak Models

# Effective Operator Analysis

Generic interaction to g-2 can be written as

$$\mathcal{L}_{\text{eff}} = \frac{1}{\Lambda} (\mu_L \sigma^{\nu\rho} \mu^c) F_{\nu\rho}$$



In 2 component notation: arrows track chirality

Arrows point in **opposite** direction (**chiral flip**)

but like with Yukawas, this is not gauge invariant

$$\mathcal{L}_{\text{mass}} = y_\mu H^\dagger L \mu^c \rightarrow y_\mu v \mu_L \mu^c \equiv m_\mu \mu_L \mu^c$$

... so also need an **EWSB insertion**

$$\psi_{\text{dirac}} = \begin{pmatrix} \mu_L \\ \mu^{c\dagger} \end{pmatrix}$$

# Effective Operator Analysis

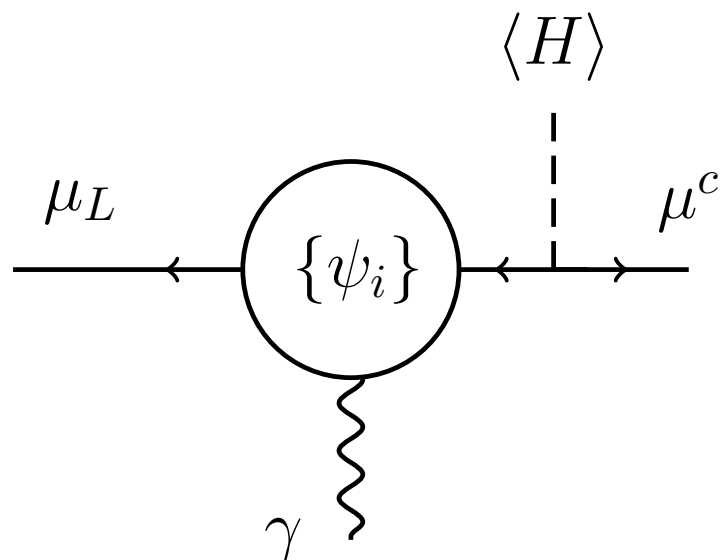
$$\mathcal{L}_{\text{eff}} = C_{\text{eff}} \frac{v}{M^2} (\mu_L \sigma^{\nu\rho} \mu^c) F_{\nu\rho} + \text{h.c.}$$

Do EWSB + chiral flip come from muon mass insertion?

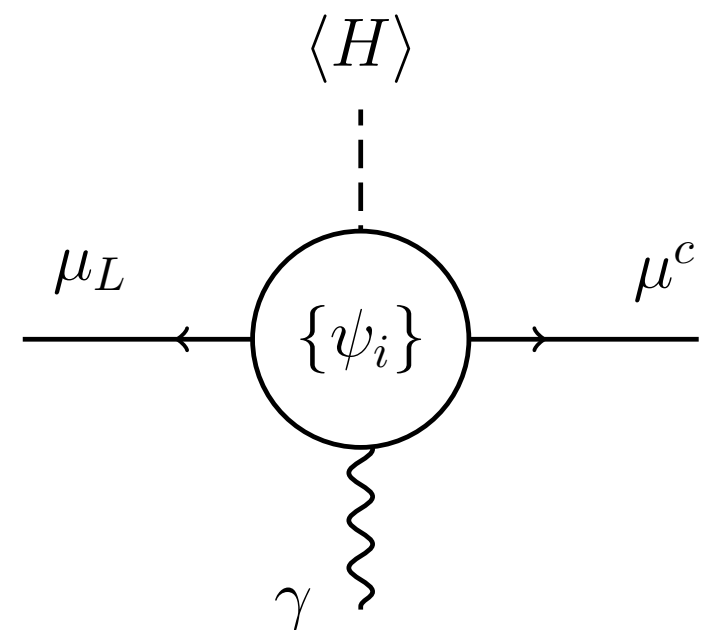
YES

NO

Singlet Models

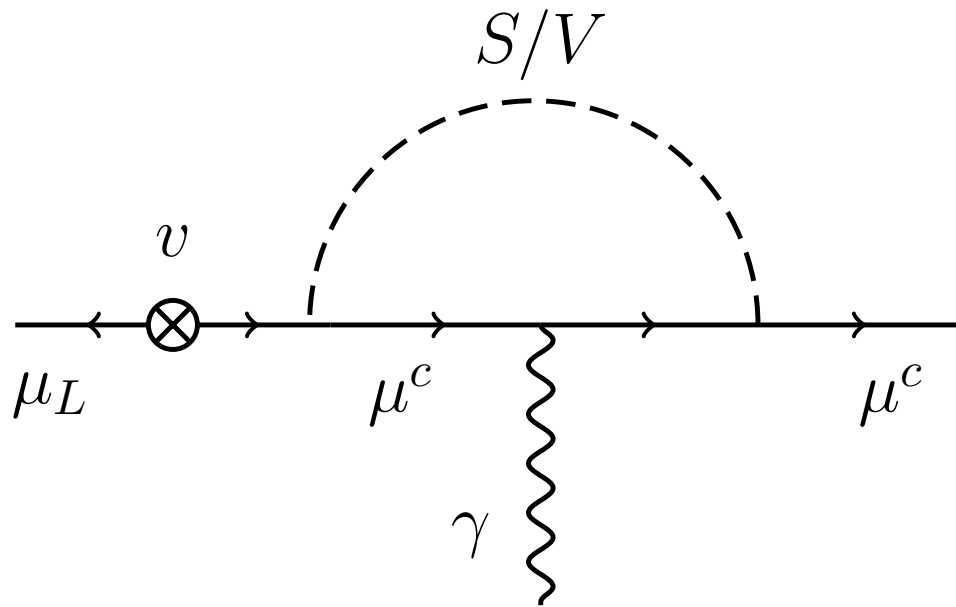


Electroweak Models



# Singlet Models

## Chiral flip and EWSB on muon line



## Simple BSM Landscape

Must be scalar (S) or vector (V)

Must be SM gauge singlet

Must be MeV-TeV (BBN / unitarity)

$$\Delta a_\mu^V = \frac{g_V^2}{4\pi^2} \int_0^1 dz \frac{m_\mu^2 z(1-z)^2}{m_\mu^2(1-z)^2 + m_V^2 z} \simeq 1.3 \times 10^{-10} \left( \frac{g_V}{10^{-4}} \right)^2 \quad (m_V \ll m_\mu)$$

# Options For Singlets

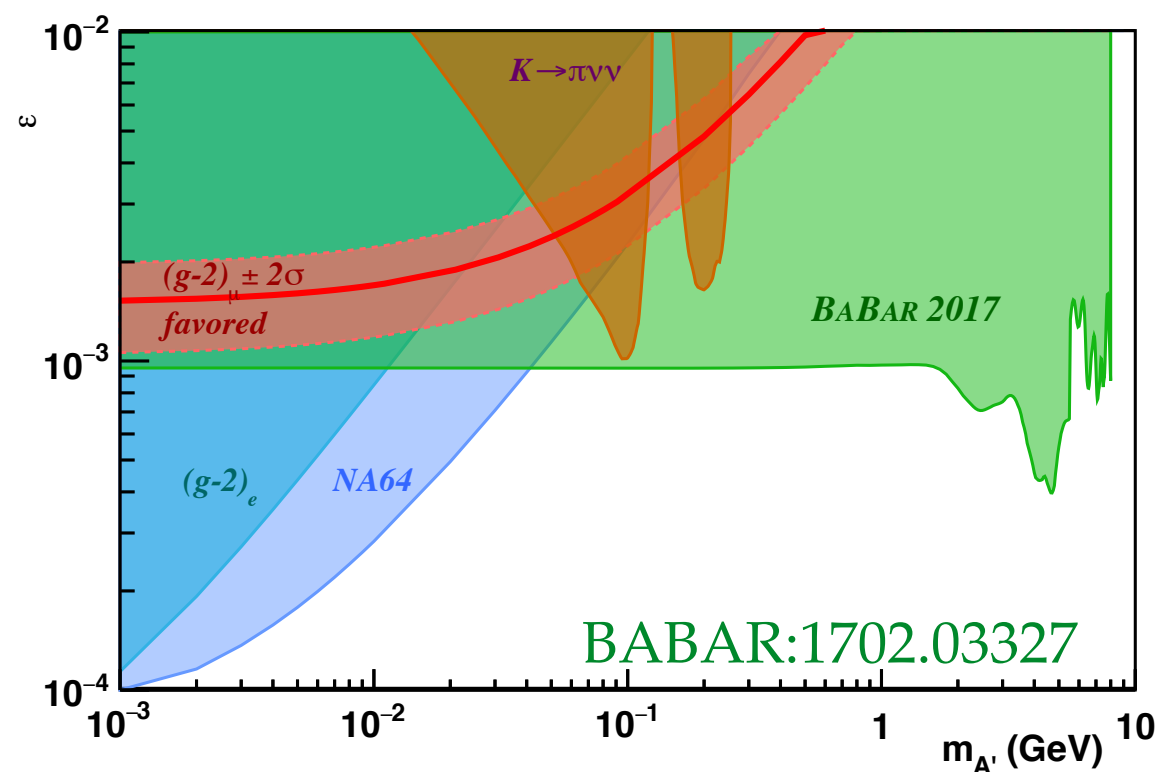
- 1) Mix  $S/V$  with neutral SM bosons
- 2) Couple  $S/V$  to heavy states that mix with the muon
- 3)  $V$  is the gauge boson of a new  $U(1)$  SM extension

# Options For Singlets

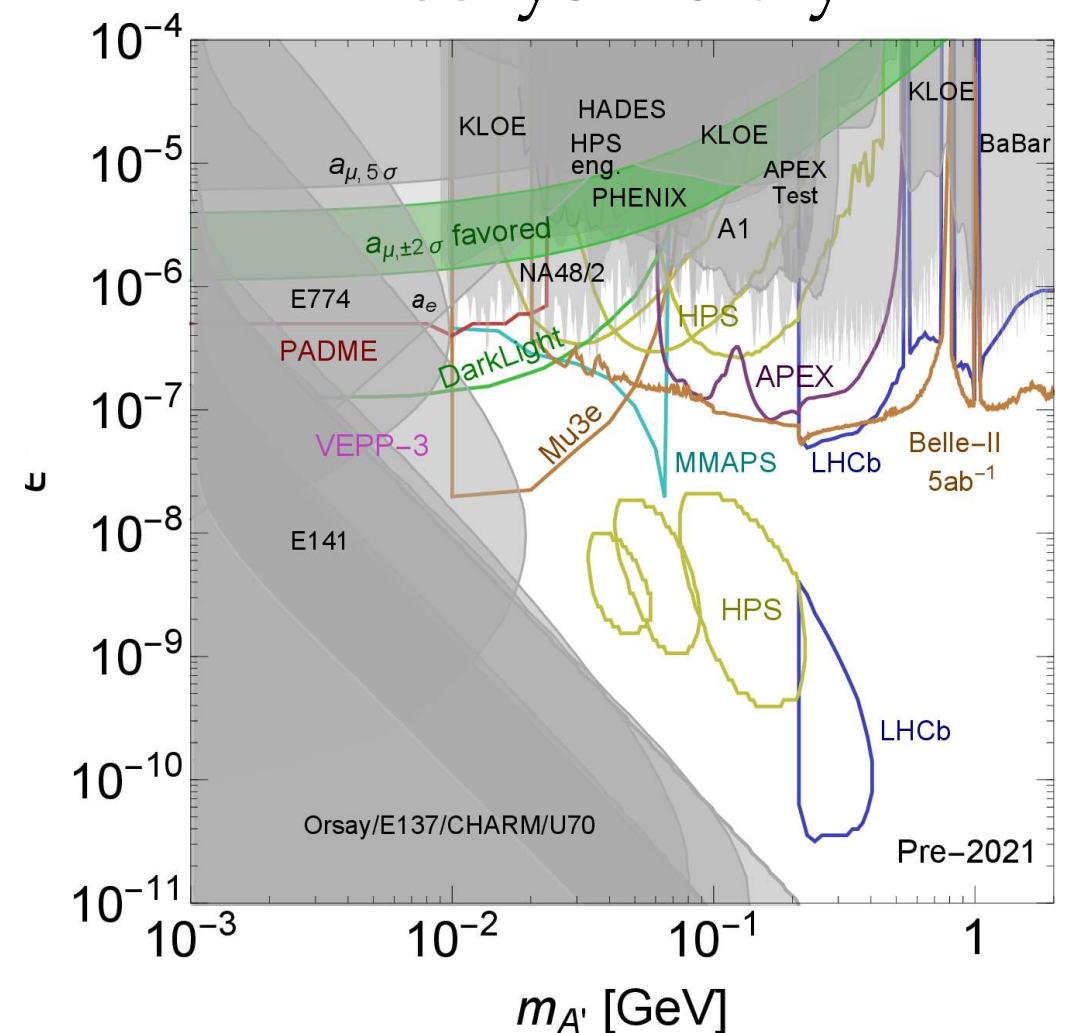
## 1) Mix S/V with neutral SM bosons

Kinetically mixed dark photon  $A'$  ruled out  $\mathcal{L}_{\text{int}} = \epsilon e A'_\mu J_{\text{EM}}^\mu$

### Decays invisibly



### Decays visibly



See Mohlabeng for semi-visible decays 1809.07768

1707.04591

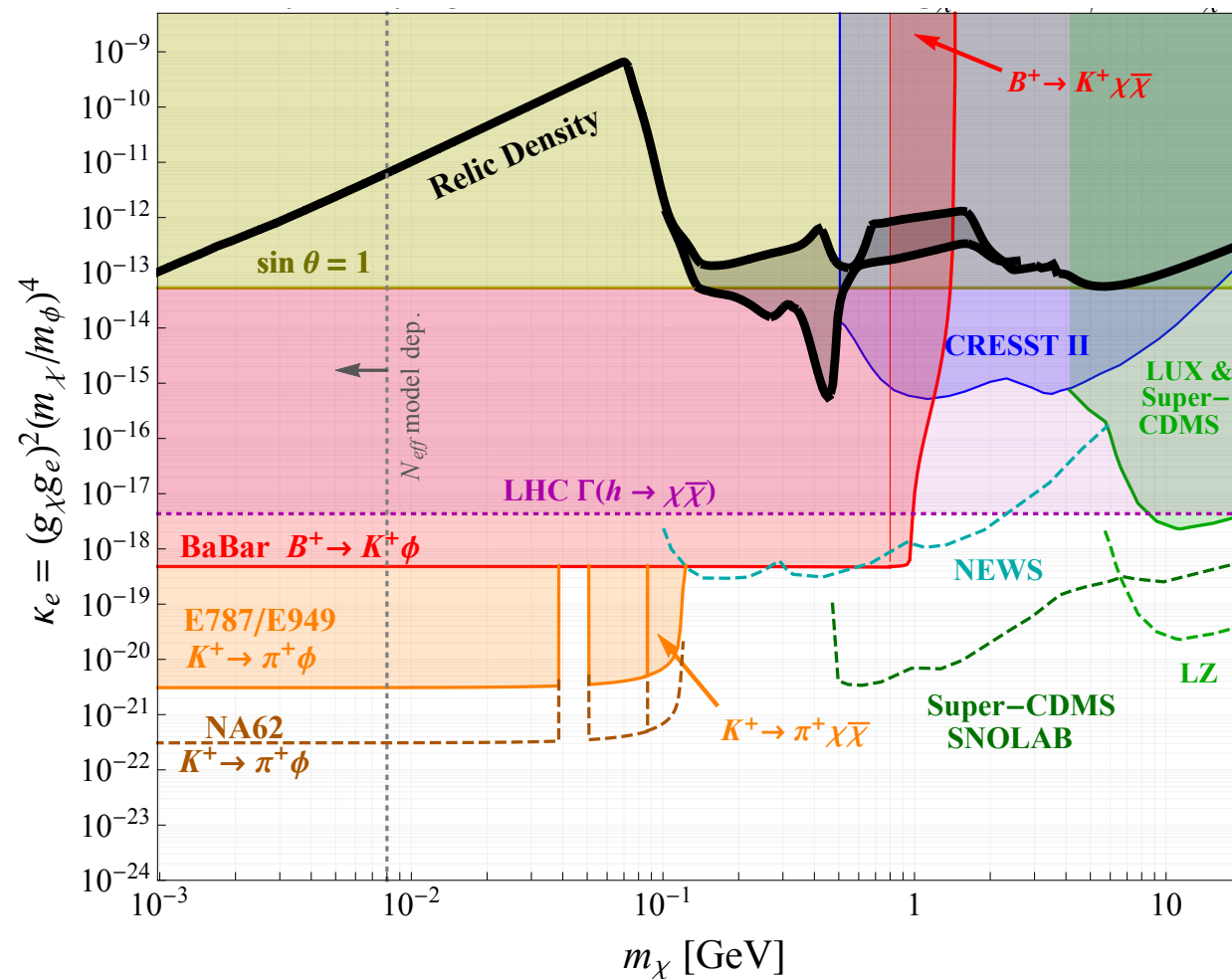
# Options For Singlets

## 1) Mix S/V with neutral SM bosons

Higgs mixed scalar  $\phi$  ruled out

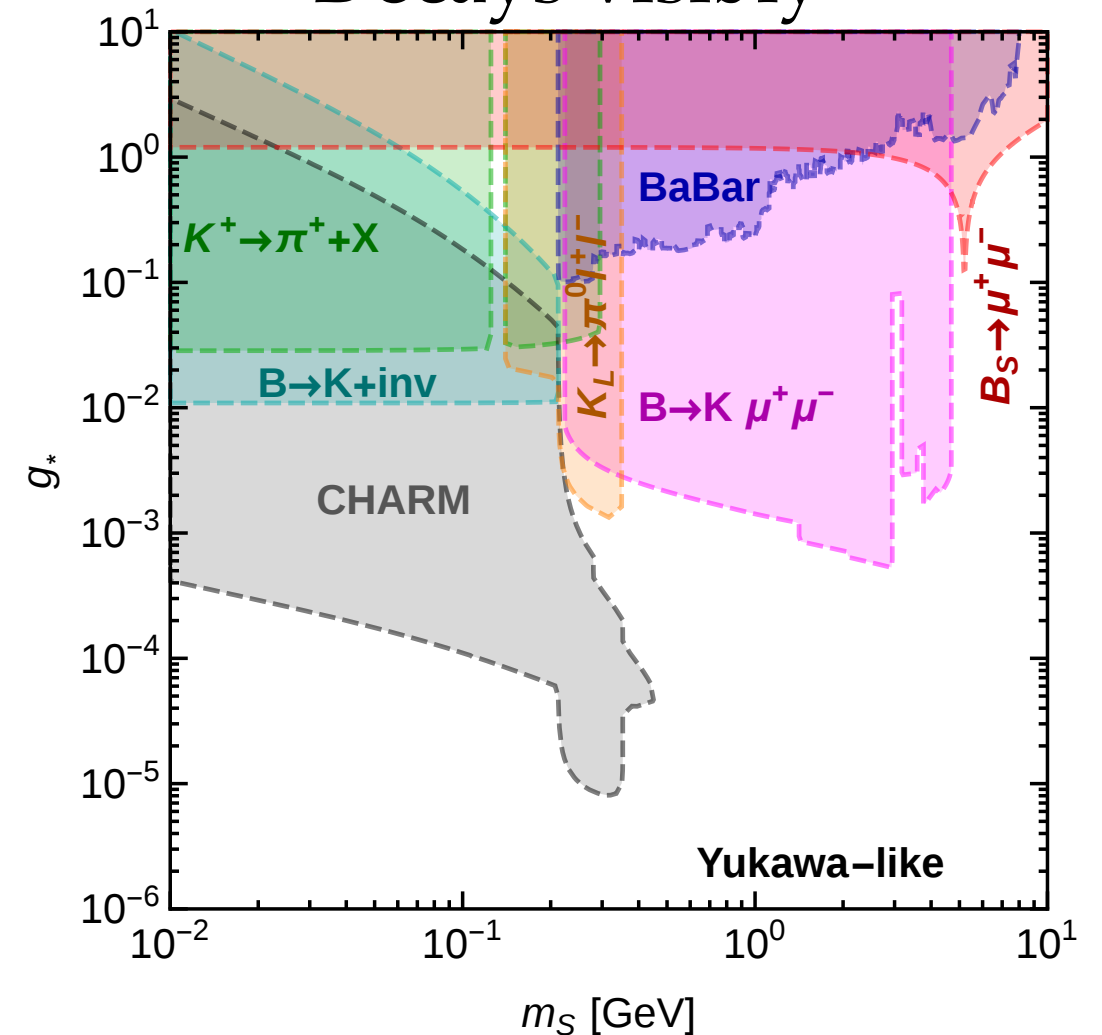
$$\mathcal{L}_{\text{int}} = \sin \theta \phi \frac{m_f}{v} \bar{f} f$$

