



# Asymmetries in the early universe



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# primordial B and L asymmetries

baryon asymmetry at BBN ( $\sim 1$  MeV) and CMB decoupling ( $\sim$  eV) :  $\frac{n_B}{s} \simeq 8.7 \times 10^{-11}$

In SM,  $B - L$  and  $B + L$  are conserved below EWPT / sphaleron freeze-out ( $\sim 100$  GeV). Above, sphaleron processes drive  $B + L = 0$ .

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However:

$B + L$  asymmetry can be much larger at earlier times

$B - L$  asymmetry can be much larger if  $B - L$  violation introduced

Asymmetries in electron neutrinos from BBN, CMB:  
(charged particles constrained by charge neutrality)

$$\frac{|n_{\nu_e} - n_{\bar{\nu}_e}|}{s} \sim \frac{|\mu_{\nu_e}|}{T} \lesssim 10^{-2}$$

Due to neutrino oscillations, large  $\mu_{\nu_\alpha}$  with  $\sum \mu_{\nu_\alpha} = 0$  only constrained to:  $|\mu_{\nu_\alpha}|/T \lesssim \mathcal{O}(1)$

Pastor, Pinto, Raffelt '08,  
Mangano et al '11,  
Castorina et al '12, ...  
Pitrou et al '18, ...  
Escudero, Ibarra, Maura '22

or not ?

# primordial B and L asymmetries

Observationally,  
O(1) lepton flavour asymmetries  
are not excluded

Hints from BBN (helium anomaly)  
and CMB (polarization)  
for large CP violation

Burns, Tait, Valli `22, Minami, Komatsu `20

Implications for baryogenesis,  
CP-violating BSM physics,  
thermal phase transitions,....

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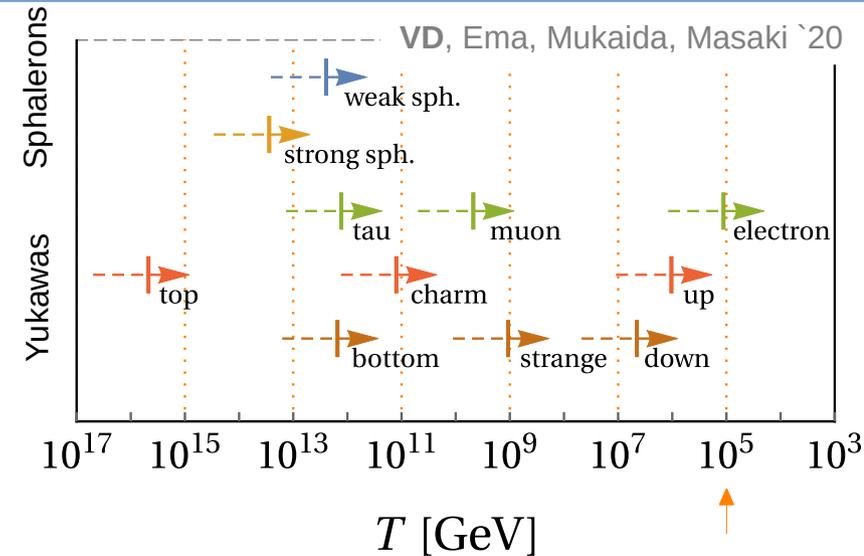
Implications for baryogenesis,  
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Outline of this talk:

- implications of large spontaneous CP violation in the early universe
- new bounds on lepton flavour asymmetries
- implications for baryogenesis

# SM interactions and conserved charges

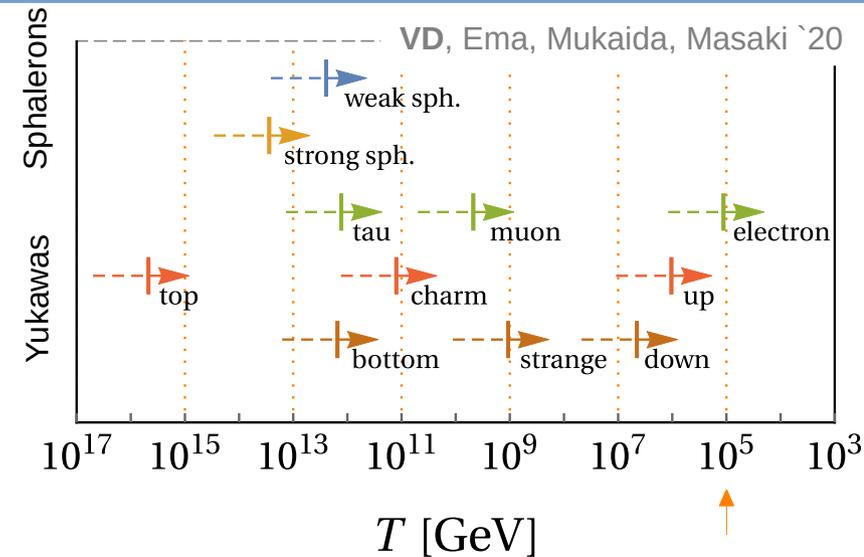
- exactly conserved charges:  $B/3 - L_\alpha, Y$   
(lepton flavour, hypercharge)
- in the early Universe, SM interactions cannot keep up with expansion



