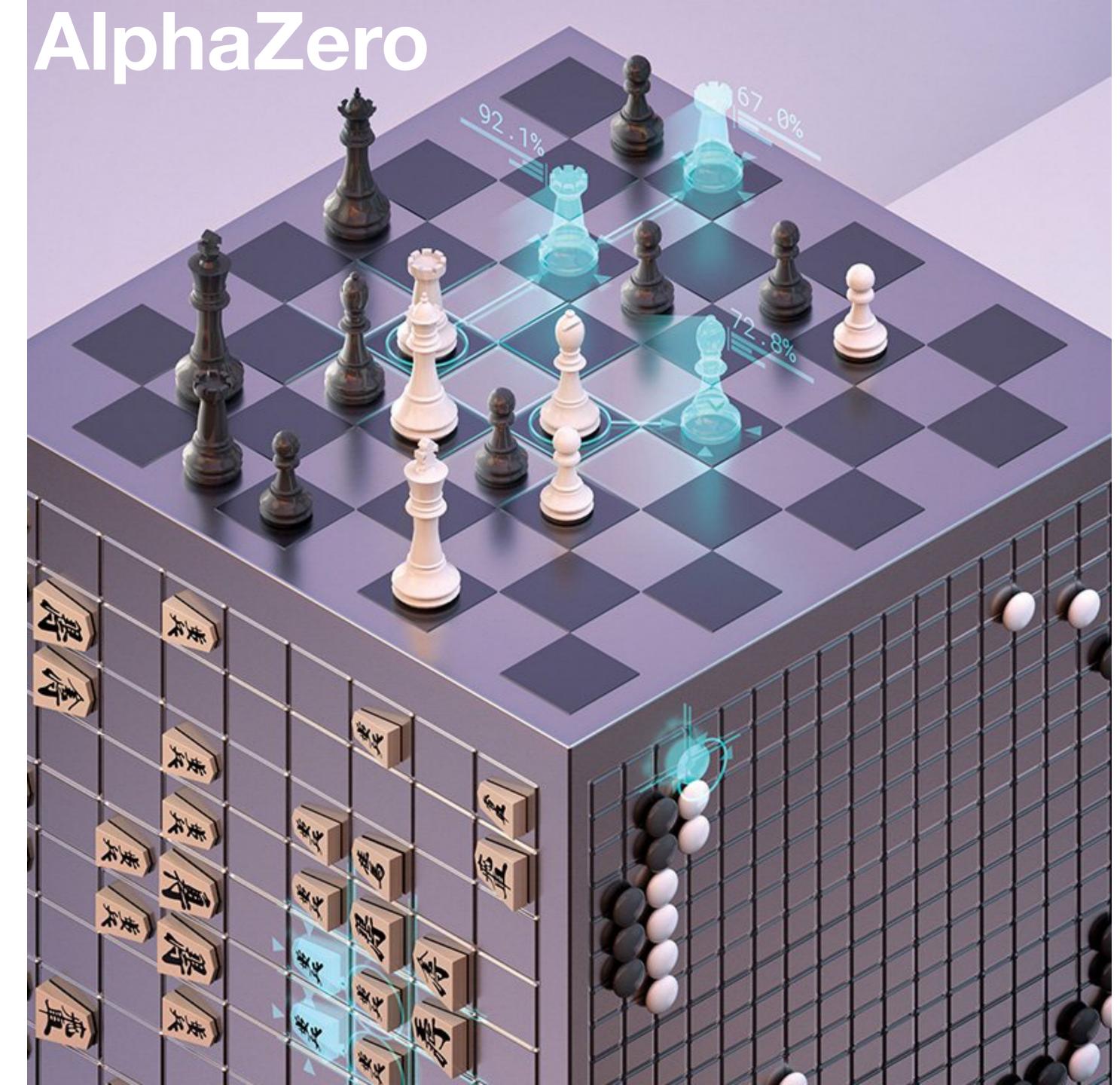
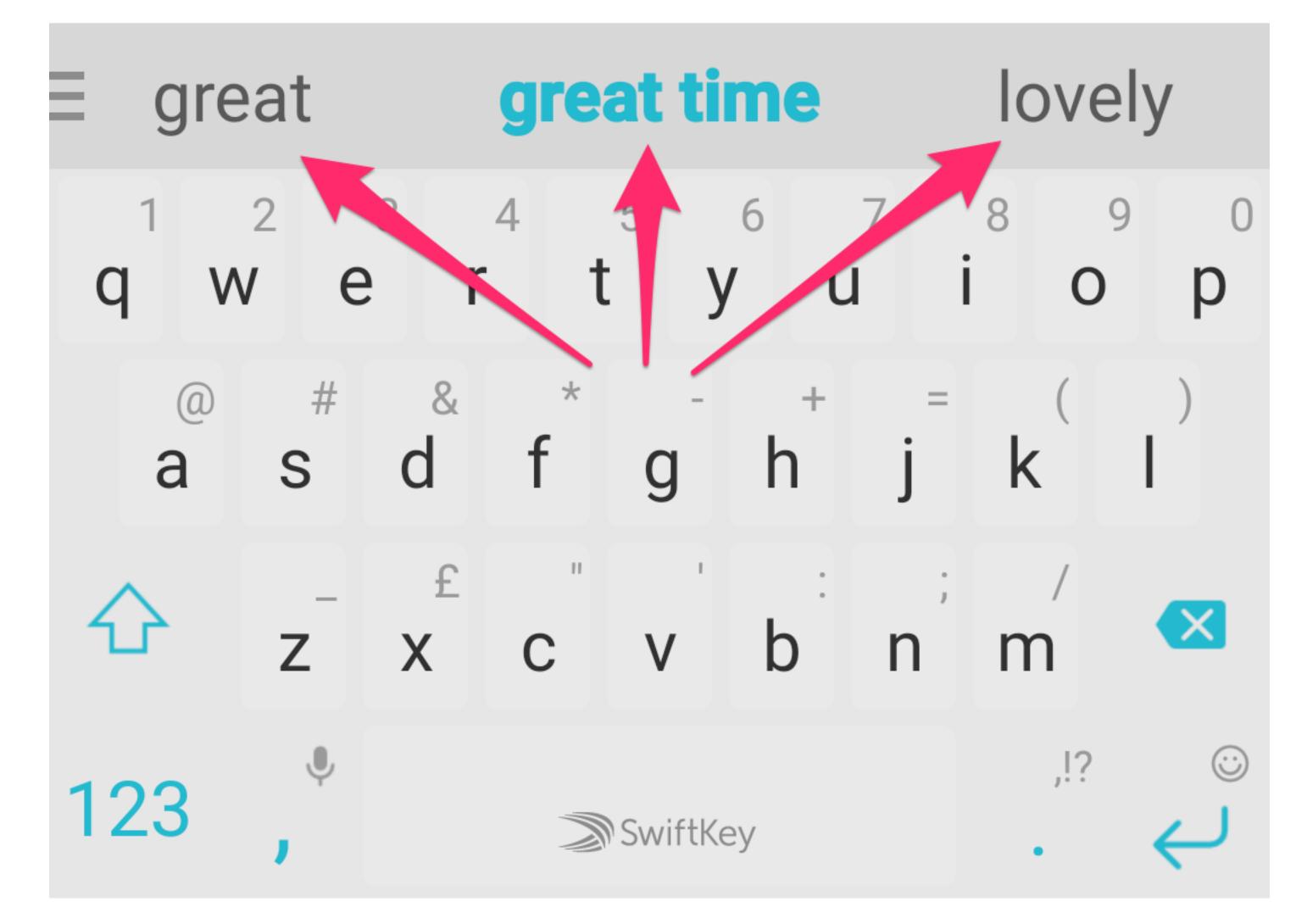
# Machine learning for people who already know all the math.

Anton de la Fuente



#### I had such a





# Google

Q How to X how to 意味 Q how to use Q how to 歌詞 Q how to pronounce Q how to build a girl Q how to basic Q how to be single Q how to avoid a climate disaster Q Google 検索 I'm Feeling Lucky 不適切な検索候補の報告

# Google

#### Q どうやって

- Q どうやって
- Q どうやって 英語
- Q どうやって死にてえ マイキー
- Q どうやって生きていこう
- Q どうやって 韓国語
- Q どうやって戦えばいいんだ
- Q どうやってここまで
- Q どうやって学校に行きますか 英語

Google 検索

I'm Feeling Lucky

不適切な検索候補の報告



# Written by AI 人工知能が書いた

The best kind of ramen is the one you can eat while doing your taxes. At least, that's what the government's recently published "Ramen: The Global Ramen Experiment" suggests.

Next, I will tell you about string theory. String theory is a mathematical model of our universe, a theory that describes not only how our spacetime is constructed, but how it is built into the fabric of reality.









### an armchair in the shape of an avocado アボカドの形をした椅子





















### a tapir made of accordion アコーディオンで作った獏さん







- How is playing chess and writing text curve fitting?
- What do these functions look like?  $\bullet$
- Why don't we overfit or get stuck in a local minimum?

### Outline

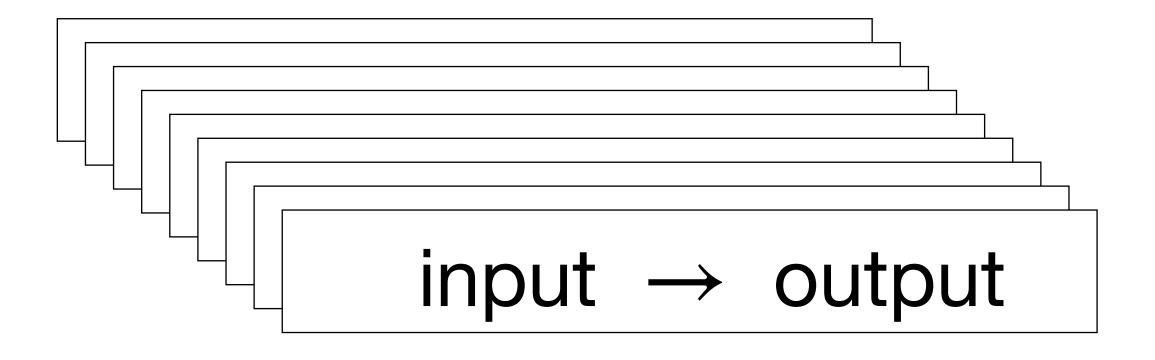
- How is playing chess and writing text curve fitting?
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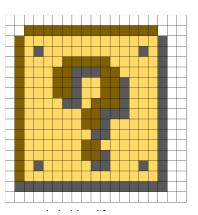
### Outline

# Goal of machine learning

#### Training data 学習データ

#### New input 新しい入力 →





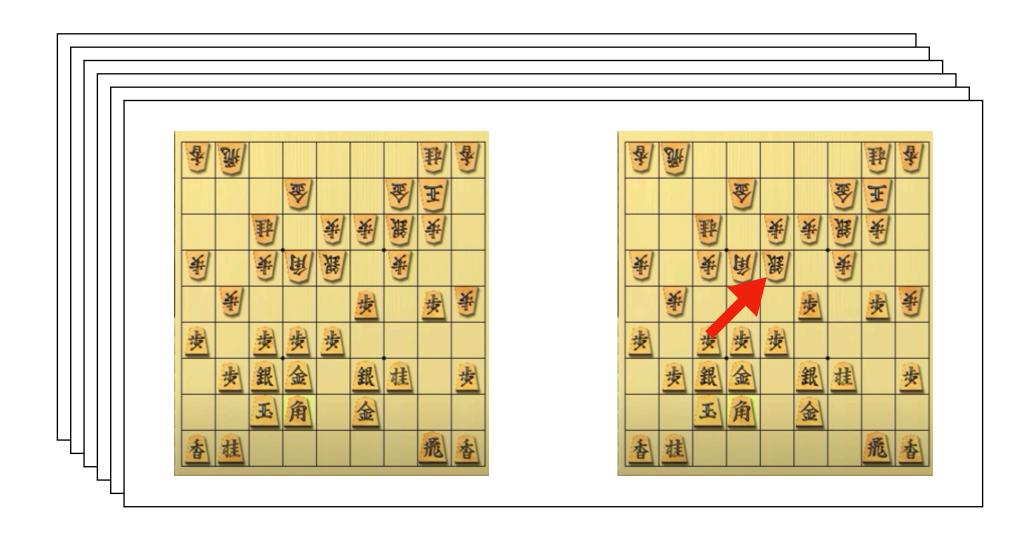
### Function domain and range

### $Data = \{(x_{\alpha}, y_{\alpha})\}$

# $p(x, \theta) \in \mathbb{R}^{M' \times N'}$ probability distribution parameters $\theta$

# $\begin{aligned} x_{\alpha} \in \mathbb{R}^{M \times N} \\ y_{\alpha} \in \mathbb{R}^{M' \times N'} \text{ one-hot} \end{aligned}$

