

# On small Black Holes and stable Higher Spin States in Heterotic Strings

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# Foreword

- ▶ Recent interest in Black-Hole production at LHC [Giudice, Rattazzi, Wells; Giddings, Thomas; Dimopoulos, Landsberg; Meade, Randall; Kanti] ... not without some worries [Giddings, Mangano] and disturbing features
- ▶ Large Extra Dimensions (LED), TeV scale Gravity and Strings [Arkani-Hamed, Dimopoulos, Dvali; Antoniadis; ...]
- ▶ String/BH correspondence [Dabholkar, Harvey; Horowitz, Polchinski; Damour, Veneziano; 't Hooft; Susskind; ...]
- ▶ (non)BPS BH's and Higher Spins in String Theory [Dabholkar; Sen; Callan, Maldacena; Cvetič, Youm; Strominger, Vafa; ...]
- ▶ Higher Spin States are a hallmark of String Theory!!! [Veneziano, Shapiro-Virasoro, ... A. Sagnotti, O. Schlotterer, D. Lüst, ...]

# Plan of the Talk

- ▶ Small BH's, TeV gravity and Large Extra Dimensions
- ▶ (BPS) BH's and HS's in (Heterotic) Strings
- ▶ Vertex Operators, BRS conditions, Supermultiplets
  - ▶ BPS states with charge and spin
  - ▶ First Massive Level
  - ▶ Second Massive Level
  - ▶ Tri-linear couplings
- ▶ Scattering Amplitudes and (Pair) Production
  - ▶ 2 vector bosons - 2 small BPS BH's ('hidden'/'visible')
  - ▶ 2 gravitons - 2 small BPS BH's
- ▶ Cross Sections
  - ▶ Energy and Angular distributions
  - ▶ Caveat / comments on LED scenari
- ▶ Conclusions and Outlook

## BH production and decay in High Energy collisions

LED scenari  $M_{Pl} = M_d(M_d L)^{d-4}$ ,  $M_d \ll M_{Pl}$  for  $L \gg 1/M_d$

For large BH's with  $M_{BH} \gg M_d$ , partonic cross-section

$$\sigma_{ij \rightarrow BH}(s) = \mathcal{F}_d(s) \left[ \sqrt{s}/M_d^{d-2} \right]^{\frac{2}{d-3}}$$

For small BH's need (acrobatic) extrapolation or ... String Theory

At colliders, expect BH production for  $b < R_H(E, J)$  [Thorne; ...]

Spectacular Experimental Signatures for  $M_d \approx 1\text{TeV}$

[Giudice, Rattazzi, Wells; Giddings, Thomas; Dimopoulos, Landsberg; Maede, Randall; Kanti ...]

- ▶ Very large cross sections, LHC rates up to 1 Hz
- ▶ **Growth with Energy** (!?) of parton cross sections
- ▶ Large multiplicities, high sphericity
- ▶ Suppression of hard processes for  $E$  above threshold

... Self-completeness of (non)-perturbative (Super) Gravity?

[Bern, Dixon, ...; MB, Ferrara, Kallosh; Dvali, Gomez; ...]

# BPS BH's and Higher Spins in Heterotic Strings

BH's solutions in String Theory:

- ▶ Large BH's, **finite-area** horizon in sugra approximation
- ▶ Small BH's, **zero-area** horizon in sugra approximation

Fundamental strings correspond to small BH's.

Heterotic strings on  $T^6$  tori:  $\mathcal{N} = 4$  in  $D = 4$

Perturbative spectrum, level matching [Narain, Sarmadi, Witten; ...]

$$4(N_L - \delta_L) + \alpha' |\mathbf{p}_L|^2 = \alpha' M^2 = 4(N_R - 1) + \alpha' |\mathbf{p}_R|^2$$

