

Study of chargino-neutralino production at hadron colliders in a long-lived slepton scenario

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Based on 0806.1057 [hep-ph]

Mini review of SUSY breaking

MSSM

MSSM is defined by

Supersymmetric
Standard Model

+

$O(100)$ soft SUSY breaking terms ???

This is analogous to

Standard Model

-

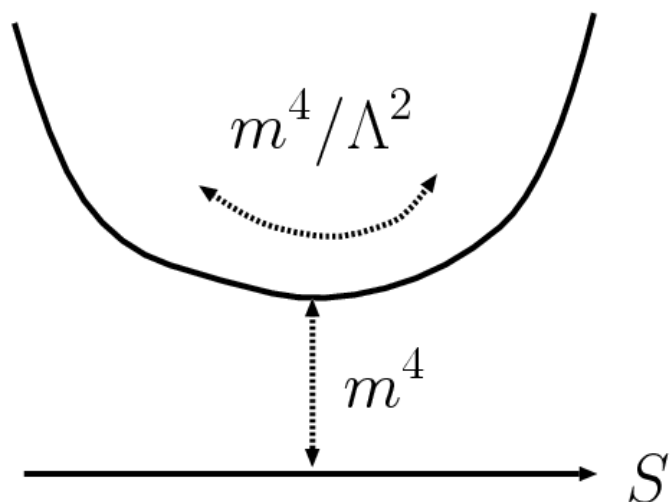
Higgs boson

$SU(3) \times SU(2) \times U(1)$ gauge theory + fermion masses

W+Z boson masses

We want the **Standard MSSM** for this model to be a consistent theory.

