LHC Phenomenology of Type II Seesaw

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Outline

- Introduction to type II seesaw
  - Higgs spectrum and decay channels

EJC, Lee, Park, 0304069

- LHC search
  - Doubly charged Higgs production and decay
  - CMS result
- Same-sign tetra-leptons
  - Triplet-antitriplet oscillation

EJC & Sharma, 1206.6278

- Higgs Phenomenology
  - EWPD
  - Perturbativity & vacuum stability
  - Higgs-to-diphoton rate

EJC, Lee & Sharma, 1209.1303

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Introduction

- An SU(2) doublet boson (Y=1/2) is responsible for the masses of quarks and charged leptons as well as for the electroweak symmetry breaking.

July 4, 2012 !

- What about neutrino masses? Maybe due to an "SU(2) triplet boson (Y=1)" :

Type II Seesaw

- Peculiar prediction of a doubly charged boson:

$$\Delta = (\Delta^{++}, \Delta^{+}, \Delta^{0})$$

- Main search channel: $\Delta^{++} \rightarrow l^{+}\, l^{+}$

Type II Seesaw

- Introduce Higgs doublet (Y=1/2) & triplet (Y=1):

$$\Phi = (\Phi^+, \Phi^0) \qquad \Delta = \begin{pmatrix} \Delta^+/\sqrt{2} & \Delta^{++} \\ \Delta^0 & -\Delta^+/\sqrt{2} \end{pmatrix}$$

- Triplet VEV generates neutrino mass matrix:

$$\mathcal{L}_Y = f_{\alpha\beta}\, L_\alpha^T C i\tau_2 \Delta L_\beta + \frac{1}{\sqrt{2}}\mu\, \Phi^T i\tau_2 \Delta \Phi + h.c. \;\Rightarrow\; v_\Delta = \mu \frac{v_\Phi^2}{M_\Delta^2}$$

$$m^\nu_{\alpha\beta} = f_{\alpha\beta} v_\Delta \;\Rightarrow\; f_{\alpha\beta}\frac{v_\Delta}{v_\Phi} \sim 10^{-12}$$

- Collider can tell the neutrino mass pattern: Measure $\mathrm{BR}(\Delta^{++} \xrightarrow{f_{\alpha\beta}} l^+_\alpha l^+_\beta)$! EJC, Lee, Park, 0304069

Higgs sector

- Higgs potential of type II seesaw

$$
\begin{aligned}
V(\Phi,\Delta) = m^2\Phi^\dagger\Phi + M^2\mathrm{Tr}(\Delta^\dagger\Delta) \\
+ \lambda_1(\Phi^\dagger\Phi)^2 + \lambda_2[\mathrm{Tr}(\Delta^\dagger\Delta)]^2 + 2\lambda_3\mathrm{Det}(\Delta^\dagger\Delta) \\
+ \lambda_4(\Phi^\dagger\Phi)\mathrm{Tr}(\Delta^\dagger\Delta) + \lambda_5(\Phi^\dagger\tau_i\Phi)\mathrm{Tr}(\Delta^\dagger\tau_i\Delta) \\
+ \frac{1}{\sqrt{2}}\mu\Phi^T i\tau_2\Delta\Phi + h.c.
\end{aligned}
$$

- Five Higgs boson mass eigenstates

$$
\begin{matrix} \Delta^{++}, \Delta^{+}, \Delta^{0} \\ \Phi^{+}, \Phi^{0} \end{matrix} \Rightarrow h^0, H^0, A^0, H^+, H^{++}
$$

Higgs mixing

- Doublet-triplet mixing controlled by ξ = v_Δ/v_Φ:

$$\phi_I^0 = G^0 - 2\xi A^0 \qquad \phi^+ = G^+ + \sqrt{2}\xi H^+ \qquad \phi_R^0 = h^0 - a\xi\, H^0$$
$$\Delta_I^0 = A^0 + 2\xi G^0 \qquad \Delta^+ = H^+ - \sqrt{2}\xi G^+ \qquad \Delta_R^0 = H^0 + a\xi\, h^0$$

$$a = 2 + (4\lambda_1 - \lambda_4 - \lambda_5)v_\Phi^2/(M_{H^0}^2 - m_{h^0}^2)$$

- We will work in the limit of ξ << 1.
- (note) ρ parameter constraint:

$$\rho = (1+2\xi^2)/(1+4\xi^2) \rightarrow \xi < 0.03$$

Higgs spectrum

- Mass gap among triplet components:

$$\Delta M \approx \frac{\lambda_5}{g^2}\frac{M_W^2}{M} < M_W$$

$$M^2_{H^{\pm\pm}} = M^2 + 2\frac{\lambda_4 - \lambda_5}{g^2}M_W^2$$

$$M^2_{H^\pm} = M^2_{H^{\pm\pm}} + 2\frac{\lambda_5}{g^2}M_W^2$$

$$M^2_{H^0,A^0} = M^2_{H^\pm} + 2\frac{\lambda_5}{g^2}M_W^2 \,.$$

$$\Delta M = M_{H^+} - M_{H^{++}}$$

- Mass gap between H^0 & A^0:

$$\delta M_{HA} \approx 2M_{H^0}\frac{v_\Delta^2}{v_\Phi^2}\frac{M^2_{H^0}}{M^2_{H^0} - m^2_{h^0}}$$

$$\mathcal{L}_\Delta = \frac{1}{\sqrt{2}}\mu\Phi^T i\tau_2\Delta^\dagger\Phi + h.c. \Rightarrow -\mu v_\Phi h^0 H^0$$

$$v_\Delta = \frac{\mu v_\Phi^2}{\sqrt{2}M^2_{H^0}}$$

Higgs triplet decay channels

- Two mass hierarchies: EJC, Lee, Park, 0304069

$$M_{H^{++}} < M_{H^+} < M_{H^0/A^0} \quad \text{if} \quad \lambda_5 > 0$$

$$M_{H^{++}} > M_{H^+} > M_{H^0/A^0} \quad \text{if} \quad \lambda_5 < 0$$

- Gauge decays if ΔM (λ_5) large enough:

$$H^0/A^0 \to H^\pm W^\mp \to H^{\pm\pm} W^\mp W^\mp$$

$$H^{++} \to H^\pm W^\pm \to H^0/A^0 W^\pm W^\pm$$

$\Leftarrow$ $\Delta M(\lambda_5)$

Higgs triplet decay channels

- Di-lepton (same-sign) decays through $f_{\alpha\beta}$:

$$H^{++} \to l^+_\alpha l^+_\beta$$

$$H^+ \to l^+_\alpha \nu_\beta \qquad \Longleftarrow \quad f_{\alpha\beta}$$

$$H^0/A^0 \to \nu_\alpha \nu_\beta$$

- Di-quark/di-boson decays through ξ:

$$H^{++} \to W^+ W^+$$

$$\begin{aligned} H^+ &\to t\bar{b} \\ &\to ZW, hW \end{aligned} \qquad \Longleftarrow \quad \xi \equiv v_\Delta / v_\Phi$$

$$\begin{aligned} H^0/A^0 &\to t\bar{t},\ b\bar{b} \\ &\to ZZ, hh/Zh \end{aligned}$$

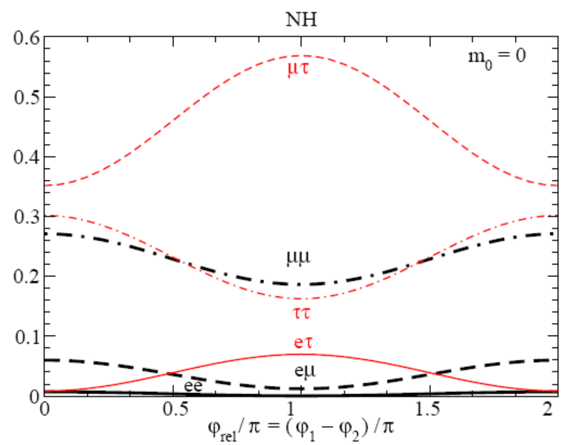
Best search channel: SSD from H^{++}

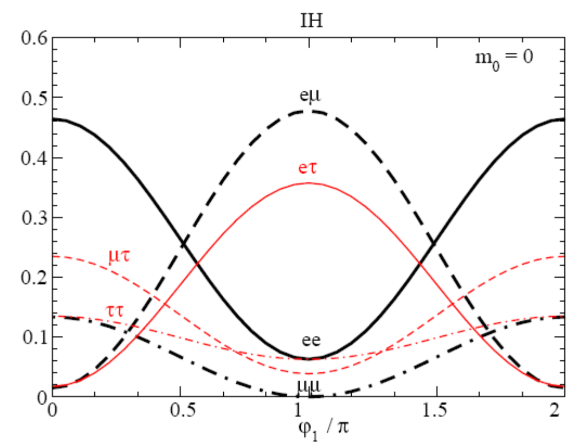
- Measure BR($H^{++} \rightarrow l^+ l^+$) to determine the neutrino mass pattern: e.g.) NH vs. IH

EJC, Lee, Park, 0304069
Garagoya, Schwetz, 0712.1453
Kadastik, Raidal, Lebane, 0712.3912
Akeroyd, Aoki, Sugiyama, 0712.4019
Perez, et.al., 0805.3536

$$\mathrm{BR}(ee) : \mathrm{BR}(e\mu) : \mathrm{BR}(\mu\mu) =$$
$$4r\sin^4\theta_{12} : r\sin^2 2\theta_{12} : 1 \ (\mathrm{NH});$$
$$4 : \tfrac{r^2}{4}\sin^2 2\theta_{12} : 1 \ (\mathrm{IH1});$$
$$4 : 4\tan^2 2\theta_{12} : 1 \ (\mathrm{IH2})$$

$$r \equiv \frac{\Delta m^2_{\mathrm{sol}}}{\Delta m^2_{\mathrm{atm}}} \sim 0.03$$