# Chess · Shogi 将棋 · Go 碁

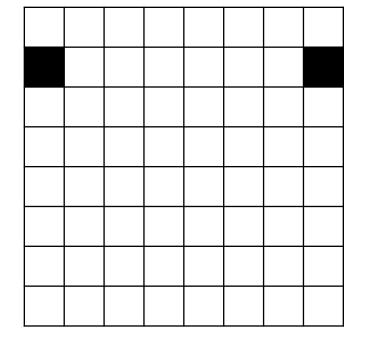


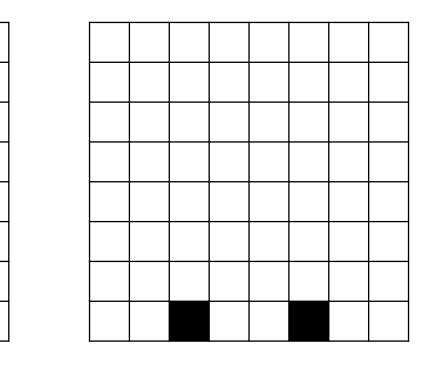
#### (Position, move made by winning player) (駒の位置、勝った棋士の次の一手)

#### 44 million games 44百万の試合

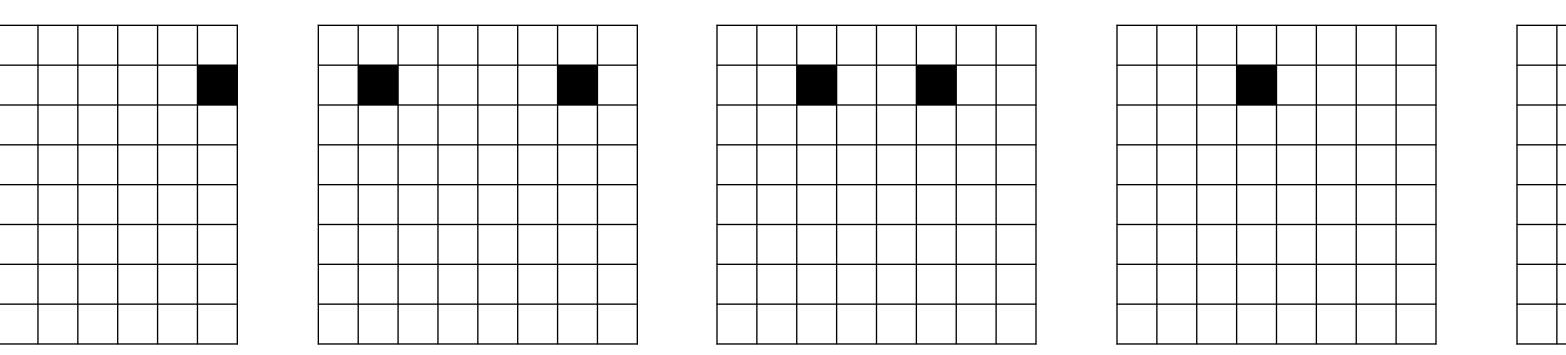
# Chess input space $x \in \mathbb{R}^{8 \times 8 \times (6+6+1)}$

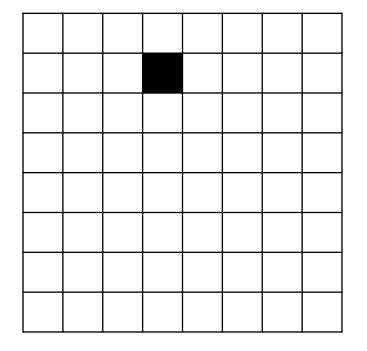






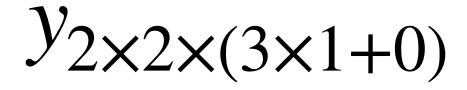
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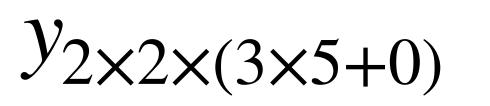


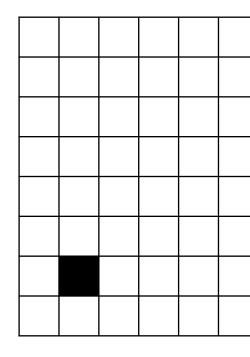


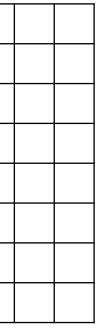


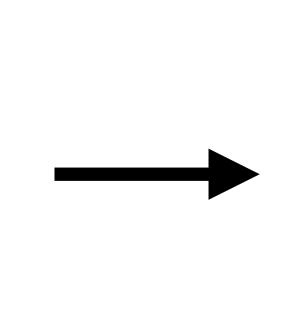
# Chess output space $y \in \mathbb{R}^{8 \times 8 \times (8 \times 7 + 8)}$

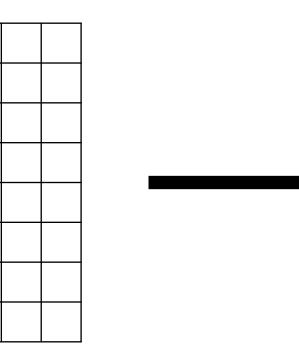


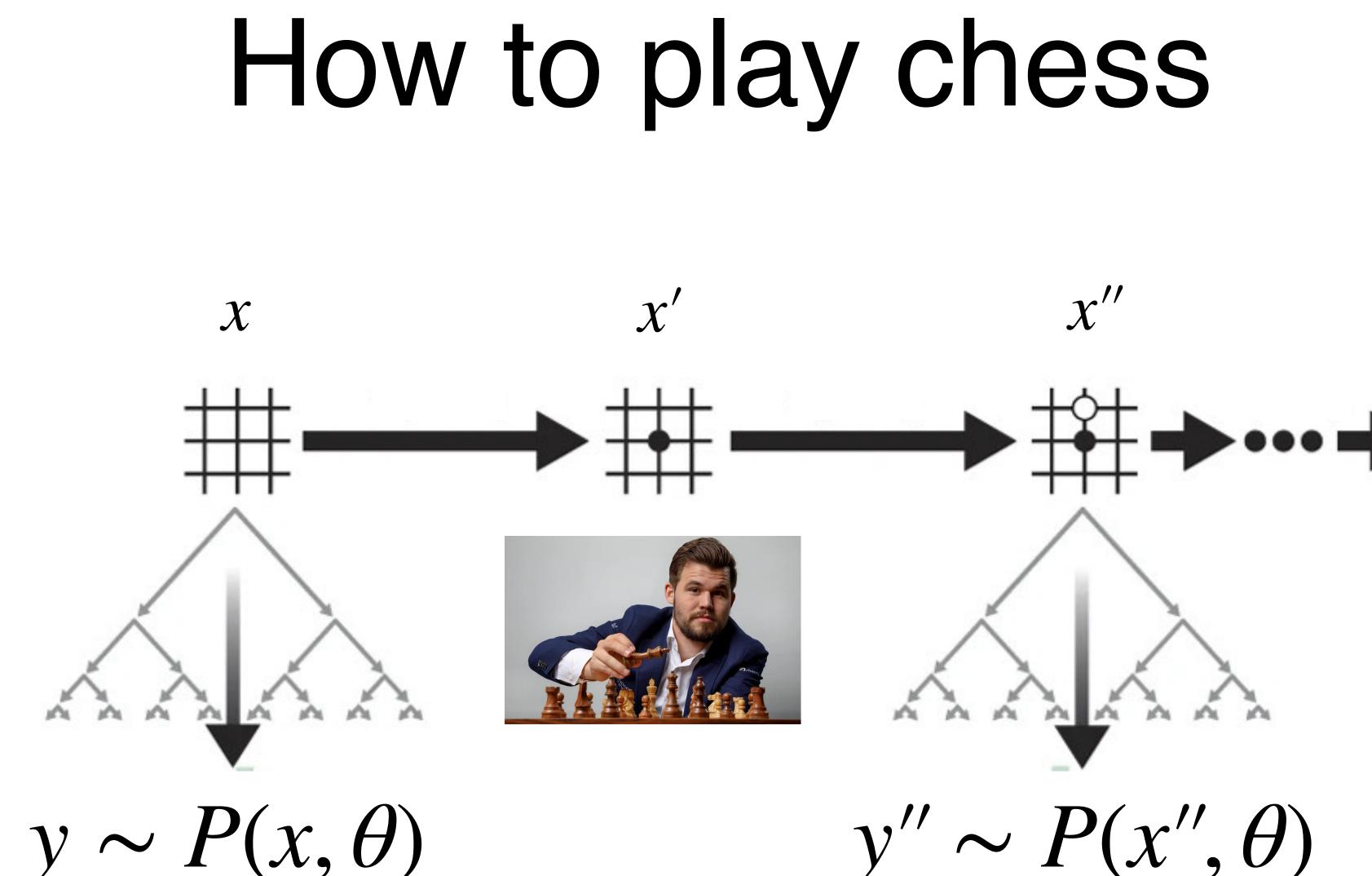




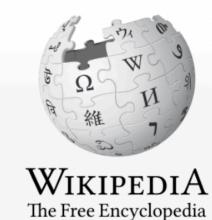




# Text-writing training data



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#### Kavli Institute for the Physics and Mathematics of the Universe

From Wikipedia, the free encyclopedia

The Kavli Institute for the Physics and Mathematics of the Universe (IPMU) is an international research institute for physics and mathematics situated in Kashiwa, Japan, near Tokyo. Its full name is "Kavli Institute for the Physics and Mathematics of the Universe, The University of Tokyo Institutes for Advanced Study, the University of Tokyo, Kashiwa, Japan".