SUSY breaking/mediation



$$K = S^\dagger S - \frac{(S^\dagger S)^2}{\Lambda^2}$$

$$W = m^2 S$$

Classification of the mediation models

SUSY breaking sector

$$\mathcal{L} \ni f(S) \underbrace{F^{\mu\nu} F_{\mu\nu}}$$

SM gauge fields

Gravity

$$f(S) = c_0 + \frac{c_1 S}{M_{\text{Pl}}} + \dots$$

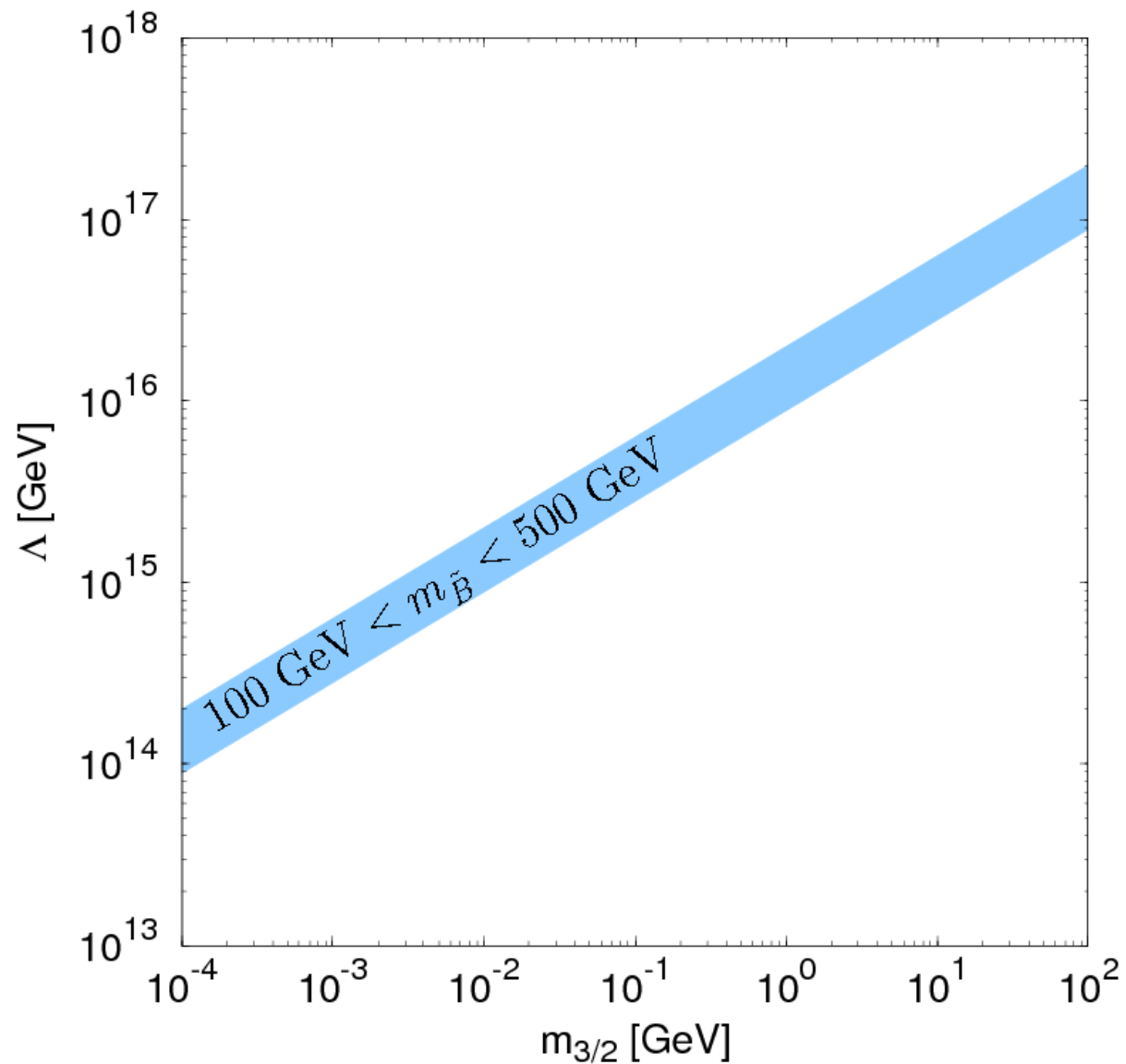
Gauge

$$f(S) = c_0 + c_L \frac{\alpha}{4\pi} \log S + \dots$$

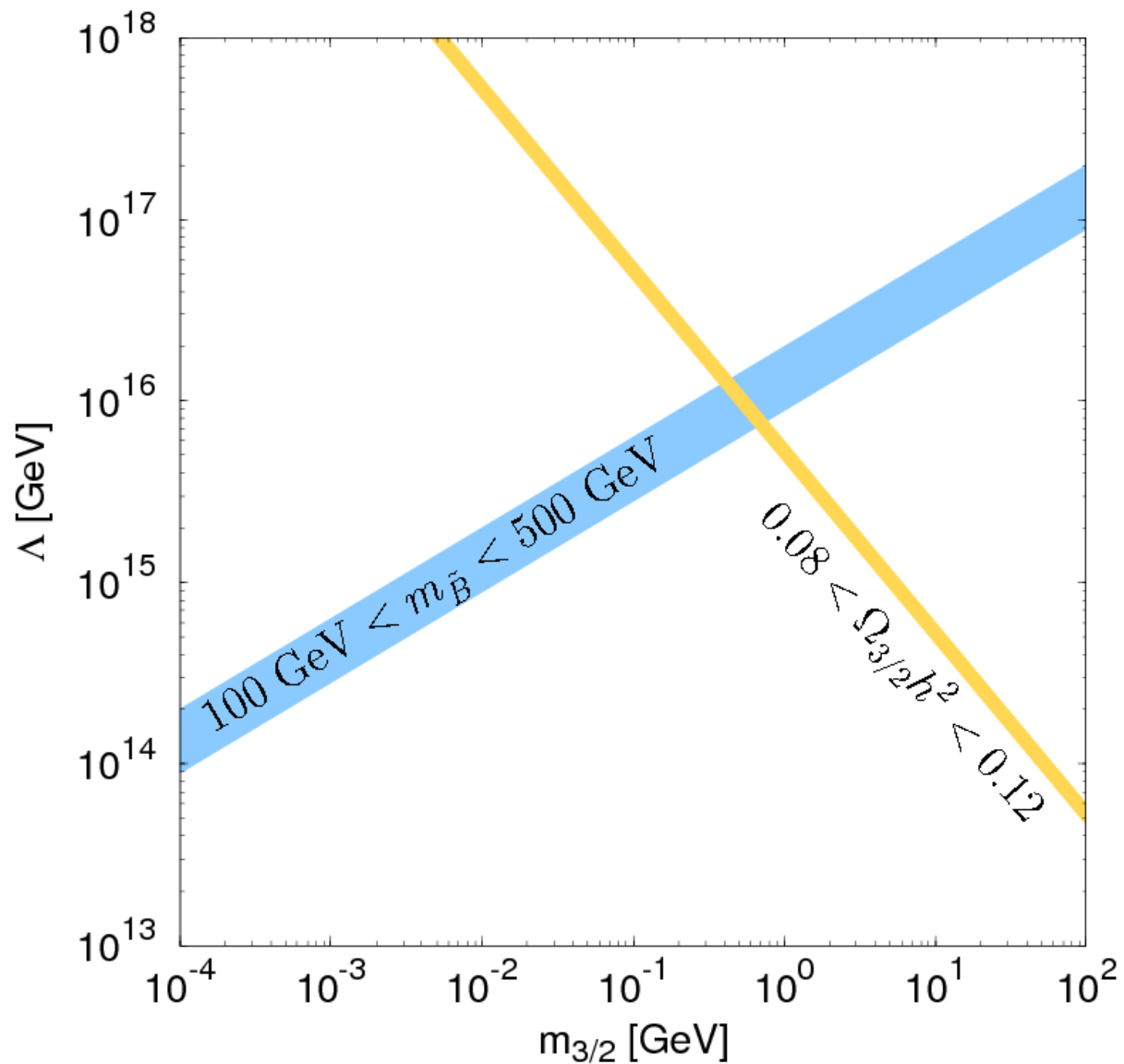
Anomaly

$$f(S) \simeq c_0$$

Gaugino masses

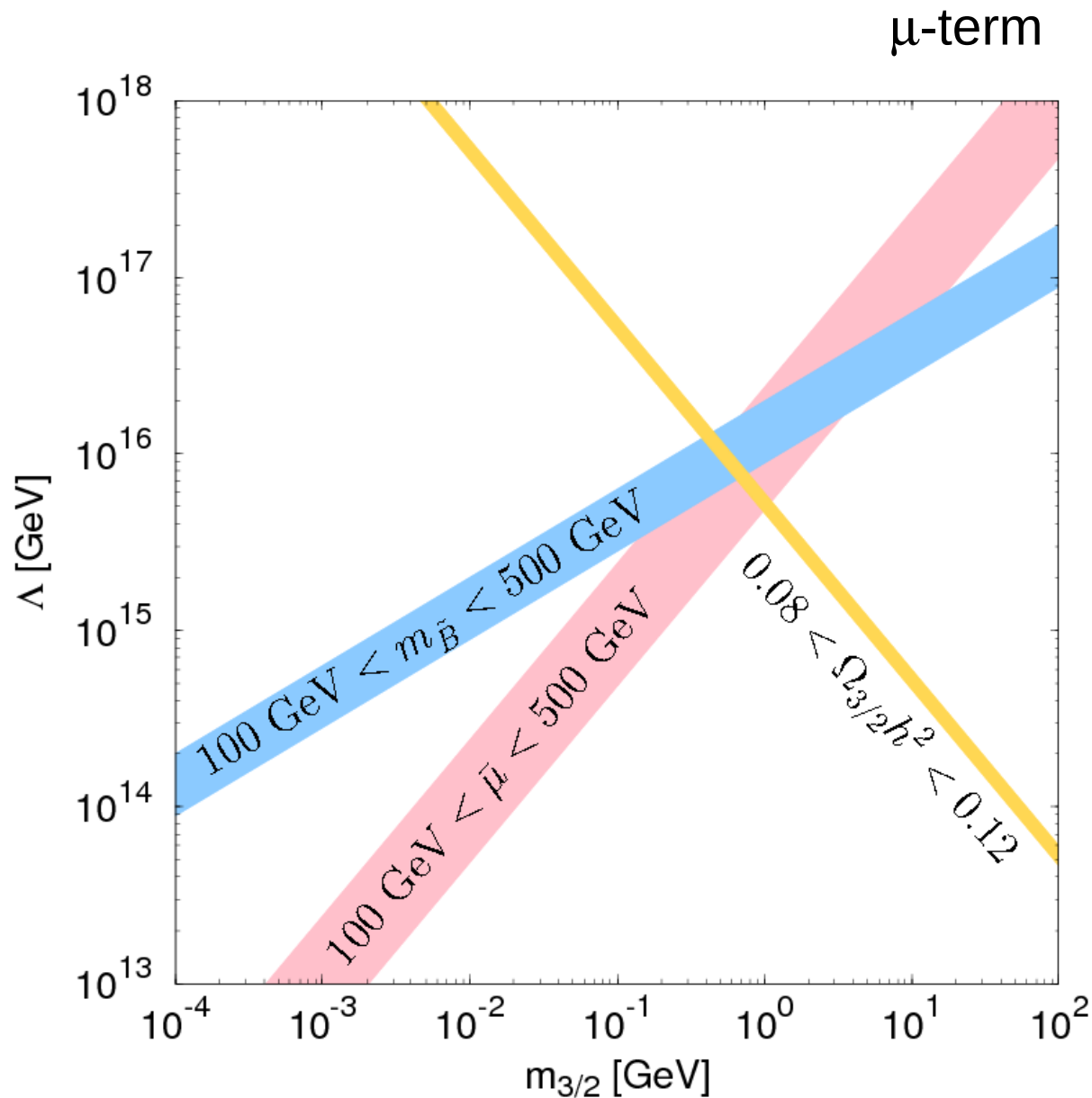


Dark Matter!



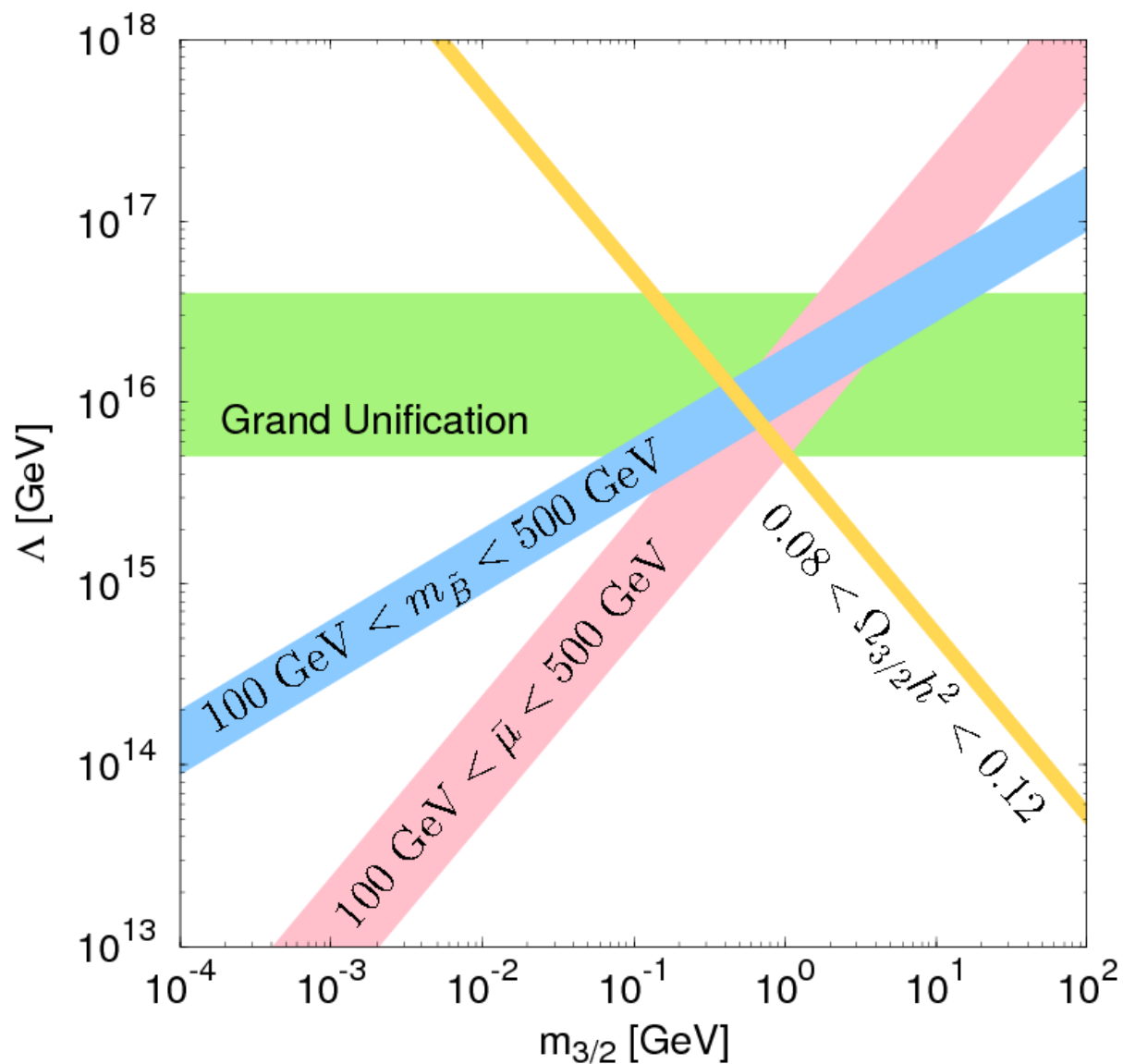
Sweet Spot Supersymmetry

[Ibe, RK '06]