6 'central' charges  $\mathbf{p}_L$ , 22 'matter' charges  $\mathbf{p}_R$ , i.e.  $\mathbf{Q} = (\mathbf{m}, \mathbf{n}, \mathbf{r})$

only massless, 1/2 BPS and long mltp's. [For 1/4 BPS need  $\mathbf{P} \neq 0$ ]

$$\mathbf{Q} \cdot \mathbf{Q} = \frac{\alpha'}{2} |\mathbf{p}_L|^2 - \frac{\alpha'}{2} |\mathbf{p}_R|^2 = 2\mathbf{m}\mathbf{n} - |\mathbf{r}|^2 = 2(N_R - 1) - 2(N_L - \delta_L)$$

1/2 BPS states:

$$N_L = \delta_L, M_{BPS}^2 = |\mathbf{p}_L|^2 \rightarrow \mathbf{Q} \cdot \mathbf{Q} \geq -2, J \leq N_R + 1$$

$$\mathbf{Q} \cdot \mathbf{Q} < -2 \rightarrow \text{non-BPS, yet 'extremal' if } M^2 = |\mathbf{p}_R|^2$$

At fixed  $M_{Pl}$ ,  $M_s = g_s^{(4)} M_{Pl} \rightarrow 0$  for  $g_s^{(4)} \rightarrow 0$  (boundary) !

## (Thermo)statical properties

For 'large' charges, neglecting spin<sup>†</sup>

$$d_{1/2BPS}^{Het}(N_R) \approx \exp(4\pi\sqrt{N_R}) = \exp S_{BH}^{Wald}$$

$S_{BH}^{Macro} = S_{BH}^{micro}$ , 'mini BH's' with two charges, horizon stretched by higher curvature  $\alpha'$  corrections\* [Sen; Dabholkar; Kallosh, Maloney; Prester; ...]

Yet  $T_{BH} = 0$  for all 'extremal' (NOT necessarily BPS) BH's

→ NO Hawking radiation.

For  $J^{Max} > 1$ , 1/2 BPS HS multiplets with  $(2J + 1)(8_B - 8_F)$  states:

$$\{(J + 1), 4(J + \frac{1}{2}), 6(J), 4(J - \frac{1}{2}), (J - 1)\} \quad SO(6) \rightarrow SO(5)$$

In  $D = 4$ , susy incompatible with horizon 'rotation' [Cvetic, Youm; Peet; ...]

... (in)stability of HS BPS states?

<sup>†</sup> otherwise  $C_R = 24 \rightarrow C_R = 21$ , yet helicity Str's  $\mathcal{B}_4^{(J)} = (2J + 1)\mathcal{B}_4^{(0)}$

\*absent in  $\mathcal{N} = 8, 6, 5$  SUGRA's IF UV finite [Bern, Dixon, ...; MB, Ferrara, Kallosh]

## (Thermo) Dynamical Properties

For near-extremal BH's,  $T_{BH} \neq 0$ : gray-body factor, Hawking radiation [Callan, Maldacena; Hashimoto, Klebanov; Garousi, Myers; ...]

Dynamics of very massive string states [Iengo, Russo; Chialva; ...]

Size and energy distribution, string/BH form factors [Cornalba, Costa, Penedones, Vieira; Chialva; ...]

Production of massive string states at colliders in un-oriented brane worlds [Dudas, Mourad; MB, Santini; Anchordequoi, Goldeberg, Lüst, Nawata, Schlotterer, Stieberger, Taylor; ...]

BH S-matrix [Veneziano, Wosiek; ...], High Energy collisions [Amati, Ciafaloni, Veneziano; Gross, Mende],

Our aim here: pair production of small charged BPS BH's [Gingrich; ...; MB, Lopez] and BPS HS states [wip] in Heterotic Strings ...

CAVEAT: Mass scales and Large Extra Dimensions

## Mass scales and Large Extra Dimensions

In Heterotic Strings  $g_s^2/\hat{V}_{int} = g_{YM}^2$  so that

$$M_s^2 = g_{YM}^2 M_{Pl}^2$$

To have  $M_{BH} \sim M_s \sim TeV$ , need implausibly small gauge coupling  $g_{YM} \sim 10^{-15} \rightarrow$  **very difficult to accommodate LED**.

