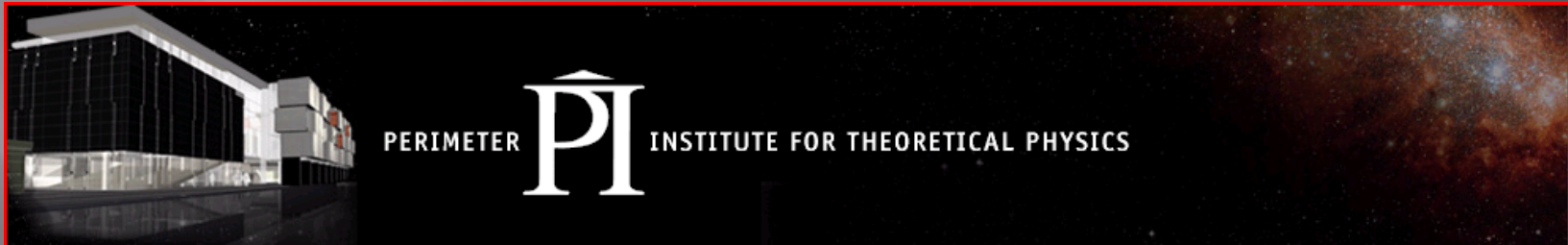


Joint Seminar on Cosmology and Gravitation, IPMU, 27 Feb. 2009

*THE END OF*  
THE COSMOLOGICAL CONSTANT PROBLEM!

Niayesh Afshordi



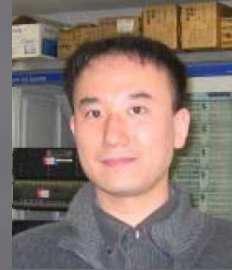
Theory + Data = IPMU

# Outline

- ▣ History of cosmological constant problem
- ▣ Cosmic acceleration and coincidence
- ▣ Degravitating the quantum vacuum and the Gravitational Aether
- ▣ Testing the Aether
- ▣ Stellar black holes and cosmic acceleration
- ▣ Conclusions and the Missing Links

# My Collaborators

- ▣ Kazunory Kohri (Lancaster)



- ▣ Georg Robbers (Heidelberg → MPA)



- ▣ Tom Giblin (Perimeter/Bates College)

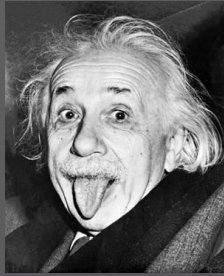


- ▣ Chanda Prescod-Weinstein (Perimeter)



# History of the C.C. problem

- ▣ In 1917, Einstein introduced  $\Lambda$ -term to make Universe static:  $G_{\mu\nu} = \Lambda g_{\mu\nu} + T_{\mu\nu}$
- ▣ In 1920's, Pauli calculates size of Einstein Universe, including the zero-point quantum fluctuations of the Electromagnetic field  $\sim 30$  km!
- ▣ Meanwhile, Hubble discovers galaxies are at  $> 10^{16}$  km! Moreover, Universe isn't static, so no need for  $\Lambda$ .



# Revival of $\Lambda$



- ▣ In 1989, Weinberg provides a “no-go” theorem in his review: No local QFT can naturally give  $\Lambda = 0$  without fine-tuning
- ▣ Standard Model:  $\Lambda \sim (100 \text{ GeV})^4$
- ▣ In 1990's, several probes (CMB, galaxy clusters, galaxy correlation function, globular cluster ages, and eventually supernovae) pointed to  $\Lambda \sim (10^{-3} \text{ eV})^4$ 
  - Old CC problem: Why CC is so small?
  - New CC problem: Why does it become important now?

