



## Precision Measurements at Hadron Colliders

### C.-P. Yuan

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I thank my collaborators for providing many useful slides. Special thanks to Chuan-Ren Chen, Qing-Hong Cao, Hong-Liang Lai, Pavel Nadolsky, and Wu-Ki Tung.

C T E Q

### Era of Precision Measurements @ $e^-e^+$



By comparing measurements and theoretical prediction of electroweak precision observables

- the electroweak sector of Standard Model (SM) is probed at the quantum-loop level
- the consistency of SM is checked by comparing direct measurements with indirect determinations of input parameters, e.g. m<sub>t</sub> and M<sub>w</sub>.
- the parameters of models beyond the SM can be constrained.

Global SM fit to all electroweak data: from LEPEWWG (Winter 2004)



	Measurement	Fit	$ O^{\text{meas}}-O^{\text{fit}} /\sigma^{\text{meas}}$ 0 1 2 3
$\Delta \alpha_{had}^{(5)}(m_Z)$	$0.02761 \pm 0.00036$	0.02770	
m <sub>z</sub> [GeV]	$91.1875 \pm 0.0021$	91.1874	
Γ <sub>z</sub> [GeV]	$2.4952 \pm 0.0023$	2.4965	-
$\sigma_{had}^0$ [nb]	41.540 ± 0.037	41.481	
R <sub>I</sub>	$20.767 \pm 0.025$	20.739	
A <sup>0,I</sup>	$0.01714 \pm 0.00095$	0.01642	
$A_{I}(P_{\tau})$	$0.1465 \pm 0.0032$	0.1480	-
R <sub>b</sub>	$0.21630 \pm 0.00066$	0.21562	
R <sub>c</sub>	$0.1723 \pm 0.0031$	0.1723	
A <sup>0,b</sup>	$0.0992 \pm 0.0016$	0.1037	
A <sup>0,c</sup>	0.0707 ± 0.0035	0.0742	
Ab	$0.923 \pm 0.020$	0.935	
A <sub>c</sub>	$0.670 \pm 0.027$	0.668	
A <sub>I</sub> (SLD)	$0.1513 \pm 0.0021$	0.1480	
$sin^2 \theta_{eff}^{lept}(Q_{fb})$	$0.2324 \pm 0.0012$	0.2314	
m <sub>w</sub> [GeV]	$80.425 \pm 0.034$	80.390	
Г <sub>w</sub> [GeV]	$2.133 \pm 0.069$	2.093	-
m <sub>t</sub> [GeV]	178.0 ± 4.3	178.4	
			0 1 2 3





 Most precise measurement of W boson mass was done at Tevatron.

 Most precise measurement of Top quark mass was done at Tevatron.

## Phase II: Precision Measurements



B 🎎















 Precision measurements at Tevatron Run-2 and LHC: W/Z Physics

 Impact of New CTEQ Parton Distribution Functions to LHC Phenomenology: W/Z, Top and Higgs Physics





### *W*-boson physics

- W-boson production and decay at hadron collider
- 2 How to measure W-boson mass and width?
- High order radiative corrections:
  - **QCD** (NLO, NNLO, Resummation)
  - EW (QED-like, NLO)
- **4** ResBos-A and its predictions



### W-boson production at hadron colliders













### W-boson Decay



Hadronic mode 



unknown  $p_{z}^{\nu}$   $\longrightarrow$  cannot reconstruct invariant mass of W boson

Transverse momentum of the charged lepton



 $p_T^e$ 

In (ud) c.m. system,

 $\mathbf{C} \mathbf{T} \mathbf{E} \mathbf{Q}$ 



Jacobin factor

$$\frac{\mathrm{d}\cos\theta}{\mathrm{d}\hat{p}_T^2} = -\frac{2}{\hat{s}} \frac{1}{\sqrt{1 - \frac{4\hat{p}_T^2}{\hat{s}}}}$$
$$\implies \frac{\mathrm{d}\hat{\sigma}}{\mathrm{d}\hat{p}_T^2} \sim \frac{\mathrm{d}\hat{\sigma}}{\mathrm{d}\cos\theta} \times \frac{1}{\sqrt{1 - 4\hat{p}_T^2/\hat{s}}}$$