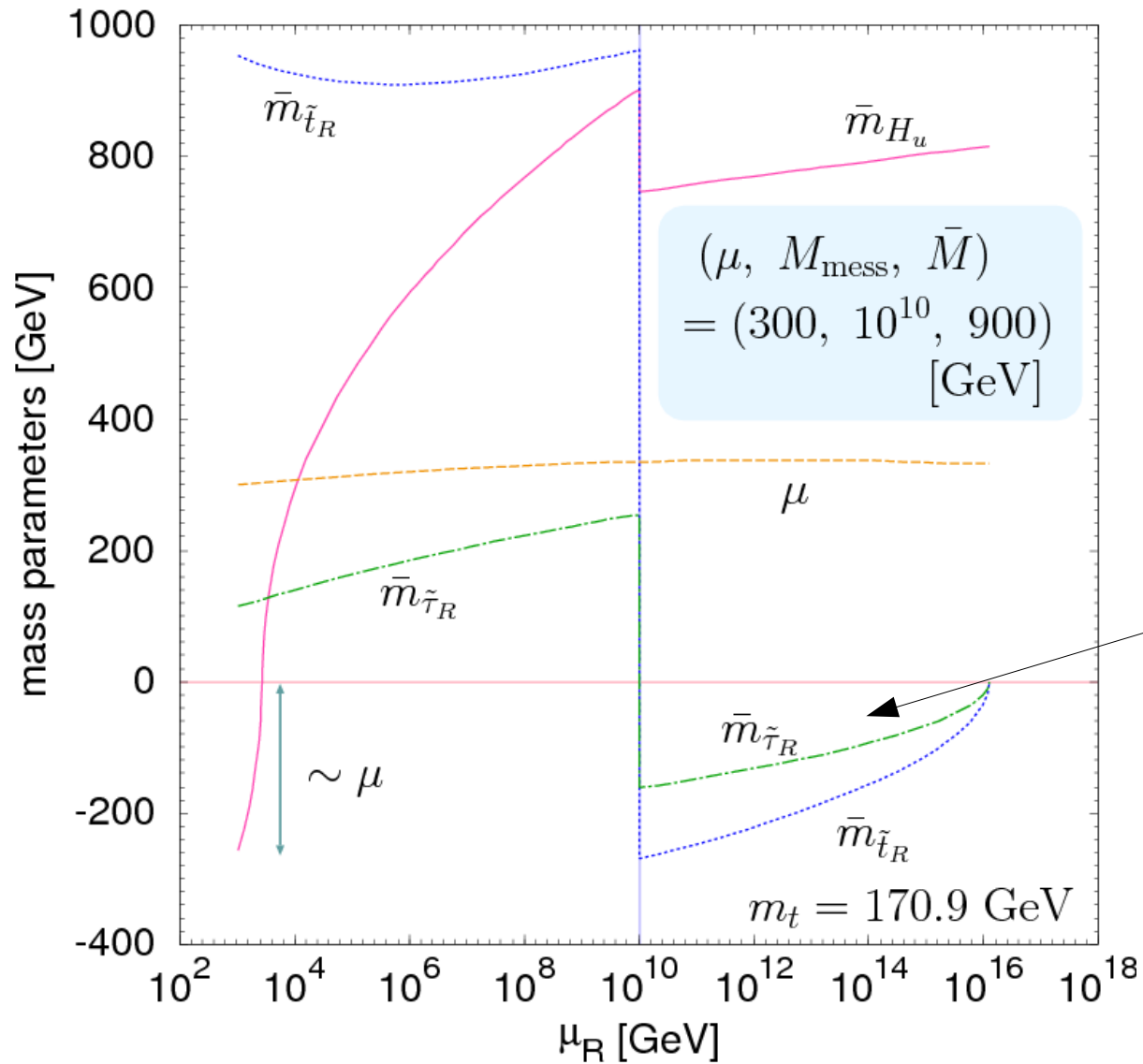


Assuming direct interaction between SUSY breaking and the Higgs fields.

Grand Unification!



Sweet Spot and stau NLSP



Negative contributions through the Yukawa interaction.

It is a result of a specific (but almost unique successful) model, but it is in general true that the Yukawa interaction can make stau lighter than other superparticles.

Given that there is no strong motivation to believe in gravity mediation, the stau NLSP scenario is I think worth looking at.

The LHC signatures are very different from conventional (and unmotivated) scenarios.

Overview of stau NLSP at LHC

[Drees, Tata '90][Feng, Moroi '97]
[Nisati, Petrarca, Salvini '97][Martin, Wells '98]
[Hinchliffe, Paige '98][Polesello, Rimoldi '99]
[Ambrosanio, Mele, Petrarca, Polesello, Rimoldi '00]

If the gravitino mass is large enough ($\gg 100\text{keV}$), staus decay outside the detector.

Stau looks like a **muon** which is a very nice particle for collider physics!

Very accurate mass ($\pm 10\text{-}100\text{MeV}$) and momentum measurement (a few %) are possible at ATLAS (and probably at CMS).

[Polesello, Rimoldi '99][Ambrosanio, Mele, Petrarca, Polesello, Rimoldi '00]

→ **Lots of applications!**

* Neutralino (and other sparticle) mass measurement

[Hinchliffe, Paige '98][Ellis, Raklev, Oye '06][Ibe, RK '06]

* Spin measurement

[Rajaraman, Smith '07]

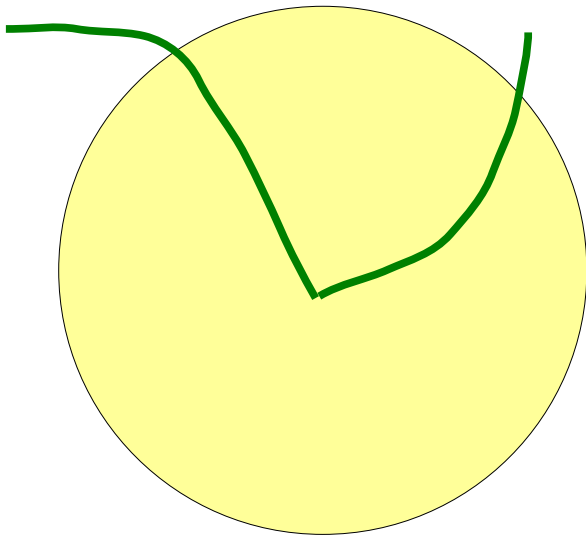
* New search for Lepton Flavor Violation

[Hamaguchi, Ibarra '04][RK '08]

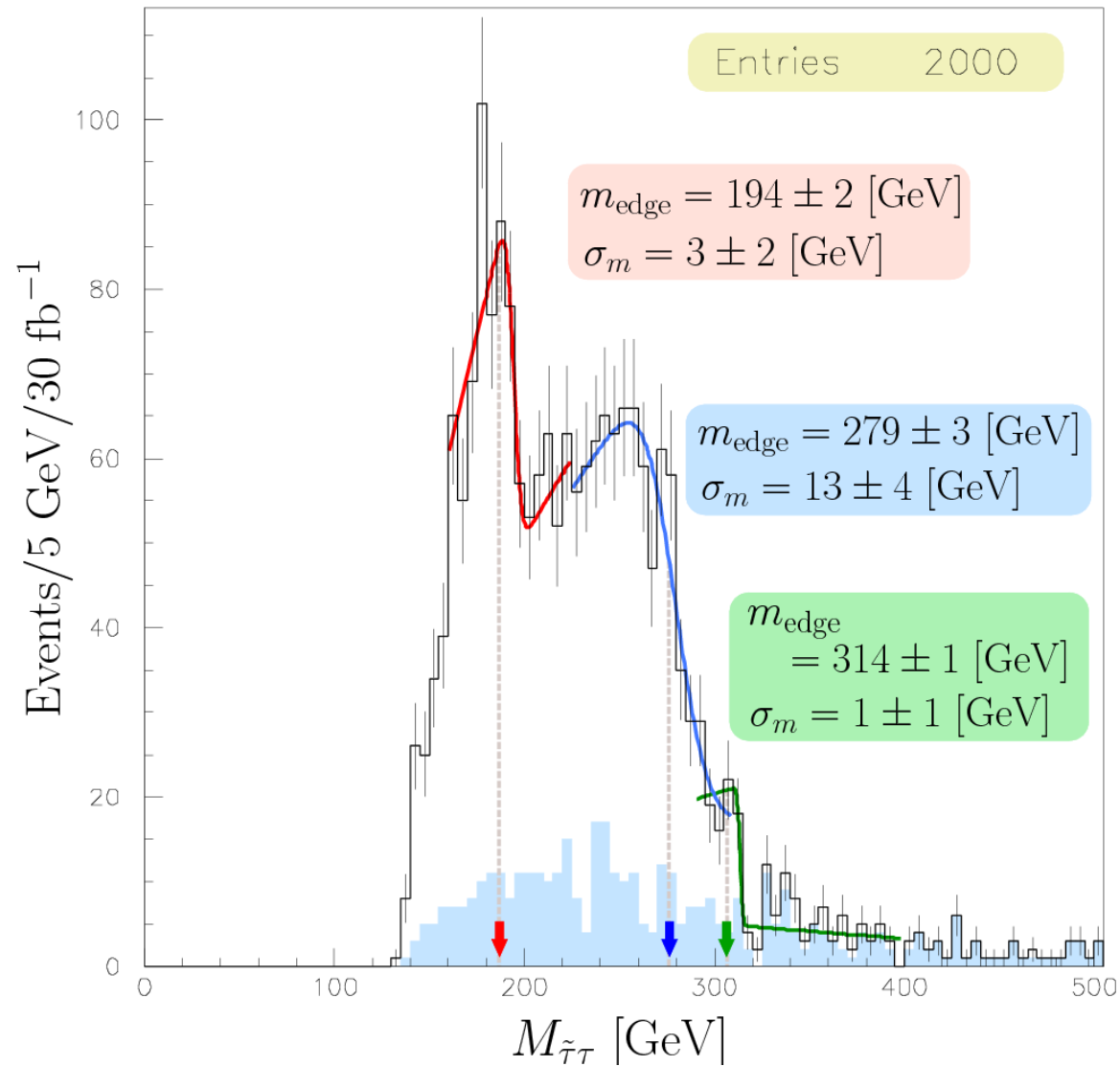
* lifetime measurement

[Buchmuller, Hamaguchi, Ratz, Yangida '04]