# Cosmological constant problem

- Einstein Equation

**Modified Gravity**

$$G_{\mu\nu} = \langle T_{\mu\nu} \rangle$$

space-time curvature:  
 $(10^{-3} \text{ eV})^4$

vacuum energy density :  
 $\gtrsim \pm (100 \text{ GeV})^4$   
+ excitations

Only known solution: Landscape + Anthropics\*

# Can Quantum Gravity solve the CC problem?

▣ **No! because:**

Quantum Gravity models reduce to GR+ Effective Field Theory at low energies, *by construction*

→ solution must change classical gravity

# Here is an alternative: Gravitational Aether

$$(8\pi G)^{-1}G_{\mu\nu}[g_{\mu\nu}] = T_{\mu\nu} - \frac{1}{4}Tg_{\mu\nu} + \dots ,$$

- ▣ The metric is now blind to vacuum energy:

$$T_{\mu\nu} = \rho_{\text{vac}}g_{\mu\nu} + \text{excitations.}$$

- ▣ In order to satisfy the Bianchi identity:

$$(8\pi G)^{-1}G_{\mu\nu}[g_{\mu\nu}] = T_{\mu\nu} - \frac{1}{4}Tg_{\mu\nu} + T'_{\mu\nu}$$

$$T'^{\mu\nu}{}_{;\nu} = \frac{1}{4}T_{;\nu}$$

- ▣ Further assume:

$$T'_{\mu\nu} = p' [(1 + \omega^{-1})u_{\mu}u_{\nu} - g_{\mu\nu}] ,$$



# FRW cosmology with Gravitational Aether

□ Friedmann equation: 
$$H^2 + \frac{k}{a^2} = \frac{8\pi G}{3} \rho_{\text{eff}}.$$

$$\rho_{\text{eff}} = \rho - \frac{T}{4} + \frac{p'}{\omega} = \frac{3(1+w)(\omega - 1/3)\rho}{4(\omega - w)},$$

i.e., effective  $G$  depends on the Eq. of state.

□ Radiation vs. Matter era: 
$$\frac{G_N}{G_R} \equiv \frac{\rho_{\text{eff}}/\rho|_{w=0}}{\rho_{\text{eff}}/\rho|_{w=1/3}} = \frac{3}{4} - \frac{1}{4\omega} < 0.75$$

□ BBN (Cyburt, Fields, Olive, & Skillman 2005)

$$G_N/G_R = 0.97 \pm 0.09$$

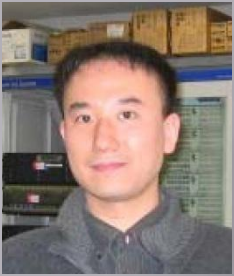
□ Ly- $\alpha$ +WMAP3 (Seljak, Slosar, McDonald 2006):

