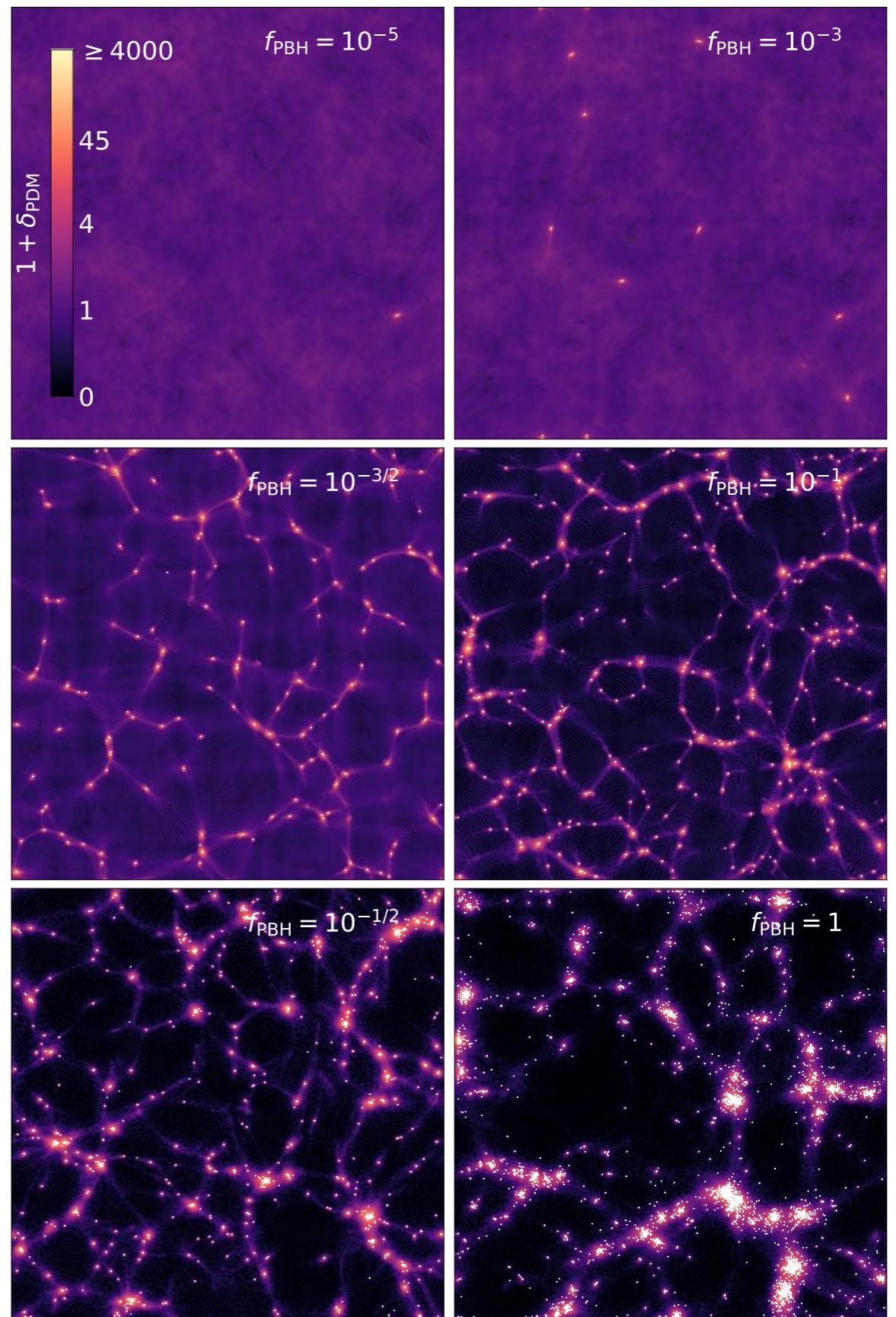


Primordial Black Hole Clustering and Gas Accretion

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Solar mass primordial black holes (PBHs)...

- ...could be dark matter! Or some fraction of it:

$$f_{\text{PBH}} = \frac{\Omega_{\text{PBH}}}{\Omega_{\text{CDM}}}$$

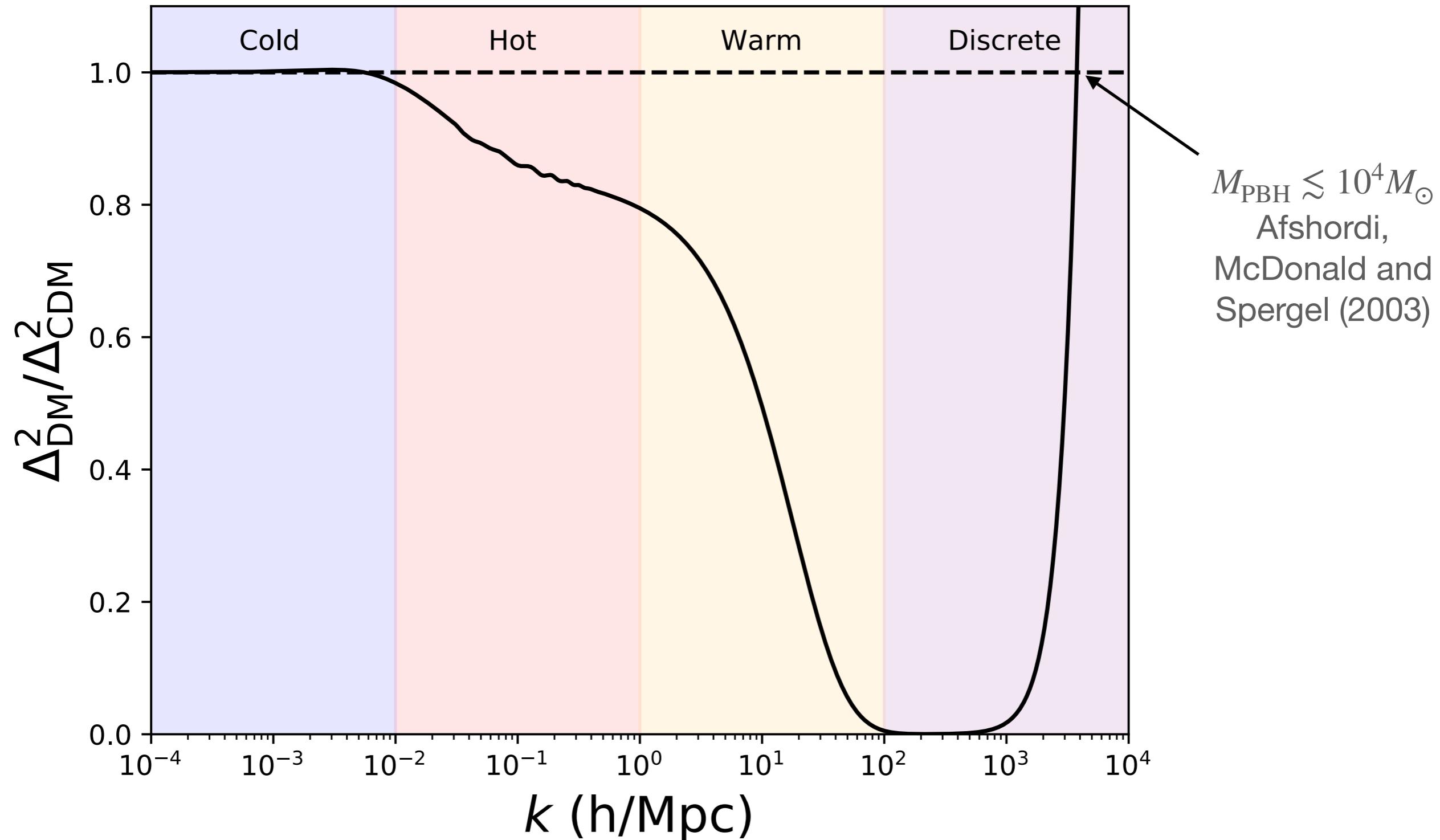
- ...could be LIGO events!