The main subjects of study at IPMU are particle physics, high energy physics, astrophysics, astronomy and mathematics. The institute addresses five key questions: "How did the universe begin? What is its fate? What is it made of? What are its fundamental laws? Why do we exist?"<sup>[1]</sup>

- (The Kavli Institute for, the)
- (The Kavli Institute for the, Physics)
- (The Kavli Institute for the Physics, and)

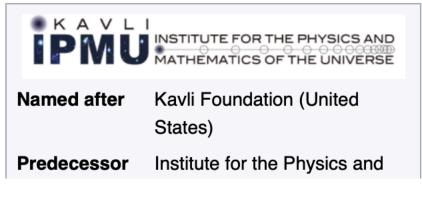
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#### Kavli Institute for the Physics and Mathematics of the Universe

Q



#### • Next word prediction, 600 Billion words 次の単語を予測、6千億の単語

# Encode words as vectors R 50000

The =  $(1,0,0,0,\cdots)$ is =  $(0, 1, 0, 0, \cdots)$ apple =  $(0, 0, 1, 0, \dots)$ Japan =  $(0, 0, 0, 1, \cdots)$ 

> present ation ec S

#### Sentences are a concatenation of words

$$x = \left[ x_{\text{Life}}, x_{\text{is}}, x_{\text{great}}, x_{!}, x_{\text{pad}}, x_{\text{pad}}, \dots, x_{\text{pad}} \right]$$

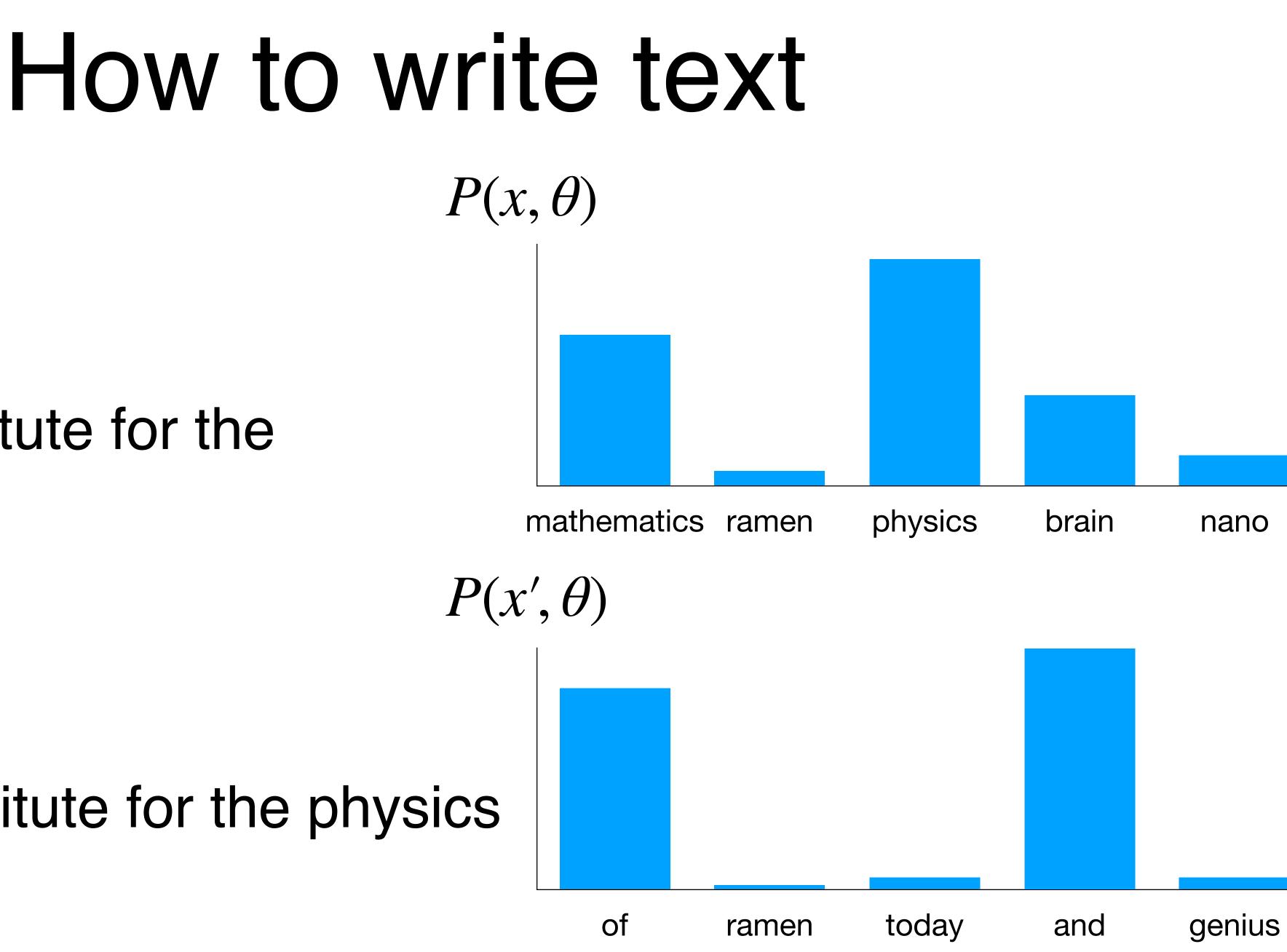
#### input $\in \mathbb{R}^{50000 \times 512}$

#### output $\in \mathbb{R}^{50000}$

probability distribution

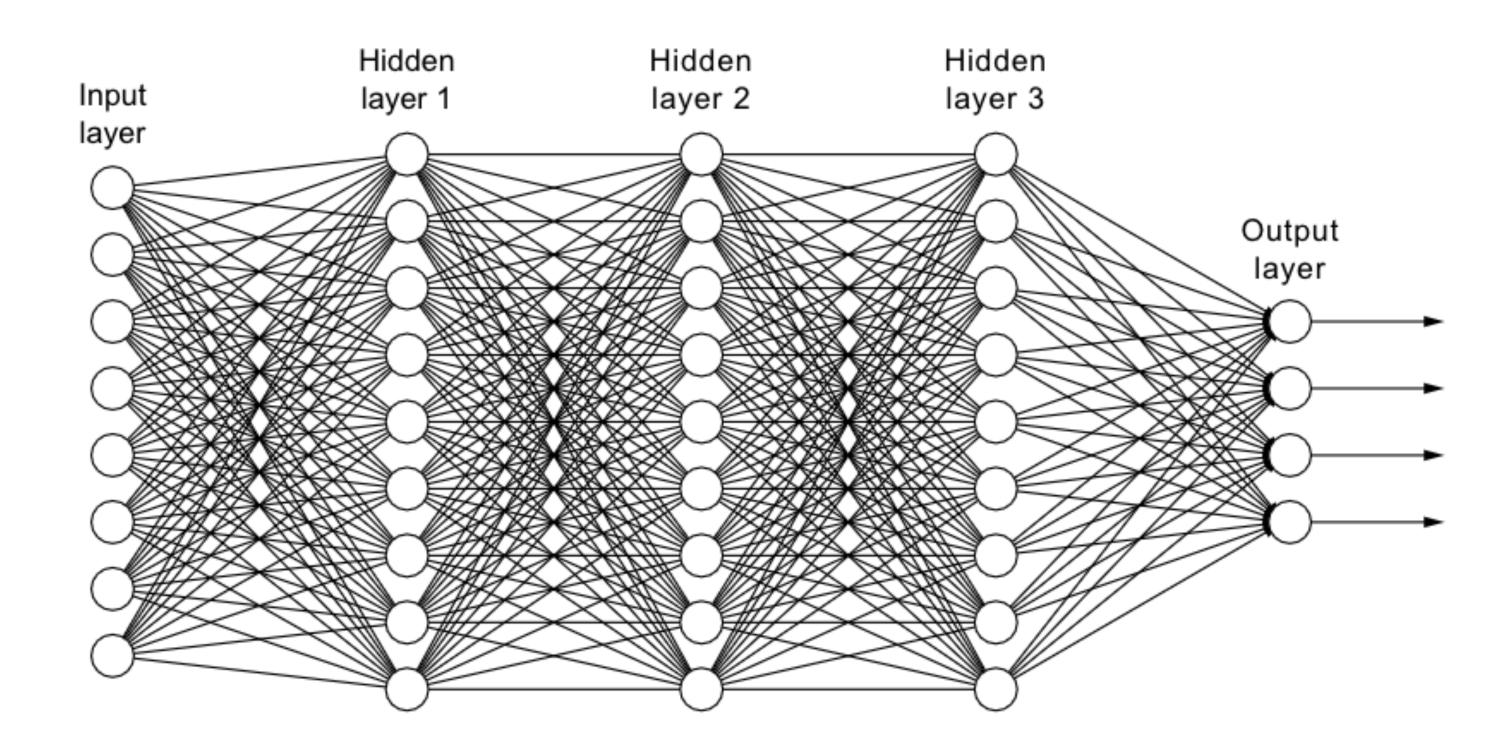
#### x = The Kavli Institute for the

#### x' = The Kavli Institute for the physics

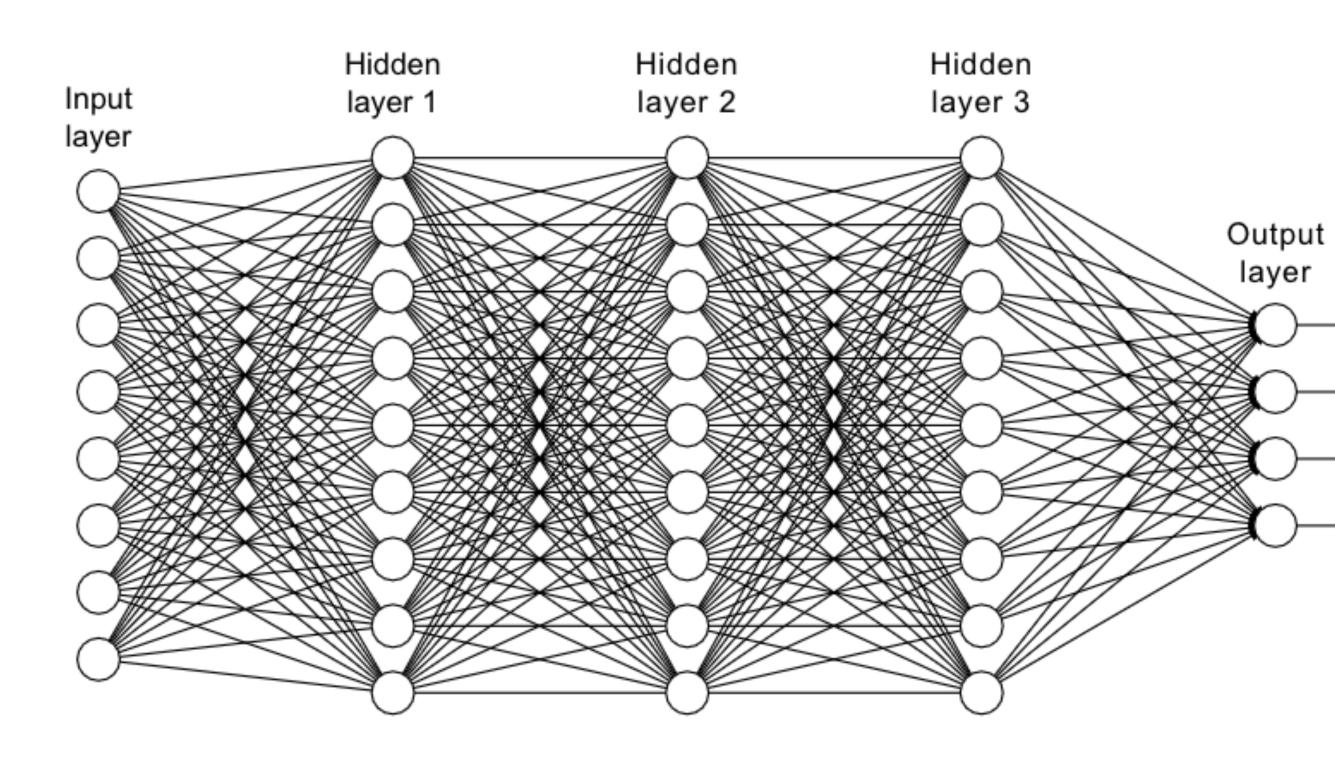


### Outline

- How is playing chess and writing text curve fitting?
- What do these functions look like?
- Why don't we overfit or get stuck in a local minimum?