$$G_N/G_R = 0.73 \pm 0.04$$

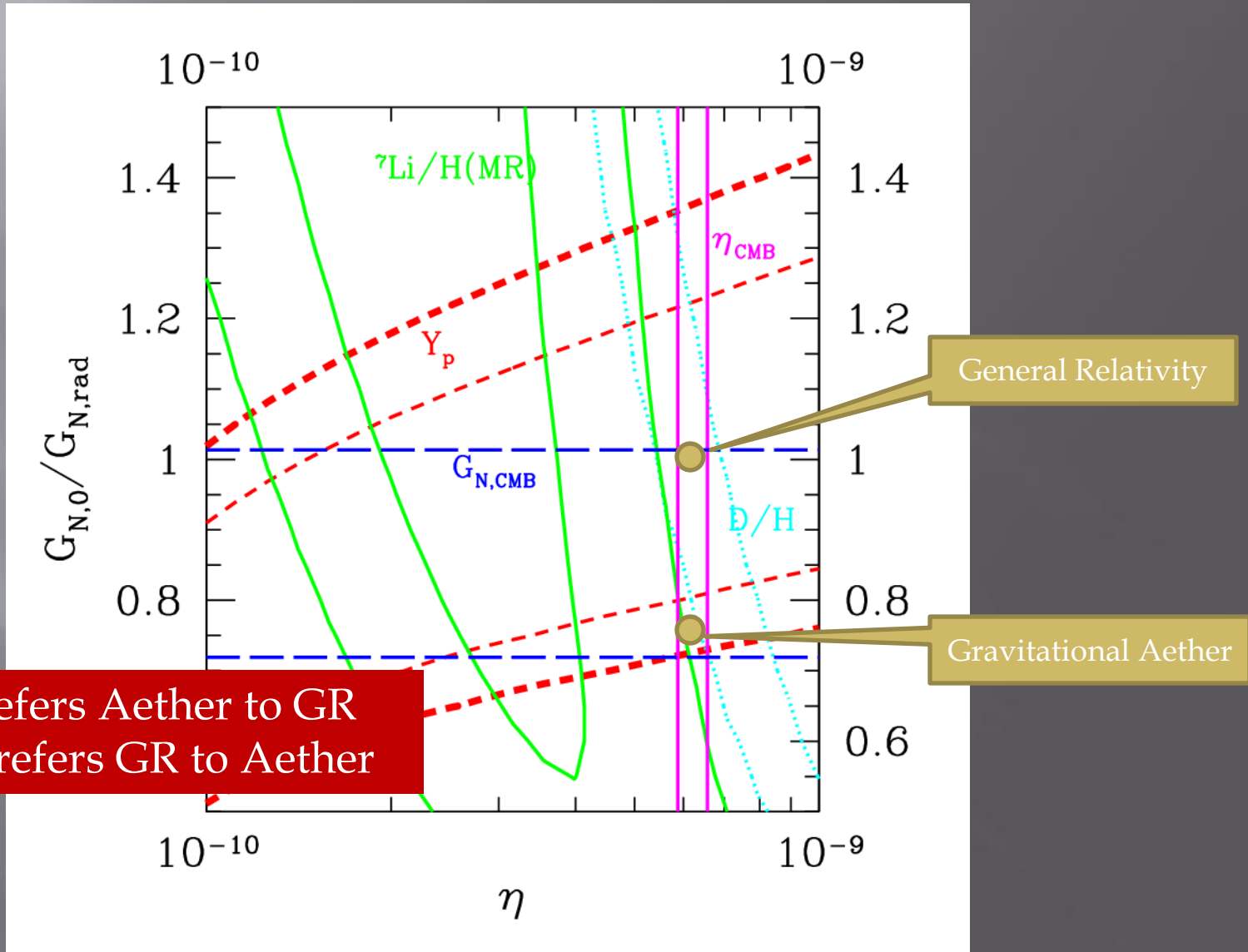
# Incompressible Aether!

- ▣ We require  $\omega \gtrsim 5$
  - ▣ Superluminal propagation:  $c_s = \omega^{1/2} > 1$  ?
  - ▣ Does not necessarily violate causality
    - c.f. K-essence: Mukhanov et al., Steinhilber et al.
  - ▣ Cuscuton ( $c_s = \infty$ ) : does not propagate information (Afshordi, Chung, Geshnizjani 2007)
- Field/Fluid equation becomes a constraint equation