• Definition:

$$m_T^2(\ell,\nu) = 2 p_T^{\ell} p_T^{\nu} (1 - \cos \phi_{\ell\nu})$$
from overall  $p_T$  imbalance

$$\implies \frac{\mathrm{d}\hat{\sigma}}{\mathrm{d}m_T^2} \sim \frac{1}{\sqrt{1 - m_T^2/\hat{s}}}$$



unaffected by longitudinal boosts of  $\ell \nu$  system

 $\mathbb{R}$  not sensitive to  $q_T^W$ 

tail knows about  $\Gamma_W$  (direct measurement)

:

sensitive region for measuring  $M_W$ :  $M_T \sim 60 - 100 \text{GeV}$  $\Gamma_W M_T > 100 \text{ GeV}$ 

# **CTEQ** Theory requirements for Tevatron Run-II and LHC:



- Theory framework for Tevatron Run-I
  - $O(\alpha_S)$  (NLO-QCD) corrections
  - $O(\alpha)$  (QED) corrections
- Run-II experimental targets:  $\delta \sigma_{tot} / \sigma_{tot} \sim 2 - 3\%$  $\delta M_W \sim 30 \text{ MeV}$
- Many factors contribute at a percent level:
  - $O(\alpha_s^2)$  (NNLO-QCD) corrections
  - $O(\alpha)$  (NLO-EW) corrections
  - uncertainties of parton distributions
  - power corrections to resummed cross sections

Adequate for comparison to Run-I data

Task: consistent and efficient implementation of these effects





#### NNLO hard cross section







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# **Rapidity distributions**

- Little shape difference from NLO to NNLO
  - K-factor should be sufficient
- Z rapidity distributions could/will be used as input for pdf fits







- Cannot describe data with small  $q_T$  of W-boson.
- Cannot precisely determine  $m_W$  at hadron colliders without knowing the transverse momentum of W-boson. Most events fall in the small  $q_T$  region.















W-boson production and decay How to measure W mass and width High order radiative corrections ResBos-A and its predictions

Theory requirements for Run-II High order QCD corrections (NLO, NNLO, Resum) High order EW corrections ResBos-A and its predictions

#### What is QCD resummation?

All order quantum corrections



Resummation is to reorganize the results in terms of the large Log's.

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#### What is QCD resummation ?

reorganization of logs



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#### CSS resummation formalism

[Non-perturbative functions] are functions of  $(b,Q,x_A,x_B)$  which include QCD effects beyond Leading Twist.

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#### Resummation effects agree with data very well

### $P\bar{P} \rightarrow Z$ @ Tevatron

Predicted by ResBos:

A fortran program that includes the effect of multiple soft gluon emission on the production of W and Z bosons in hadron collisions.



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• Difference between u(x) and d(x) in proton cause  $u\bar{d} \to W^+$  and  $\bar{u}d \to W^-$  to be boosted in opposite directions





## **Rapidity Distribution**

C T E Q





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All recent CTEQ and MSTW PDF fits include the effects of soft gluon resummation predicted by ResBos.





• The complete NLO EW correction to W and Z boson production in hadron collisions are known.

• The NLO QED corrections to the decay of W and Z bosons can be factored out from the complete NLO EW corrections in a gauge invariant way.

NLO EW corrections to W boson production



Born

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pure weak contribution



₩-Z box contribution



**virtual photon contribution** 



real photon contribution



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ResBos-A and its predictions

#### EW corrections (QED-like)



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• **ResBos-A**: improved **ResBos** by including final state NLO QED corrections



to W and Z production and decay

hep-ph/0401026

Qing-Hong Cao and CPY

and

denote FQED radiation corrections, which dominates the W mass shift.