### Decays invisibly



GK 1512.04119

### Decays visibly



SHiP collab 1504.04855

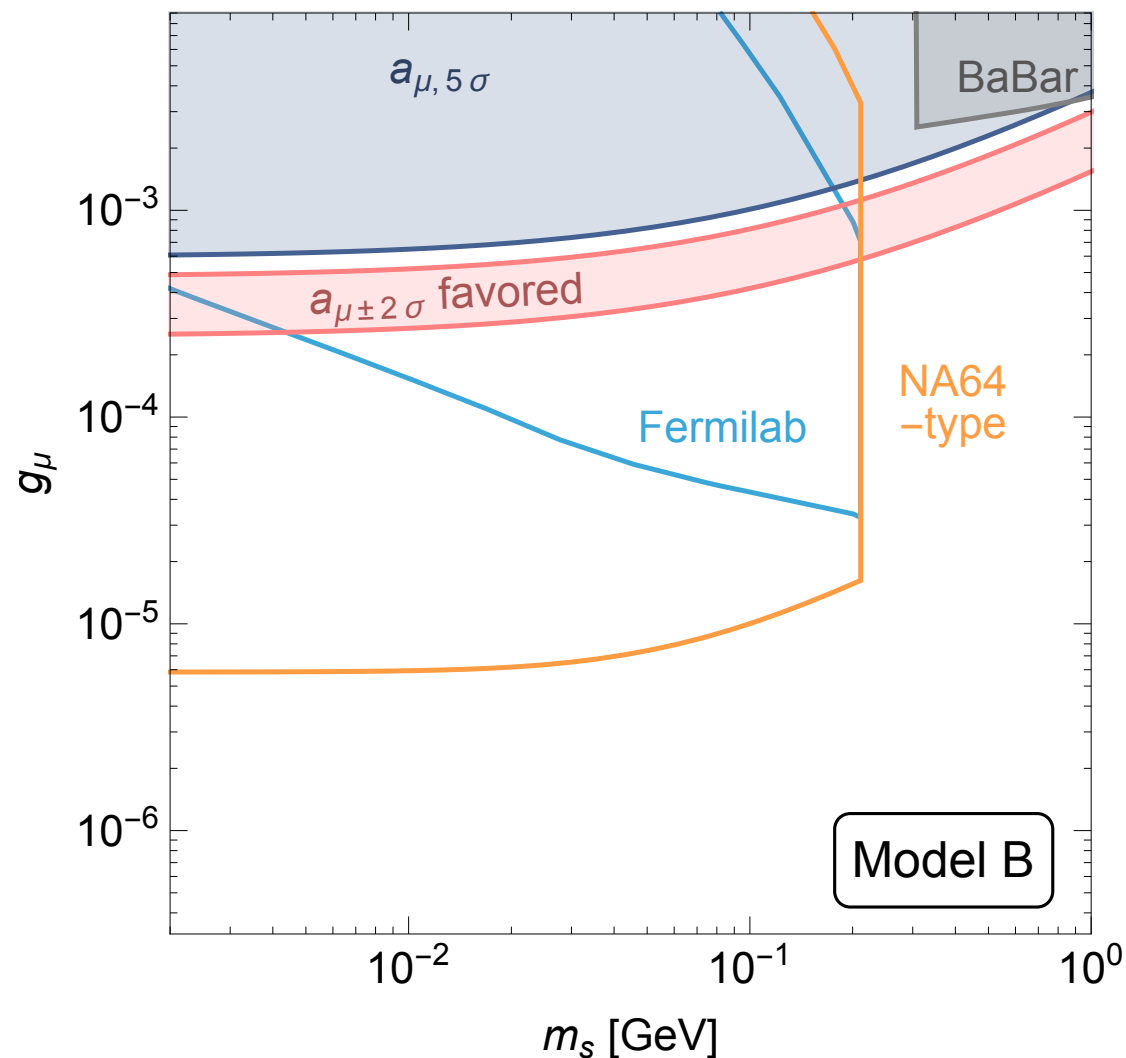


# Options For Singlets

## 2) Couple S to heavy states that mix with the muon

$$\mathcal{L} \supset -\frac{1}{2}m_S^2 - \left( y_\mu H^\dagger L\mu^c + \frac{c_s}{M} S H^\dagger L\mu^c \right) \rightarrow \mathcal{L}_{\text{eff}} = g_\mu S \mu\mu^c$$

$S \rightarrow \gamma\gamma$  via muon loop

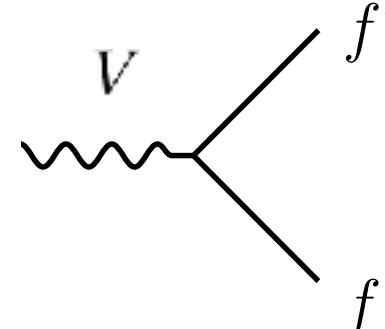


Muon only coupling  
Decays through loop  
... or decays invisibly

# Options For Singlets

3)  $V$  is the gauge boson of a new  $U(1)$  SM extension

SM particles now carry a new gauge quantum number

$$\mathcal{L} \supset g V_\mu J_{\text{SM}}^\mu, \quad J_{\text{SM}}^\mu \equiv \sum_f Q_f \bar{f} \gamma^\mu f$$


Only anomaly free possibilities:

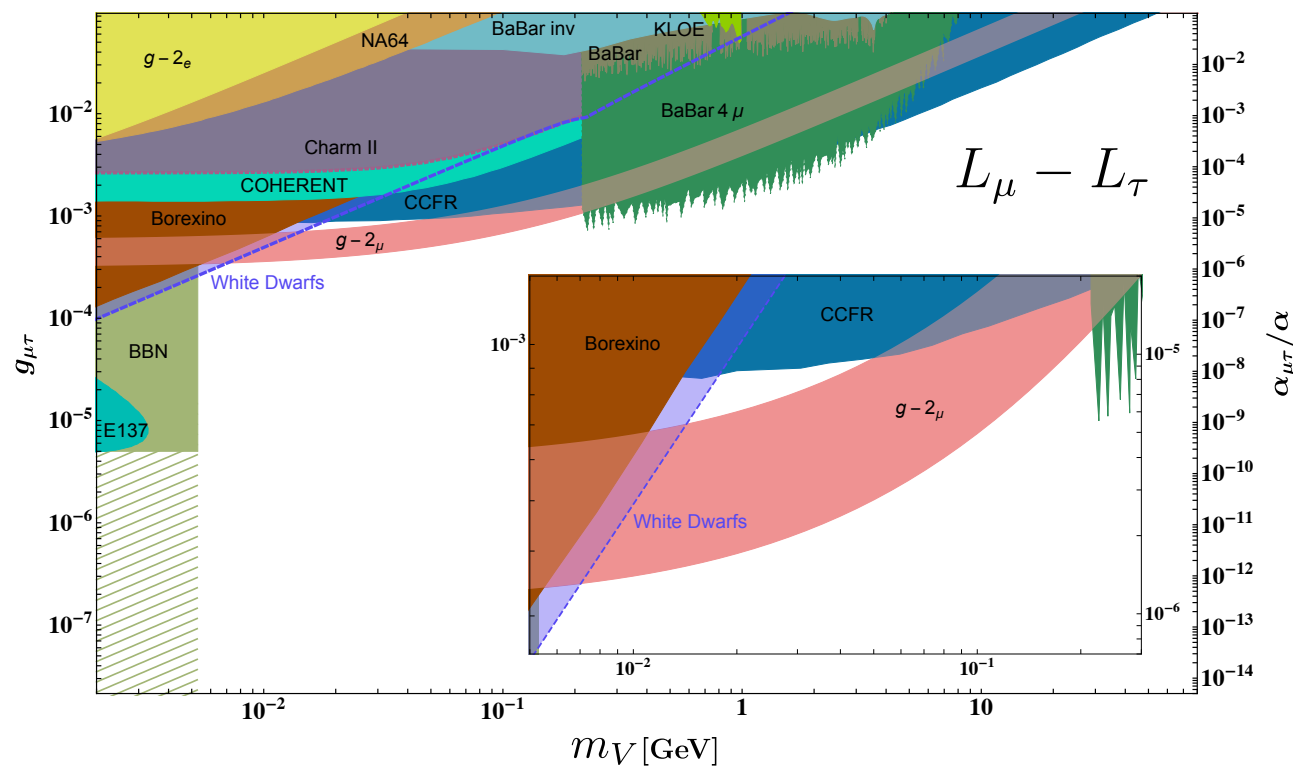
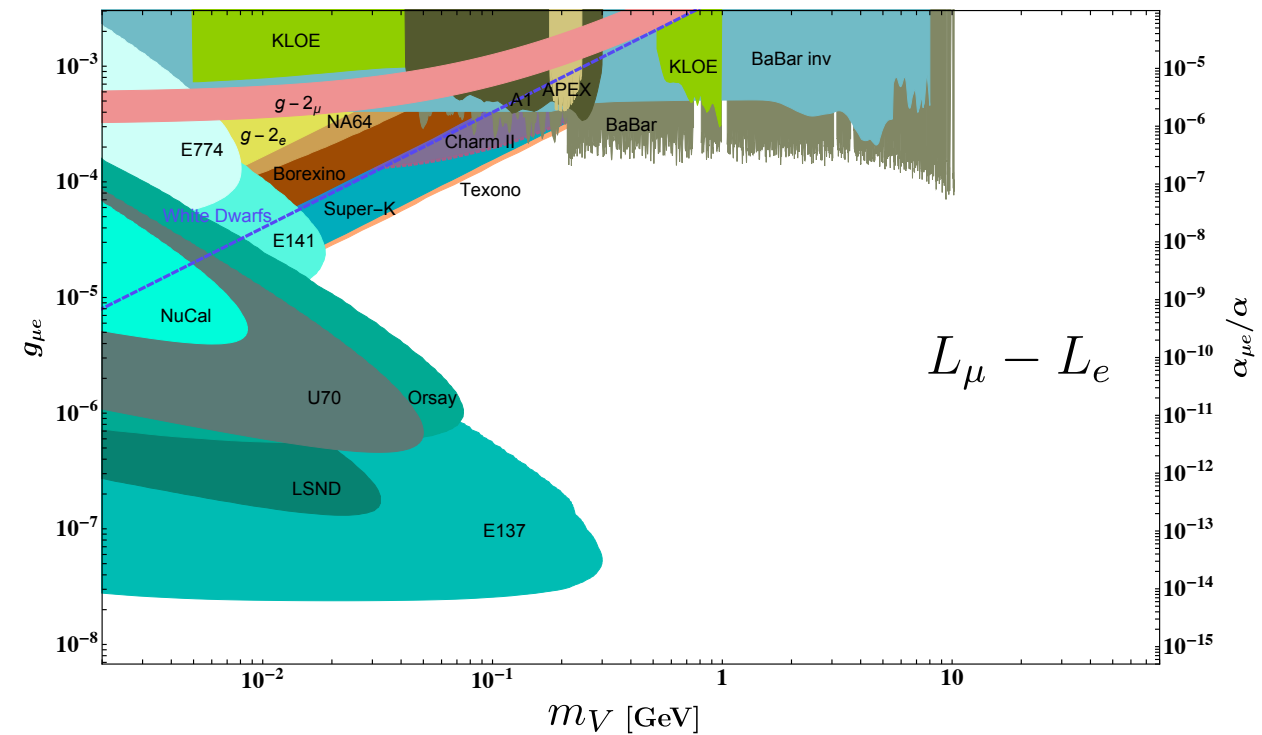
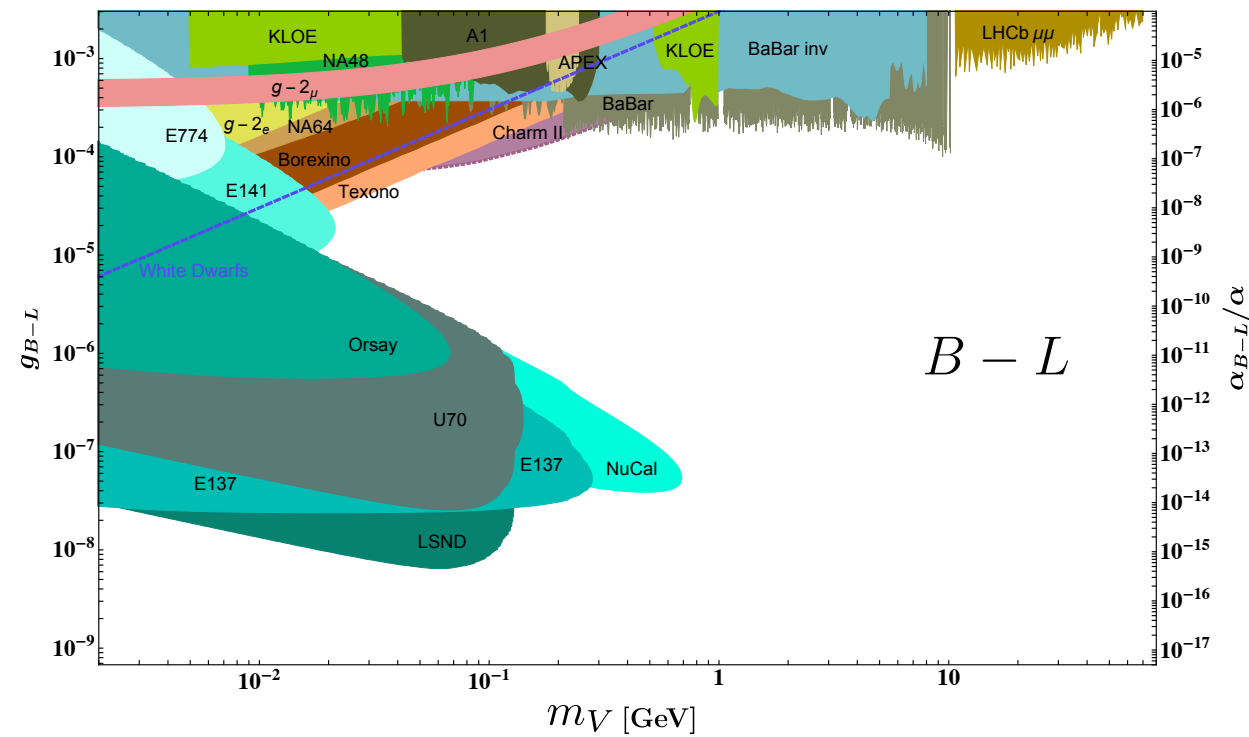
$$U(1)_{B-L}, \quad U(1)_{L_i-L_j}, \quad U(1)_{B-3L_i}$$

All similar, but some differences in bounds

Two parameter family of models:  $\{g, m_V\}$

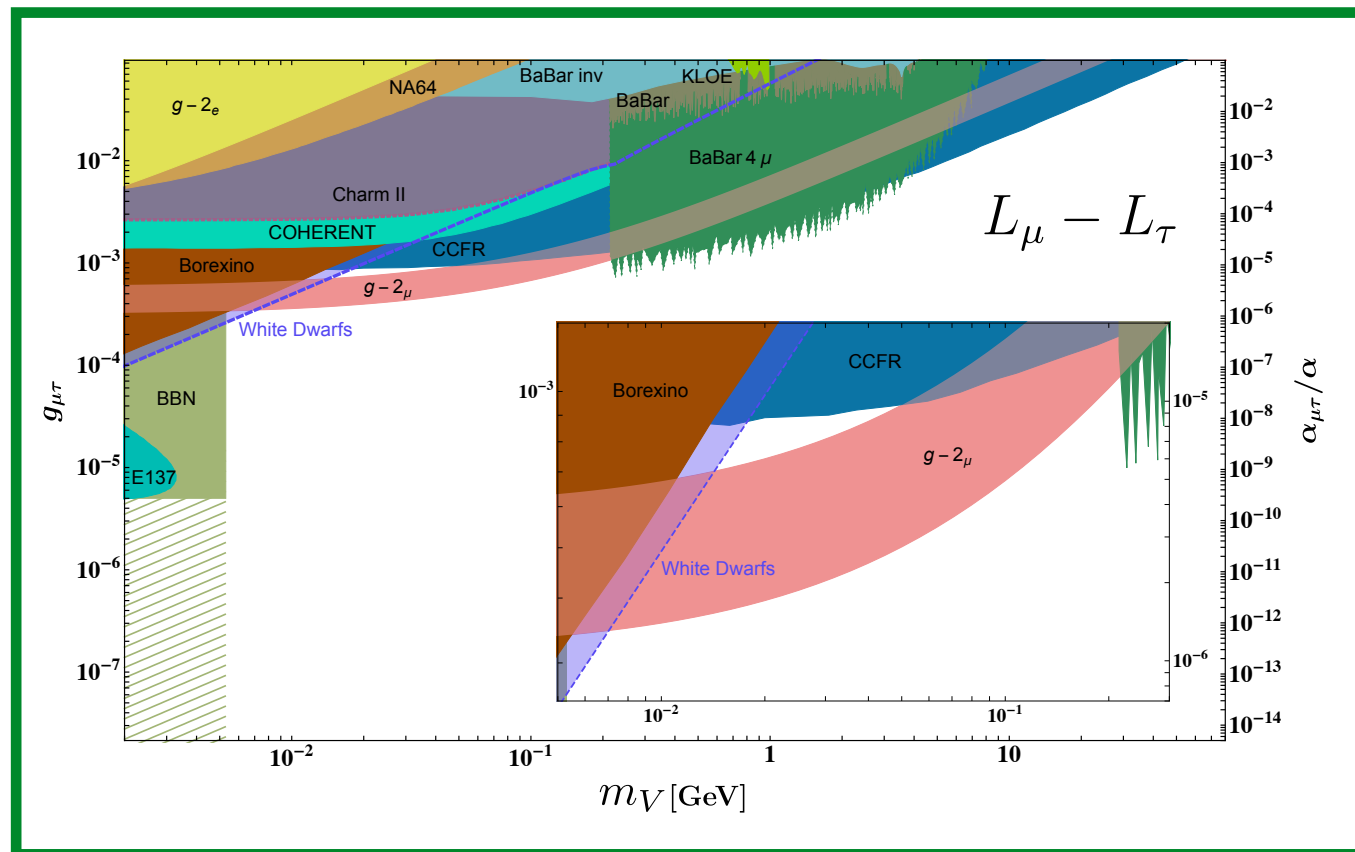
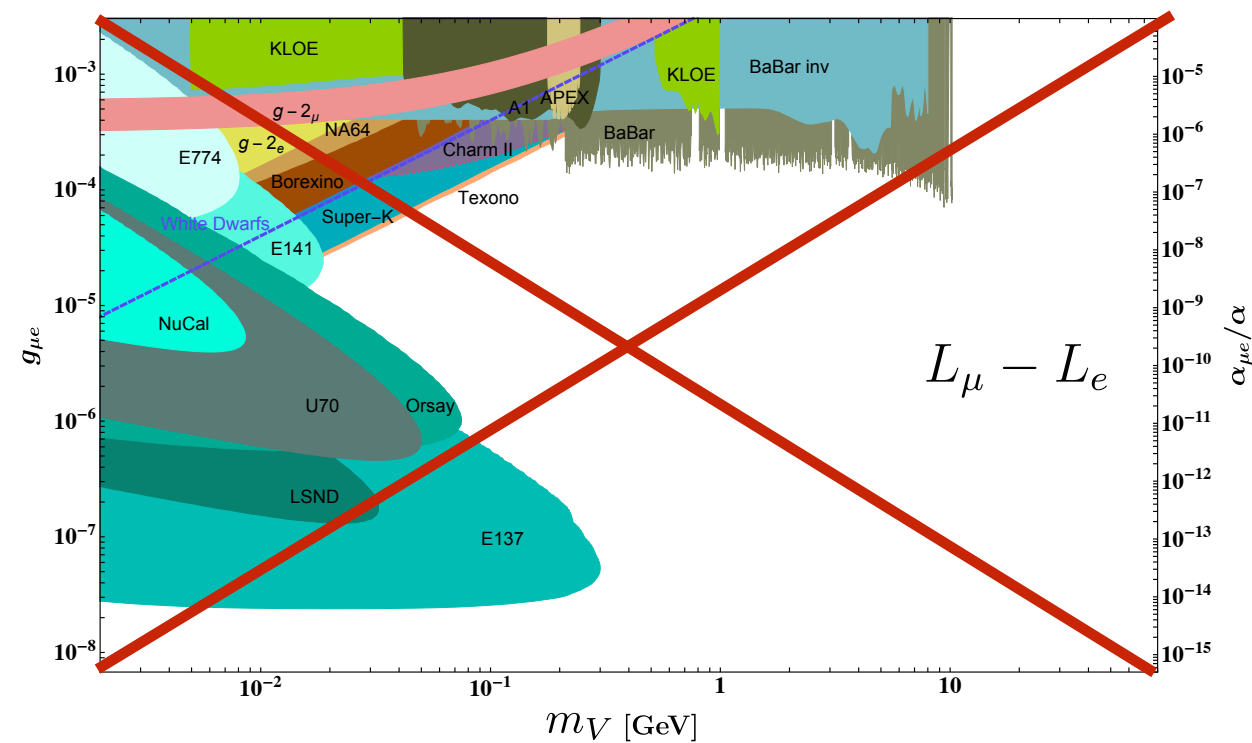
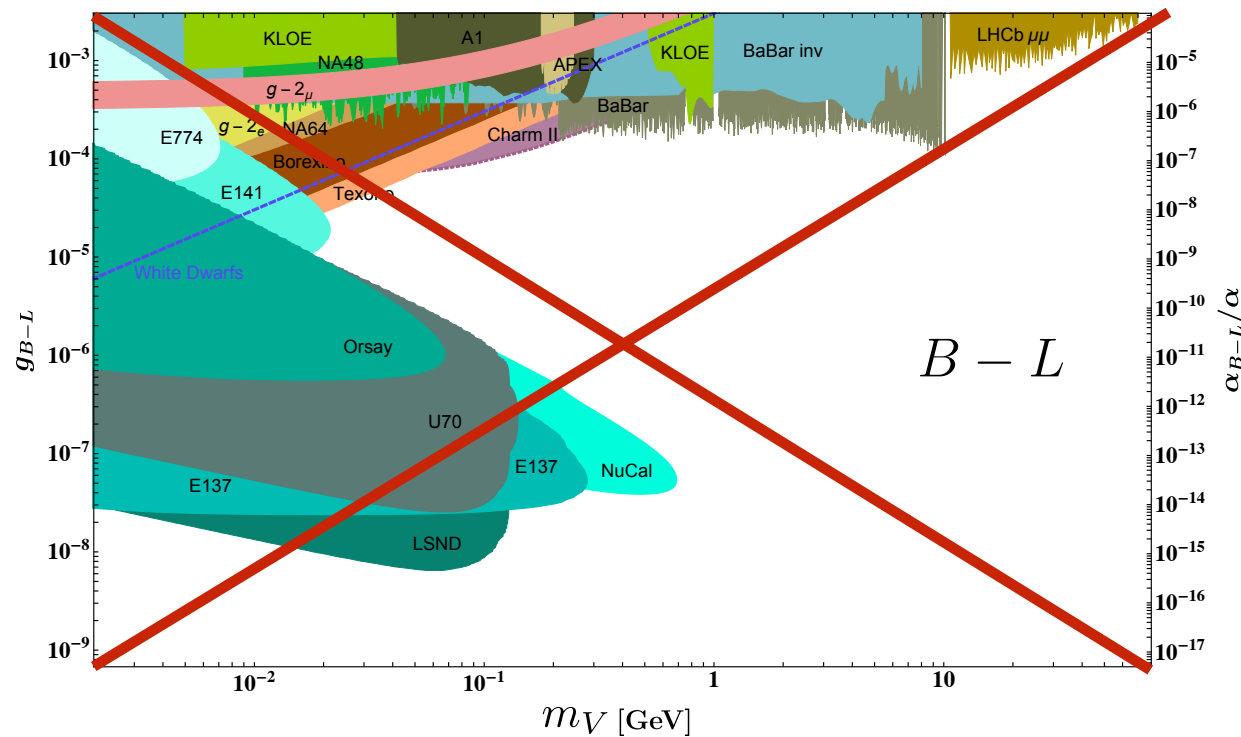
# Options For Singlets