→ additional approximately conserved charges  $q_X = n_X - n_{\bar{X}} = \mu_X T^2 / 6$  :

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	$T$ [GeV]	$y_e$	$y_{ds}$	$y_d$	$y_s$	$y_{sb}$	$y_\mu$	$y_c$	$y_\tau$	$y_b$	WS	SS	$y_t$
(v)	$(10^5, 10^6)$	$q_e$	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
(iv)	$(10^6, 10^9)$	$q_e$	$q_{2B_1 - B_2 - B_3}$	$q_{u-d}$	✓	✓	✓	✓	✓	✓	✓	✓	✓
(iii)	$(10^9, 10^{11-12})$	$q_e$	$q_{2B_1 - B_2 - B_3}$	$q_{u-d}$	$q_{d-s}$	$q_{B_1 - B_2}$	$q_\mu$	✓	✓	✓	✓	✓	✓
(ii)	$(10^{11-12}, 10^{13})$	$q_e$	$q_{2B_1 - B_2 - B_3}$	$q_{u-d}$	$q_{d-s}$	$q_{B_1 - B_2}$	$q_\mu$	$q_{u-c}$	$q_\tau$	$q_{d-b}$	$q_B$	✓	✓
(i)	$(10^{13}, 10^{15})$	$q_e$	$q_{2B_1 - B_2 - B_3}$	$q_{u-d}$	$q_{d-s}$	$q_{B_1 - B_2}$	$q_\mu$	$q_{u-c}$	$q_\tau$	$q_{d-b}$	$q_B$	$q_u$	✓

# conserved charges + # equilibrated interactions = # particle species = 16

asymmetries are redistributed across different species



# chiral plasma instability

chiral magnetohydrodynamics (MHD) : hyper gauge fields, plasma w asymmetries

classical Maxwell eqs with

$$J_Y = \sigma_Y (E_Y + \mathbf{v} \times B_Y) + \frac{2\alpha_Y}{\pi} \mu_{Y,5} B_Y$$

conductivity

fluid velocity  
→ inverse cascade

chiral magnetic effect  
→ chiral plasma instability

neglecting  
fluid velocity

$$\mu_{Y,5} = \sum_i \varepsilon_i g_i Y_i^2 \mu_i$$

chiral chemical potential

helicity:

$$\partial_\eta h_k = -\frac{2k^2}{\sigma_Y} h_k + \frac{4\alpha_Y}{\pi} \frac{\mu_{Y,5}}{\sigma_Y} \rho_{B,k}$$

magn. energy  
density:

$$\partial_\eta \rho_{B,k} = -\frac{2k^2}{\sigma_Y} \rho_{B,k} + \frac{\alpha_Y}{\pi} \frac{\mu_{Y,5}}{\sigma_Y} k^2 h_k$$

diffusion

chiral magnetic effect

modes of one helicity with  $k < k_{\text{CPI}} \equiv \alpha_Y |\mu_{Y,5}| / \pi$  become tachyonically unstable for  $|\mu_{Y,5}| \neq 0$

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→ chiral chemical potential converted into helical gauge fields  $h = \pi T^2 / \alpha_Y c_5(T) \mu_{Y,5}^{\text{ini}}$  at

$$T_{\text{CPI}} \sim 10^5 \text{ GeV} \left( \frac{10^2}{g_*} \right)^{\frac{1}{2}} \left( \frac{\alpha_Y}{0.01} \right)^2 \left( \frac{10^2 T}{\sigma_Y} \right) \left( \frac{\mu_{Y,5}/T}{2 \cdot 10^{-3}} \right)^2 \Big|_{T_{\text{CPI}}}$$

$T_{Y_e}$

particle asymmetries can be converted to helical gauge fields

# inverse cascade

Brandenburger et al `17  
Schober et al `18

neglecting the fluid velocity, diffusion will erase helical gauge fields on short scales.

