

SUSY $(g-2)_\mu$ with & without Neutralino Dark Matter

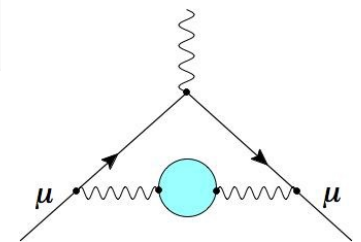
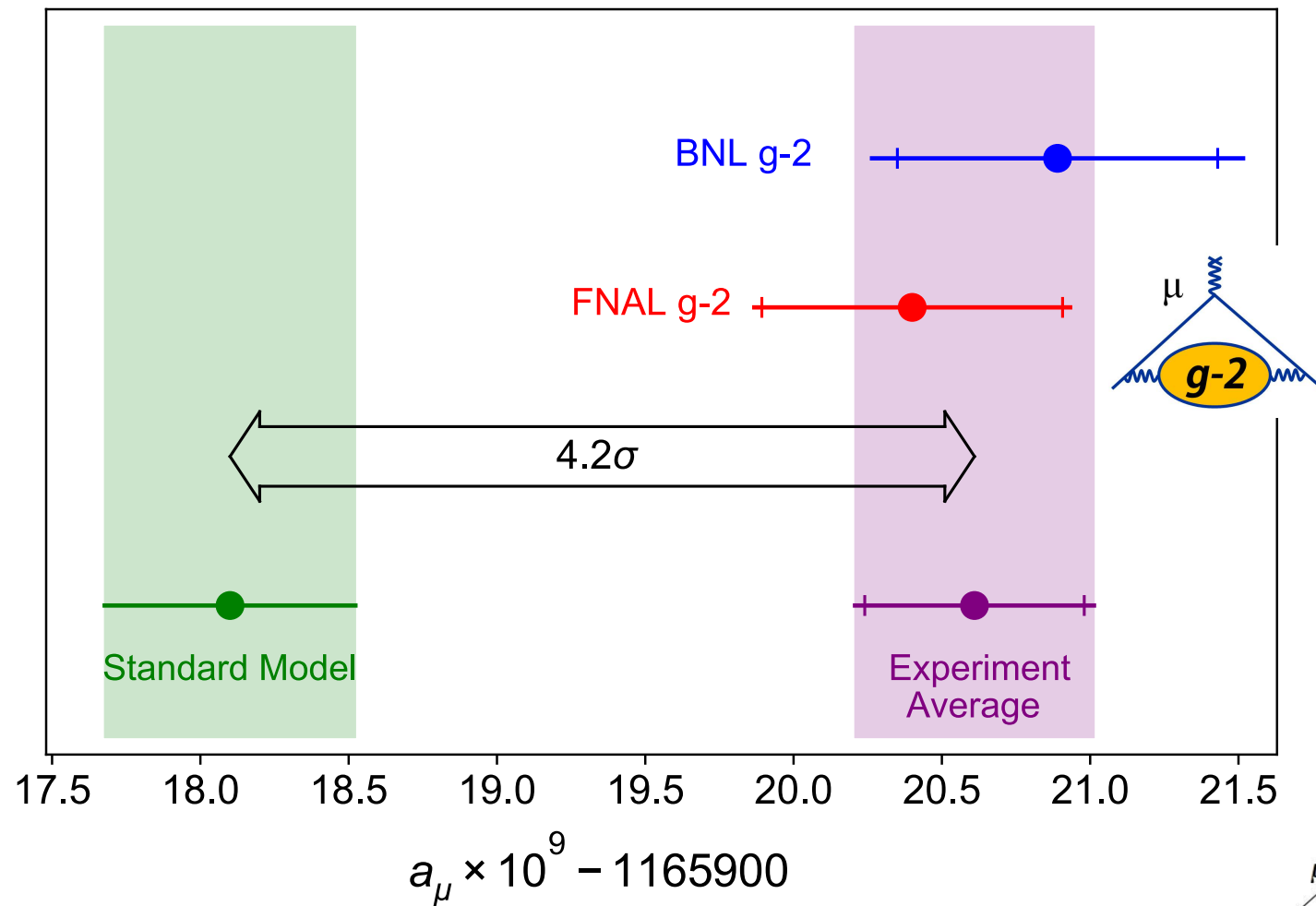
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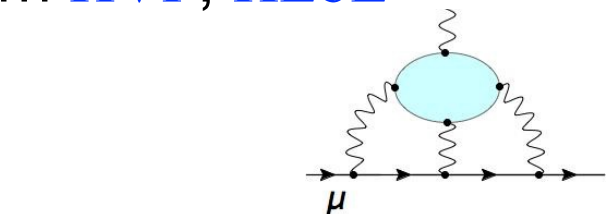
$(g - 2)_\mu$ anomaly

[Phys. Rev. LeS. 126 (2021) 14, 141801]



		QED	HVP	EW	
a_μ^{theo}	=	0.00	1165	91	810 (43)
a_μ^{exp}	=	0.00	1165	92	061 (41)

from HVP, HLbL



stat err dominant

$$a_\mu^{\text{exp}} - a_\mu^{\text{theo}} \simeq (25 \pm 6) \times 10^{-10} \simeq \Delta a_\mu^{\text{BSM}} ?$$

Motivation

- There are many BSM scenarios that can explain the $(g-2)_\mu$ anomaly:

Leptoquarks, Z' , VLL, 2HDM, axion, ..

- Supersymmetry is particularly motivated since it offers:

Coupling Unification, Radiative EWSB, Baryogenesis, DM, ...

- There are many studies on SUSY $g-2$ already:

[Athrona, Balazsa, Jacoba, Kotlarskic, Stockinger, Stockinger-Kim]; [Chakraborti, Heinemeyer, Saha]; [Endo, Hamaguchi, Iwamoto, Kitahara]; [Cox, Han, Yanagida]; [Baum, Carena, Shah, Wagner]; [Badziak, KS]; [Hagiwara, Ma, Mukhopadhyay'18], ...

- Most studies assume the neutralino is the Lightest SUSY Particle (LSP) and stable.

Q: What happens if neutralino is unstable? (e.g. RPV, Gravitino LSP)

A: DM constraints go away, but LHC constraints change. **How?**

		QED	HVP	EW	
a_μ^{theo}	=	0.00	1165	91	810 (43)
a_μ^{exp}	=	0.00	1165	92	061 (41)

- The deviation is size of the EW correction in SM:

$$a_\mu^{\text{exp}} - a_\mu^{\text{theo}} \simeq (25 \pm 6) \times 10^{-10} \sim \mathcal{O} \left(\Delta a_\mu^{\text{SM,EW}} \right)$$

- We need **very light BSM particles** **OR** **enhancement from couplings**

$$\Delta a_\mu^{\text{BSM}} \sim \Delta a^{\text{SM,EW}} \cdot \underbrace{\left(\frac{m_W^2}{m_{\text{BSM}}^2} \right)}_{\mathcal{O}(1)} \cdot \left(\frac{g_{\text{BSM}}}{g_{\text{SM}}} \right)$$

Chiral ($\tan\beta$) enhancement in SUSY

- (g-2) operator requires chirality flip:

$$\mathcal{L}_{\text{eff}} \ni i\tilde{a}_\mu \cdot \bar{\psi}_L \sigma^{\mu\nu} \psi_R F_{\mu\nu}$$

$$\overrightarrow{\mu} = g \left(\frac{e}{2m} \right) \vec{s}$$

$$a_\mu = \frac{(g-2)}{2} \equiv m_\mu \tilde{a}_\mu$$

$$\text{SM: } \tilde{a}_\mu^{\text{SM}} \propto Y_\mu \langle H \rangle = m_\mu$$

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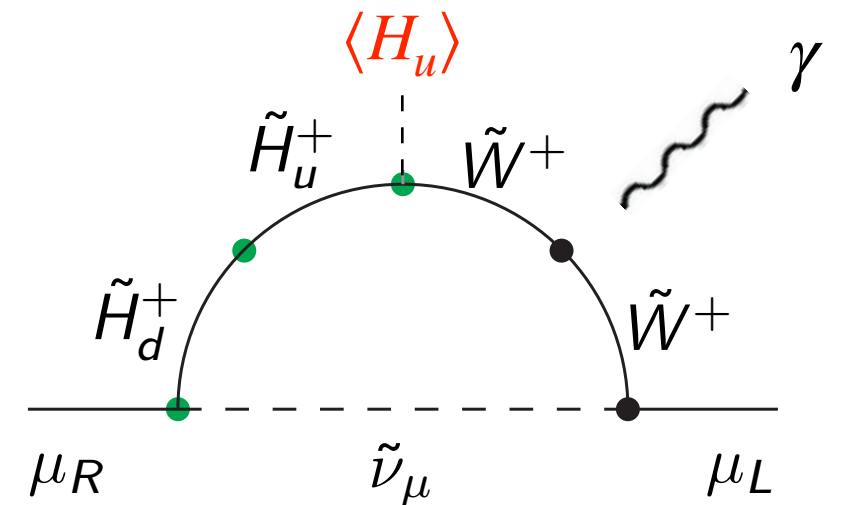
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$$a_\mu = \frac{(g-2)}{2} \equiv m_\mu \tilde{a}_\mu$$

$$\text{SM: } \tilde{a}_\mu^{\text{SM}} \propto Y_\mu \langle H \rangle = m_\mu$$

$$\text{SUSY: } \Delta \tilde{a}_\mu^{\text{SUSY}} \propto Y_\mu \langle H_u \rangle = m_\mu \cdot \tan \beta$$

$$m_\mu = Y_\mu \langle H_d \rangle \quad \tan \beta \equiv \frac{\langle H_u \rangle}{\langle H_d \rangle}$$



$$\langle H_u \rangle^2 + \langle H_d \rangle^2 = \langle H \rangle^2$$

\uparrow
 $(246 \text{ GeV})^2$

Chiral ($\tan\beta$) enhancement in SUSY

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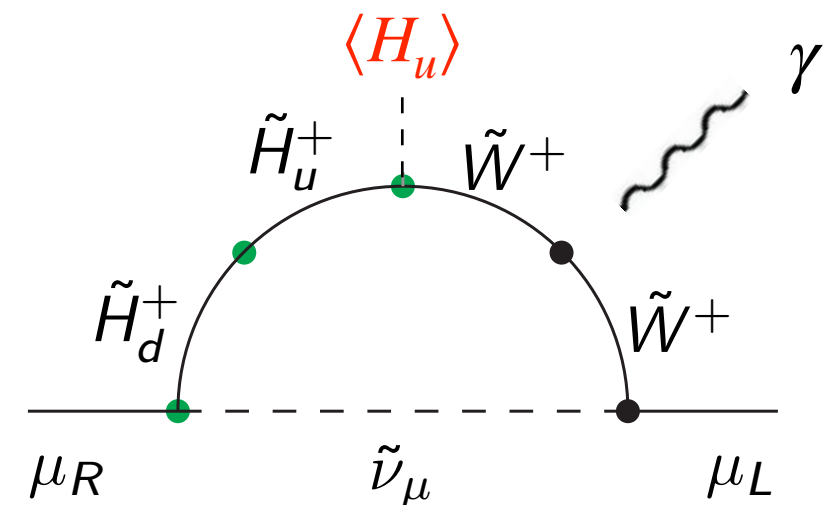
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$$\langle H_u \rangle^2 + \langle H_d \rangle^2 = \langle H \rangle^2$$

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 $(246 \text{ GeV})^2$

$$\Delta a_\mu^{\text{BSM}} \sim \Delta a^{\text{SM,EW}} \cdot \left(\frac{m_W^2}{m_{\text{SUSY}}^2} \right) \cdot \tan \beta$$

$$\tan \beta \in [5 - 60] \Rightarrow m_{\text{SUSY}} \in [200 - 600] \text{ GeV}$$

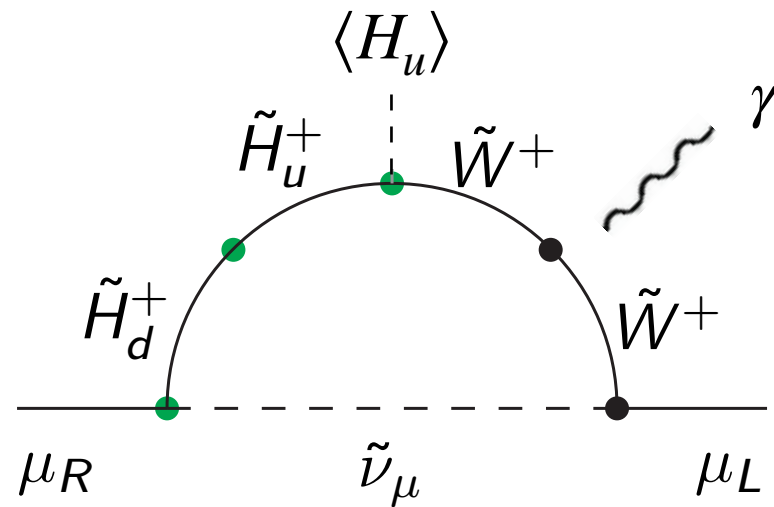
- Due to strong LHC constraints, we *decouple coloured SUSY particles* (they do not contribute to $(g-2)_\mu$ anyway).
- a_μ^{SUSY} depends on **5 mass parameters** and $\tan\beta$:

$$\begin{array}{ll}
 \textcolor{red}{M}_1 : \text{Bino mass} & \left(\textcolor{red}{m}_{\tilde{l}_R} \equiv \widetilde{m}_{\tilde{e}_R}^2 = \widetilde{m}_{\tilde{\mu}_R}^2 = \widetilde{m}_{\tilde{\tau}_R}^2 \right. \\
 \textcolor{red}{M}_2 : \text{Wino mass} & \left. \textcolor{red}{m}_{\tilde{l}_L} \equiv \widetilde{m}_{\tilde{\nu}_e} = \widetilde{m}_{\tilde{\nu}_\mu} = \widetilde{m}_{\tilde{\nu}_\tau} = \widetilde{m}_{\tilde{e}_L} = \widetilde{m}_{\tilde{\mu}_L} = \widetilde{m}_{\tilde{\tau}_L} \right. \\
 \textcolor{red}{\mu} : \text{Higgsino mass} & \left. \textcolor{blue}{\tan \beta} \equiv \langle H_u \rangle / \langle H_d \rangle \right)
 \end{array}$$

no LFV due to universal soft masses: avoid strong constraint from $\mu \rightarrow e \gamma$

$$\Delta a_{\mu}^{\text{SUSY}} = \Delta a_{\mu}^{\text{WHL}} + \Delta a_{\mu}^{\text{BHL}} + \Delta a_{\mu}^{\text{BHR}} + \Delta a_{\mu}^{\text{BLR}}$$

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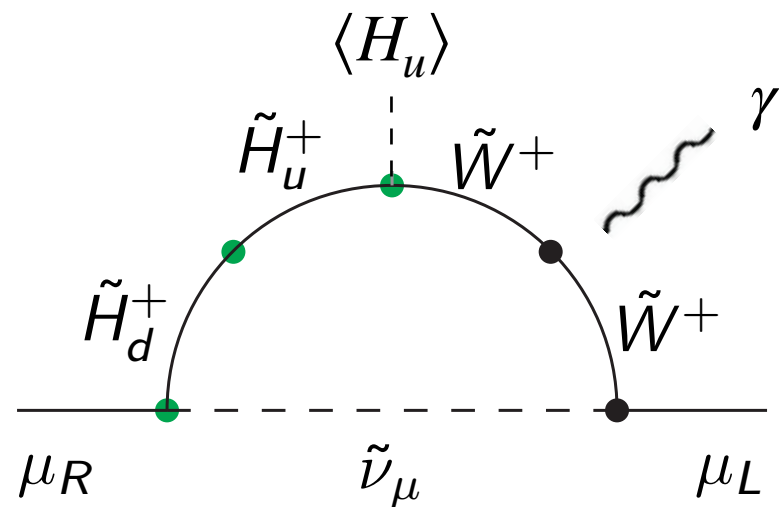
$$\Delta a_\mu^{\text{WHL}}(M_2, \mu, m_{\tilde{l}_L}) = \frac{\alpha_W}{8\pi} \frac{m_\mu^2}{M_2 \mu} \tan \beta \cdot f_W(\{\mathbf{m}\})$$

M_1 : Bino (\tilde{B}) mass

M_2 : Wino (\tilde{W}) mass

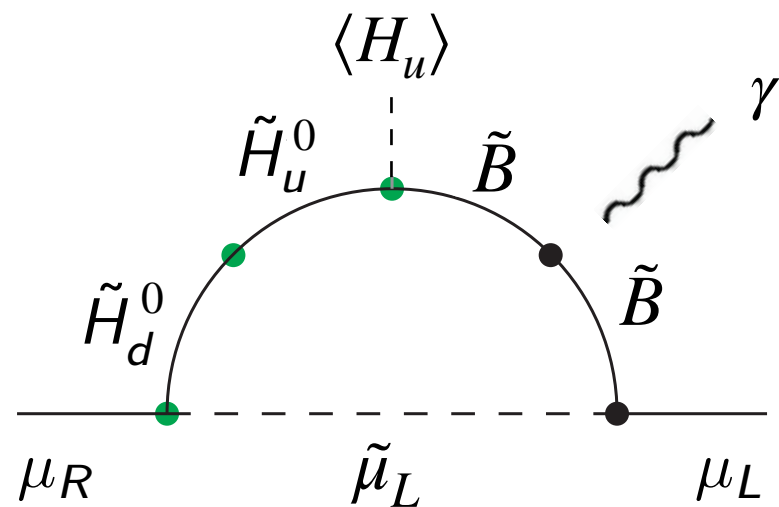
μ : Higgsino (\tilde{H}_u, \tilde{H}_d) mass

$$\Delta a_\mu^{\text{SUSY}} = \Delta a_\mu^{\text{WHL}} + \Delta a_\mu^{\text{BHL}} + \Delta a_\mu^{\text{BHR}} + \Delta a_\mu^{\text{BLR}}$$



$$\Delta a_\mu^{\text{WHL}}(M_2, \mu, m_{\tilde{l}_L}) = \frac{\alpha_W}{8\pi} \frac{m_\mu^2}{M_2 \mu} \tan \beta \cdot f_W(\{\mathbf{m}\})$$

$$\Delta a_\mu^{\text{BHL}}(M_1, \mu, m_{\tilde{l}_L}) = \frac{\alpha_Y}{8\pi} \frac{m_\mu^2}{M_1 \mu} \tan \beta \cdot f_N(\{\mathbf{m}\})$$

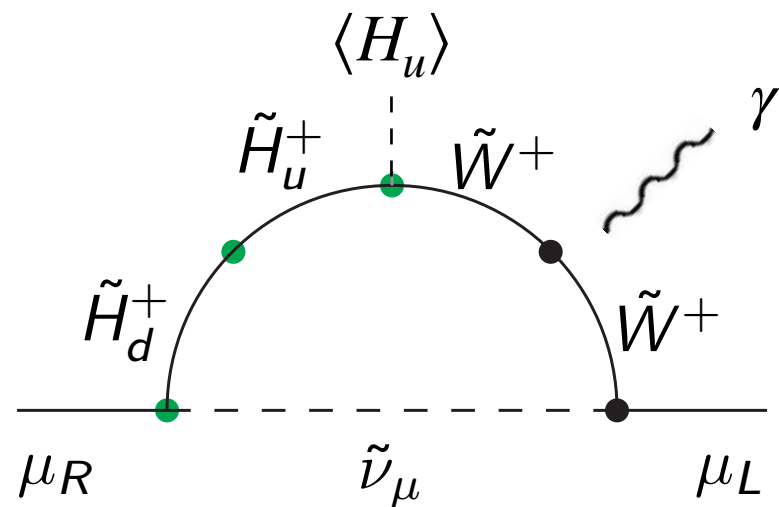


M_1 : Bino (\tilde{B}) mass

M_2 : Wino (\tilde{W}) mass

μ : Higgsino (\tilde{H}_u, \tilde{H}_d) mass

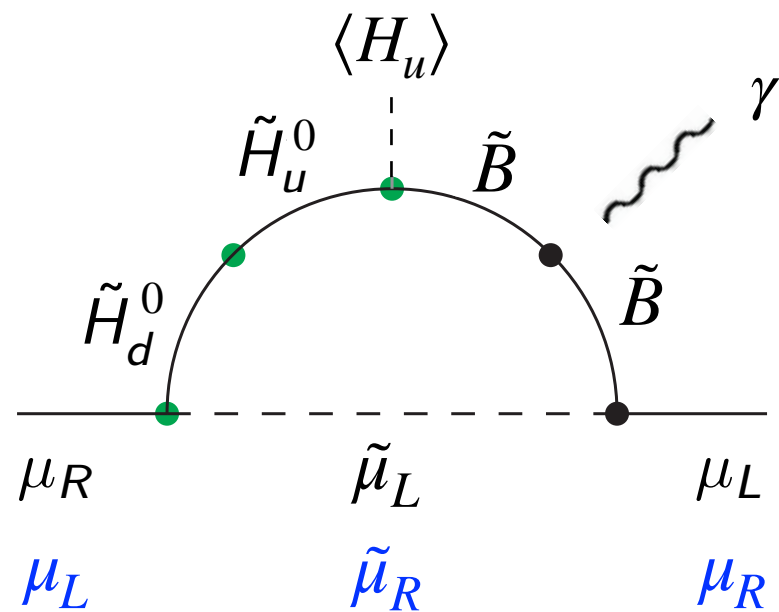
$$\Delta a_\mu^{\text{SUSY}} = \Delta a_\mu^{\text{WHL}} + \Delta a_\mu^{\text{BHL}} + \Delta a_\mu^{\text{BHR}} + \Delta a_\mu^{\text{BLR}}$$



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$$\Delta a_\mu^{\text{BHR}}(M_1, \mu, m_{\tilde{l}_R}) = -\frac{\alpha_Y}{8\pi} \frac{m_\mu^2}{M_1 \mu} \tan \beta \cdot f_N(\{\mathbf{m}\})$$

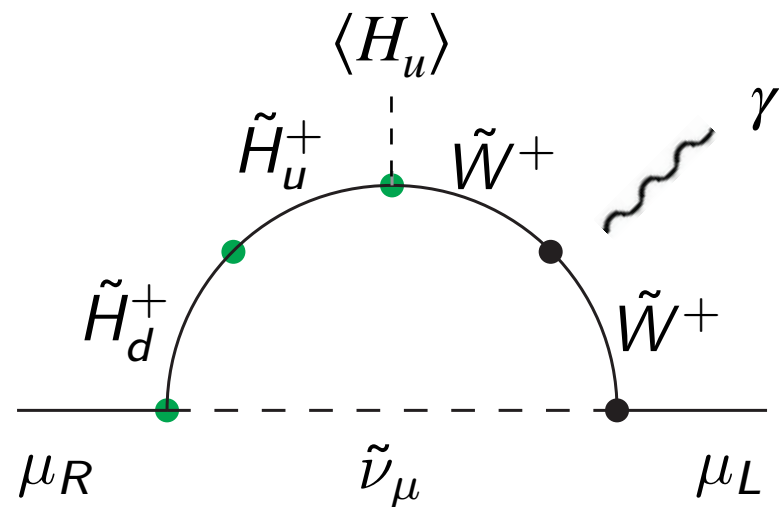


M_1 : Bino (\tilde{B}) mass

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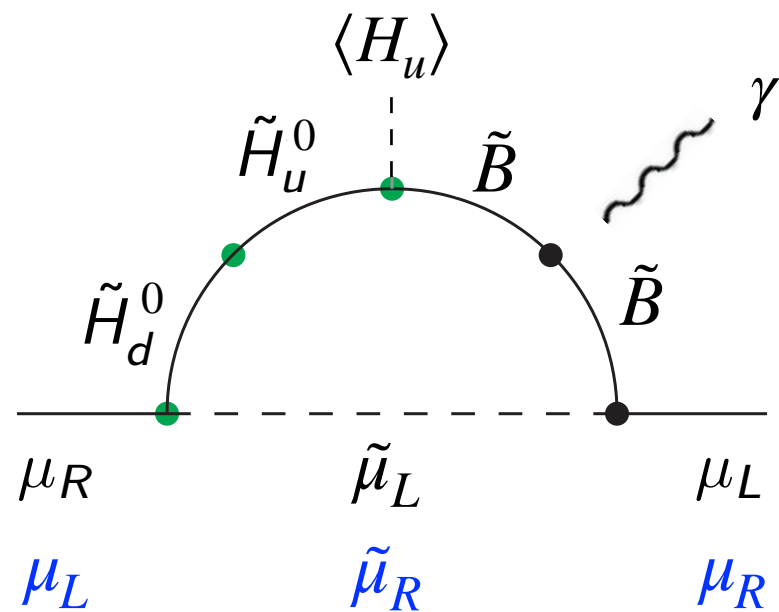
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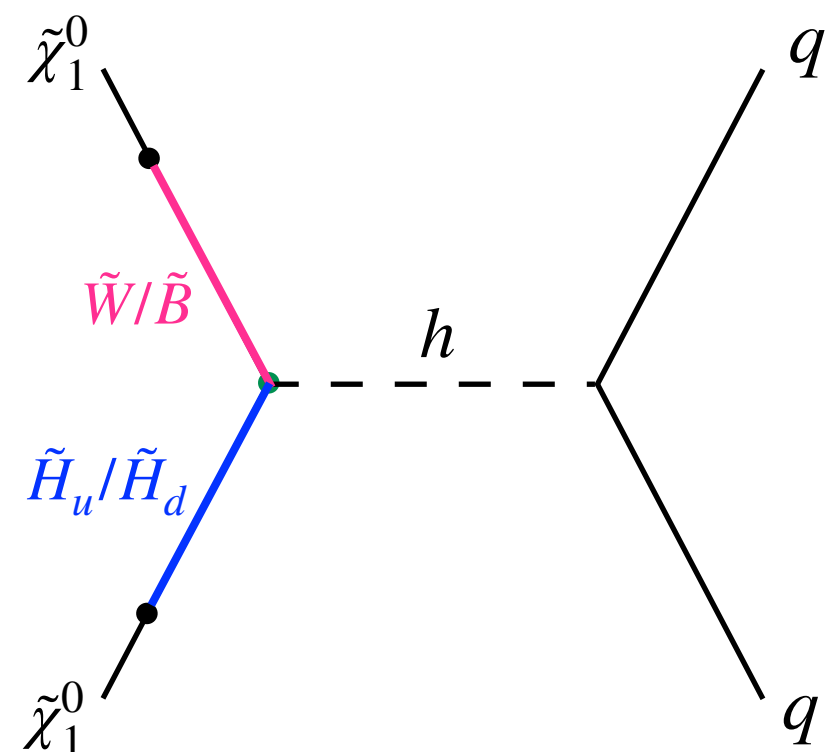
$$\Delta a_\mu^{\text{WHL}}(M_2, \mu, m_{\tilde{l}_L}) = \frac{\alpha_W}{8\pi} \frac{m_\mu^2}{M_2 \mu} \tan \beta \cdot f_W(\{\mathbf{m}\})$$

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$$\Delta a_\mu^{\text{BHR}}(M_1, \mu, m_{\tilde{l}_R}) = -\frac{\alpha_Y}{8\pi} \frac{m_\mu^2}{M_1 \mu} \tan \beta \cdot f_N(\{\mathbf{m}\})$$



Large gaugino-Higgsino mixing leads to a **large cross-section for DM Direct Detection:**

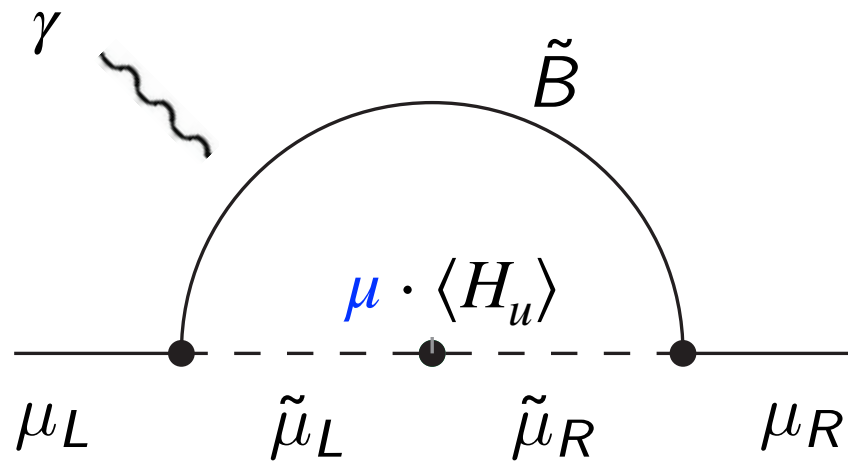


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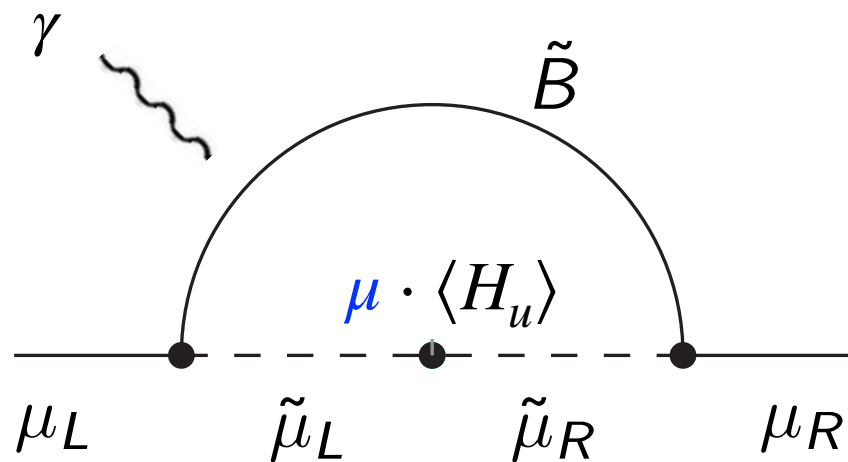
$$\Delta a_\mu^{\text{SUSY}} = \Delta a_\mu^{\text{WHL}} + \Delta a_\mu^{\text{BHL}} + \Delta a_\mu^{\text{BHR}} + \Delta a_\mu^{\text{BLR}}$$



$$\Delta a_\mu^{\text{BLR}}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu) = \frac{\alpha_Y}{4\pi} \frac{m_\mu^2 M_1 \mu}{m_{\mu_L}^2 m_{\mu_R}^2} \tan \beta \cdot f_{\text{BLR}}(\{\mathbf{m}\})$$

\uparrow
 large μ needed

$$\Delta a_\mu^{\text{SUSY}} = \Delta a_\mu^{\text{WHL}} + \Delta a_\mu^{\text{BHL}} + \Delta a_\mu^{\text{BHR}} + \Delta a_\mu^{\text{BLR}}$$



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↑
large μ needed

Constraints:

❖ Stau mass² becomes negative or too small!

