

# Probing Majorana Phases and Neutrino Mass Spectrum in the Higgs Triplet Model at the LHC

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- TeV scale mechanisms (“testable”) for neutrino mass generation
  - Higgs Triplet Model
  - Production of  $H^{\pm\pm}$  at hadron colliders
  - Precise measurements of  $H^{\pm\pm} \rightarrow l^{\pm}l^{\pm}$  at the LHC
  - Testing HTM at the LHC
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A.A, Mayumi Aoki (ICRR, Kashiwa), Hiroaki Sugiyama (SISSA, Trieste), arXiv:0712.4019[hep-ph]

IPMU Workshop on “Neutrino Mass”, Kashiwa, 19 March 2008

## TeV scale models of neutrino mass generation

*Many models for neutrino mass generation!*

Models with a specific signature at High Energy Colliders (Tevatron/LHC) are phenomenologically appealing

One such model is:

Higgs Triplet Model (HTM)

Schechter/Valle 80, Cheng/Li 80

Distinctive signature:

$H^{\pm\pm}$  with coupling to  $W, Z$  and leptons

## Higgs Triplet Model (HTM)

SM Lagrangian with one  $SU(2)_L$   $I = 1, Y = 2$  Higgs triplet

$$\Delta = \begin{pmatrix} \delta^+/\sqrt{2} & \delta^{++} \\ \delta^0 & -\delta^+/\sqrt{2} \end{pmatrix}$$

Higgs potential:

$$V = m^2(\Phi^\dagger\Phi) + \lambda_1(\Phi^\dagger\Phi)^2 + M^2\text{Tr}(\Delta^\dagger\Delta) \\ + \lambda_i \text{ (quartic terms)} + \frac{1}{\sqrt{2}}\mu(\Phi^T i\tau_2 \Delta^\dagger\Phi) + h.c$$

Triplet vacuum expectation value:

$$\langle \delta^0 \rangle = v_L \sim \mu v^2 / M^2 \quad (1 \text{ eV} < v_L < 8 \text{ GeV})$$

## Higgs boson spectrum

The HTM has 7 Higgs bosons:  $H^{\pm\pm}, H^{\pm}, H^0, A^0, h^0$

- $H^{\pm}, H^0, A^0, h^0$  are mixtures of doublet and triplet fields
- Mixing  $\sim v_L/v$  and  $v_L \ll v$
- $h^0$  plays role of *SM Higgs boson* (essentially  $I = 1/2$  doublet)
- $H^{\pm\pm}$  *purely triplet* and  $H^{\pm}, H^0, A^0$  *essentially triplet*
- $H^{\pm\pm}, H^{\pm}, H^0, A^0$  close to degenerate  $\sim M$
- For  $H^{\pm\pm}$  in range at LHC require  $M < 1$  TeV.

# Neutrino mass in Higgs Triplet Model (HTM)

No right-handed neutrino:

Neutrino mass from triplet-lepton-lepton coupling ( $h_{ij}$ ):

$$h_{ij} \left[ \sqrt{2} \bar{l}_i^c P_L l_j H^{++} + (\bar{l}_i^c P_L \nu_j + \bar{l}_j^c P_L \nu_i) H^+ - \sqrt{2} \bar{\nu}_i^c P_L \nu_j H^0 \right] + h.c$$

Light neutrinos receive a Majorana mass:  $\mathcal{M}_\nu \sim v_L h_{ij}$

$$h_{ij} = \frac{1}{\sqrt{2}v_L} V_{\text{MNS}} \text{diag}(m_1, m_2, m_3) V_{\text{MNS}}^T$$

( $V_{\text{MNS}} = V_l^\dagger V_\nu$ ; take  $V_l = I$  and  $V_\nu = V_{\text{MNS}}$ )

## Limits on $h_{ij}$

Presence of  $H^{\pm\pm}$  would lead to lepton flavour violating decays

Many limits exist for  $h_{ij}$  (assuming  $m_{H^{\pm\pm}} < 1$  TeV):

Cuypers/Davidson 98

- $\text{BR}(\mu \rightarrow eee) < 10^{-12} \rightarrow h_{\mu e} h_{ee} < 10^{-7}$ : 1988; no forthcoming experiment
- $\text{BR}(\tau \rightarrow l_i l_j l_k) < 10^{-8} \rightarrow h_{\tau i} h_{jk} < 10^{-4}$  Limits from ongoing B factories
- $\text{BR}(\mu \rightarrow e\gamma) < 10^{-11} \rightarrow \sum_i h_{\mu i} h_{ei} < 10^{-6}$  sensitivity to  $\text{BR} > 10^{-13}$  from 2008

All constraints can be respected with suitably chosen  $h_{ij}$

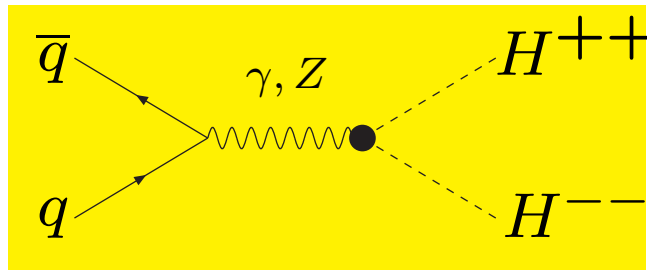
Absolute values not so important for  $H^{\pm\pm}$  direct searches

Production of  $H^{\pm\pm}$  at Hadron Colliders  
(Tevatron and LHC)

# Production of $H^{\pm\pm}$ at Tevatron

First searches at a Hadron collider in 2003 **CDF, D0**

$$\mathcal{L} = i \left[ (\partial^\mu H^{--}) H^{++} \right] (gW_{3L\mu} + g'B_\mu) + h.c$$