fluid velocity introduces non-linear mode coupling, free energy is minimized when helicity stored in long-wave length modes → inverse cascade

For sufficiently large helical fields (ie Reynolds number  $> 1$ ) inverse cascade is triggered and helicity is protected from diffusion

helical gauge fields can survive even after chemical potentials are erased

# baryogenesis from decaying hypermagnetic fields

At EW phase transition, hypermagnetic helicity converted to EM helicity

→ generation of B+L asymmetry due to ABJ anomaly

Joyce, Shaposhnikov '97

Sphaleron wash-out decouples at EW phase transition

→ final B+L asymmetry sensitive to detailed time evolution of EW PT

Baryon asymmetry today estimated as:

Kamada, Long '16

$$\frac{n_B^h}{s} = c_B^{\text{dec}} \frac{\alpha_Y}{2\pi} \frac{h}{n_\gamma} \sim 10^{-6} h/T^3 \sim 10^{-4} (\mu_{Y,5}/T)_{T_{\text{CPI}}}$$

for  $|\mu| \gtrsim 10^{-6}$  danger of massive overproduction of baryon asymmetry in SM EW PT !

# summary and outline

- **implications of large spontaneous CP violation in the early universe**
  - SM interactions re-shuffle particle asymmetries
  - chiral plasma instability:  $\mu \mapsto h$
  - helicity can survive until EW PT and generate (large) baryon asymmetry
- **new bounds on lepton flavour asymmetries**
- **implications for baryogenesis**
  - baryogenesis from axion inflation
  - axiogenesis

# a bound on lepton flavour asymmetries

e.g. at  $T \sim 10^{5.6}$  GeV

Domcke, Kamada, Mukaida, Schmitz, Yamada '22

$$\frac{\mu_{Y,5}}{T} = \frac{711}{481} \frac{\mu_e}{T} + \frac{5}{13} \frac{\mu_{\Delta_e}}{T} - \frac{4}{37} \frac{\mu_{\Delta_{\mu+\tau}}}{T},$$

$$\Delta_\alpha = B/3 - L_\alpha$$

all SM interactions  
in equilibrium  
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consider only B-L conserving lepton flavour asymmetries  $\mu_e^{\text{ini}} = 0, \quad \sum_\alpha \mu_{\Delta_\alpha} = 0$

$$\rightarrow \mu_{Y,5} \sim \mu_{\Delta_\alpha} \neq 0$$

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last SM coupling (electron Yukawa) comes into equilibrium

overproduction of baryon asymmetry if

$$T_{\text{CPI}} \gtrsim 10^5 \text{ GeV} \quad \rightarrow \quad \left| \frac{\mu_{\Delta_e}}{T} \right| = \left| \frac{\mu_{\Delta_\mu} + \mu_{\Delta_\tau}}{T} \right| > 0.01 \quad \text{and}$$

$$\frac{n_B}{s} > 10^{-10} \quad \rightarrow \quad |\mu_{\Delta_\alpha}/T| \gtrsim 10^{-5}$$

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bound on LFAs,  
two orders of magnitude  
stronger than BBN bound

# a bound on lepton flavour asymmetries

Domcke, Kamada, Mukaida, Schmitz, Yamada `22

$$|\mu_{\Delta_\alpha}|/T < 0.01$$

- applies also for  $B-L = 0$  → in that case factor 100 stronger than BBN bound
- applies at  $T > 10^5$  GeV → constraint on primordial asymmetries
- helium anomaly in EMPRESS data suggests  $\mu_{\Delta_e}/T \sim 0.04$  Burns, Tait, Valli `22
  - possible only if generated at  $10^5$  GeV  $> T > \text{MeV}$   
(in particular large B-L violation after EWPT still viable)
- disfavours leptoflavourgenesis Mukaida, Schmitz, Yamada `21
- if marginally fulfilled, provides a viable (though tuned) baryogenesis mechanism
- sensitive to CPI dynamics, not sensitive to EW PT dynamics

# outline

- implications of large spontaneous CP violation in the early universe
- new bounds on lepton flavour asymmetries
- **implications for baryogenesis**
  - ♦ baryogenesis from axion inflation
  - ♦ axiogenesis

# baryogenesis from axion inflation

'axion' inflation, a minimal setup for SM + inflation:

Domcke, Kamada, Mukaida, Schmitz, Yamada '22

$$\mathcal{L} = \sqrt{-g} \left[ \frac{1}{2} \partial^\mu \phi \partial_\mu \phi - V(\phi) \right] - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \sum_\alpha \bar{\psi}_\alpha (i \partial \cdot \gamma - g Q A \cdot \gamma) \psi_\alpha + \frac{\alpha \phi}{4\pi f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

axion with scalar potential
(hyper charge) U(1) gauge field
massless (SM) fermions
axion gauge field coupling

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- exponential production of helical gauge fields through tachyonic instability for  $\dot{\phi} \neq 0$
- chemical potentials for fermions

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→ two contribution to final baryon asymmetry:

$$\chi = \frac{qCS}{2T^3} \Big|_{\text{rh}}$$

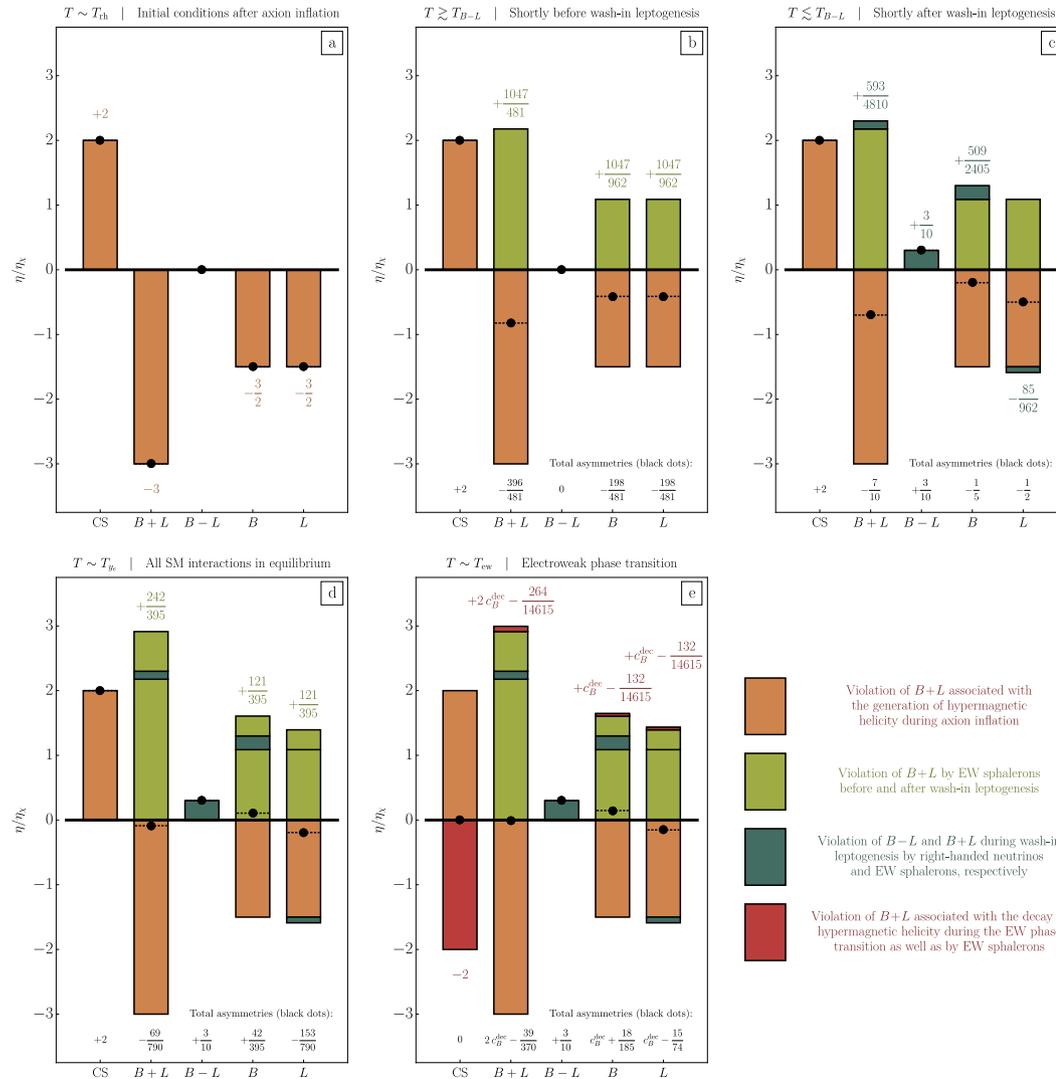
$$\eta_B^h \simeq 7.5 \cdot 10^{-3} \left( \frac{c_B^{\text{dec}}}{0.05} \right) \chi$$

from decaying helical hypermagn. gauge fields

$$\eta_B^N \simeq 0.01 \left( \frac{c_B^N}{0.1} \right) \chi$$

from re-shuffling chemical potentials if right-handed neutrinos included (B-L) = wash-in leptogenesis