3)  $V$  is the gauge boson of a new  $U(1)$  SM extension



# Options For Singlets

3)  $V$  is the gauge boson of a new  $U(1)$



Only one possibility left  
Viable between  $\text{MeV} - 2m_\mu$

$< \text{MeV}$  spoils BBN  
 $> 2m_\mu$  decays to muons

# Summary of Singlet Models

Experimental bounds require muon-philic forces

## Scalar model

$$\mathcal{L} \supset \frac{1}{2}(\partial_\mu S)^2 - \frac{1}{2}m_S^2 S^2 - \sum_{\ell=e,\mu,\tau} g_\ell S \bar{\ell} \ell,$$

Generically need  $g_{e,q} \ll g_\mu$

Need extra SM charged fields in UV

Model dependent decays — **invisible = safest**

## Vector model

$$U(1)_{\mu-\tau}$$

$$\mathcal{L} \supset \frac{m_V^2}{2} V_\alpha V^\alpha + g_V V_\alpha J_{\mu-\tau}^\alpha$$

$$J_{\mu-\tau}^\alpha \equiv \bar{\mu} \gamma^\alpha \mu + \bar{\nu}_\mu \gamma^\alpha P_L \nu_\mu - (\mu \rightarrow \tau)$$

For viable mass range  $< 200$  MeV, V always\* decays invisibly

# Overview

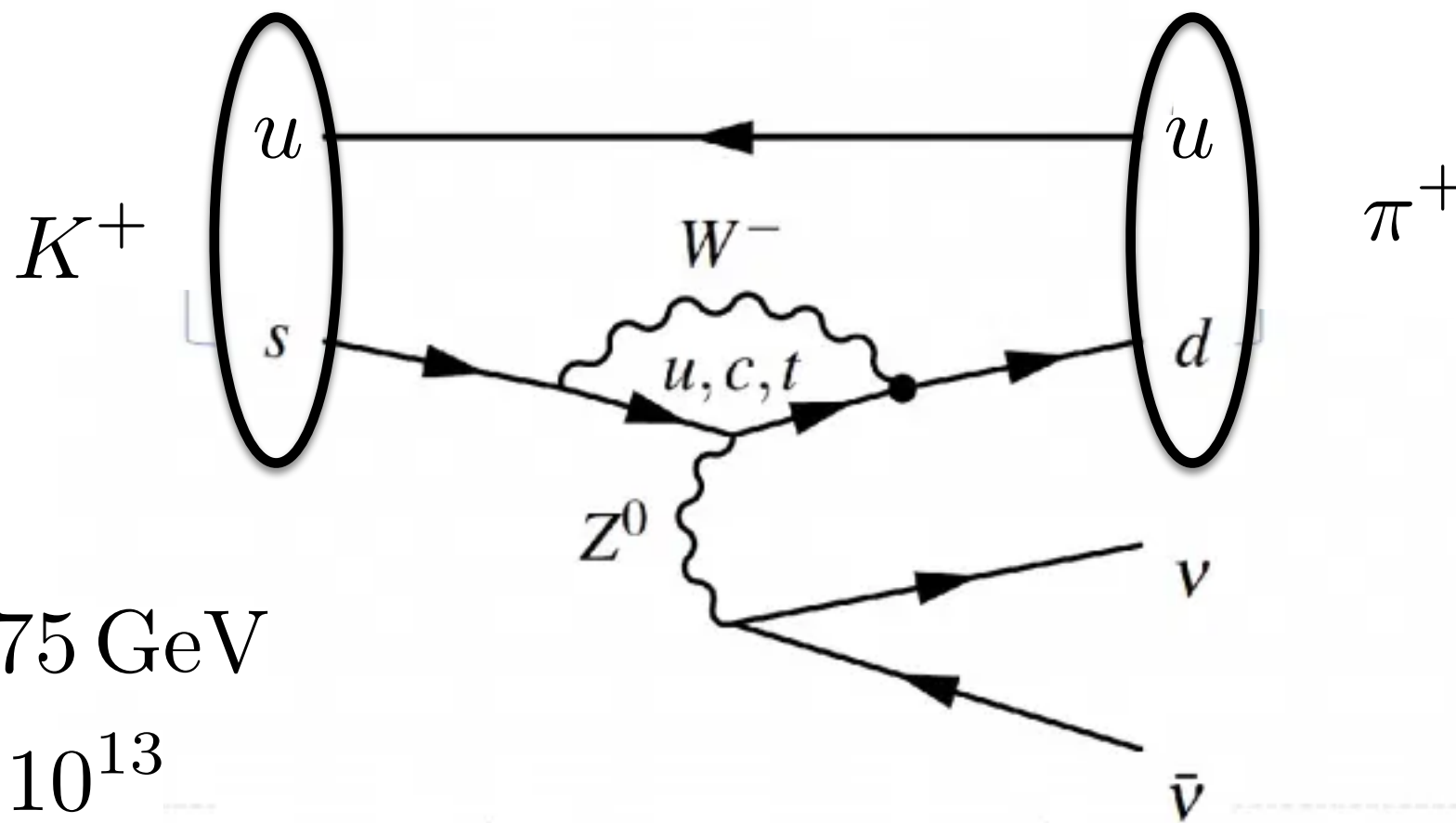
Current Status of  $g-2$

*Discovering Singlet Models*  
NA62 Experiment

Electroweak Models

# NA62 Physics Goals

Designed to measure rare SM kaon decays



$$E_{K^+} \approx 75 \text{ GeV}$$

$$N_{K^+} \sim 10^{13}$$

$$m_{\text{miss}}^2 = (p_\nu + p_{\bar{\nu}})^2 = (p_K - p_\pi)^2$$

$$Br(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (11.0_{-3.5}^{+4.0} \text{stat.} \pm 0.3 \text{sys.}) \times 10^{-11}$$

First NA62 observation announced at ICHEP, August 2020

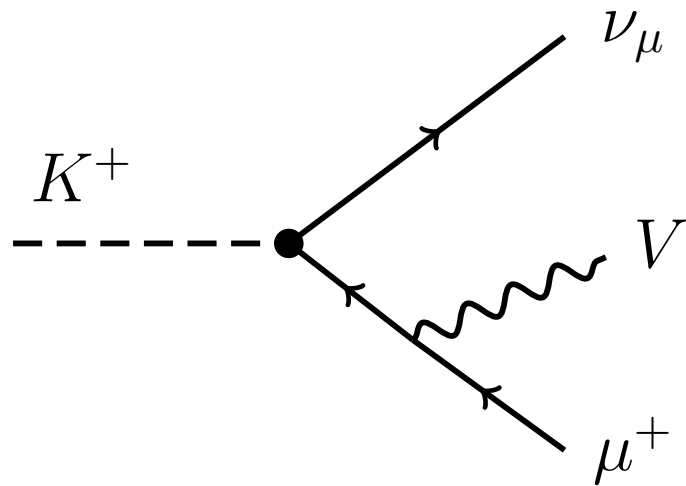
<https://indico.cern.ch/event/868940/contributions/3815641/>

# Invisible New Particles @ NA62

## Step 1: define process & observables

Dominant decay channel  $\text{BR}(K^+ \rightarrow \mu^+ \nu_\mu) = 0.64$

Our proposed strategy:  $K^+ \rightarrow \mu^+ \nu_\mu V$ , then  $V \rightarrow \nu \bar{\nu}$



Construct observable

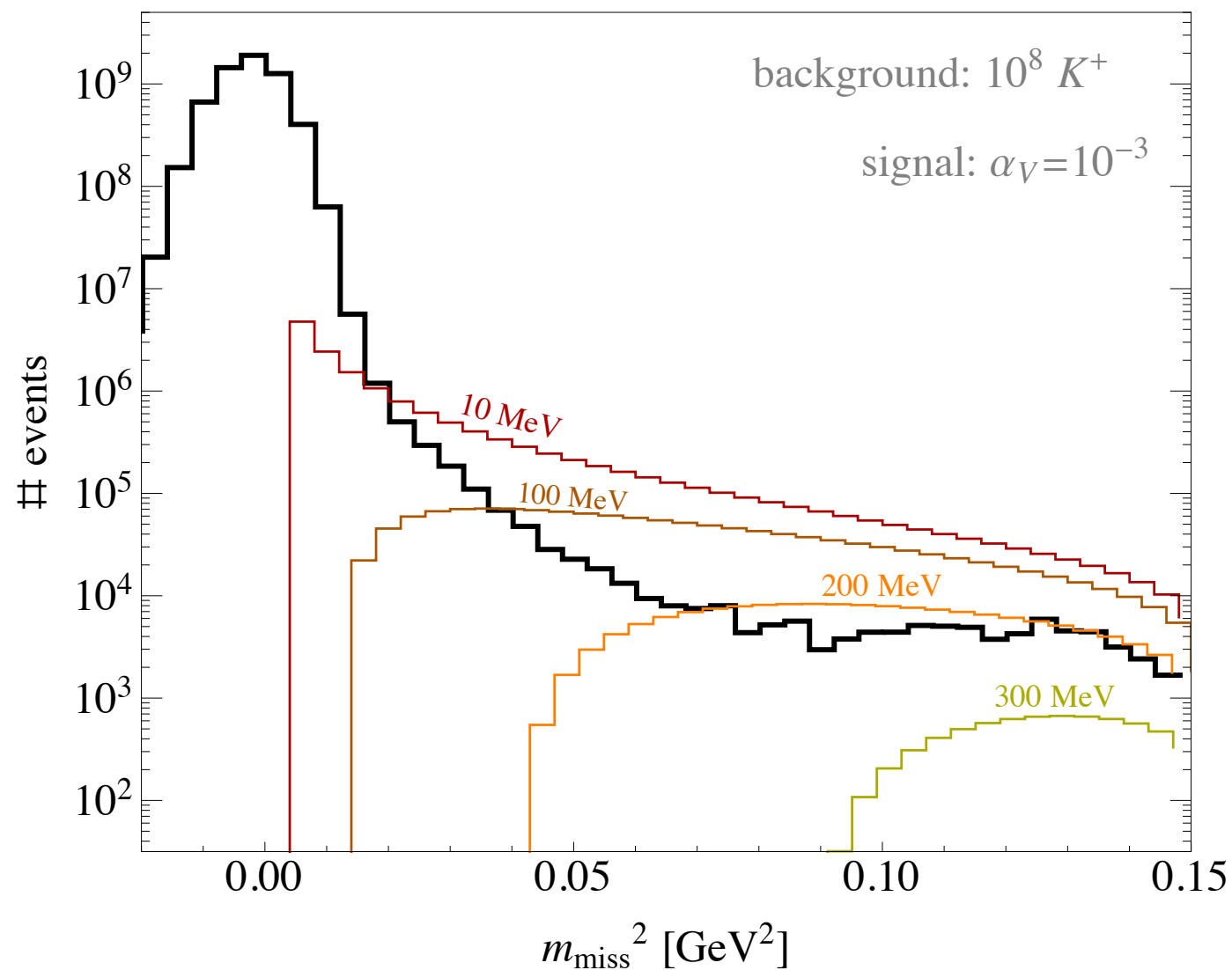
$$m_{\text{miss}}^2 = (p_{\nu_\mu} + p_V)^2 = (p_K - p_{\mu^+})^2$$

$$\frac{d\Gamma(K^+ \rightarrow \mu^+ \nu X)}{dm_{\text{miss}}^2} = \frac{1}{256\pi^3 m_K^3} \int \sum |\mathcal{M}|^2 dm_{\mu X}^2$$



# Invisible New Particles @ NA62

## Step 2: define cuts from BG distribution



Proposed analysis cut

$$m_{\text{cut}}^2 > 0.05 \text{ GeV}^2$$

Minimizes BG from

$$K^+ \rightarrow \mu^+ \nu \gamma \quad (E_\gamma < 10 \text{ MeV})$$

$$K^+ \rightarrow \mu^+ \nu \gamma \quad (E_\gamma > 10 \text{ MeV})$$

$$K^+ \rightarrow \mu^+ \nu (\gamma) \quad (\text{upstream})$$

$$K^+ \rightarrow \pi^+ \pi^+ \pi^-$$

NA62 currently keeps only  
1 / 400 single muon evts.

(bandwidth)

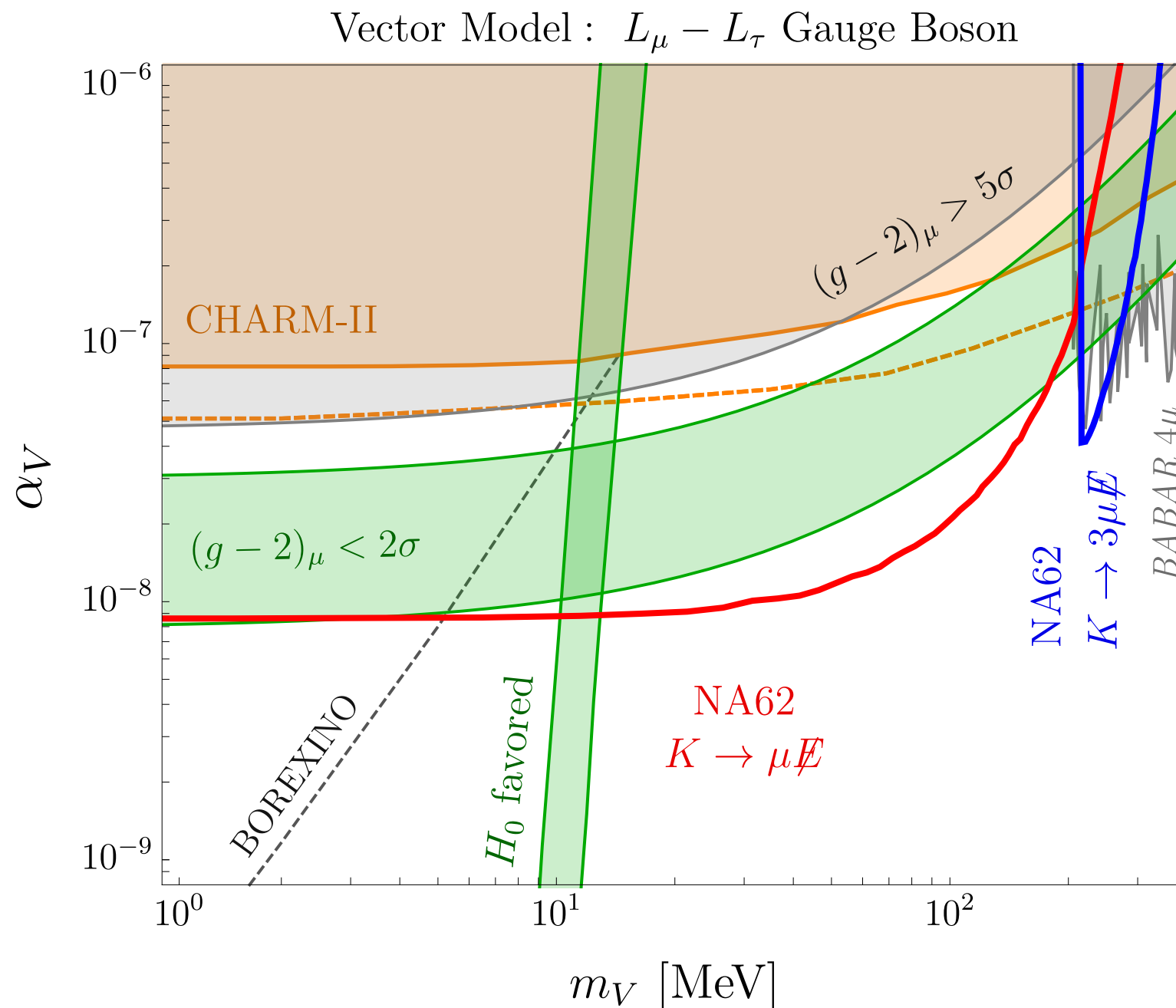
$$S = \frac{N_{K^+} \mathcal{A}}{\Gamma_{K^+}} \int_{m_{\text{cut}}^2}^{m_{\text{max}}^2} dm_{\text{miss}}^2 \frac{d\Gamma_{K^+ \rightarrow \mu^+ \nu X}}{dm_{\text{miss}}^2}$$

acceptance  $\mathcal{A} = 0.35$

BG from NA62 1712.00297

# Invisible New Particles @ NA62

## Step 3: calculate reach

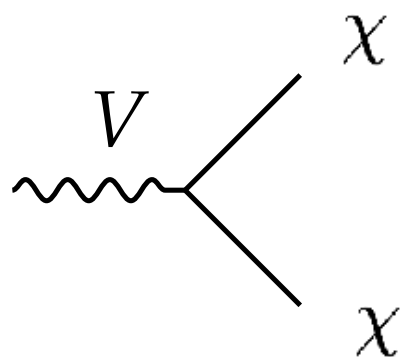


NA62 is doing this analysis now <https://na62.web.cern.ch/Documents/SPSC-SR-266.pdf>