- charge breaking vacuum: $m_{\text{stau}1}^2 > 0$

- LEP bound: $m_{\text{stau}1} > 90 \text{ GeV}$

- stau LSP: $m_{\text{stau}1} > m_{\text{neutralino}1}$

- **Vacuum (meta-)stability:**

$$(\tilde{\tau} \text{ mass matrix}) \sim \begin{pmatrix} m_{\tilde{\tau}_R}^2 & Y_\tau \mu \langle H_u \rangle \\ Y_\tau \mu \langle H_u \rangle & m_{\tilde{\tau}_L}^2 \end{pmatrix}$$

$$|m_{\tilde{\ell}_{LR}}^2| \leq \left[1.01 \times 10^2 \text{ GeV} \sqrt{m_{\tilde{\ell}_L} m_{\tilde{\ell}_R}} + 1.01 \times 10^2 \text{ GeV} (m_{\tilde{\ell}_L} + 1.03 m_{\tilde{\ell}_R}) - 2.27 \times 10^4 \text{ GeV}^2 + \frac{2.97 \times 10^6 \text{ GeV}^3}{m_{\tilde{\ell}_L} + m_{\tilde{\ell}_R}} - 1.14 \times 10^8 \text{ GeV}^4 \left(\frac{1}{m_{\tilde{\ell}_L}^2} + \frac{0.983}{m_{\tilde{\ell}_R}^2} \right) \right]$$

[Kitahara, Yoshinaga 13]; [Endo, Hamaguchi, Kitahara, Yoshinaga 13]

❖ **Overproduction of Bino-like neutralinos** in the early universe: $\Omega_{\tilde{\chi}_1^0} < \Omega_{\text{DM}}$

slepton-coannihilation needed $\Rightarrow m_{\text{slepton}} \sim m_{\text{Bino}}$

Summary of g-2 in MSSM

$$\Delta a_\mu^{\text{SUSY}} = \Delta a_\mu^{\text{WHL}} + \Delta a_\mu^{\text{BHL}} + \Delta a_\mu^{\text{BHR}} + \Delta a_\mu^{\text{BLR}}$$

$$\left[\begin{array}{l} \Delta a_\mu^{\text{WHL}}(M_2, \mu, m_{\tilde{l}_L}) \\ \Delta a_\mu^{\text{BHL}}(M_1, \mu, m_{\tilde{l}_L}) \\ \Delta a_\mu^{\text{BHR}}(M_1, \mu, m_{\tilde{l}_R}) \end{array} \right]$$

Higgsino, one gaugino, one slepton all must be light:

⇒ LHC constraint with large \cancel{E}_T

gaugino-Higgsino mixing ⇒ DM direct detection

$$\Delta a_\mu^{\text{BLR}}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu)$$

↑
large

Bino and both L and R sleptons must be light:

⇒ LHC constraint with large \cancel{E}_T

⇒ Bino abundance $\Omega_{\tilde{\chi}_1^0} < \Omega_{\text{DM}}$

⇒ Charged LSP, Vacuum stability

Unstable Neutralino (Gravitino, RPV)

$$\Delta a_\mu^{\text{SUSY}} = \Delta a_\mu^{\text{WHL}} + \Delta a_\mu^{\text{BHL}} + \Delta a_\mu^{\text{BHR}} + \Delta a_\mu^{\text{BLR}}$$

$$\Delta a_\mu^{\text{WHL}}(M_2, \mu, m_{\tilde{l}_L})$$

$$\Delta a_\mu^{\text{BHL}}(M_1, \mu, m_{\tilde{l}_L})$$

$$\Delta a_\mu^{\text{BHR}}(M_1, \mu, m_{\tilde{l}_R})$$

Higgsino, one gaugino, one slepton all must be light:

⇒ LHC constraint with large \cancel{E}_T ← Modified

gaugino-Higgsino mixing ⇒ ~~DM direct detection~~

$$\Delta a_\mu^{\text{BLR}}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu)$$

↑
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Bino and both L and R sleptons must be light:

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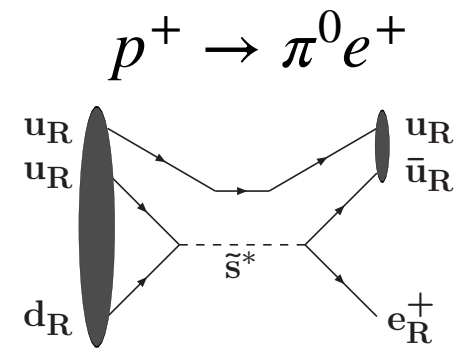
⇒ ~~Bino abundance~~ $\Omega_{\chi_1^0} < \Omega_{\text{DM}}$

⇒ Charged LSP, Vacuum stability

R-Parity Violation; UDD

$$W_{\text{RPV}} = \underbrace{\lambda''_{ijk} U_i^c D_j^c D_k^c}_{\text{B}} + \underbrace{\lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c + \kappa_i L_i H_u}_{\text{L}}$$

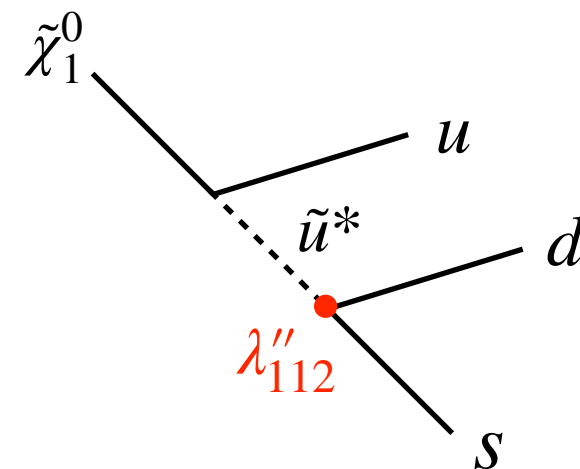
- Allowing both **B** and **L** violation leads to a rapid proton decay:
- We introduce only the **UDD** operator with: $\lambda''_{112} \neq 0$
- Constraint from K0-K0bar mixing can easily be satisfied:



$$|\lambda''_{112} \lambda''_{123}| \lesssim 2.8 \times 10^{-2} \left(\frac{m_{\tilde{s}_R, \tilde{u}_R}}{1 \text{ TeV}} \right) \quad [1810.08228]$$

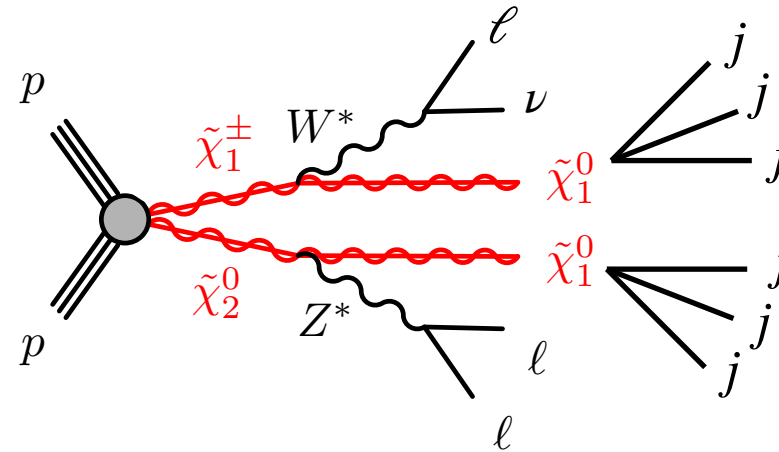
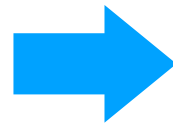
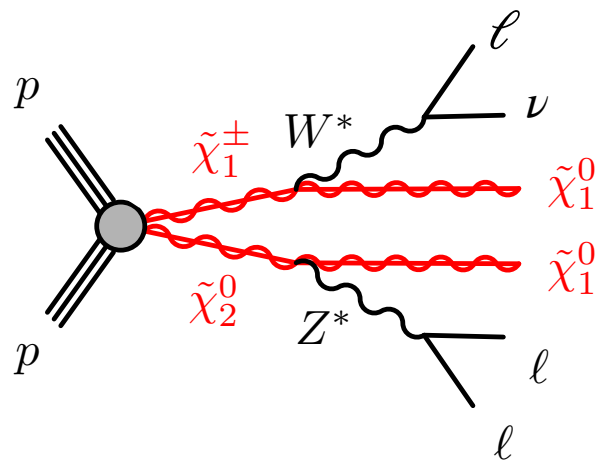
$$|\lambda''_{112} \lambda''_{113}| \lesssim 1.2 \times 10^{-1} \left(\frac{m_{\tilde{d}_R, \tilde{u}_R}}{1 \text{ TeV}} \right)$$

- **LHC signature is the most challenging:**
no leptons, no b-jets in the neutralino decay



R-Parity Violation; UDD

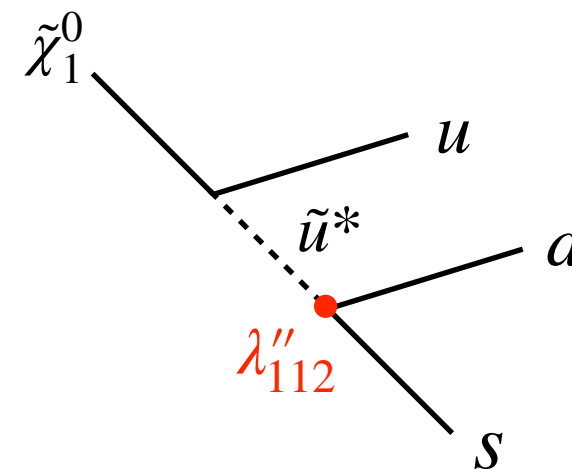
neutralino
LSP



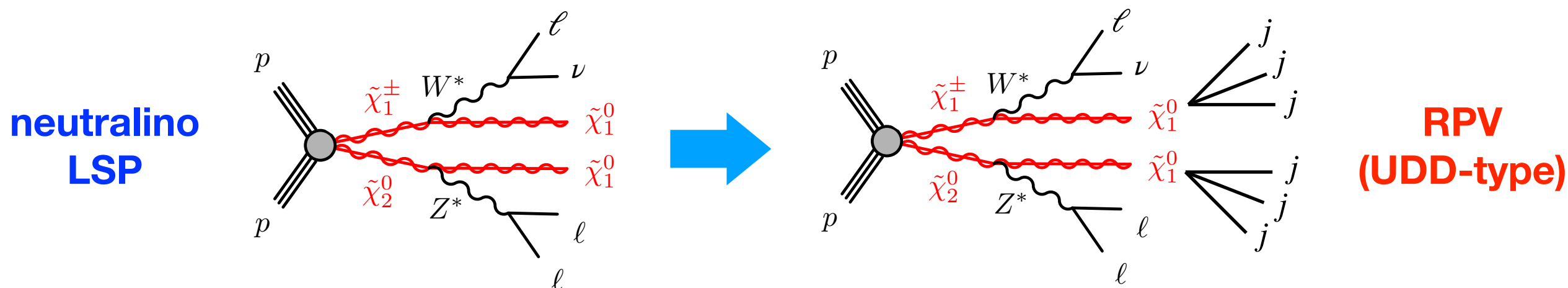
RPV
(UDD-type)

No missing energy, but multi-jet

- LHC signature is the most challenging:
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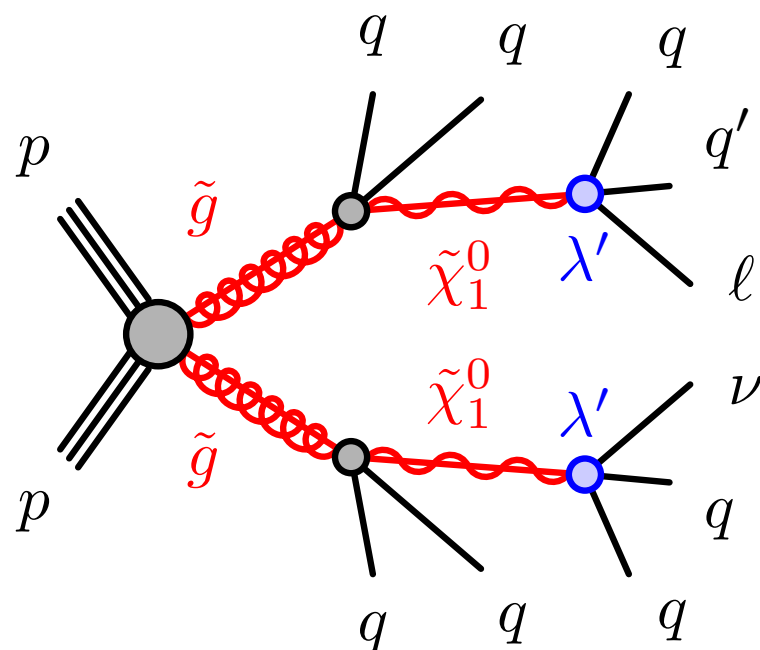
R-Parity Violation; UDD



No missing energy, but multi-jet

- There exist ATLAS and CMS analyses sensitive to such final states:

ATLAS [2106.09609]



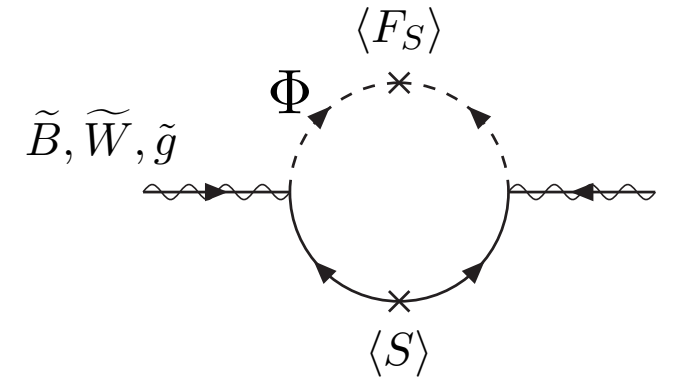
CMS [1709.05406]

Bin	Final state	Definition
1	2 SS leptons	0 jets, $M_T > 100$ GeV and $p_T^{\text{miss}} > 140$ GeV
2	2 SS leptons	1 jet, $M_T < 100$ GeV, $p_T^{\ell\ell} < 100$ GeV and $p_T^{\text{miss}} > 200$ GeV
3	3 light leptons	$M_T > 120$ GeV and $p_T^{\text{miss}} > 200$ GeV
4	3 light leptons	$p_T^{\text{miss}} > 250$ GeV
5	2 light leptons and 1 tau	$M_{T2}(\ell_1, \tau) > 50$ GeV and $p_T^{\text{miss}} > 200$ GeV
6	1 light lepton and 2 taus	$M_{T2}(\ell, \tau_1) > 50$ GeV and $p_T^{\text{miss}} > 200$ GeV
7	1 light lepton and 2 taus	$p_T^{\text{miss}} > 75$ GeV
8	more than 3 leptons	$p_T^{\text{miss}} > 200$ GeV

Gravitino LSP

- In the gauge-mediated SUSY breaking (GMSB) scenario, **light gravitino is motivated by naturalness:**

$$\delta m_h^2 \propto m_{SUSY}^2 \ln \left(\frac{\Lambda_{\text{mess}}}{M_{\text{PL}}} \right) \quad m_{3/2} = \frac{4\pi}{\sqrt{3}\alpha_W} M_2 \frac{\Lambda_{\text{mess}}}{M_{\text{PL}}}$$



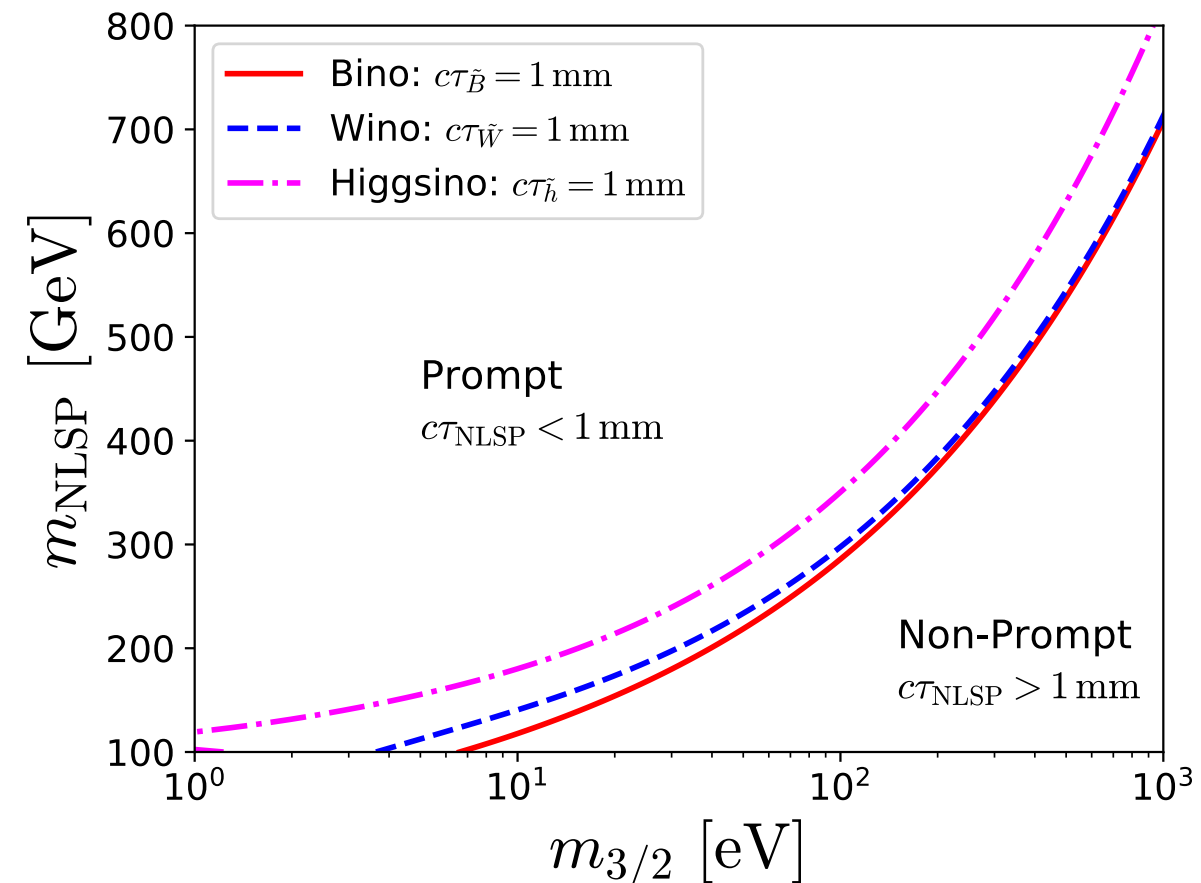
- The decay rate of the NLSP neutralino into the gravitino can be calculated. For light gravitinos ($< 10\text{-}100\text{ eV}$), the **neutralino decays are prompt**.

$$\Gamma(\tilde{\chi}_1^0 \rightarrow \tilde{G}\gamma) = |N_{11}c_W + N_{12}s_W|^2 \mathcal{A},$$

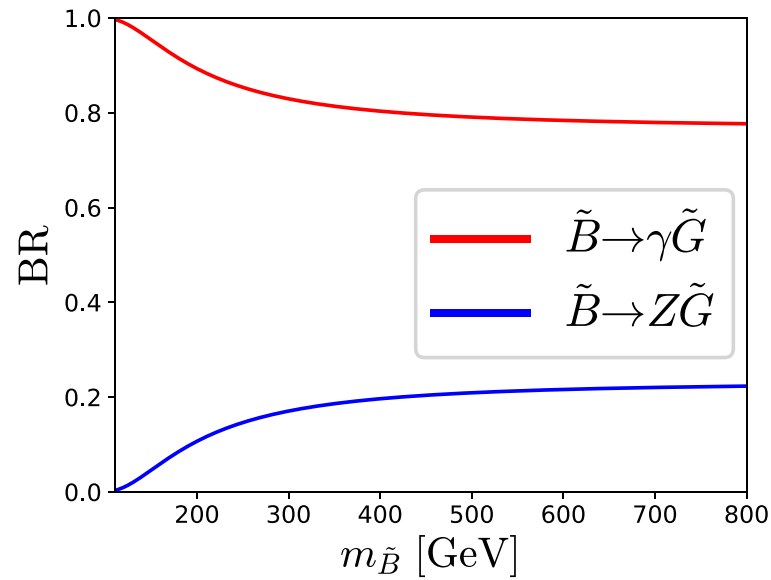
$$\Gamma(\tilde{\chi}_1^0 \rightarrow \tilde{G}Z) = \left(|N_{12}c_W - N_{11}s_W|^2 + \frac{1}{2} |N_{13}c_\beta - N_{14}s_\beta|^2 \right) \left(1 - \frac{m_Z^2}{m_{\tilde{\chi}_1^0}^2} \right)^4 \mathcal{A},$$

$$\Gamma(\tilde{\chi}_1^0 \rightarrow \tilde{G}h) = \frac{1}{2} |N_{13}c_\beta + N_{14}s_\beta|^2 \left(1 - \frac{m_h^2}{m_{\tilde{\chi}_1^0}^2} \right)^4 \mathcal{A},$$

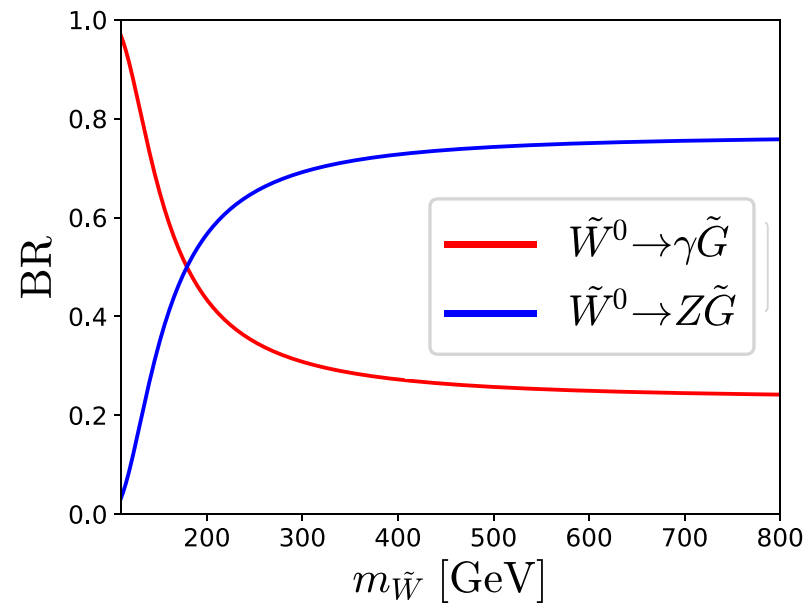
$$\mathcal{A} = \frac{m_{\tilde{\chi}_1^0}^5}{16\pi m_{3/2}^2 M_{\text{pl}}^2} \sim \frac{1}{0.3\text{ mm}} \left(\frac{m_{\tilde{\chi}_1^0}}{100\text{ GeV}} \right)^5 \left(\frac{m_{3/2}}{10\text{ eV}} \right)^{-2}$$



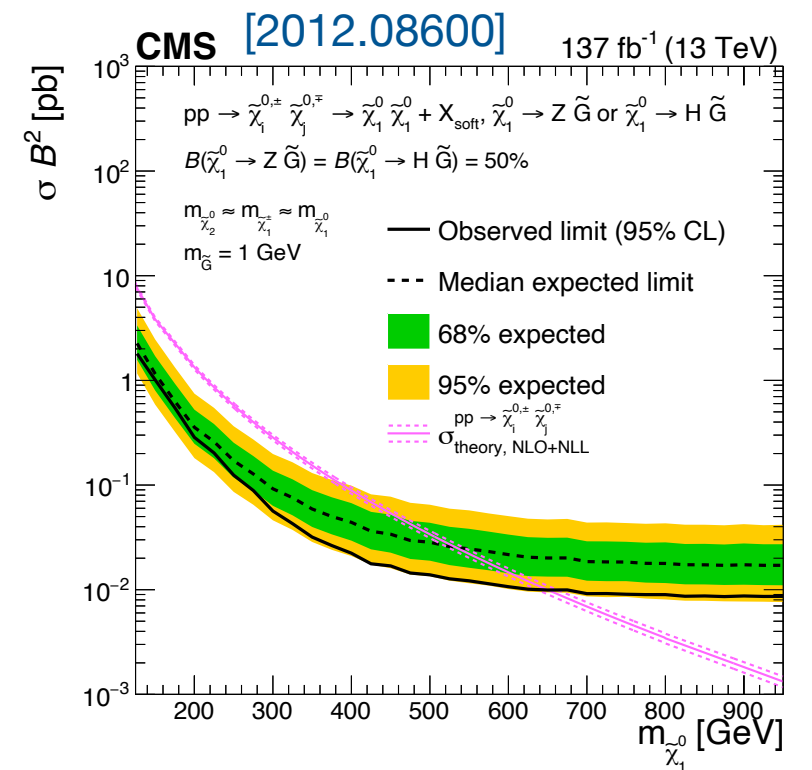
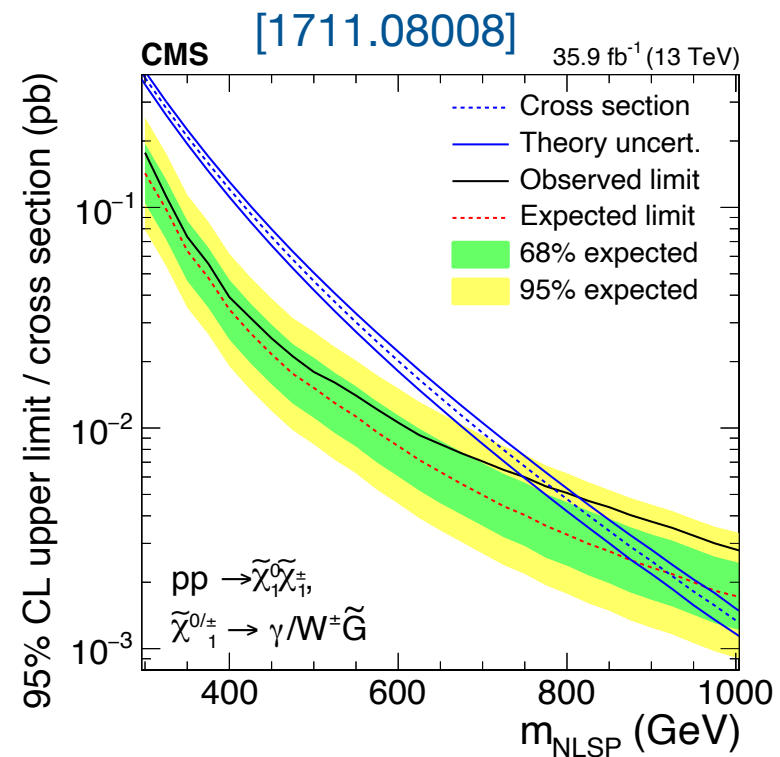
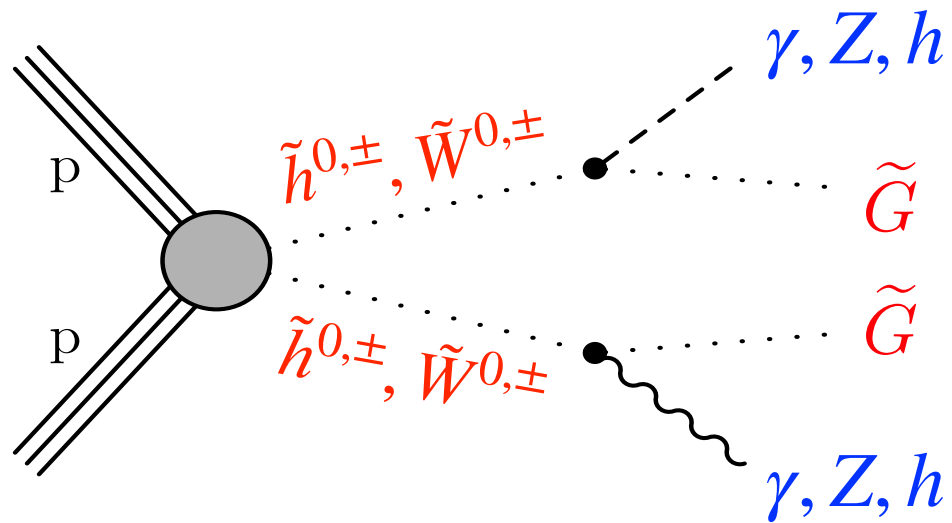
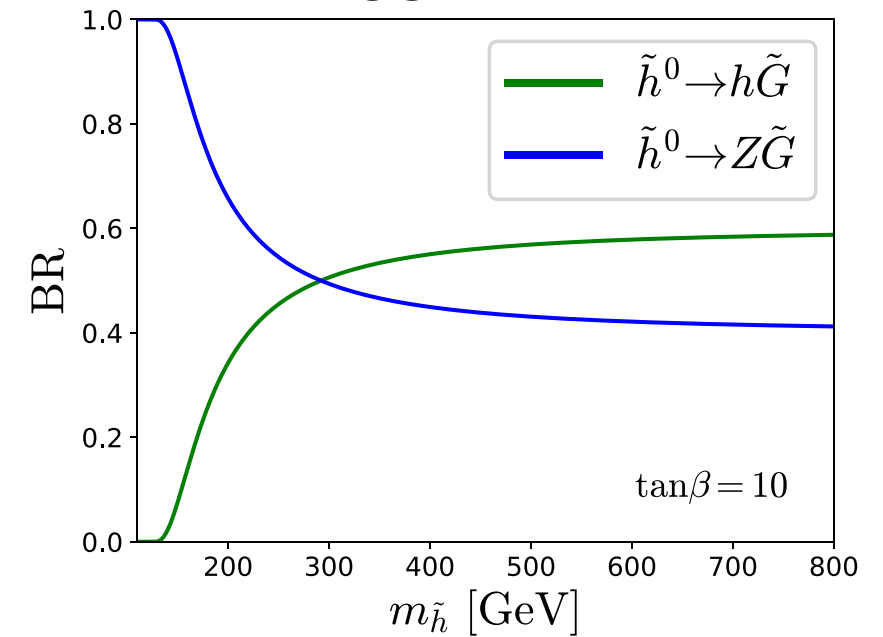
Bino-like