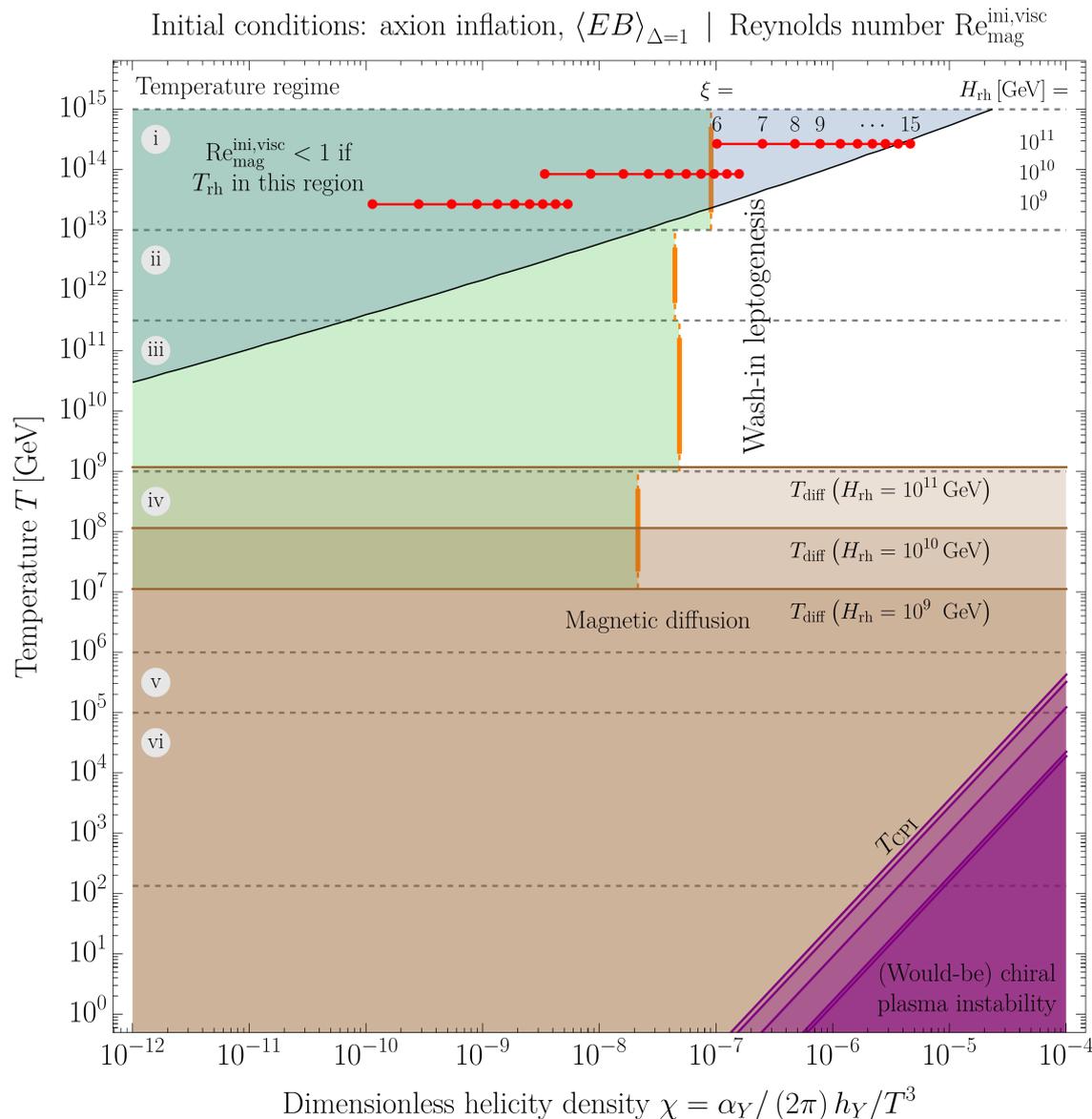
# baryogenesis from axion inflation



- evolution of primordial asymmetries for axion inflation
- analytical expressions for general initial conditions at all temperature ranges given in