In theories with open and un-oriented strings  $g_s \hat{V}_\perp / \hat{V}_{T^6} = g_{YM}^2$  with  $\hat{V}_\perp$  volume of internal space transverse to 'visible' D-branes

$$M_s^2 = g_{YM}^4 M_{Pl}^2 \frac{\hat{V}_{int}^2}{\hat{V}_\perp^2}$$

compatible with reasonably small  $g_{YM}$ , low string scale (*i.e.* BH or HS masses) and large extra (transverse) directions. BH's as bound-states of D-branes, dynamical properties more involved!

## Vertex Operators and BRST invariance

Two-charge massive 1/2 BPS states in NS sector ( $N = 0, \dots, 9$ )

$$V_{1/2BPS}^{(-1)} = \Phi_{N, A_1 \dots A_n}^{(N_R)} e^{-\varphi} \psi^N e^{i\mathbf{p}_L \cdot \mathbf{X}_L} \prod_{r=1}^n \bar{\partial}^{\ell_r} X^{A_r} e^{i\mathbf{p}_R \cdot \mathbf{X}_R} e^{i\mathbf{p} \cdot \mathbf{X}}$$

with  $p^2 = -M^2 = -|\mathbf{p}_L|^2$  and  $\Phi^{(N_R)}[\bar{\partial}^{\ell} X^A]$  polynomial of degree  $N_R = \sum_r \ell_r = 1 + \mathbf{nm} - \frac{1}{2}|\mathbf{r}|^2$  in derivatives of R-moving (internal) bosonic coordinates  $A = 0, \dots, 25$  ( $A \rightarrow \mu, i, a$ )

$$J = J_L + J_R \quad J_R^{Max} = N_R \quad J_{L, 1/2BPS}^{Max} = 1$$

Further BRST conditions (schematically)

$$P_L^M \Phi_{M, A_1 \dots A_n}^{(N_R)} = 0 \quad P_R^{A_r} \Phi_{M, A_1 \dots A_r \dots A_n}^{(N_R)} = 0 \quad \forall r$$

$$\eta^{A_r A_s} \Phi_{M, A_1 \dots A_r \dots A_s \dots A_n}^{(N_R)} = 0 \quad \forall r, s$$

## (No) tri-linear amplitudes among 1/2 BPS states

$$V_{1/2BPS}^{(-1)} = A_M \psi^M e^{-\varphi} e^{iPX} V_R$$

where  $\psi^M = (\psi^\mu, \psi^i)$  and  $V_R$  Right-moving part (bosonic string)

$$P^2 = 0 = p^2 + |p_L|^2 \quad P^M A_M = p^\mu a_\mu + p_L^i \phi_i = 0$$

*i.e.* Left-moving part identical to massless in  $D = 10$ .

$$G_L(z_1, z_2, z_3) = \langle cV_L^{(-1)}(z_1)cV_L^{(0)}(z_2)cV_L^{(-1)}(z_3) \rangle$$

where  $V_L^{(0)}(z) = A_M(\partial X^M + iP\psi\psi^M)e^{iPX}$ . Contractions yield

$$G_L = [A_1(P_2 - P_3)A_2A_3 + A_2(P_3 - P_1)A_3A_1 + A_3(P_1 - P_2)A_1A_2] \delta\left(\sum_i P_i\right)$$

independent of  $z_i$ , totally anti-symmetric and vanishing on-shell.

## First massive level, NS sector (Left-movers)

$$V_H = H_{(MN)}[\partial X^M \partial X^N + iP\psi\psi^M \partial X^N + \psi^M \partial\psi^N]e^{iPX}$$

massive spin 2, 44 physical polarizations and

$$V_C = C_{[LMN]}(\partial X^L + iP\psi\psi^L)\psi^M\psi^N e^{iPX}$$

massive 3-form, 84 physical polarizations

Altogether 128 bosonic and as many fermionic dof's ( $256 = 2^8$ )