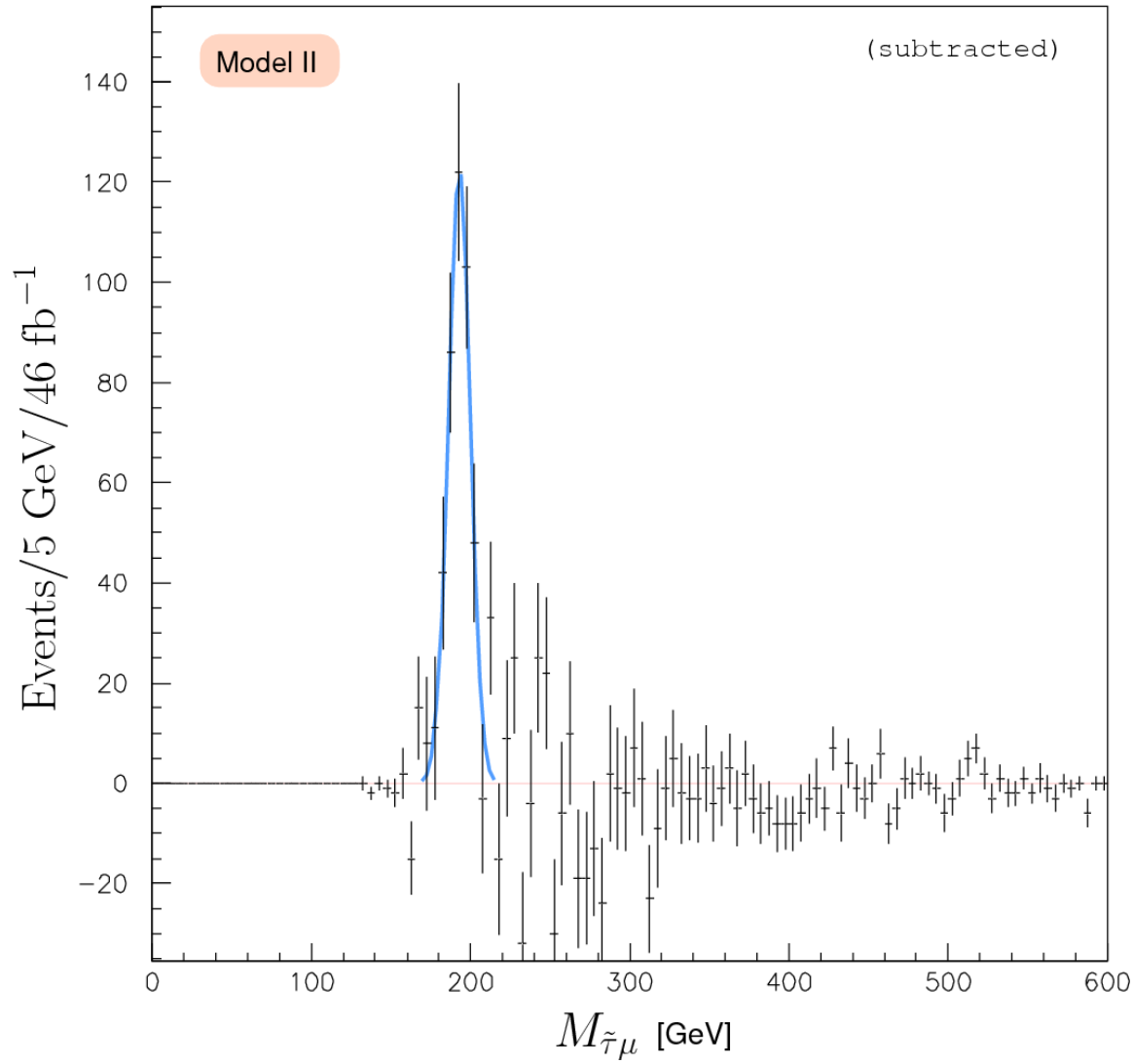
[Hamaguchi, Kuno, Nakaya, Nojiri '04][Feng, Smith '04]



Neutralino mass measurement (Sweet Spot example)