Did LIGO Detect Dark Matter? Bird et al. (2016)
Also: Sasaki et al. 2016, Ali-Haïmoud et al. 2017

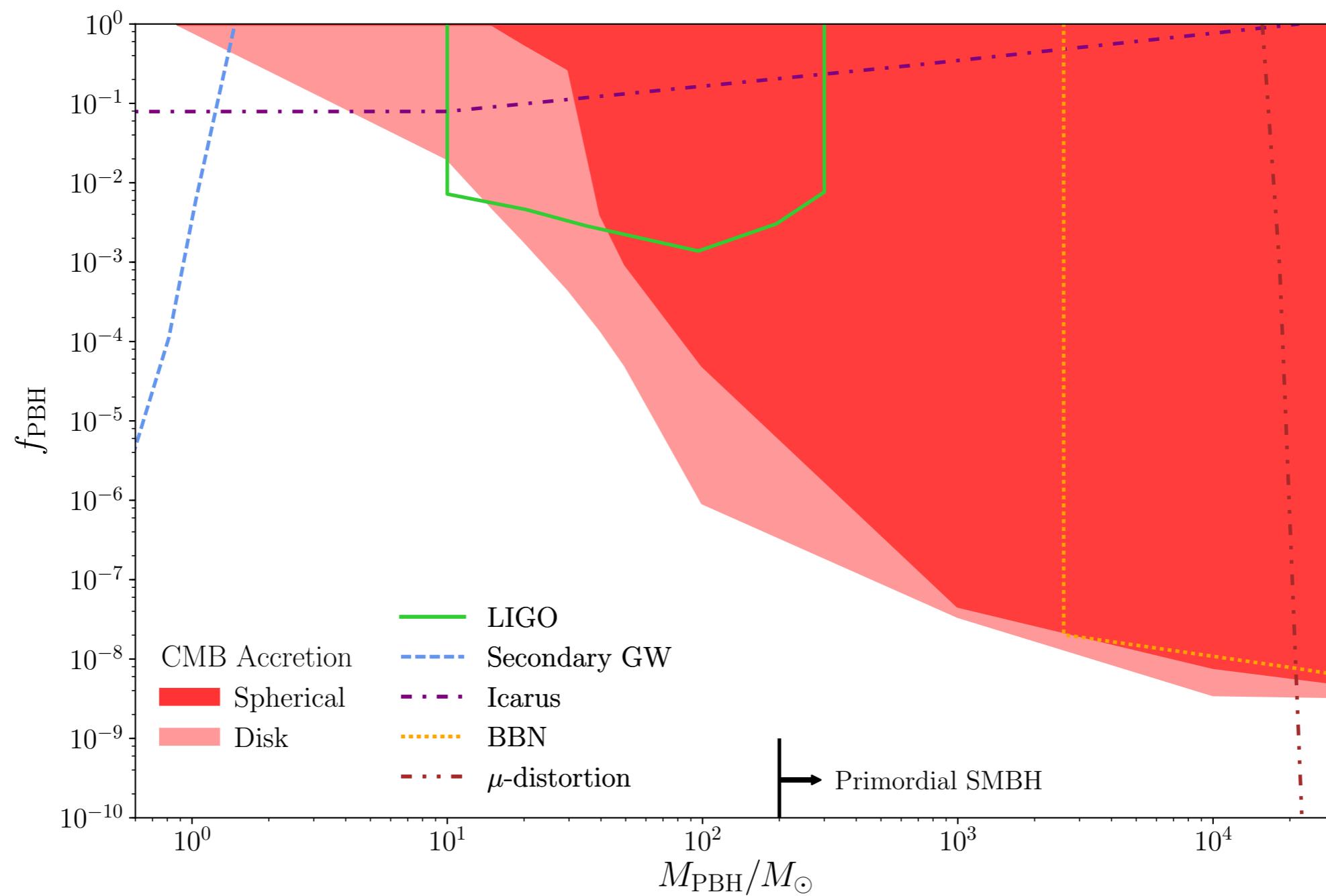
- ...could be seeds for supermassive black holes!

Serpico et al. (2020)

...could be dark matter...



...but there are constraints



Serpico et al. (2020)

Cosmic microwave background (CMB) constraints

- Where do they come from?
 - PBHs accrete gas after recombination
 - Gas heats up and radiation is emitted
 - Radiation changes thermal and ionization histories
 - More information: Ricotti, Ostriker and Mack (2008), Ali-Haïmoud and Kamionkowski (2017)
- Need to model gas accretion

Gas accretion

- Bondi-Hoyle-Littleton rate:

$$\dot{M} \propto \rho_\infty \frac{(GM)^2}{(V^2 + c_s^2)^{3/2}}$$

Bondi (1952)

- But what values to use?