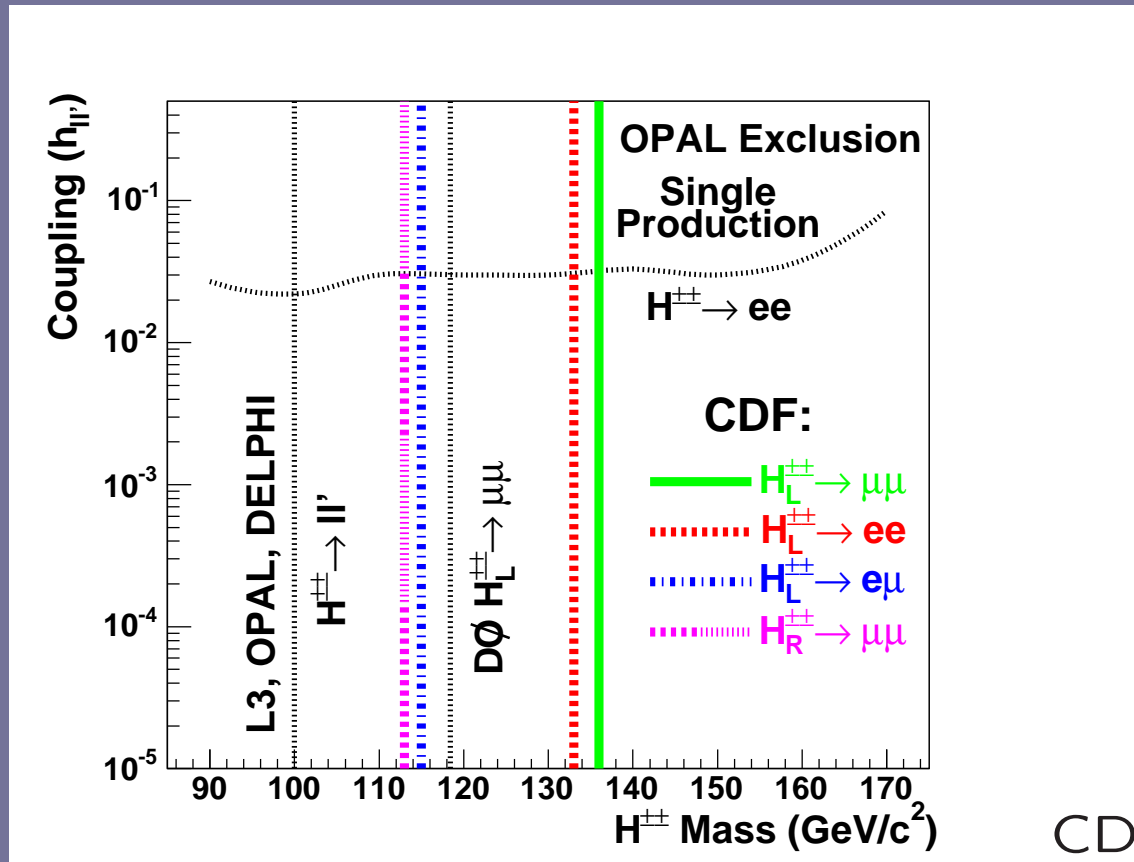
- $\sigma_{H^{++}H^{--}}$  is a simple function of  $m_{H^{\pm\pm}}$
- $\sigma_{H^{++}H^{--}}$  has no dependence on  $h_{ij}$



## Search strategy

- $H^{\pm\pm}$  decays via  $h_{ij}$  to *same charge*  $ee, \mu\mu, \tau\tau, e\mu, e\tau, \mu\tau$
- 4 leptons from pair produced  $H^{++}H^{--}$
- For  $e^{\pm}e^{\pm}, e^{\pm}\mu^{\pm}, \mu^{\pm}\mu^{\pm}$ , sufficient to search for two leptons of high momentum and same charge
- Background almost negligible ( $\approx 1$  event)
- Mass limits presented for  $\text{BR}(H^{\pm\pm} \rightarrow l_i^{\pm}l_j^{\pm}) = 100\%$   
in a given channel

# Comparison of $H^{\pm\pm}$ searches



Strongest mass limits for any Higgs boson!

Branching ratio for  $H^{\pm\pm} \rightarrow l^{\pm}l^{\pm}$  and  
testing HTM at LHC

Akeroyd, Aoki, Sugiyama, arXiv:0712.4019[hep-ph]

## Light $H^{\pm\pm}$ at LHC

Simulations by Azuelos et al 05, Hebbeker et al 06, Hektor et al 07, Han et al 07

- Discovery for  $m_{H^{\pm\pm}} < 400$  GeV with  $1 \text{ fb}^{-1}$
- Precise measurements of  $\text{BR}(H^{\pm\pm} \rightarrow l^{\pm}l^{\pm})$  possible for  $l = e, \mu$
- Sensitivity to  $\text{BR}(H^{\pm\pm} \rightarrow l^{\pm}l^{\pm}) \sim 1\%$  for  $l = e, \mu$

Large Event Numbers for  $H^{\pm\pm}$ :

$m_{H^{\pm\pm}}$ (GeV)	$N_{4l}$ ( $30 \text{ fb}^{-1}$ )	$N_{4l}$ ( $300 \text{ fb}^{-1}$ )
200	1500	15000
300	300	3000
400	90	900

## Branching ratios of $H^{\pm\pm} \rightarrow l^{\pm}l^{\pm}$

$\text{BR}(H^{\pm\pm} \rightarrow l_i^{\pm}l_j^{\pm})$  depends on relative values of  $h_{ij}$

$$\Gamma(H^{\pm\pm} \rightarrow l_i^{\pm}l_j^{\pm}) \sim \frac{m_{H^{\pm\pm}}}{8\pi} |h_{ij}|^2$$