Tri-linear couplings = Physical (Left-moving) Amplitudes

$$G_L^{HAA} = H_{MN}F_1^{ML}F_{2L}^N \quad \text{with} \quad F_{MN} = P_M A_N - P_N A_M$$

and

$$G_L^{CAA} = (P_1 - P_2)^L A_1^M A_2^N C_{LMN}$$

both symmetric under 1-2 exchange and gauge invariant

$$\psi_{-3/2}^i |0\rangle \longrightarrow 8 = \square$$

$$\alpha_{-1}^i \psi_{-1/2}^j |0\rangle \longrightarrow 64 = \bullet + \square\square + \begin{array}{|c|} \hline \square \\ \hline \square \\ \hline \end{array}$$

$$\psi_{-1/2}^i \psi_{-1/2}^j \psi_{-1/2}^k \longrightarrow 56 = \begin{array}{|c|} \hline \square \\ \hline \square \\ \hline \square \\ \hline \end{array}$$

d.o.f	$SO(9)$	$SO(8)$
84	$\begin{array}{ c } \hline \square \\ \hline \square \\ \hline \square \\ \hline \end{array}$	$\begin{array}{ c } \hline \square \\ \hline \square \\ \hline \square \\ \hline \end{array} + \begin{array}{ c } \hline \square \\ \hline \square \\ \hline \end{array}$
44	$\square\square$	$\bullet + \square + \square\square$

Table: First massive level (NS sector),  $SO(9)$  irreps

## Second massive level, NS sector (Left-movers)

$$\psi_{-5/2}^i |0\rangle \longrightarrow 8 = \square$$

$$\alpha_{-1}^i \psi_{-3/2}^j |0\rangle \longrightarrow 64 = \bullet + \square\square + \begin{array}{|c|} \hline \square \\ \hline \end{array}$$

$$\alpha_{-2}^i \psi_{-1/2}^j |0\rangle \longrightarrow 64 = \bullet + \square\square + \begin{array}{|c|} \hline \square \\ \hline \end{array}$$

$$\psi_{-3/2}^i \psi_{-1/2}^j \psi_{-1/2}^k |0\rangle \longrightarrow 224 = \square + \begin{array}{|c|} \hline \square \\ \hline \end{array} + \begin{array}{|c|c|} \hline \square & \square \\ \hline \end{array}$$

$$\alpha_{-1}^i \alpha_{-1}^j \psi_{-1/2}^k |0\rangle \longrightarrow 288 = \square + \square\square\square + \begin{array}{|c|c|} \hline \square & \square \\ \hline \end{array}$$

$$\alpha_{-1}^i \psi_{-1/2}^j \psi_{-1/2}^k \psi_{-1/2}^l |0\rangle \longrightarrow 448 = \begin{array}{|c|} \hline \square \\ \hline \end{array} + \begin{array}{|c|} \hline \square \\ \hline \end{array} + \begin{array}{|c|c|} \hline \square & \square \\ \hline \end{array}$$

$$\psi_{-1/2}^i \psi_{-1/2}^j \psi_{-1/2}^k \psi_{-1/2}^l \psi_{-1/2}^m |0\rangle \longrightarrow 56 = \begin{array}{|c|} \hline \square \\ \hline \end{array}$$

## Second massive level, $SO(9)$ decomposition

d.o.f	$SO(9)$	$SO(8)$
126		
156		$\bullet + \square + \square\square + \square\square\square$
594		
231		
36		
9		$\bullet + \square$

## Second massive level (Left-Movers), BRS conditions

$$P^L A_{[LMNPQ]} + E_{[MNPQ]} = 0$$

$$iP^N E_{M[NPQ]} + S_{(M[P]Q)} + C_{M[PQ]} = 0$$

$$iP^Q C_{M[PQ]} + M_{MP} + 2L_{PM} = 0$$

$$iP^M C_{M[PQ]} + 2L_{[PQ]} + \eta^{MN} E_{M[NPQ]} = 0$$

$$iP^Q S_{(MP)Q} + M_{(MP)} = 0$$

$$iP^N L_{MN} = 0$$

$$W_M + iP^N M_{MN} + \eta^{PQ} S_{(MP)Q} = 0$$

$$2iP^M W_M + \eta^{MN} M_{MN} - 2\eta^{MN} L_{MN} = 0$$

## Second massive level (Left-Movers), Vertex operators

$$S_{(MNP)}^{(156)} (\partial X^M \partial X^N \psi^P + \dots) e^{-\varphi} e^{iPX}$$