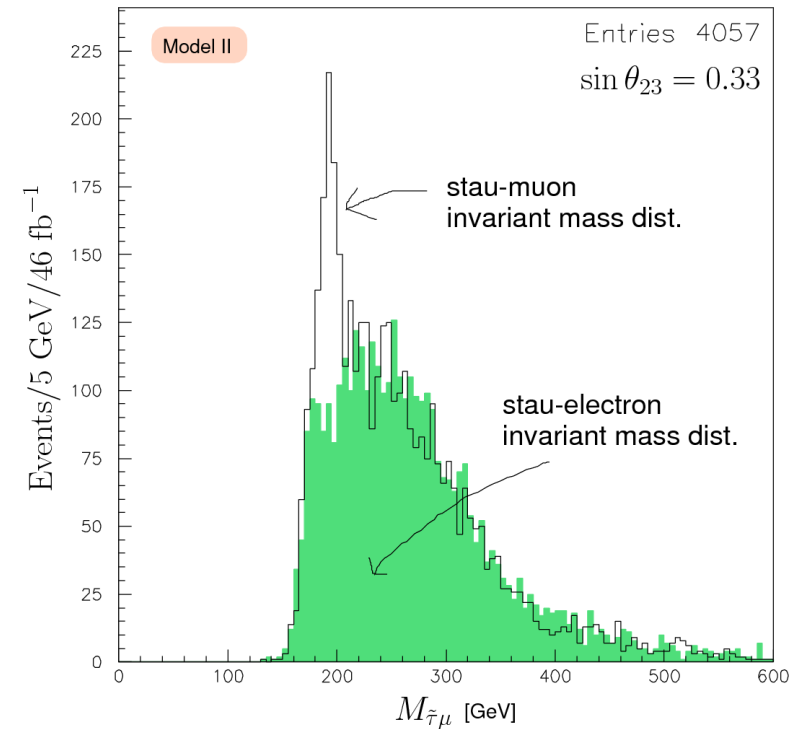


Search for LFV neutralino decay



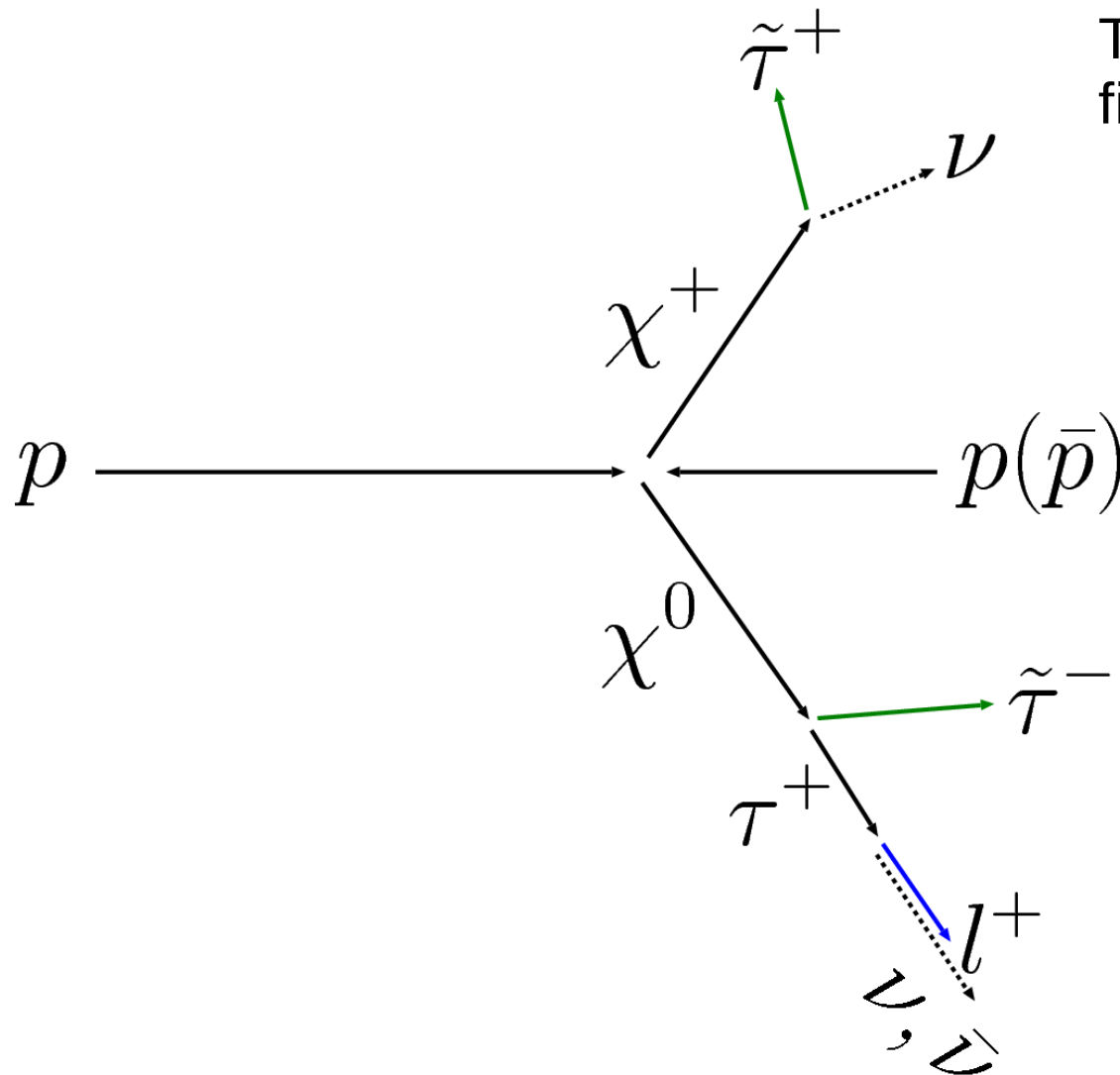
Sensitivity to the mixing angle is $O(0.1)$.

This can be **better** than $\tau \rightarrow \mu\gamma$ decay



Chargino-neutralino production with long-lived stau

With long-lived staus in the final state, we can do detailed studies of exclusive processes at hadron colliders just like at a [Linear Collider](#)!



This process has a [purely leptonic](#) final state. Clean!

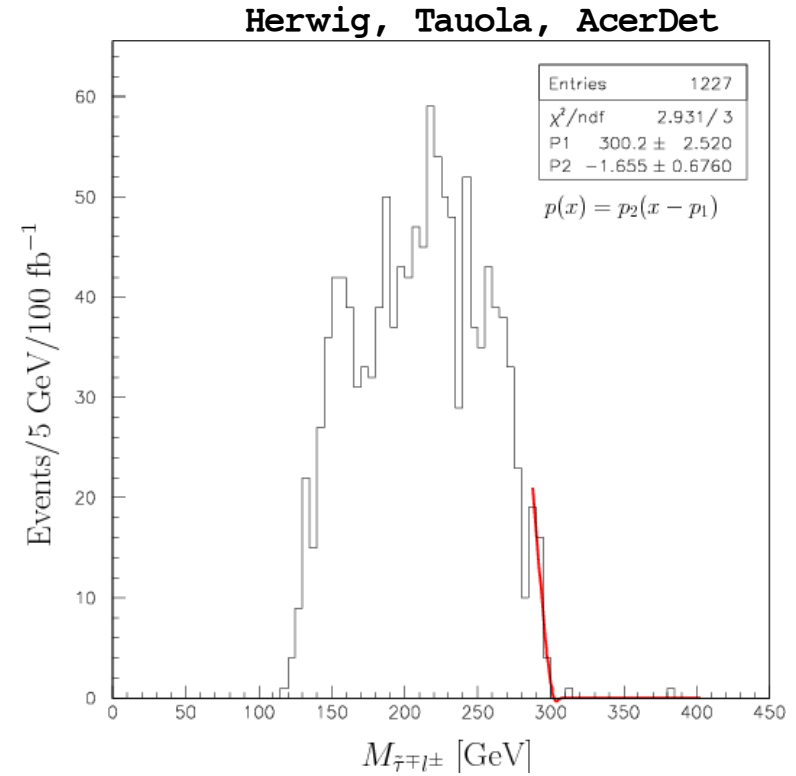
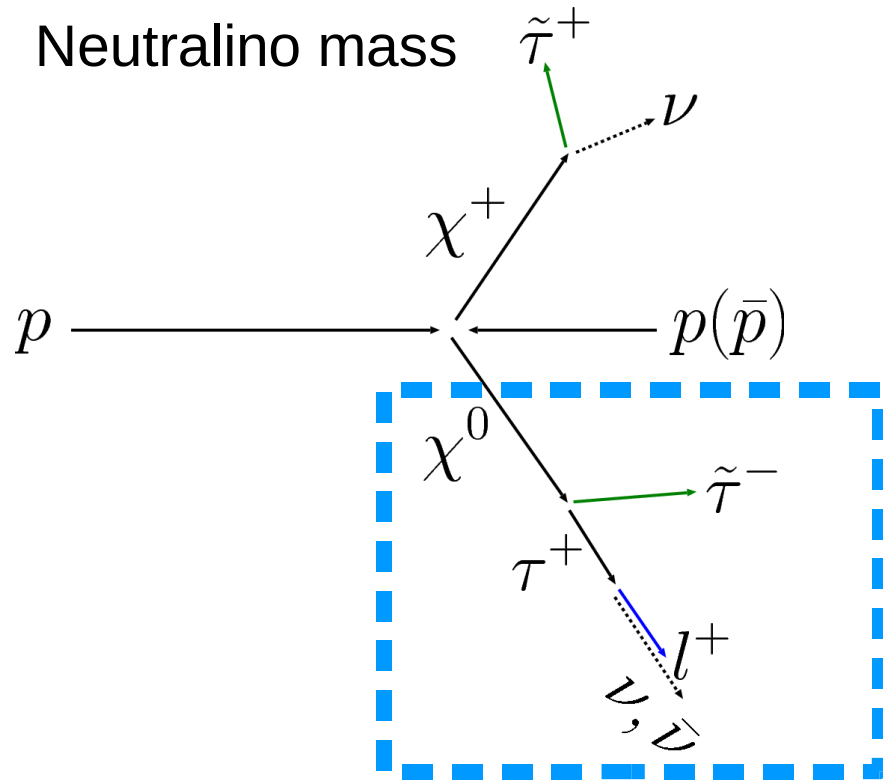
If we know the neutralino and chargino masses, we can [fully reconstruct](#) the event up to a two-fold ambiguity.

We can do many things!

- * mass measurements
- * spin measurements
- * P violation measurements
- * CP violation measurements

They are going to be [excellent tests of supersymmetry](#)!!!

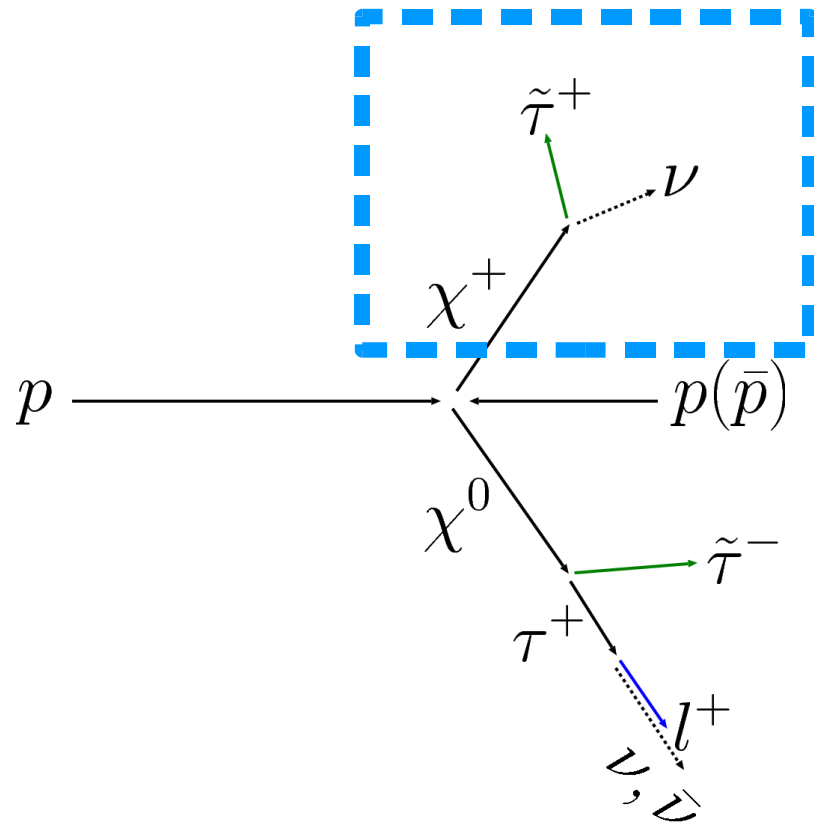
Mass measurements



$\delta M = 3 \text{ GeV}$

(Pure Higgsino model with $\mu = 300 \text{ GeV}$
and right-handed $m(\text{stau}) = 109 \text{ GeV}$)