### Neural Network



### Neural Network

$$h^{1} = \max(0, W^{1}x + b^{1})$$

$$h^{2} = \max(0, W^{2}h^{1} + b^{2})$$

$$h^{3} = \max(0, W^{3}h^{2} + b^{3})$$

$$h^{4} = W^{4}h^{3} + b^{4}$$

$$h^{4}$$

$$p_i = \frac{e^{n_i}}{\sum_j e^{h_j^4}}$$

## Transformers

### $[h_1, h_2, h_3, \cdots, h_{512}]$

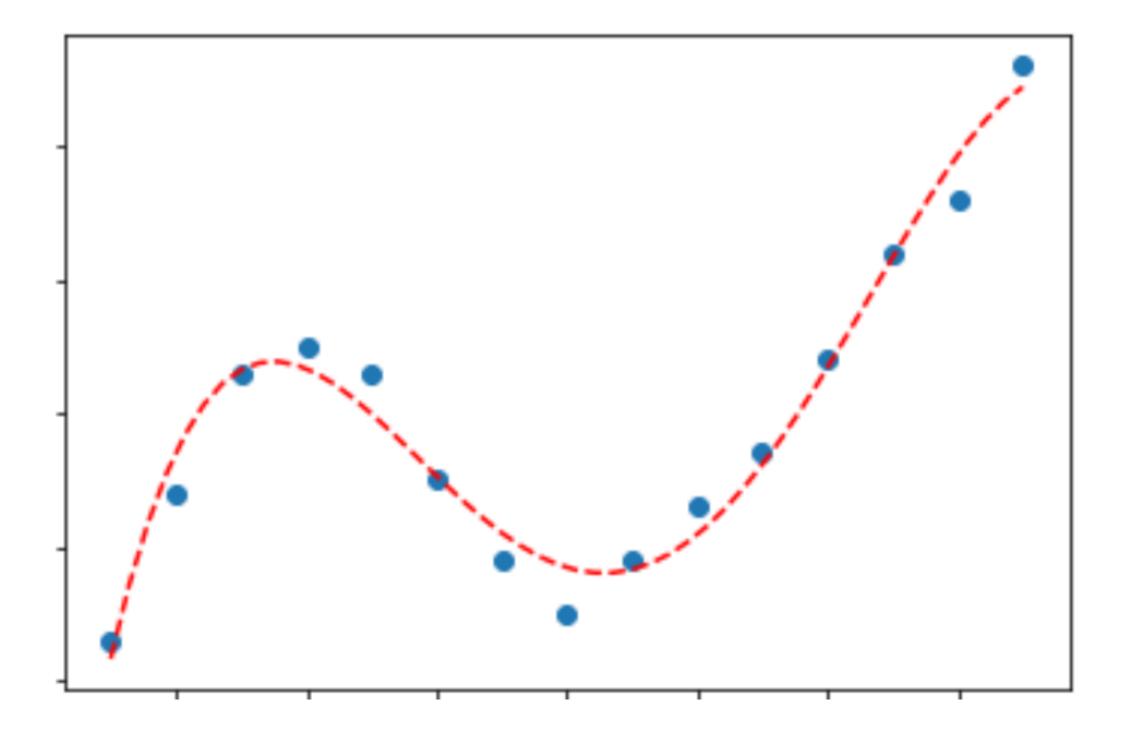
 $h'_i = V \alpha_{ij} h_j$ 

 $h_i \in \mathbb{R}^N$ 

 $\alpha_{ij} = \frac{e^{h_i M h_j}}{\sum_k e^{h_i M h_k}}$ 

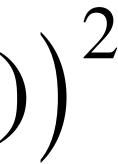
- How is playing chess and writing text curve fitting?
- What do these functions look like?
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### Outline



#### LOSS

# $Loss(\theta) = -\sum_{\alpha}^{N_{data}} (y_{\alpha} - p(x_{\alpha}, \theta))^{2}$ $\alpha = 1$

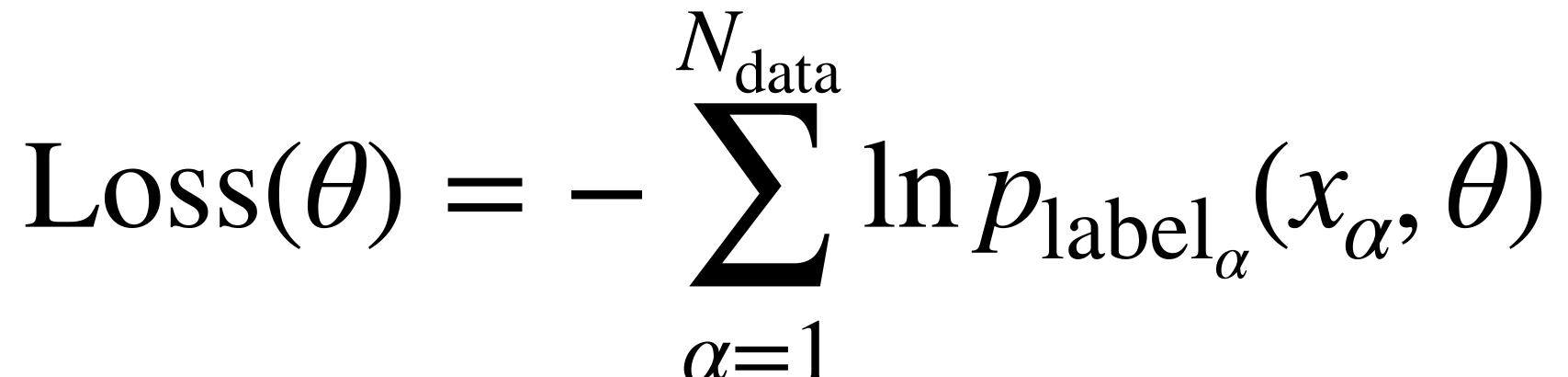


### Data = $\{(x_{\alpha}, y_{\alpha})\}$

### Multiple class loss

# $x_{\alpha} \in \mathbb{R}^{M \times N}$ $y_{\alpha} \in \mathbb{R}^{M' \times N'}$ one-hot $label_{\alpha} = index of non-zero element$