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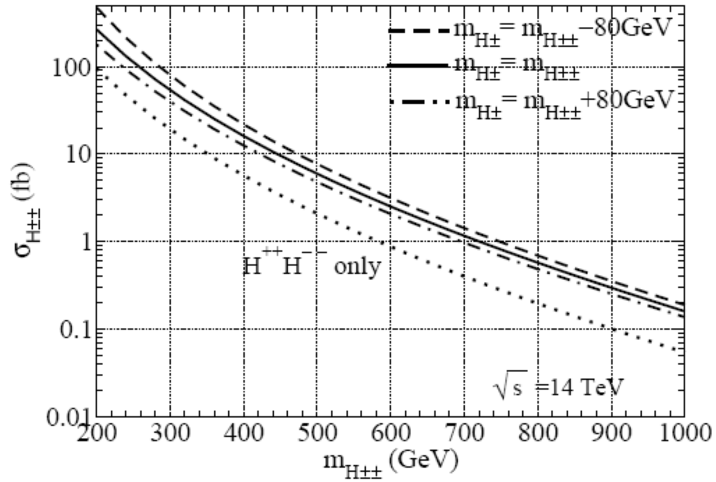
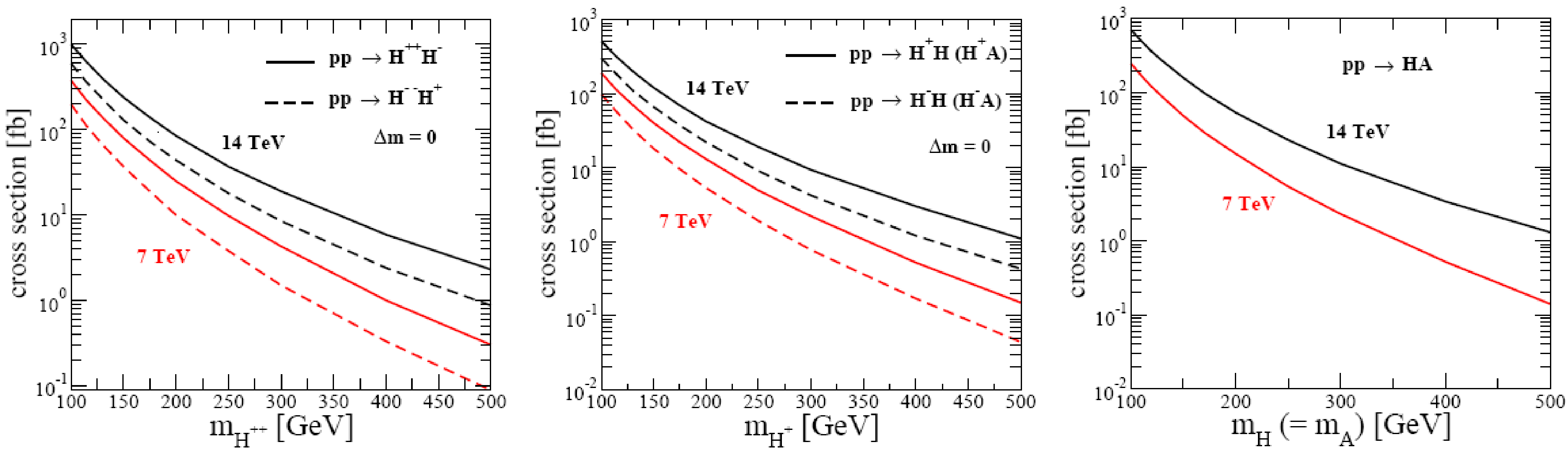
Production at LHC



Akeroyd, Aoki, 0506176
Aoki, Kanemura, Yagyu, 1110.4625

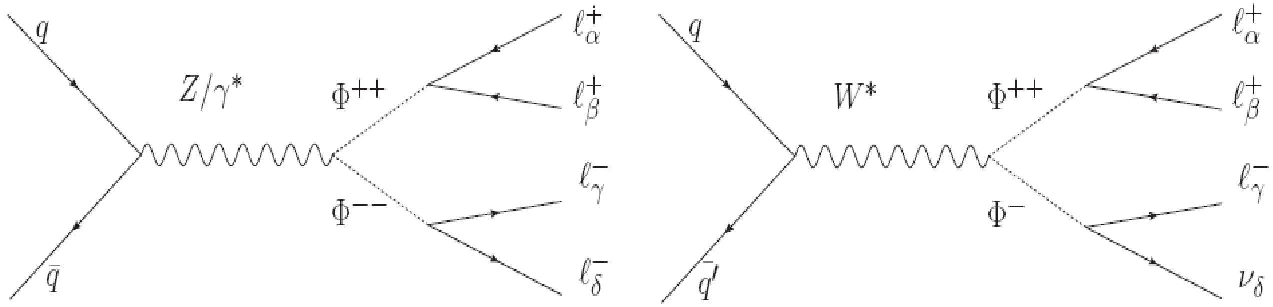


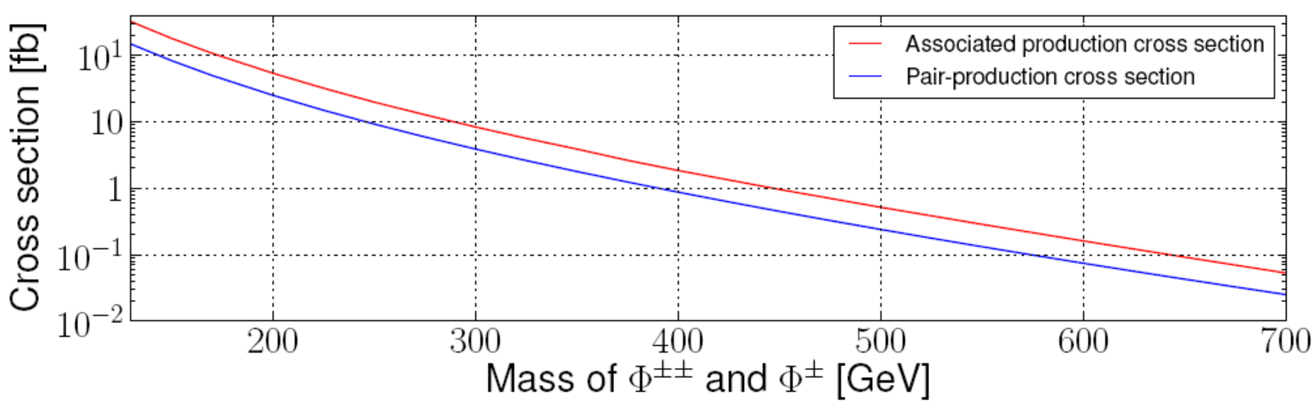
CMS search

CMS, 1207.2666

- CMS looks for $pp \to H^{++} H^{-} \to l^{+} l^{+} l^{-} \nu$

  & $pp \to H^{++} H^{--} \to l^{+} l^{+} l^{-} l^{-}$.
- Assumption of 100% leptonic decay & $\Delta M=0$.





LHC7 limit

- $H^{++} H^{-} \to l^{+} l^{+} l^{-} \nu$ & $H^{++} H^{--} \to l^{+} l^{+} l^{-} l^{-}$

Benchmark point	Combined 95% CL limit [GeV]	95% CL limit for pair production only [GeV]
$\mathcal{B}(\Phi^{++} \to e^+e^+) = 100\%$	444	382
$\mathcal{B}(\Phi^{++} \to e^+\mu^+) = 100\%$	453	391
$\mathcal{B}(\Phi^{++} \to e^+\tau^+) = 100\%$	373	293
$\mathcal{B}(\Phi^{++} \to \mu^+\mu^+) = 100\%$	459	395
$\mathcal{B}(\Phi^{++} \to \mu^+\tau^+) = 100\%$	375	300
$\mathcal{B}(\Phi^{++} \to \tau^+\tau^+) = 100\%$	204	169
BP1	383	333
BP2	408	359
BP3	403	355
BP4	400	353

Benchmark point	ee	$e\mu$	$e\tau$	$\mu\mu$	$\mu\tau$	$\tau\tau$
BP1	0	0.01	0.01	0.30	0.38	0.30
BP2	1/2	0	0	1/8	1/4	1/8
BP3	1/3	0	0	1/3	0	1/3
BP4	1/6	1/6	1/6	1/6	1/6	1/6

Search for other channels?

- CMS searches only for 3l+missing or 2 SSD :

  $H^{++} \rightarrow l^+l^+$ ($H^+ \rightarrow l^+\nu$) assuming f >> ξ.

- If ξ >> f, other channels open :

  $H^{++} \rightarrow W^+W^+$; $H^+ \rightarrow W^+Z$, tb ; $H^0/A^0 \rightarrow$ ZZ, hh/Zh, tt

- Missing triplet if λ_5<0 and f >> ξ :

  $H^{++} \rightarrow H^+W^* \rightarrow H^0/A^0 W^* W^* \rightarrow \nu\nu W^* W^*$.

- No mass limit yet in these two cases.

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Triplet–antitriplet mixing

- Triplet (lepton) number is conserved in the production:

$$pp \longrightarrow \Delta\bar{\Delta}$$

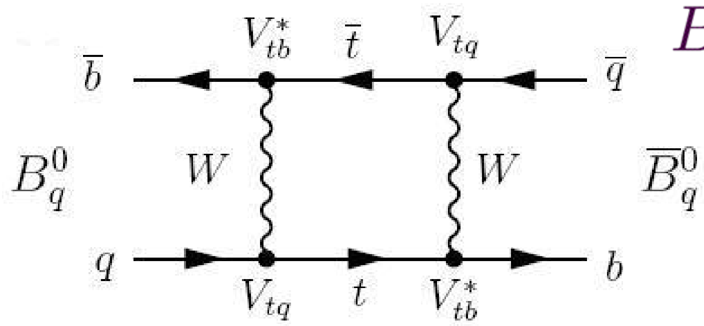
- Triplet number breaking by doublet-triplet mixing:

$$\mathcal{L}_{\not{\Delta}} = \frac{1}{\sqrt{2}}\mu\Phi^T i\tau_2\Delta^\dagger\Phi + h.c.$$

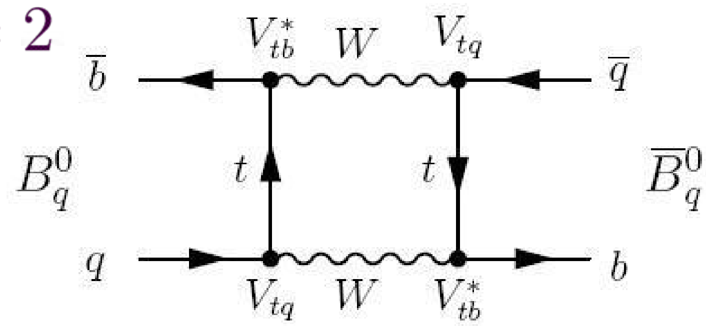
- It induces a tiny mass splitting:

$$\mathcal{L}_{\not{\Delta}} = -\mu v_\Phi h^0 H^0 \Rightarrow \boxed{\delta M_{HA} \approx 2M_{H^0}\frac{v_\Delta^2}{v_0^2}\frac{M_{H^0}^2}{M_{H^0}^2 - m_{h^0}^2}}$$