Chargino mass



Once we know the neutralino mass, we know the rescaling factor of the lepton momentum.

$$z_l \equiv \frac{E_l}{E_\tau}, \quad \left(P_{\tilde{\tau}^-} + \frac{P_l}{z_l} \right)^2 = m_{\chi^0}^2$$

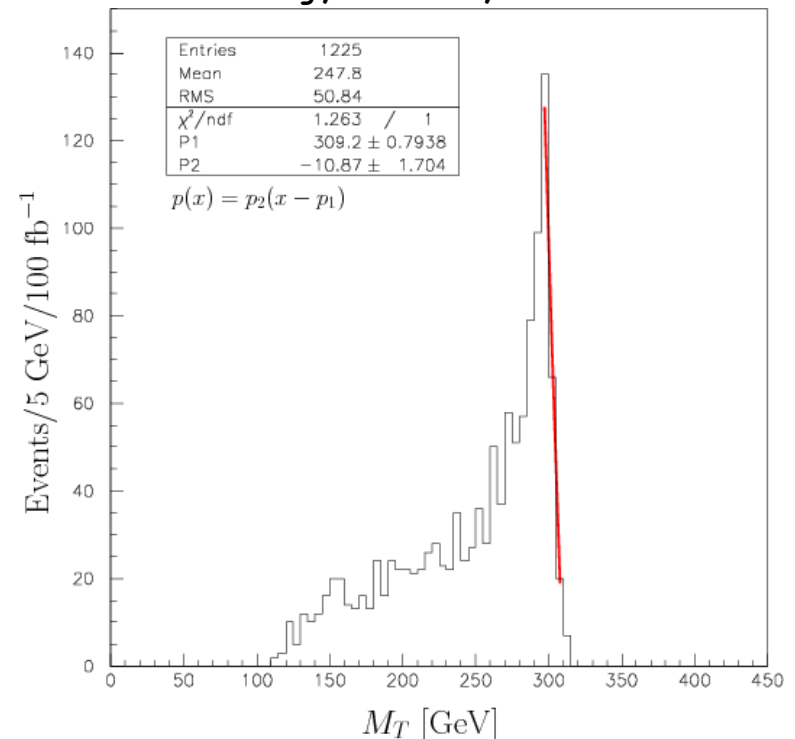
→ Transverse momentum of the **neutrino** from the chargino decay **can be solved**.

→ Transverse mass

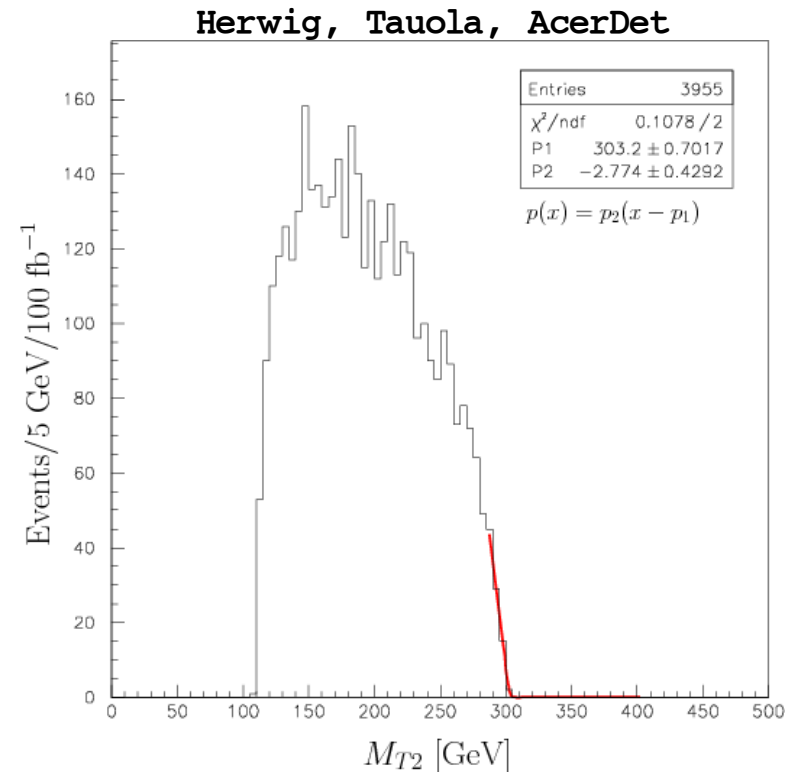
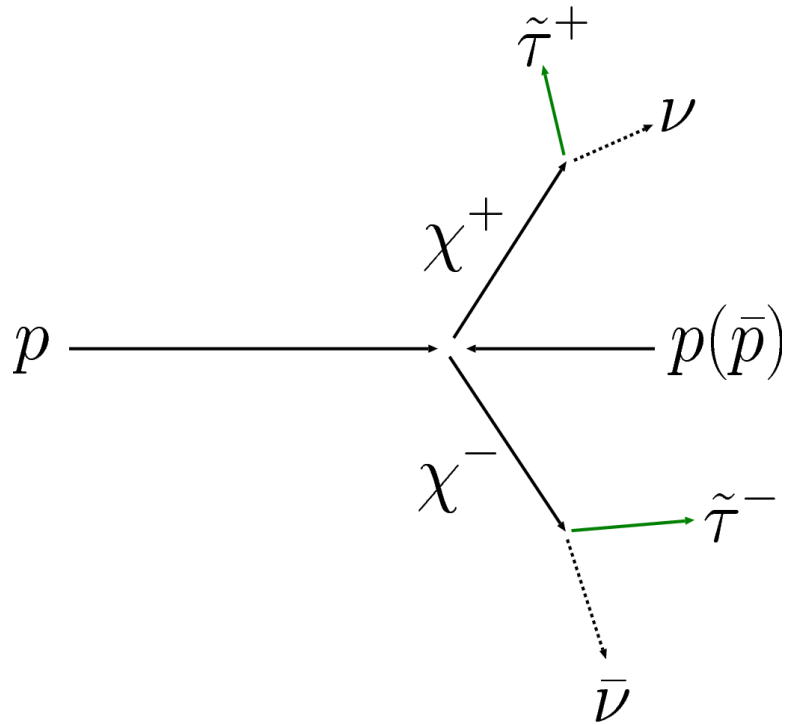
$$\delta M = 0.8 \text{ GeV}$$

(although it will depend on the resolution of the missing momentum measurement.)

Herwig, Tauola, AcerDet



By the way, the chargino mass can also be measured by using chargino-pair production events.

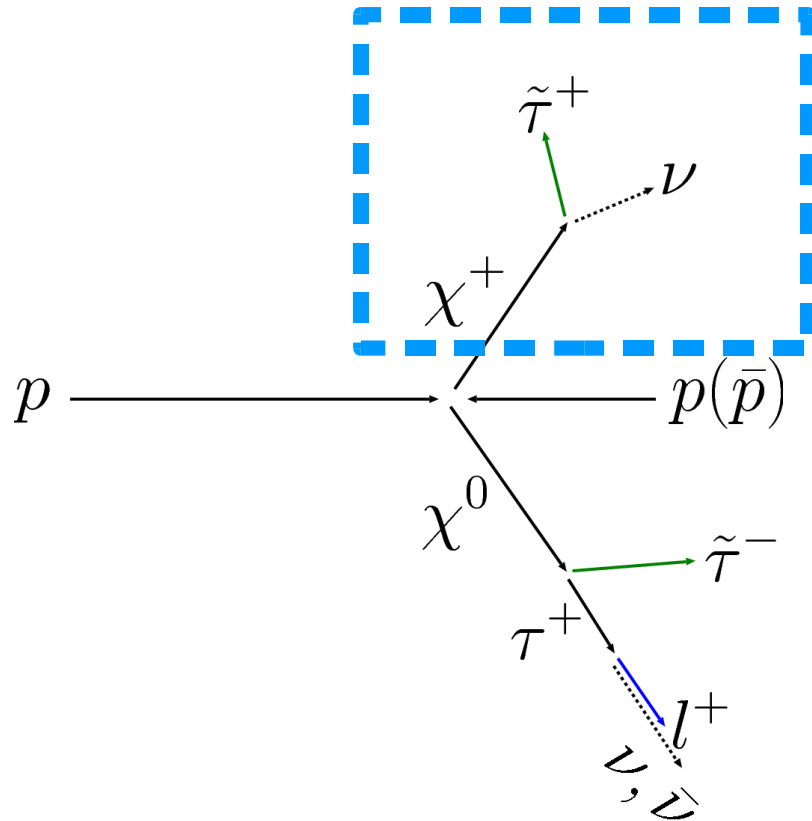


The M_{T2} variable can be used for this process.

[Lester, Summers '99]

This method directly measures the chargino mass.