# The *Real* BBN Constraints



K. Kohri

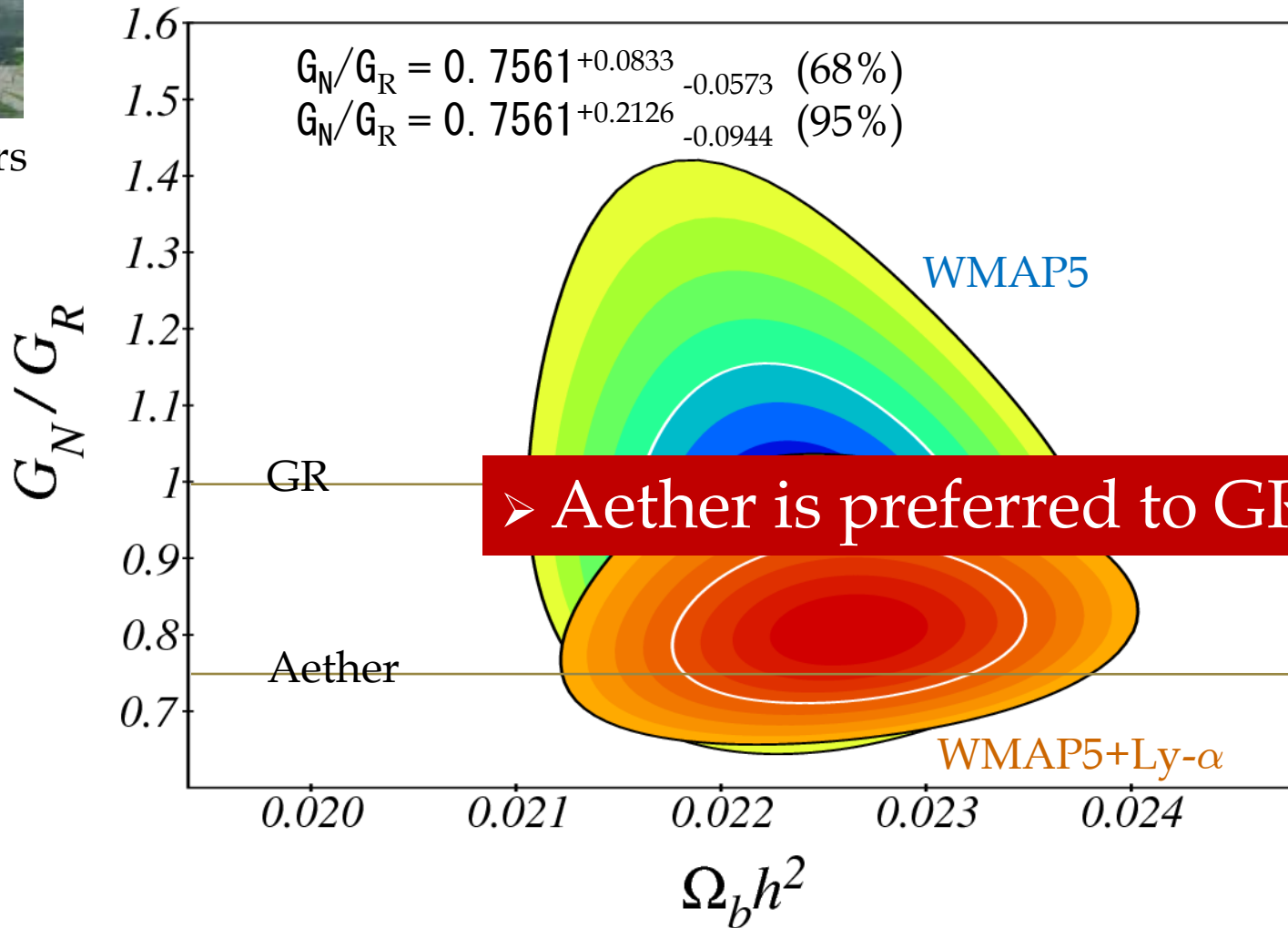


➤  $\text{Li}7$  prefers Aether to GR  
➤  $\text{He}4$  prefers GR to Aether

# Ly- $\alpha$ forest + WMAP5



G. Robbers



# Non-relativistic Perturbations:

- Euler + continuity equations  $\rightarrow$

$$p' + \frac{1}{4}T = p' \mathcal{O}(u^2, \phi) + \text{const.}$$

- Perturbations around a static background:

$$\frac{\partial^2 T \mathbf{u}}{\partial t^2} = \omega \nabla \nabla \cdot (T \mathbf{u})$$

- Longitudinal modes propagate superluminally/disperse
- What about rotation/gravito-magnetic effect?
- Aether follows the velocity of non-relativistic matter
- Gravitational constant depends on pressure:  $\propto (1+w) G$ , (modifies  $\zeta_4$ : unconstrained PPN parameter)  $G_{\text{eff}}$

# How does aether affect tests of gravity?

- ▣ As long as:
  - Aether tracks matter
  - Internal pressure is negligible
- Aether is indistinguishable from GR
- ▣ But:
  - Aether is irrotational → e.g. observing gravitomagnetic effect due to earth rotation can test it (Gravity Probe B)
  - Internal structure of self-gravitating objects with relativistic pressure (e.g. neutron stars, supernovae) will be sensitive to aether

# But Physical theories should have an action!

- ▣ *Not Necessarily!*
- ▣ *E.g.* coarse-grained theories have information-loss  $\rightarrow$  they're not unitary  $\rightarrow$  no action
- ▣ *E.g.* Fluid mechanics does not have an action: c.f. viscosity, turbulence, diffusion
- ▣ *Gravity Action is only necessary for Quantization (i.e. Quantum Gravity)*
- ▣ In contrast, our model describes quantum field theory in *classical* curved space-time

# two related works

## ▣ De-Gravitation, Cascading gravity

(Dvali, Khoury, Hofmann, Tolley, de Rham, ...)