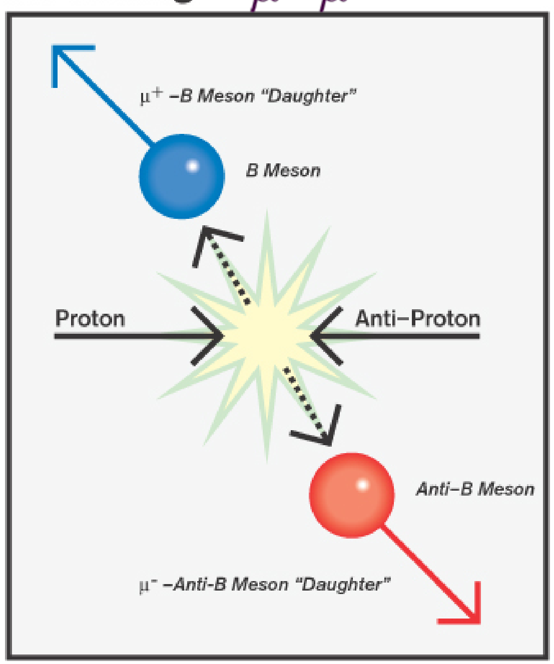
B-$\overline{\text{B}}$ Mixing



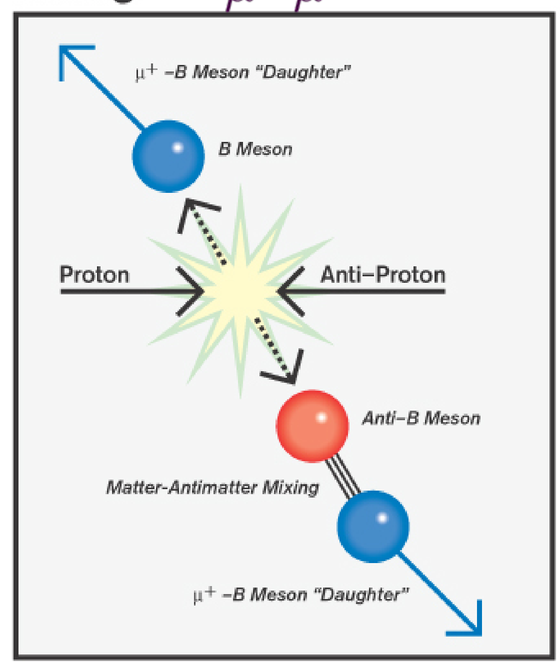
$B = 2$



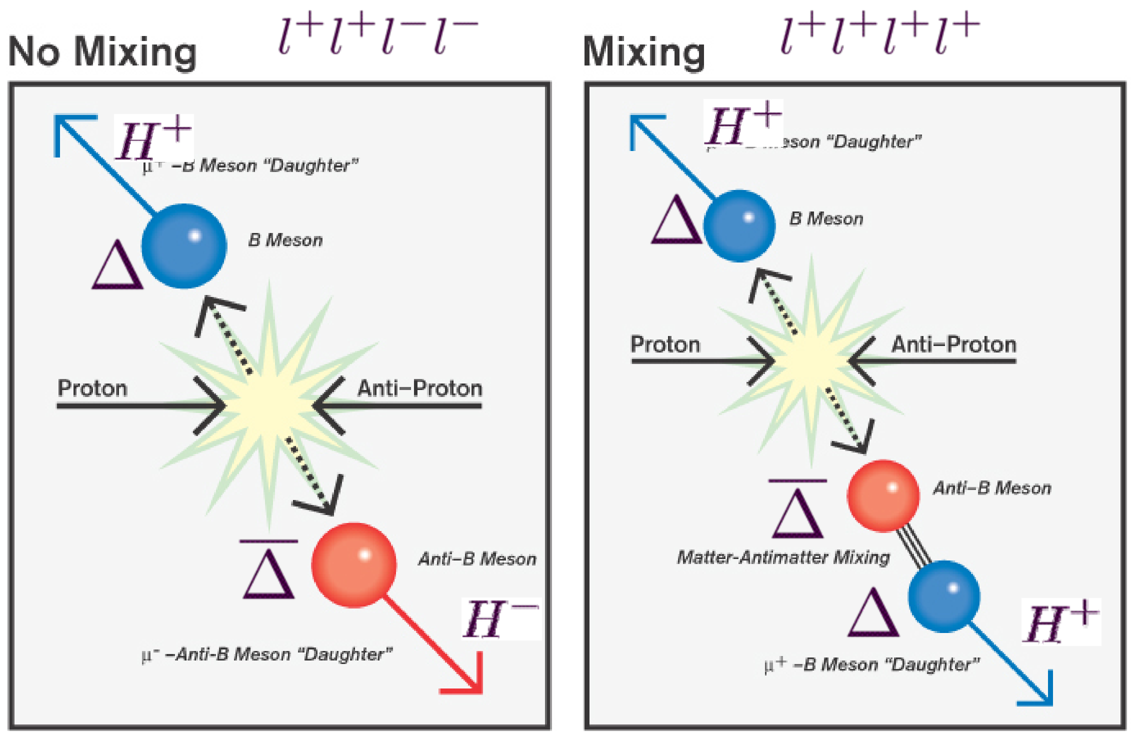
No Mixing $\mu^+\mu^-$



Mixing $\mu^+\mu^+$



Δ-$\bar{\Delta}$ Mixing



Δ-$\overline{\Delta}$ Oscillation

- Initial Δ = H^0 + i A^0 evolves as

$$|\Delta(t)\rangle = g_+(t)|\Delta\rangle + g_-(t)|\overline{\Delta}\rangle$$

$$[\Gamma = \Gamma_{H^0} = \Gamma_{A^0}]$$

$$g_\pm(t) = \frac{1}{2}e^{-\Gamma t/2}\left(e^{iM_{H^0}t} \pm e^{iM_{A^0}t}\right)$$

- Probabilities of Δ going to Δ or $\overline{\Delta}$ are

$$\chi_\pm \equiv \frac{\int_0^\infty dt|g_\pm(t)|^2}{\int_0^\infty dt|g_+(t)|^2 + \int_0^\infty dt|g_-(t)|^2}$$

$$\chi_\pm = \begin{cases} \frac{2+x^2}{2(1+x^2)} \\ \frac{x^2}{2(1+x^2)} \end{cases}$$

$$x \equiv \frac{\delta M}{\Gamma} = \frac{\tau_{dec}}{\tau_{osc}}$$

Same-Sign Tetra-Leptons

- Lepton number violating processes:

$$pp \to \Delta^0 \bar{\Delta}^0 \Rightarrow \Delta^0 \Delta^0 \ \to H^+ H^+ 2W^- \ \to H^{++} H^{++} 4W^-$$
$$\Delta^+ \bar{\Delta}^0 \Rightarrow \Delta^+ \Delta^0 \to H^{++} H^+ 2W^- \to H^{++} H^{++} 3W^-$$

- Production cross-section:

$$\begin{aligned}
\sigma\left(4\ell^\pm + 3W^{\mp^*}\right) &= \sigma\left(pp \to H^\pm H^0 + H^\pm A^0\right) \left[\frac{x_{HA}^2}{1+x_{HA}^2}\right] \mathrm{BF}(H^0/A^0 \to H^\pm W^{\mp^*}) \\
&\times \left[\mathrm{BF}(H^\pm \to H^{\pm\pm} W^{\mp^*})\right]^2 \left[\mathrm{BF}(H^{\pm\pm} \to \ell^\pm \ell^\pm)\right]^2 ; \\
\sigma\left(4\ell^\pm + 4W^{\mp^*}\right) &= \sigma\left(pp \to H^0 A^0\right) \left[\frac{2+x_{HA}^2}{1+x_{HA}^2} \frac{x_{HA}^2}{1+x_{HA}^2}\right] \mathrm{BF}(H^0 \to H^\pm W^{\mp^*}) \mathrm{BF}(A^0 \to H^\pm W^{\mp^*}) \\
&\times \left[\mathrm{BF}(H^\pm \to H^{\pm\pm} W^{\mp^*})\right]^2 \left[\mathrm{BF}(H^{\pm\pm} \to \ell^\pm \ell^\pm)\right]^2 .
\end{aligned}$$

Same-Sign Tetra-Leptons

- Is this observable?

  i) H^{++} is the lightest and $f_{\alpha\beta} > \xi$.

  ii) ΔM sufficiently large to allow $\Delta^0 \to H^+ W^- \to H^{++} 2W^-$.

  iii) Sizable oscillation parameter: x~1.

$$\delta M_{HA} \sim 2\frac{v_\Delta^2}{v_\Phi^2} M_{H^0} \qquad \Gamma_{H^0/A^0} \sim \frac{G_F^2 \Delta M^5}{\pi^3}$$

$$v_\Delta \sim 10^{-4}\mathrm{GeV}, \quad \Delta M \sim 2\mathrm{GeV} \;\; \Rightarrow \delta M_{HA} \sim \Gamma_{H^0/A^0} \sim 10^{-11}\mathrm{GeV}$$

Lepton Yukawas of the Higgs triplet

- The observed neutrino mass matrix (assuming vanishing CP phases) determines the coupling $f = M^\nu / v_\Delta$ for given v_Δ :

$$M^\nu = \begin{pmatrix} 0.00403 & 0.00816 & 0.00259 \\ 0.00816 & 0.0264 & 0.0215 \\ 0.00259 & 0.0215 & 0.0286 \end{pmatrix} \text{ for NH}$$

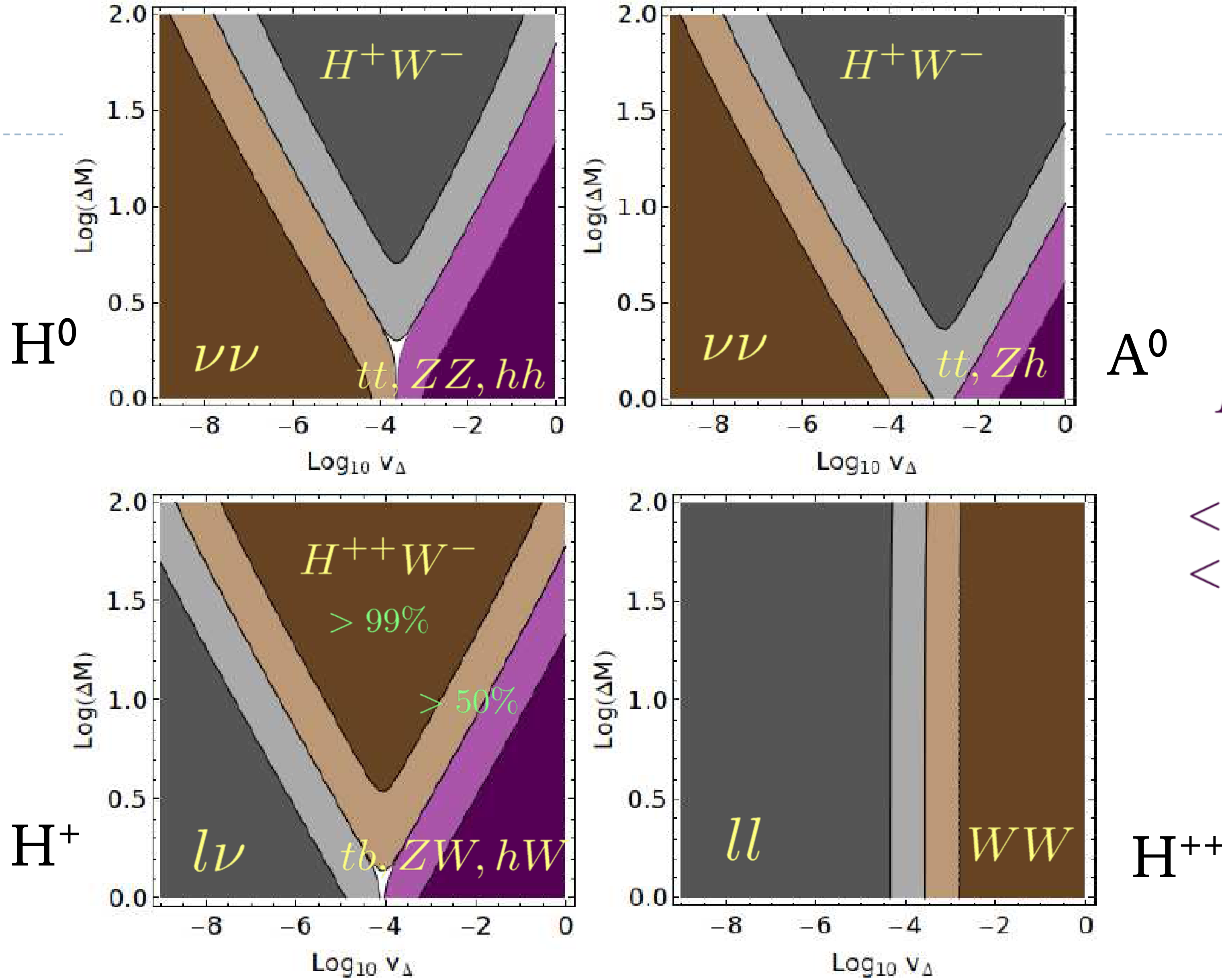
$$M^\nu = \begin{pmatrix} 0.0479 & -0.00557 & -0.00573 \\ -0.00557 & 0.0239 & -0.0240 \\ -0.00573 & -0.0240 & 0.02693 \end{pmatrix} \text{ for IH}$$