### Multiple class loss

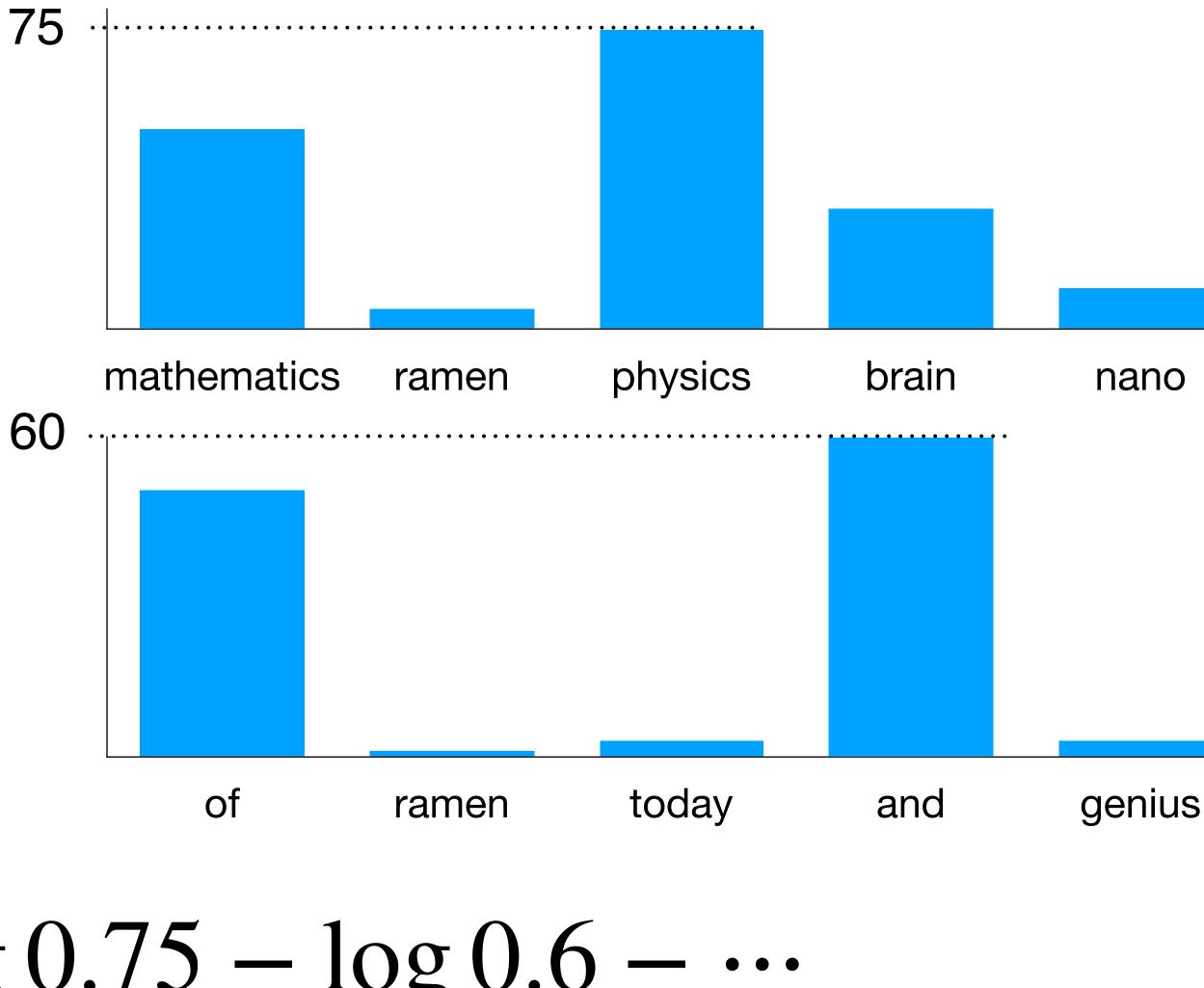


#### The Kavli Institute for the

#### The Kavli Institute for the physics

#### $Loss(\theta) = -\log 0.75 - \log 0.6 - \cdots$

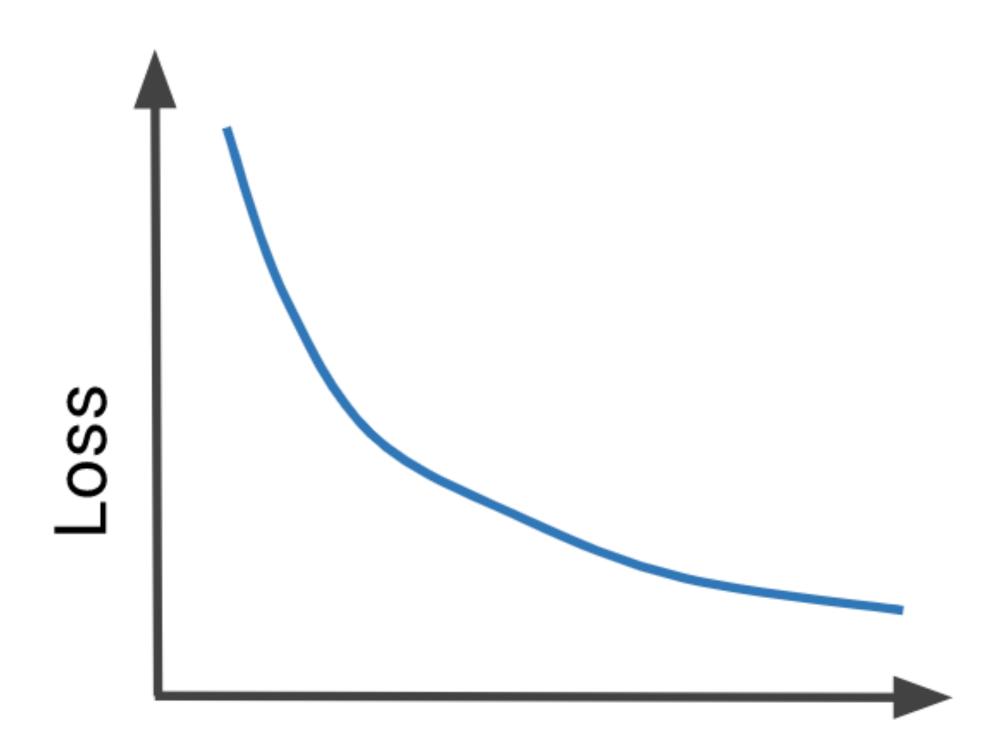
# Example



### Gradient Descent

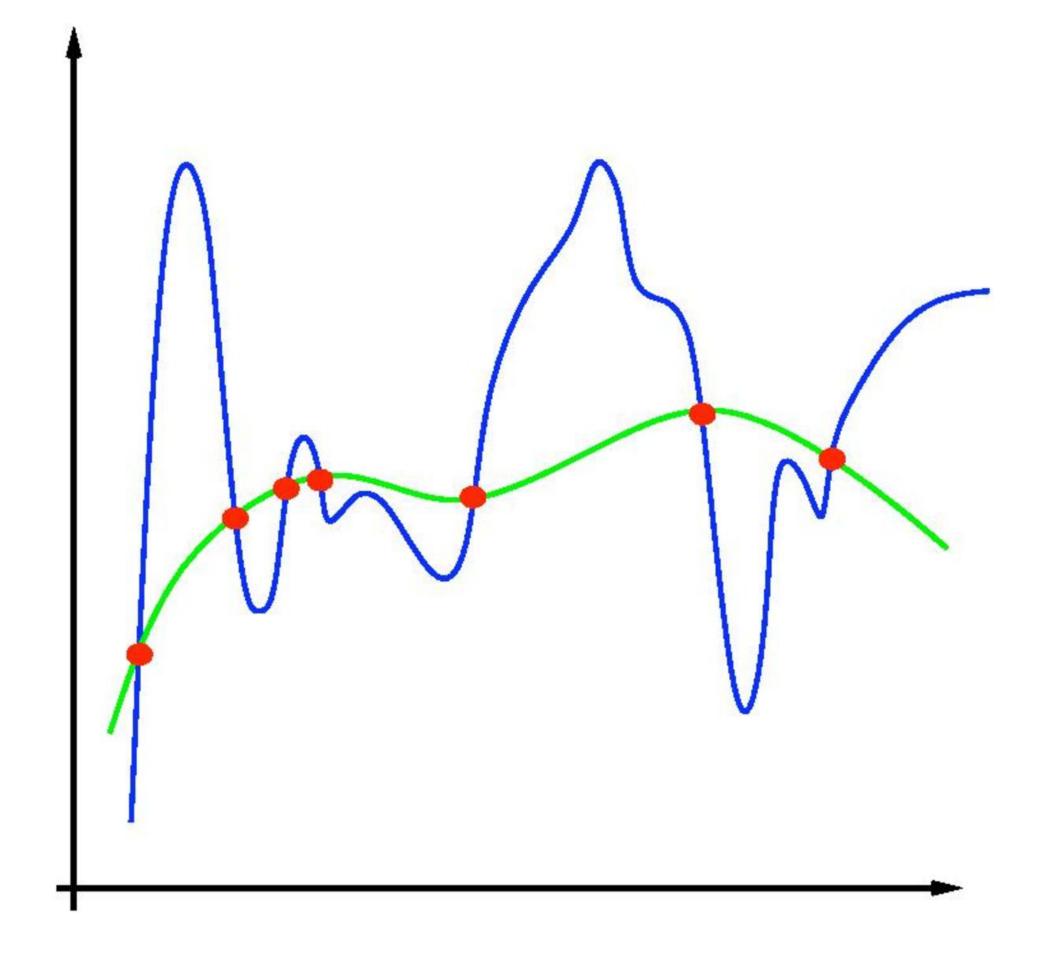
 $\theta = \theta - \epsilon \partial_{\theta} Loss$ 

### Loss decreases during learning (optimization)





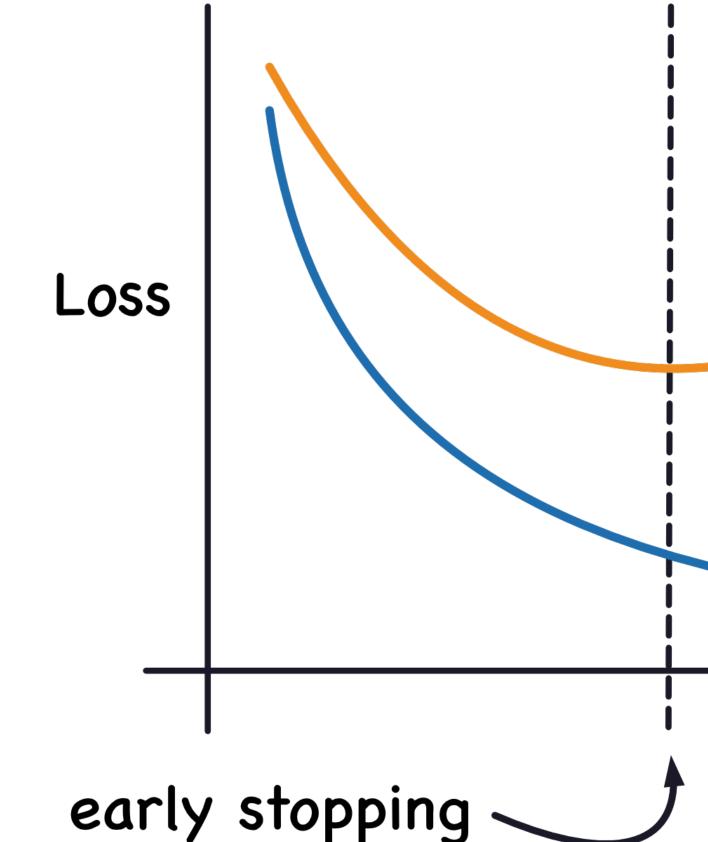




# Overfitting

# Preventing Overfitting

Underfitting



Overfitting

validation

training

Epochs

## Local Minimum?

### $\theta = \theta - \epsilon \partial_{\theta} Loss$

### N<sub>data</sub> $= \theta + \epsilon \partial_{\theta} \sum \ln p_{\text{label}_{\alpha}}$ $\alpha = 1$

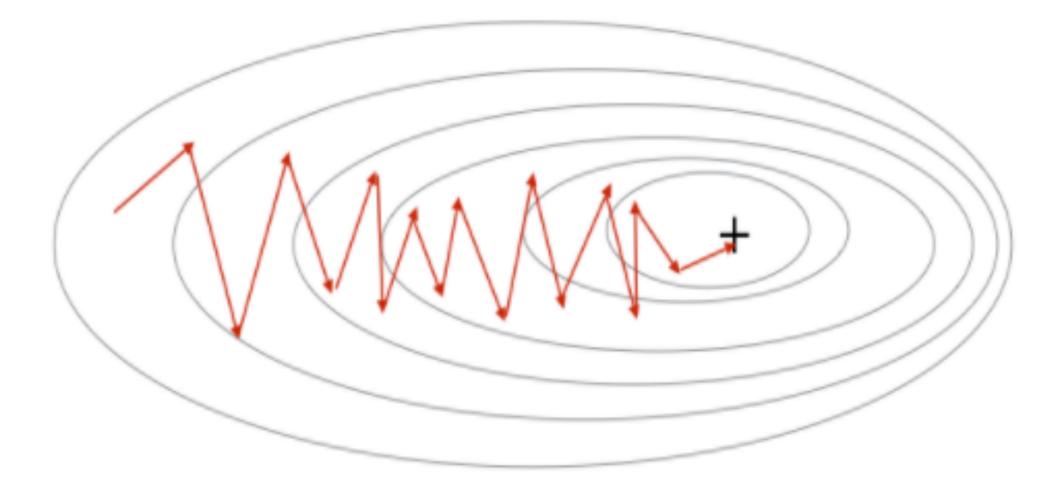
### Stochastic Gradient Descent

 $\theta = \theta - \epsilon \partial_{\theta} Loss$ 

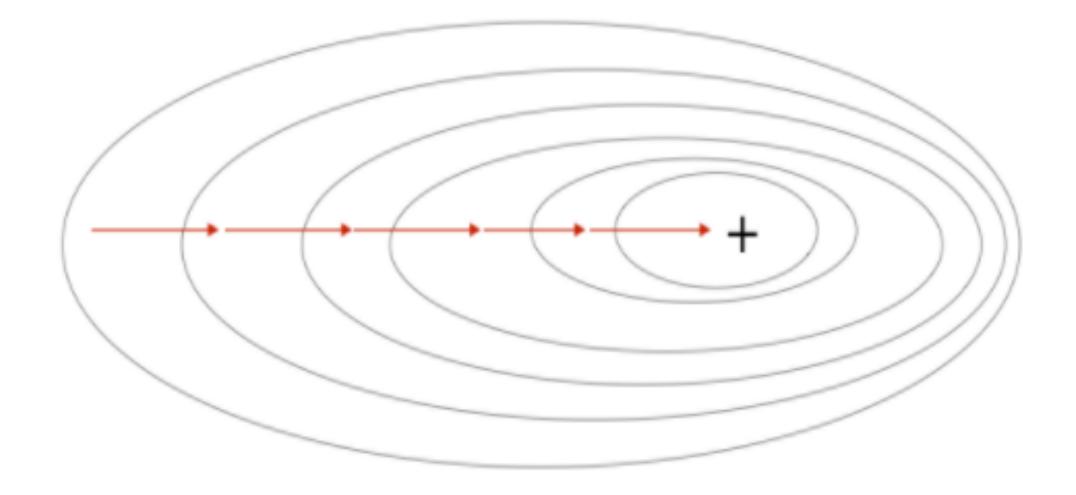
# N<sub>batch</sub> $= \theta + \epsilon \partial_{\theta} \sum \ln p_{\text{label}_{\alpha}}$

## Stochastic Gradient Descent

#### Stochastic Gradient Descent



#### Gradient Descent

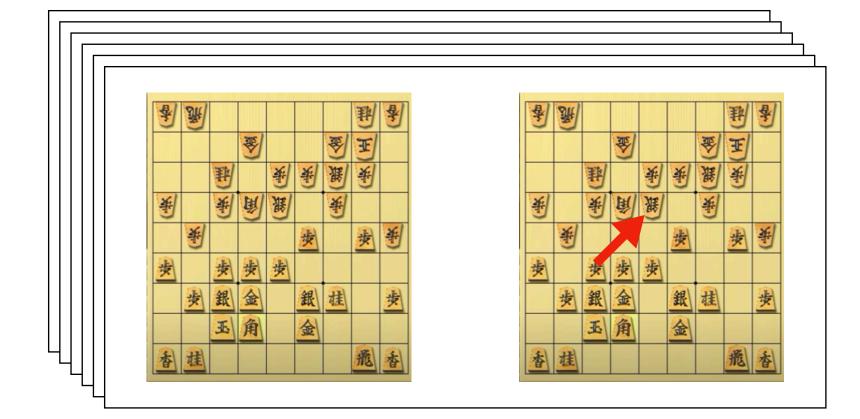


- How is playing chess and writing text curve fitting?
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### Outline