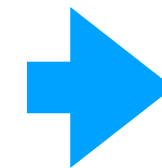
Wino-like



Higgsino-like



- Higgsino, Wino direct production excluded up to $\sim 700 \text{ GeV}$
- SUSY g-2 requires Higgsino or Wino with $m < 600 \text{ GeV}$



**SUSY (g-2)_μ
incompatible
with LHC**

Analysis Framework

SUSY g-2: 1-loop + leading 2-loop GM2Calc [\[Eur.Phys.J. C76 \(2016\) no.2, 62\]](#)

Neutralino abundance, Direct Detection: MicrOMEGAs [\[2003.08621\]](#)

Decay of SUSY particles: SUSY-HIT [\[hep-ph/0609292\]](#)

LHC constraints:

- **MSSM:** ① Mapping simplified model limits to the model point (σ BR)
- **RPV:** ② Pythia 8 + CheckMATE 2 [\[1907.09874\]](#), [\[1611.09856\]](#)
- **Gravitino LSP:** Both ① and ②

Results are preliminary

List of ATLAS & CMS searches included in our analysis

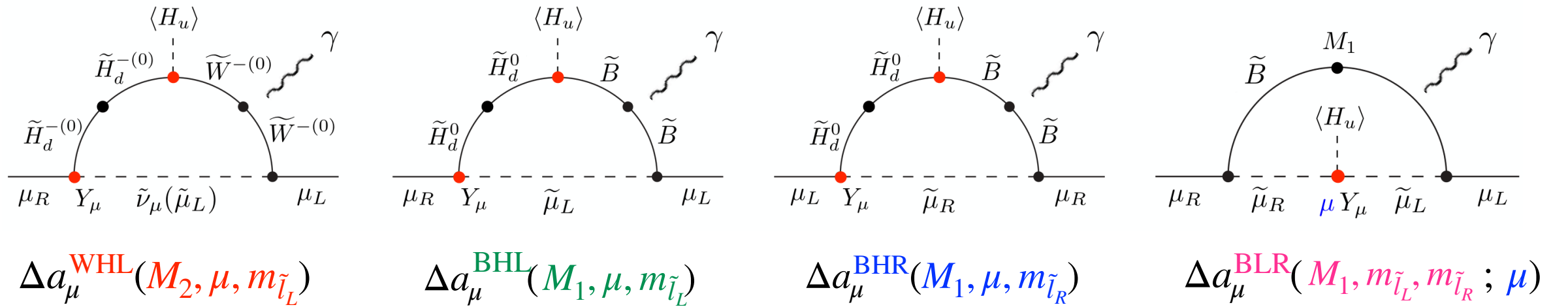
13 TeV

Name	E/TeV	$\mathcal{L}/\text{fb}^{-1}$	Description
atlas_1604_01306	13	3.2	Monophoton
atlas_1605_09318	13	3.3	3 b-jets + 0-1 lepton + MET
atlas_1609_01599	13	36	Monophoton
atlas_1704_03848	13	36	Monophoton
atlas_conf_2015_082	13	3.2	2 leptons (Z) + jets + MET
atlas_conf_2016_013	13	3.2	1 lepton + jets (4 tops, VVL quarks)
atlas_conf_2016_050	13	13.3	1 lepton + (b) jets + MET
atlas_conf_2016_054	13	13.3	1 lepton + (b) jets + MET
atlas_conf_2016_076	13	13.3	2 lepton + jets + MET
atlas_conf_2016_096	13	13.3	Multi-lepton + MET
atlas_conf_2017_060	13	36	Monojet
atlas_conf_2016_066	13	13.3	Photons, jets and MET
atlas_1712_08119	13	36	soft leptons (compressed EWKinos)
atlas_1712_02332	13	36	squarks and gluinos, 0 lepton, 2-6 jets
atlas_1709_04183	13	36	Jets + MET (stops)
atlas_1802_03158	13	36	search for GMSB with photons
atlas_1708_07875	13	36	EWKino search with taus and MET
atlas_1706_03731	13	36	Multilepton + Jets + MET (RPC and RPV)
atlas_1908_08215	13	36	2 leptons + MET (EWKinos)
atlas_1909_08457	13	139	SS lepton + MET (squark, gluino)
atlas_conf_2019_040	13	139	Jets + MET (squark, gluino)
atlas_conf_2019_020	13	139	3 leptons (EWKino)
atlas_1803_02762	13	36	2 or 3 leptons (EWKino)
atlas_conf_2018_041	13	80	Multi- b -jets (stops, sbottoms)
atlas_2101_01629	13	139	1 lepton + jets + MET
atlas_conf_2020_048	13	139	Monojet
atlas_2004_14060	13	139	$t\bar{t}$ + MET
atlas_1908_03122	13	139	Higgs bosons + b -jets + MET
atlas_2103_11684	13	139	4 or more leptons (RPV, GMSB)
atlas_2106_09609	13	139	Multijets + leptons (RPV)
atlas_1911_06660	13	139	Search for Direct Stau Production
cms_pas_sus_15_011	13	2.2	2 leptons + jets + MET
cms_sus_16_039	13	35.9	electrowekinos in multilepton final state
cms_sus_16_025	13	12.9	electroweakino and stop compressed spectra
cms_sus_16_048	13	35.9	two soft opposite sign leptons

8 TeV

Name	E/TeV	$\mathcal{L}/\text{fb}^{-1}$	Description
atlas_1308_1841	8	20.3	0 lepton + ≥ 7 jets + MET
atlas_1308_2631	8	20.1	0 leptons + 2 b-jets + MET
atlas_1402_7029	8	20.3	3 leptons + MET (chargino+neutralino)
atlas_1403_4853	8	20.3	2 leptons + MET (direct stop)
atlas_1403_5222	8	20.3	stop production with Z boson and b-jets
atlas_1404_2500	8	20.3	Same sign dilepton or 3 lepton
atlas_1405_7875	8	20.3	0 lepton + 2-6 jets + MET
atlas_1407_0583	8	20.3	ATLAS, 1 lepton + (b-)jets + MET (stop)
atlas_1407_0608	8	20.3	Monojet or charm jet (stop)
atlas_1411_1559	8	20.3	monophoton plus MET
atlas_1501_07110	8	20.3	1 lepton + 125GeV Higgs + MET
atlas_1502_01518	8	20.3	Monojet + MET
atlas_1503_03290	8	20.3	2 leptons + jets + MET
atlas_1506_08616	8	20.3	di-lepton and 2b-jets + lepton
atlas_1507_05493	8	20.3	photonic signatures of gauge-mediated SUSY
atlas_conf_2012_104	8	20.3	1 lepton + ≥ 4 jets + MET
atlas_conf_2013_024	8	20.3	0 leptons + 6 (2 b-)jets + MET
atlas_conf_2013_049	8	20.3	2 leptons + MET
atlas_conf_2013_061	8	20.3	0-1 leptons + ≥ 3 b-jets + MET
atlas_conf_2013_089	8	20.3	2 leptons (razor)
atlas_conf_2015_004	8	20.3	invisible Higgs decay in VBF
atlas_1403_5294	8	20.3	2 leptons + MET, (SUSY electroweak)
atlas_higg_2013_03	8	20.3	2 leptons + MET, (invisible Higgs)
atlas_1502_05686	8	20.3	search for massive sparticles decaying to many jets
cms_1303_2985	8	11.7	α_T + b-jets
cms_1408_3583	8	19.7	monojet + MET
cms_1502_06031	8	19.4	2 leptons, jets, MET (only on-Z)
cms_1504_03198	8	19.7	1 lepton, ≥ 3 jets, ≥ 1 b-jet, MET (DM + 2 top)
cms_sus_13_016	8	19.5	OS lepton 3+ b-tags

Parameter planes



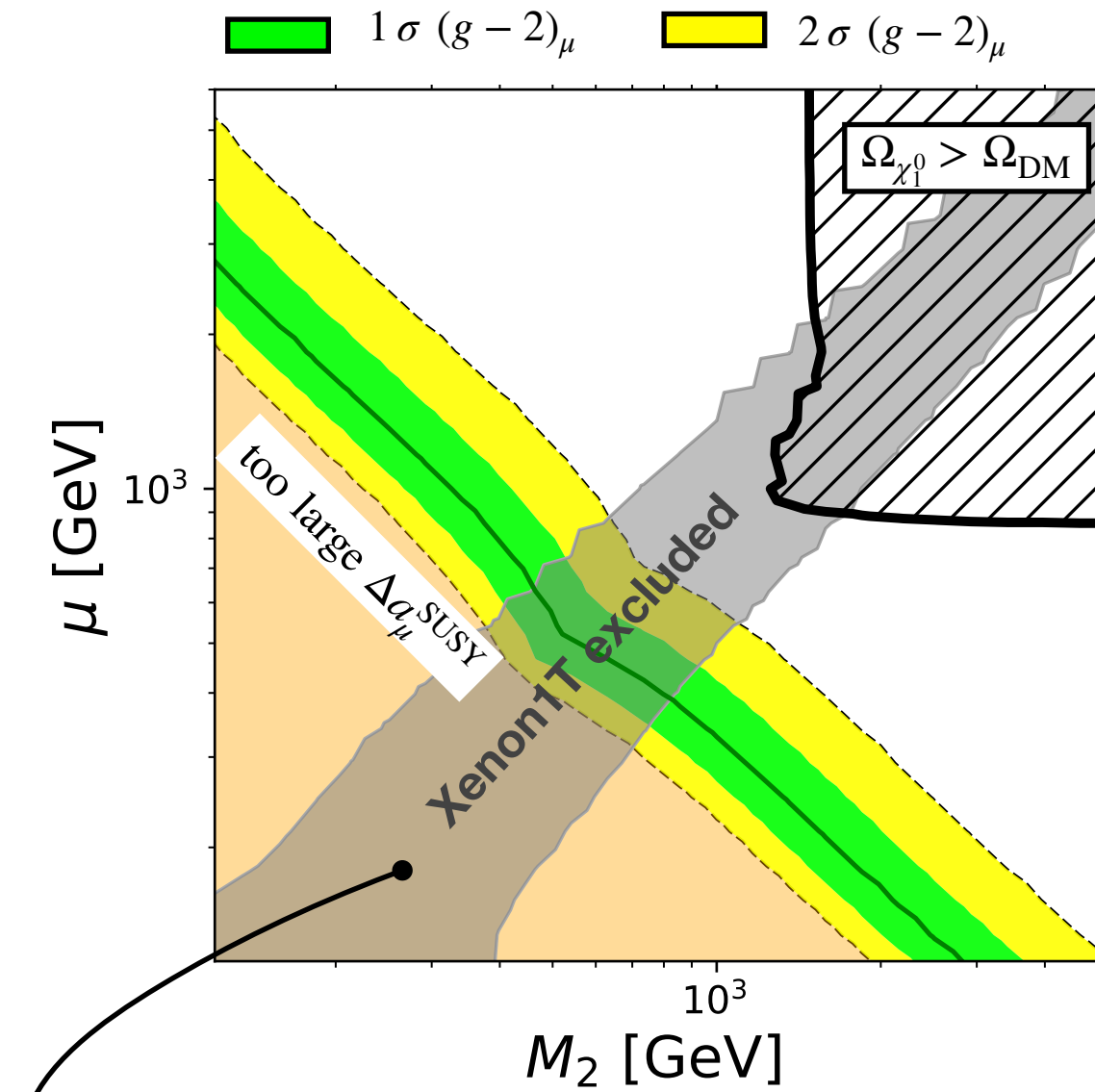
2D planes

name	axes	other parameters	$\tan \beta$
WHL	(M_2, μ)	$\tilde{m}_{l_L} = \min(M_2, \mu) + 20 \text{ GeV}$, $M_1 = \tilde{m}_{l_R} = 10 \text{ TeV}$	50
BHL	(M_1, μ)	$\tilde{m}_{l_L} = \min(M_1, \mu) + 20 \text{ GeV}$, $M_2 = \tilde{m}_{l_R} = 10 \text{ TeV}$	50
BHR	(M_1, μ)	$\tilde{m}_{l_R} = \min(M_1, \mu) + 20 \text{ GeV}$, $M_2 = \tilde{m}_{l_L} = 10 \text{ TeV}$	50
BLR	$(\tilde{m}_{l_L}, \tilde{m}_{l_R})$	$M_1 = m_{\tilde{\tau}_1} - 20 \text{ GeV}$, $\mu = \mu_{\text{max}}$, $M_2 = 10 \text{ TeV}$	50

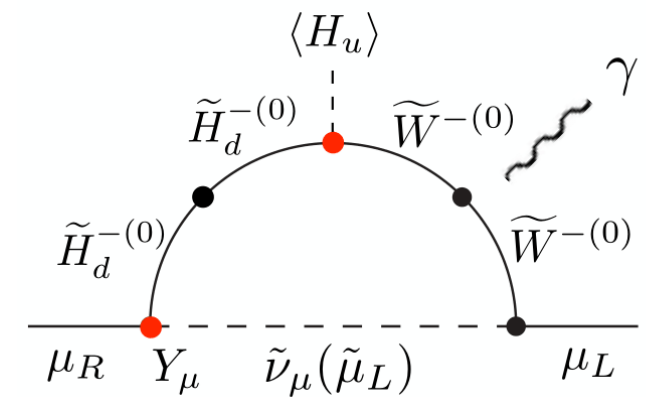
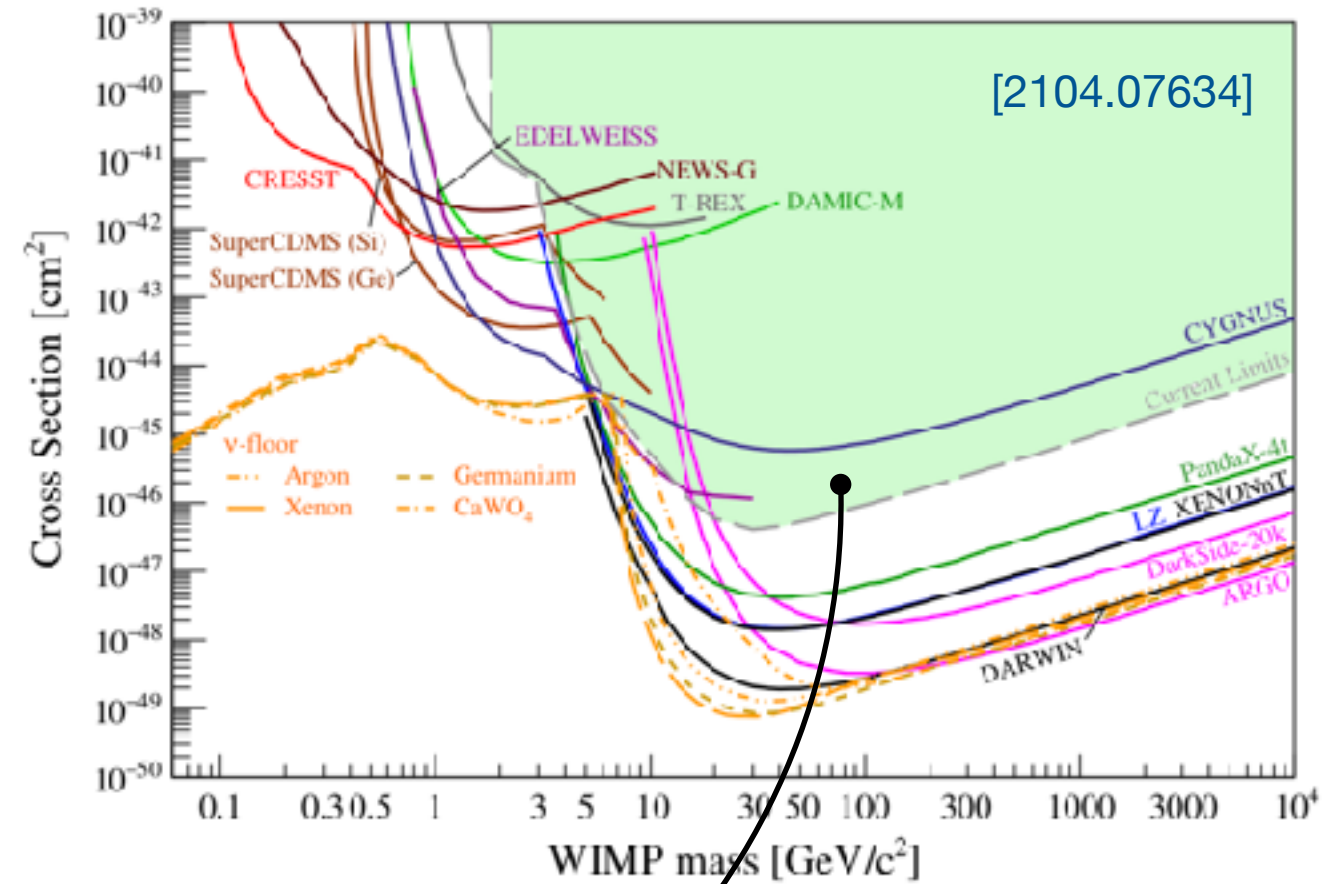
WHL (MSSM)

$$m_{\tilde{l}_L} = \min(M_2, \mu) + 20 \text{ GeV}$$

$$\tan \beta = 50, \quad M_1 = m_{\tilde{l}_R} = 10 \text{ TeV}$$



$$\sigma_{\chi N \rightarrow \chi N}^{\text{SI}}(m_{\tilde{\chi}_1^0}) \cdot \frac{\Omega_{\tilde{\chi}_1^0}}{\Omega_{\text{DM}}} > \sigma_{\text{Xenon1T}}^{\text{SI}}(m_{\text{DM}})$$

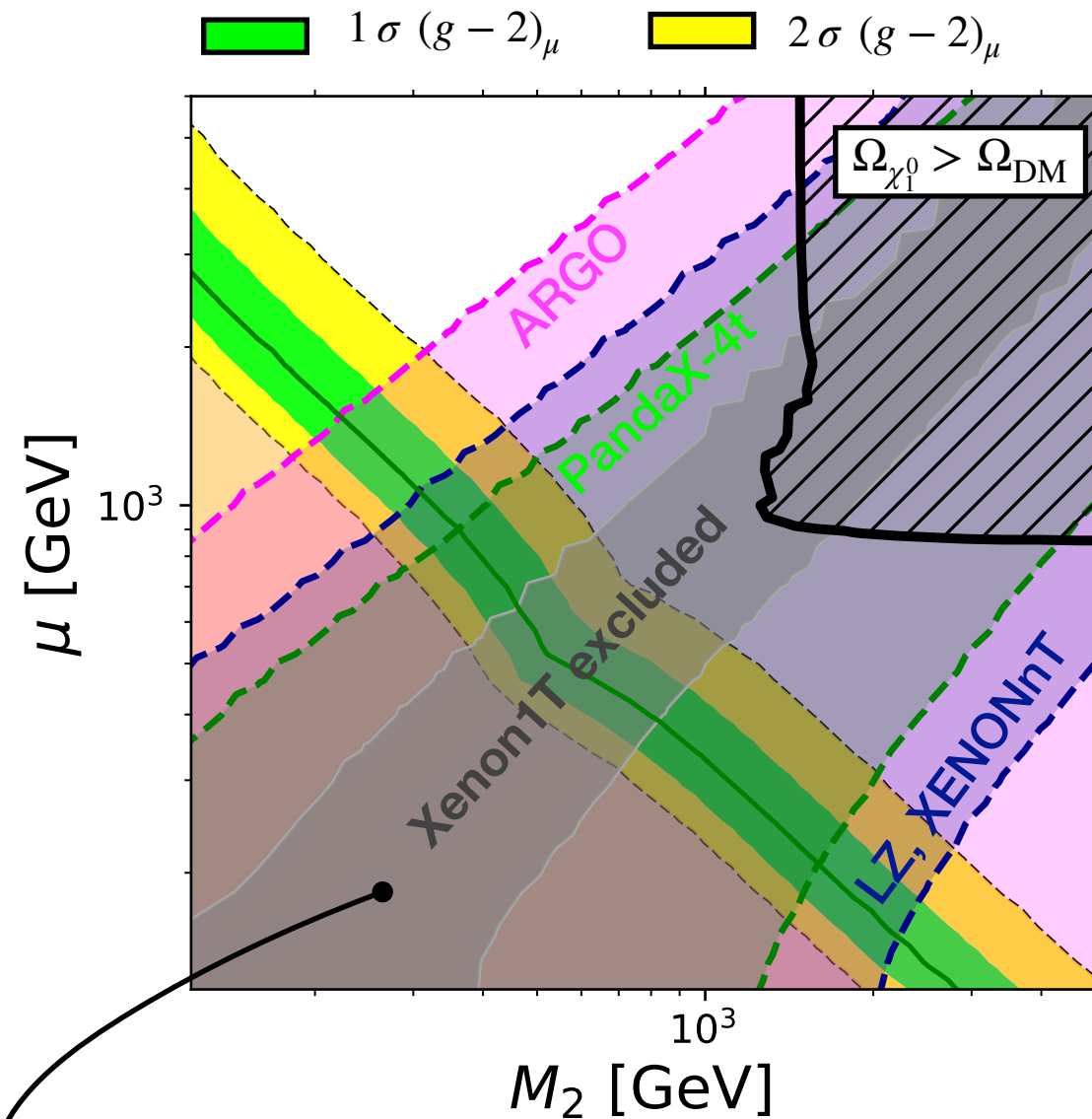


WHL

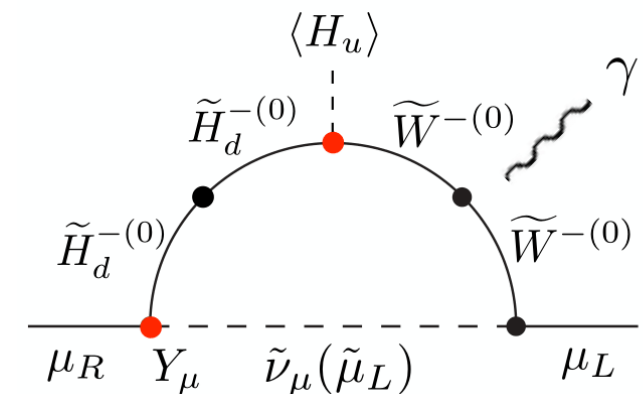
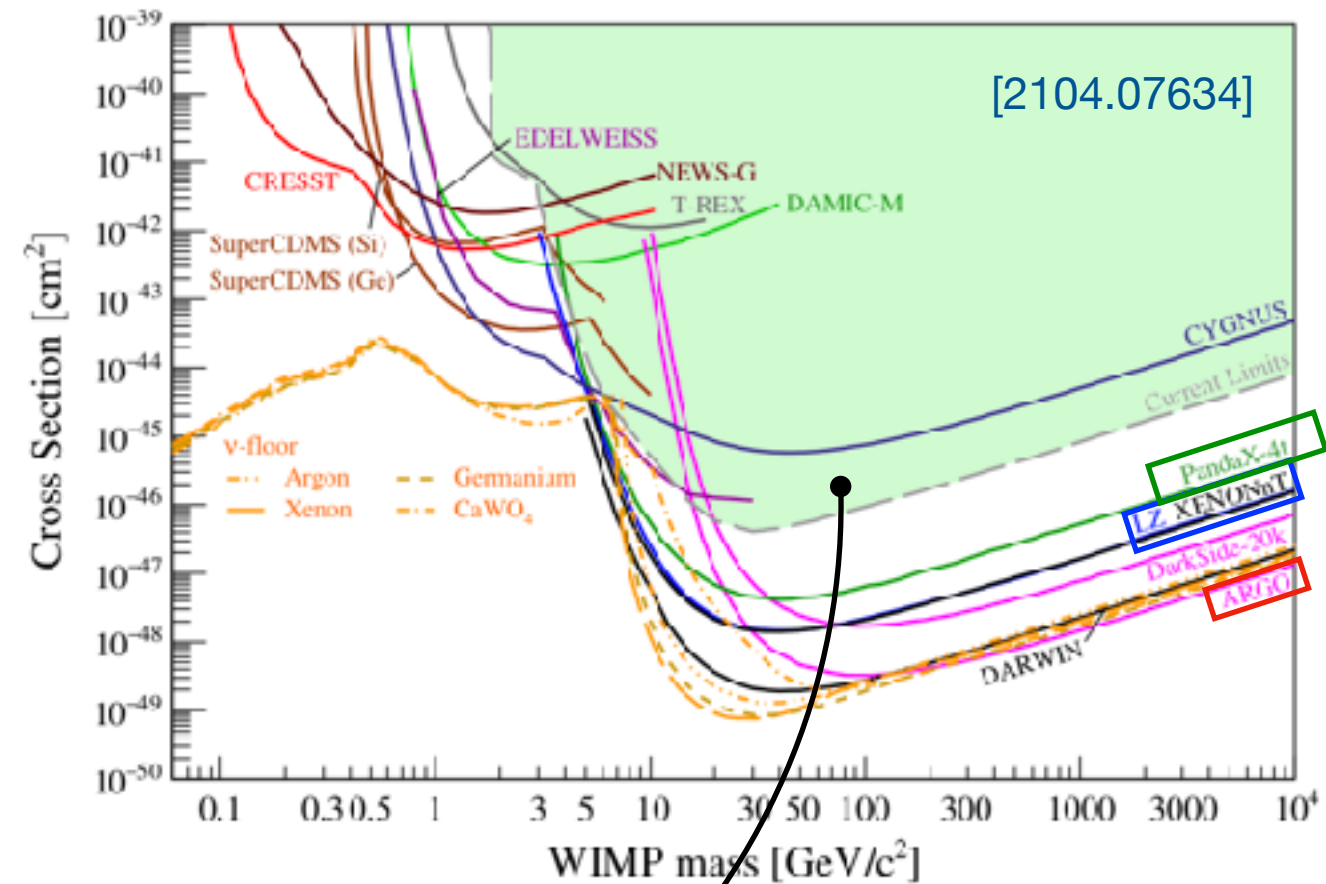
WHL (MSSM, **future DM-DD**)