- Di-lepton channel dominates for $v_\Delta < 10^{-4}$ GeV:

$$f\xi \sim 10^{-12} \Rightarrow f \sim \xi \sim 10^{-6}$$

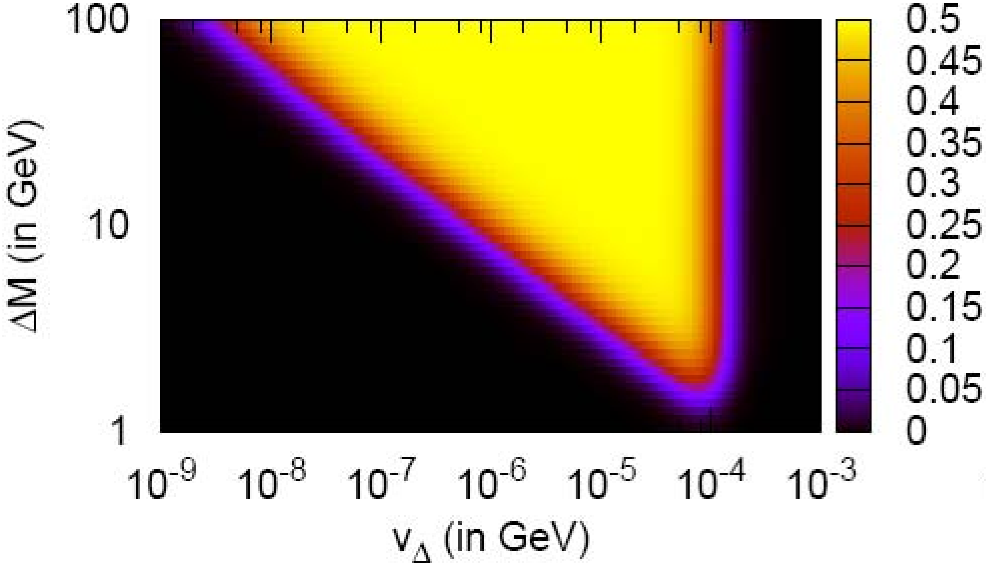
Triplet decay channels

H^0	A^0	H^+	H^{++}
$\to t\bar{t}$	$\to t\bar{t}$	$\to t\bar{b}$	$\to \ell^+\ell^+$
$\to b\bar{b}$	$\to b\bar{b}$	$\to \ell^+\nu$	$\to W^{+^*}W^{+^*}$
$\to \nu\bar{\nu}$	$\to \nu\bar{\nu}$	$\to W^+Z$	
$\to ZZ$	$\to Zh^0$	$\to W^+h^0$	
$\to h^0h^0$	$\to H^{\pm}W^{\mp^*}$	$\to H^{++}W^{-^*}$	
$\to H^{\pm}W^{\mp^*}$			

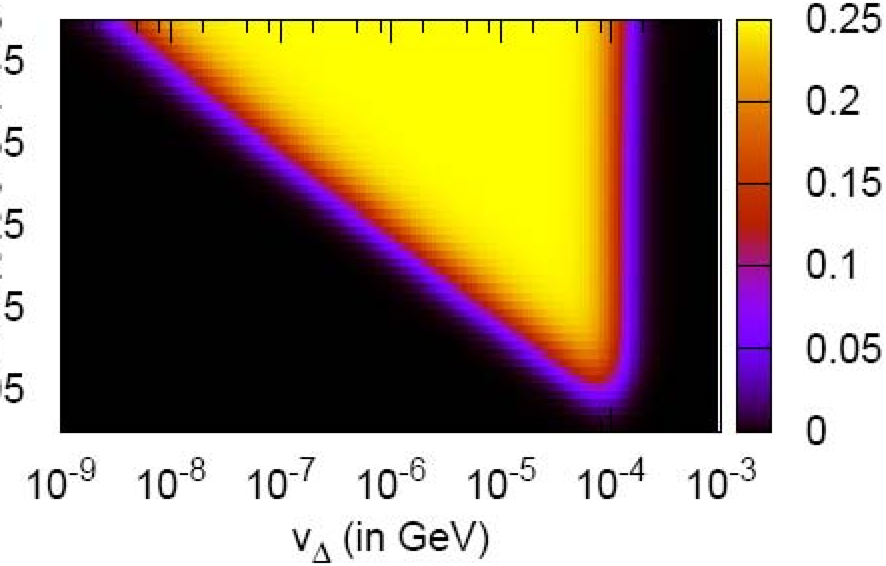


$M_{H^{++}} = 300\text{GeV} < M_{H^+} < M_{H^0/A^0}$

Maximizing the branching fraction



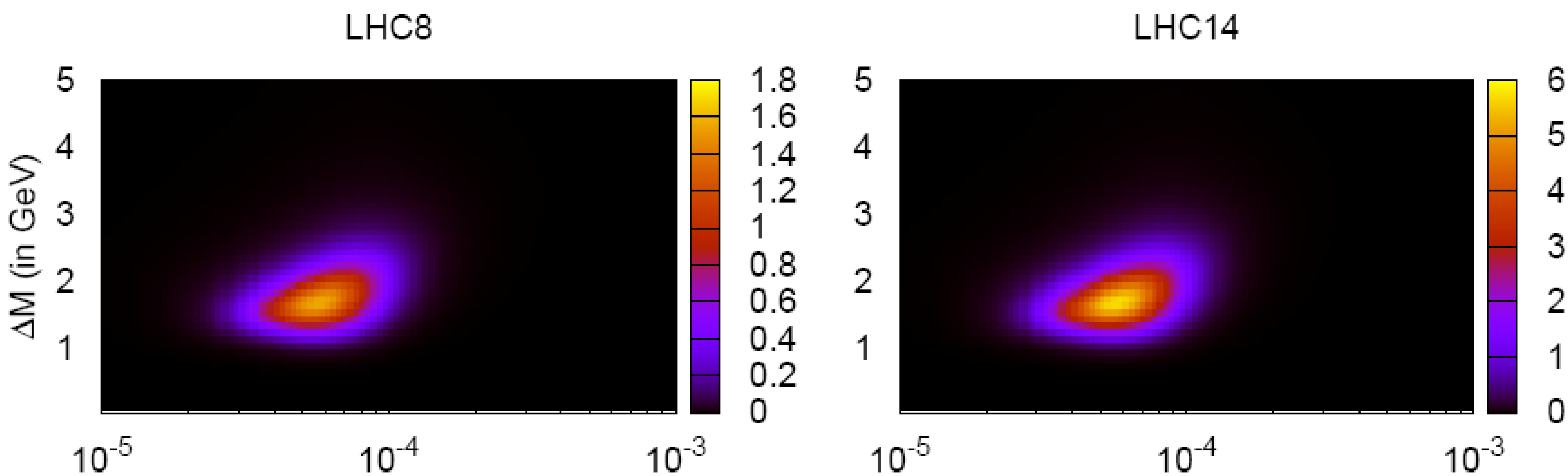
for $4l + 3W^*$



for $4l + 4W^*$

SS4L cross-section

- SS4L production including the oscillation factor:



$$M_{H^{\pm\pm}} = 400\text{GeV}$$

- Benchmark point:

  $v_\Delta = 7\text{x}10^{-5}$ GeV, ΔM=1.5 GeV.

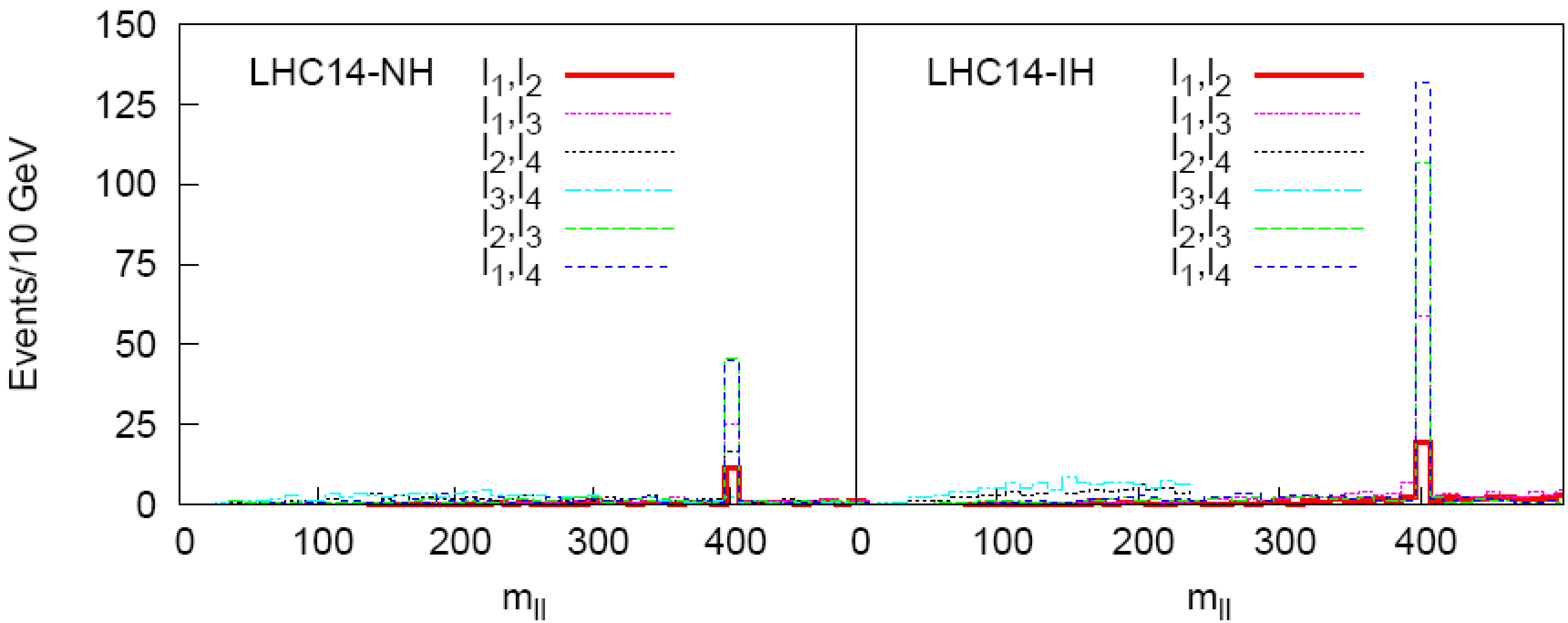
Event numbers

Final State	σ/fb (8 TeV)	σ/fb (14 TeV)
H^+H^0	0.761	2.931
H^+A^0	0.761	2.931
H^-H^0	0.275	1.209
H^-A^0	0.275	1.209
H^0A^0	1.014	4.322

No background
Lepton selection cuts only

Luminosity	Final state	Pre-selection	Selection
$15 fb^{-1}$	$\ell^\pm\ell^\pm\ell^\pm\ell^\pm$ (LHC8-NH)	4	3
	$\ell^\pm\ell^\pm\ell^\pm\ell^\pm$ (LHC8-IH)	9	8
$100 fb^{-1}$	$\ell^\pm\ell^\pm\ell^\pm\ell^\pm$ (LHC14-NH)	110	94
	$\ell^\pm\ell^\pm\ell^\pm\ell^\pm$ (LHC14-IH)	240	210

Mass reconstruction



Conclusion I

- Type II seesaw may show a novel signature of same-sign tetra-leptons due to the mixing between two neutral (triplet) Higgs bosons.
- LHC14 with 100/bf could see more than 10 such signals for the triplet Higgs boson lighter than 600-700 GeV.
- The tiny VEV and mass gaps of the Higgs triplet may be measured through the oscillation phenomena.