## Reinforcement learning 強化学習

#### Self play 自分と対戦



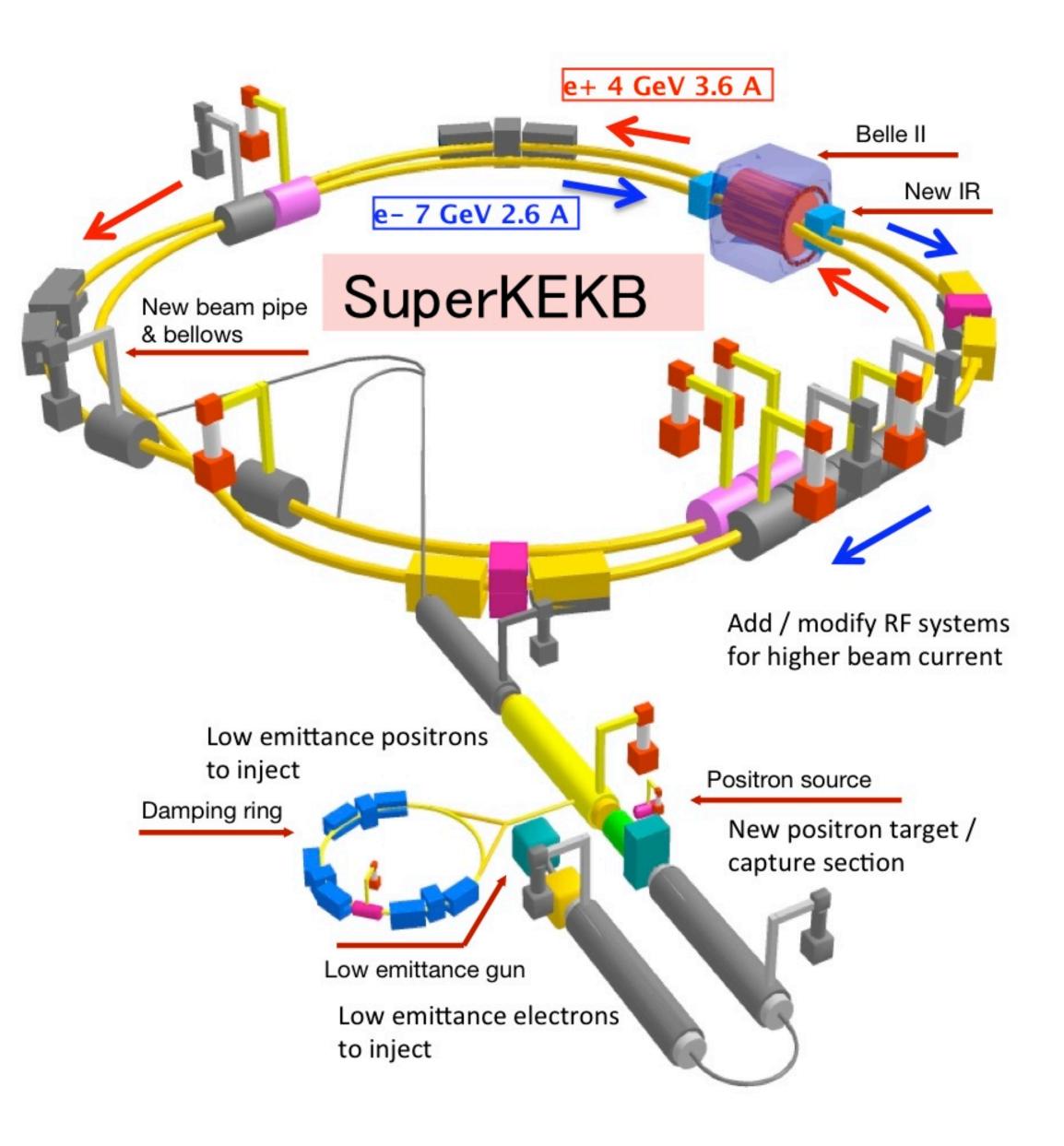
(Position, move made by winning player) (駒の位置、勝った棋士の次の一手)

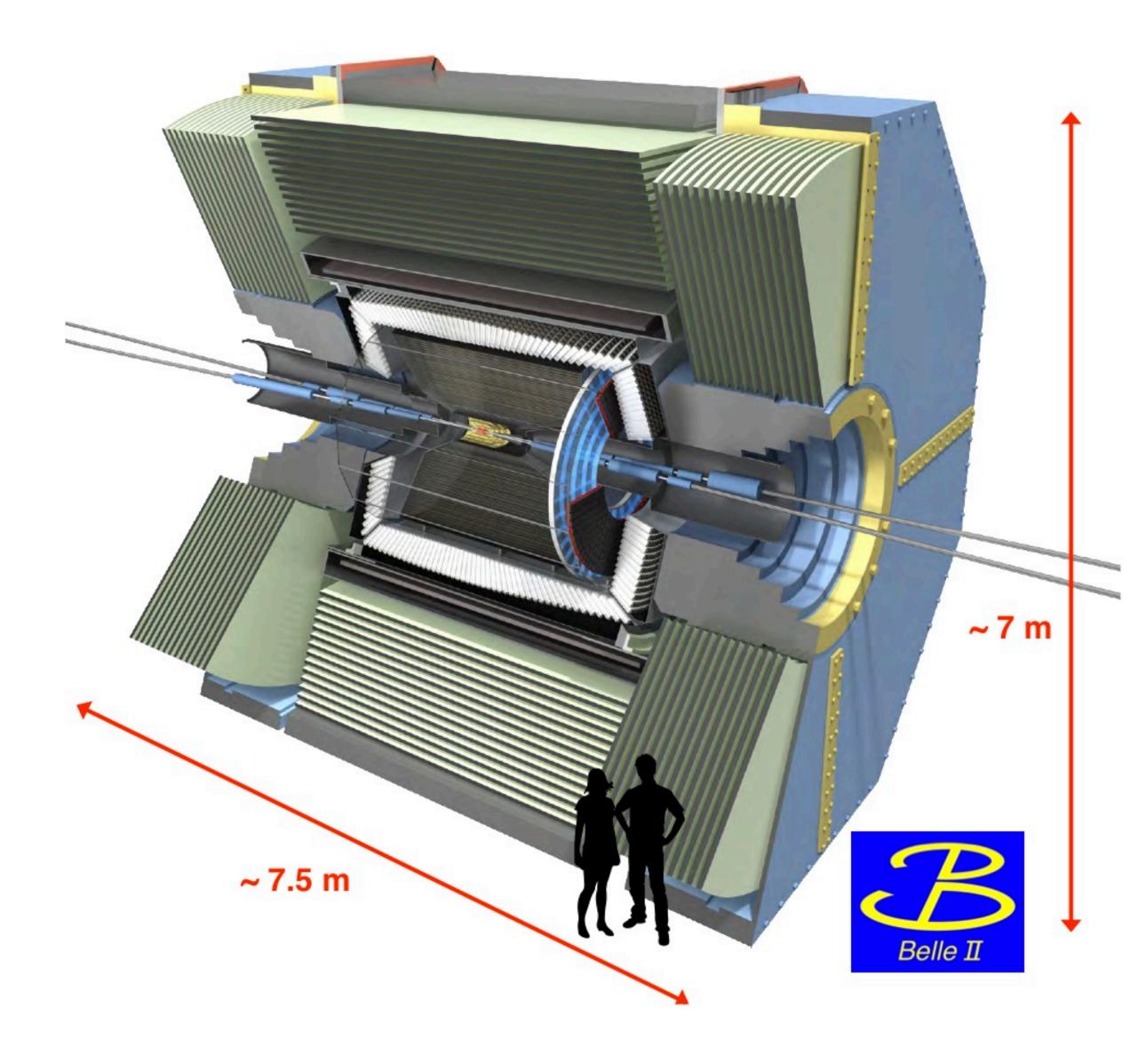
→ Learn 学び

#### Repeat 繰り返す

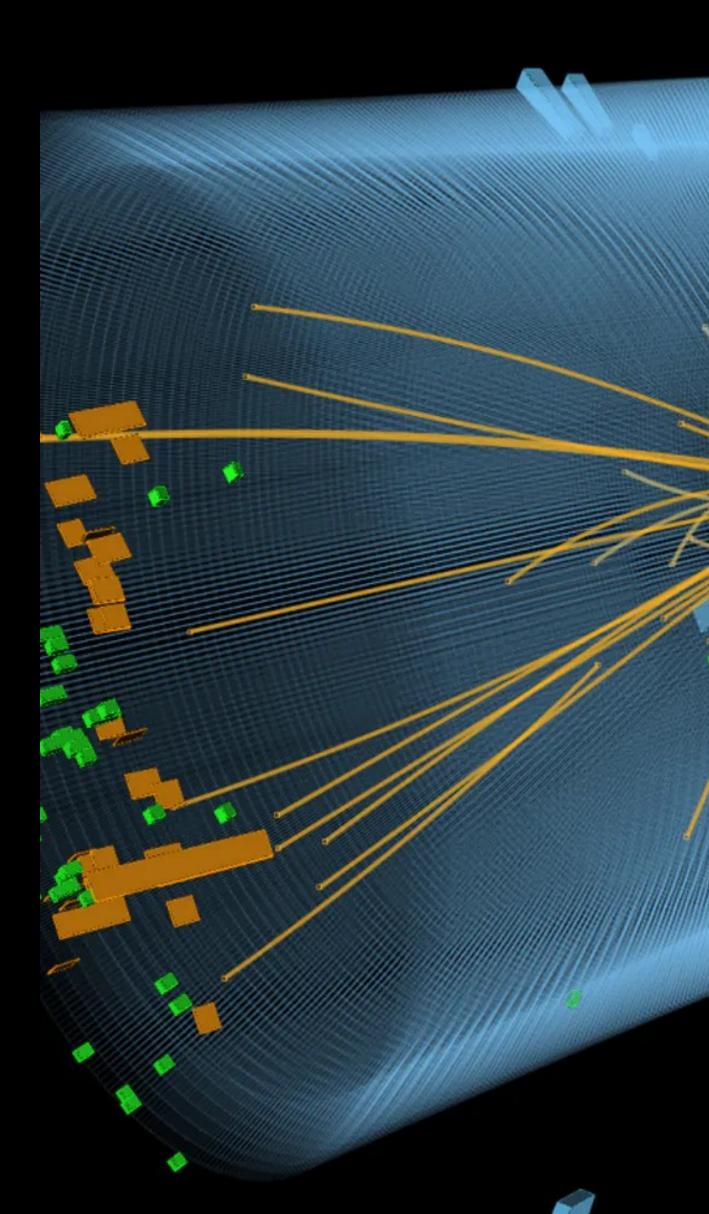
### Curve fitting inside a loop

generate data  $\rightarrow$  curve fit  $\rightarrow$  generate data  $\rightarrow$  curve fit  $\rightarrow \cdots$ 





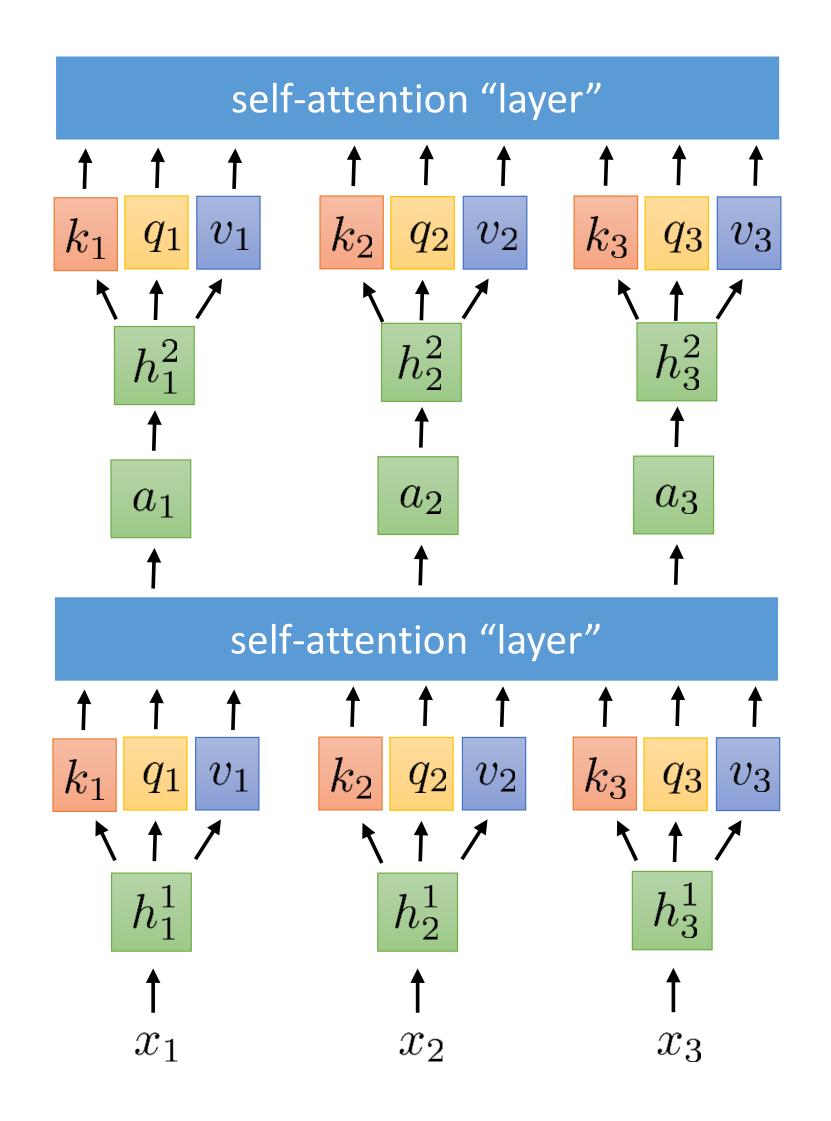
#### (particle, p, $\cos \theta$ ) $\longrightarrow$ detector response (PID variables)