$$m_{\tilde{l}_L} = \min(M_2, \mu) + 20 \text{ GeV}$$

$$\tan \beta = 50, \quad M_1 = m_{\tilde{l}_R} = 10 \text{ TeV}$$

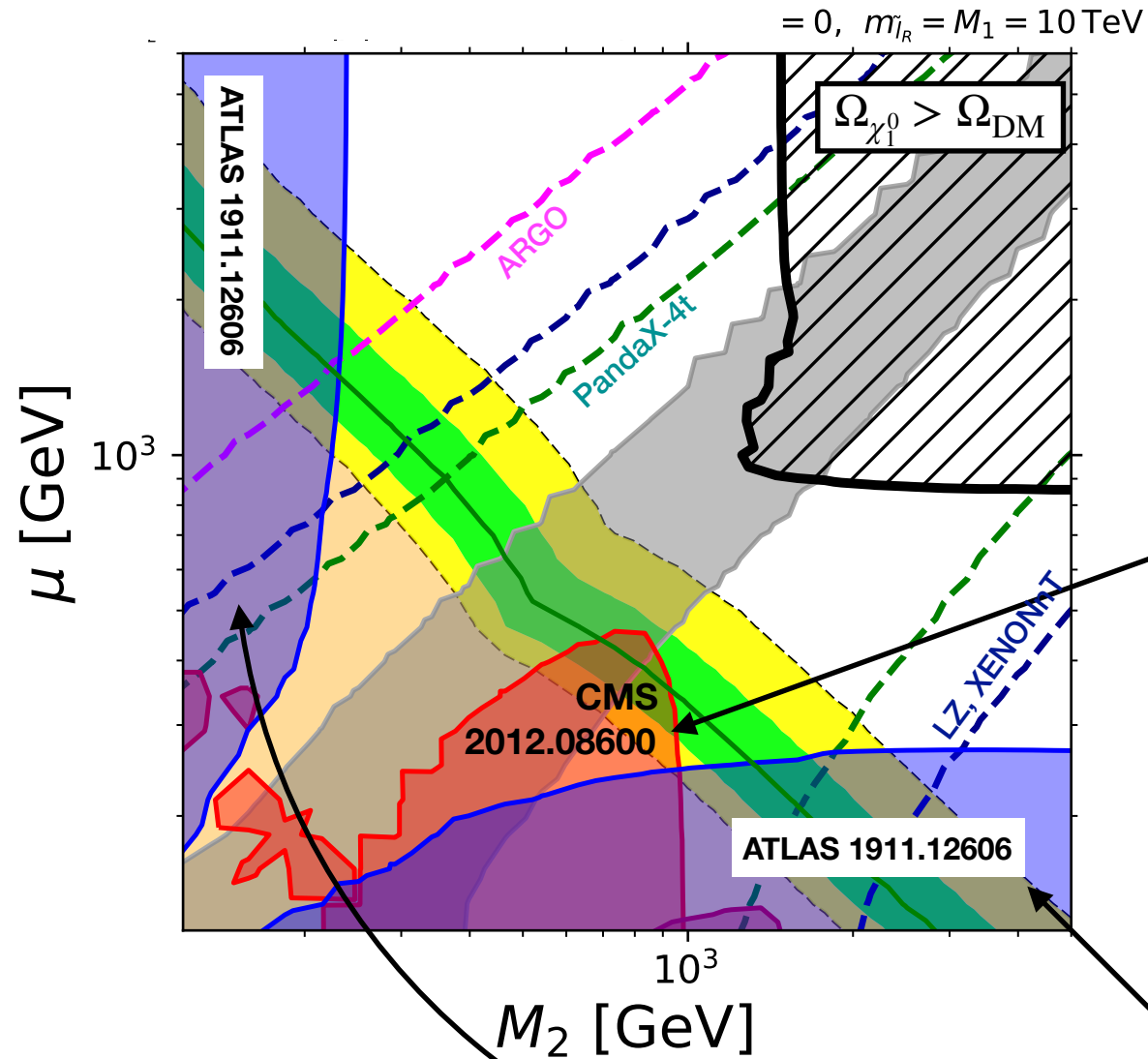


$$\sigma_{\chi N \rightarrow \chi N}^{\text{SI}}(m_{\tilde{\chi}_1^0}) \cdot \frac{\Omega_{\tilde{\chi}_1^0}}{\Omega_{\text{DM}}} > \sigma_{\text{Xenon1T}}^{\text{SI}}(m_{\text{DM}})$$



WHL

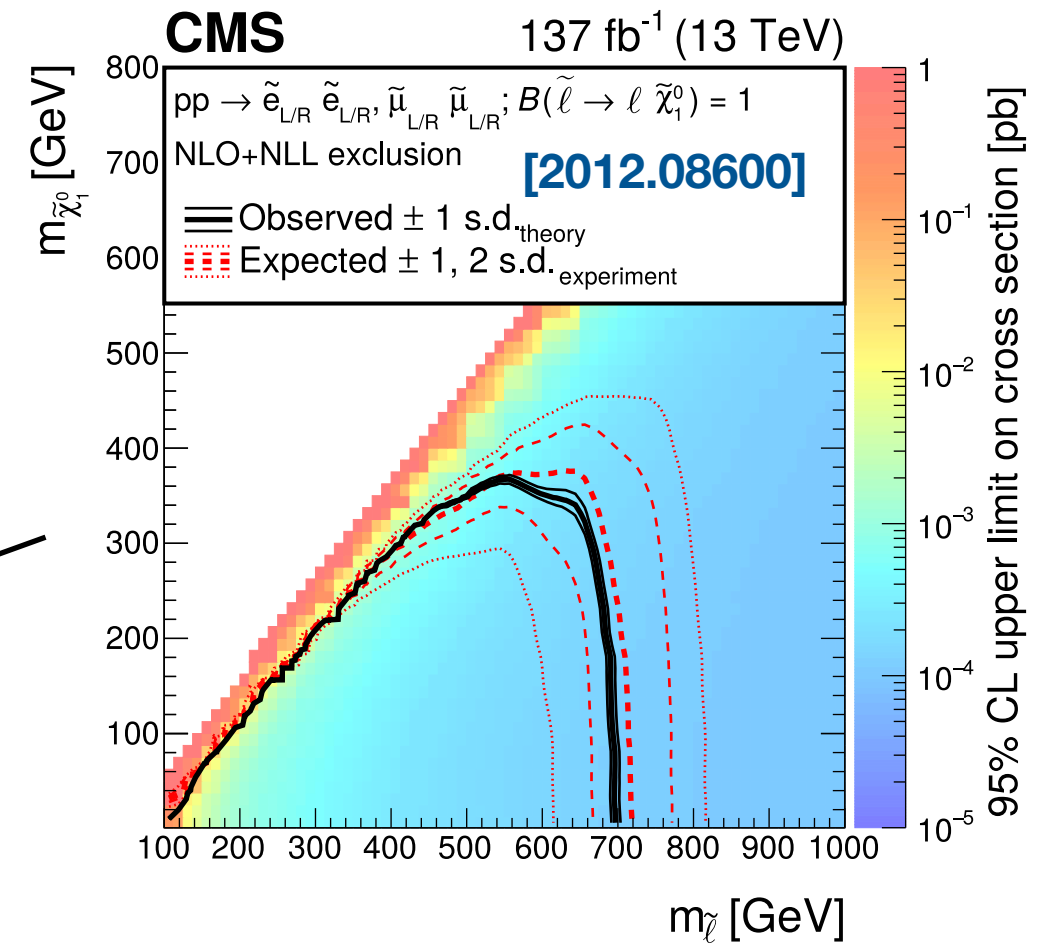
WHL (MSSM, LHC)



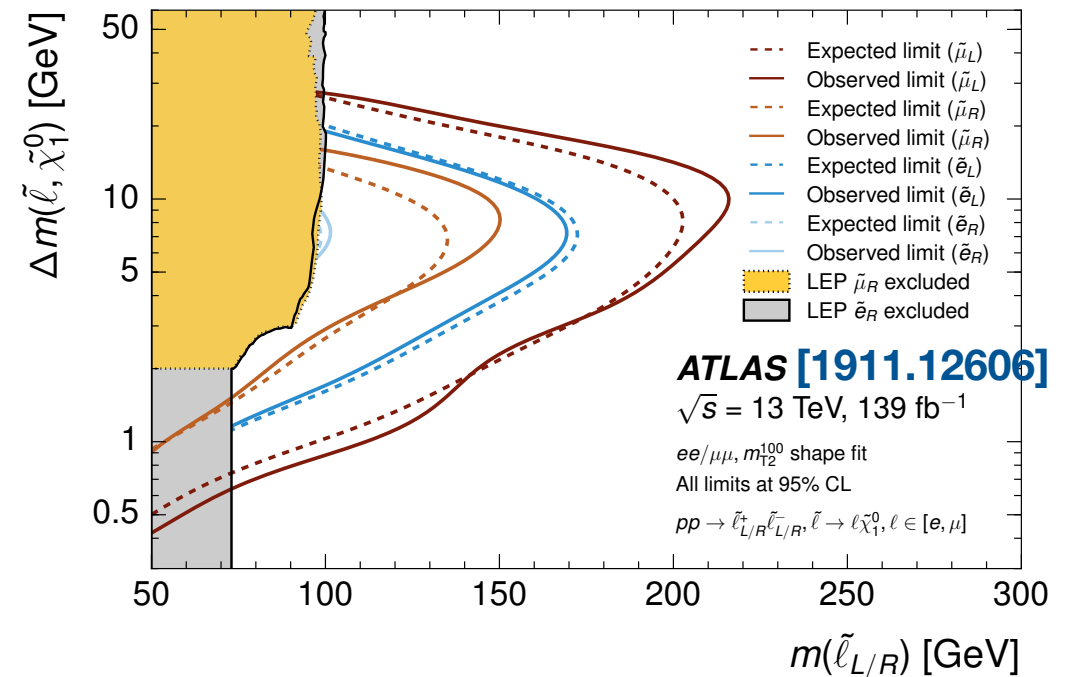
$$m_{\tilde{l}_L} = \min(M_2, \mu) + 20 \text{ GeV}$$

$$\tan \beta = 50, M_1 = m_{\tilde{l}_R} = 10 \text{ TeV}$$

$$pp \rightarrow \widetilde{W}\widetilde{W}, \widetilde{W}^{0,\pm} \rightarrow \ell + (\tilde{\ell}, \tilde{\nu})$$



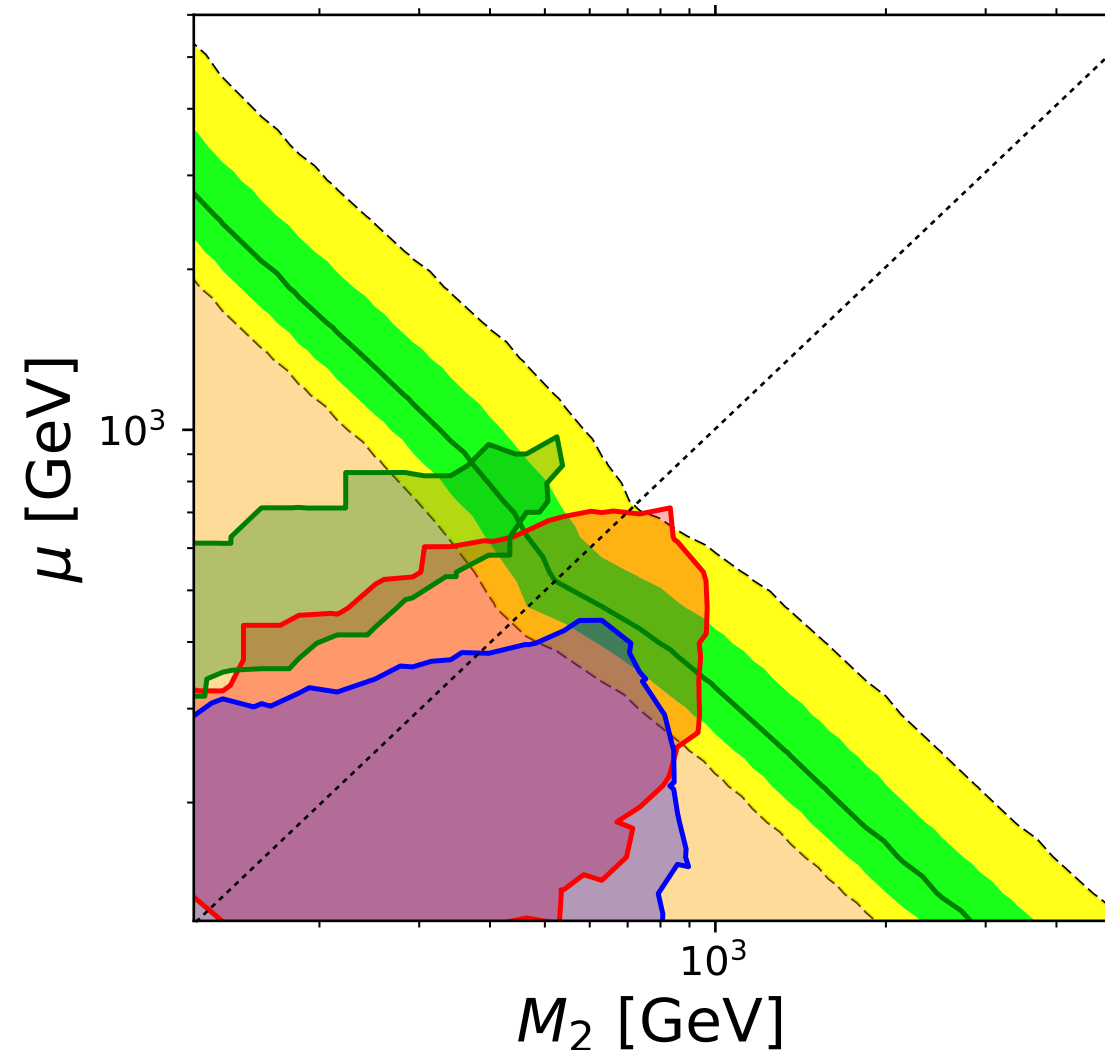
$$pp \rightarrow \tilde{\ell}\tilde{\ell}, \tilde{\ell} \rightarrow \ell + \tilde{\chi}_1^0$$



WHL (RPV UDD)

$$m_{\tilde{l}_L} = \min(M_2, \mu) + 20 \text{ GeV}$$

$$\tan \beta = 50, \quad M_1 = m_{\tilde{l}_R} = 10 \text{ TeV}$$

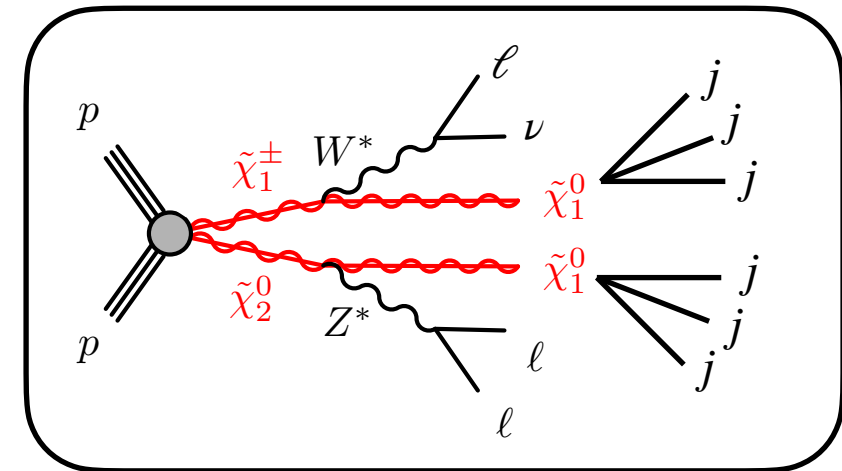


RPV ATLAS13 139/fb [2106.09609]

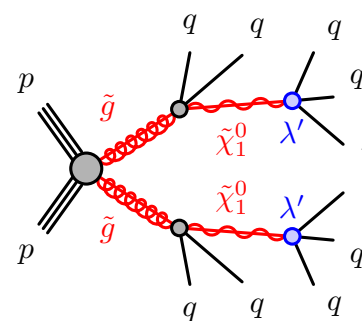
Multi & SS-leptons CMS13 36/fb [1709.05406]

Multijet ATLAS13 139/fb [2106.09609]

$$pp \rightarrow W^\pm W^{0,\mp}, \quad \tilde{h}^{0,\pm} \tilde{h}^{0,\mp}$$



soft lepton + multi-jet final state



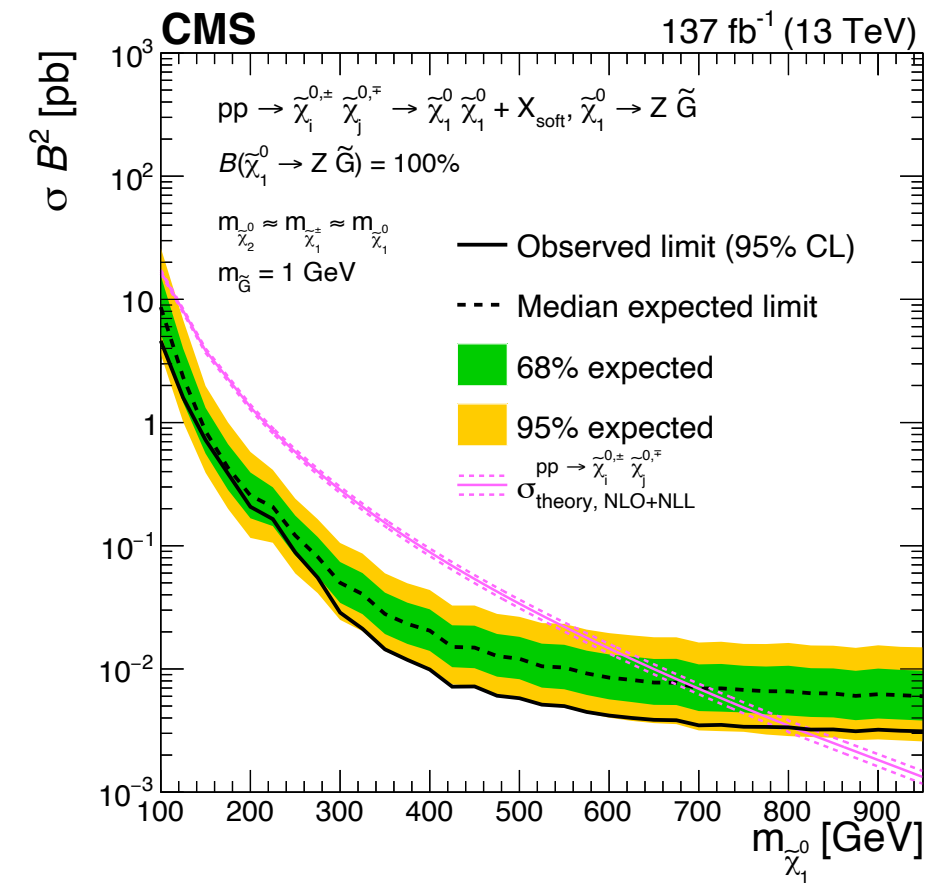
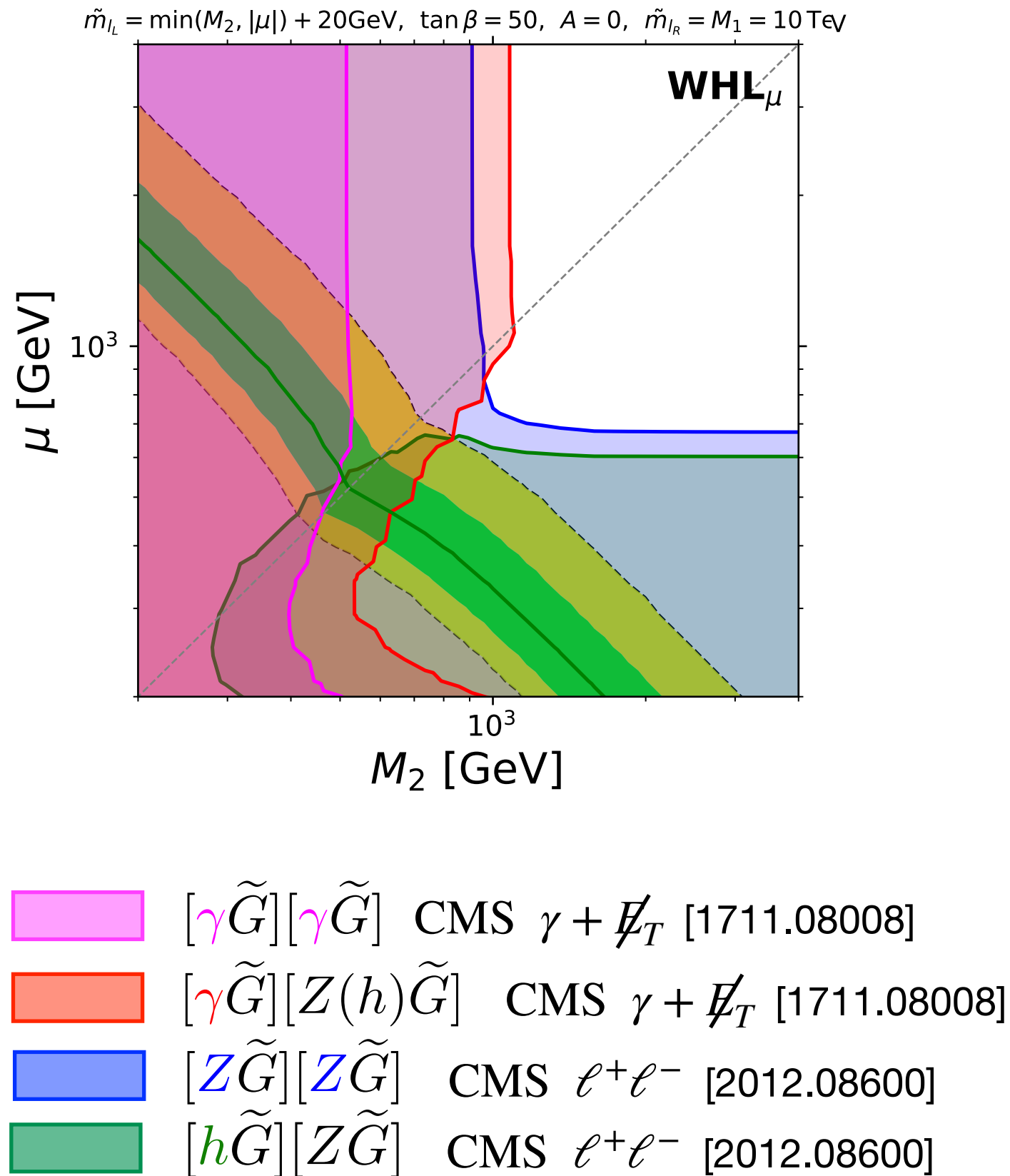
**More g-2 region available
due to absence of DM
constraints**

Bin	Final state	Definition
1	2 SS leptons	0 jets, $M_T > 100 \text{ GeV}$ and $p_T^{\text{miss}} > 140 \text{ GeV}$
2	2 SS leptons	1 jet, $M_T < 100 \text{ GeV}$, $p_T^{\ell\ell} < 100 \text{ GeV}$ and $p_T^{\text{miss}} > 200 \text{ GeV}$
3	3 light leptons	$M_T > 120 \text{ GeV}$ and $p_T^{\text{miss}} > 200 \text{ GeV}$
4	3 light leptons	$p_T^{\text{miss}} > 250 \text{ GeV}$
5	2 light leptons and 1 tau	$M_{T2}(\ell_1, \tau) > 50 \text{ GeV}$ and $p_T^{\text{miss}} > 200 \text{ GeV}$
6	1 light lepton and 2 taus	$M_{T2}(\ell, \tau_1) > 50 \text{ GeV}$ and $p_T^{\text{miss}} > 200 \text{ GeV}$
7	1 light lepton and 2 taus	$p_T^{\text{miss}} > 75 \text{ GeV}$
8	more than 3 leptons	$p_T^{\text{miss}} > 200 \text{ GeV}$

WHL (Gravitino LSP)

$$m_{\tilde{l}_L} = \min(M_2, \mu) + 20 \text{ GeV}$$

$$\tan \beta = 50, \quad M_1 = m_{\tilde{l}_R} = 10 \text{ TeV}$$



MSSM

BHL

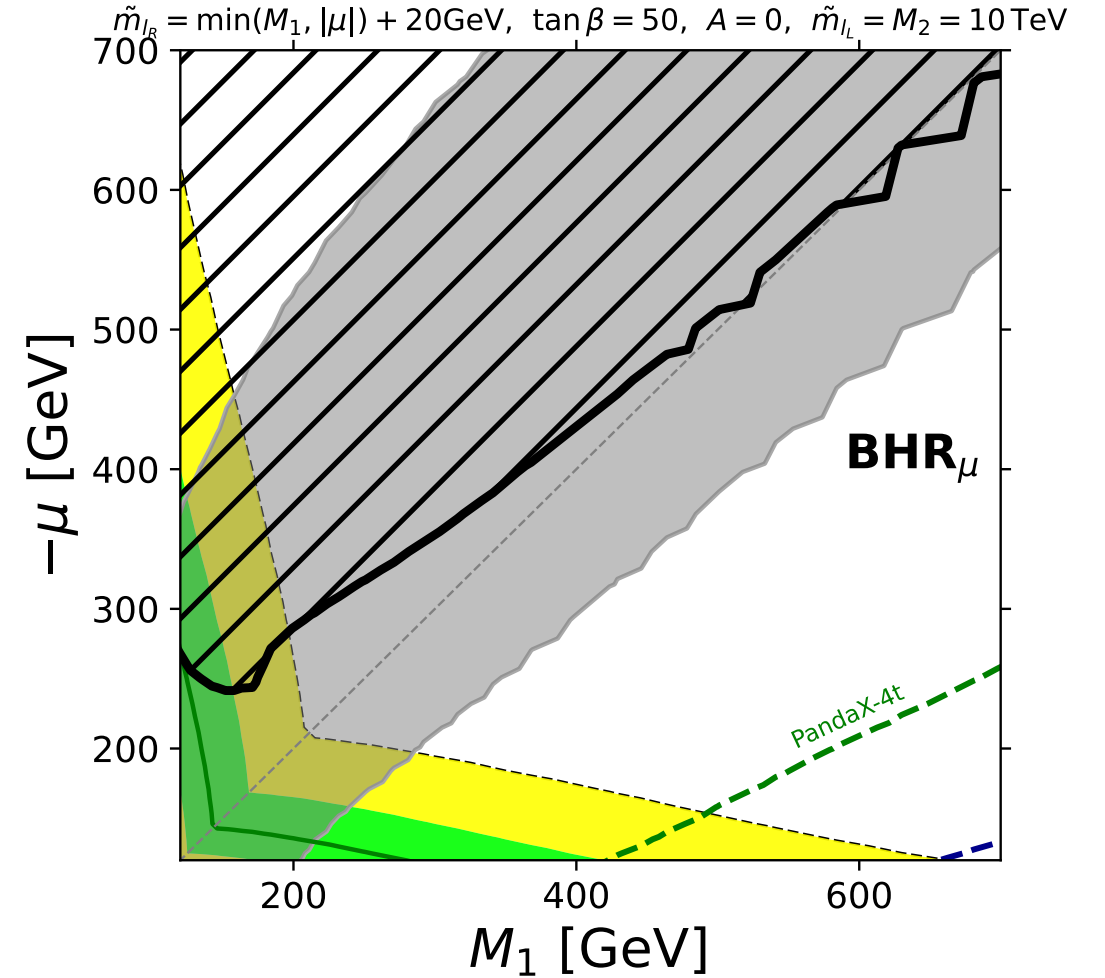
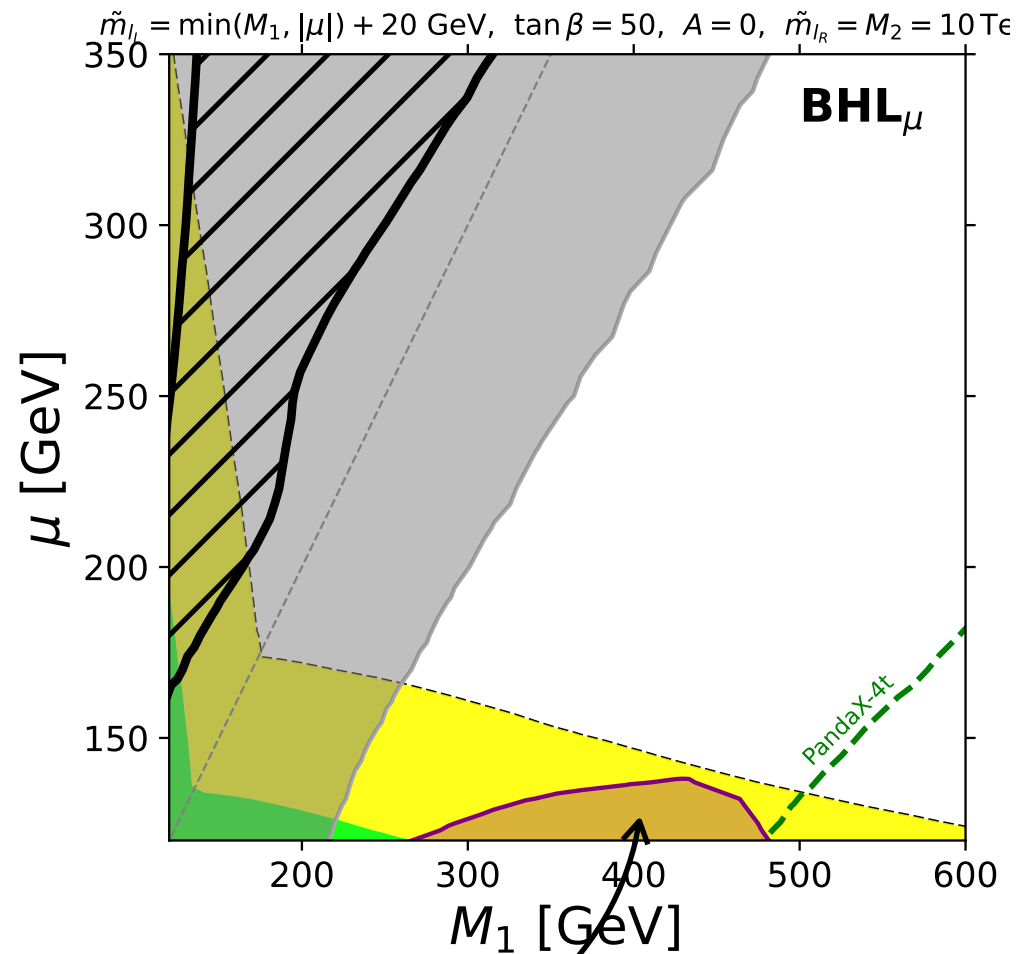
$$m_{\tilde{l}_L} = \min(M_1, \mu) + 20 \text{ GeV}$$

$$\tan \beta = 50, \quad M_2 = m_{\tilde{l}_R} = 10 \text{ TeV}$$

BHR

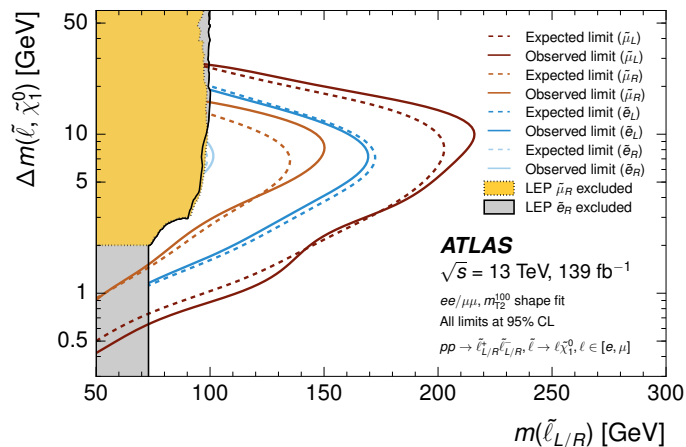
$$m_{\tilde{l}_R} = \min(M_1, |\mu|) + 20 \text{ GeV}$$

$$\tan \beta = 50, \quad M_2 = m_{\tilde{l}_L} = 10 \text{ TeV}$$



[1911.12606]

$$pp \rightarrow \tilde{\ell}\tilde{\ell}, \quad \tilde{\ell} \rightarrow \ell + \tilde{\chi}_1^0$$