- $M = M_{\text{PBH}}$

- $V \propto \sigma_{\text{rel}}$



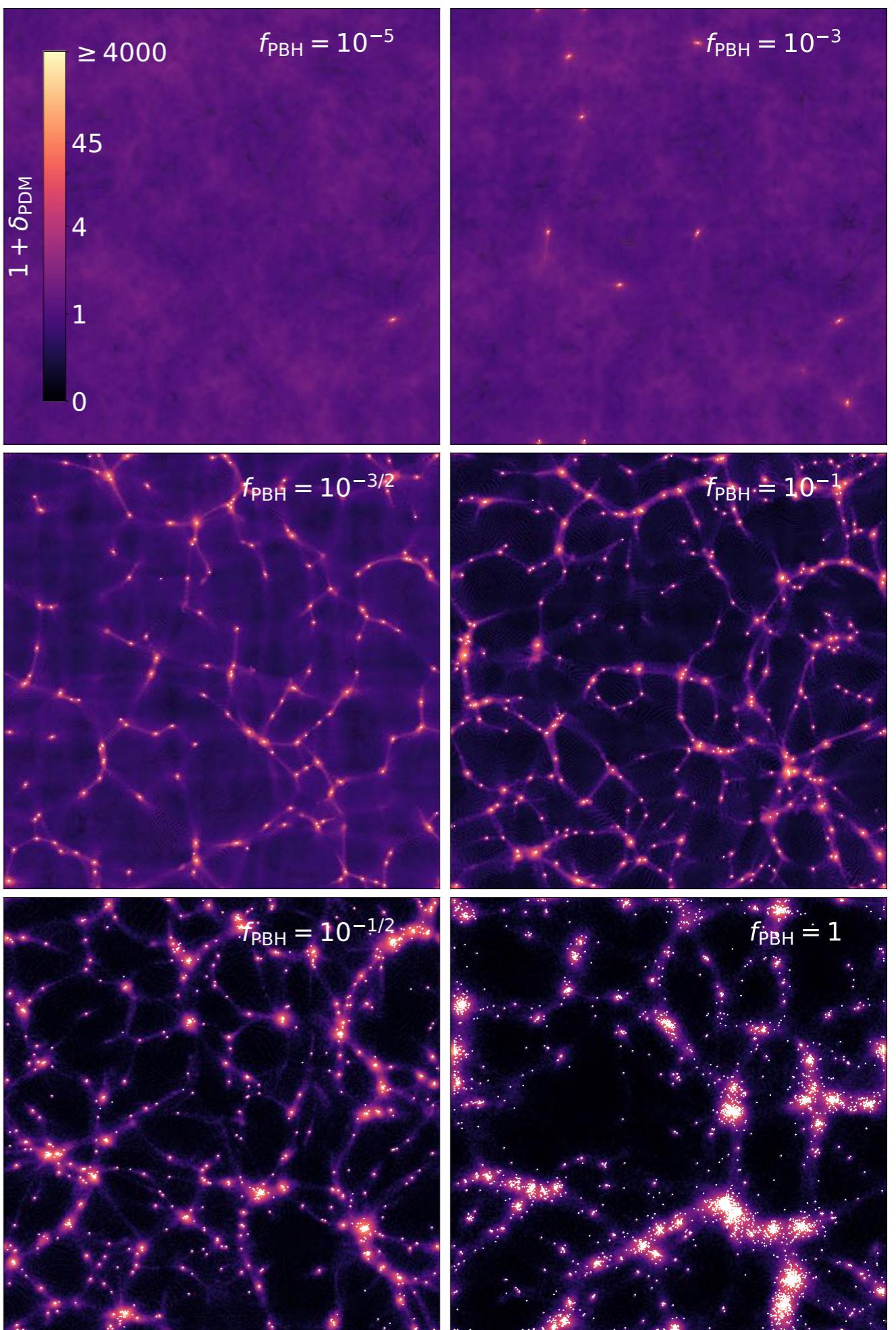
- $\rho_\infty = \bar{\rho}_b a^{-3}$

- $c_s^2 \propto \bar{T}_b$

Conservative choices, but are
any of these values correct?

Simulations

- Redshift: $10^6 \geq z \geq 10^2$
- Volume: $(35 \text{ kpc})^3$
- Cold dark matter
 - PBHs ($M_{\text{PBH}} = 30 M_\odot$)
 - Poisson distributed
 - Other DM if $f_{\text{PBH}} < 1$
 - Baryons?

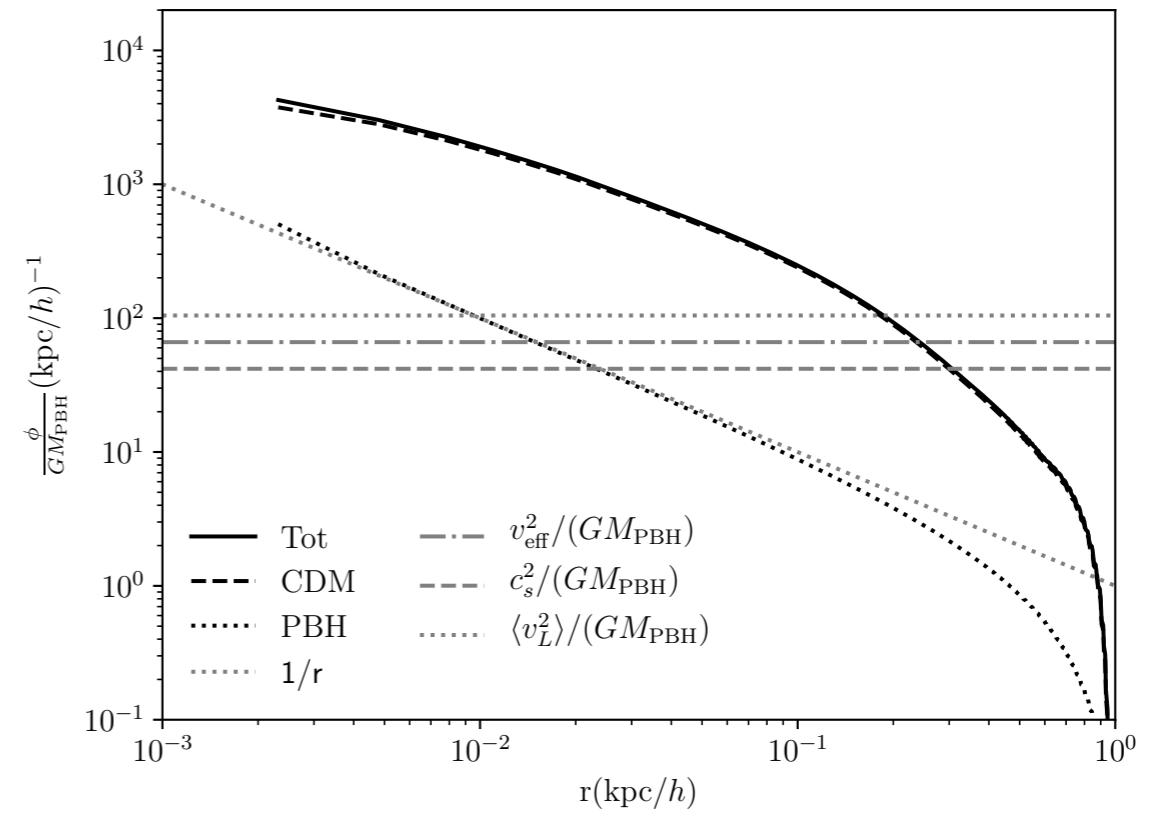
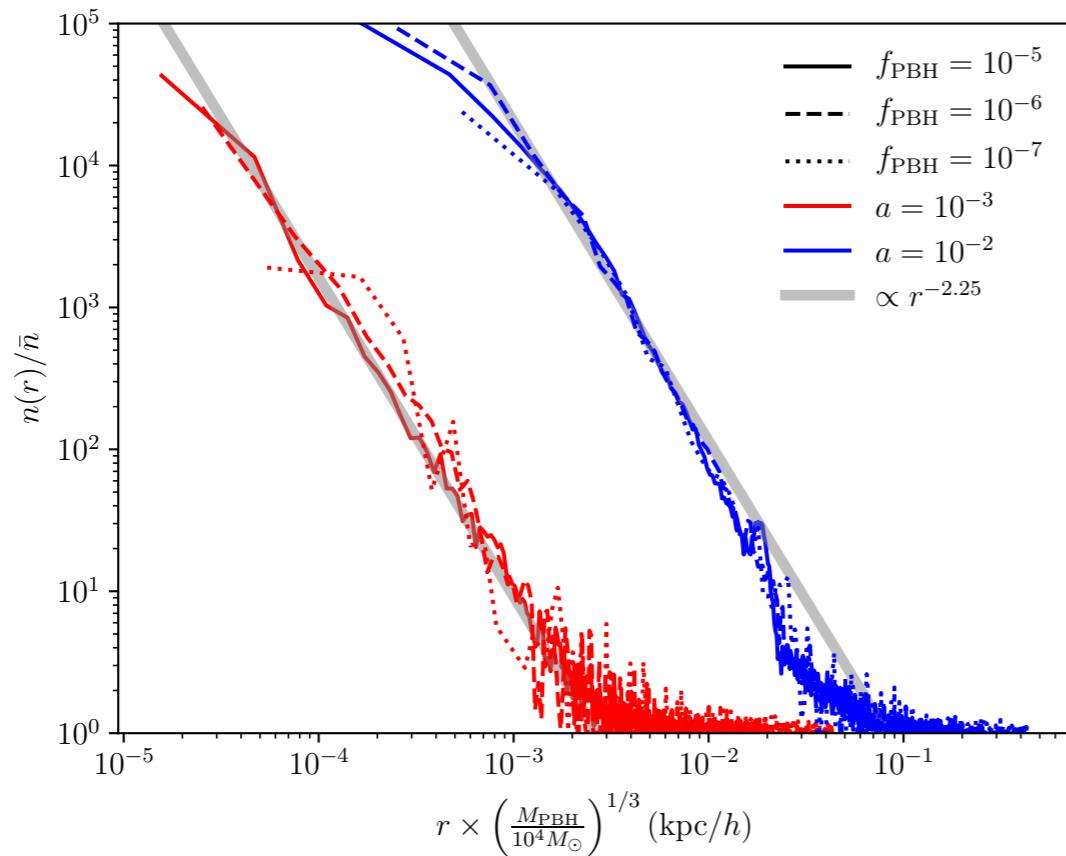