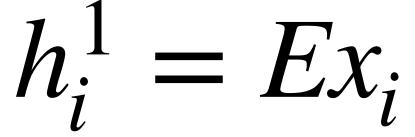


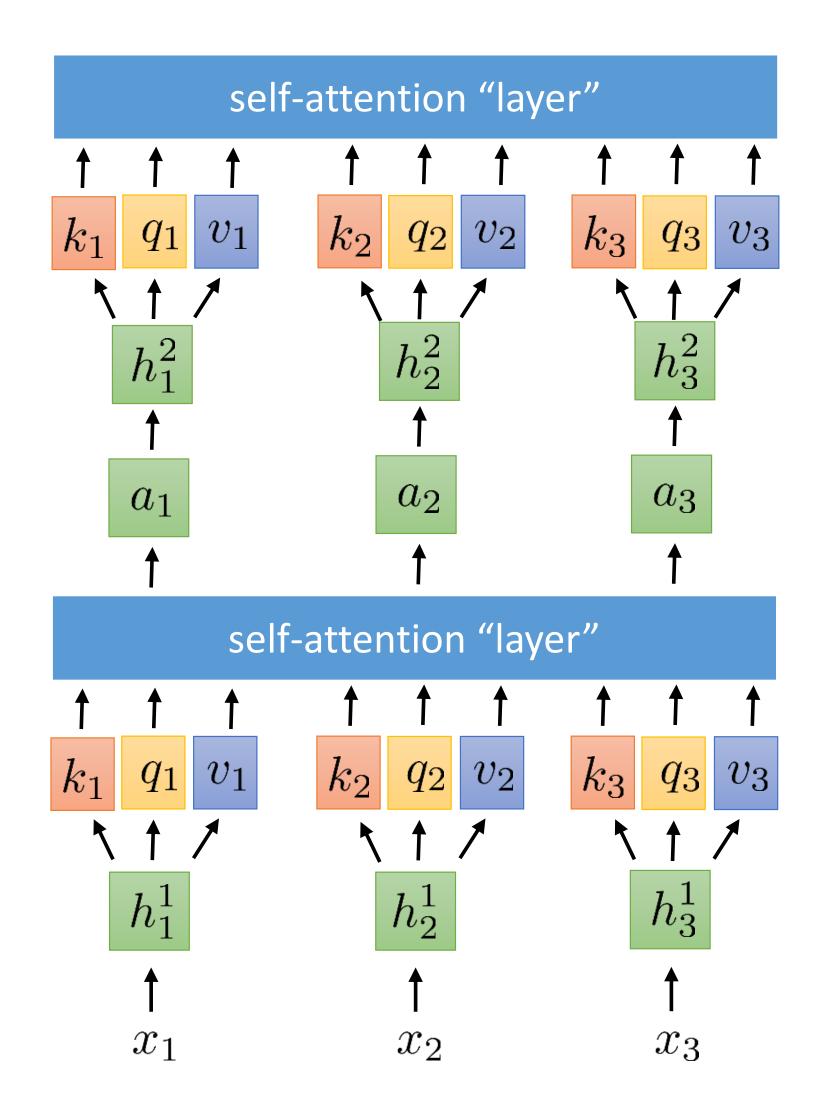
Appendix

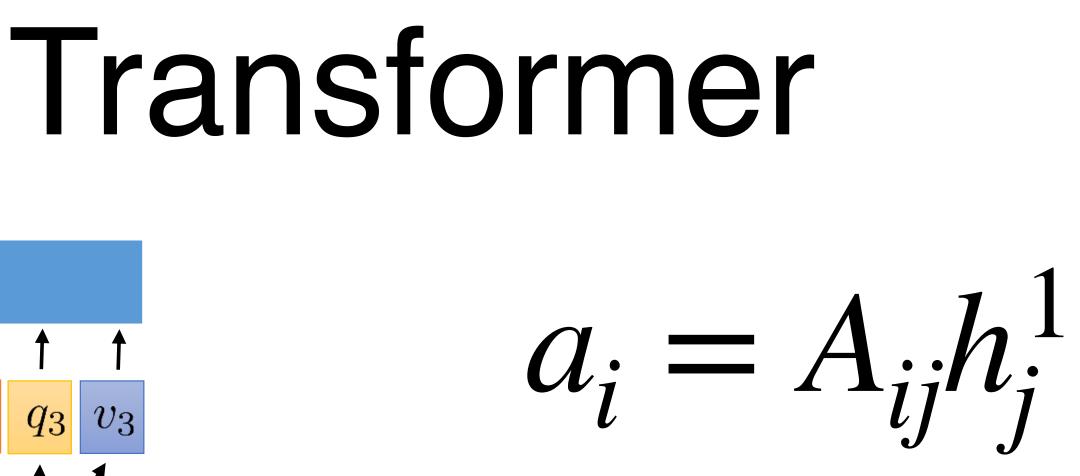
### Transformer



# $k_i = Kh_i$ $q_i = Qh_i$ $v_i = Vh_i$



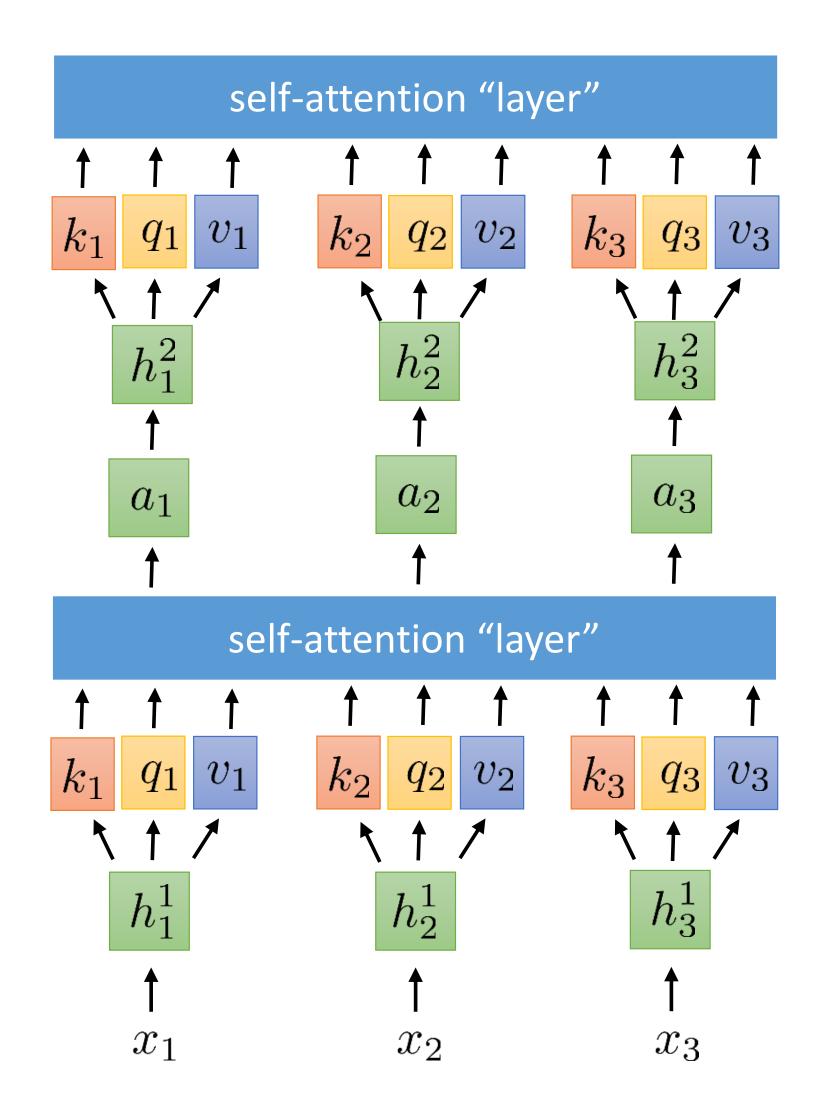




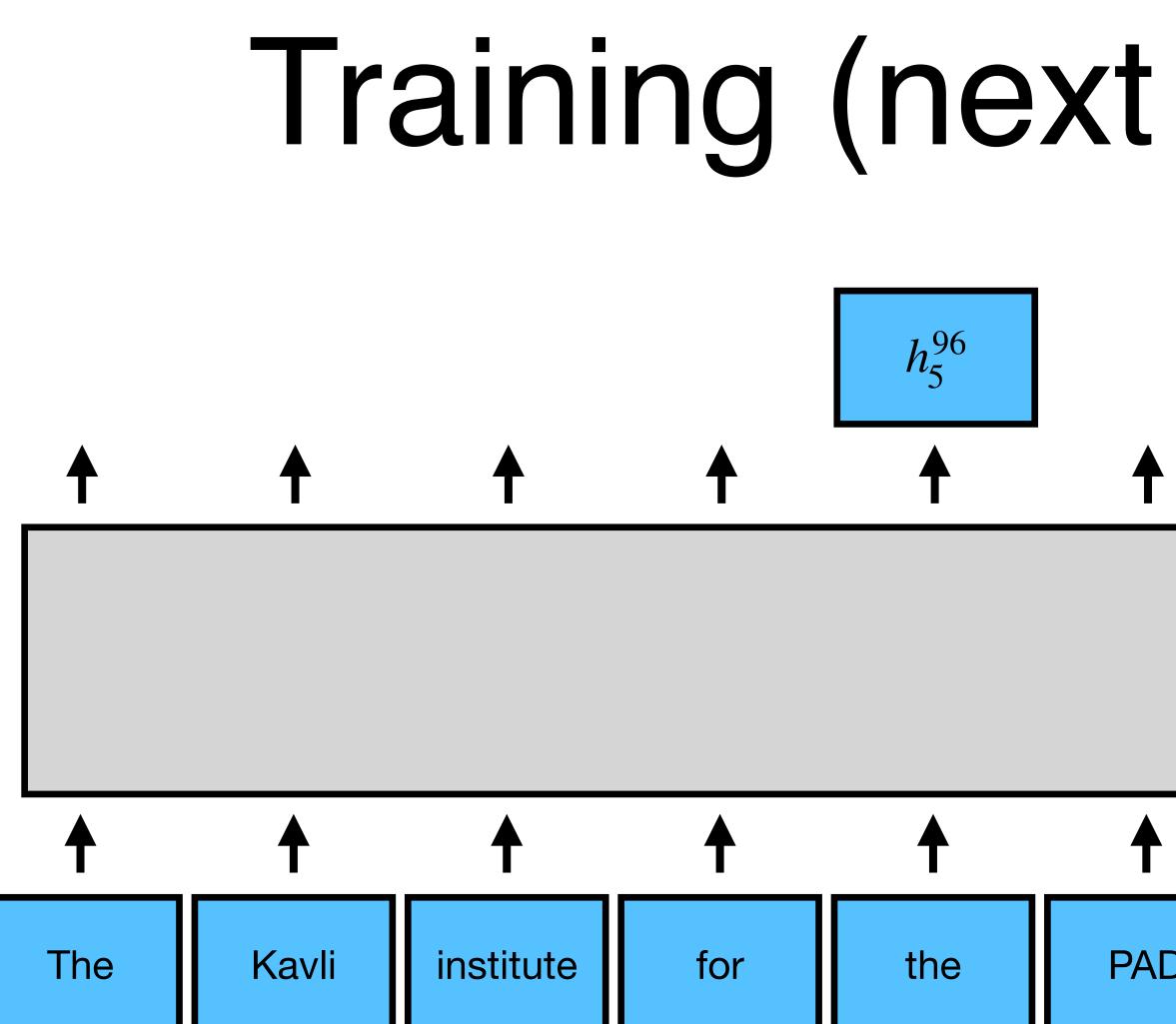
 $e^{q_i \cdot k_j}$ 

 $\sum_{l} e^{q_i \cdot k_l}$ IJ