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EWPD

- Triplet contribution to S, T & U: Lavoura, Li, 9309262
- Most recent STU fit:

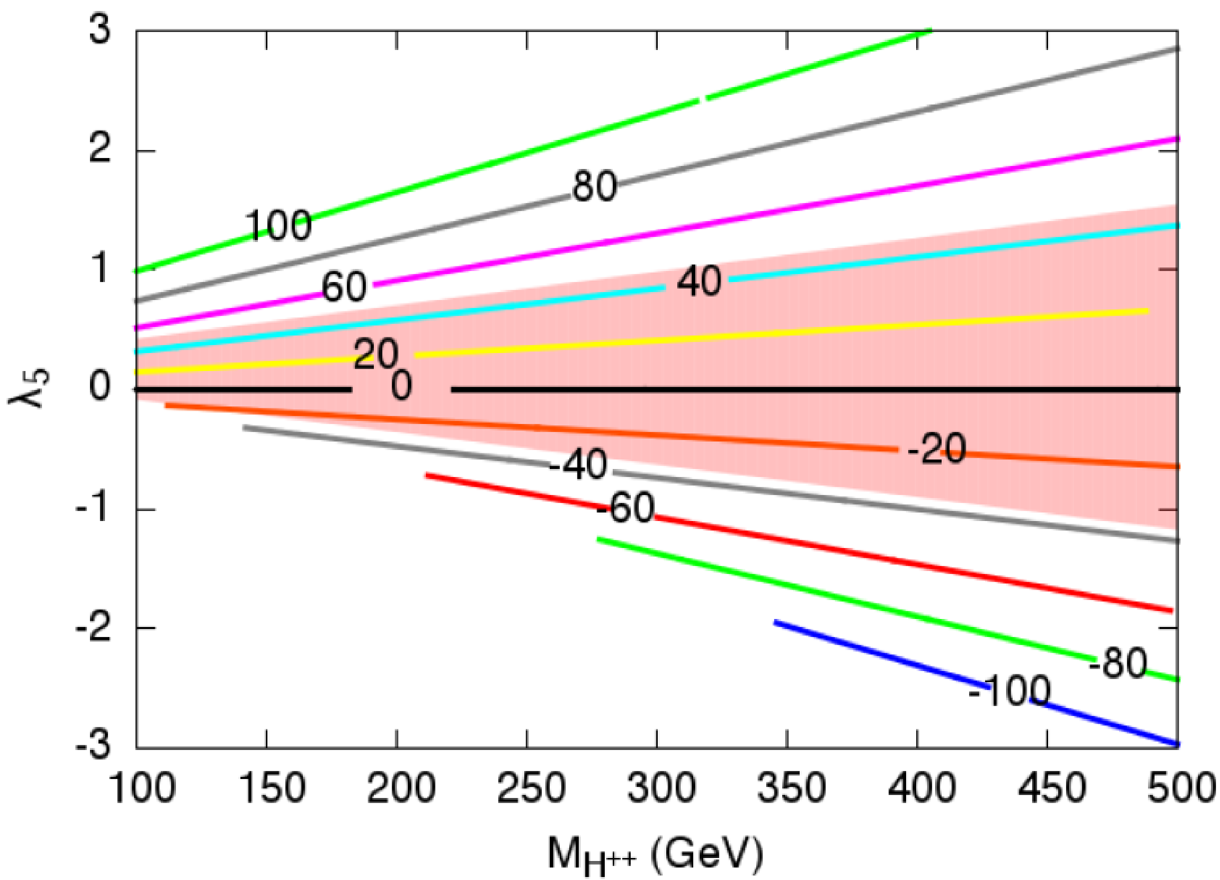
$$S_{\text{best fit}} = 0.03\,, \quad \sigma_S = 0.10$$
$$T_{\text{best fit}} = 0.05\,, \quad \sigma_T = 0.12$$
$$U_{\text{best fit}} = 0.03\,, \quad \sigma_U = 0.10$$
$$\rho_{ST} = 0.89, \quad \rho_{SU} = -0.54, \quad \rho_{TU} = -0.83$$

Baak, et.al., 1209.2716

- It strongly constrains the mass splitting.

$$\begin{pmatrix} \Delta S \\ \Delta T \\ \Delta U \end{pmatrix}^T \begin{pmatrix} \sigma_S\sigma_S & \sigma_S\sigma_T\rho_{ST} & \sigma_S\sigma_U\rho_{SU} \\ \sigma_S\sigma_T\rho_{ST} & \sigma_T\sigma_T & \sigma_T\sigma_U\rho_{TU} \\ \sigma_U\sigma_S\rho_{US} & \sigma_U\sigma_T\rho_{TU} & \sigma_U\sigma_U \end{pmatrix}^{-1} \begin{pmatrix} \Delta S \\ \Delta T \\ \Delta U \end{pmatrix} < -2\ln(1-CL)$$

EWPD



3
2
1
0
-1
-2
-3
100
150
200
250
300
350
400
450
500
λ_5
$M_{H^{++}}$ (GeV)
100
80
60
40
20
0
-20
-40
-60
-80
-100

Constrained λ_5

- EWPD limits $|\Delta M| <\sim 40$ GeV for $\xi << 10^{-2}$.
- Strong constraints on λ_5 for small triplet mass:

$$\lambda_5 = (-0.1, 0.4), \quad (-0.2, 0.6), \quad (-0.35, 0.7)$$

$$M_{H^{++}} = 100,\ 150,\ \text{and}\ 200\ \text{GeV},$$

Vacuum stability & perturbativity

- Higgs sector of type II seesaw:

$$
\begin{aligned}
V(\Phi,\Delta) = {} & m^2\Phi^\dagger\Phi + M^2\mathrm{Tr}(\Delta^\dagger\Delta) \\
& + \lambda_1(\Phi^\dagger\Phi)^2 + \lambda_2[\mathrm{Tr}(\Delta^\dagger\Delta)]^2 + 2\lambda_3\mathrm{Det}(\Delta^\dagger\Delta) \\
& + \lambda_4(\Phi^\dagger\Phi)\mathrm{Tr}(\Delta^\dagger\Delta) + \lambda_5(\Phi^\dagger\tau_i\Phi)\mathrm{Tr}(\Delta^\dagger\tau_i\Delta) \\
& + \frac{1}{\sqrt{2}}\mu\Phi^T i\tau_2\Delta\Phi + h.c.
\end{aligned}
$$

- Vacuum stability of the SM Higgs changes due to its couplings to the Higgs triplet.
- Triplet self coupling (λ_2) tends to diverge rapidly.
- Strong constraints on $\lambda_{2,3,4,5}$.
- Take λ_1=0.13 and μ << v_Φ.

Vacuum stability & perturbativity

- Demand the absolute vacuum stability condition.

Arhrib, et.al., 1105.1925

  - $\lambda_1 > 0,$
  - $\lambda_2 > 0,$
  - $\lambda_2 + \frac{1}{2}\lambda_3 > 0$
  - $\lambda_4 \pm \lambda_5 + 2\sqrt{\lambda_1\lambda_2} > 0,$
  - $\lambda_4 \pm \lambda_5 + 2\sqrt{\lambda_1(\lambda_2 + \frac{1}{2}\lambda_3)} > 0.$

- Perturbativity: $|\lambda_i| \leq \sqrt{4\pi}.$

Vacuum stability & perturbativity

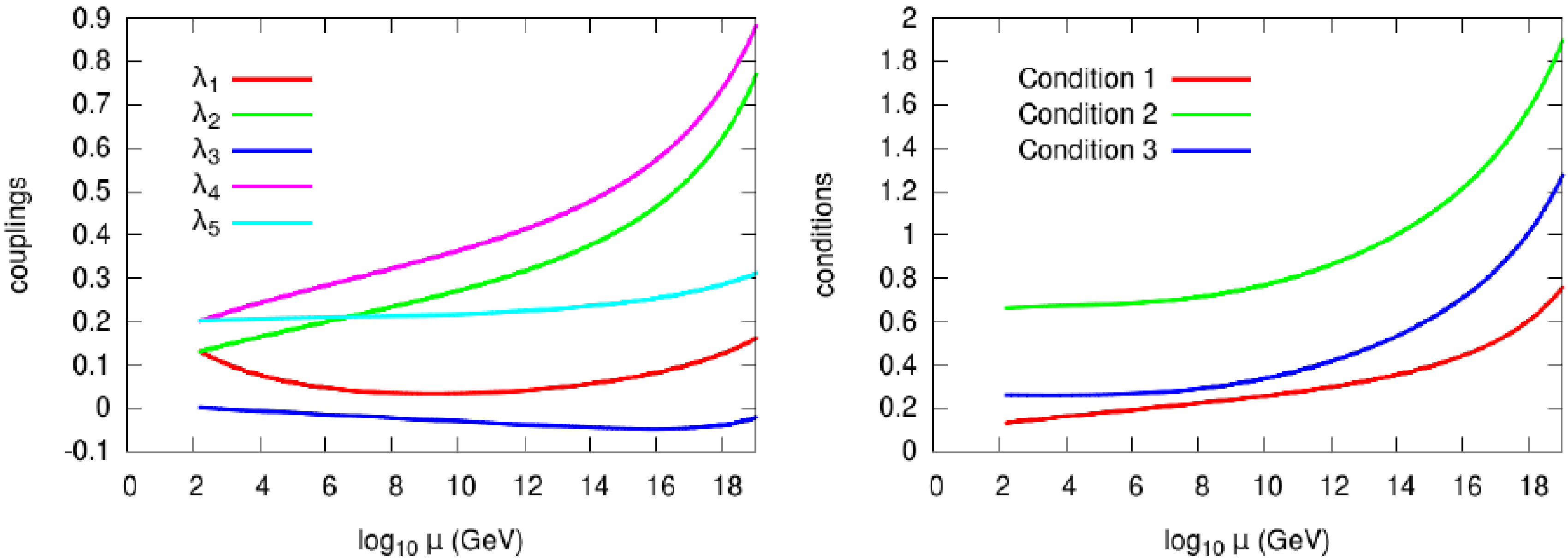
- Use 1-loop RGE:

Chao, Zhang, 0611323
Schmidt, 07053841

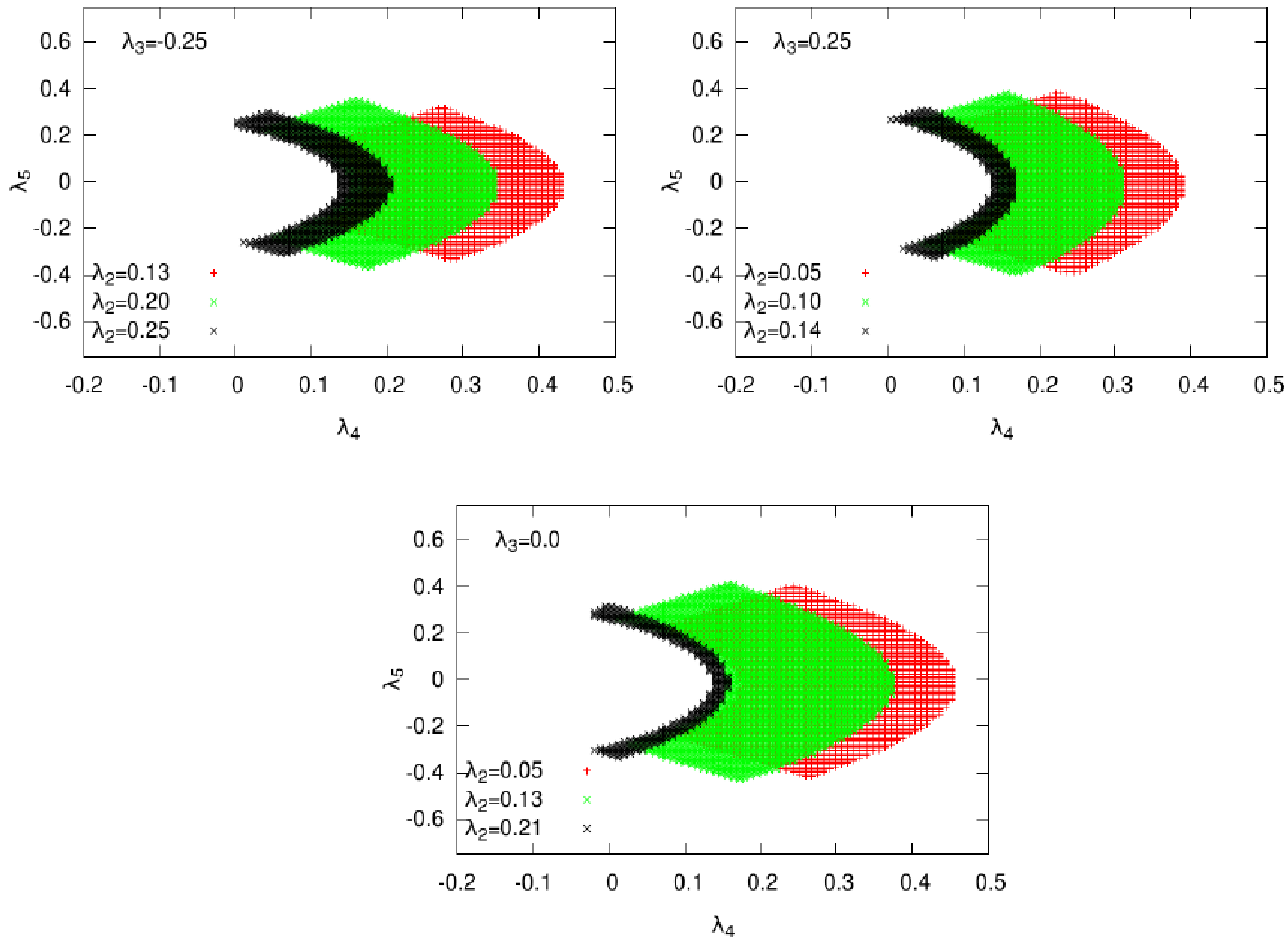
$$
\begin{aligned}
16\pi^2 \frac{d\lambda_1}{dt} &= 24\lambda_1^2 + \lambda_1(-9g_2^2 - 3g'^2 + 12y_t^2) + \frac{3}{4}g_2^4 + \frac{3}{8}(g'^2 + g_2^2)^2 \\
&- 6y_t^4 + 3\lambda_4^2 + 2\lambda_5^2 \\
16\pi^2 \frac{d\lambda_2}{dt} &= \lambda_2(-12g'^2 - 24g_2^2) + 6g'^4 + 9g_2^4 + 12g'^2 g_2^2 + 28\lambda_2^2 \\
&+ 8\lambda_2\lambda_3 + 4\lambda_3^2 + 2\lambda_4^2 + 2\lambda_5^2 \\
16\pi^2 \frac{d\lambda_3}{dt} &= \lambda_3(-12g'^2 - 24g_2^2) + 6g_2^4 - 24g'^2 g_2^2 + 6\lambda_3^2 \\
&+ 24\lambda_2\lambda_3 - 4\lambda_5^2 \\
16\pi^2 \frac{d\lambda_4}{dt} &= \lambda_4(-\frac{15}{2}g'^2 - \frac{33}{2}g_2^2) + \frac{9}{5}g'^4 + 6g_2^4 + \lambda_4(12\lambda_1 \\
&+ 16\lambda_2 + 4\lambda_3 + 4\lambda_4 + 6y_t^2) + 8\lambda_5^2 \\
16\pi^2 \frac{d\lambda_5}{dt} &= \lambda_4(-\frac{15}{2}g'^2 - \frac{33}{2}g_2^2) + 6g'^2 g_2^2 + \lambda_5(4\lambda_1 + 4\lambda_2 \\
&- 4\lambda_3 + 8\lambda_4 + 6y_t^2),
\end{aligned}
$$