$$A_{[MNPQR]}^{(126)} \psi^M \psi^N \psi^P \psi^Q \psi^R e^{-\varphi} e^{iPX}$$

$$E_{(M[NPQ]}^{(594)} (\partial X^M \psi^N \psi^P \psi^Q + \dots) e^{-\varphi} e^{iPX}$$

$$C_{(M[NP]}^{(231)} (\partial \psi^M \psi^N \psi^P + \dots) e^{-\varphi} e^{iPX}$$

$$B_{[MN]}^{(36)} (\partial \psi^M \partial X^N + \dots) e^{-\varphi} e^{iPX}$$

$$V_M^{(9)} (\partial^2 \psi^M + \dots) e^{-\varphi} e^{iPX}$$

## R-movers 3-point couplings

For totally symmetric traceless tensors  $H^i_{(A_1 \dots A_{s_i})}$  (not necessarily first Regge trajectory) with  $t_i$  such that  $\sum_i s'_i$  even,  $s'_i = s_i - t_i$

$$G_R = \sum_{t_i \leq s_i} \sqrt{\alpha'}^{\sum_i t_i} \prod_i \binom{s_i}{t_i} \binom{s_i - t_i}{s'_{i,i+1}} P_{23}^{A_1} \dots P_{23}^{A_{t_1}} H_{A_1 \dots A_{t_1}}^1 D_{1 \dots D_{s'_1}} F_{1 \dots F_{s'_{12}}} P_{31}^{B_1} \dots P_{31}^{B_{t_2}} H_{B_1 \dots B_{t_2}}^2 F_{1 \dots F_{s'_{12}}} E_{1 \dots E_{s'_{23}}} P_{12}^{C_1} \dots P_{12}^{C_{t_3}} H_{C_1 \dots C_{t_3}}^3 E_{1 \dots E_{s'_{23}}} D_{1 \dots D_{s'_{31}}}$$

with  $s'_{ij} = (s'_i + s'_j - s'_k)/2$  and  $P_{ij}^A = P_i^A - P_j^A$ , (anti)symmetric under exchange of two identical vertex operators (say 1 and 2), for  $s_3$  even (odd)

For non-abelian current algebras

at  $N_R = 1$  currents  $J^a$  yield  $f_{abc} = \text{Tr}(T_a[T_b, T_c])$

at  $N_R = 2$  primary  $H_a = d_{abc} J^b J^c$  with  $d_{abc} = \text{Tr}(T_a\{T_b, T_c\})$ , symmetric coupling to two currents, similar to open strings

## Amplitudes for scalar mini BH's

Tree level amplitudes for pair production of **charged scalar BH's**

$$\mathcal{A}_{vv \rightarrow \Phi \bar{\Phi}} = \int d^2z \langle V_{\Phi}(p_1) V_v(k_2; a_2) V_v(k_3; a_3) V_{\bar{\Phi}}(p_4) \rangle$$

$$\mathcal{M}_{hh \rightarrow \Phi \bar{\Phi}} = \int d^2z \langle V_{\Phi}(p_1) V_h(k_2; h_2) V_h(k_3; h_3) V_{\bar{\Phi}}(p_4) \rangle$$

$V_v, V_h, V_{\Phi}, V_{\bar{\Phi}}$  vertex operators for vector bosons, gravitons and small BPS BH's. Relevant integrals ( $\alpha' = 2$ )

$$\mathcal{I}(a, n, b, m) = \int d^2z |z|^a |1-z|^b z^n (1-z)^m$$

produce **Shapiro-Virasoro-like 'form factors'**

$$\mathcal{F}_{SV} = \frac{\Gamma(1 + k_2 k_3) \Gamma(k_2 p_1) \Gamma(k_2 p_4)}{\Gamma(2 - k_2 k_3) \Gamma(-k_2 p_1) \Gamma(-k_2 p_4)}$$

up to rational function of  $p$ 's

## Three simple cases with $N_R = 2$

- ▶ 2 Vectors - 2 small BH amplitude: mutually neutral case
- ▶ 2 Vectors - 2 small BH amplitude: mutually charged case
- ▶ 2 Gravitons - 2 small BH amplitude