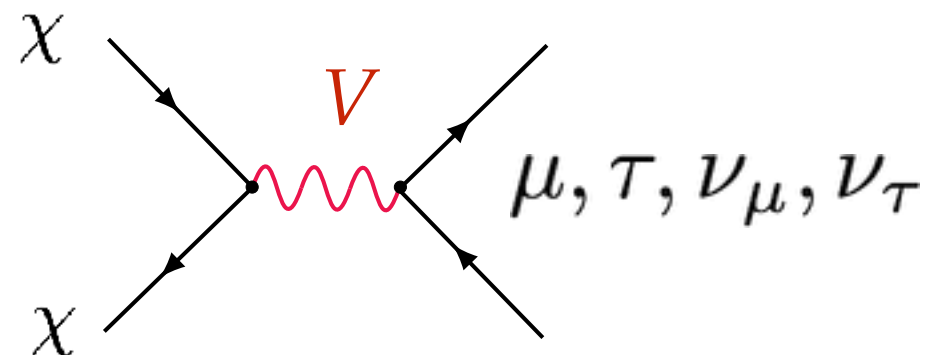
# Invisible New Particles @ NA62

Now let's couple  $V$  to dark matter  $\chi$

If  $V$  is sufficiently heavy  $m_V > 2m_\chi$



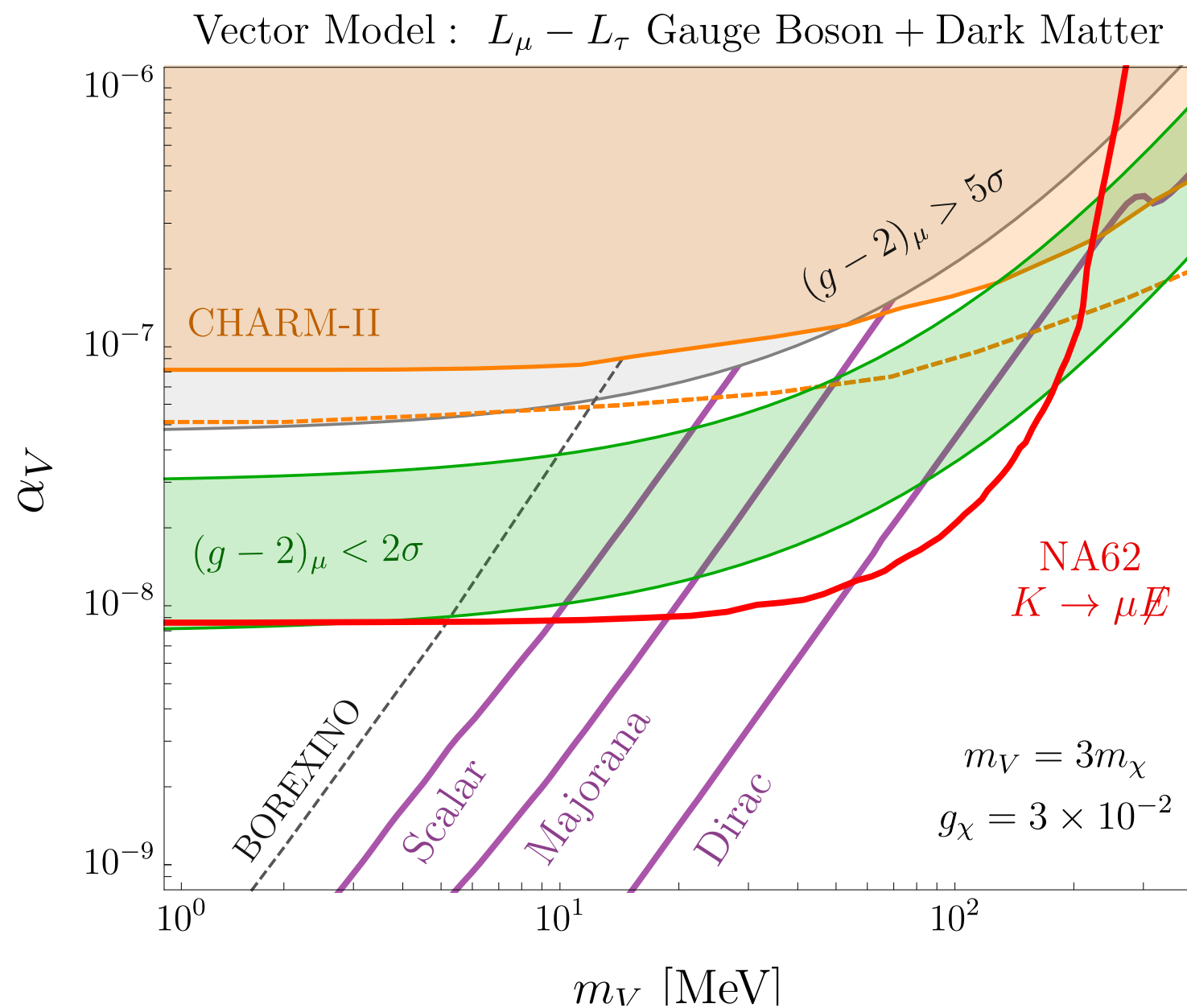
It can decay to DM  
in the laboratory



... and mediate DM freeze-out  
in the early universe

DM annihilation is s-channel and rate depends on  $V$ -SM coupling

# Invisible New Particles @ NA62

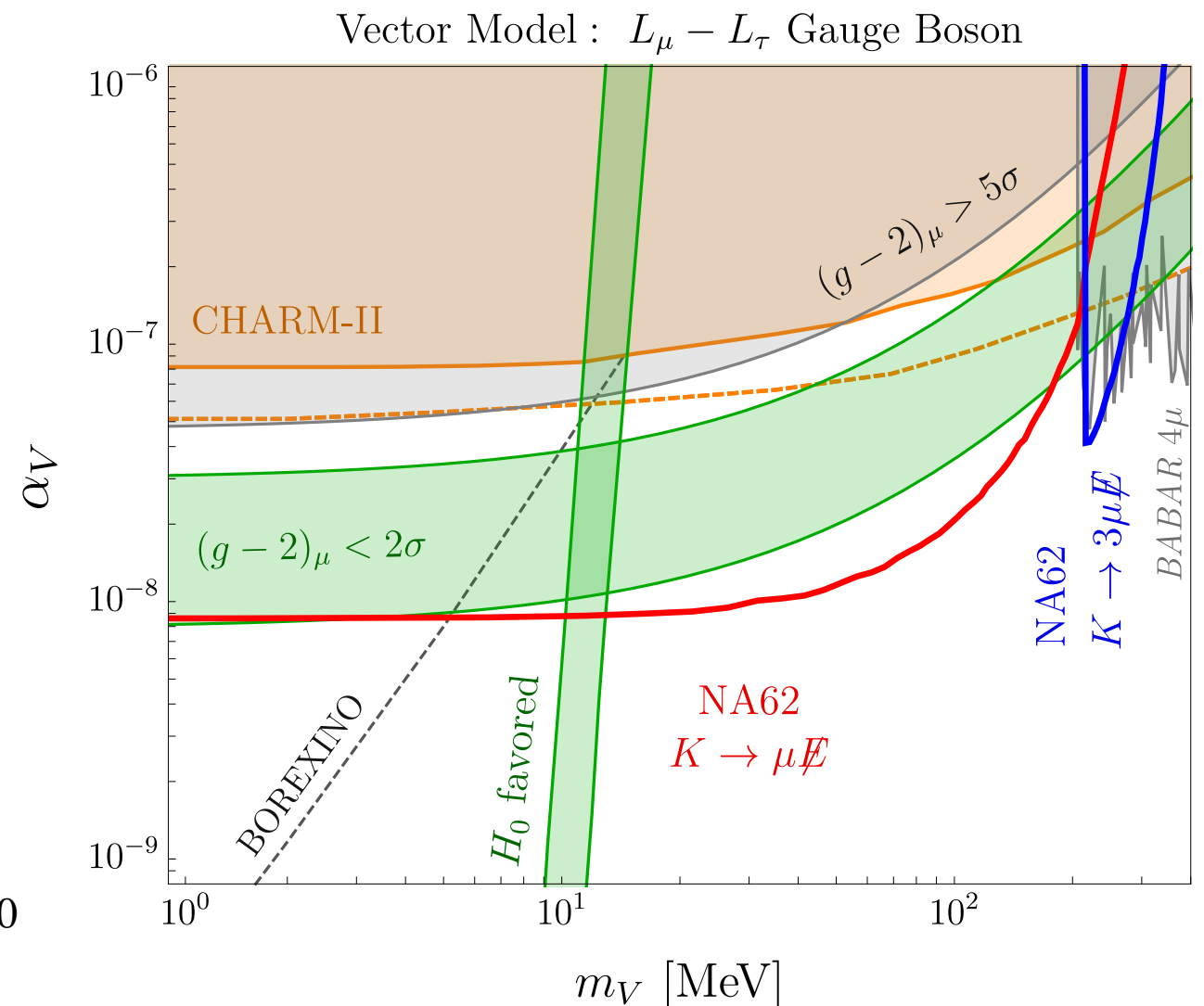
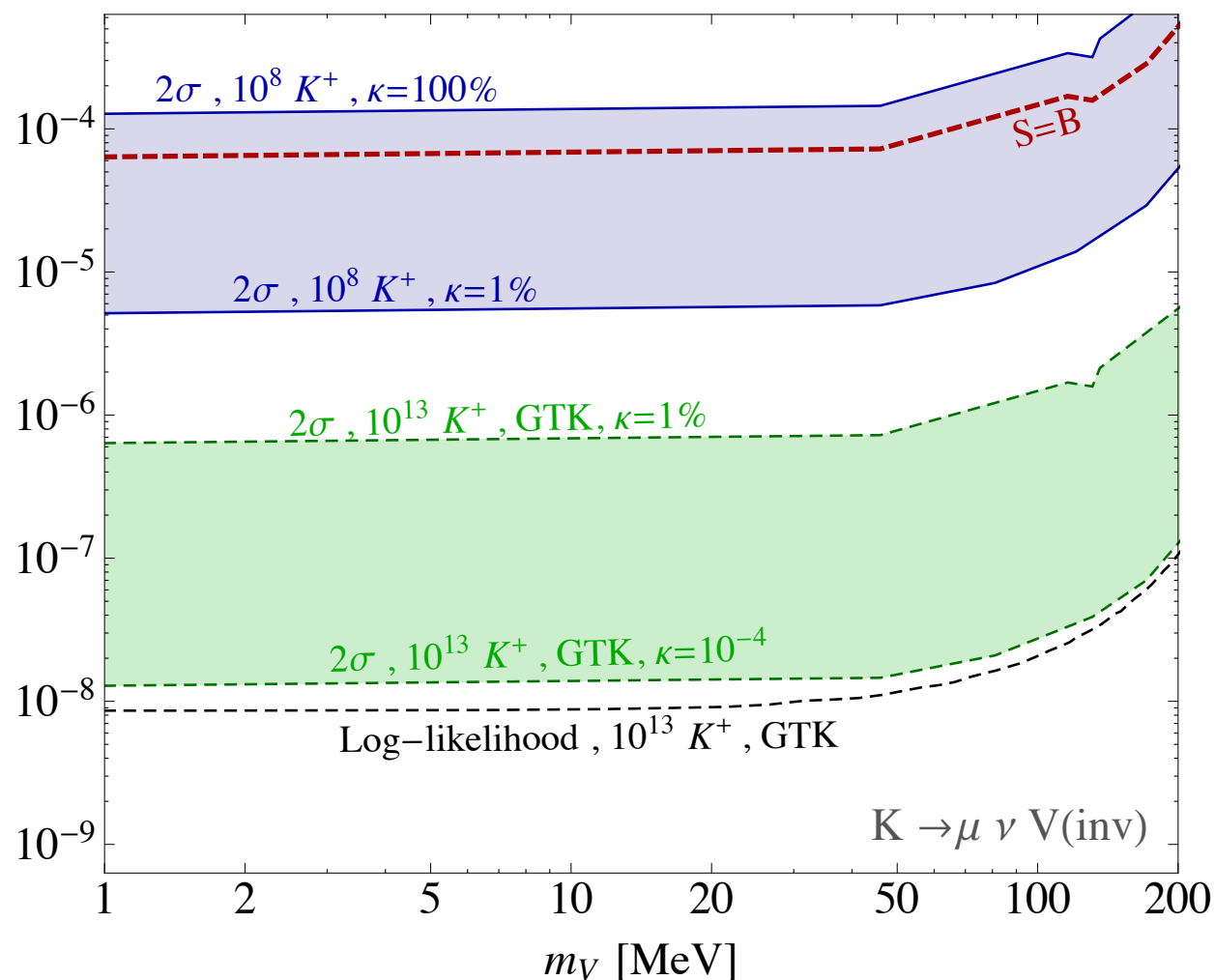


Same analysis as before

NA62 covers DM and g-2 parameter space

# Invisible New Particles @ NA62

Cautious!



Vary systematics

A lot depends on currently unknown systematics for this search  
Stay tuned... but can we do better in principle?