RGE running

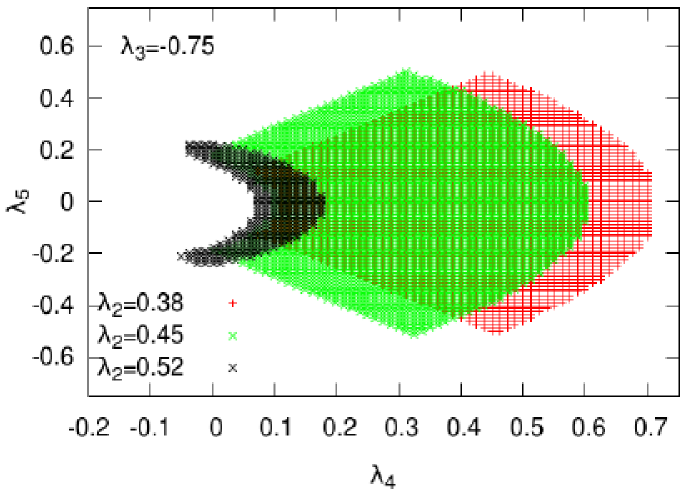
- An example

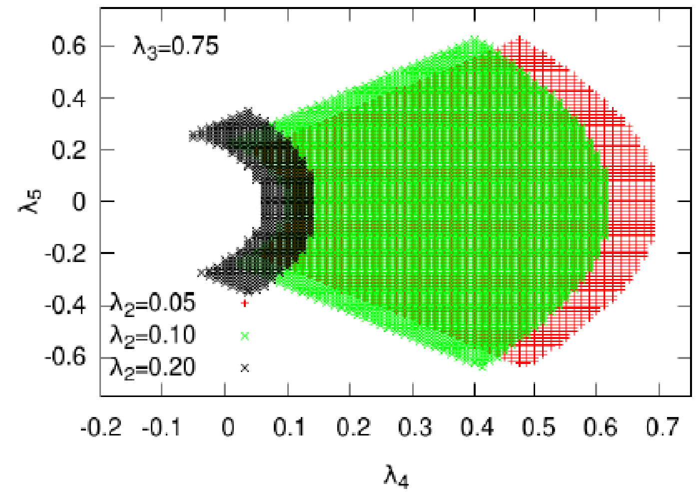


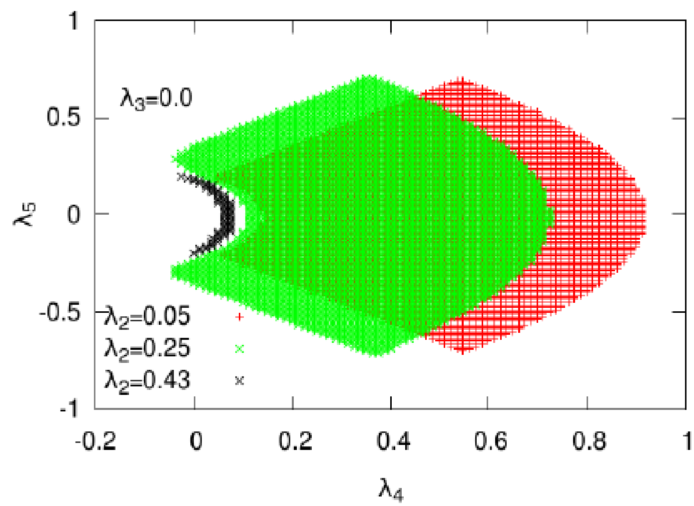
Cut-off scale 10^{19} GeV



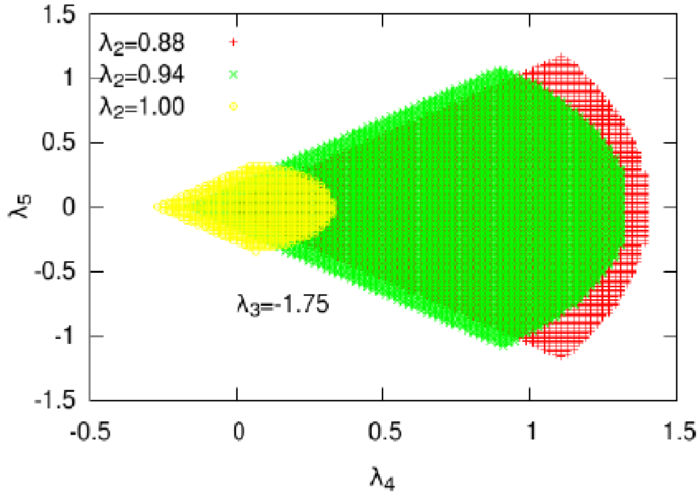
Cut-off scale 10^{10} GeV

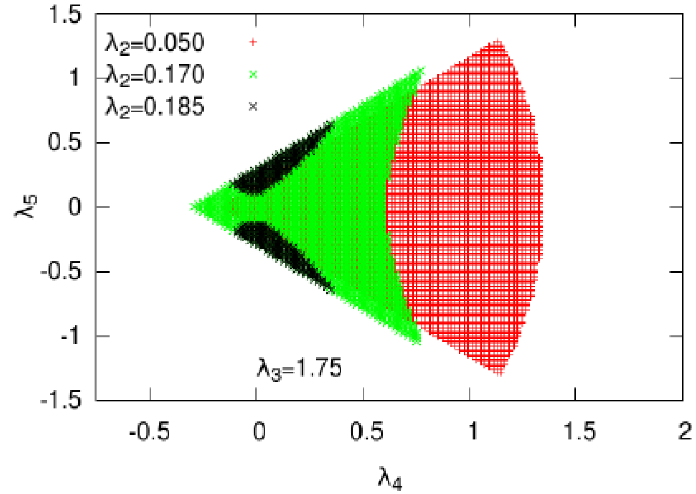


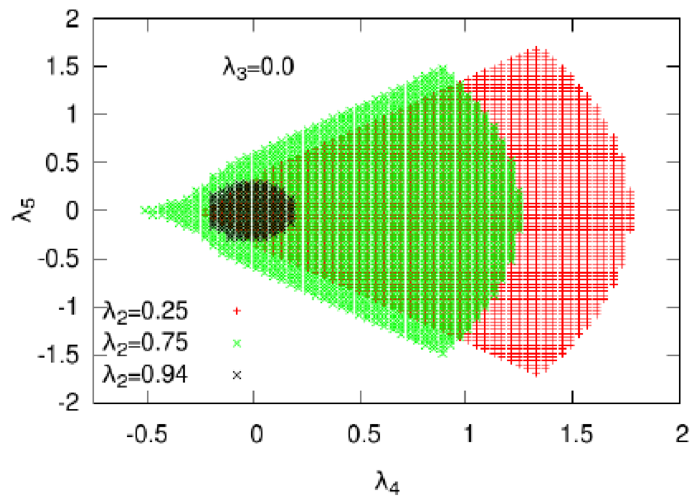




Cut-off scale 10^5 GeV





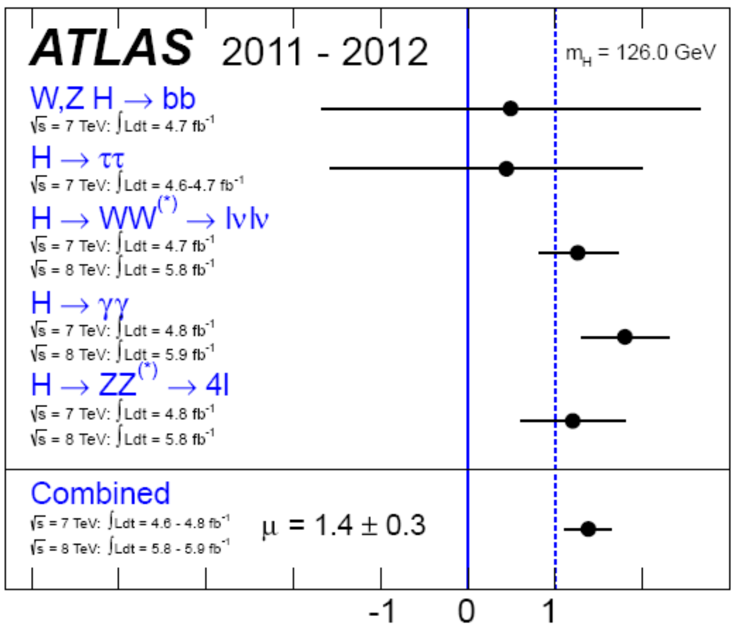


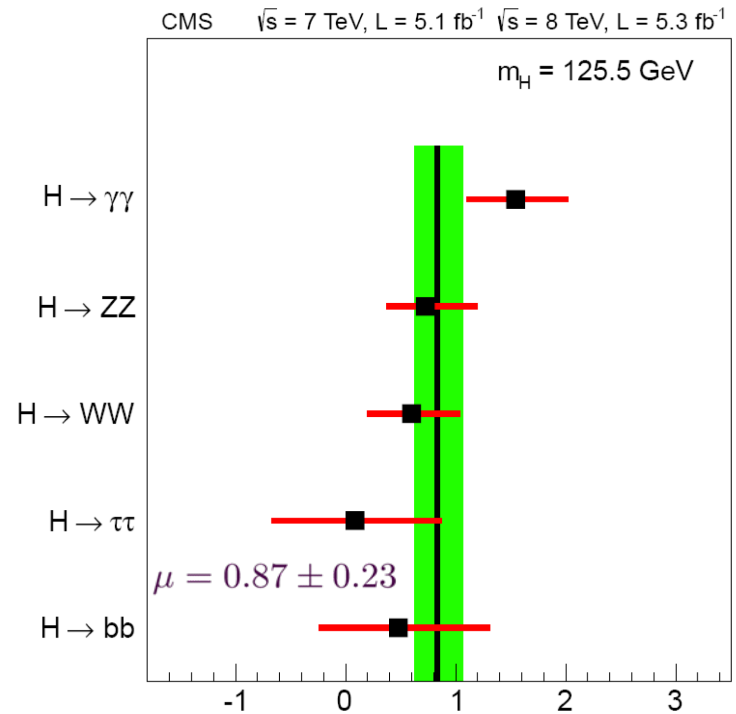
Allowed ranges

	10^5 GeV	10^{10} GeV	10^{19} GeV
λ_2	$(0, 1)$	$(0, 0.5)$	$(0, 0.25)$
λ_3	$(-2.0, 2.4)$	$(-1.0, 1.25)$	$(-0.55, 0.62)$
λ_4	$(-0.5, 1.7)$	$(-0.1, 0.9)$	$(0, 0.5)$
λ_5	$(-1.5, 1.5)$	$(-0.7, 0.7)$	$(-0.4, 0.4)$

Higgs-to-diphoton

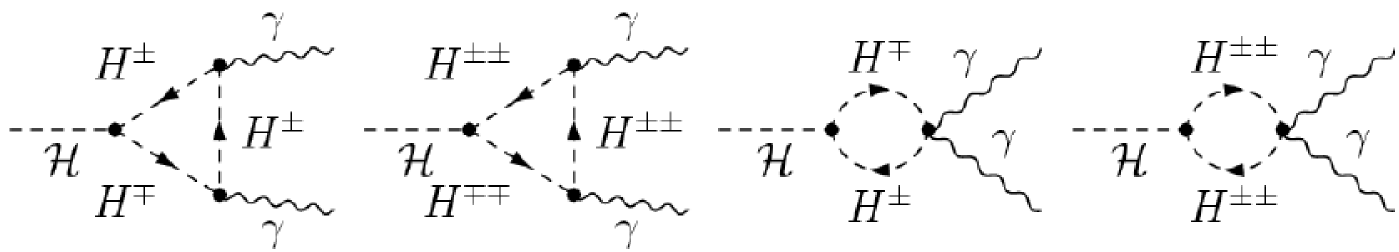
- 1-loop process – sensitive to New Physics.
- A large deviation in the current data.
- Its precision data is important to constrain NP.





Higgs-to-diphoton

- H^{++} & H^{+} contribution:



$$\Gamma(h \to \gamma\gamma) = \frac{G_F \alpha^2 m_h^3}{128\sqrt{2}\pi^3} \left| \sum_f N_c Q_f^2 \, g_{ff}^h A_{1/2}^h(x_f) + g_{WW}^h A_1^h(x_W) \right.$$

$$\left. + g_{H^+H^-}^h A_0^h(x_{H^+}) + 4 g_{H^{++}H^{--}}^h A_0^h(x_{H^{++}}) \right|^2$$

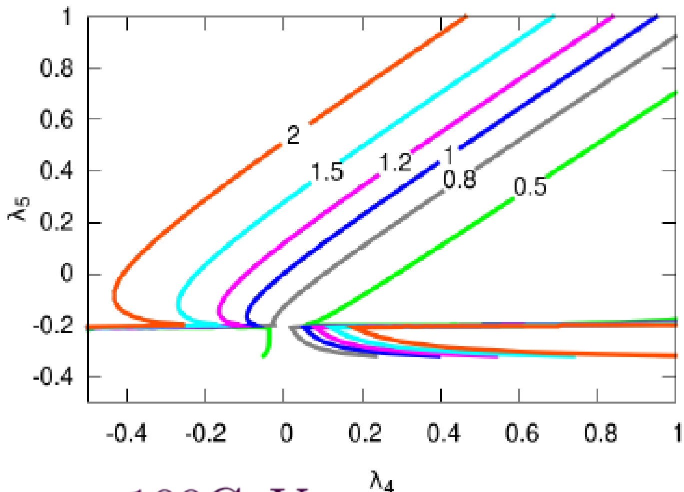
- $g_{H^+H^+}^h = \frac{\lambda_4}{2} \frac{v_0^2}{M_{H^+}^2},$
- $g_{H^{++}H^{++}}^h = \frac{\lambda_4 - \lambda_5}{2} \frac{v_0^2}{M_{H^{++}}^2},$

Arhrib, et.al., 1112.5453
Kanemura, Yagyu, 1201.6287
Akeryod, Moretti, 1206.0535

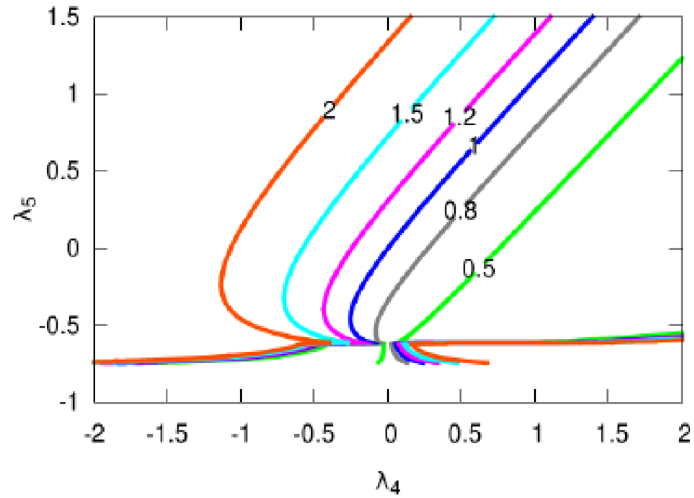
Higgs-to-diphoton

- Sizable H^{++}/H^{+} contribution if light enough (< 250 GeV).
- CMS limit does not apply if BR($H^{++} \to l^+l^+$) is not 100%.
- Calculate possible deviation by Higgs triplet combined with conditions from EWPD, vacuum stability and perturbativity.