- ▣ decouples  $\rho_{\text{vac}}$  through a massive graviton/induced gravity
- ▣ No non-linear + tractable realization

## ▣ Einstein-Aether theory

(Ted Jacobson, et al. )

- ▣ Lorentz breaking vector field:  $u_{\mu}$

Minimal coupling to gravity

→ does not address the cosmological constant problem



# Aether and Black Holes



C. Prescod-Weinstein

- ▣ Aether around a spherical Black Hole:

$$ds^2 = -e^{2\phi} dt^2 + \left(1 - \frac{2m}{r}\right)^{-1} dr^2 + r^2 d\Omega^2$$

$$e^\phi = \left(1 - \frac{2m}{r}\right)^{\frac{1}{2}} [4\pi p_0 f(r) + 1]$$

$$P = p_0 e^{-\phi}$$

- ▣ Limits far from and close to the horizon:

$$f(r) = \frac{r^2}{2} + 3mr + O\left[\frac{1}{r}\right]^0 \quad r \gg 2m$$

$$f(r) = -8 \frac{\sqrt{2} m^{5/2}}{\sqrt{-2m+r}} + \frac{15}{2} m^2 \ln[2m] + \sqrt{O[-2m+r]} \quad r - 2m \ll 2m$$

# Stellar BH' s and cosmic acceleration

- ▣ The same integration constant describes solution close to and far from the BH “horizon”

→ *UV-IR coupling*

- ▣ Maximum redshift:  $1/(-32\pi p_0 m^2)$

- ▣ Assuming this to be = *Planck Energy/Hawking Temp.*

→  $p_0 = -1/(256 \pi^2 m^3) = -\rho_\Lambda$ , for  **$m = 2.45 M_\odot$  !!!!**

→ **Formation of stellar Black Holes can trigger late-time cosmic acceleration**

Tras-Planckian  
corrections to gravity



C. Prescod-Weinstein

# Late-time Acceleration scenario

- $g_{00}$  around the black hole looks like de-Sitter space, so dust particles (i.e. stars/galaxies) accelerate away from the center
- As this happens around every BH, the coarse-grained Universe should look like  $\Lambda$  + matter
- With multiple black holes:  
$$\log m_* = \langle \log m \rangle_{\text{mass weighted}}$$
- As super-massive BH's grow, the effective  $\rho_{\text{DE}} \propto m_*^{-3}$  decreases

# But didn't you just kill Inflation?!

**No!**

- ▣  $G_{\text{eff}} \propto (1+w) G$
- ▣  $\rightarrow$  since  $w \neq -1$  during inflation, one could still get inflation with slight modifications
- ▣ For Inflation:
  - $w_{\text{eff}} = dP/d\rho \simeq -1$  (rather than  $P/\rho$ )
  - $\zeta \sim H/M_{\text{P}} \sim 10^{-5}$  (no  $\epsilon$  in the denominator)
  - similar slow-roll conditions, but with  $V'(\varphi)$  instead of  $V(\varphi)$
  - Gravity waves ??, need an action for the theory

# Conclusions

- ▣ Decouple gravity from vacuum energy by introducing an incompressible gravitational aether
- ▣ Aether ( $G_{\text{mat.}}/G_{\text{rad.}}=3/4$ ) is preferred by cosmological observations (Ly- $\alpha$ , WMAP, SDSS); **BBN constraints remain inconclusive**
- ▣ Ties horizon physics of stellar black holes to cosmology, explaining late-time cosmic acceleration
- ▣ Follows dust matter, and can satisfy tests of General Relativity \*
- ▣ Inflationary scenarios are only slightly modified

# missing links and future prospects

- ▣ Future CMB/LSS surveys will constrain  $G_{\text{mat.}}/G_{\text{rad.}}$  with 10 times better precision
- ▣ Precision tests of gravity: Rotation
- ▣ Fundamental theory and quantization
- ▣ How to patch BH space-times to make an accelerating FRW?
- ▣ Correlations between star formation/AGN activity and cosmic acceleration?
- ▣ *Should we re-evaluate our Dark Energy program?*