Domcke, Kamada, Mukaida, Schmitz, Yamada '22

# baryogenesis from axion inflation



$$\xi = \frac{\alpha_Y \dot{\phi}}{2H f_a}$$

onset of CPI cancels off helicity and chemical potentials

diffusion erases gauge fields (for conservative estimate of Reynolds number)

for RHN mass scale above diffusion temperature, successful wash-in leptogenesis

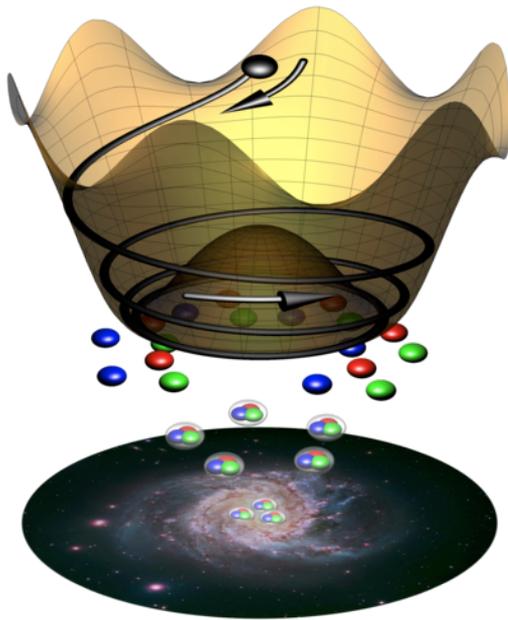
$\chi \sim 10^{-8}$  naturally achieved in axion inflation

axion inflation can account for successful baryogenesis

# implications for axiogenesis

## Kinetic misalignment & axiogenesis

[ Co, Hall, Harigaya '19; Co, Harigaya '19 ]



rotating PQ field

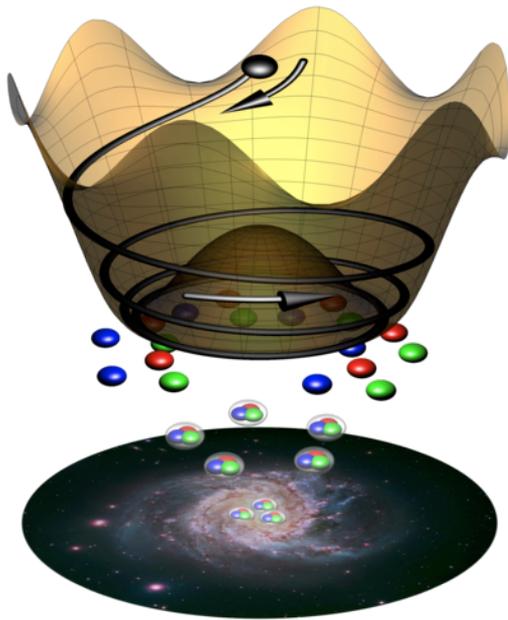
axion DM via kinetic misalignment

baryon asymmetry from via  
spontaneous baryogenesis  
(but in simplest model insufficient to explain BAU)

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rotating PQ field

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baryon asymmetry from via  
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(but in simplest model insufficient to explain BAU)

- rotating PQ field induces large CP violation



can trigger chiral plasma instability

- rotation of PQ field lasts until QCD PT



CPI possible below  $10^5$  GeV

[ Co, Domcke, Harigaya `22 ]

# implications for axiogenesis

scaling of PQ field:

$$\begin{aligned} r &\propto T^{3/2}, & |\dot{\theta}| &= N_{\text{DW}} m_\sigma, & \rho_\theta &\propto T^3 \\ r &= N_{\text{DW}} f_a, & \dot{\theta} &\propto T^3, & \rho_\theta &\propto T^6 \end{aligned}$$

before PQ field settles at  $T = T_S$

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DM production: ( $T < T_{\text{QCD}} < T_S$ )  $\curvearrowright r|\dot{\theta}|^2/s$

$$\Omega_a h^2 = \Omega_{\text{DM}} h^2 \times c_\Omega \left( \frac{10^9 \text{ GeV}}{f_a} \right) \left( \frac{Y_\theta}{73.3} \right)$$