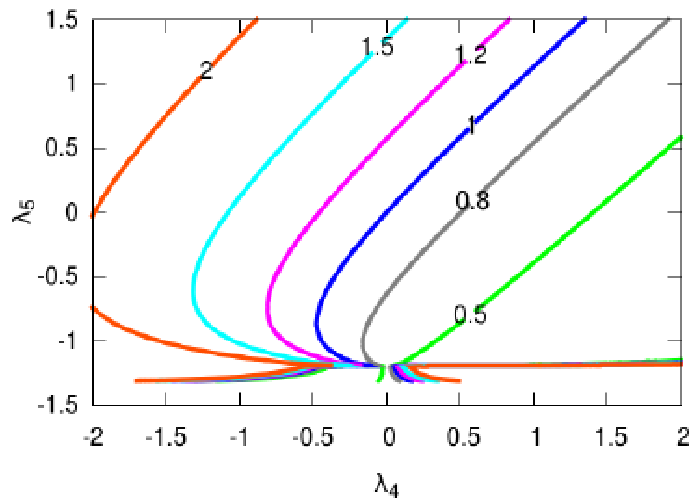
$$R_{\gamma\gamma} = \Gamma(h \to \gamma\gamma)/\Gamma(h \to \gamma\gamma)_{\text{SM}}$$



$m_{H^{++}} = 100\text{GeV}$

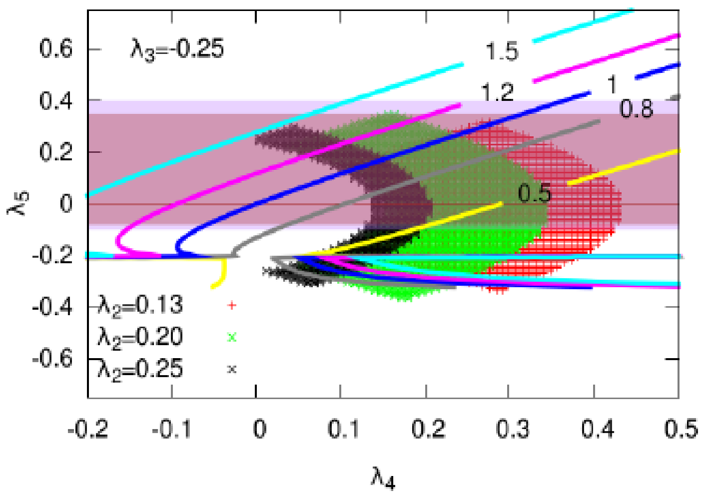


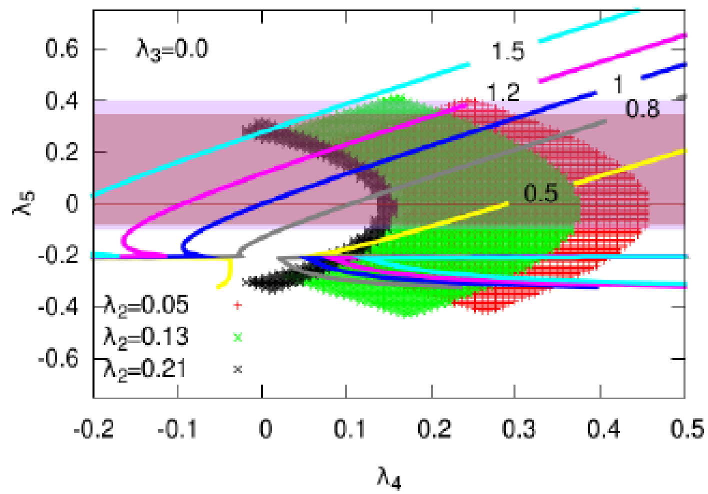
$m_{H^{++}} = 150\text{GeV}$

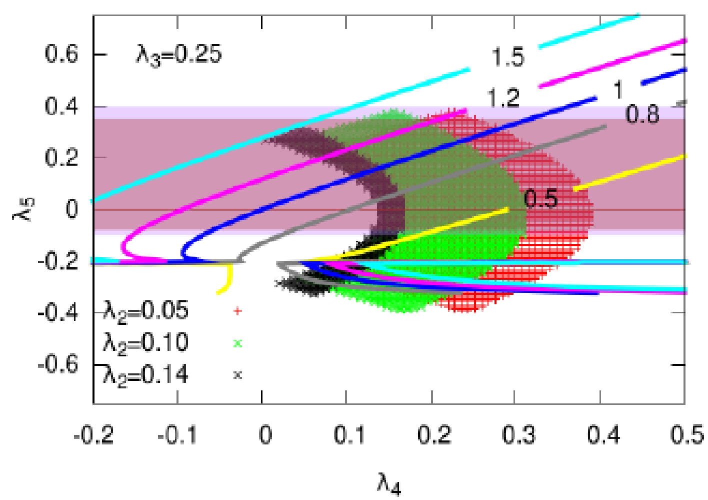


$m_{H^{++}} = 200\text{GeV}$

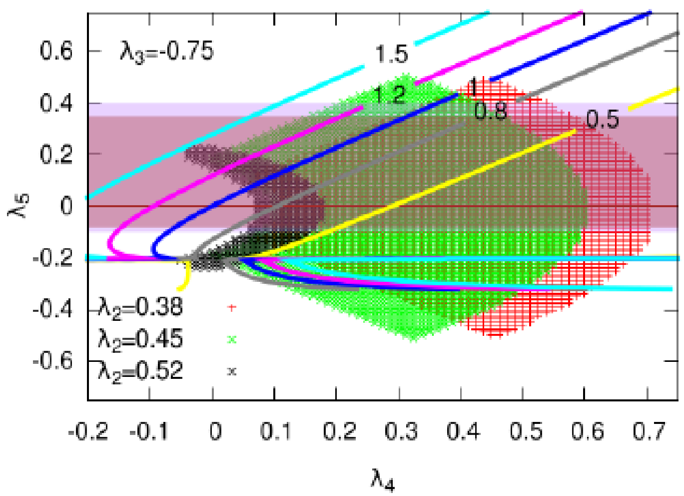
Combined results for 10^{19} GeV

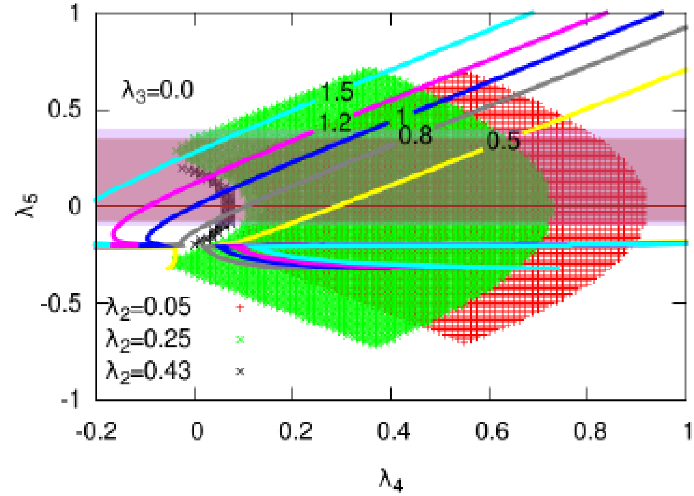


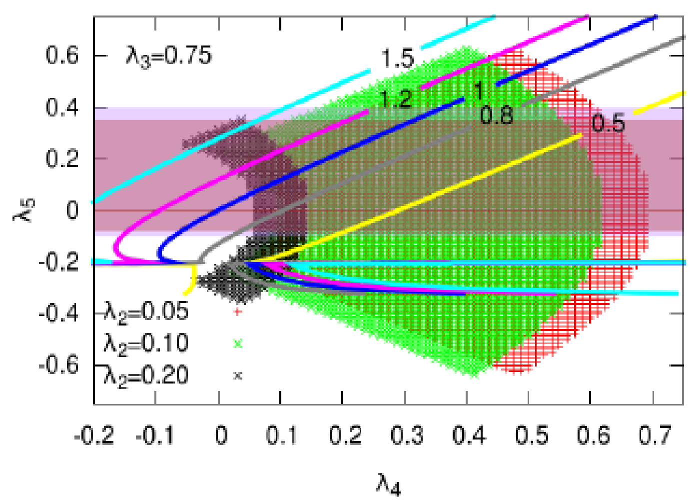




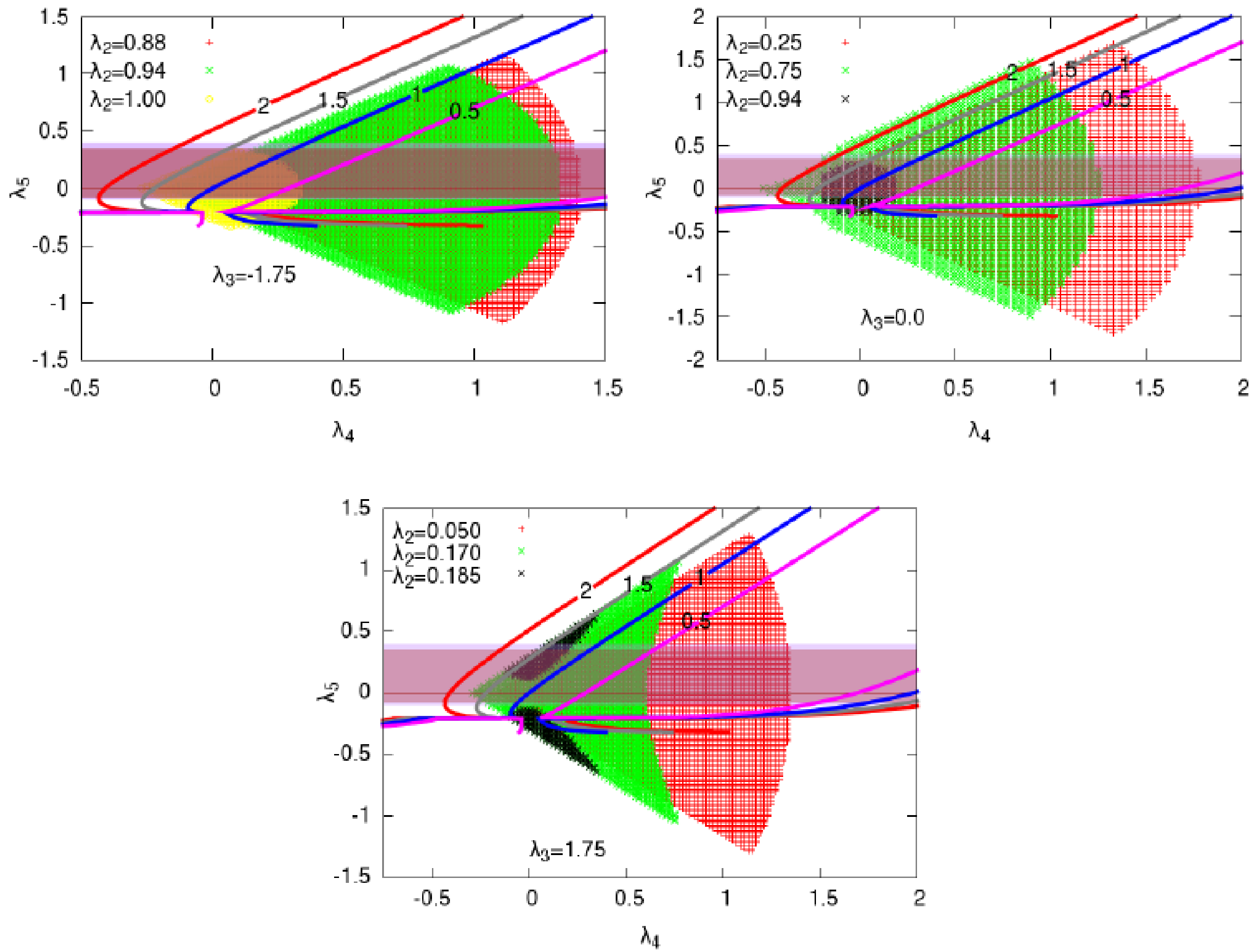
Combined results for 10^{10} GeV







Combined results for 10^5 GeV



Conclusion II

- EWPD constrains tightly the triplet mass splitting:

$$|\Delta M| < 40 \text{ GeV.}$$

- Vacuum stability and perturbativity put strong bounds on the Higgs couplings, roughly λ_i <~ 1.
- Higgs-to-diphoton rate can be enhanced up to 100% ~ 50% for the triplet mass 100 GeV depending on the cut-off scale.
- The Higgs precision data will severely constrain the Higgs triplet parameter space.

Thank you