- Large regions are excluded by $\Omega_{\tilde{\chi}_1^0} > \Omega_{\text{DM}}$ and DM-DD.
- Future DM-DD experiments will explore the entire region
- LHC limits very weak

RPV

BHL

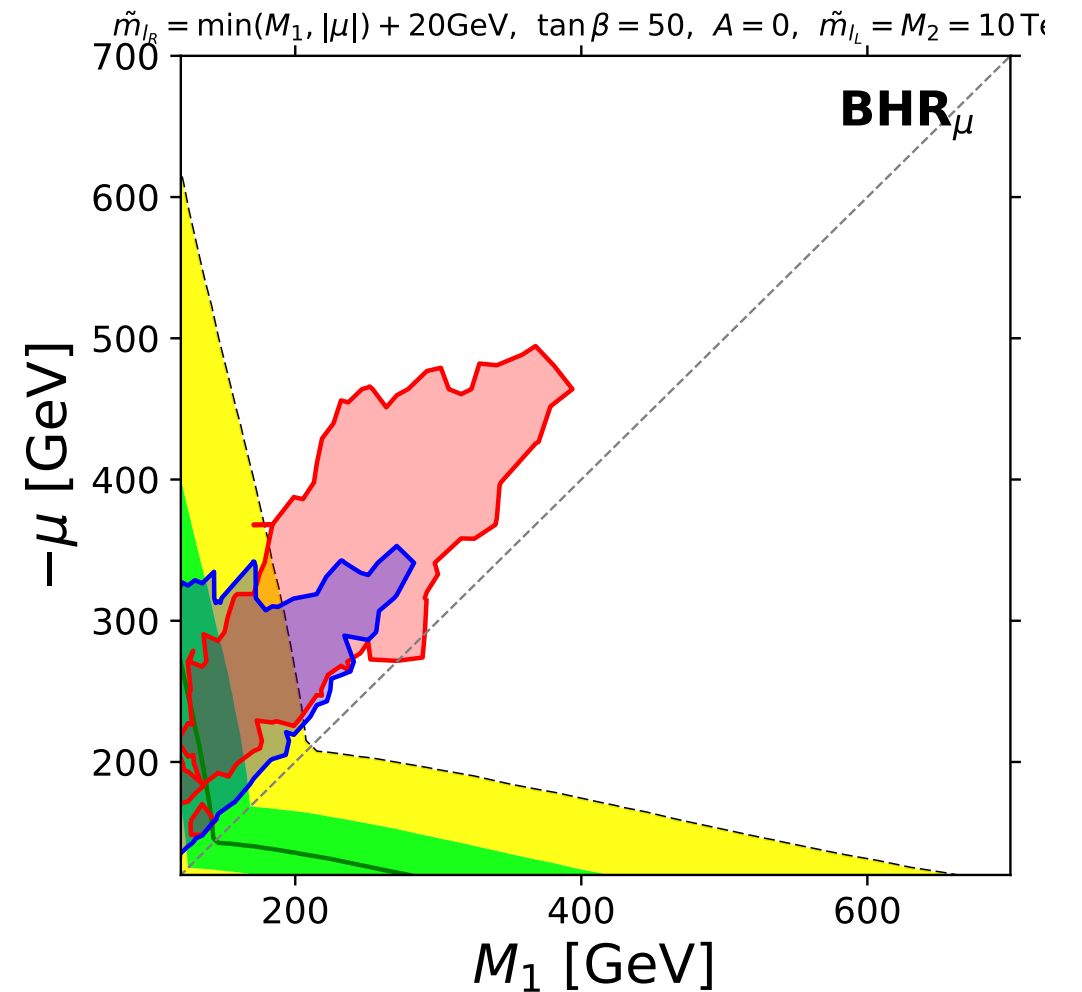
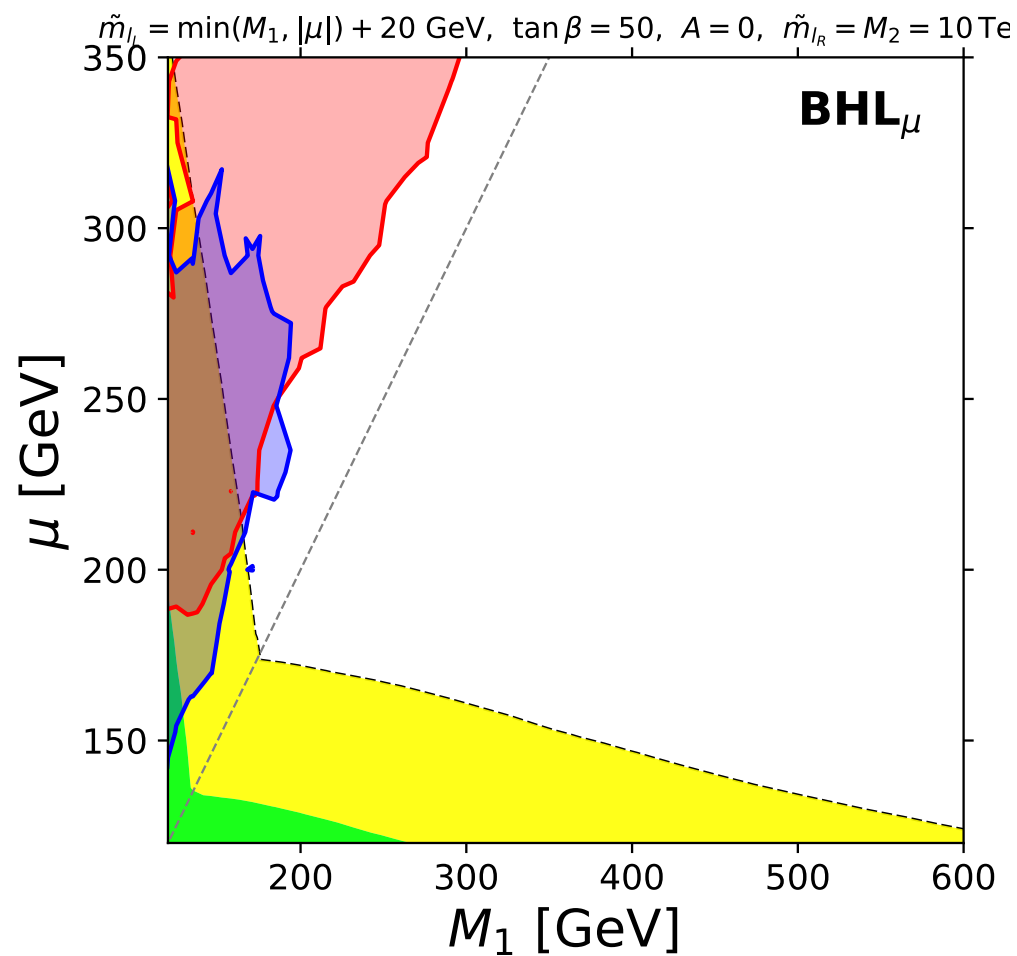
$$m_{\tilde{l}_L} = \min(M_1, \mu) + 20 \text{ GeV}$$

$$\tan \beta = 50, \quad M_2 = m_{\tilde{l}_R} = 10 \text{ TeV}$$

BHR

$$m_{\tilde{l}_R} = \min(M_1, |\mu|) + 20 \text{ GeV}$$

$$\tan \beta = 50, \quad M_2 = m_{\tilde{l}_L} = 10 \text{ TeV}$$



RPV ATLAS13 139/fb [2106.09609]



Multi & SS-leptons CMS13 36/fb [1709.05406]

⦿ **Stronger LHC limits**

⦿ **More g-2 region available**

Gravitino LSP

BHL

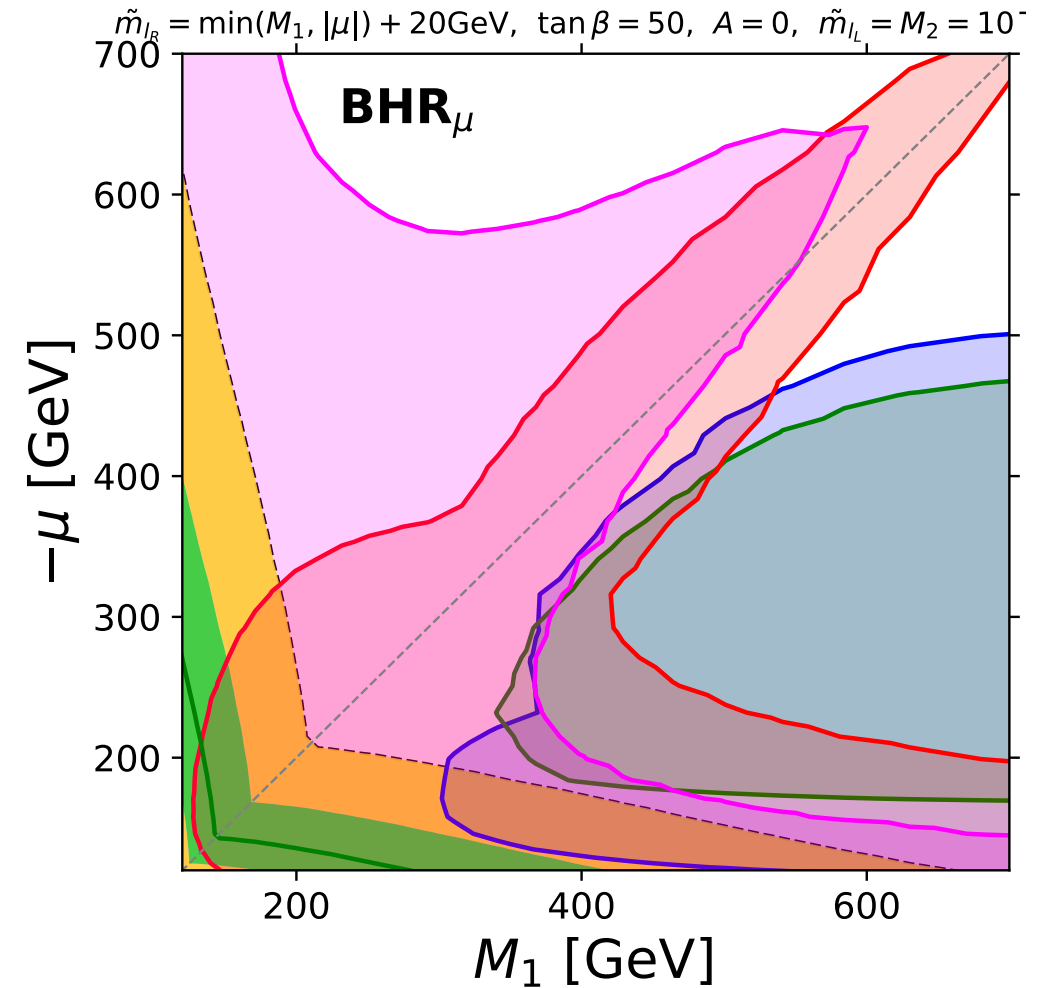
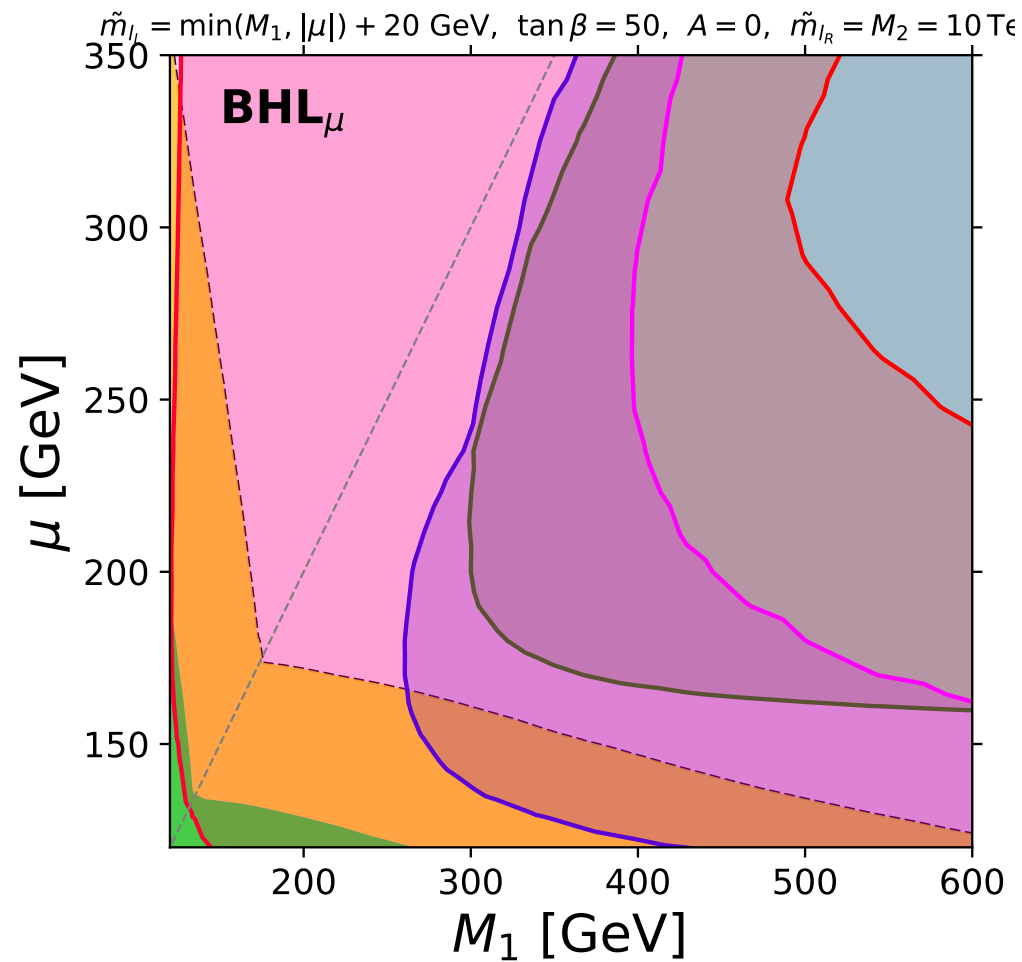
$$m_{\tilde{l}_L} = \min(M_1, \mu) + 20 \text{ GeV}$$

$$\tan \beta = 50, \quad M_2 = m_{\tilde{l}_R} = 10 \text{ TeV}$$

BHR

$$m_{\tilde{l}_R} = \min(M_1, |\mu|) + 20 \text{ GeV}$$

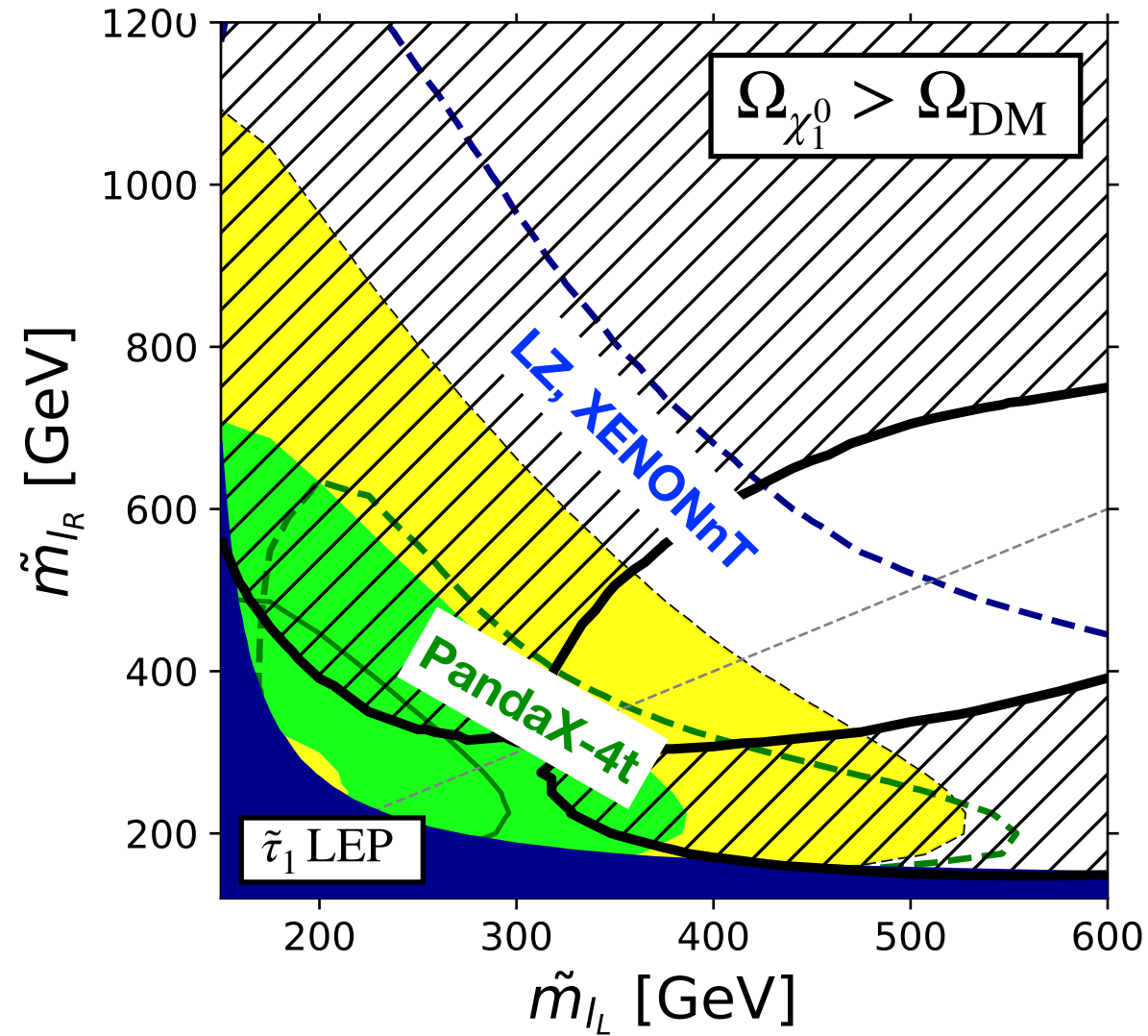
$$\tan \beta = 50, \quad M_2 = m_{\tilde{l}_L} = 10 \text{ TeV}$$



- $[\gamma \tilde{G}][\gamma \tilde{G}]$ CMS $\gamma + \cancel{E}_T$ [1711.08008]
- $[\gamma \tilde{G}][Z(h) \tilde{G}]$ CMS $\gamma + \cancel{E}_T$ [1711.08008]
- $[Z \tilde{G}][Z \tilde{G}]$ CMS $\ell^+ \ell^-$ [2012.08600]
- $[h \tilde{G}][Z \tilde{G}]$ CMS $\ell^+ \ell^-$ [2012.08600]

BLR

MSSM

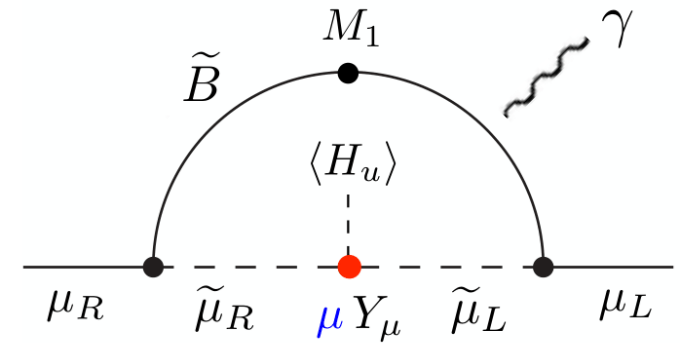


$$M_1 = m_{\tilde{\tau}_1} - 20 \text{ GeV}, \quad M_2 = 10 \text{ TeV}$$

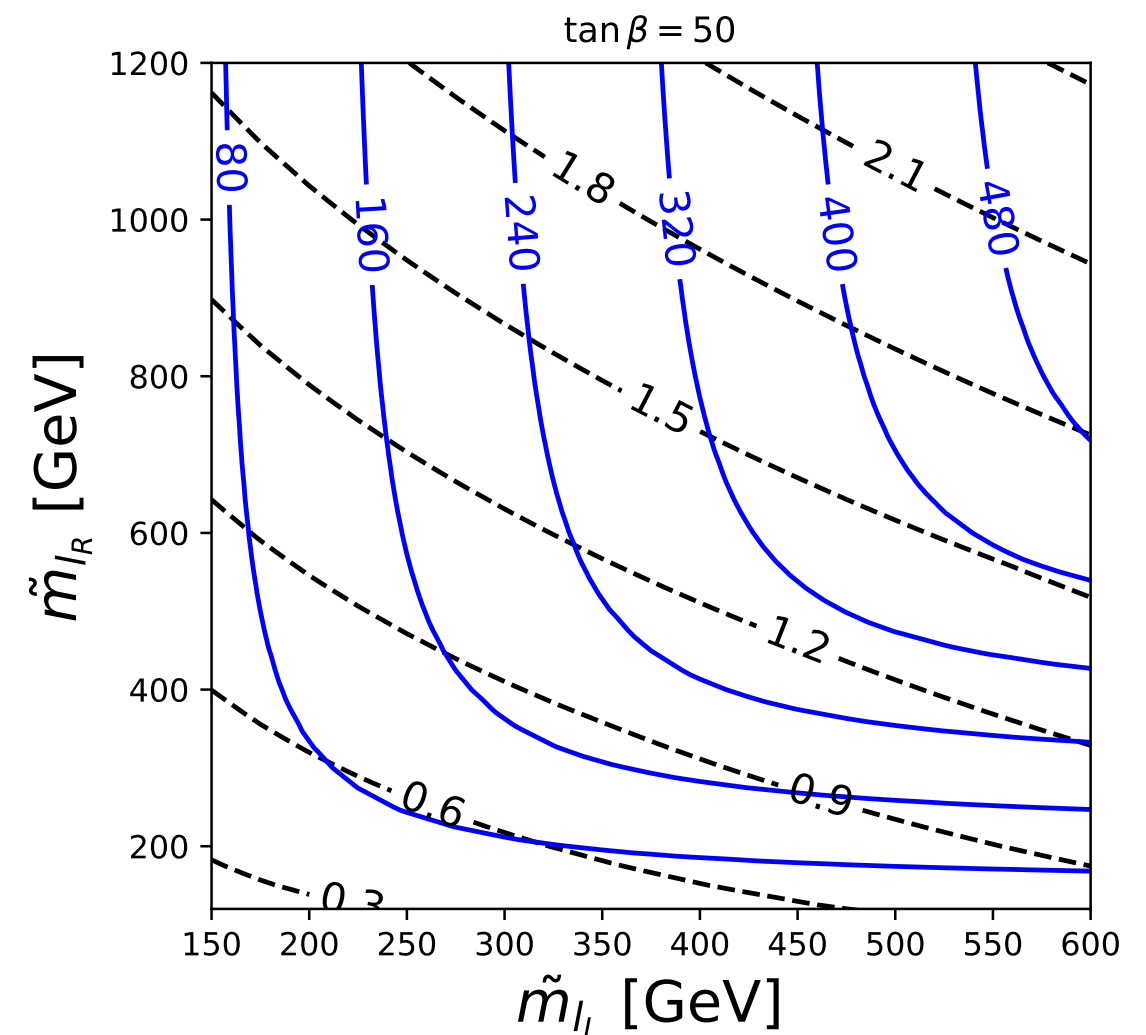
$$\mu = \mu_{\text{max}}, \quad \tan \beta = 50$$

maximum allowed by
vacuum (meta-)stability

$$\Delta a_\mu^{\text{BLR}}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu)$$