$$f_{\text{PBH}} \ll 1$$

- PBHs are rare, and mostly isolated from one another
 - Can use background values for ρ_∞ , c_s
- Accretion will depend on what the rest of the dark matter is!
 - Other dark matter doesn't cluster
 - Other dark matter does cluster

$f_{\text{PBH}} \ll 1$

- Other dark matter is cold, collisionless “particle dark matter,” forms a halo around the PBH



Serpico et al. (2020)

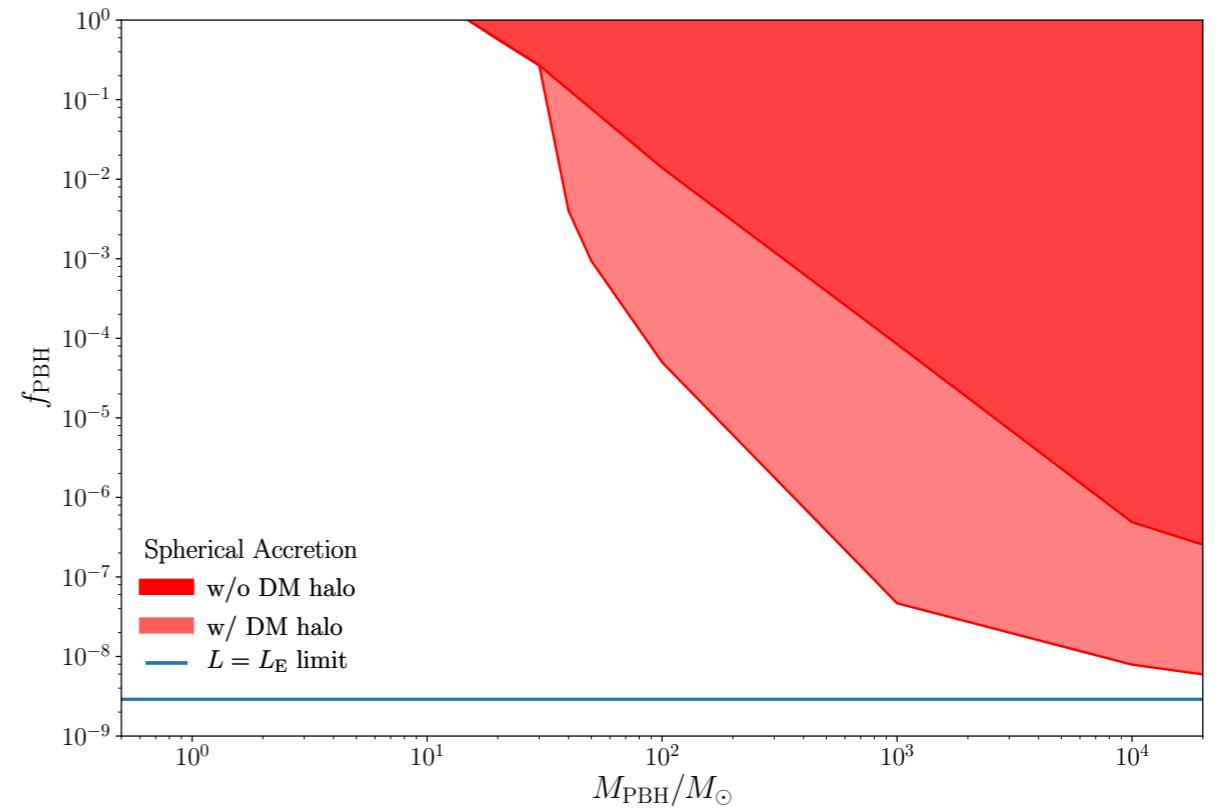
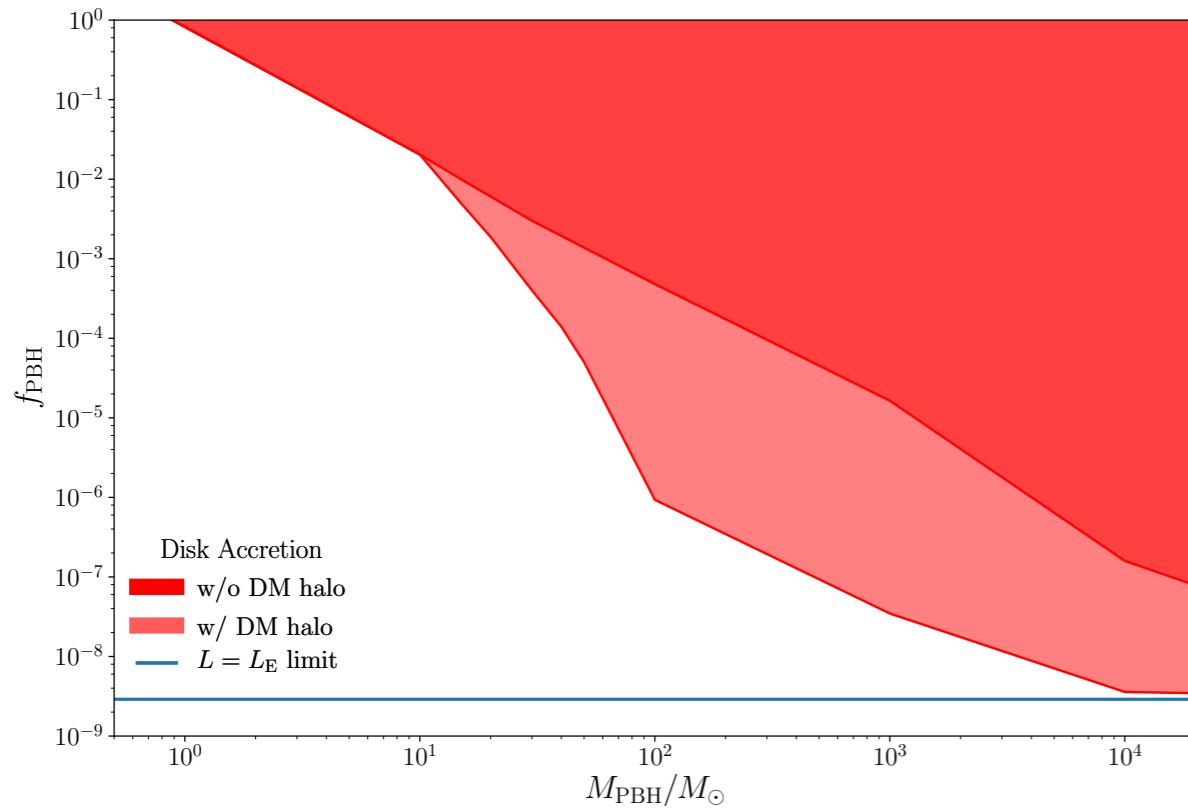
Self-similar Profile: $\rho \propto r^{-9/4}$

(Bertschinger 1985, see also Adamek et al. 2019)

$$\dot{M} \propto \rho_\infty \frac{(GM)^2}{(V^2 + c_s^2)^{3/2}} \rightarrow M \geq M_{\text{PBH}}$$

$$f_{\text{PBH}} \ll 1$$

- Constraints significantly improve...