Now with the knowledge of the chargino mass, **z-direction of the neutrino momentum** from the chargino decay can be solved:



$$(P_{\tilde{\tau}^+} + P_{\nu})^2 = m_{\chi^+}^2$$

Unfortunately, we have **two solutions** to this equation.

But anyway, we can **fully reconstruct** the event **up to a two-fold ambiguity** once the neutralino and chargino masses are known.

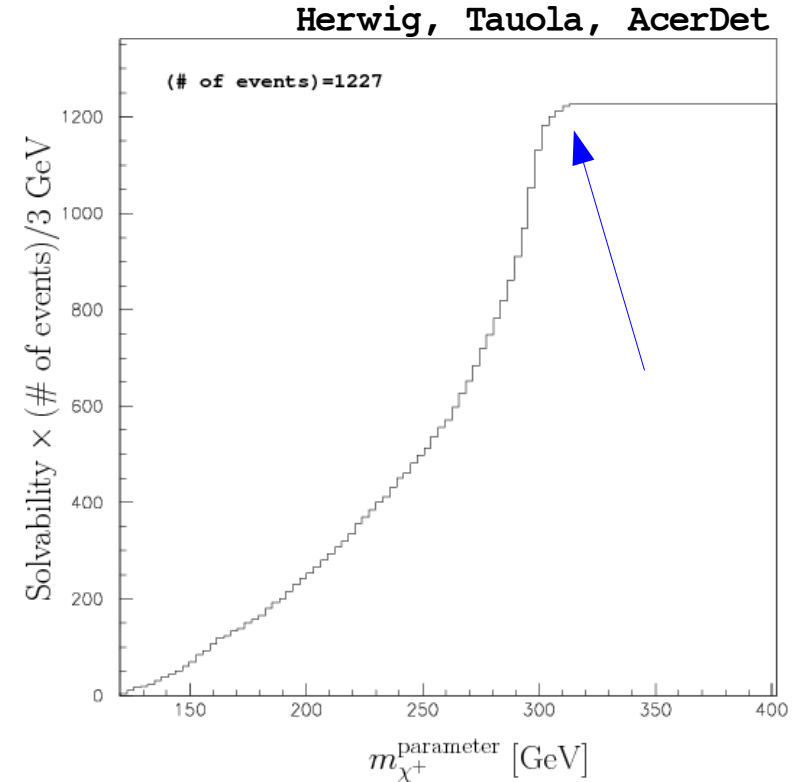
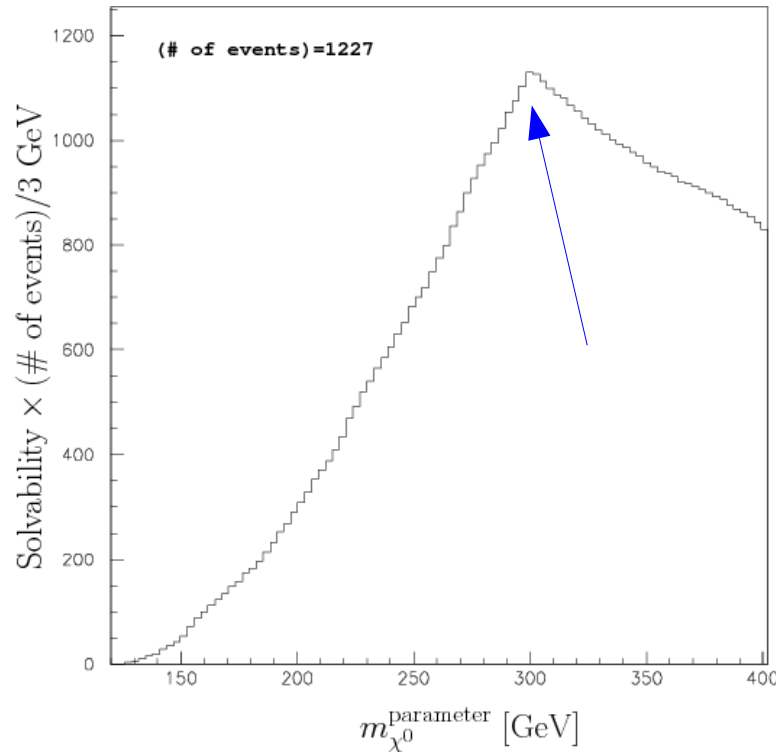
In this situation, we can do mass measurement in a more direct method.

Solvability analysis for neutralino and chargino masses

[Kawagoe, Nojiri, Polsello '04]

[Davis et al, (CMS collaboration) '06]

[Cheng, Gunion, Han, Marandella, McElrath '07]



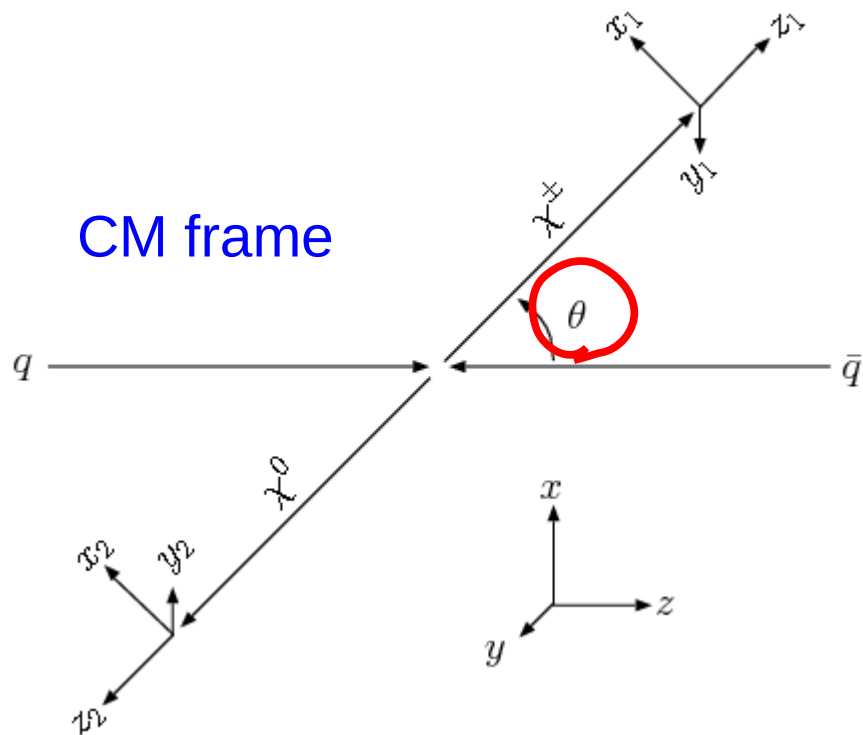
Try to solve kinematics with various input masses. Solvability is defined as the probability to give a physical solution, i.e., $P_z(v)$ is a real number and $0 < z_l < 1$.

By looking for a **peak** or a **point where solvability saturates**, we can get masses.

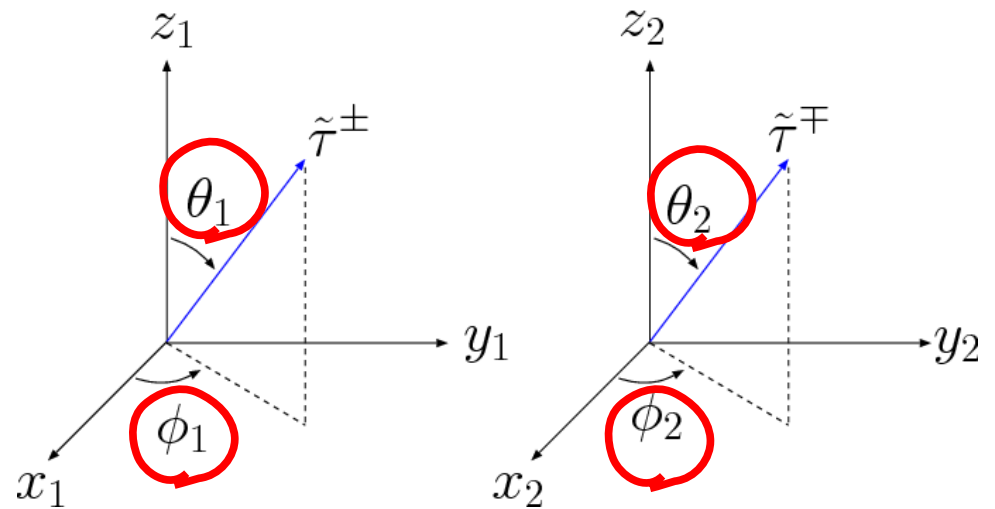
$\delta M \sim$ a few GeV.

Various distributions

Define kinematic variables



Rest frame of chargino



Rest frame of neutralino

Lepton energy fraction in leptonic tau decay

$$z_l \equiv \frac{E_l}{E_\tau}, \quad 0 \leq z_l \leq 1$$

There are six kinematic variables.