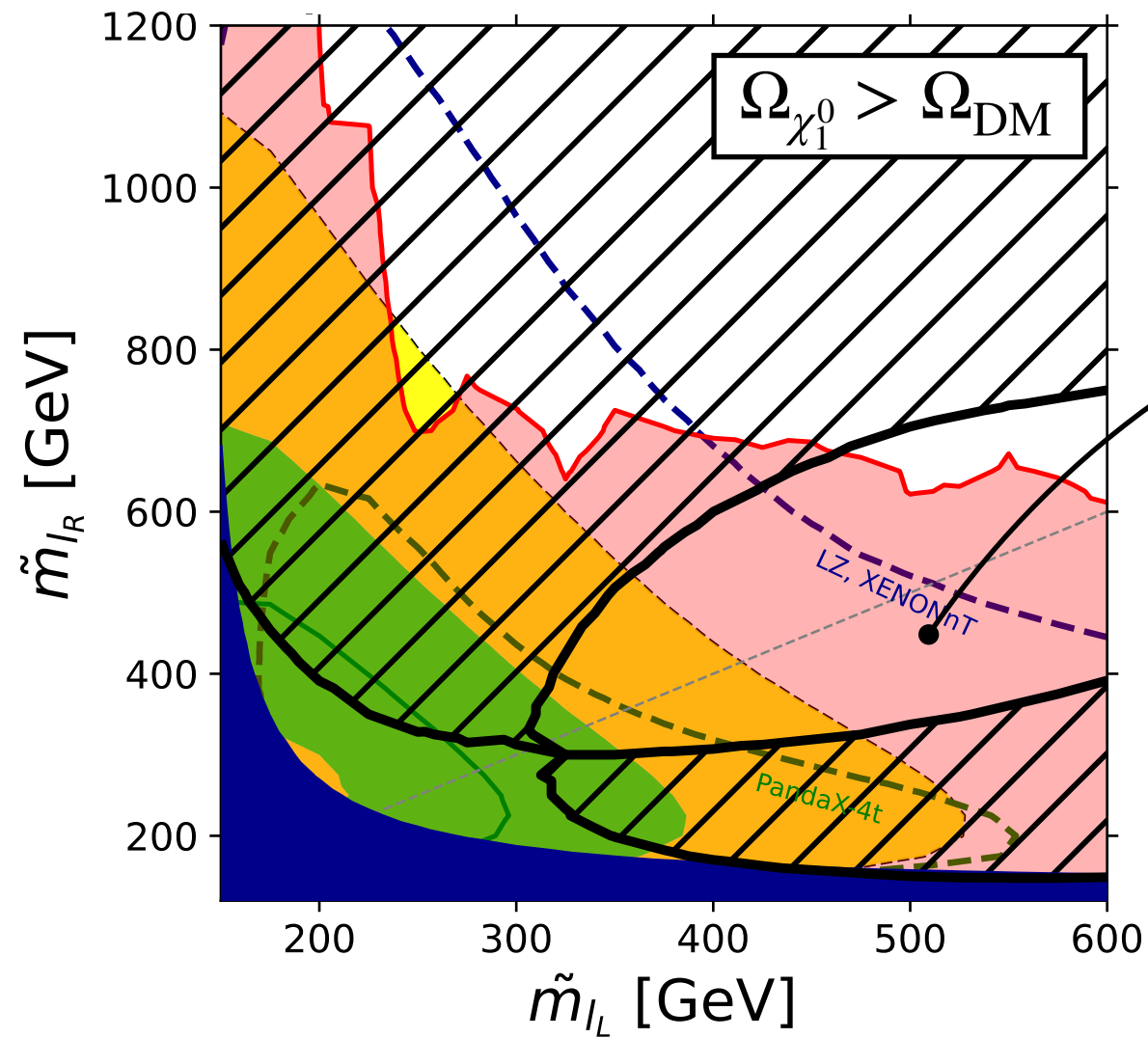


$$\mu / \text{TeV}, \quad M_1 / \text{GeV}$$



BLR

MSSM

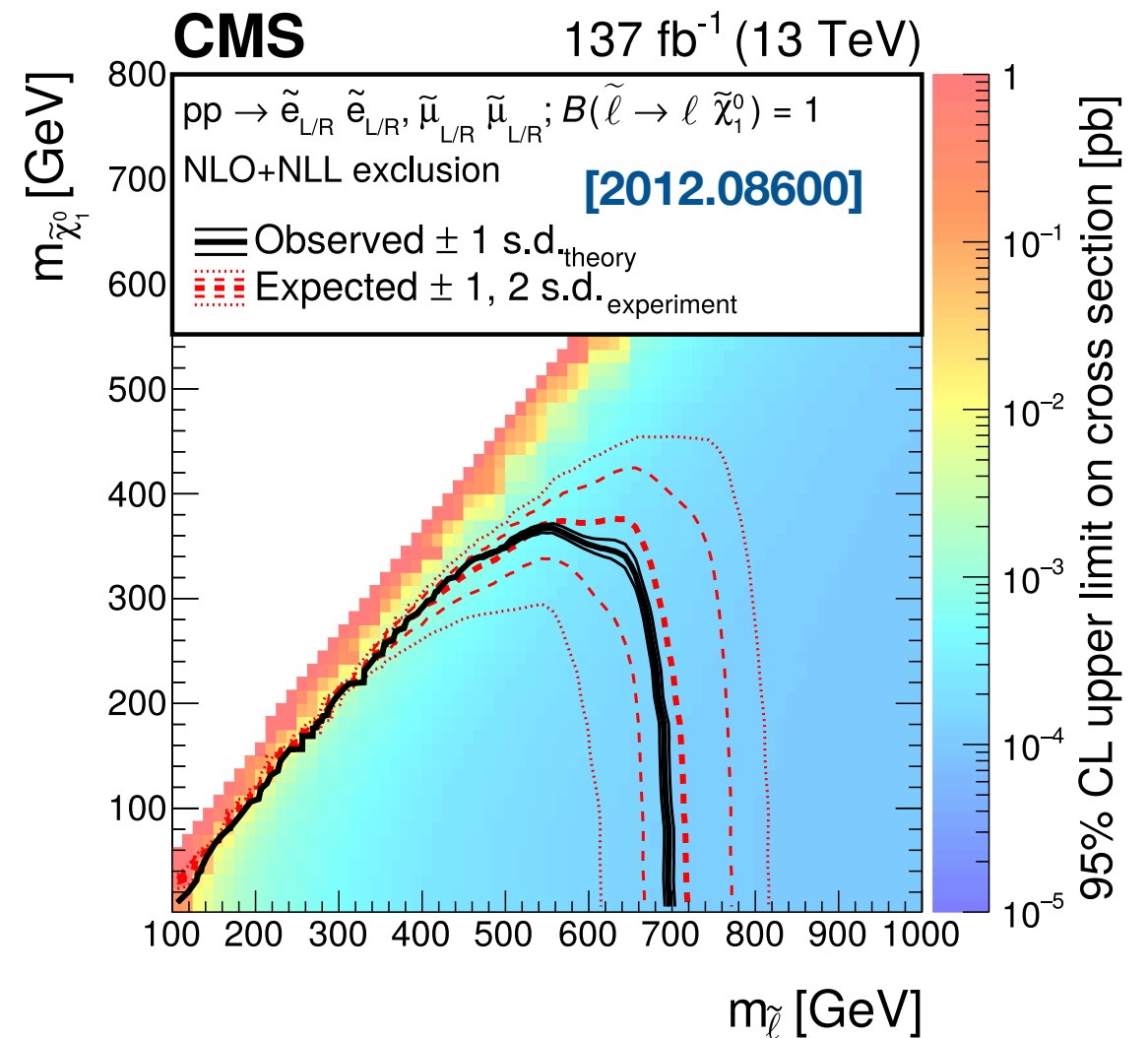
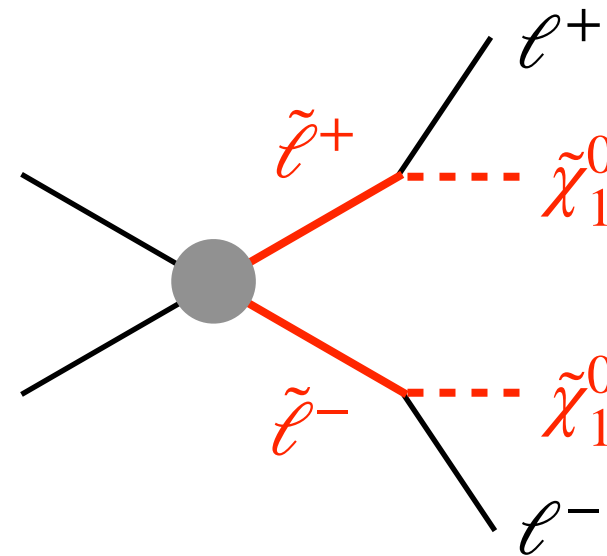


$$M_1 = m_{\tilde{\tau}_1} - 20 \text{ GeV}, \quad M_2 = 10 \text{ TeV}$$

$$\mu = \mu_{\text{max}}, \quad \tan \beta = 50$$

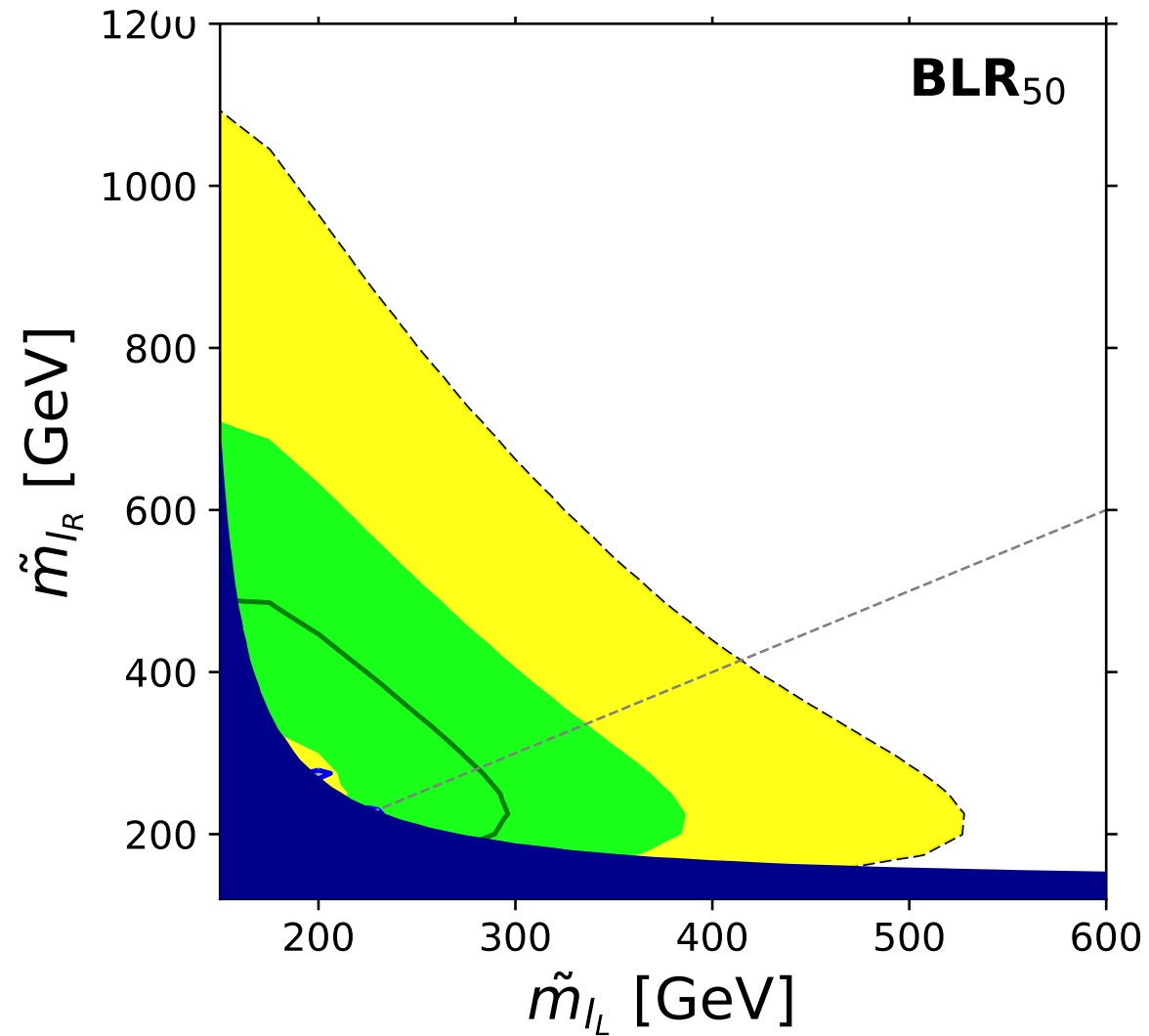
maximum allowed by
vacuum (meta-)stability

$$\Delta a_\mu^{\text{BLR}}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu)$$



BLR

RPV

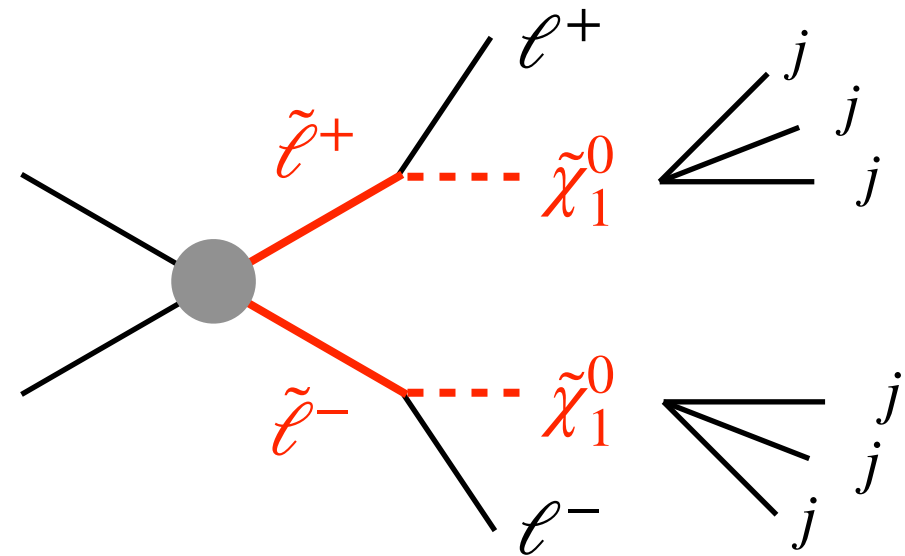


$$M_1 = m_{\tilde{\tau}_1} - 20 \text{ GeV}, \quad M_2 = 10 \text{ TeV}$$

$$\mu = \mu_{\text{max}}, \quad \tan \beta = 50$$

maximum allowed by
vacuum (meta-)stability

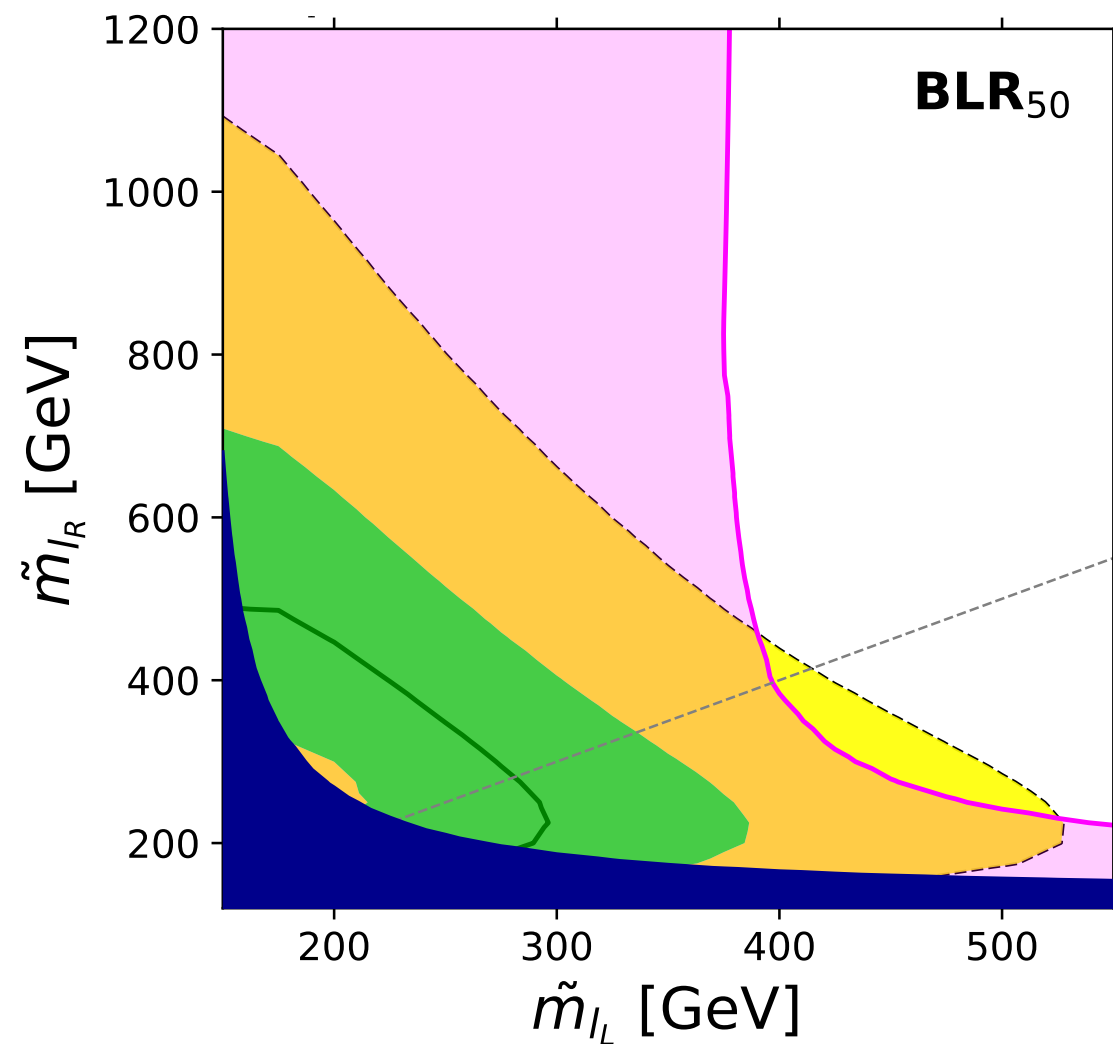
$$\Delta a_\mu^{\text{BLR}}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu)$$



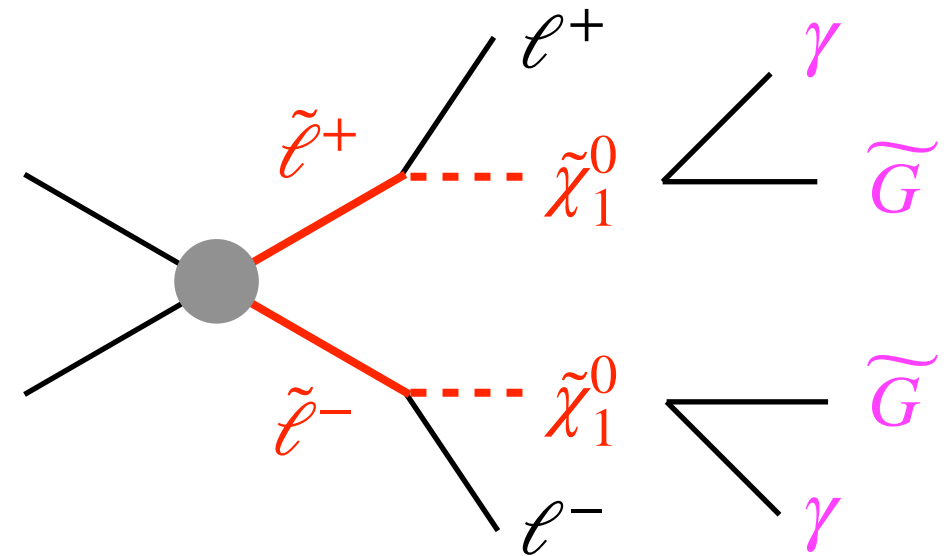
g-2 region is unconstrained

BLR

Gravitino LSP



$$\Delta a_\mu^{\text{BLR}}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu)$$



[$\gamma \tilde{G}$][$\gamma \tilde{G}$] CMS $\gamma + E_T$ [1711.08008]

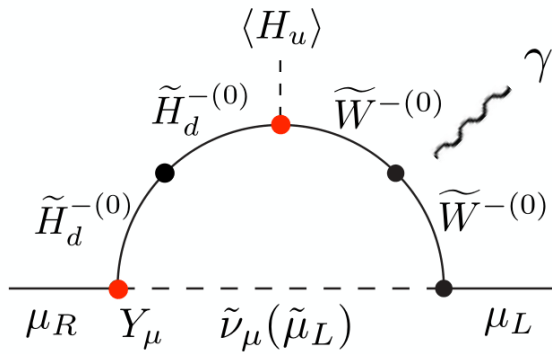
g-2 region is excluded by LHC

$$M_1 = m_{\tilde{\tau}_1} - 20 \text{ GeV}, \quad M_2 = 10 \text{ TeV}$$

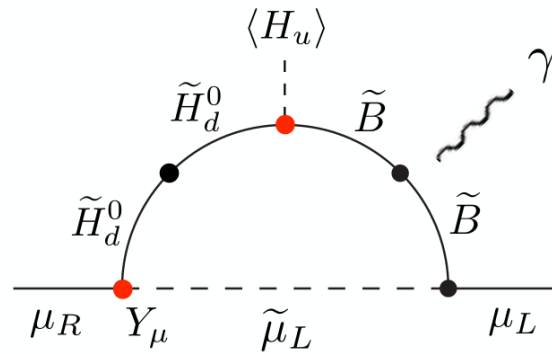
$$\mu = \mu_{\text{max}}, \quad \tan \beta = 50$$

maximum allowed by
vacuum (meta-)stability

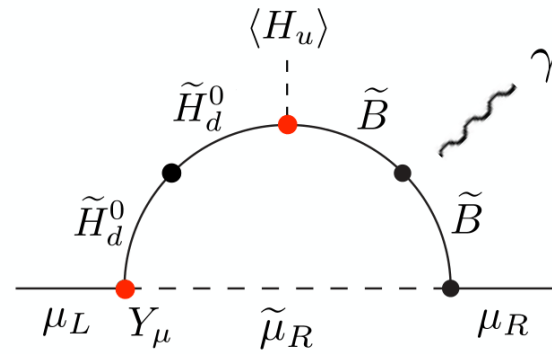
Short Summary



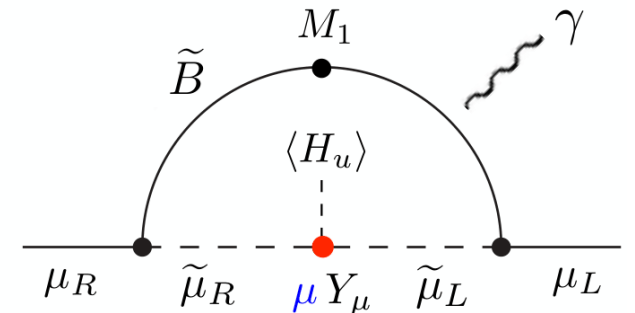
WHL



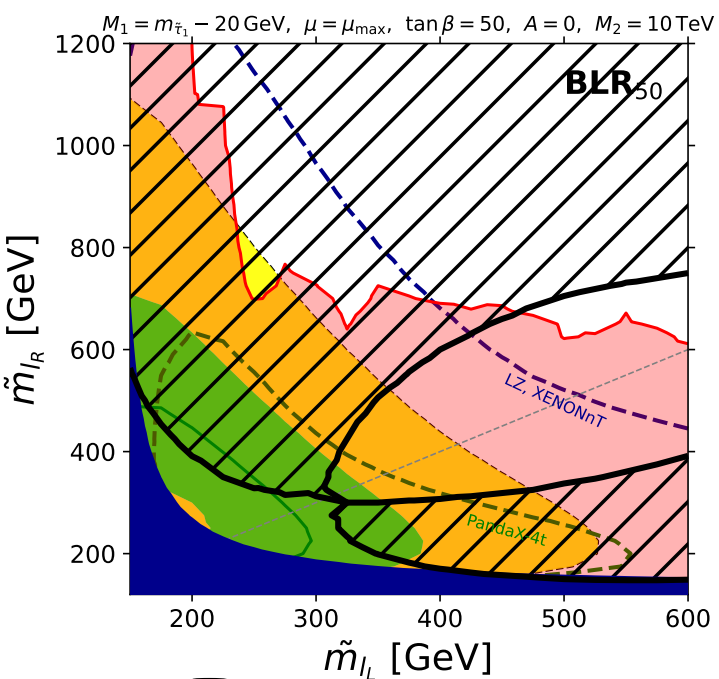
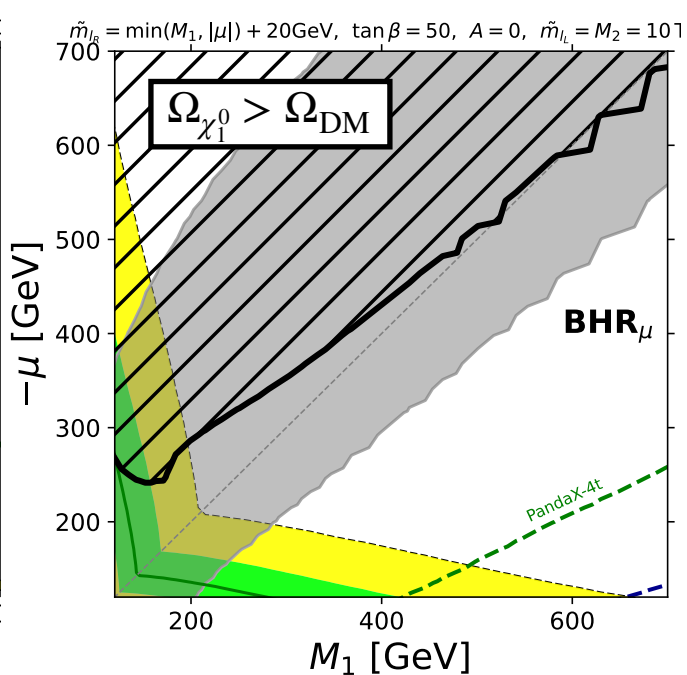
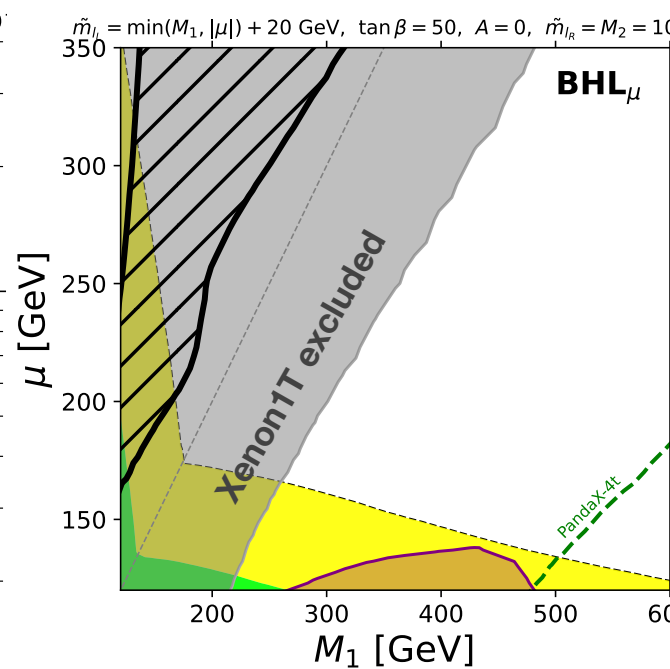
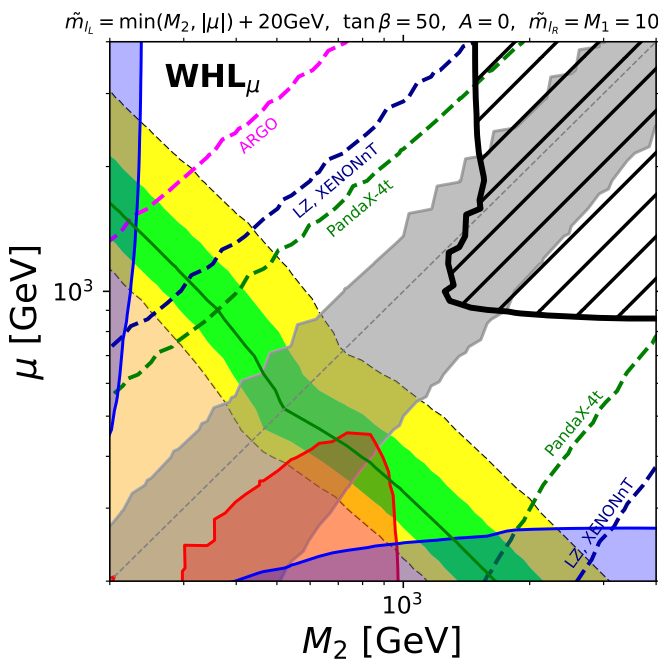
BHL



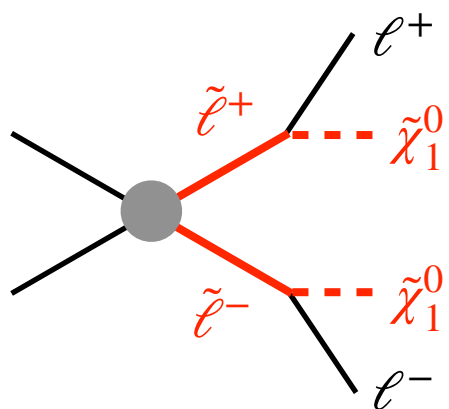
BHR



BLR

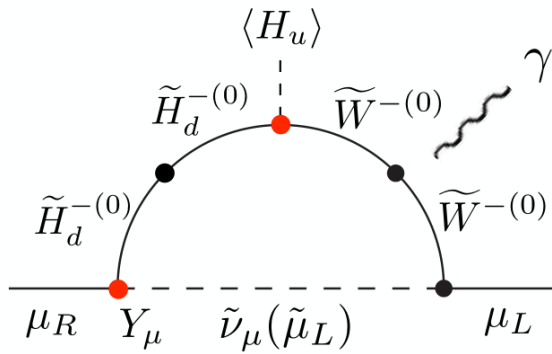


MSSM

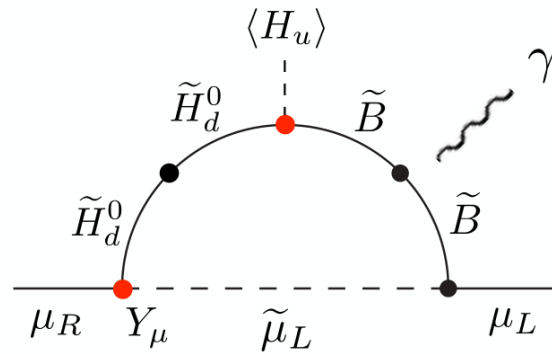


- Large regions are excluded by $\Omega_{\tilde{\chi}_1^0} > \Omega_{\text{DM}}$ and DM-DD.
- LHC constraints from lepton + \cancel{E}_T