In HTM  $h_{ij}$  is directly related to neutrino mass matrix

$$h_{ij} = \frac{1}{\sqrt{2}v_L} V_{\text{MNS}} \text{diag}(m_1, m_2, m_3) V_{\text{MNS}}^T$$

Prediction for  $\text{BR}(H^{\pm\pm} \rightarrow l_i^{\pm}l_j^{\pm})$  determined by: Chun, Lee, Park 03

- Neutrino mass hierarchy (normal, inverted)
- Neutrino oscillation parameters (masses, mixing angles)

## Explicit expressions for $h_{ij}$

All  $h_{ij}$  are functions of nine parameters:

$$h_{ee} = \frac{1}{\sqrt{2}v_{\Delta}}(m_1 c_{12}^2 c_{13}^2 + m_2 s_{12}^2 c_{13}^2 e^{i\varphi_1} + m_3 s_{13}^2 e^{-2i\delta} e^{i\varphi_2})$$

Five parameters are experimentally constrained:

$$\Delta m_{21}^2 \equiv m_2^2 - m_1^2 \simeq 7.9 \times 10^{-5} \text{eV}^2, \quad |\Delta m_{31}^2| \equiv |m_3^2 - m_1^2| \simeq 2.7 \times 10^{-3} \text{eV}^2, \\ \sin^2 2\theta_{12} \simeq 0.86, \quad \sin^2 2\theta_{23} \simeq 1, \quad \sin^2 2\theta_{13} \lesssim 0.13.$$

Main uncertainty in  $h_{ij}$  comes from:

- Absolute mass of lightest neutrino:  $0 < m_0 < 1 \text{eV}$
- Majorana phases  $0 < \phi_1, \phi_2 < 2\pi$

These three parameters are **unconstrained** by neutrino oscillation data

# Testing the HTM at LHC via precise measurements

## of $\text{BR}(H^{\pm\pm} \rightarrow l^{\pm}l^{\pm})$

There are several models of neutrino mass generation with possibly light  $H^{\pm\pm} \rightarrow l^{\pm}l^{\pm}$ :

- **Left-Right Symmetric Model**:  $I = 1, Y = 2$  triplet

Neutrino mass via seesaw mechanism,  $h_{ij}$  arbitrary

- **Zee-Babu Model**  $I = 0, Y = 4$  singlet

Radiative neutrino mass; some correlation of  $h_{ij}$  with neutrino mass matrix

→ HTM predicts **distinctive regions** for  $\text{BR}(H^{\pm\pm} \rightarrow l^{\pm}l^{\pm})$

which can be tested at LHC for  $m_{H^{\pm\pm}} < 400$  GeV

## Dependence of $\text{BR}(H^{\pm\pm} \rightarrow l^{\pm}l^{\pm})$ on $m_0, \phi_1, \phi_2$

- Neglect Majorana phases,  $\phi_1 = \phi_2 = 0$ :

$\text{BR}(H^{\pm\pm} \rightarrow l^{\pm}l^{\pm})$  essentially determined by absolute neutrino mass  $m_0$

- Include Majorana phases,  $\phi_1 \neq 0, \phi_2 \neq 0$ :

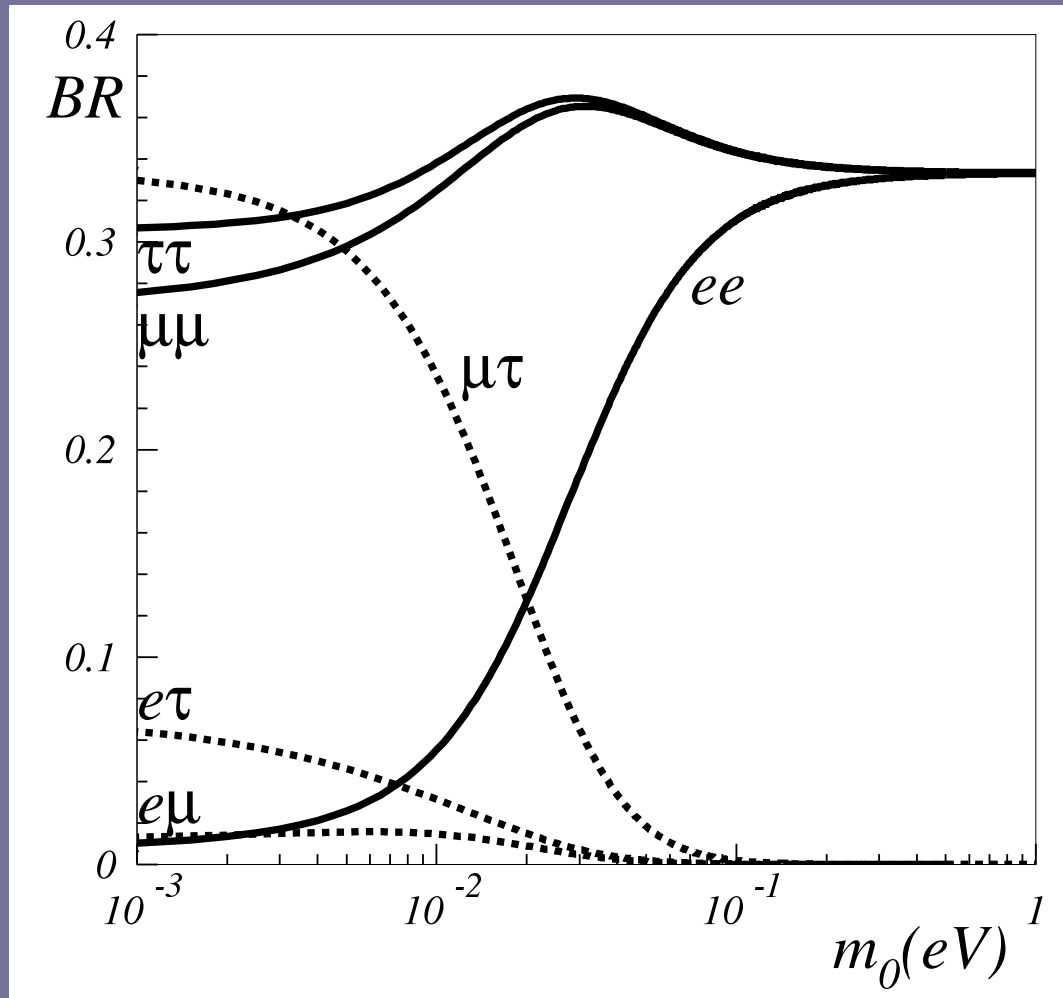
Allowed regions for  $\text{BR}(H^{\pm\pm} \rightarrow l^{\pm}l^{\pm})$  considerably larger but still smaller than case of arbitrary  $h_{ij}$