# implications for axiogenesis

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 r \propto T^{3/2}, & |\dot{\theta}| = N_{\text{DW}} m_\sigma, & \rho_\theta \propto T^3 & \text{before PQ field settles at } T = T_S \\
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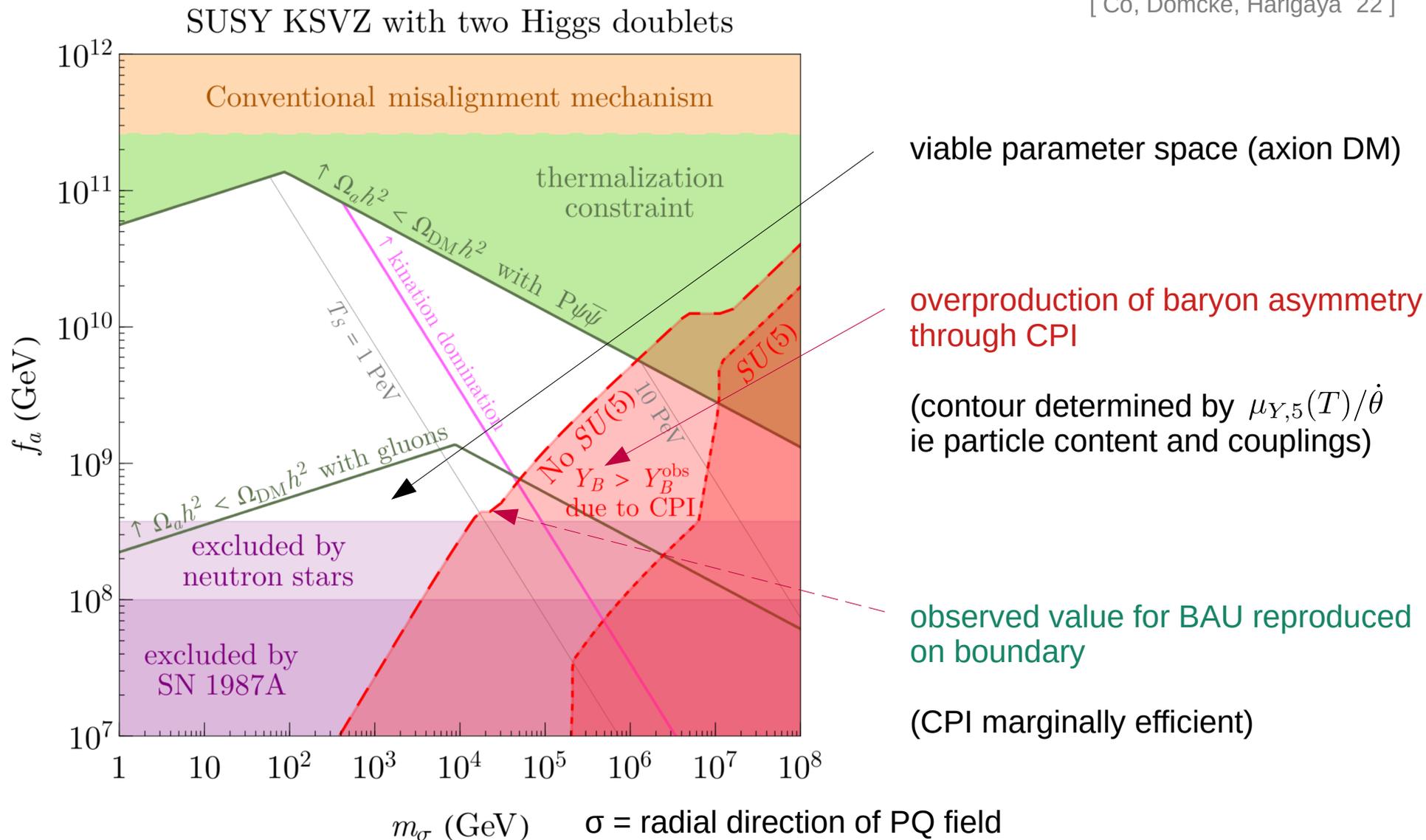
chiral plasma instability: ( $T_{\text{CPI}} > T_S$ )

$$T_{\text{CPI}}^{\text{MD}} \simeq 3.0 \text{ PeV} |c_5|^{4/5} c_\Omega^{1/5} \left( \frac{10}{c_{\text{CPI}}} \frac{50 T}{\sigma_Y} \right)^{2/5} \left( \frac{N_{\text{DW}} m_\sigma}{10^5 \text{ GeV}} \right)^{3/5} \left( \frac{10^9 \text{ GeV}}{f_a} \right)^{1/5} \left( \frac{g_{\text{MSSM}}}{g_*(T_{\text{CPI}}^{\text{MD}})} \right)^{1/5}$$

- CPI is avoided only if  $T_{\text{CPI}} < T_S$
- If CPI occurs, overproduction of BAU in entire parameter space viable for DM

# implications for axiogenesis

[ Co, Domcke, Harigaya '22 ]