## W Mass @ CDF Run-2

 $W \rightarrow ev$  transverse mass distribution



Statistical error only.





 $p_T^e$  is sensitive to  $q_T^W$ 







## W Boson $q_T$ @ D0 Run-2

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## Z-boson physics

- Help to improve the measurement of W-boson
  - 🖙 calibrate detector
  - indirect measurement of W-boson width
- **2** ResBos-A and its predictions
  - effective Born approximation
  - various kinematical distributions

CTEQ

### Precision measurement of Z-boson



#### R help to calibrate detector



Combine lepton and neutrino  $p_{\tau}$  to form transverse mass  $(m_{\tau})$  for best statistical power

CDF RUN II 200 100 20  $p_T^Z$  (GeV)

muon

neutrino





Photon and Z interference effect has been implemented, therefore ResBos-A can be use to low energy Drell-Yan process.

 $\mathbf{C} \mathbf{T} \mathbf{E} \mathbf{Q}$ 

 $\gamma/Z$ 

Effective Born Approximation is adopted in order to include the dominant higher order EW corrections around the Z-pole.

$$\alpha \to \alpha(\hat{s})$$
,  $v_f \to v_f^{\text{eff}} = \frac{1}{2s_w} \frac{M_Z}{M_W} (I_3^f - 2Q_f \sin^2 \theta_{\text{eff}}^f)$ 

Effect from pQCD soft gluon resummation is included, at the same level of accuracy as that for W boson production and decay.


# Z Mass @ CDF Run-2



### $Z{\rightarrow}\mu{+}\mu{-}$ invariant mass distribution





- 1. We are entering the era of precision measurement at hadron colliders.
- 2. For precision measurement of W mass, it is needed to include both QCD and EW corrections consistently and efficiently.

As the first step toward this goal, ResBos-A includes both the initial state multiple soft gluon resummation effect and final state QED corrections (which dominates the W mass shift).

3. Precision measurement of Z boson, via the ratio method, can improve W-boson mass measurement and provide indirect measurement of W-boson width.







# Impact of New CTEQ Parton Distribution Functions to LHC Phenomenology:

### W/Z, Top and Higgs Physics



## New Physics signal found?



## Cross sections at the LHC



- Experience at the Tevatron is very useful, but scattering at the LHC is not necessarily just "rescaled" scattering at the Tevatron
- Small typical momentum fractions x in many key searches
  - dominance of gluon and sea quark scattering
  - large phase space for gluon emission
  - intensive QCD backgrounds
  - or to summarize,...lots of Standard Model to wade through to find the BSM pony

#### LHC parton kinematics



### **LHC Parton Kinematics**





Impact of new CTEQ PDF sets to SM processes: *W*, *Z*, top, Higgs

### CTEQ6.6 PDF's, heavy flavors and PDF induced correlations between LHC observables

In collaboration with

Hong-Liang Lai, Pavel Nadolsky, Qing-Hong Cao, Joey Huston, Jon Pumplin, Dan Stump, Wu-Ki Tung

#### Global analysis at Michigan State/Taiwan/Washington

a part of the Coordinated Theoretical Experimental study of QCD (CTEQ) in U.S.A.

development of general-purpose PDF's

(Wu-Ki Tung and collaborators)

new CTEQ6.6M standard set and 44 extreme eigenvector sets (arXiv:0802.0007)

- improved treatment of s, c, b PDF's
- correlation analysis of collider observables
- available in the LHAPDF-5.4 library and at www.cteq.org

#### "Standard candle" processes: $W, Z, t\bar{t}$ production

- Cross sections for  $pp \rightarrow W^{\pm}X$ ,  $pp \rightarrow Z^{0}X$  at the LHC can be measured with accuracy  $\delta\sigma/\sigma \sim 1\%$  (tens of millions of events even at low luminosity)
- These measurements will be employed to monitor the LHC luminosity in real time and tightly constrain PDF's (Dittmar, Pauss, Zurcher; Khoze, Martin, Orava, Ryskin; Giele, Keller'....)