→ we quantify the prediction for  $\text{BR}(H^{\pm\pm} \rightarrow l^{\pm}l^{\pm})$  in the HTM

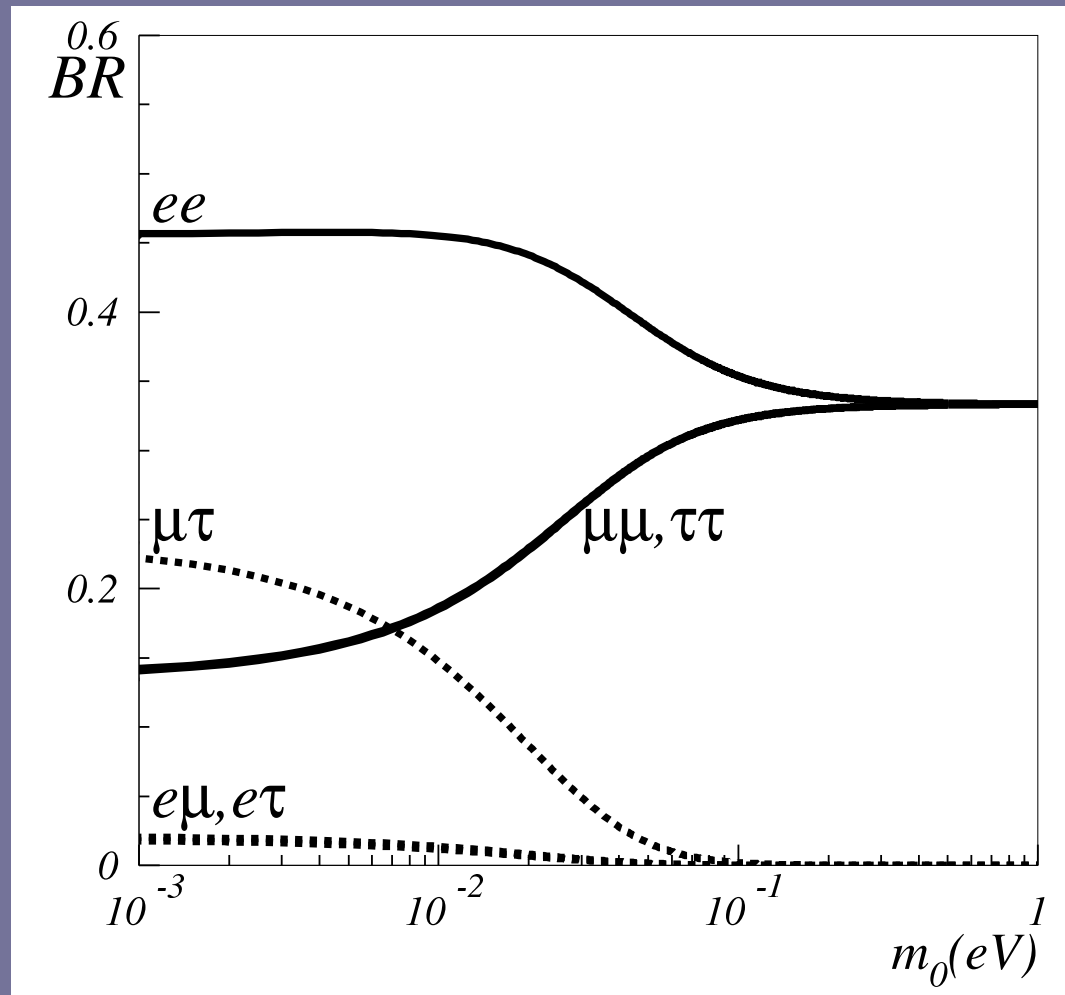
(see also Garayoa et al, arXiv:0712.1453[hep-ph] and Kadastik et al, 0712.3912[hep-ph])