## 2 Vectors - 2 small BH: mutually neutral case

Small BH's charged wrt  $U(1)^6$  ('hidden' gauge group) but **neutral wrt to  $G$**  ('visible' non-abelian gauge group) of the incoming gauge bosons

$$\mathcal{A}_{\nu\nu\rightarrow\Phi\bar{\Phi}}^{ij,a,b,kl}(p_i) = \frac{6g_{YM}^2}{M_s^2} (2\pi)^4 \delta(\Sigma_i p_i) (\tilde{a}_2 \tilde{a}_3) \mathcal{F}_{SV} F \delta_{\perp}^{ik} \bar{\delta}_{\perp}^{jl} \delta^{ab}$$

$$\delta_{\perp}^{ik} = \delta^{ik} - p_L^i p_L^k / M^2, \quad \bar{\delta}_{\perp}^{jl} = \delta^{jl} - p_R^j p_R^l / |\mathbf{p}_R|^2$$

$F = (k_2 p_1)(k_3 p_1) / (k_2 k_3)$  ubiquitous kinematical factor

$\tilde{a}_i = a_i - (p_4 a_i / p_4 k_i) k_i$  manifestly **gauge invariant**

'Formal' **field theory limit**  $\alpha' \rightarrow 0$  ( $M_s \rightarrow \infty$ ) with fixed  $M$ ,

$\mathcal{F}_{SV} \rightarrow 1$ : **graviton exchange**, suppressed by  $g_{YM}^2 / M_s^2 \sim 1 / M_{Pl}^2$

## 2 Vectors - 2 small BH: mutually charged case

Small BH's **charged** wrt to incoming gauge bosons (**G group**)

$$\mathcal{A}_{\nu\nu\rightarrow\Phi\bar{\Phi}}^{ika,b,c,jld}(p_i) = \frac{g_{YM}^2}{M_s^2} (2\pi)^4 \delta(\Sigma_i p_i) \delta_{\perp}^{ij} \bar{\delta}_{\perp}^{kl} (\tilde{a}_2 \tilde{a}_3) F \mathcal{F}_{SV} \mathcal{I}$$

where

$$\mathcal{I} = \left\{ T_{13} T_{24} + 2 T_{[13][24]} + \frac{2(2 + \alpha' k_3 p_4)}{\alpha' k_3 p_1} [T_{13} T_{24} + T_{[13][24]}] \right. \\ \left. + \frac{(4 + \alpha' k_3 p_4)(2 + \alpha' k_3 p_4)}{\alpha' k_3 p_1 (2 - \alpha' k_3 p_1)} T_{13} T_{24} + (2 \leftrightarrow 3) \right\} + T_{14} T_{23}$$

with  $T_{ij} = \text{tr}(T_{a_i} T_{a_j})$  and  $T_{[ij][kl]} = \text{tr}([T_{a_i}, T_{a_j}][T_{a_k}, T_{a_l}])$   
'Formal' field theory limit  $\alpha' \rightarrow 0$  ( $M_s \rightarrow \infty$ ) with fixed  $M$ ,  
 $\mathcal{F}_{SV} \rightarrow 1$ , only terms with 'poles' survive, **SYM theory result**.  
Relative suppression  $\mathcal{A}_{neutral}/\mathcal{A}_{charge} \sim 1/M_s^2$ .