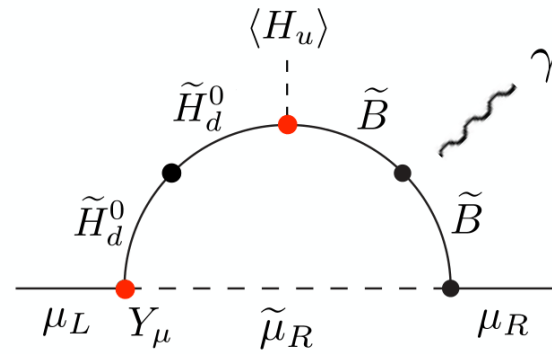
Short Summary



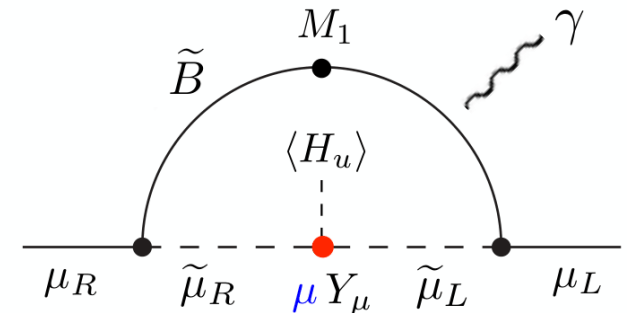
WHL



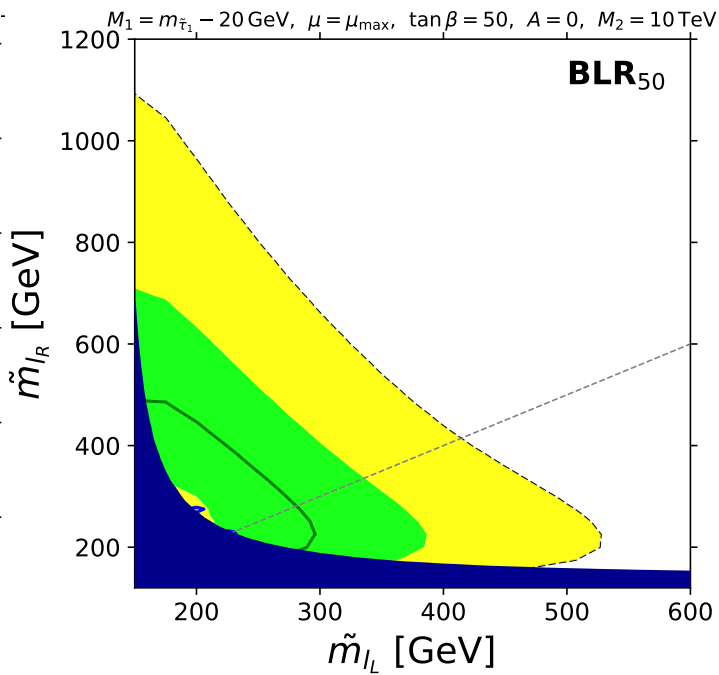
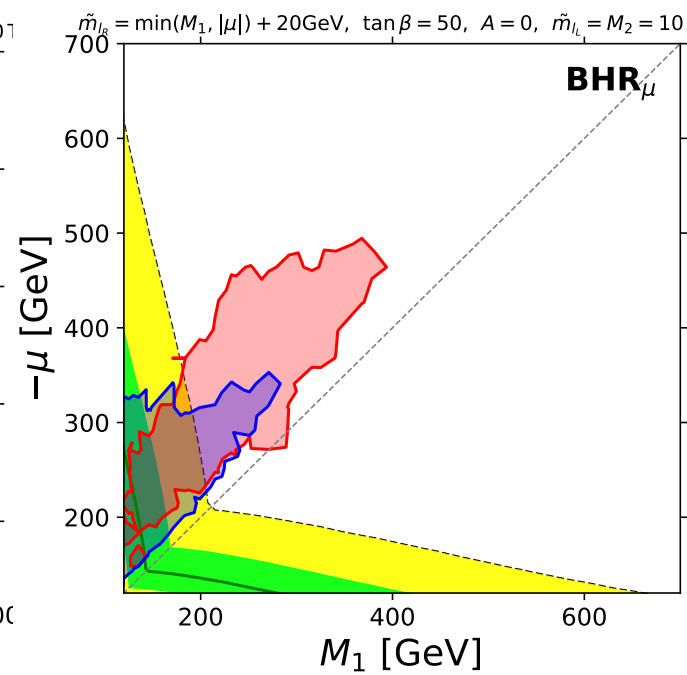
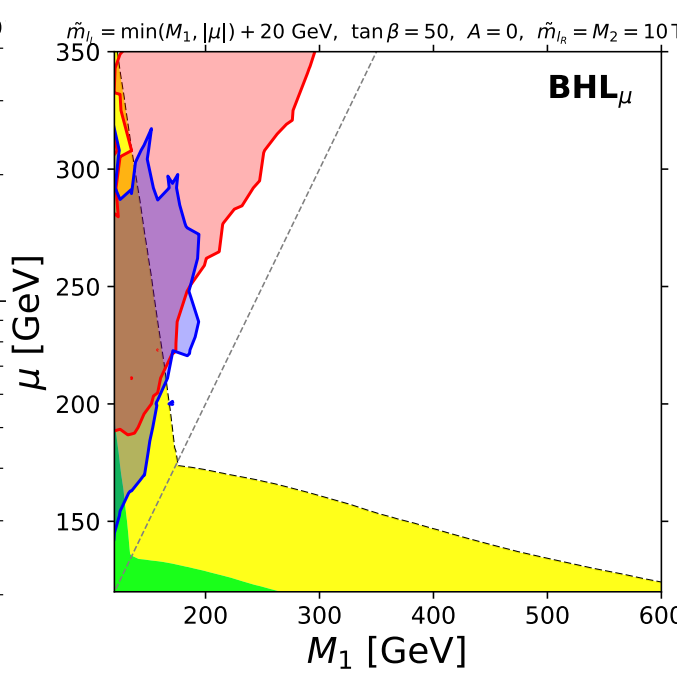
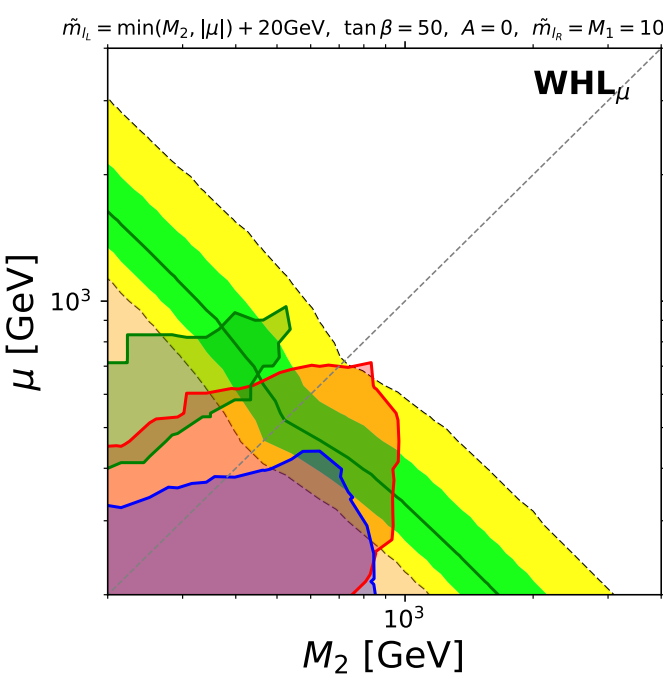
BHL



BHR

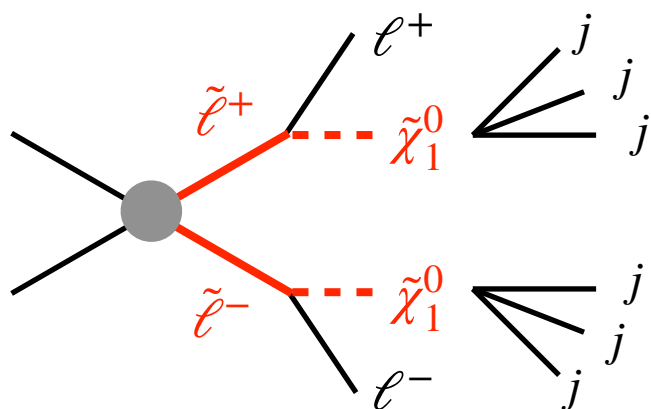


BLR

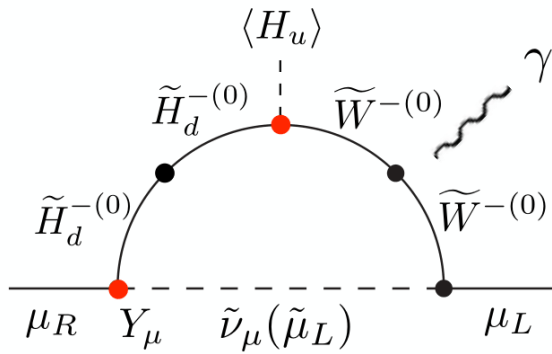


RPV

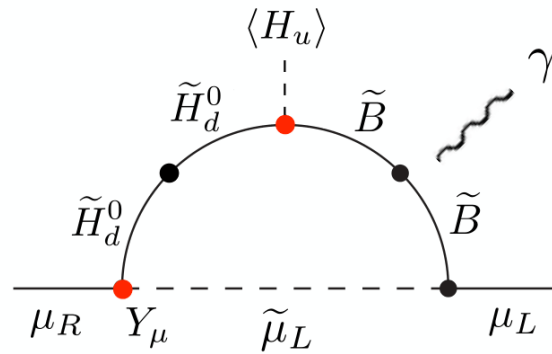
- No DM constraints
- LHC constraints from multijet + lepton



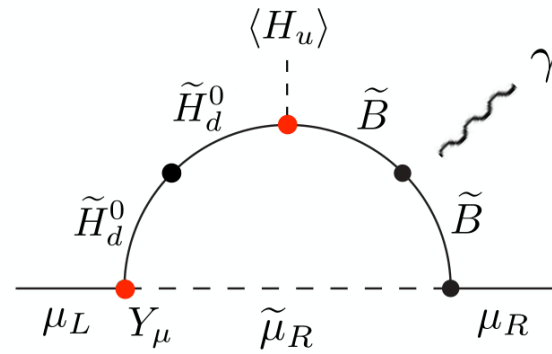
Short Summary



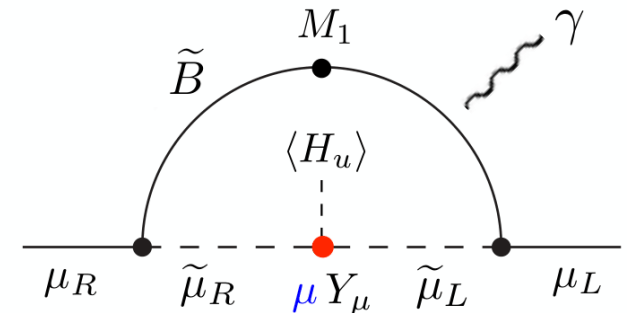
WHL



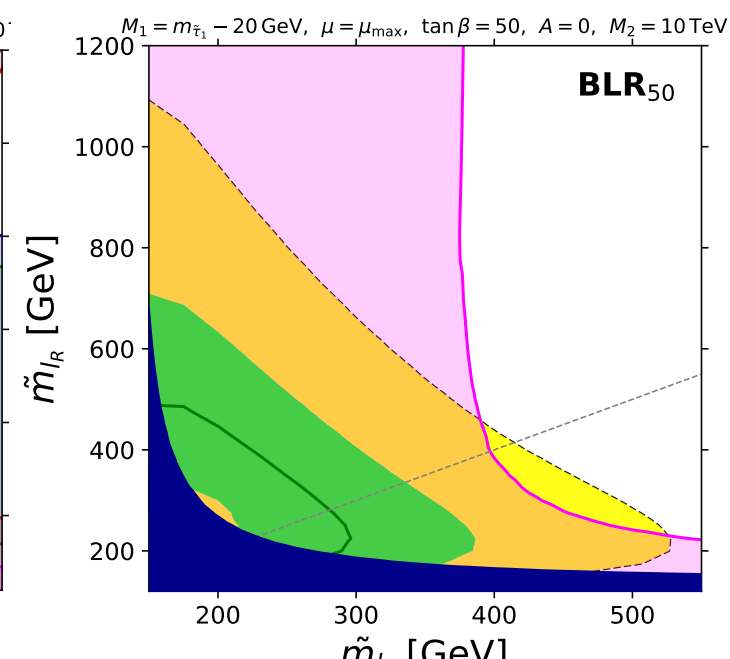
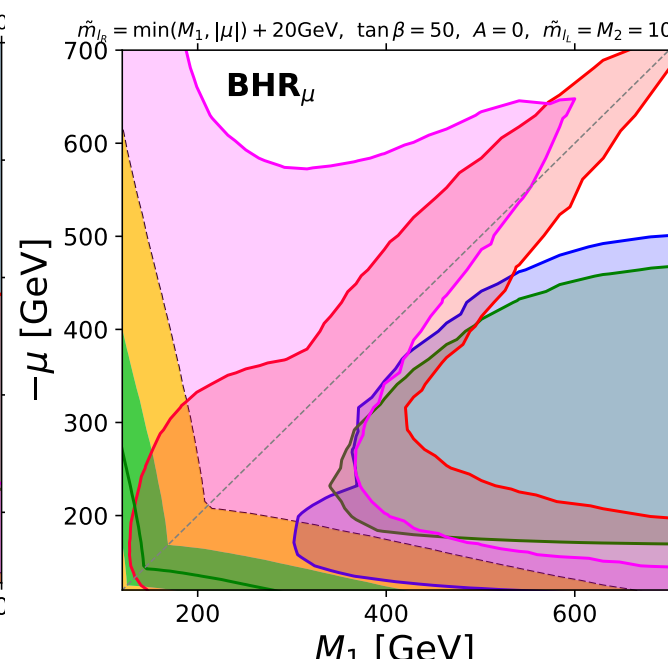
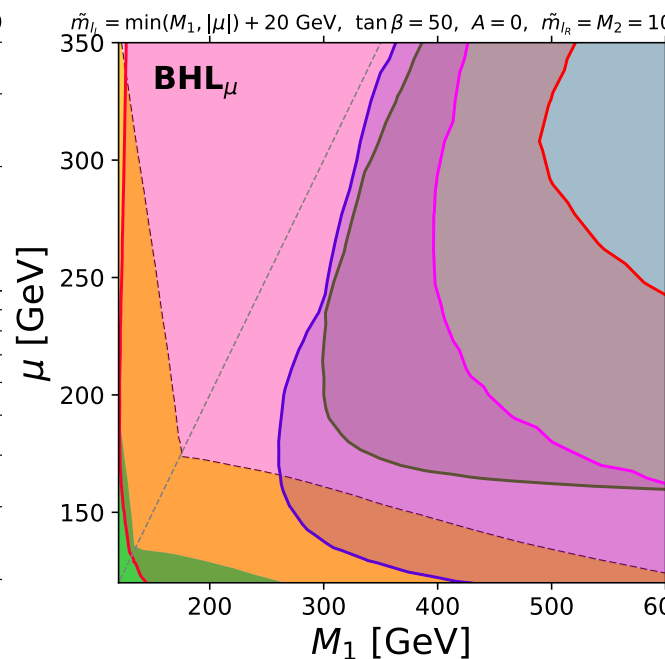
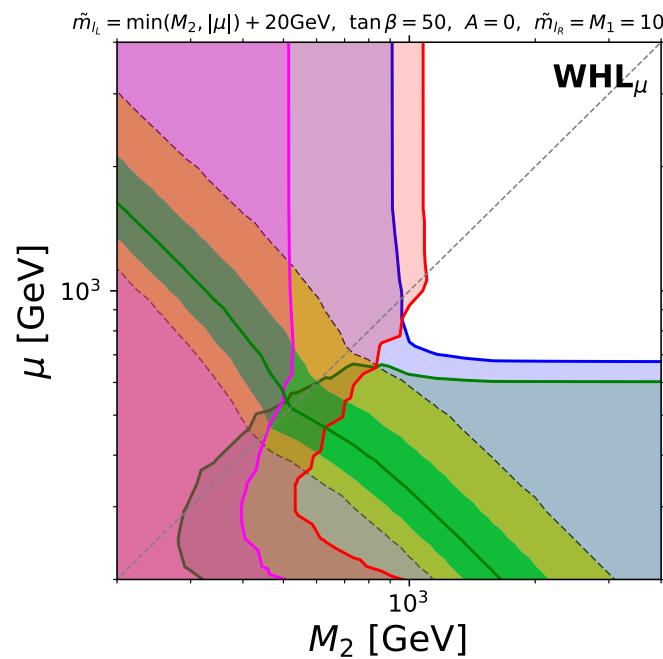
BHL



BHR



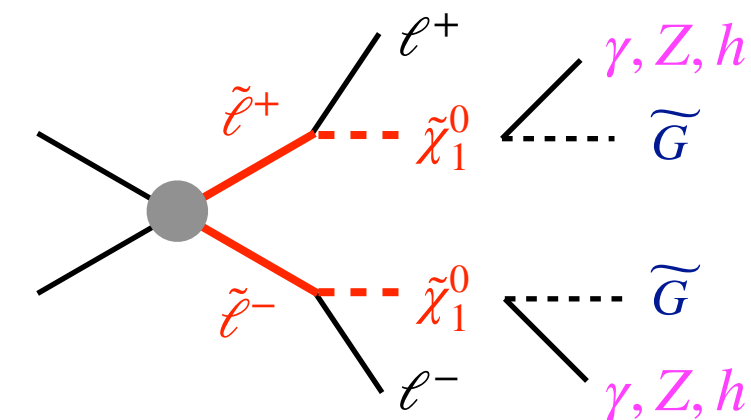
BLR



Gravitino LSP

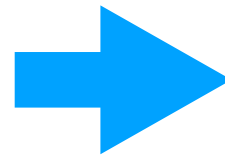
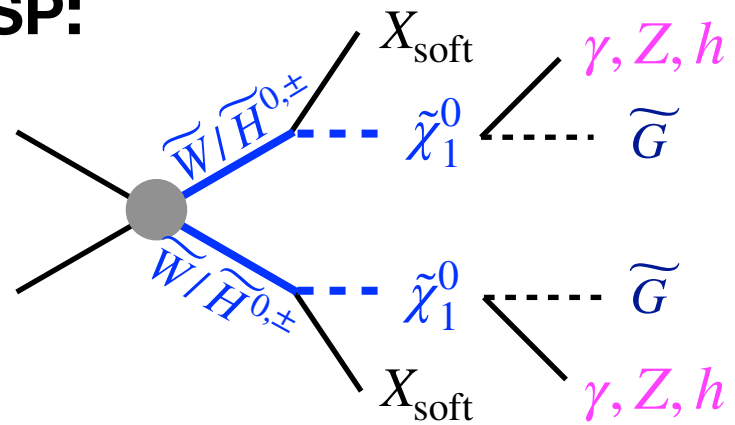
● No DM constraints

● all g-2 region is excluded mainly by $\gamma + \cancel{E}_T$

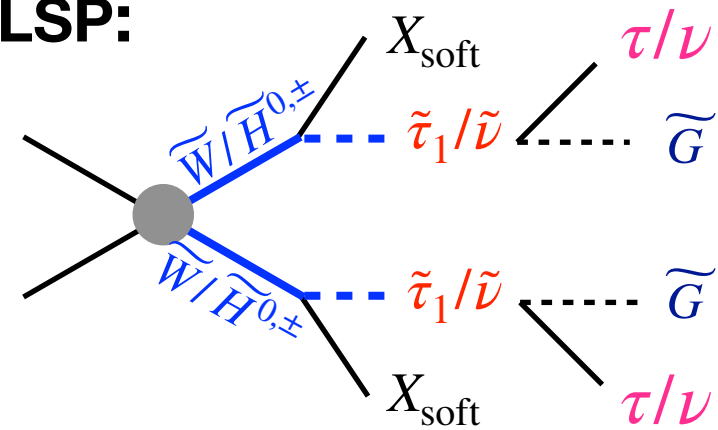


Gravitino LSP scenario really excluded?

$\tilde{\chi}_1^0$ NLSP:

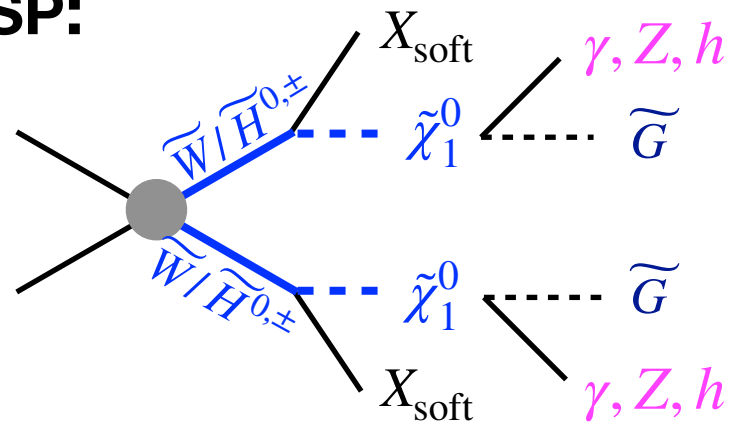


$\tilde{\tau}_1/\tilde{\nu}$ NLSP:

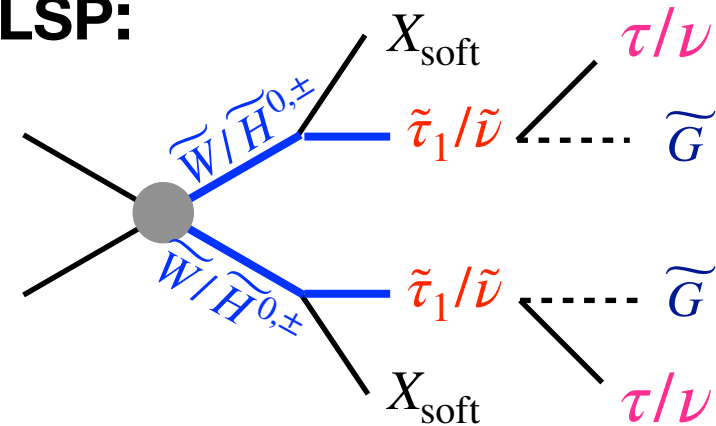


Gravitino LSP scenario really excluded?

$\tilde{\chi}_1^0$ NLSP:



$\tilde{\tau}_1/\tilde{\nu}$ NLSP:



WHL plane:

$$(M_2 \text{ vs } \mu) \text{ with } \tilde{m}_{l_L} = \min(M_2, \mu) + 20 \text{ GeV} \implies m_{l_L} = \min(M_2, \mu) - 20 \text{ GeV}$$

BHL plane:

$$(M_1 \text{ vs } \mu) \text{ with } \tilde{m}_{l_L} = \min(M_1, \mu) + 20 \text{ GeV} \implies m_{l_L} = \min(M_2, \mu) - 20 \text{ GeV}$$