# Overview

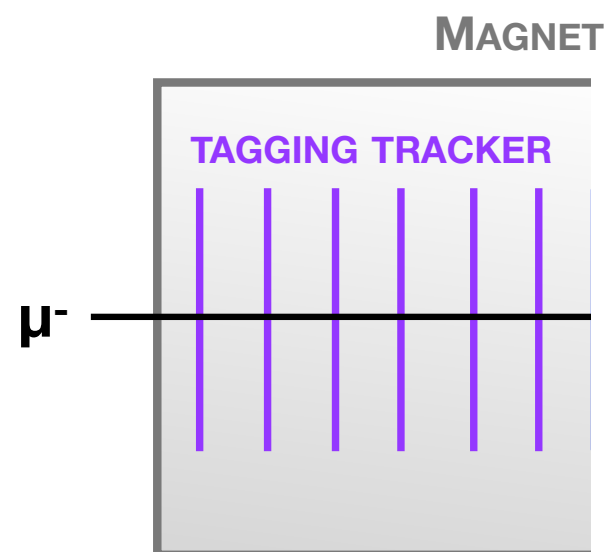
Current Status of g-2

*Discovering Singlet Models*

Muon Missing Momentum  $M^3$

Electroweak Models

# Muon Missing Momentum Concept



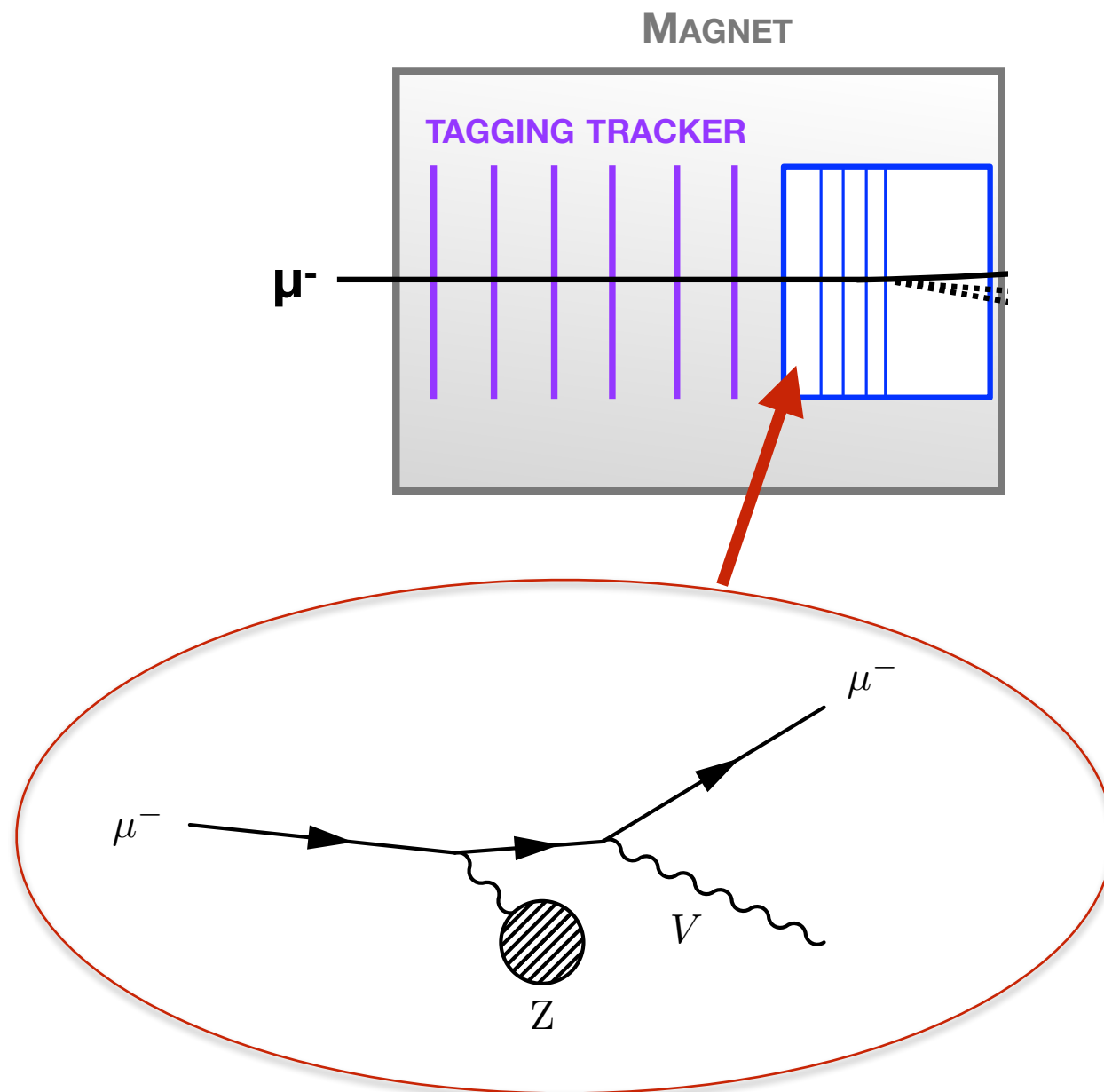
$$E_{\text{in}} \sim 15 \text{ GeV}$$

$$N_{\mu} \sim 10^{10} - 10^{13}$$

Low current beam

1) Measure  $E_{\text{in}}$  with tracker

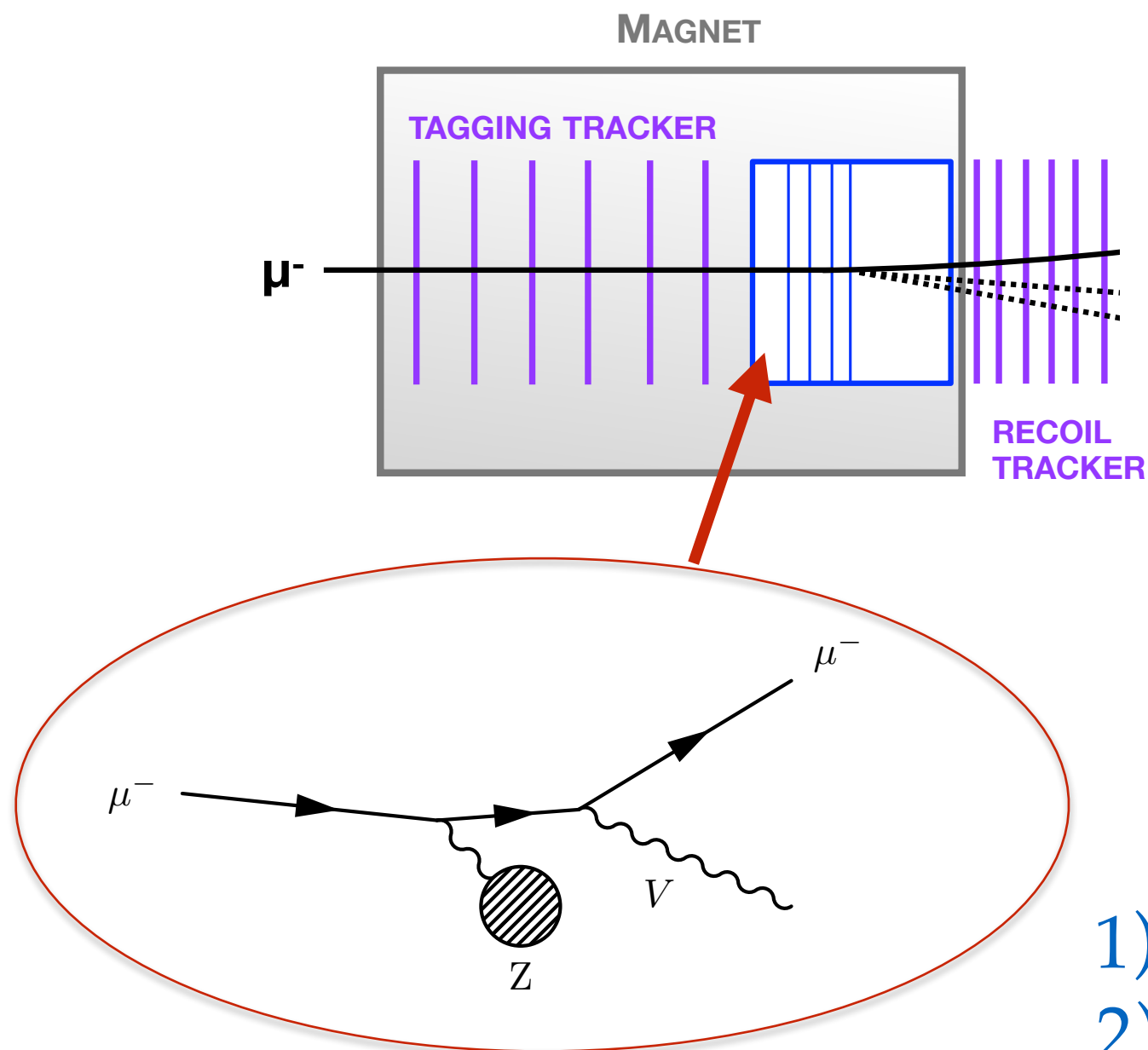
# Muon Missing Momentum Concept



- 1) Measure  $E_{in}$  with tracker
- 2) Pass beam through target

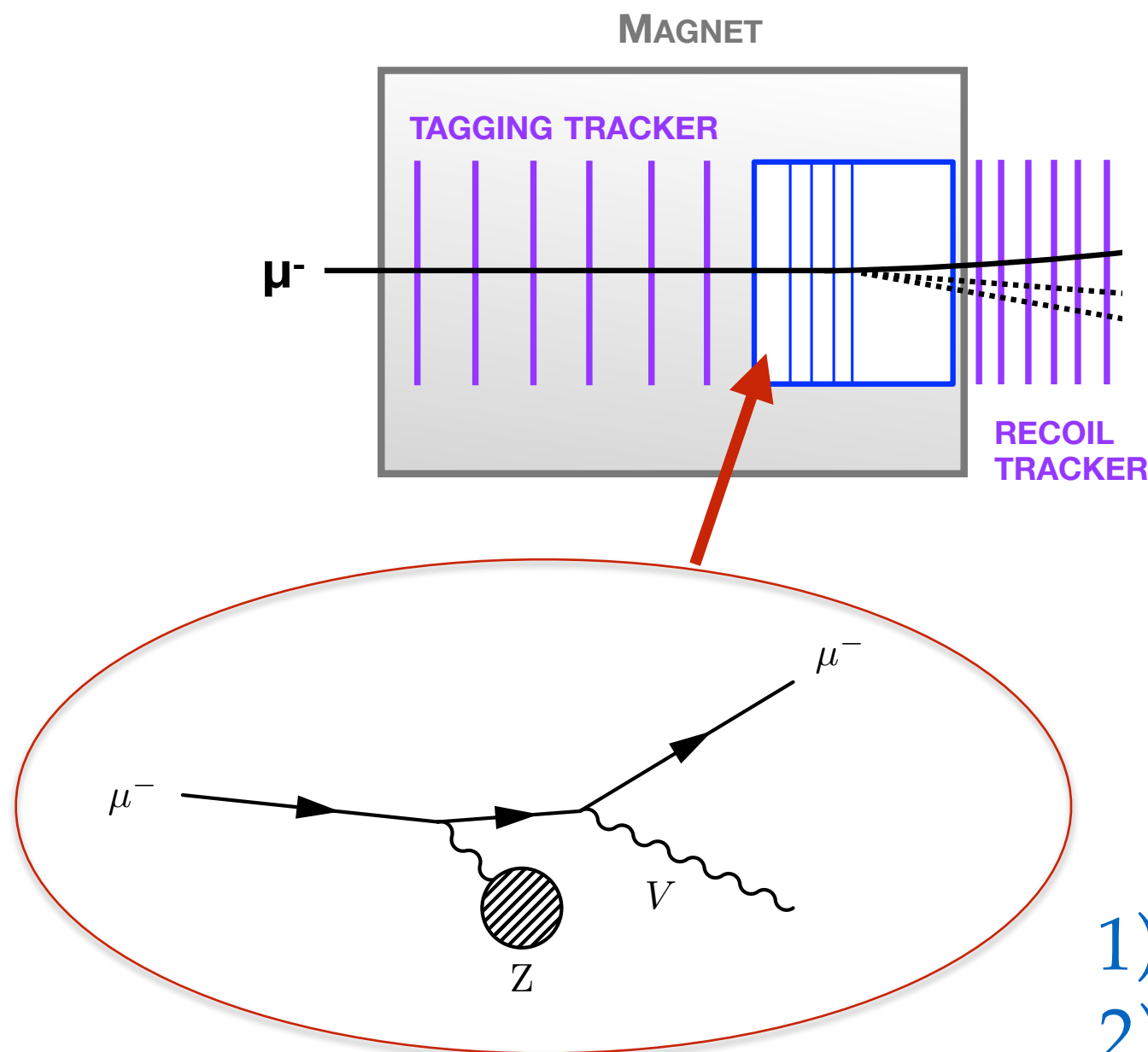


# Muon Missing Momentum Concept



- 1) Measure  $E_{in}$  with tracker
- 2) Pass beam through target
- 3) Measure  $E_{out}$  with tracker

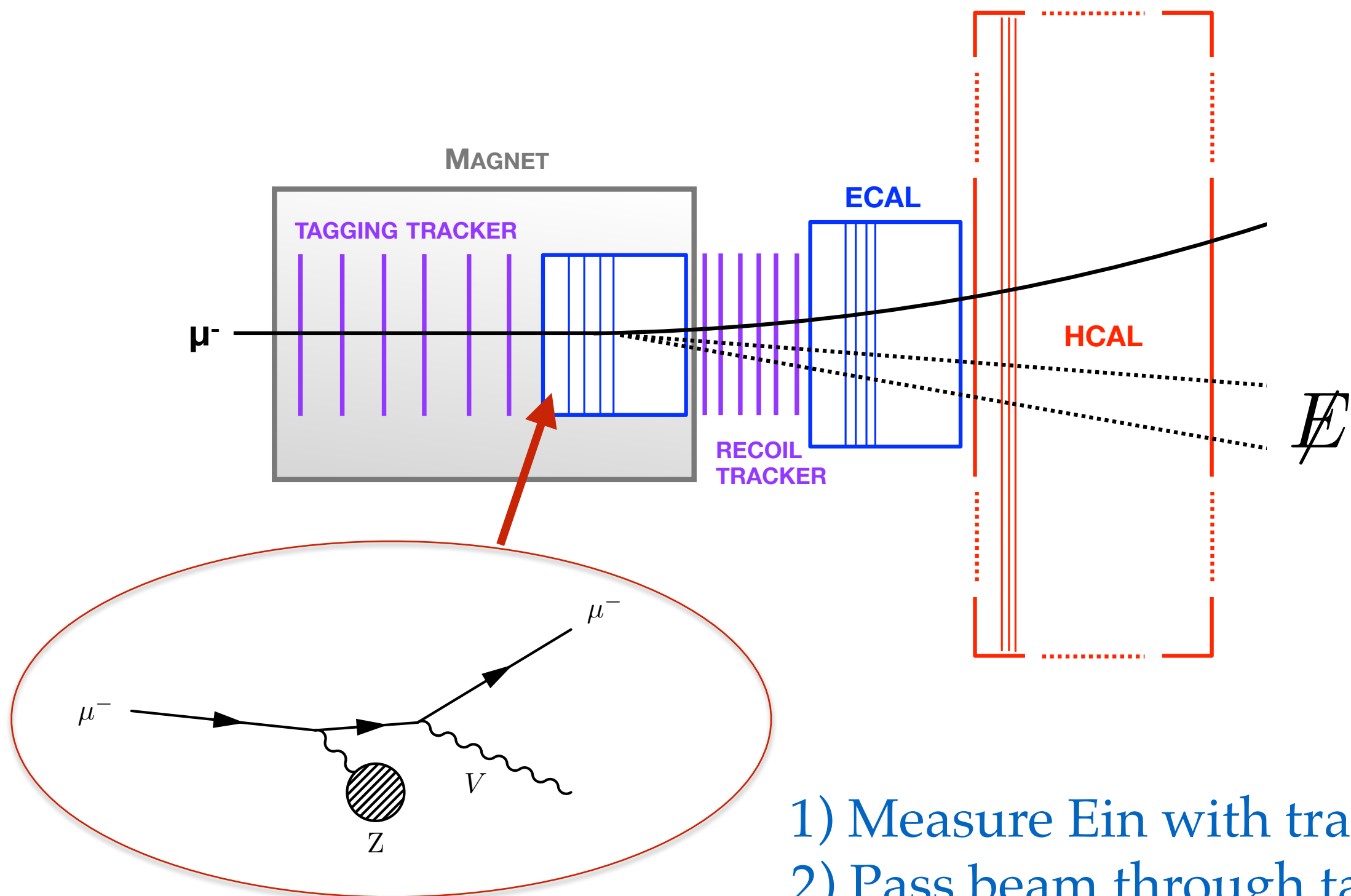
# Muon Missing Momentum Concept



Demand  $E_{\text{out}} < 9 \text{ GeV}$

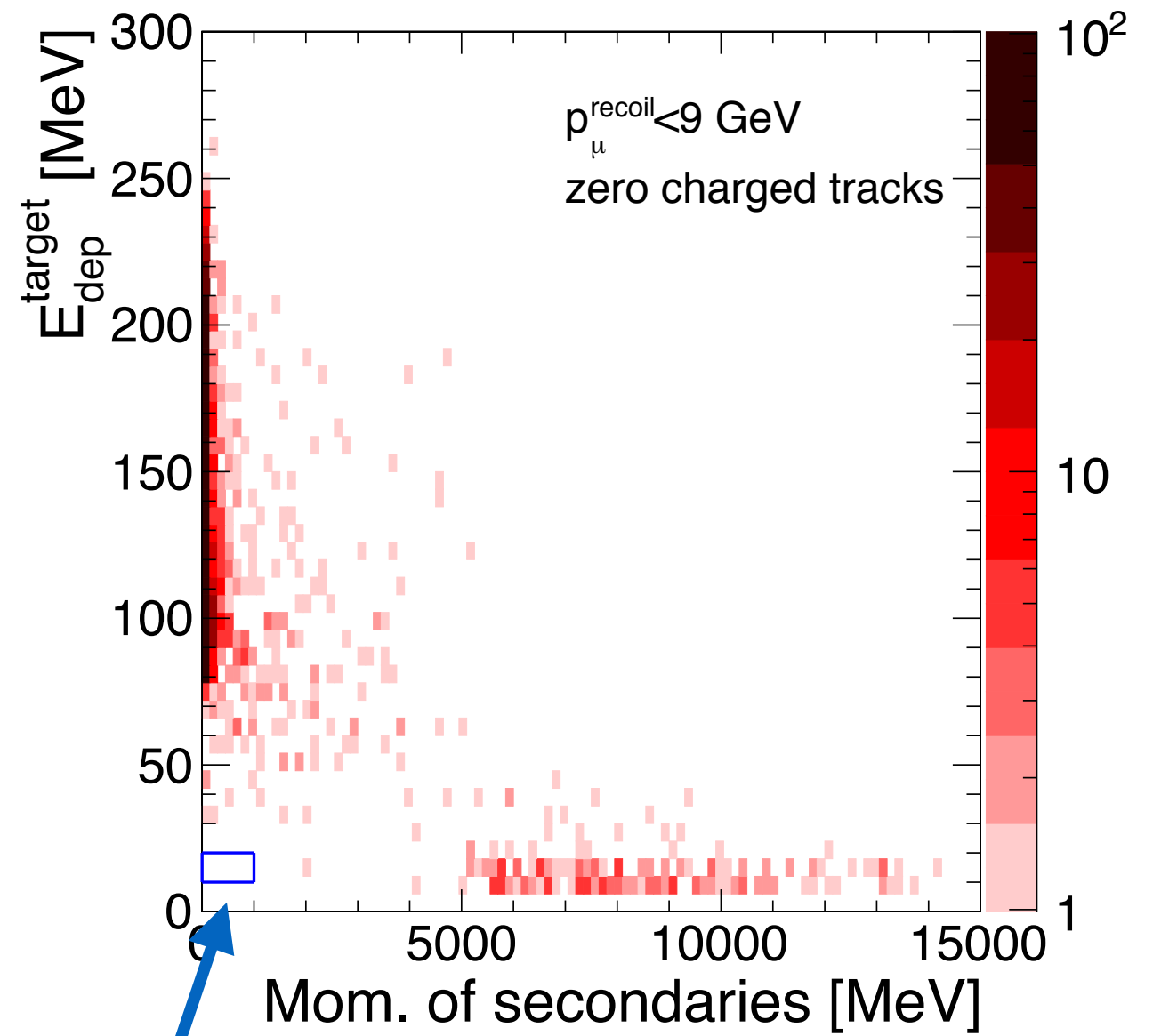
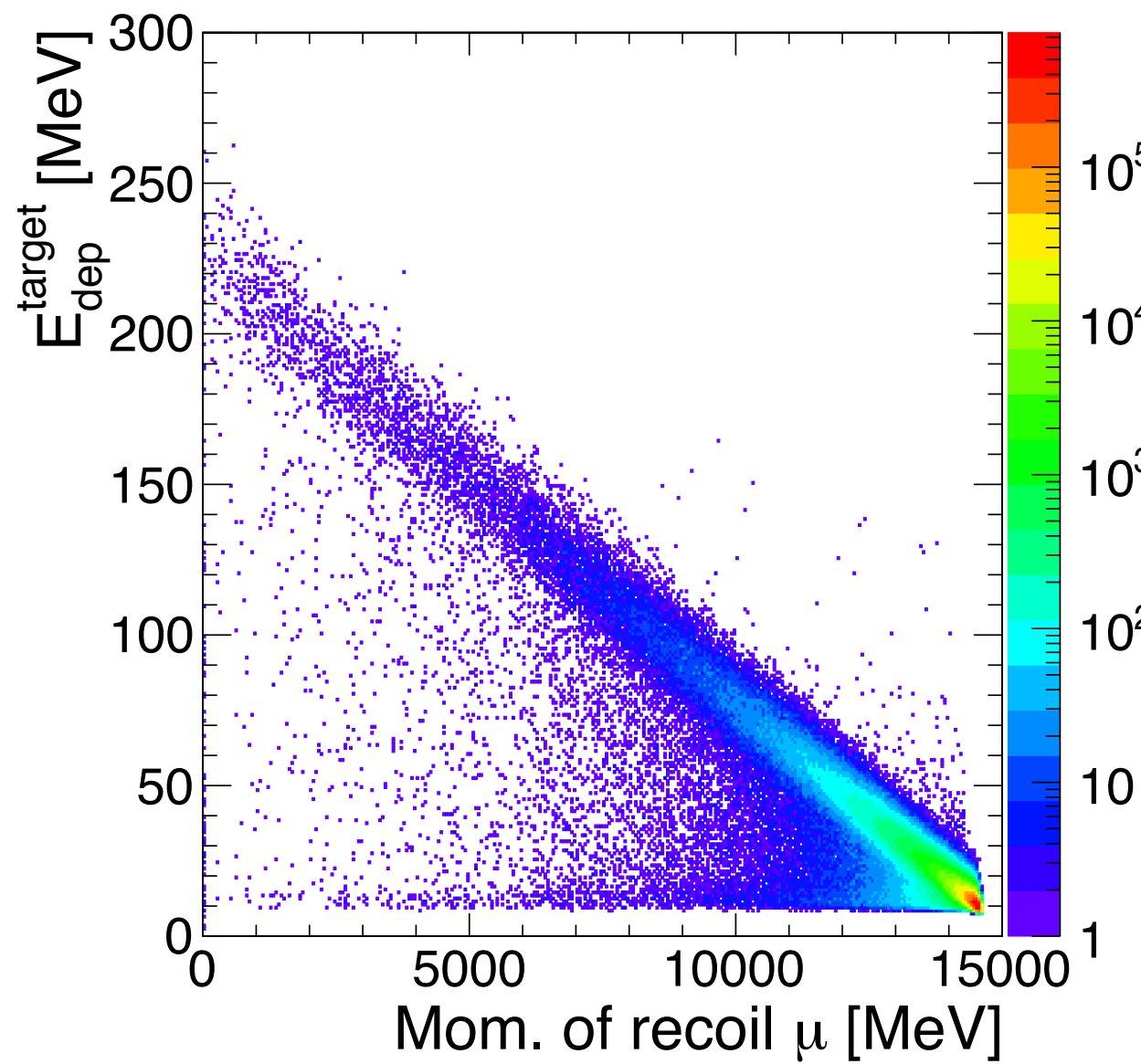
- 1) Measure  $E_{\text{in}}$  with tracker
- 2) Pass beam through target
- 3) Measure  $E_{\text{out}}$  with tracker
- 4) Trigger on missing energy

# Muon Missing Momentum Concept



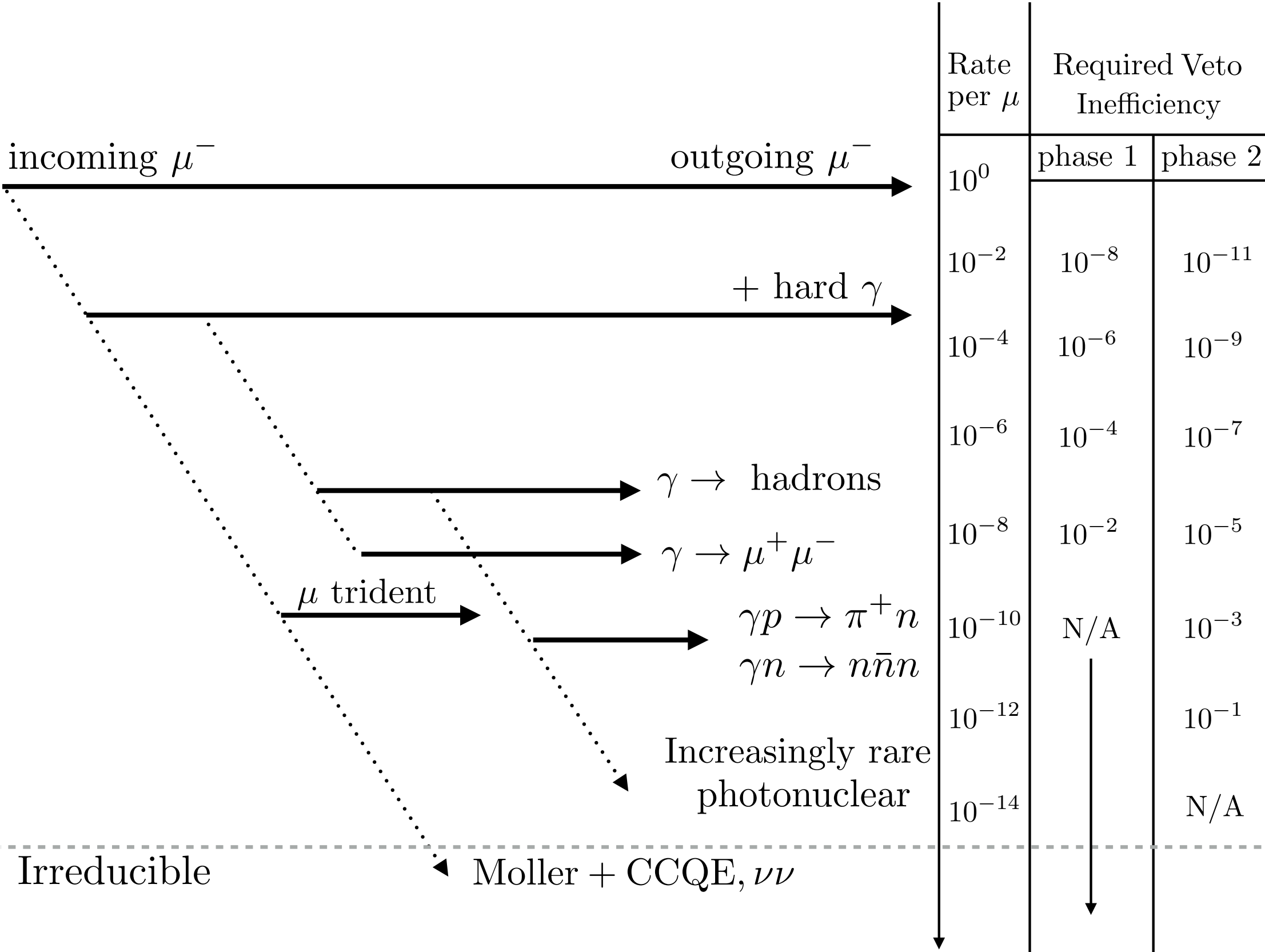
- 1) Measure  $E_{in}$  with tracker
- 2) Pass beam through target
- 3) Measure  $E_{out}$  with tracker
- 4) Trigger on missing energy
- 5) Veto additional SM activity