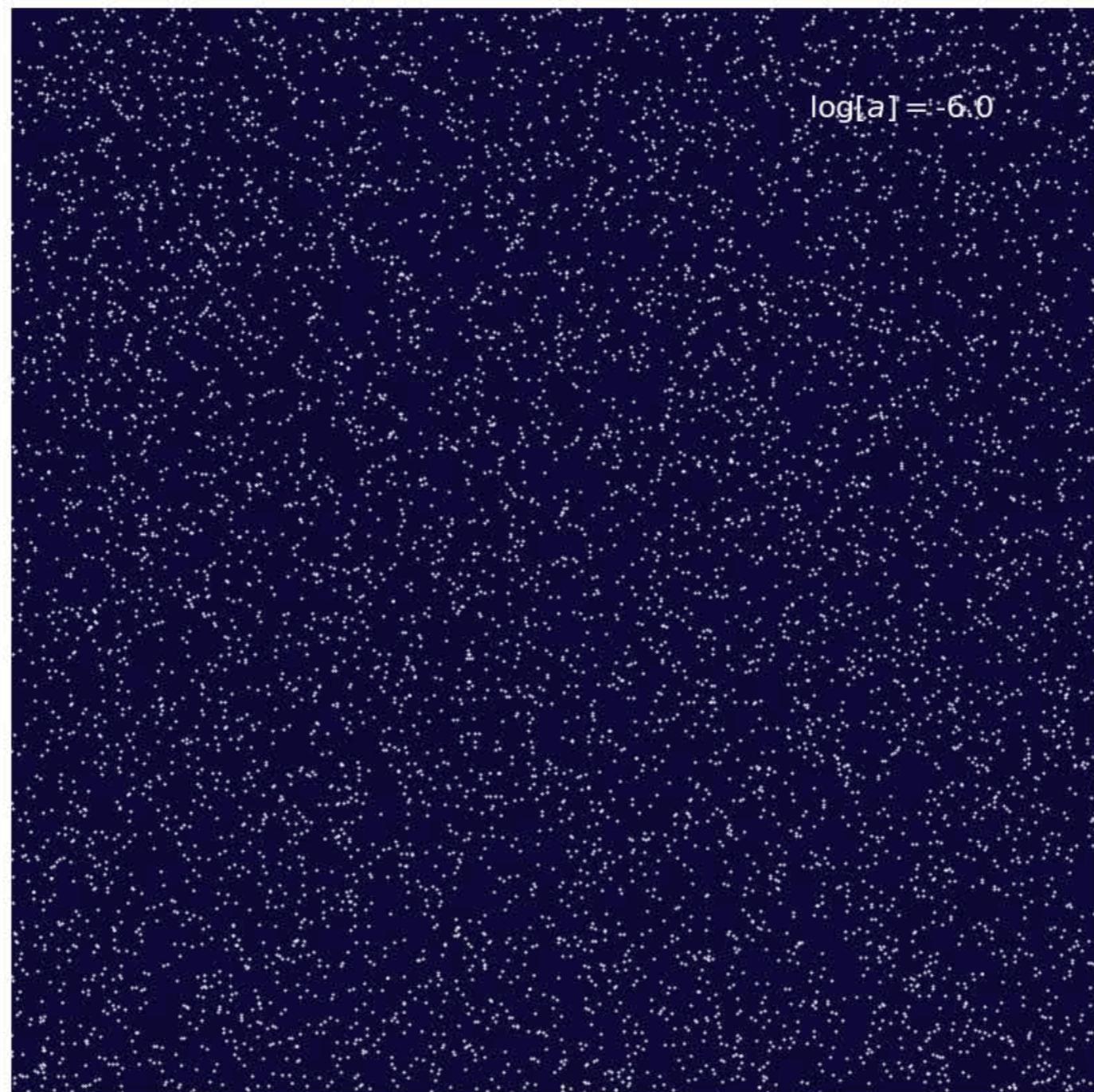


Serpico et al. (2020)