We will see that  $t\bar{t}$  production may also potentially become a calibration process at the LHC because of its strong anticorrelation with Z production

#### CTEQ6.6 PDF's



dashes: CTEQ6.1M (zero-mass scheme)

CTEQ6.6 u, d are above CTEQ6.1 at  $x \leq 10^{-2}$ 

- The result of suppressed charm contribution to F<sub>2</sub>(x, Q) at HERA in the GM-VFN scheme
- very different strange PDF's

#### Impact of charm contributions to DIS at HERA



■ W,Z production at the LHC:  $x \sim 10^{-3} - 10^{-2}$ 

Suppression of charm contribution to  $F_2(x, Q^2)$  in the GM-VFN scheme results in larger  $(\bar{u}^0(x), (\bar{d}^0(x))$  at small  $x \Rightarrow$  larger  $\sigma_{W,Z}^{LHC}$ 

 $\delta \bar{q}_{light}(x)/\bar{q}_{light}(x) = 3\% \quad \Rightarrow \quad \delta \mathcal{L}_{q_i \bar{q}_j}/\mathcal{L}_{q_i \bar{q}_j} = 2(\delta \bar{q}_{light}/\bar{q}_{light}) = 6\%$ 







At large x, the extremes are given by eigenvector sets 23,24 and 31,32.

#### W and Z cross sections at the LHC



- Such changes in  $\sigma_{Z,W}$  exceed NNLO corrections or anticipated experimental error of  $\sim 1\%$
- Two latest MSTW predictions are compatible with the CTEQ6.6 result

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HERA-LHC workshop

#### W and Z cross sections at the LHC



At the LHC,  $\sigma_{W,Z}$  (CTEQ6.6M) $\approx 1.06\sigma_{W,Z}$  (CTEQ6.1M)

► reflects a 6% increase in light quark luminosities  $\mathcal{L}_{q_i\bar{q_j}}(x_1, x_2, Q) = q_i(x_1, Q)\bar{q_j}(x_2, Q)$  at relevant x and Q

Pavel Nadolsky (MSU)



- NLO calculations using ResBos, WTTOT, MCFM
- CTEQ6.5 and CTEQ6.6 cross sections are qualitatively same
- At LHC,  $\sigma_{W,Z}$  (CTEQ6.6M) $\approx 1.06\sigma_{W,Z}$  (CTEQ6.1M)
  - ► reflects a 6% increase in light quark luminosities  $\mathcal{L}_{q_i\bar{q}_i}(x_1, x_2, Q) = q_i(x_1, Q)\bar{q}_j(x_2, Q)$  at relevant x and Q

finer differences with CTEQ6.5 in precision predictions for W, Z production, strange-quark scattering

#### Correlations and ratio of W and Z cross sections



Radiative contributions, PDF dependence have similar structure in W, Z, and alike cross sections; cancel well in Xsection ratios

#### Correlations between physical observables through PDF degrees of freedom

Misleadingly simple questions

- 1. Why are PDF induced variations in  $\sigma_W$  and  $\sigma_Z$  strongly correlated?
- 2. Since both *W* and *Z* are mostly produced in light-quark scattering, is their PDF uncertainty mostly coming from light-quark PDF's?
- 3. How can we test this?

Answers can be found by systematically studying correlations in the PDF parameter space

#### An inefficient application of the Hessian method

Compute  $\sigma_W$  for 44 extreme PDF eigensets

Eventual eigenparameter(s) producing largest variation(s), such as #4 or 8



 $\bigcirc$  Check that the same eigenparameters produce largest variations in  $\sigma_Z$ 

 $\Theta$ It is not obvious how to relate abstract eigenparameters to physical PDF's u(x), d(x), etc.