# GEANT Simulation

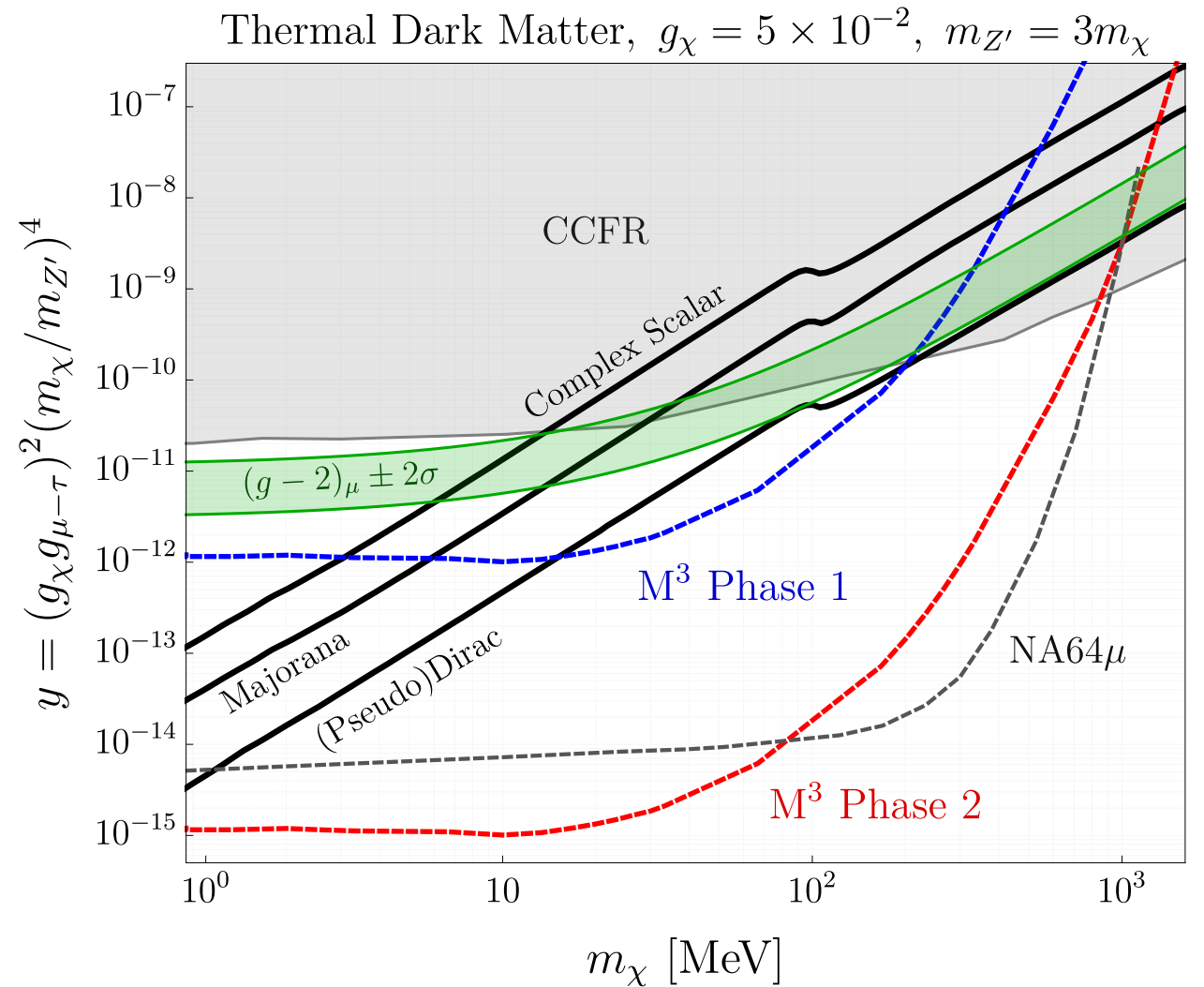
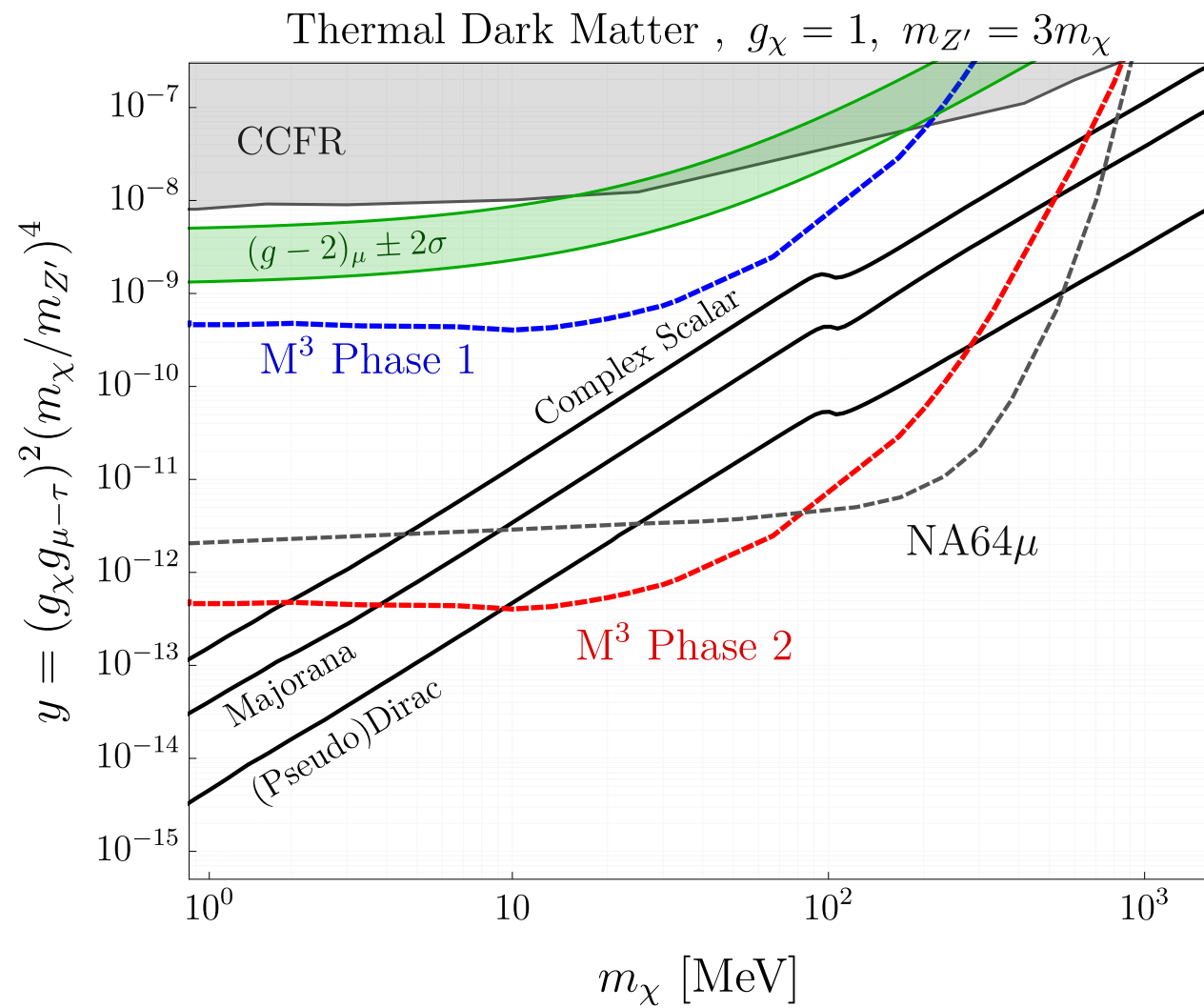


Signal region

# Background Rates



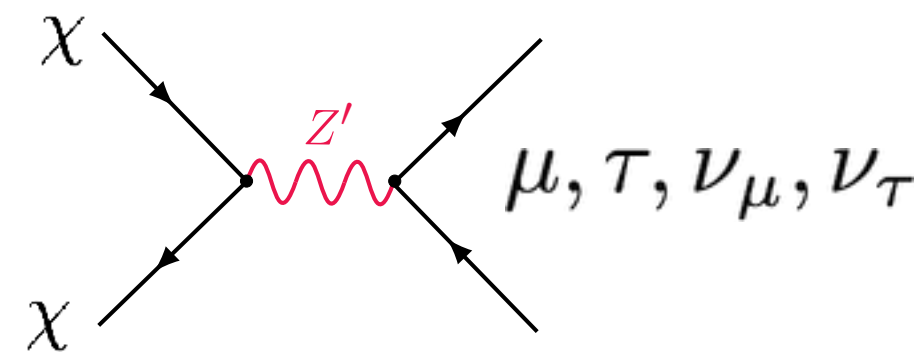
# Comprehensive Coverage



Gauged  $L_\mu - L_\tau$  Interaction

Also resolve muon g-2 with light physics

Compatible parameter space for freeze-out



Phase 1,2: 1e10, 1e13 muons

# Overview

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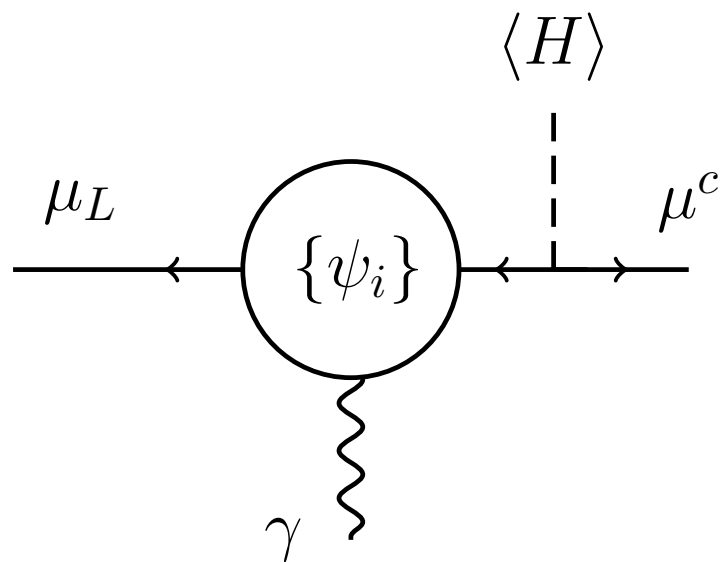
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$$\mathcal{L}_{\text{eff}} = C_{\text{eff}} \frac{v}{M^2} (\mu_L \sigma^{\nu\rho} \mu^c) F_{\nu\rho} + \text{h.c.}$$

Do EWSB + chiral flip come from muon mass insertion?

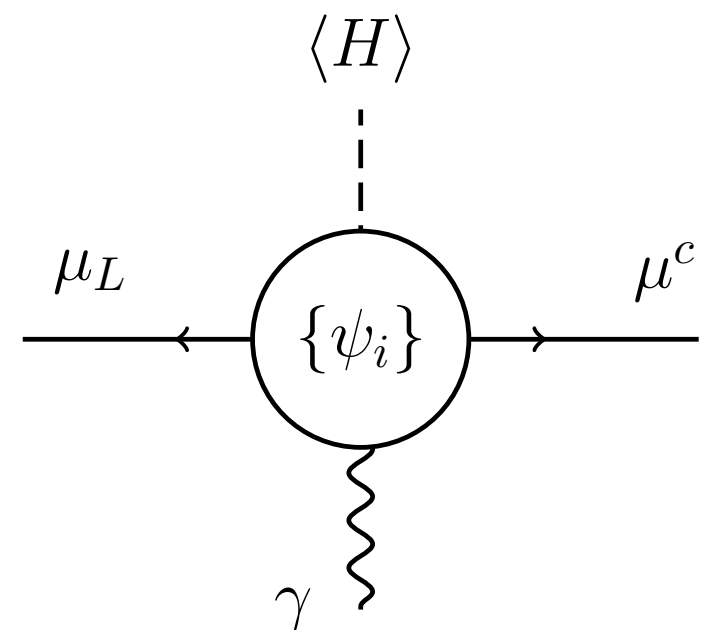
YES

Singlet Models



NO

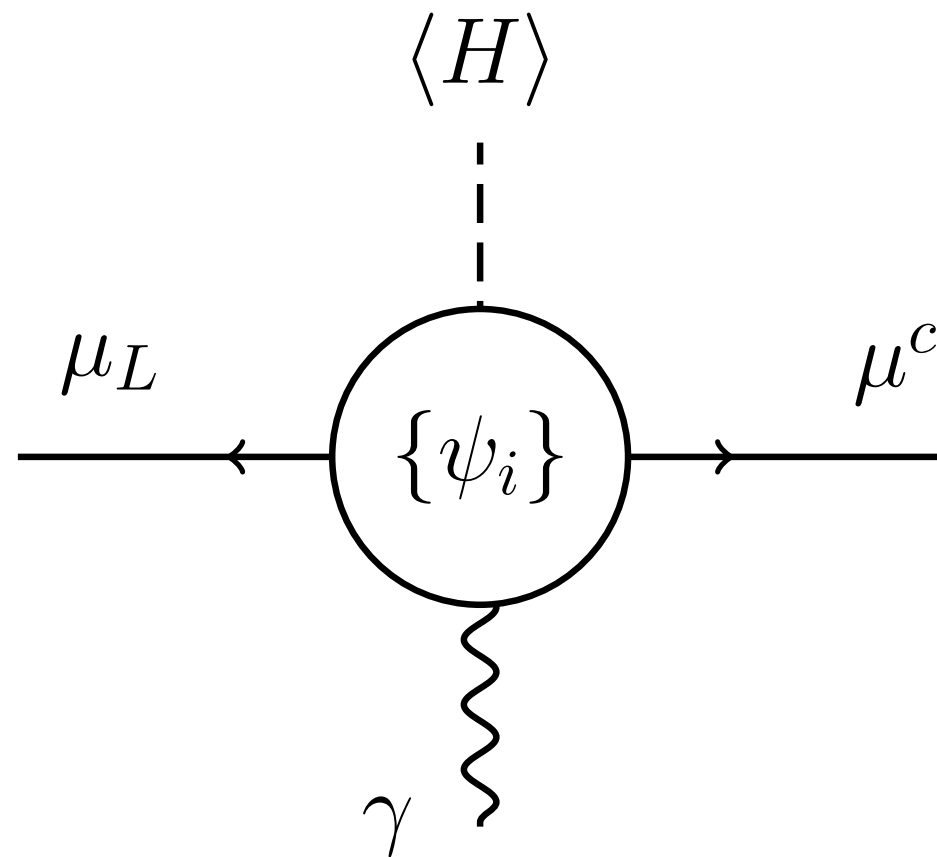
Electroweak Models





# Electroweak Models

Chiral flip and EWSB on BSM lines



**Hard to fully catalog BSM**

Most new EW stuff will work  
 $M > 100$  GeV from LEP limits

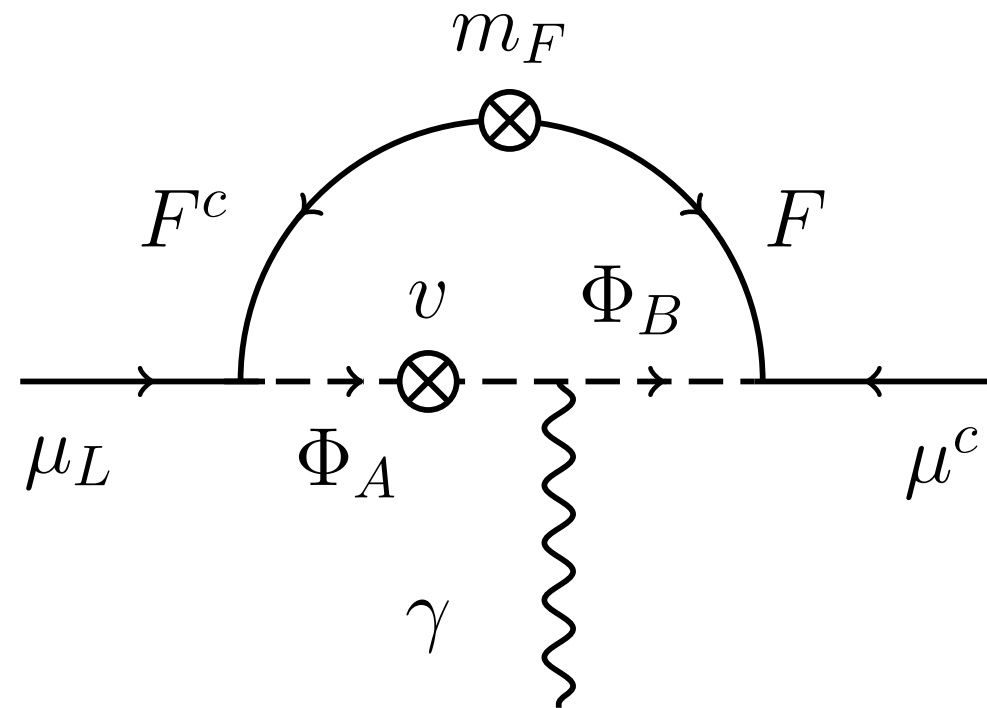
Many free params (eg MSSM)  
Many models testable @ LHC

**“Nightmare” Heavy BSM**

Muon-philic  $\sim 100$  TeV &  $O(1)$  couplings  
Need *muon* collider to fully test these

# Electroweak Models

Representative ultra-heavy model



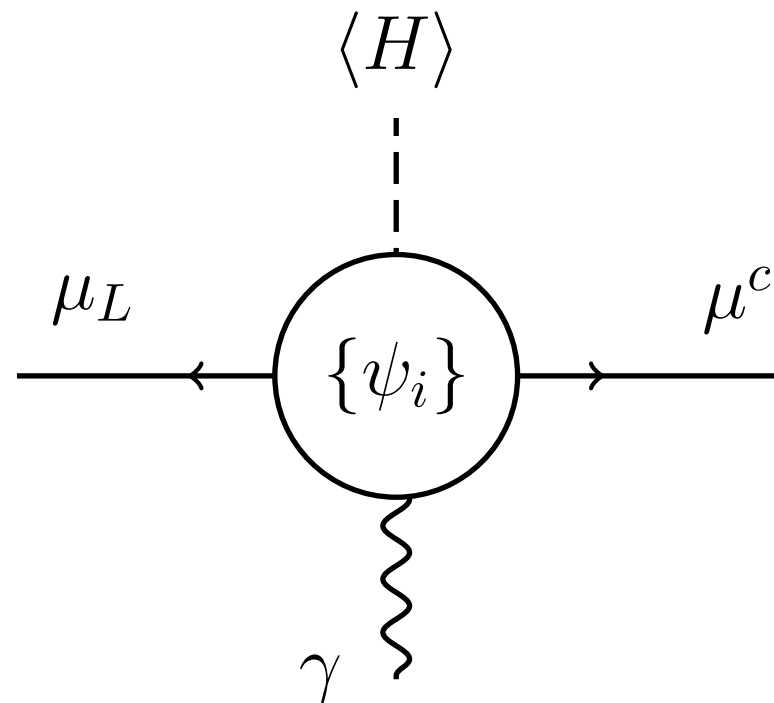
$$\mathcal{L}_{\text{SSF}} \supset -y_1 F^c L_{(\mu)} \Phi_A^* - y_2 F \mu^c \Phi_B - \kappa H \Phi_A^* \Phi_B \\ - m_A^2 |\Phi_A|^2 - m_B^2 |\Phi_B|^2 - m_F F F^c + \text{h.c.} .$$

**What is maximum mass of the *lightest* charged particle?**

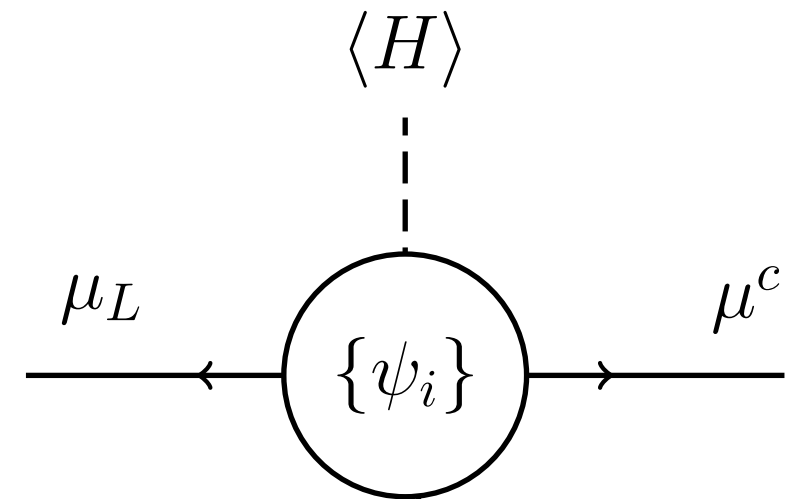
Model	$R$	$R_A$	$R_B$	Highest possible mass (TeV) of lightest charged BSM state	
				Unitarity only	
				$N_{\text{BSM}}:$ 1      10	
SSF	$1_{-1}$	$2_{1/2}$	$1_0$	65.2	241
	$1_{-2}$	$2_{3/2}$	$1_1$	85.9	321
	$1_0$	$2_{-1/2}$	$1_{-1}$	46.2	176
	$1_1$	$2_{-3/2}$	$1_{-2}$	81.8	302
	$2_{-1/2}$	$3_0$	$2_{-1/2}$	21.4	107
	$2_{-3/2}$	$3_1$	$2_{1/2}$	83.7	308
	$2_{1/2}$	$3_{-1}$	$2_{-3/2}$	95.5	356
	$2_{-1/2}$	$1_0$	$2_{-1/2}$	65.2	241
	$2_{-3/2}$	$1_1$	$2_{1/2}$	85.9	321
	$2_{1/2}$	$1_{-1}$	$2_{-3/2}$	44.8	155
	$3_{-1}$	$2_{1/2}$	$3_0$	95.4	359
	$3_0$	$2_{-1/2}$	$3_{-1}$	39.4	144
FFS	$1_{-1}$	$2_{1/2}$	$1_0$	37.3	118
	$1_{-2}$	$2_{3/2}$	$1_1$	67.3	213
	$1_0$	$2_{-1/2}$	$1_{-1}$	59.1	187
	$1_1$	$2_{-3/2}$	$1_{-2}$	73.2	231
	$2_{-1/2}$	$3_0$	$2_{-1/2}$	40	126
	$2_{-3/2}$	$3_1$	$2_{1/2}$	56.3	178
	$2_{1/2}$	$3_{-1}$	$2_{-3/2}$	82.3	260
	$2_{-1/2}$	$1_0$	$2_{-1/2}$	37.3	118
	$2_{-3/2}$	$1_1$	$2_{1/2}$	67.3	213
	$2_{1/2}$	$1_{-1}$	$2_{-3/2}$	46.2	146
	$3_{-1}$	$2_{1/2}$	$3_0$	71	225
	$3_0$	$2_{-1/2}$	$3_{-1}$	23.4	75
	$3_{-1}$	$2_{-1/2}$	$3_0$	23.4	75
	$3_0$	$2_{1/2}$	$3_{-1}$	23.4	75
$M_{\text{BSM,charged}}^{\text{max}}$ (max in each column)				<b>95.5</b>	<b>359</b>

This seems pretty bad, but ...