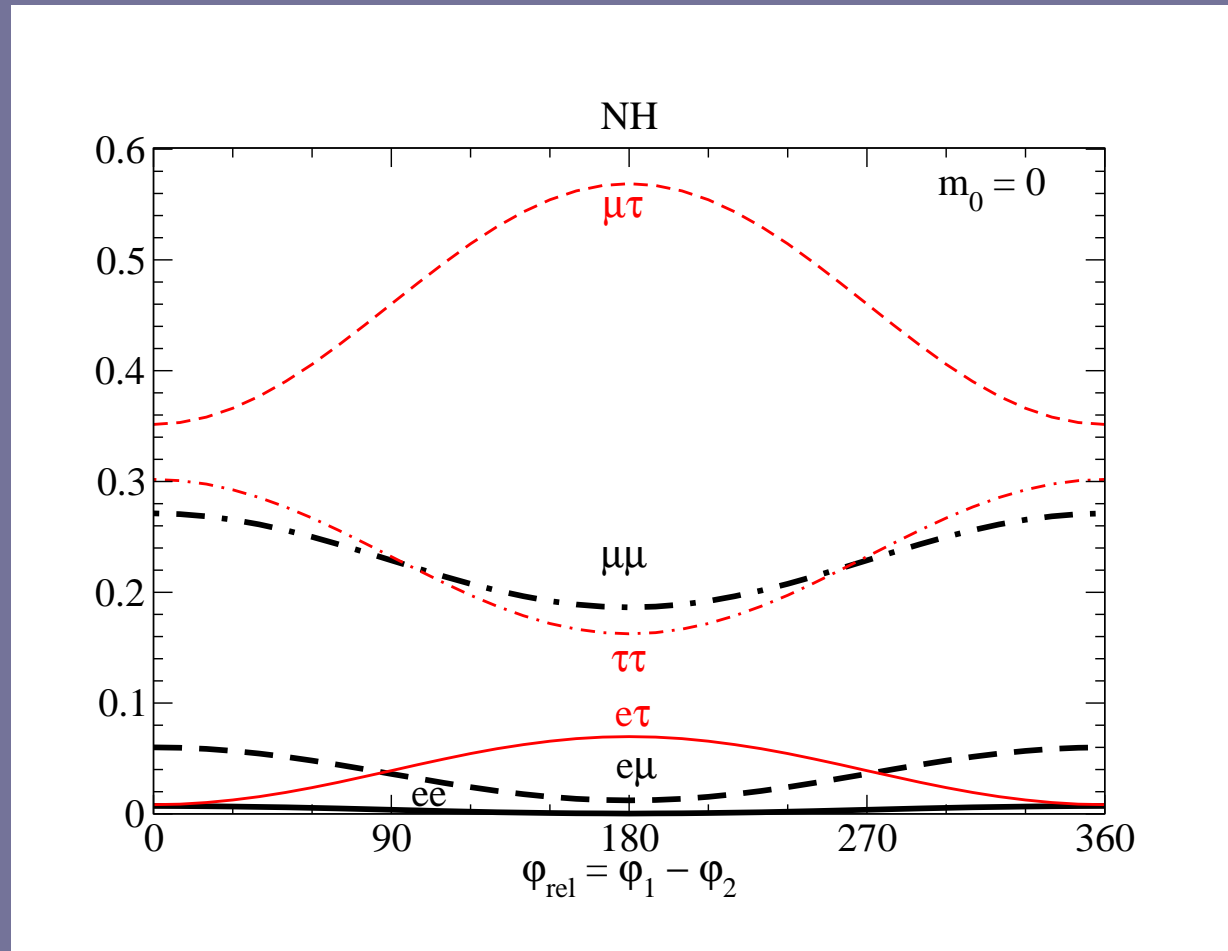
$BR(H^{\pm\pm} \rightarrow l_i^\pm l_j^\pm)$  against lightest neutrino mass ( $m_0$ ): normal hierarchy



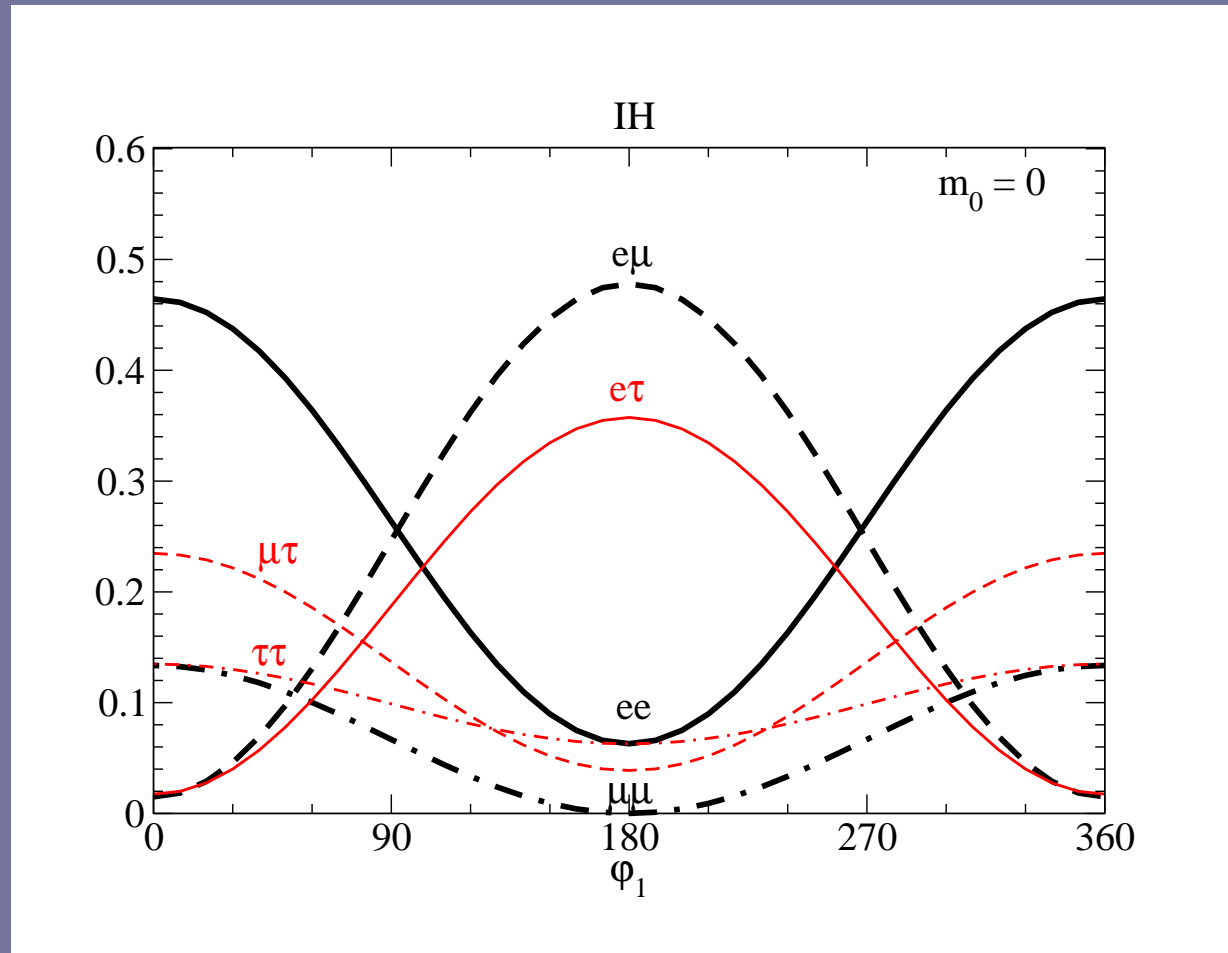
$BR(H^{\pm\pm} \rightarrow l_i^\pm l_j^\pm)$  against lightest neutrino mass ( $m_0$ ): inverted hierarchy