### Transformer



## $h_i^2 = Wa_i$

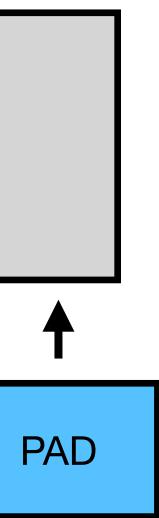


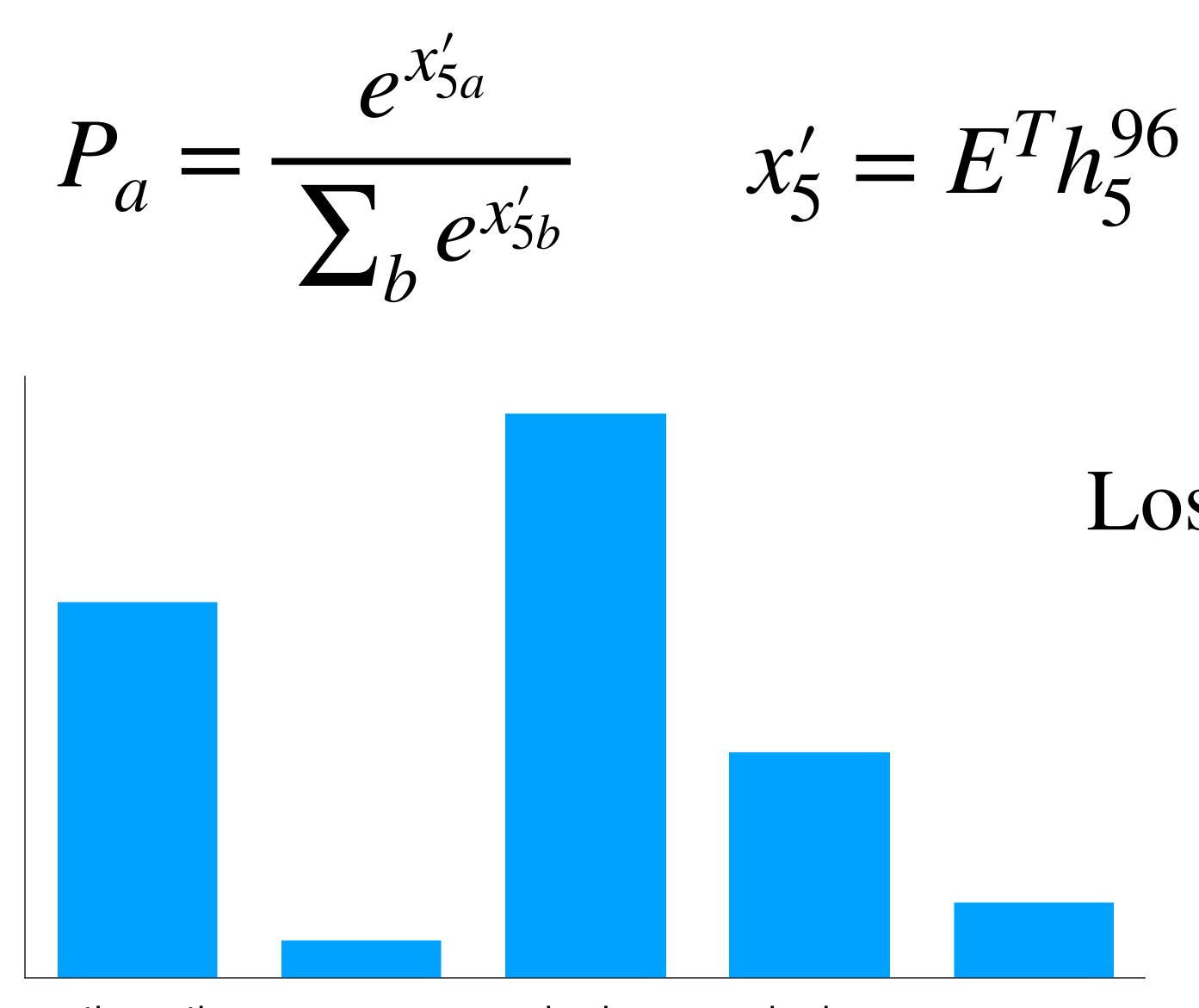
## Training (next word prediction)

#### GPT

D	PAD	PAD	PAD	PAD	PAD	







mathematics

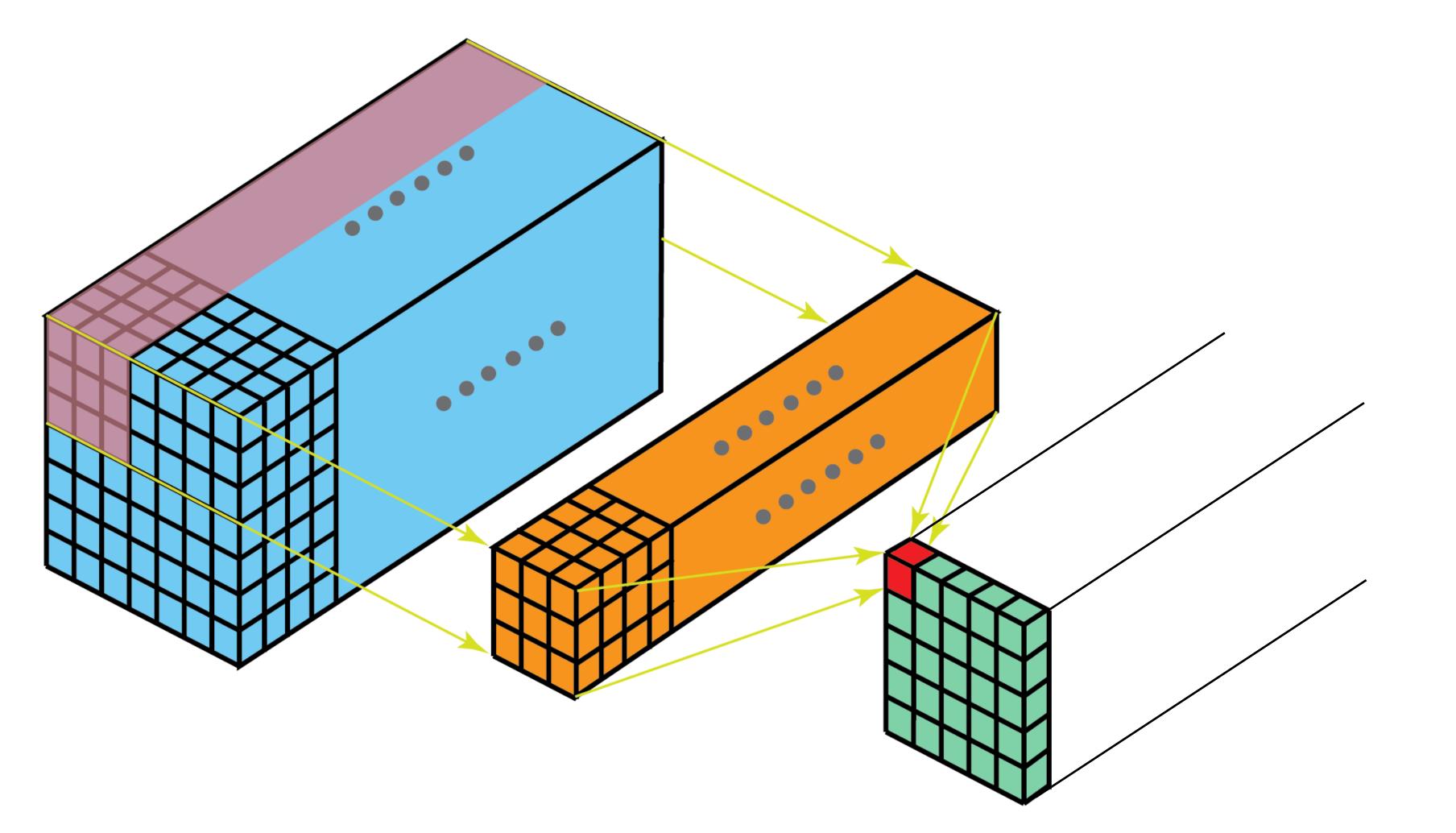
ramen

physics

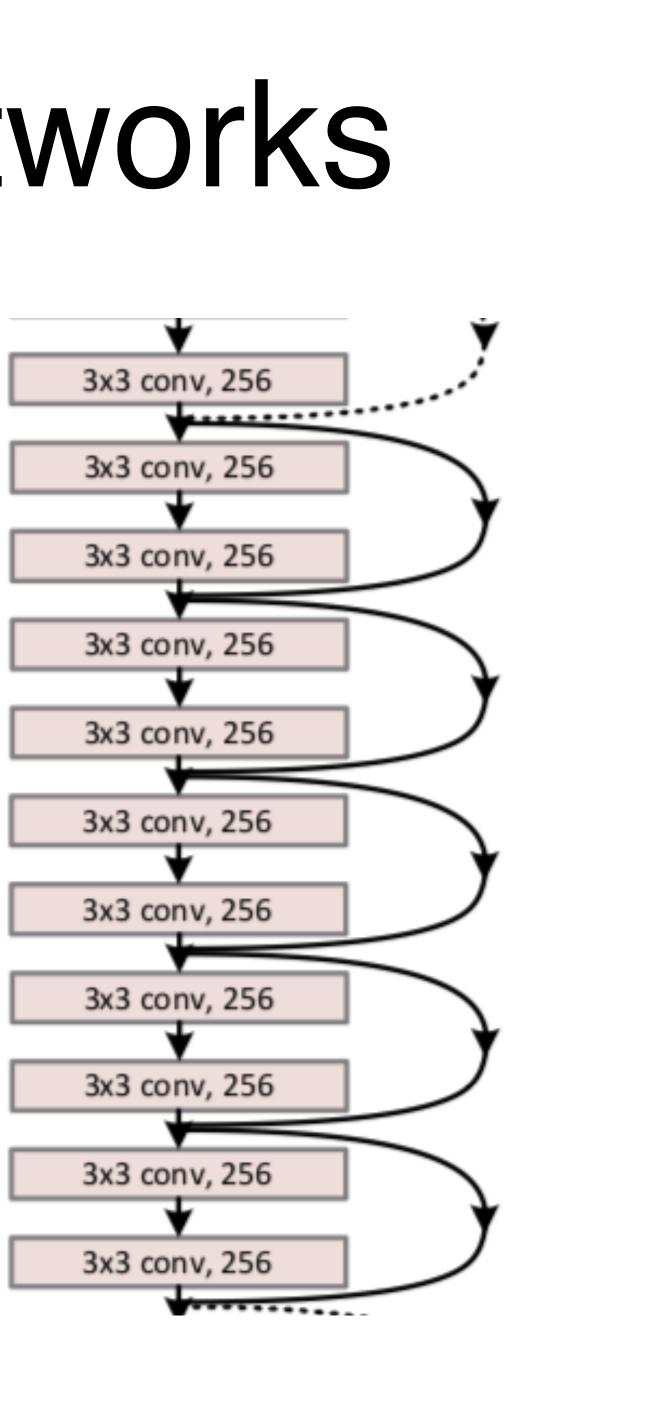
brain

### $Loss = Loss - \ln P_{i_{Physics}}$





### **Convolutional Neural Networks**



Thank you