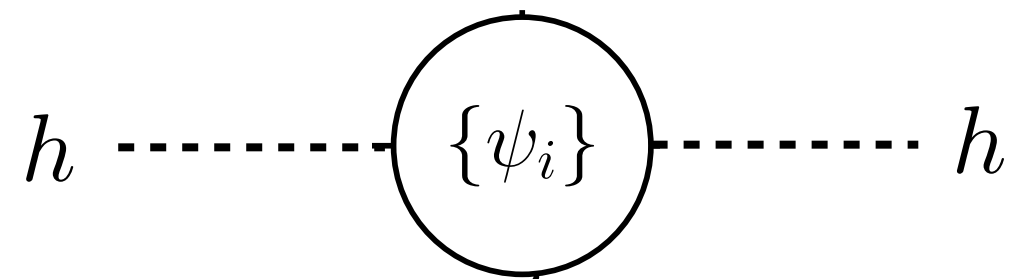
# Makes the hierarchy problem real



Required for anomaly



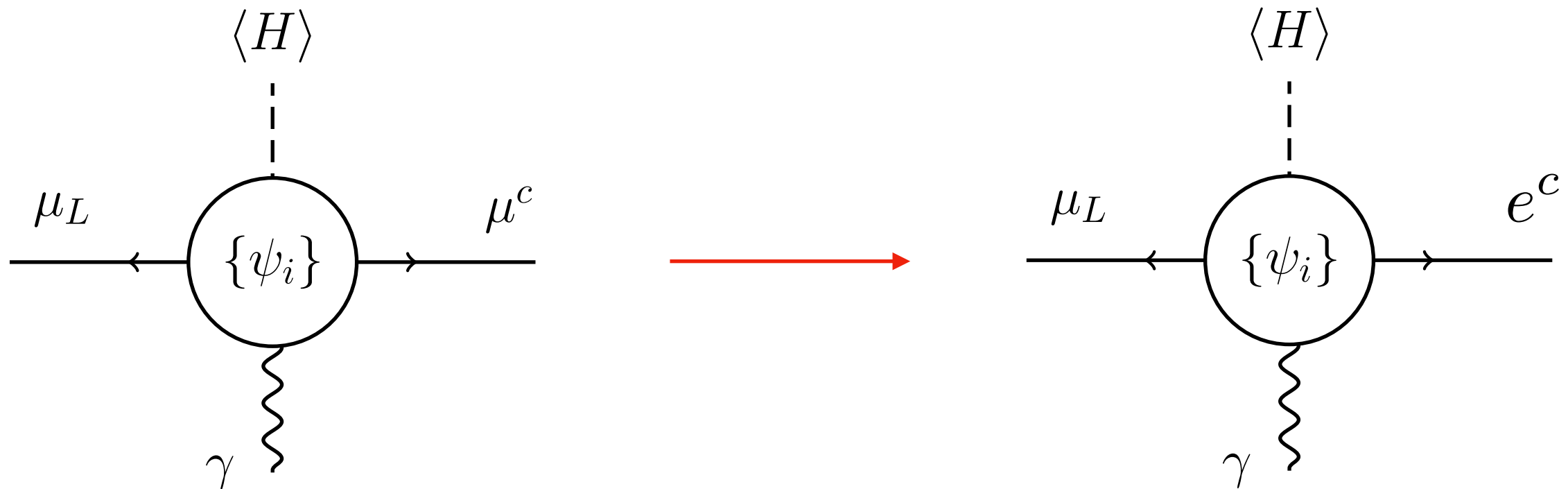
Muon mass



Higgs mass

Finite calculable  $\sim 100$  TeV corrections to Higgs/muon masses  
NOT like LHC and SUSY!

# Important connection to flavor physics



Required for anomaly

$$\text{Br}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$$

$$\text{Br}(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8}$$

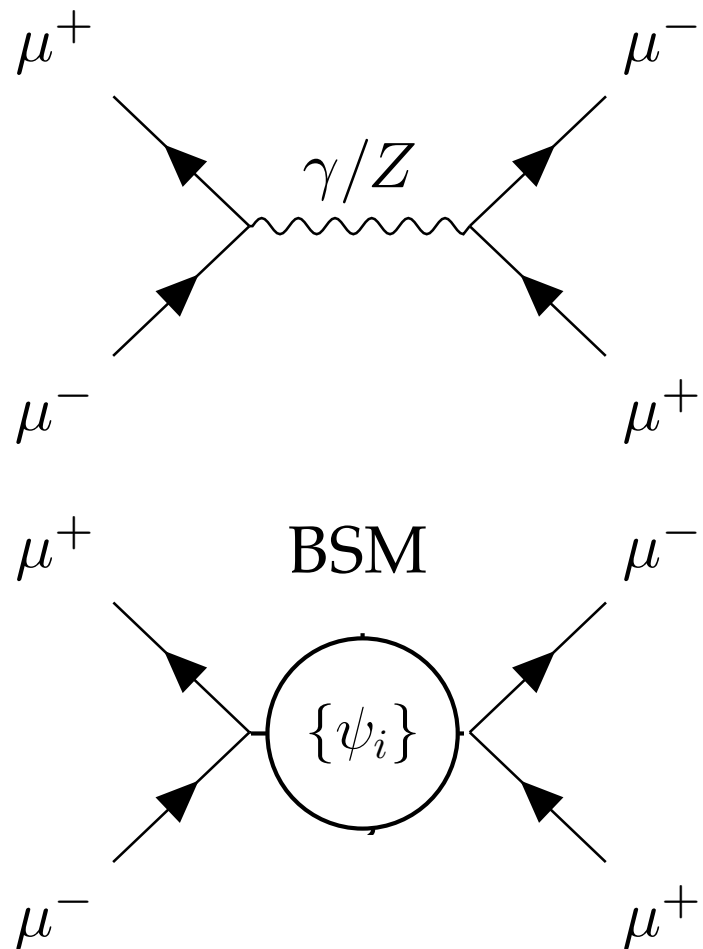
$$\text{Br}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8}$$

Dangerous FCNC without MFV or tuning

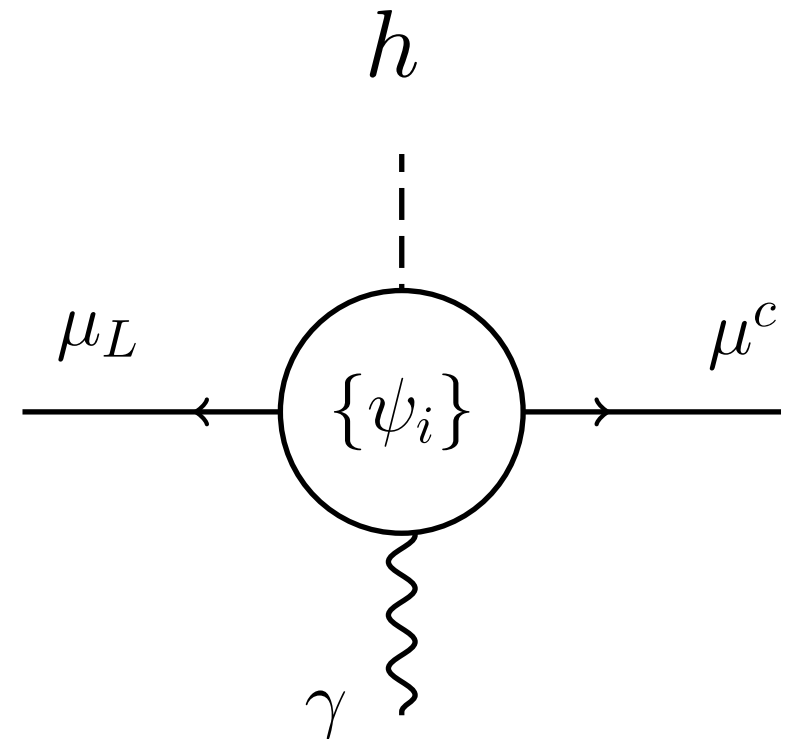
Model	$R$	$R_A$	$R_B$	Highest possible mass (TeV) of lightest charged BSM state							
				Unitarity only		Unitarity + MFV		Unitarity + Naturalness		Unitarity + Naturalness + MFV	
				$N_{\text{BSM}}:$ 1      10		$N_{\text{BSM}}:$ 1      10		$N_{\text{BSM}}:$ 1      10		$N_{\text{BSM}}:$ 1      10	
SSF	$1_{-1}$	$2_{1/2}$	$1_0$	65.2	241	12.9	47.1	11.5	11.5	6.54	10.1
	$1_{-2}$	$2_{3/2}$	$1_1$	85.9	321	18.1	64.8	19.2	19.2	8.41	12.3
	$1_0$	$2_{-1/2}$	$1_{-1}$	46.2	176	9.41	34.1	15.6	17.5	5.93	8.56
	$1_1$	$2_{-3/2}$	$1_{-2}$	81.8	302	17.1	63.7	19.3	19.3	8.38	12.1
	$2_{-1/2}$	$3_0$	$2_{-1/2}$	21.4	107	4.2	15.5	7.47	8.99	3.23	5.0
	$2_{-3/2}$	$3_1$	$2_{1/2}$	83.7	308	16.6	60.7	13.4	13.4	7.06	10.6
	$2_{1/2}$	$3_{-1}$	$2_{-3/2}$	95.5	356	18.3	67.8	15.6	15.6	7.75	11.3
	$2_{-1/2}$	$1_0$	$2_{-1/2}$	65.2	241	12.9	47.1	11.5	11.5	6.54	10.1
	$2_{-3/2}$	$1_1$	$2_{1/2}$	85.9	321	18.1	64.8	19.2	19.2	8.41	12.3
	$2_{1/2}$	$1_{-1}$	$2_{-3/2}$	44.8	155	8.8	32.3	10.9	10.9	5.64	8.56
	$3_{-1}$	$2_{1/2}$	$3_0$	95.4	359	19.4	73	20.1	30	7.75	11.5
	$3_0$	$2_{-1/2}$	$3_{-1}$	39.4	144	7.82	28.6	10.8	15.1	4.14	6.08
	$1_{-1}$	$2_{1/2}$	$1_0$	37.3	118	8.87	28	12.3	18.7	4.6	7.04
	$1_{-2}$	$2_{3/2}$	$1_1$	67.3	213	15.8	50	13.5	18.8	4.86	6.93
FFS	$1_0$	$2_{-1/2}$	$1_{-1}$	59.1	187	13.2	41.8	12.4	17.2	4.02	6.28
	$1_1$	$2_{-3/2}$	$1_{-2}$	73.2	231	17.4	55	13.9	19.7	5.04	7.25
	$2_{-1/2}$	$3_0$	$2_{-1/2}$	40	126	9.38	29.7	8.0	11.5	2.88	4.34
	$2_{-3/2}$	$3_1$	$2_{1/2}$	56.3	178	13.6	42.9	11.8	16.2	4.26	6.1
	$2_{1/2}$	$3_{-1}$	$2_{-3/2}$	82.3	260	19.2	60.6	13.6	19	4.93	7.0
	$2_{-1/2}$	$1_0$	$2_{-1/2}$	37.3	118	8.87	28	12.3	18.7	4.6	7.04
	$2_{-3/2}$	$1_1$	$2_{1/2}$	67.3	213	15.8	50	13.5	18.8	4.86	6.93
	$2_{1/2}$	$1_{-1}$	$2_{-3/2}$	46.2	146	11.2	35.4	9.83	13.8	3.49	5.18
	$3_{-1}$	$2_{1/2}$	$3_0$	71	225	17	53.6	13.1	18.1	4.04	6.97
	$3_0$	$2_{-1/2}$	$3_{-1}$	23.4	75	5.20	16.0	7.3	7.60	2.73	4.03
	$3_{-1}$	$2_{1/2}$	$3_0$	71	225	17	53.6	13.1	18.1	4.04	6.97
	$3_0$	$2_{-1/2}$	$3_{-1}$	23.4	75	5.20	16.0	7.3	7.60	2.73	4.03
	$3_{-1}$	$2_{1/2}$	$3_0$	71	225	17	53.6	13.1	18.1	4.04	6.97
	$3_0$	$2_{-1/2}$	$3_{-1}$	23.4	75	5.20	16.0	7.3	7.60	2.73	4.03
$M_{\text{BSM,charged}}^{\text{max}}$ (max in each column)				<b>95.5</b>	<b>359</b>	<b>19.4</b>	<b>73</b>	<b>20.1</b>	<b>30</b>	<b>8.41</b>	<b>12.3</b>

~ 10 TeV within scope of muon collider studies [Delahaye et al 1901.06150]

# Guaranteed BSM at Muon Colliders



Bhabha scattering



Higgs photon production

## Concluding Remarks

Exciting time for  $g-2$ , new results soon!

### If anomaly is due to SM singlets

Must be muon-philic scalar or vector

### New searches for invisibly decaying “worst case” scenario

NA62 search in progress,  $M^3$  concept being studied

### Same $S/V$ for $g-2$ can couple to dark matter

Common parameters for anomaly + freeze out

Searches can cover much of overlap regions

### If anomaly is due to EW BSM

Unitarity  $< 100$  TeV, but  $\sim 10$ s TeV from naturalness / flavor

Muon collider yields guaranteed discovery of new BSM





$$\begin{aligned}
M_{\text{BSM,charged}}^{\text{max}} \quad &\equiv \quad \max_{\substack{\text{BSM theory space} \\ \Delta a_\mu = \Delta a_\mu^{\text{obs}}}} \left\{ \min_{i \in \text{BSM spectrum}} \left( m_{\text{charged}}^{(i)} \right) \right\}
\end{aligned}$$

# Backup Slides

# Constraints: Big Bang Nucleosynthesis

$V$  is in chemical equilibrium with SM in early universe

$$n_V \propto \begin{cases} T^3 & (T \gg m_V) \\ e^{-m/T} & (T \ll m_V) \end{cases}$$

When  $T < m$ , the  $V$  decays transfer entropy to SM particles  
Must happen before neutrinos decouple from photons

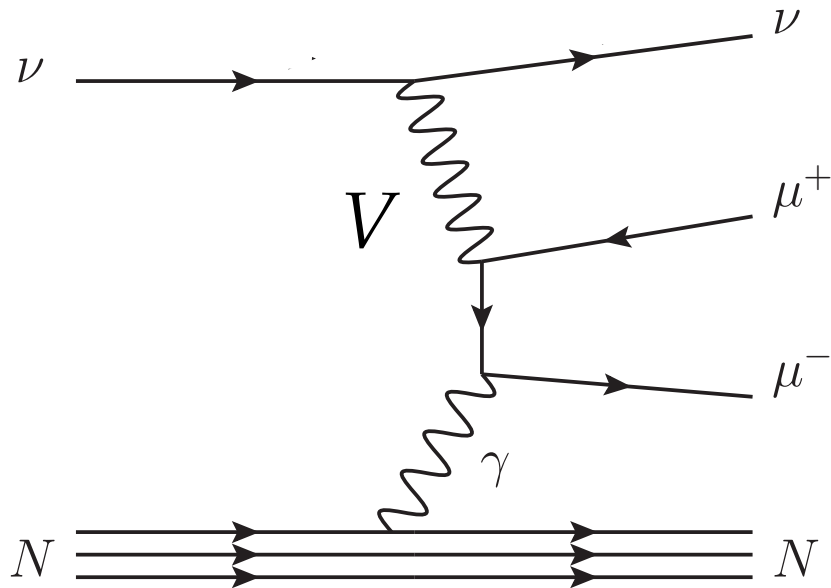
$$m \gtrsim T_{\nu,\text{dec}} \approx 2 \text{ MeV}$$

Otherwise  $V$  decays heat neutrinos not CMB  $\rightarrow \Delta N_{\text{eff}} \gtrsim 0.5$