## 2 Gravitons - 2 small BH's

Use 'factorized' graviton polarization tensors  $h_{\mu\nu}^{(2\lambda)} = a_\mu^{(\lambda)} a_\nu^{(\lambda)}$

$$\mathcal{M}_{hh \rightarrow \Phi \bar{\Phi}}^{ij,kl}(p_i) = 6 \cdot \frac{16\pi}{M_{Pl}^2} (2\pi)^4 \delta(\Sigma_i p_i) \mathcal{F}_{SV} F \delta_\perp^{ik} \bar{\delta}_\perp^{jl} \left[ (\tilde{h}_2 \tilde{h}_3) + \mathcal{H} \right]$$

where  $\tilde{h}_{i\mu\nu} = \left( \delta_\mu^\rho - \frac{k_{i\mu} p_4^\rho}{p_4 k_i} \right) \left( \delta_\nu^\sigma - \frac{k_{i\nu} p_4^\sigma}{p_4 k_i} \right) h_{\rho\sigma}$  manifestly gauge invariant and  $\mathcal{H}$  **higher-derivative  $\alpha'$  corrections**

$$\mathcal{H} = \frac{\alpha'}{2} \left\{ -(k_2 k_3) (\tilde{h}_2 \tilde{h}_3) + (k_2 k_3) (h_2 h_3) - (k_3 h_2 h_3 k_2) + \left[ \frac{(k_2 k_3) (p_1 h_2 h_3 p_4) - (p_4 h_3 k_2) (p_1 h_2 k_3)}{k_3 p_4} + (2 \leftrightarrow 3) \right] \right\}$$

'Formal' field theory limit  $\alpha' \rightarrow 0$ ,  $\mathcal{F}_{SV} \rightarrow 1$ , **gravitational amplitude  $\tilde{h}_2 \tilde{h}_3 \sim$  square of gauge theory amplitude  $\tilde{a}_2 \tilde{a}_3$**  [Kawai,

Lewellen, Tye; Choi, Shim, Song; ...]

Again relative suppression  $\mathcal{M}/\mathcal{A}_{charge} \sim 1/M_s^2$

## Differential Cross Section

Average over initial helicities and sum over **final scalar BH states** get differential cross section for the **charged case**

$$\frac{d\sigma}{d\Omega} = \frac{3g_{YM}^4 d(N_R)^2}{(8\pi)^4 M_5^2} \sqrt{1 - \mu^2} [(1 - \mu^2)^2(1 - x^2)^2 + \mu^4] \langle \mathcal{I}^2 \rangle_c$$
$$\frac{\hat{s}^3 \sin^2(\pi \hat{s})}{(1 + \hat{s})^2} \left| \sum_{n=0}^{\infty} \frac{\mathcal{R}_n(\hat{s})}{(a_n + bx)} \right|^2 \left| \sum_{k=0}^{\infty} \frac{\mathcal{R}_k(\hat{s})}{(a_k - bx)} \right|^2$$

$$\hat{w} = \alpha' w/4, \mu = M/E \leq 1, a_n = n + \hat{s}/2, b = (\hat{s}/2)\sqrt{1 - \mu^2},$$
$$\mathcal{R}_n(w) = (-1)^n (w - 1) \dots (w - n)/n!, x = \cos \theta.$$

- ▶ Threshold at  $\mu = 1$
- ▶ **Modulation** by the Regge poles, *i.e.* string excitations
- ▶ NO (significant) growth with energy, **Regge behaviour** (exponentially suppressed) in UV!

## Conclusions and Outlook

- ▶ **Huge suppression** of processes mediated by gravitons, but **relative suppression** wrt 'charged' ones  $\sim 1/M_S^2$
- ▶ **Regge poles** and **soft UV behaviour** rather than growth with CM Energy
- ▶ 1/2 BPS HS states look perturbatively stable ... may need to reconsider microscopic derivation of BH Entropy
- ▶ Similar results for **FHSV model** with  $\mathcal{N} = 2$  ( $Z_2$  shift-orbifold)
- ▶ Extremal (and thus charged) non BPS: similar story (stable)
- ▶ Non-extremal: M and S depend on  $g_s$  and moduli ... further dynamical test for string/BH correspondence principle
- ▶ Very difficult to accommodate LED and low string tension in Heterotic Strings, yet ... Local GUTs and Heterotic Landscape

[H. P. Nilles, M. Ratz, ...] or add NS5-branes [I. Antoniadis, K. Benakli, ...]