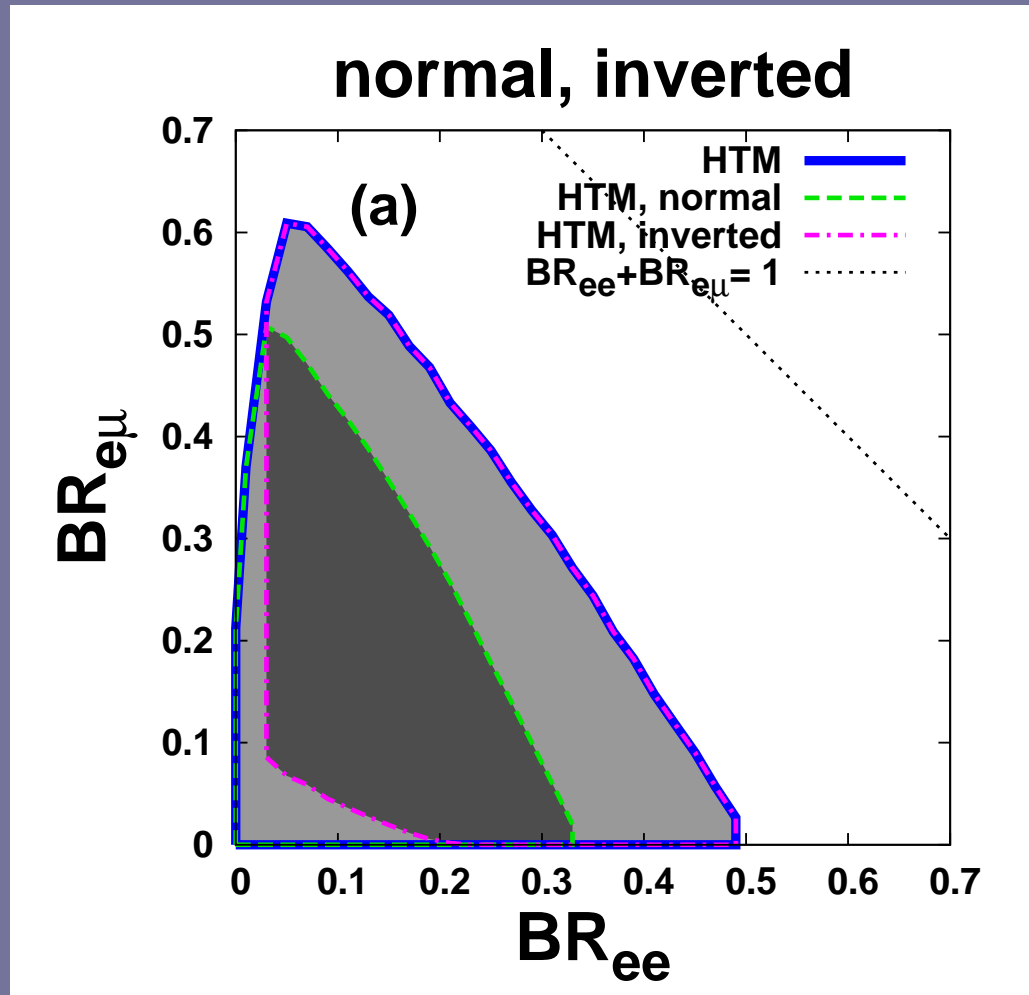
$\text{BR}(H^{\pm\pm} \rightarrow l_i^{\pm} l_j^{\pm})$  against Majorana phase and  $m_0 = 0$ : normal hierarchy