...but requires an additional assumption about dark matter

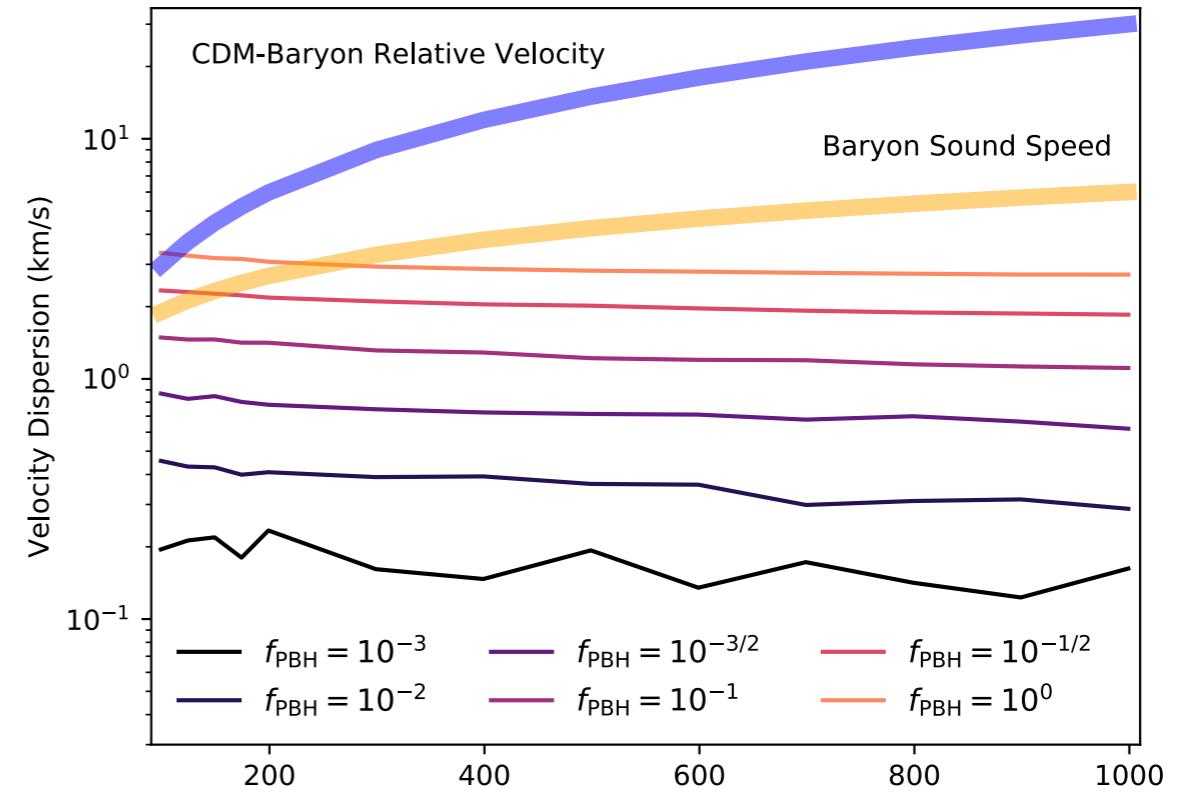
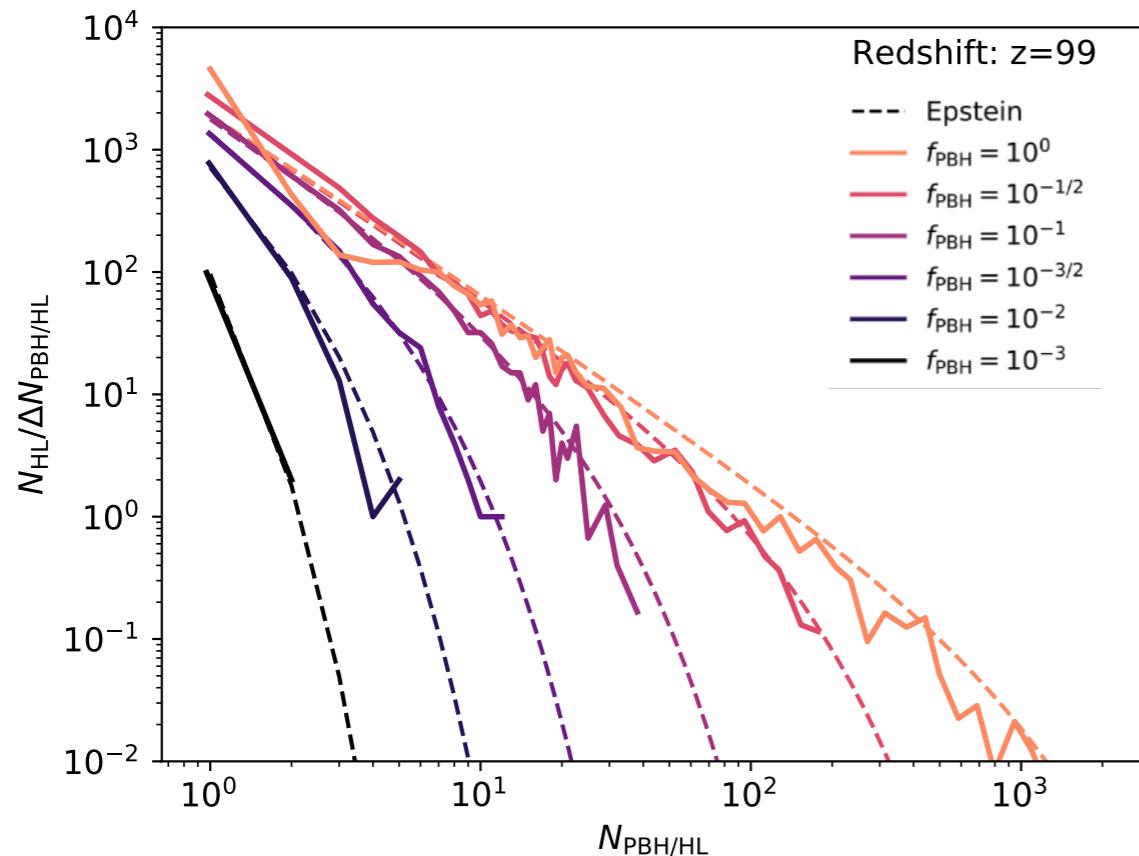
$$f_{\text{PBH}} \sim 1$$

- PBHs are common, and interact with each other gravitationally



$$f_{\text{PBH}} \sim 1$$

- Halos composed of many PBHs form



Inman and Ali-Haïmoud (2019)

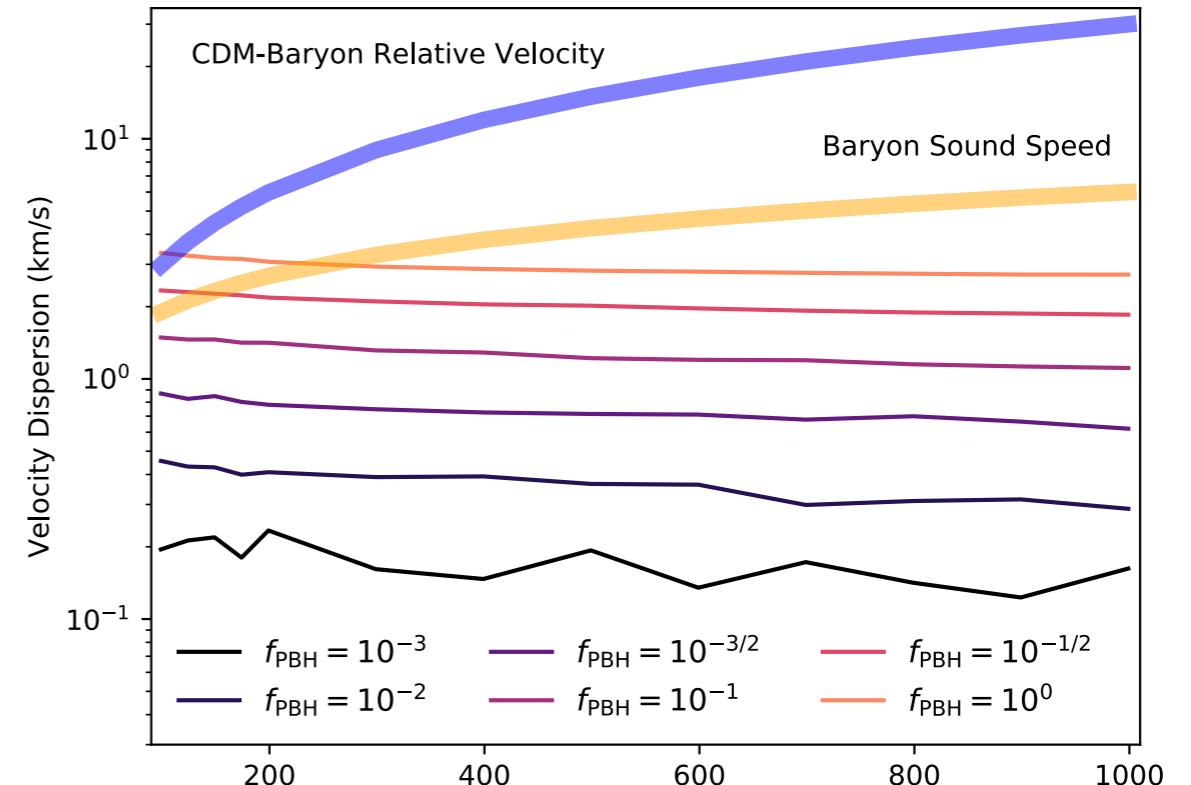
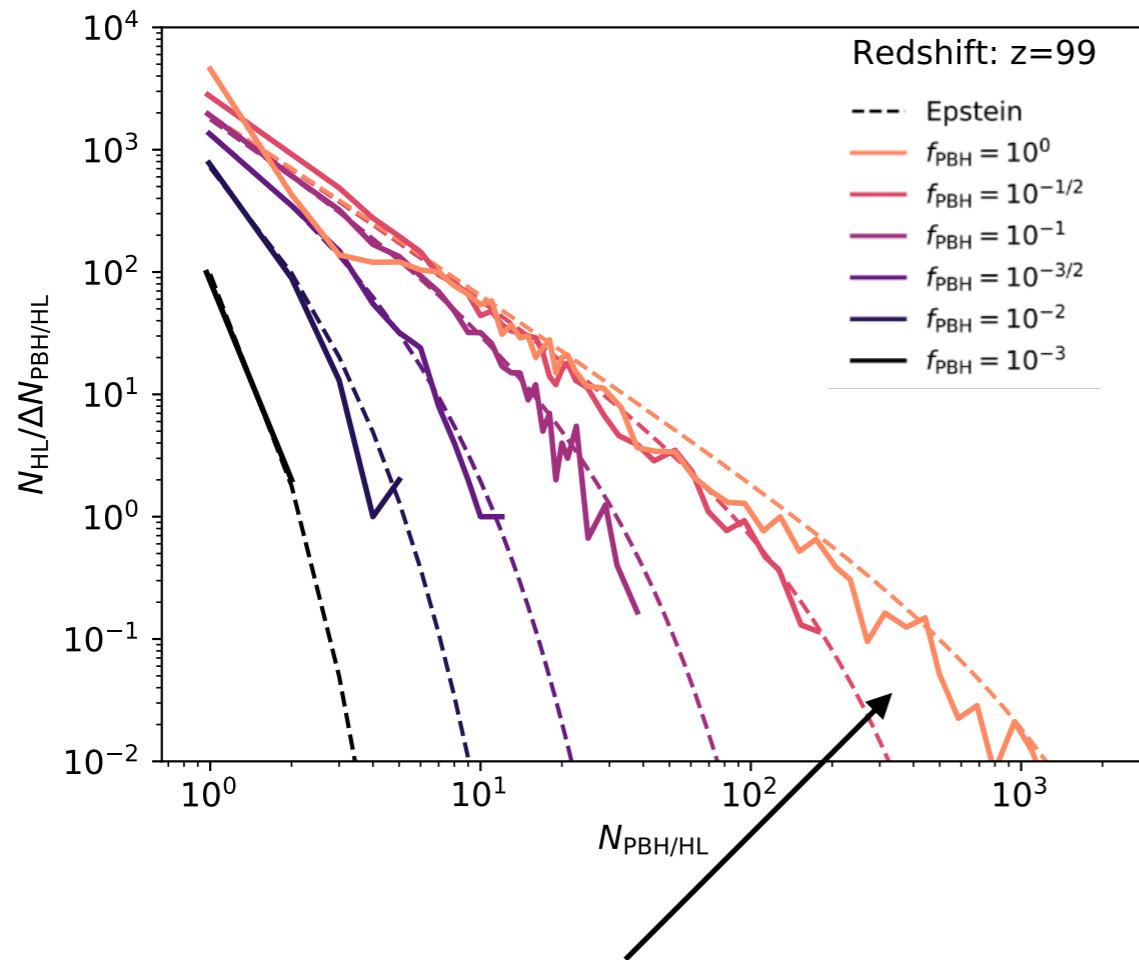
$$N_{\text{HL}}(N) = \frac{N_{\text{PBH}}}{N} \frac{\delta_*}{1 + \delta_*} \left(\frac{N}{1 + \delta_*} \right)^{N-1} \frac{\exp \left[-\frac{N}{1 + \delta_*} \right]}{(N-1)!}$$