# Summary

- (spontaneous) CP violation in the early universe can trigger chiral plasma instability, inverse cascade and baryogenesis
- new bound on primordial B-L conserving lepton flavour asymmetries,  $|\mu_{\Delta_\alpha}|/T < 0.01$
- improved understanding of baryogenesis from axion inflation
- constraints + new baryogenesis mechanism for axion kinetic misalignment mechanism
- framework to constrain or obtain observable predictions for models with large primordial asymmetries

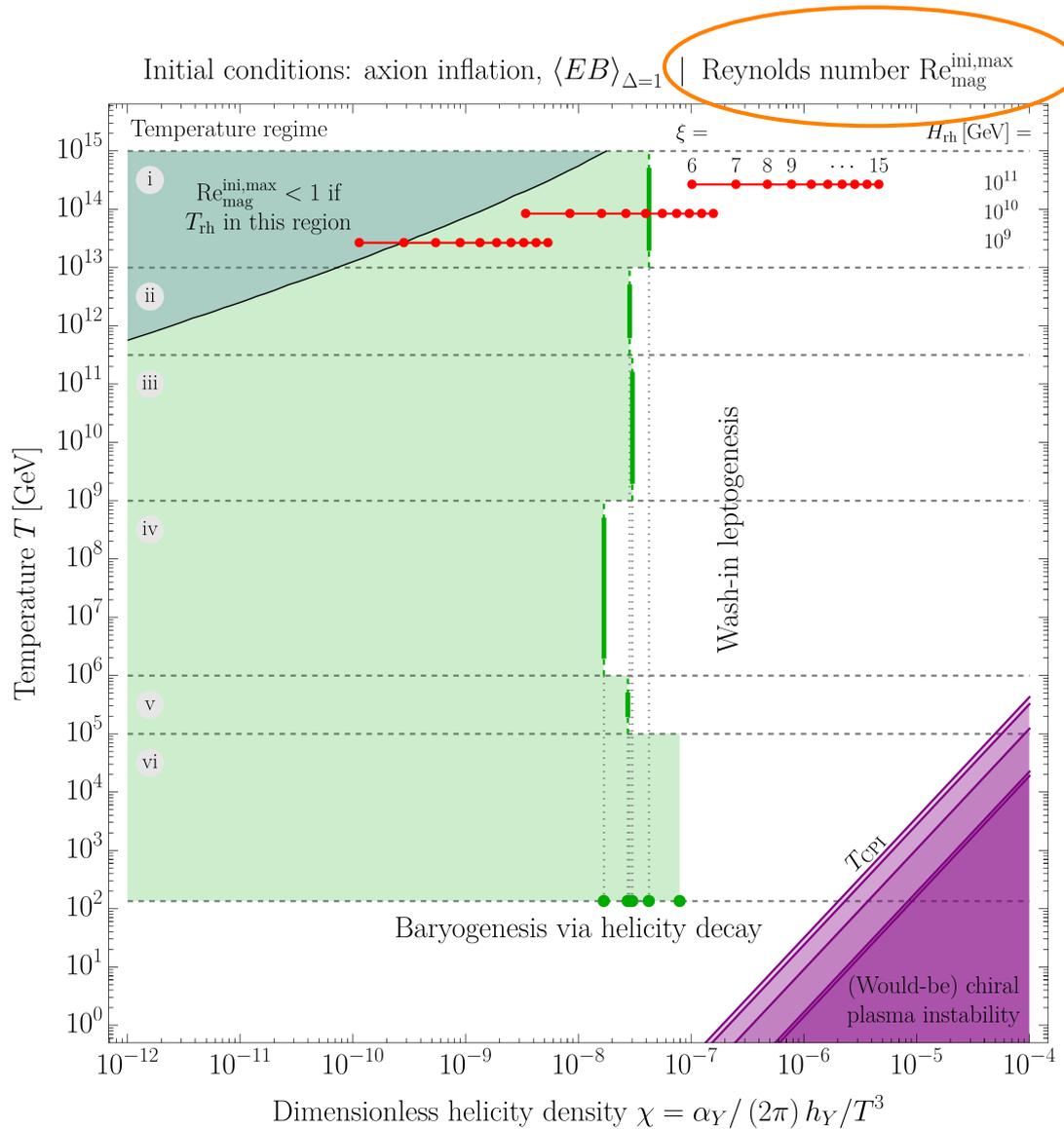
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**ありがとうございます！**

backup slides

# baryogenesis from axion inflation



baryogenesis via helicity decay  
and wash-in leptogenesis