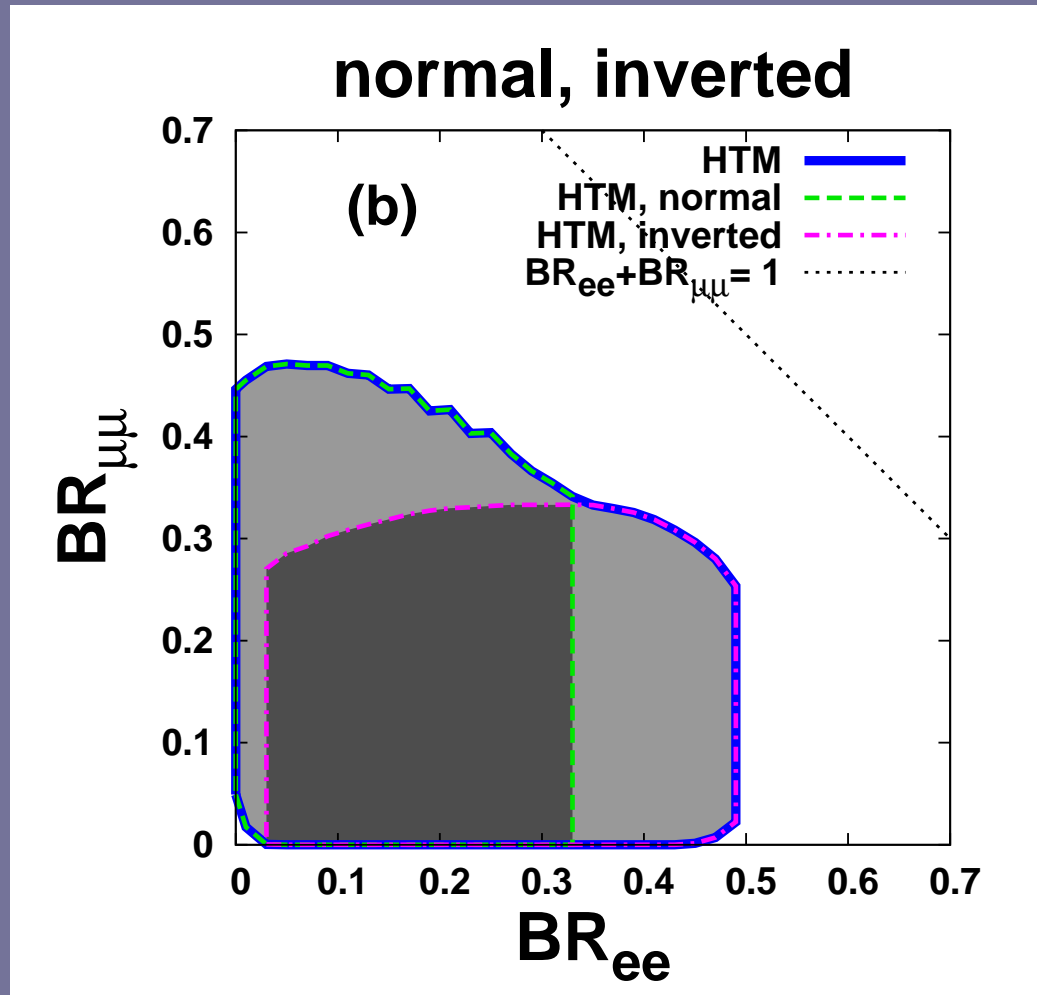
$\text{BR}(H^{\pm\pm} \rightarrow l_i^\pm l_j^\pm)$  against Majorana phase and  $m_0 = 0$ : inverted hierarchy



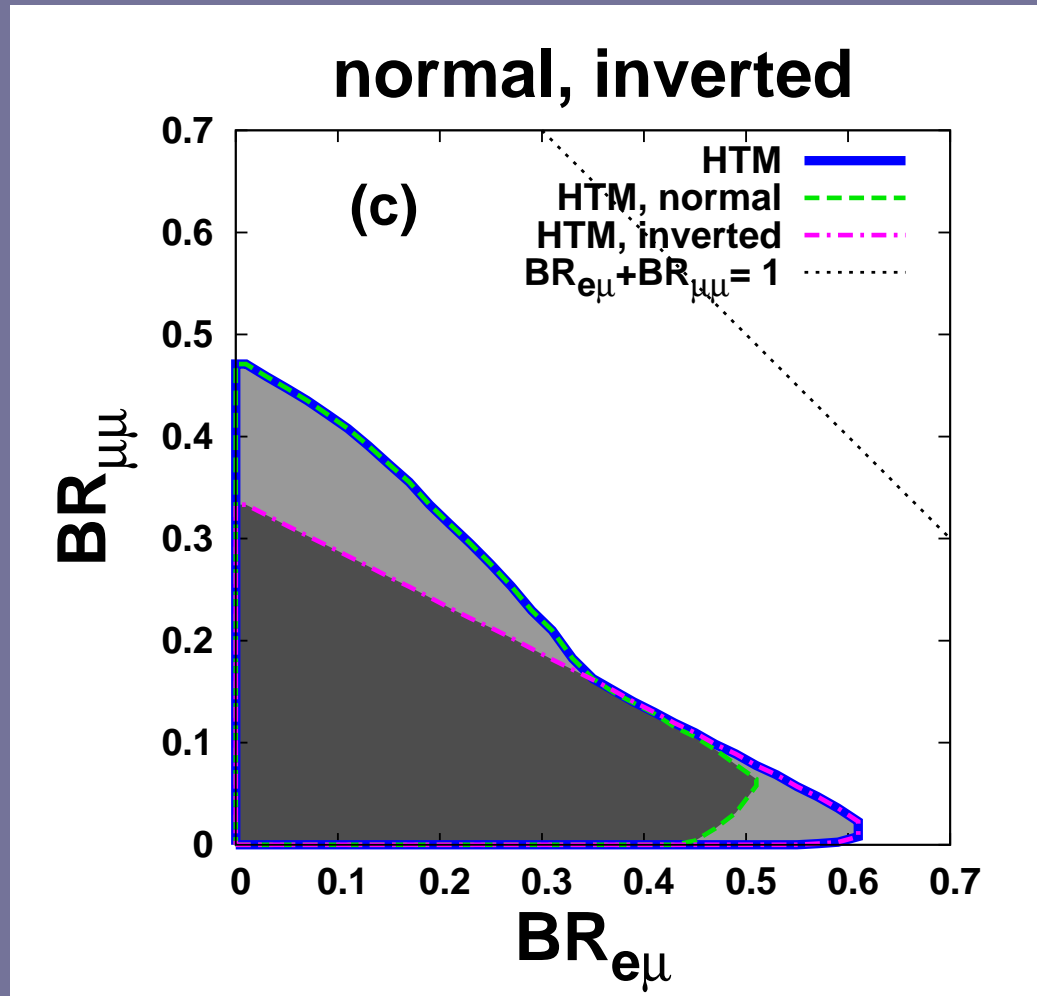
HTM prediction in the plane  $[BR(H^{\pm\pm} \rightarrow e^{\pm}e^{\pm}), BR(H^{\pm\pm} \rightarrow e^{\pm}\mu^{\pm})]$