#### Correlation analysis for collider observables

(J. Pumplin et al., PRD 65, 014013 (2002); P.N. and Z. Sullivan, hep-ph/0110378)

A technique based on the Hessian method

For 2N PDF eigensets and two cross sections X and Y:

$$\Delta X = \frac{1}{2} \sqrt{\sum_{i=1}^{N} \left( X_i^{(+)} - X_i^{(-)} \right)^2}$$

$$\cos \varphi = \frac{1}{4\Delta X \, \Delta Y} \sum_{i=1}^{N} \left( X_i^{(+)} - X_i^{(-)} \right) \left( Y_i^{(+)} - Y_i^{(-)} \right)$$

 $X_i^{(\pm)}$  are maximal (minimal) values of  $X_i$  tolerated along the *i*-th PDF eigenvector direction; N = 22 for the CTEQ6.6 set

#### Correlation angle $\varphi$

Determines the parametric form of the X - Y correlation ellipse

 $X = X_0 + \Delta X \cos \theta$  $Y = Y_0 + \Delta Y \cos(\theta + \varphi)$ 



 $\cos \varphi \approx \pm 1$ :  $\cos \varphi \approx 0$ : Measurement of X imposes  $\begin{array}{c} \text{tight} \\ \text{loose} \end{array}$  constraints on Y



Somewhat surprisingly, the remaining PDF uncertainty is mostly due to s(x)

#### Correlations of Z and $t\bar{t}$ cross sections with PDF's

LHC Z, W cross sections are strongly correlated with g(x), c(x), b(x) at  $x \sim 0.005$ 

: they are strongly anticorrelated with processes sensitive to g(x) at  $x \sim 0.1$  ( $t\bar{t}, gg \rightarrow H$  for  $M_H > 300$ GeV) as a consequence of momentum sum rule



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#### $t\bar{t}$ vs Z cross sections at the LHC



Measurements of  $\sigma_{t\bar{t}}$  and  $\sigma_Z$  probe the same (gluon) PDF degrees of freedom at different x values

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May 28, 2008 12

#### Correlations between $\sigma(gg \rightarrow H^0), \sigma_Z, \sigma_{t\bar{t}}$



As  $M_H$  increases:  $\cos \varphi(\sigma_H, \sigma_Z)$ decreases  $\cos \varphi(\sigma_H, \sigma_{t\bar{t}})$ 

increases

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#### $t\bar{t}$ production as a standard candle process

- Measurements of  $\sigma_{t\bar{t}}$  with accuracy ~ 5% may be within reach
- would provide additional constraints on the large-x gluon PDF
- will be useful for monitoring of  $\mathcal{L}_{LHC}$  luminosity in the first years and normalization of LHC event rates

See also the talk by M. Csakon; Moch, Uwer, arXiv:0804.1476; Cacciari et al., arXiv:0804.2800; Kidonakis, Vogt, arXiv:0805.3844

### **Top Quark Pair production rates**





### DØ Runll Preliminary









• What's the top mass in a full event generator, such as PYTHIA?

## NOBODY KNOWS

Parton showers generate some higher order corrections in the event shape, but with approximations.

#### Conclusions

- CTEQ6.6 study confirms most findings of the CTEQ6.5 analyses; predicts some differences in cross sections for heavy-flavor scattering, LHC EW precision physics
- Free parameters in CTEQ6.6 strange PDFs probe a new direction in the PDF parameter space, affect predictions for strange-quark scattering,  $\sigma_Z/\sigma_W$  at the LHC
- Analysis of correlations in PDF parameter space is a powerful technique to understand relations between physics observables through shared PDF degrees of freedom
- At the LHC, CTEQ6.6 tt cross section is anticorrelated with Z cross section via the gluon PDF; can potentially be used as an additional observable to monitor the LHC luminosity



# **NNLO Higgs**



- Substantial contributions to Higgs cross section from LO to NLO and from NLO to NNLO
- For this reason, Higgs cross sections most often calculated to NNLO (with NNLO pdf's)