Epstein (1983), Sheth (1995)

$$\dot{M} \propto \rho_\infty \frac{(GM)^2}{(V^2 + c_s^2)^{3/2}} \rightarrow V, c_s > V_{\text{Vir}}$$

$$f_{\text{PBH}} \sim 1$$

- Halos composed of many PBHs form



Inman and Ali-Haïmoud (2019)

Halos have $M \sim 1000 M_{\text{PBH}}$,
so what about the baryons?

$$\dot{M} \propto \rho_\infty \frac{(GM)^2}{(V^2 + c_s^2)^{3/2}} \rightarrow \rho_\infty, c_s?$$

Gas dynamics - Preliminary

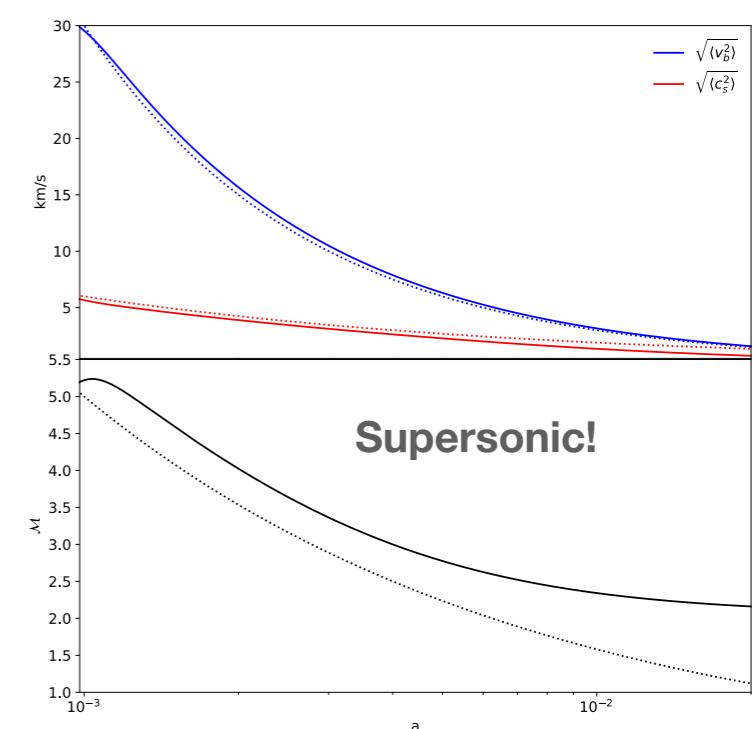
- Ideal gas coupled to CMB via Compton scattering

$$\begin{aligned} \frac{\partial \rho}{\partial t} + \nabla^k (\rho V^k) &= 0 \\ P &= \rho k_B T / (\mu m_{\text{H}}) \\ \frac{\partial \rho V^i}{\partial t} + \nabla^k (\rho V^i V^k + P \delta^{ik}) &= \rho g^k + \rho \Gamma_V(a) (V_{\text{CMB}}^k - V^k) \\ \frac{\partial E}{\partial t} + \nabla^k ((E + P)V^k) &= \rho V^k g^k + \rho V^k \Gamma_V(a) (V_{\text{CMB}}^k - V^k) + \frac{P}{(\gamma - 1)T} \Gamma_T(a) (T_{\text{CMB}} - T) \\ \Gamma_V(a) &= \frac{1}{2} \frac{m_e}{\mu m_{\text{H}}} \Gamma_T(a) \\ \mu(a) &= \frac{1 + 4f_{\text{He}}}{1 + x_e(a) + f_{\text{He}}} \\ \Gamma_T(a) &= \frac{x_e(a)}{1 + x_e(a) + f_{\text{He}}} \\ T_{\text{CMB}} &= 2.725(1 + z) \text{ K} \end{aligned}$$

Relative Velocity Effect: Gas moves w.r.t to CDM (Tseliakhovich and Hirata 2010)