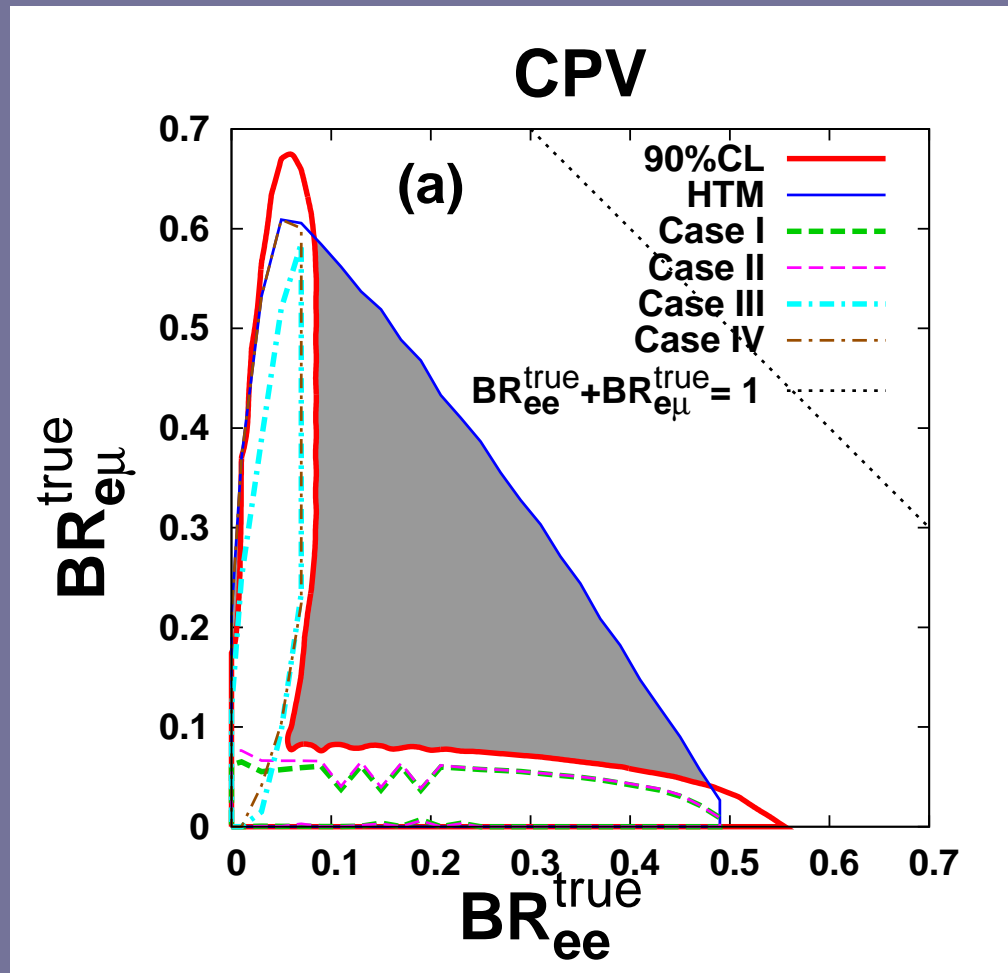
HTM prediction in the plane  $[BR(H^{\pm\pm} \rightarrow e^{\pm}e^{\pm}), BR(H^{\pm\pm} \rightarrow \mu^{\pm}\mu^{\pm})]$



HTM prediction in the plane  $[BR(H^{\pm\pm} \rightarrow e^{\pm}\mu^{\pm}), BR(H^{\pm\pm} \rightarrow \mu^{\pm}\mu^{\pm})]$



HTM prediction in the plane  $[BR(H^{\pm\pm} \rightarrow e^{\pm}e^{\pm}), BR(H^{\pm\pm} \rightarrow e^{\pm}\mu^{\pm})]$   
with/without CP violation from Majorana phases





## Conclusions

- Higgs Triplet Model generates neutrino mass  $h_{ij}v_T$
- $H^{\pm\pm} \rightarrow l^{\pm}l^{\pm}$  is a distinctive signal with BRs determined by  $h_{ij}$
- LHC can produce thousands of  $H^{\pm\pm} \rightarrow l^{\pm}l^{\pm}$  events if  $M_{H^{\pm\pm}} < 400$  GeV
- HTM predicts specific regions for  $\text{BR}(H^{\pm\pm} \rightarrow l^{\pm}l^{\pm})$  which can be tested at LHC
- Majorana phases/neutrino mass determine the allowed regions of  $\text{BR}(H^{\pm\pm} \rightarrow l^{\pm}l^{\pm})$
- Collider information on such parameters

## Other production mechanisms/decay channels for $H^{\pm\pm}$

Several production mechanisms: Barenboim et al 96, Maalampi et al 02

- $qq \rightarrow W^{\pm*} \rightarrow H^{\pm\pm}W^{\mp}$ ,  $qq \rightarrow q'q'W^{\pm*}W^{\pm*} \rightarrow q'q'H^{\pm\pm}$
- $WWH^{\pm\pm} \sim v_L$ ; appreciable rates only for  $v_L > 1$  GeV

Several decay channels:

- $H^{\pm\pm} \rightarrow W^{\pm}W^{\pm}$ ; small for  $v_L < 0.1$  MeV
- $H^{\pm\pm} \rightarrow H^{\pm}W^{\pm*}$ ; not open for  $m_{H^{\pm}} \geq m_{H^{\pm\pm}}$

Hereafter we assume the sole decay channel is  $H^{\pm\pm} \rightarrow l^{\pm}l^{\pm}$

Tevatron search for  $p\bar{p} \rightarrow H^{++}H^{--}$ ,  $H^{\pm\pm} \rightarrow e^{\pm}e^{\pm}, e^{\pm}\mu^{\pm}, \mu^{\pm}\mu^{\pm}$