$\tilde{\nu}_L$ NLSP

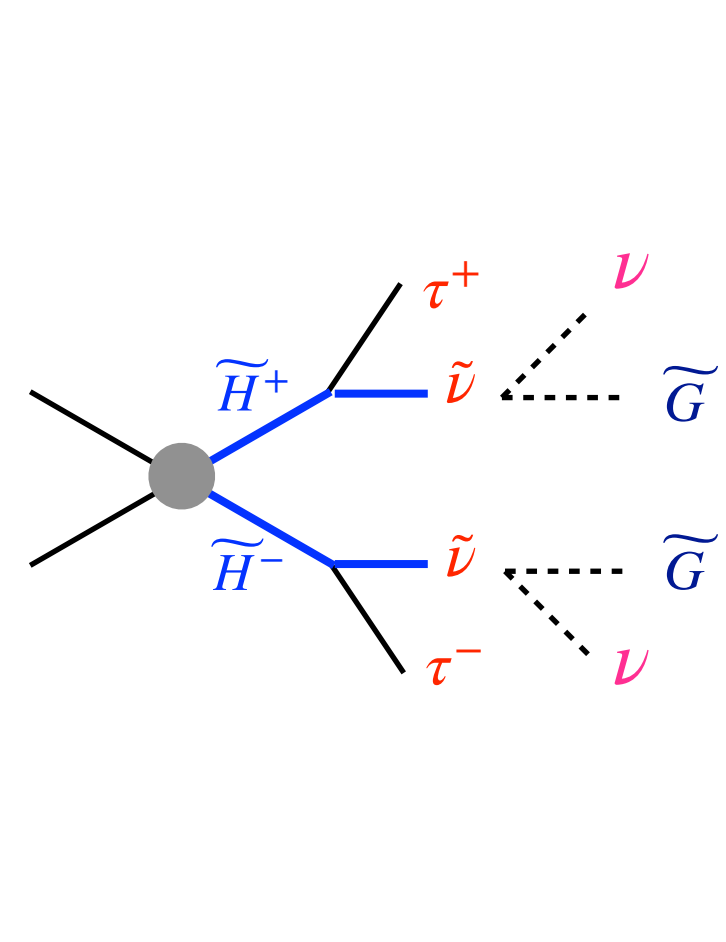
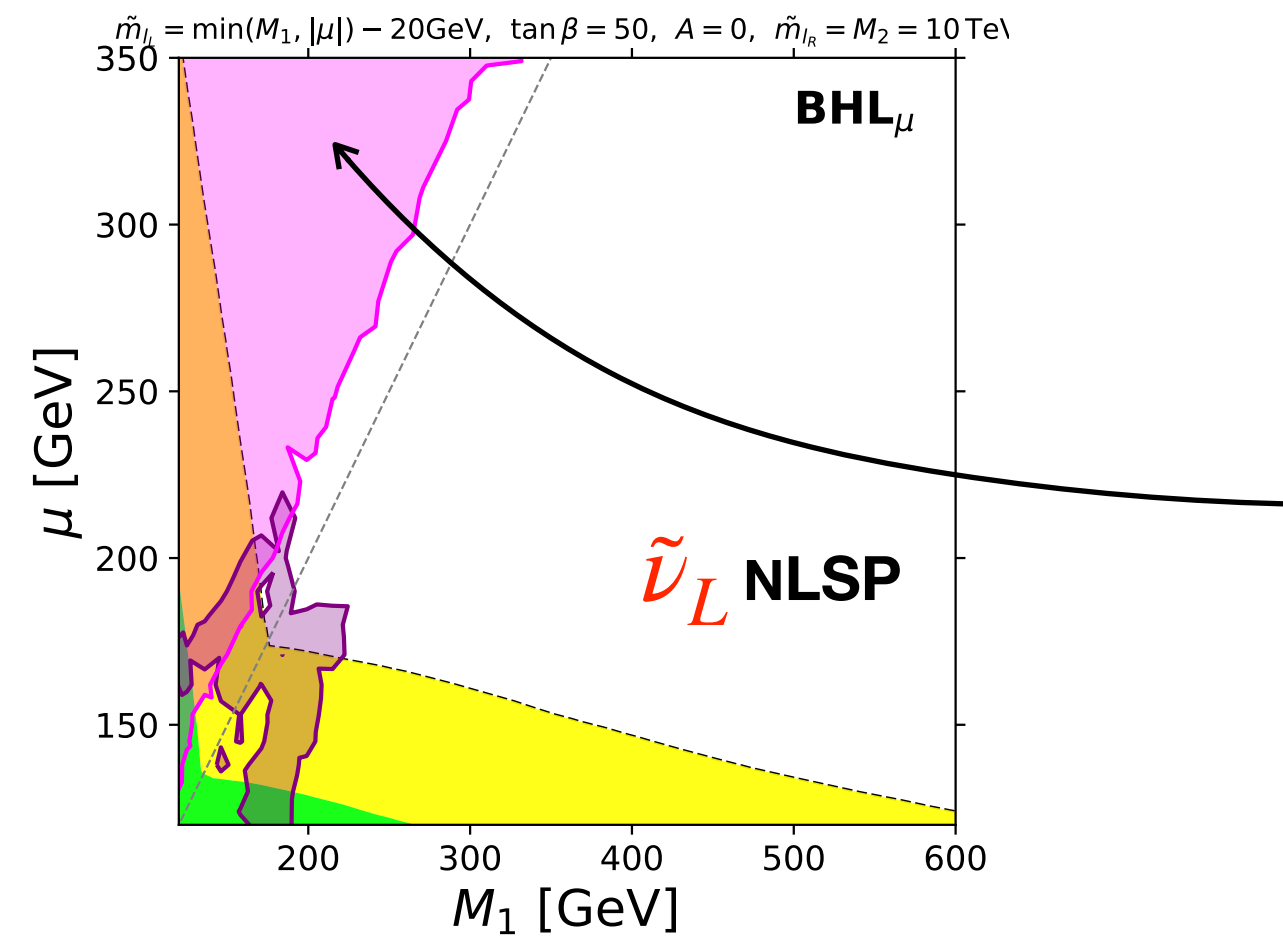
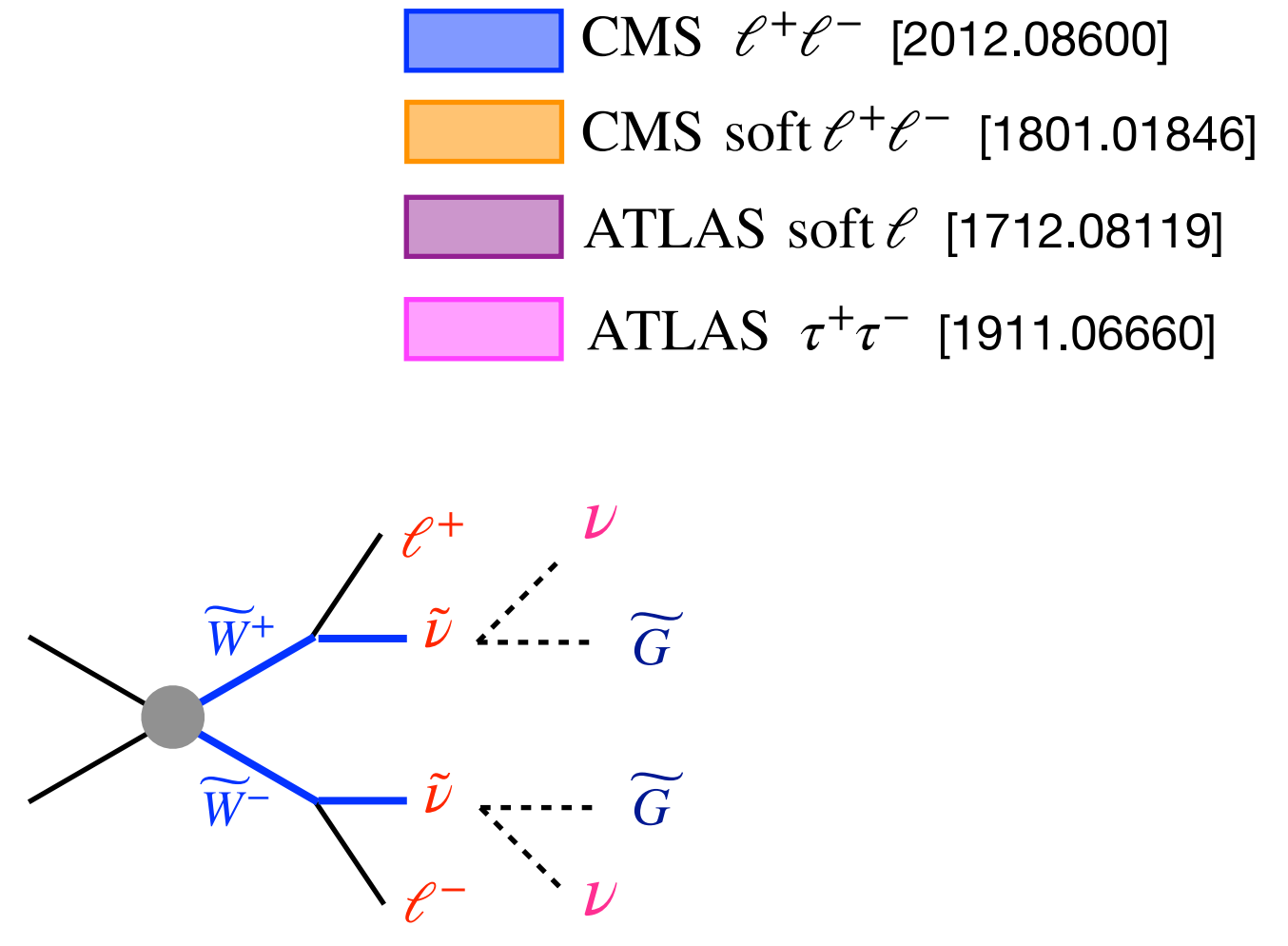
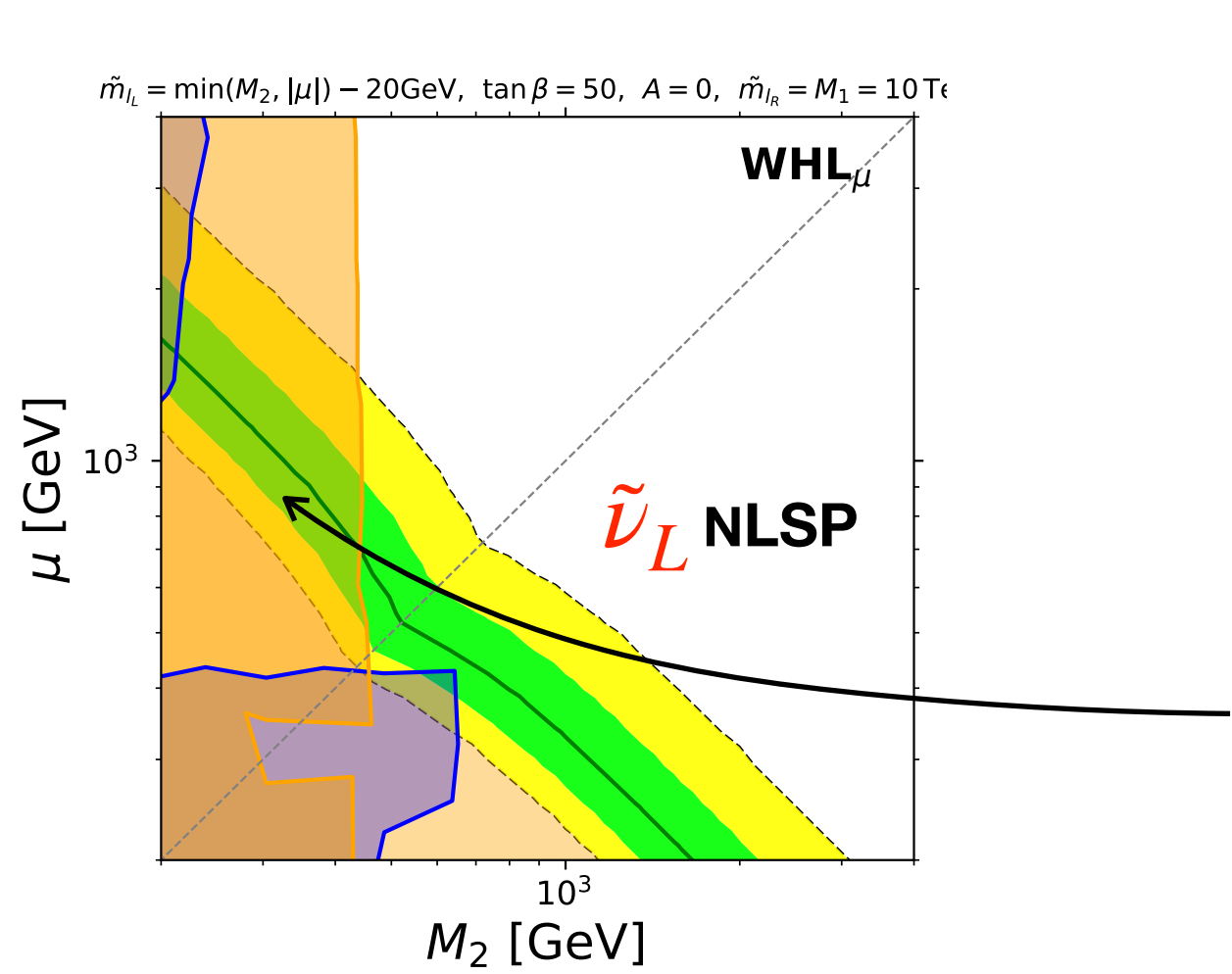
BHR plane:

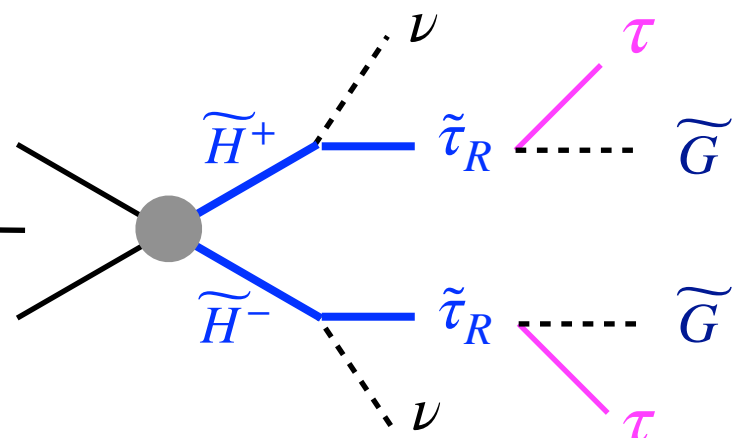
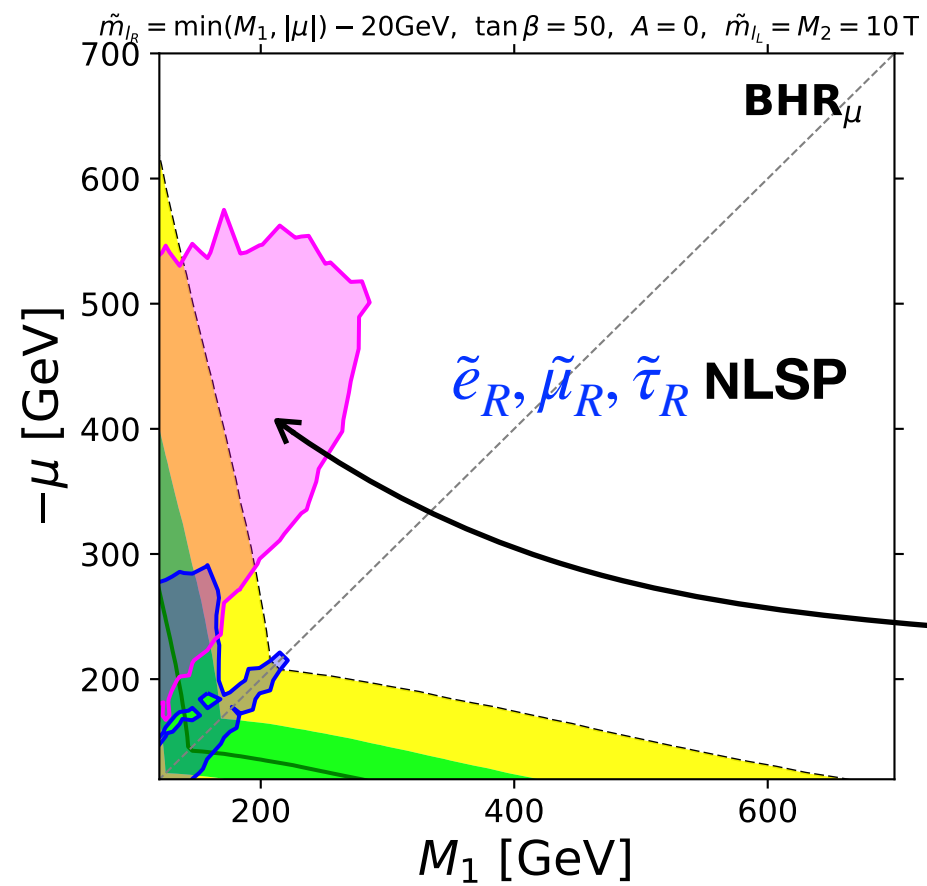
$$(M_1 \text{ vs } \mu) \text{ with } \tilde{m}_{l_R} = \min(M_1, |\mu|) + 20 \text{ GeV} \implies m_{l_R} = \min(M_1, \mu) - 20 \text{ GeV}$$

$\tilde{e}_R, \tilde{\mu}_R, \tilde{\tau}_R$ NLSP

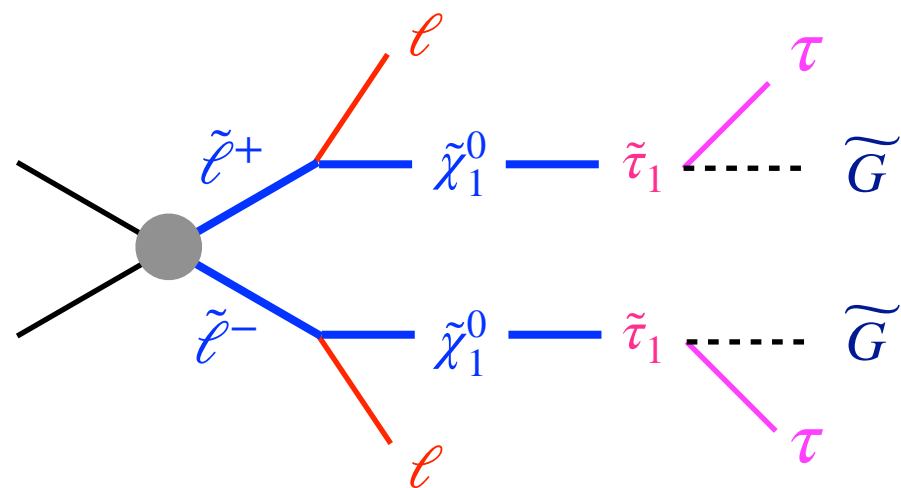
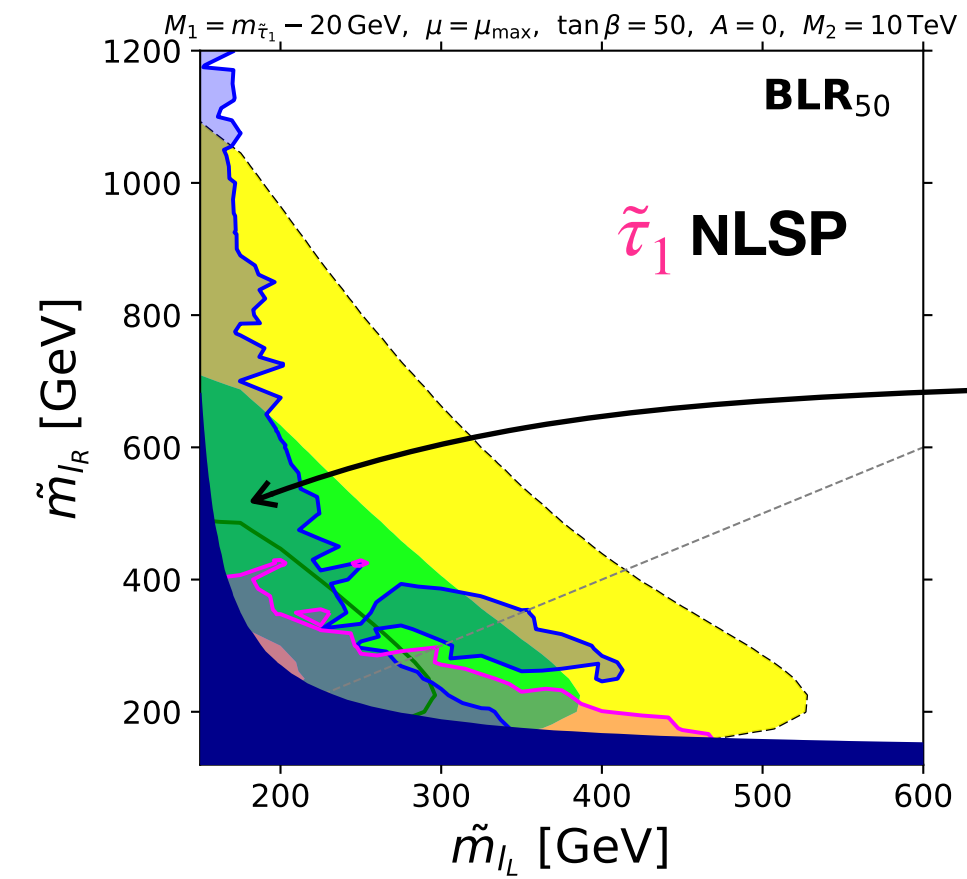
BLR plane:

$$(\tilde{m}_{l_L} \text{ vs } \tilde{m}_{l_R}) \text{ with } M_1 = m_{\tilde{\tau}_1} - 20 \text{ GeV} \implies M_1 = m_{\tilde{\tau}_1} + 20 \text{ GeV} \left\} \tilde{\tau}_1 \text{ NLSP}$$

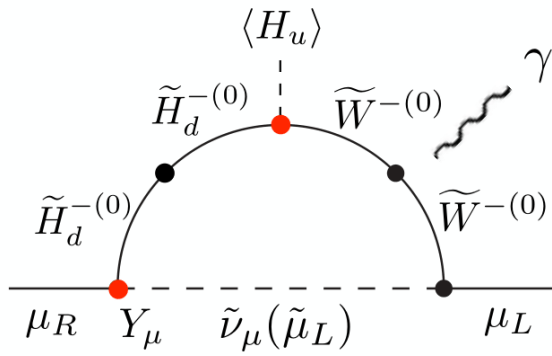




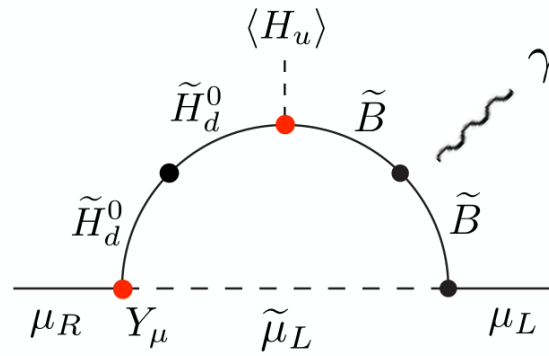
- CMS $\ell^+\ell^-$ [2012.08600]
- CMS soft $\ell^+\ell^-$ [1801.01846]
- ATLAS soft ℓ [1712.08119]
- ATLAS $\tau^+\tau^-$ [1911.06660]



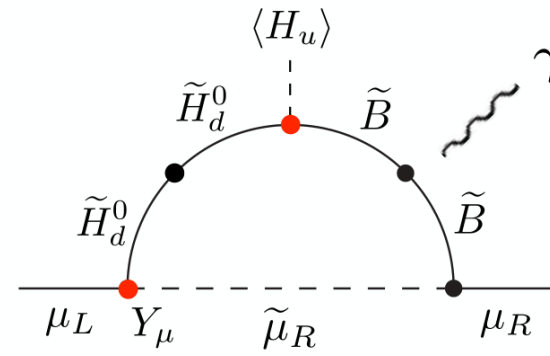
Non $\tilde{\chi}_1^0$ NLSP (Short Summary)



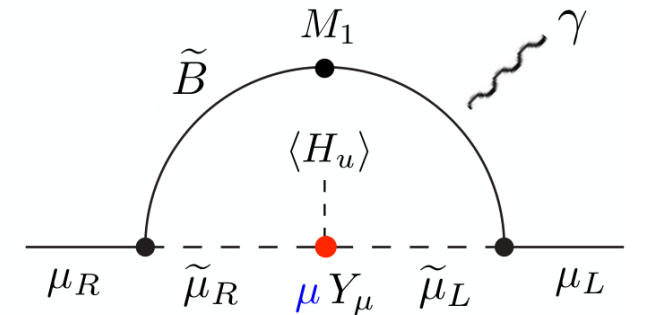
WHL



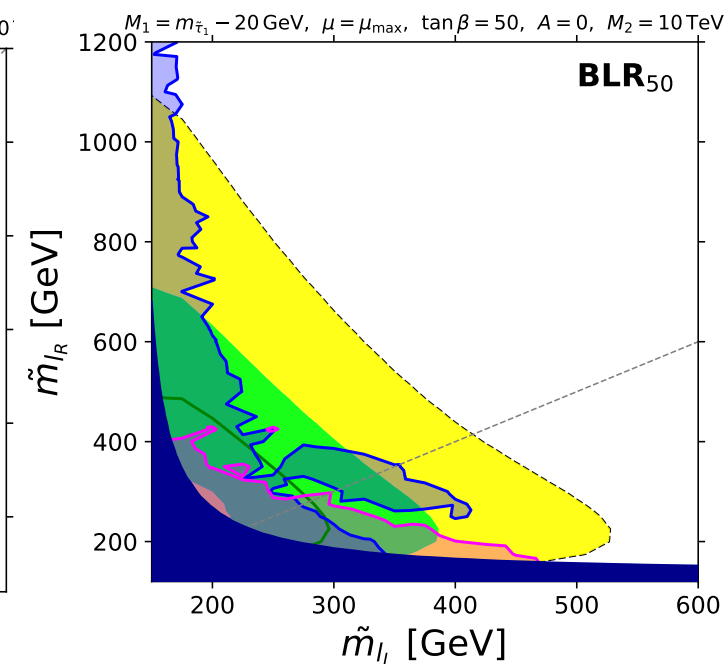
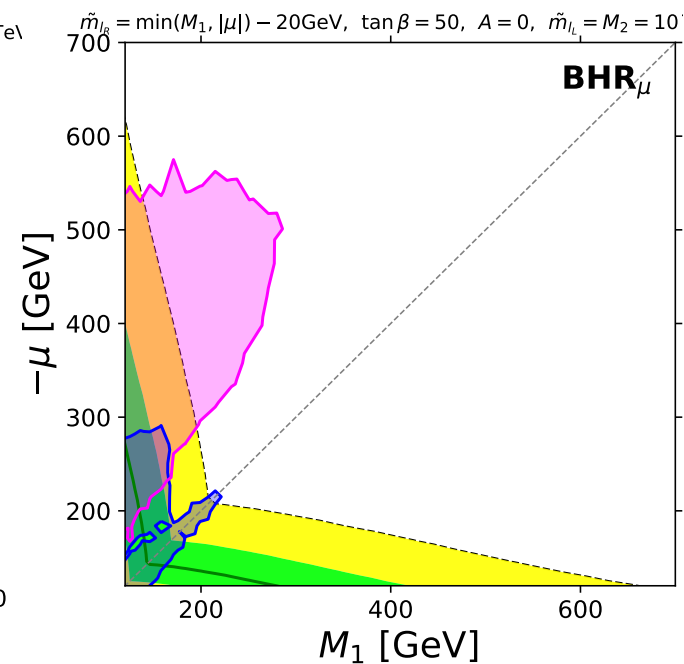
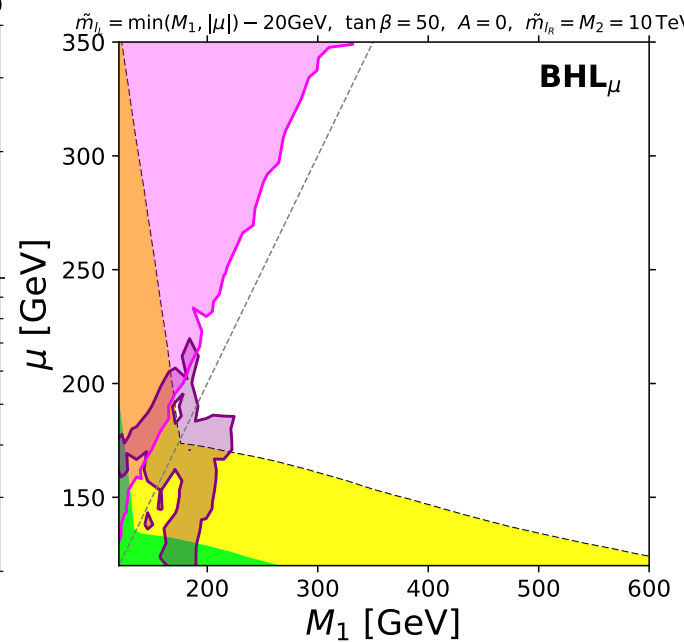
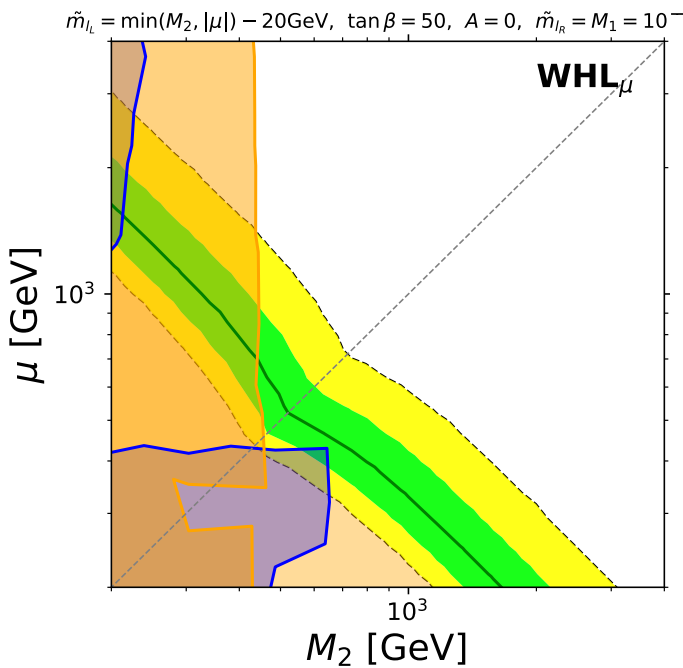
BHL



BHR



BLR



● small $|\mu|$ region is compatible with $(g-2)_\mu$

Summary

- SUSY might be a solution to the $(g-2)_\mu$ anomaly
 - stable LSP $\tilde{\chi}_1^0 \implies$ **LHC constraints from large \cancel{E}_T search**
 - slepton-gaugino-Higgsino are light \implies **stringent constraint from DM-DD detection**
 - LR slepton and Bino are light \implies **Bino overproduction**
- If $\tilde{\chi}_1^0$ is not stable LSP, DM constraints go away, and LHC signature changes.
 - ① RPV with UDD \implies LHC constraints from **multijet + lepton**
 - ② Gravitino LSP with $\tilde{\chi}_1^0$ NLSP \implies **$(g-2)_\mu$ region excluded by $\gamma + \cancel{E}_T$ channel**
 - ③ Gravitino LSP with **non** $\tilde{\chi}_1^0$ NLSP \implies LHC constraints from **soft lepton/tau**

Explanation for $(g-2)_\mu$ anomaly is possible for the scenarios ① and ③

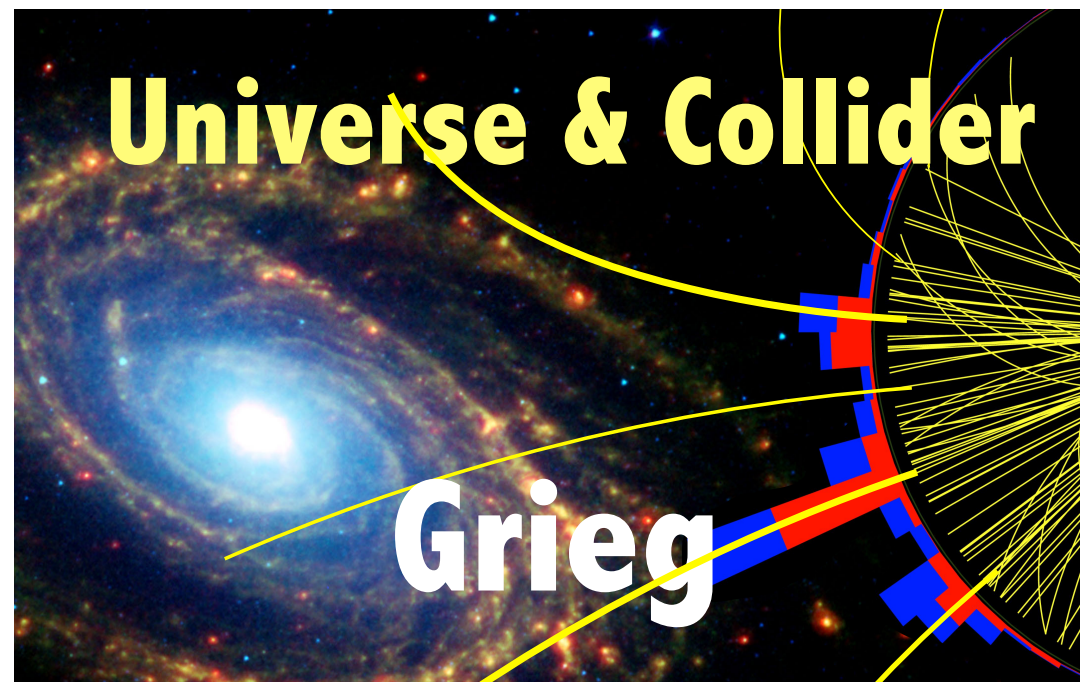


Norway
grants



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Understanding the Early Universe:
interplay of theory and collider experiments

Joint research project between the University of Warsaw & University of Bergen

$$\tilde{m}_{l_L} = \min(M_2, |\mu|) + 20\text{GeV}, \tan\beta = 50, A = 0, \tilde{m}_{l_R} = M_1 = 10\text{TeV}$$