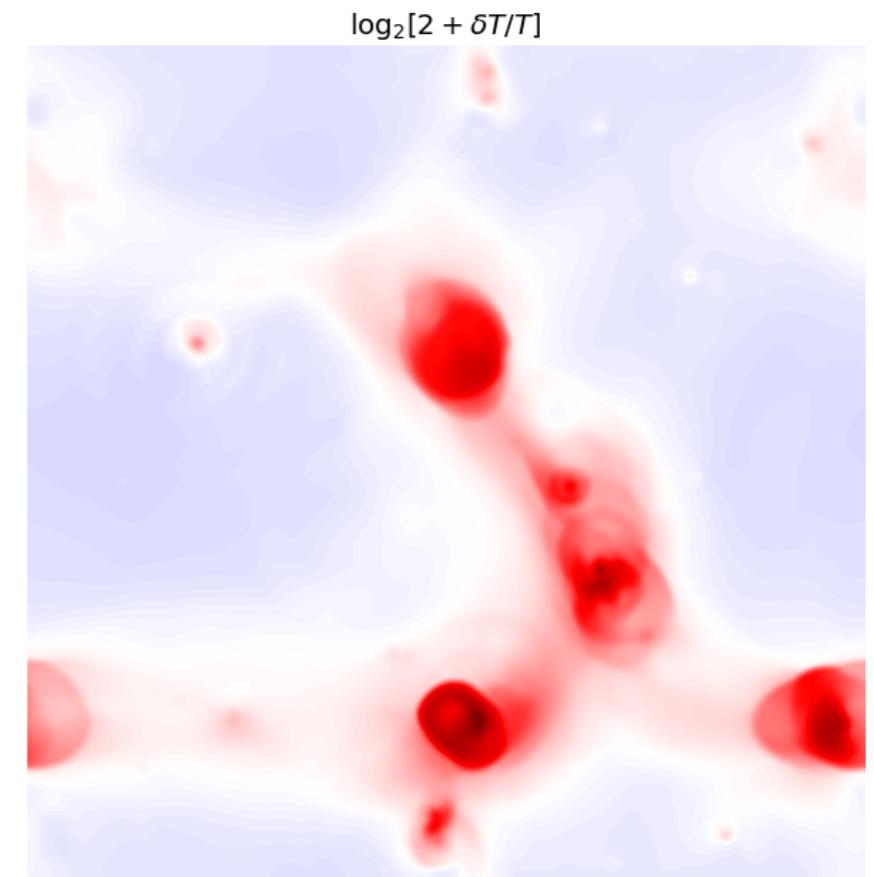
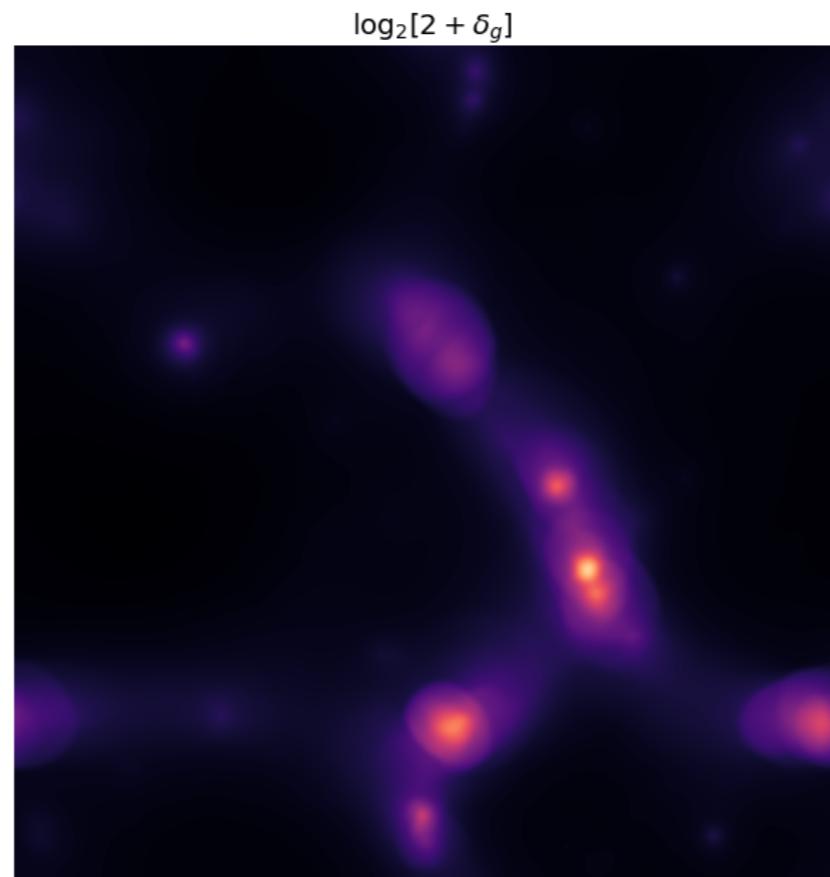
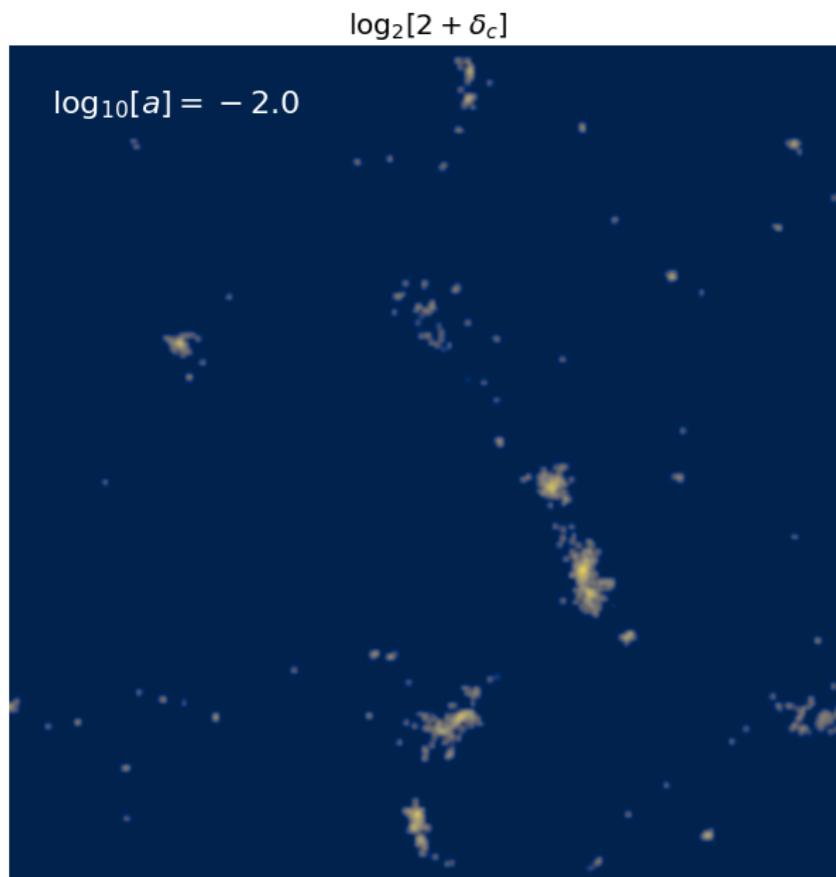
Ionization Fraction: currently use background value... but working on perturbed x_e

$$\Gamma = \frac{8\pi^2}{45} \frac{\sigma_T k_B T_{\text{CMB}}^4}{m_e \hbar^3 c^4}$$



Gas dynamics - Preliminary

- $f_{\text{PBH}} \sim 1$



$$\dot{M} = 4\pi\lambda\rho_\infty \frac{(GM)^2}{(V^2 + c_s^2)^{3/2}} \rightarrow \rho_\infty, c_s?$$

Conclusions

- PBH dark matter significantly changes the structure formation history of the Universe
- CMB constraints can be substantially improved by taking halo formation into account
- Potential improvements by including baryons in the simulations
- Other consequences of early halos - star formation, magnetogenesis,...?

Thank you for your time!

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