# gg->H with MSTW08



- Higgs cross section at NNLO is 30% (115 GeV) to 9% (300 GeV) larger at the LHC now than in 2003
- Tevatron cross section is +9% (115 GeV) to -9% (200 GeV)
- About half or more of the effect is from the changes in the gluon distribution in MRST->MSTW
  - for low x <0.05, MSTW2008 gluon > MRST2002 gluon
  - for moderate x, 0.05<x<0.5, MRST2002 gluon > MSTW2008 gluon
- (Most of ) rest of change is from increase in  $\alpha_s$  at NNLO
  - 0.1154->0.1171
  - note that α<sub>s</sub> is included in the global fit; CTEQ fixes it at world average
- EW corrections also cause some change





# Change in gluon



- About half of the change happened in 2006 and half in 2008
- Due (at least partially) to changes in the heavy quark scheme
  - more light quarks needed at small x
  - flavor threshold effects more complicated in MSTW approach than in CTEQ due to counting of orders (see arXiv:0809.0714)



 Change may have worked for Barack Obama but it upsets experimentalists









- There's been some change in the CTEQ gluon distribution as well due to the switch to the heavy quark mass scheme, but not as much
- And since we use the world average of α<sub>s</sub> (and that hasn't changed much), the Higgs cross section predictions have been somewhat more stable







# **Comparisons at NLO**

10-1

10

10<sup>-2</sup>

10'1

10<sup>-1</sup>

х

х

х



CTEQ and MSTW fairly close in x range for Higgs production at LHC





# **Compare gluons**







# W and Z cross sections



 CTEQ6.6 and MSTW2008NLO predictions for W and Z cross sections agree amazingly well

 Compare to situation with MRST2004 and CTEQ6.6








 Precision measurements at Tevatron Run-2 and LHC: W/Z Physics

 Impact of New CTEQ Parton Distribution Functions to LHC Phenomenology: W/Z, Top and Higgs Physics





## **Backup Slides**



## W Boson Mass Uncertainties (MeV)



48



Important for a measurement with 25 MeV uncertainty (4 fb<sup>-1</sup>)

## CTEQ

## **CTEQ PDF** parametrization



- PDF's (f<sub>a</sub>(x,Q)) are parametrized with a flexible form motivated by physics considerations (Regge behavior, spectator counting, for example) at fixed small Q<sub>o</sub> (1.3 GeV for CTEQ) and then evolved for Q>Q<sub>o</sub> by DGLAP
  - assume for most of the general analyses that the c and b distributions are zero at scales below their masses and are generated by QCD evolution above
- Parametrization of parton distributions at Q<sub>o</sub> used to obtain the CTEQ5 and CTEQ6 parton distributions contained 5 shape parameters (apart from normalization) for each flavor
  - global analysis data sets not sufficiently constraining to determine all of the parameters, so a number are frozen at some particular (motivated) values
  - 20 free parameters for CTEQ6.1/6.5 and 22 for CTEQ6.6 (see next slide)
- For CTEQ6.5/6.6, adopt a simpler form with 4 shape parameters for the valence quarks u<sub>v</sub>(x), d<sub>v</sub>(x) and the gluon g(x)

$$f(x) = a_o x^{a_1} (1-x)^{a_2} e^{a_3 x + a_4 x^2}$$

a reasonable generalization of the conventional minimal form

$$f(x) = a_o x^{a_1} (1 - x)^{a_2}$$

- which combines Regge behavior at x->0 and spectator counting at x->1
- Both forms above are positive definite and have simplified logarithmic derivatives





- Is this form flexible enough?
- Remember the lesson of Tevatron Run-1 jets, where low x and high x PDFs can easily be (artificially) tied together through the parametrization.
- We find that significantly better fits cannot be achieved by introducing additional parameters or changing the functional form
  - NB: prior to CTEQ6.6, the analysis generally assumed

 $s(x) = \overline{s}(x) \propto \overline{d}(x) + \overline{u}(x)$ 

that ansatz has been dropped in CTEQ6.6