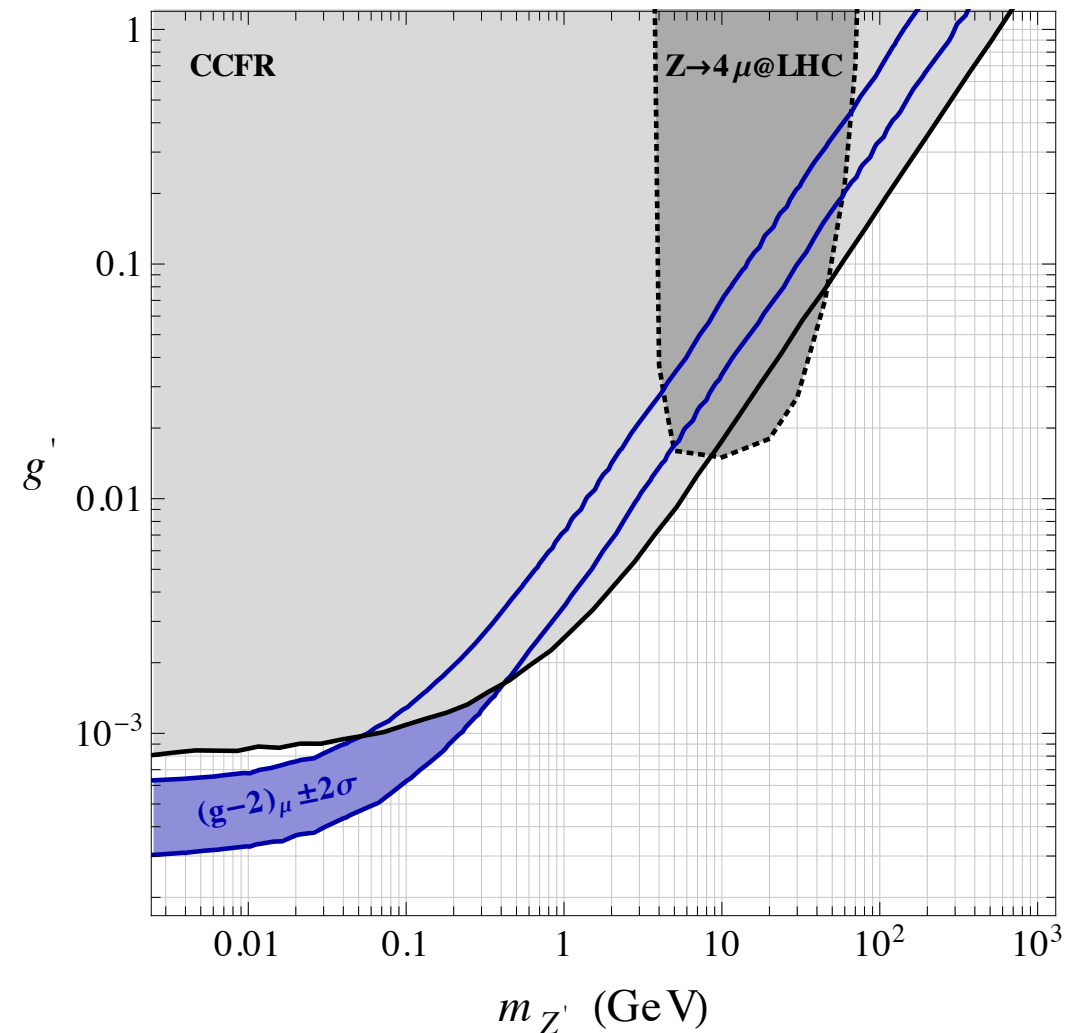
Spoils BBN element yields

\*mild contribution for  $m \sim \text{few MeV}$  may reduce Hubble tension

# Constraints: Neutrino Tridents, CCFR + CHARM II



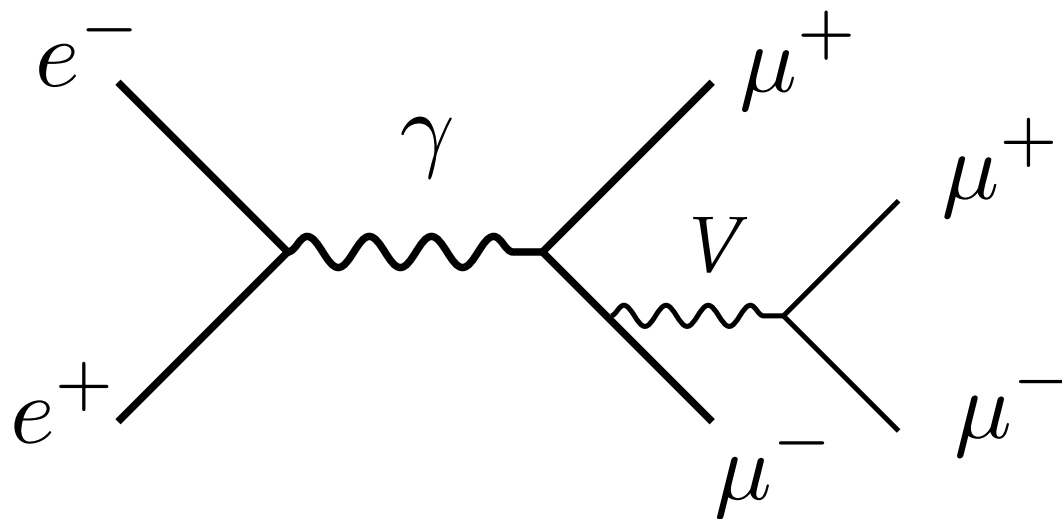
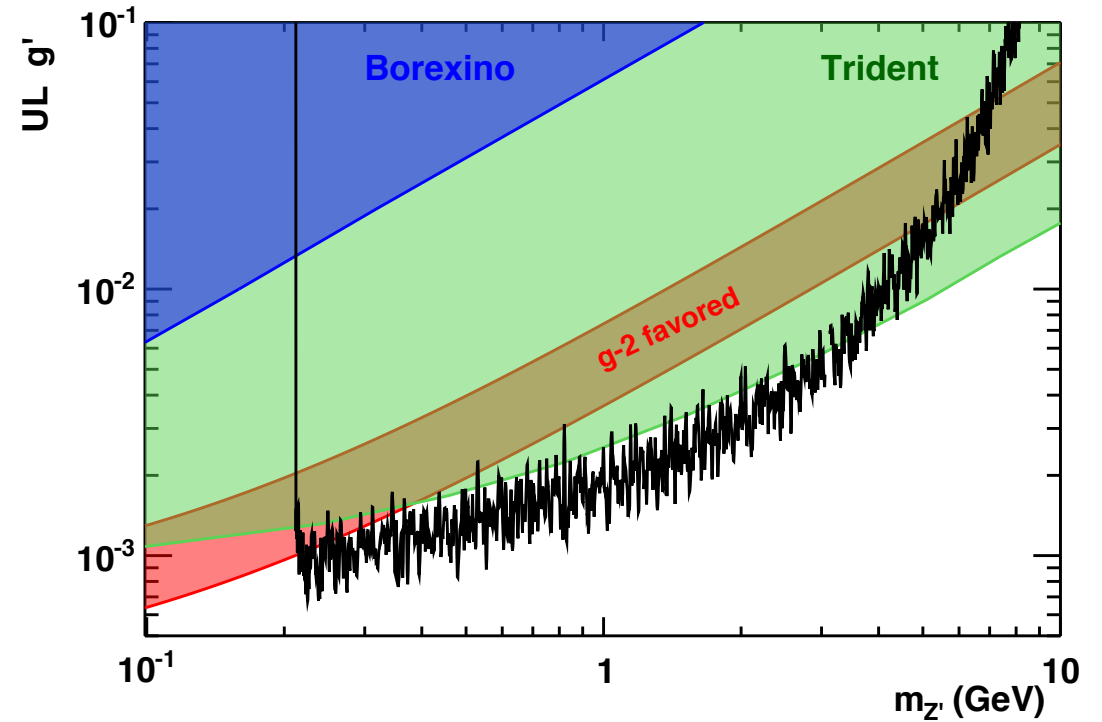
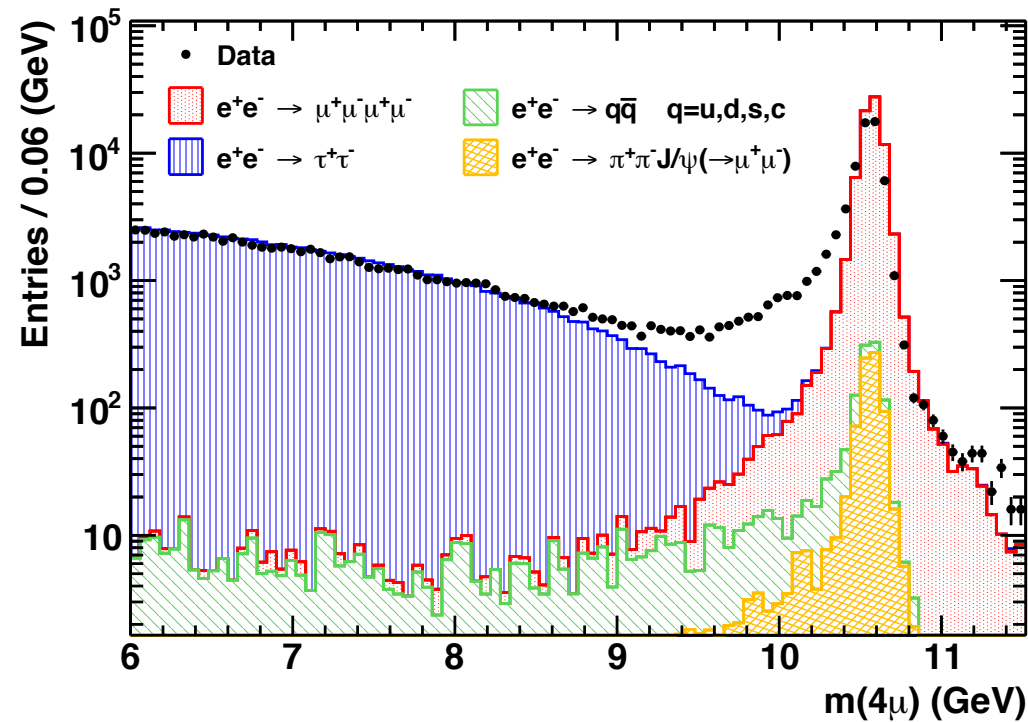
$$\frac{\sigma^{\text{CCFR}}}{\sigma^{\text{SM}}} = 0.82 \pm 0.28.$$



S. Mishra et al. (CCFR Collaboration), Phys.Rev.Lett. 66, 3117 (1991)

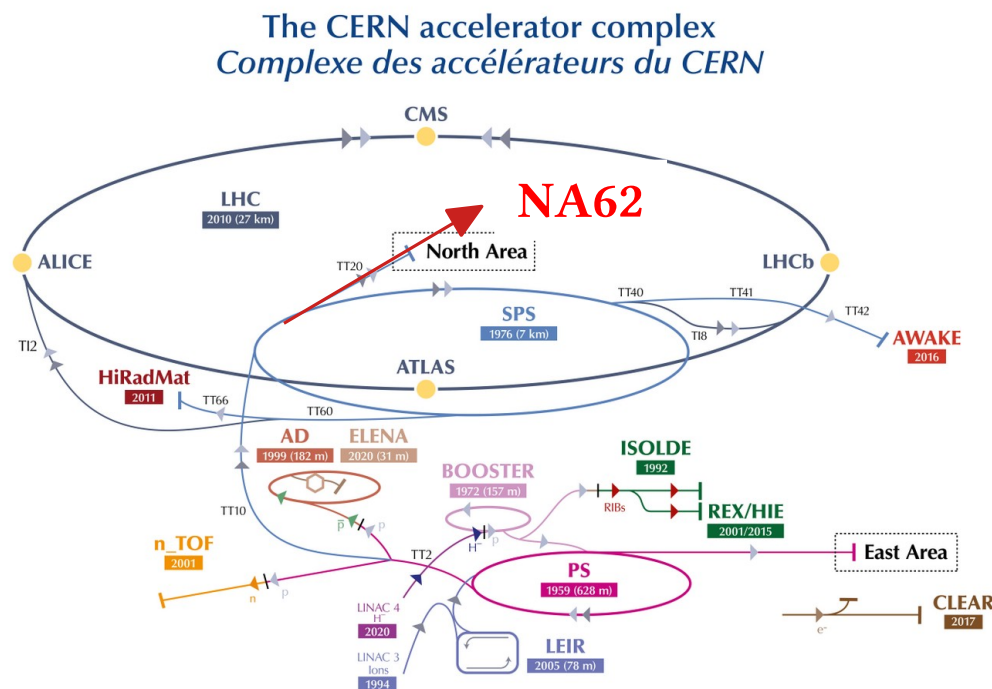
Altmanshoffer, Pospelov, Gori, Yavin 1406.2332

# Constraints: BABAR Experiment

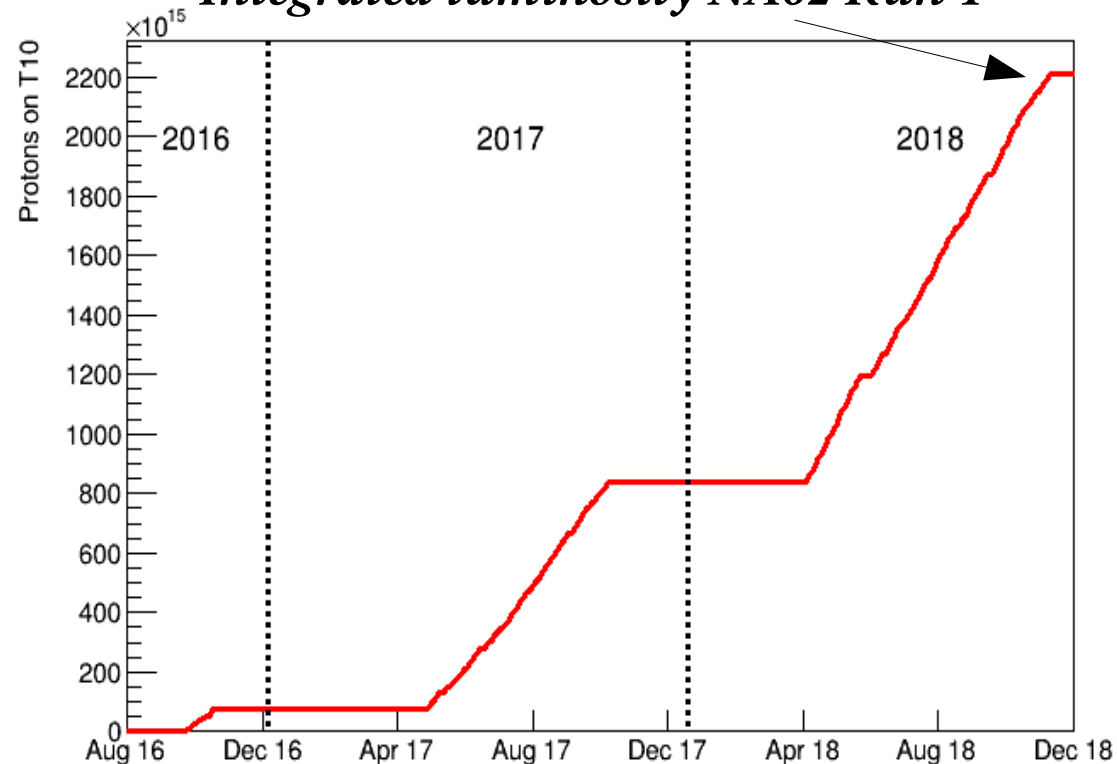


Search for 4 muon excess  
Excludes  $g-2$  for  $m > 200$  MeV

# State-of-the-art $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ experiments



Integrated luminosity NA62 Run 1



## Past experiments (E787/E949 @ BNL)

- ★ Kaon decay-at-rest technique

$$BR(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (1.73^{+1.15}_{-1.05}) \times 10^{-10}$$

Phys. Rev. D 79, 092004 (2009)

Phys. Rev. D 77, 052003 (2008)

## Present state-of-the-art $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ experiments

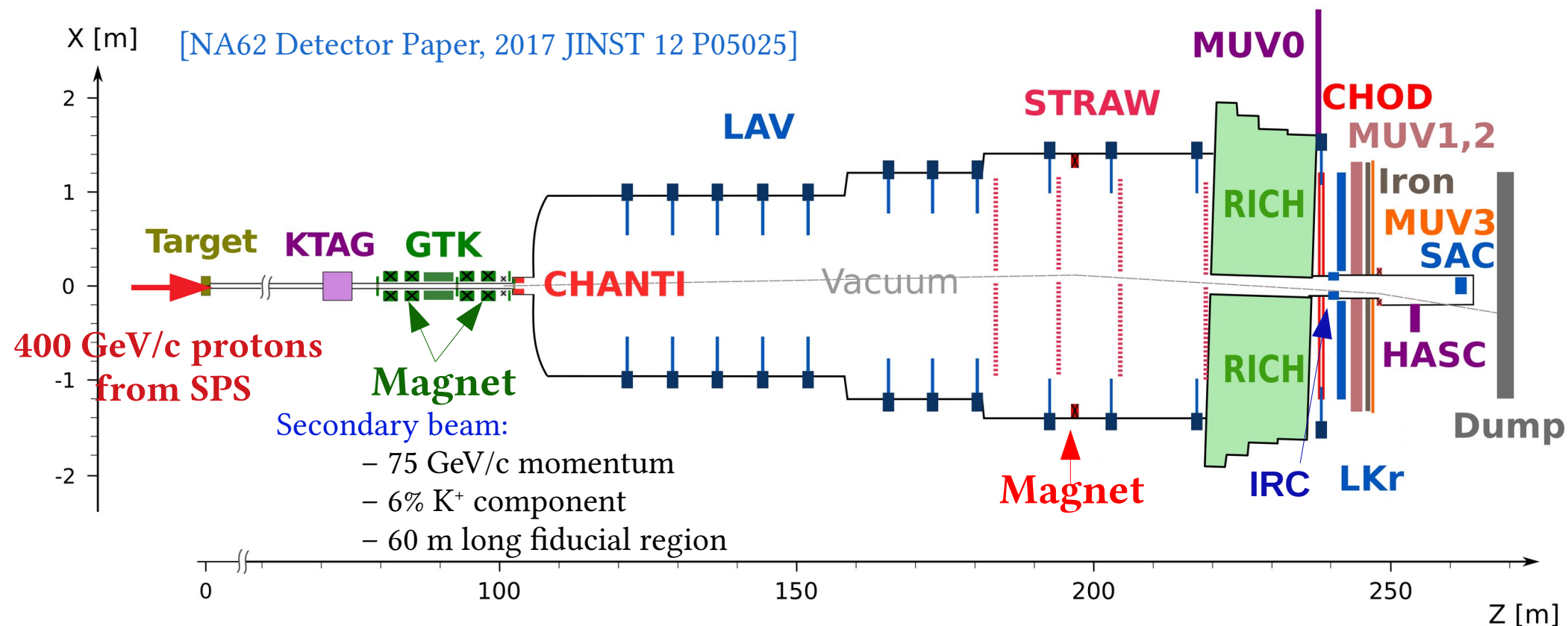
- ★ Kaon decay-in-flight technique
- ★ NA62 experiment (this talk)

### Run 1 statistics

$1.9 \times 10^{12}$  proton per spill on target

$\sim 2.2 \times 10^{18}$  POT collected in Run 1

# NA62 detector



## ■ Upstream detectors ( $K^+$ ):

- ★ **KTAG:** Differential Cherenkov counter for  $K^+$  ID
- ★ **GTK:** Si pixel beam tracker
- ★ **CHANTI:** Anti-counter for inelastic beam-GTK3 interactions

## ■ Decay Region detectors ( $\pi^+$ ):

- ★ **STRAW:** track momentum spectrometer
- ★ **CHOD:** Scintillator hodoscopes
- ★ **LKr/MUV1/MUV2 :** Calorimetric system
- ★ **RICH:** Cherenkov counter for  $\pi/\mu/e$  ID
- ★ **LAV/SAC/IRC:** Photon veto detectors
- ★ **MUV3:** Muon veto



# Invisible New Particles @ NA62

## Step 2: calculate matrix element

$$m_{ij} \equiv (p_i + p_j)^2 \qquad \lambda_\mu \equiv 2G_F f_K m_\mu V_{us} \simeq 8.7 \times 10^{-8}$$

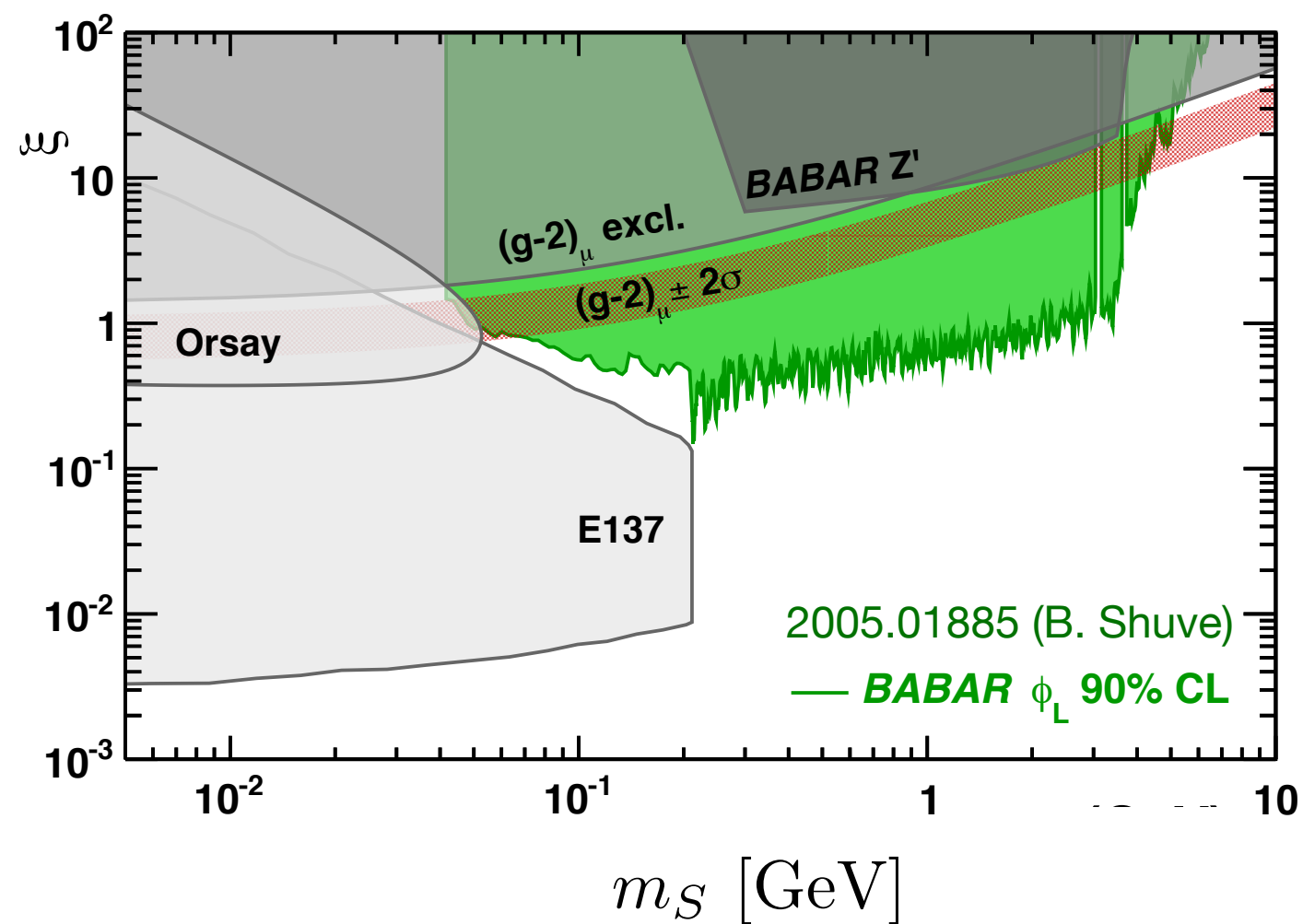
$$|\mathcal{M}_V|^2 = g_V^2 \lambda_\mu^2 \left[ 2 + \frac{(m_{12}^2 + 2m_\mu^2 - 2m_K^2)}{m_{23}^2 - m_\mu^2} \right. \\ \left. - \frac{(m_K^2 - m_\mu^2)(m_V^2 + 2m_\mu^2)}{(m_{23}^2 - m_\mu^2)^2} + 2 \frac{(m_K^2 - m_\mu^2)^2 + m_V^2 m_\mu^2}{m_{12}^2 (m_{23}^2 - m_\mu^2)} \right. \\ \left. - \frac{m_V^2 (m_K^2 - m_\mu^2)}{m_{12}^4} + \frac{(m_{23}^2 + m_\mu^2 - 2m_K^2)}{m_{12}^2} \right]$$

# Options For Singlets

Fun variation: mix  $S$  with neutral BSM bosons

Leptophilic scalar  
(eg mix with 2HDM)

$$\mathcal{L} = -\xi \sum_{\ell=e,\mu,\tau} \frac{m_\ell}{v} \bar{\ell}\ell S$$



LHC \*probably\* excludes  $> 10$  GeV region... or will soon 1808.03684