The cross section formula

The formula is pretty simple.

$$d\sigma \propto \frac{d \cos \theta}{2} \frac{d\Omega_1}{4\pi} \frac{d\Omega_2}{4\pi} dz_l \sum_{a,b=0}^3 \underbrace{D_A^a(\theta_1, \phi_1)}_{\text{chargino decay}} \rho^{ab}(\theta) \underbrace{\widetilde{D}_B^b(\theta_2, \phi_2, z_l)}_{\text{neutralino decay}}$$

chargino-neutralino production

$$\widetilde{D}_B^b(\theta_2, \phi_2, z_l) = \frac{1}{3}(1 - z_l) \left[(5 + 5z_l - 4z_l^2) D_B^b(\theta_2, \phi_2) - \underbrace{a_N}_{\text{spin summed part}} (1 + z_l - 8z_l^2) \delta^{b0} \right]$$

$$D_A^a = \begin{pmatrix} 1 \\ \pm \underbrace{a_C}_{\text{spin dependent part}} \sin \theta_1 \cos \phi_1 \\ \pm \underbrace{a_C}_{\text{spin dependent part}} \sin \theta_1 \sin \phi_1 \\ \pm \underbrace{a_C}_{\text{spin dependent part}} \cos \theta_1 \end{pmatrix}, \quad D_B^b = \begin{pmatrix} 1 \\ \mp \underbrace{a_N}_{\text{spin dependent part}} \sin \theta_2 \cos \phi_2 \\ \mp \underbrace{a_N}_{\text{spin dependent part}} \sin \theta_2 \sin \phi_2 \\ \mp \underbrace{a_N}_{\text{spin dependent part}} \cos \theta_2 \end{pmatrix}$$

$$\rho^{ab}(\theta) = \dots \quad \leftarrow \text{All the components are non-vanishing.}$$

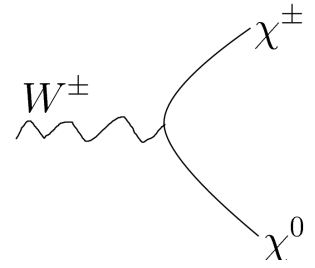
a_C and a_N are **parity asymmetry parameter** ($-1 < a < 1$) in the chargino decay and the neutralino decay, respectively. Non-trivial angular distribution measures parity violation.

$a_C=1$ because neutrino has always the left-handed chirality (maximal parity violation).

Lagrangian and asymmetry parameters

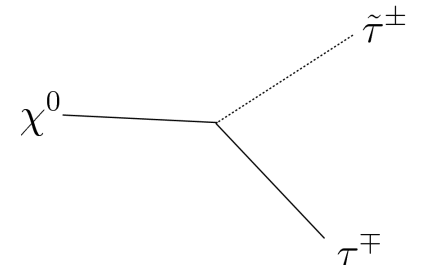
* Chargino-neutralino production:

$$\mathcal{L}_W = \bar{\chi}^0 \gamma^\mu (w_L P_L + w_R P_R) \chi^- W_\mu^+ + \text{h.c.}$$



* neutralino decay:

$$\mathcal{L}_{\chi^0} = \bar{\chi}^0 (n_R P_R + n_L P_L) \tau \tilde{\tau}^\dagger + \text{h.c.}$$



$$a_N \equiv \frac{|n_L|^2 - |n_R|^2}{|n_L|^2 + |n_R|^2}$$

← Parity violation in neutralino decay

$$a_W \equiv \frac{|w_L|^2 - |w_R|^2}{|w_L|^2 + |w_R|^2}$$

Parity violation in production

$$\xi_W \equiv \frac{2\text{Re}[w_L^* w_R]}{|w_L|^2 + |w_R|^2}$$

$$\eta_W \equiv \frac{2\text{Im}[w_L^* w_R]}{|w_L|^2 + |w_R|^2}$$

CP violation in production

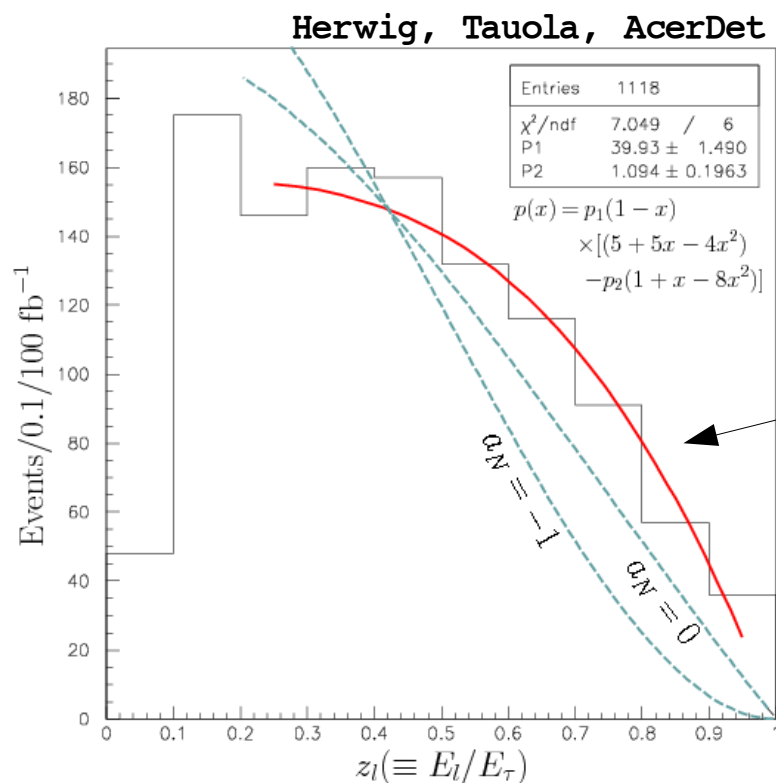
z_l distribution

z_l is a simple observable since it is a **boost invariant** quantity. We can measure it in the lab frame. There is **no two-fold ambiguity**.

$$d\sigma \propto \frac{1}{3}(1 - z_l) \left[(5 + 5z_l - 4z_l^2) - a_N(1 + z_l - 8z_l^2) \right] dz_l$$

This is a well-known distribution of the polarized tau decay. [Bullock, Hagiwara, Martin '93]
This is true for both $\chi+\chi_0$ and $\chi-\chi_0$ productions.

Again, in the **pure Higgsino** with **right-handed stau** model,



τ is left-handed

Theory value is $a_N=1$. We can distinguish from other models.

$$a_N = 1.1 \pm 0.2$$

In general, this parameter has information on the **LR mixing of the stau** and the **gaugino/higgsino mixing**.

Polar angle distributions

Again, the same formula for both $\chi+\chi_0$ and $\chi-\chi_0$ productions.

$$d\sigma \propto \left[1 + \underbrace{a_W}_{\text{red wavy}} \langle f_1(\beta_A, \beta_B) \rangle \cos \theta_1 + \underbrace{a_W a_N}_{\text{red wavy}} \langle f_1(\beta_B, \beta_A) \rangle \cos \theta_2 + \underbrace{a_N}_{\text{red wavy}} \langle f_2(\beta_A, \beta_B) \rangle \cos \theta_1 \cos \theta_2 \right] \frac{d \cos \theta_1}{2} \frac{d \cos \theta_2}{2}$$

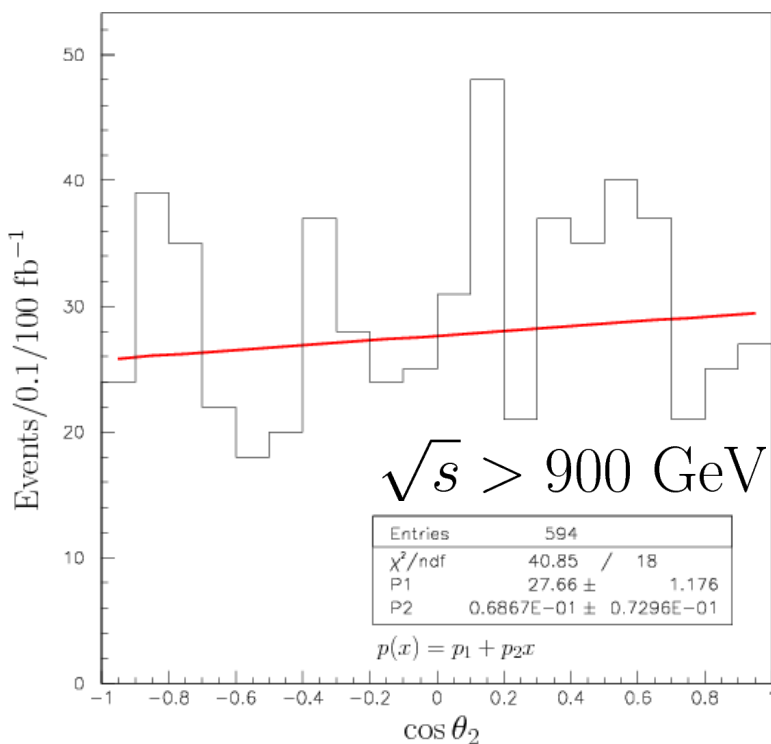
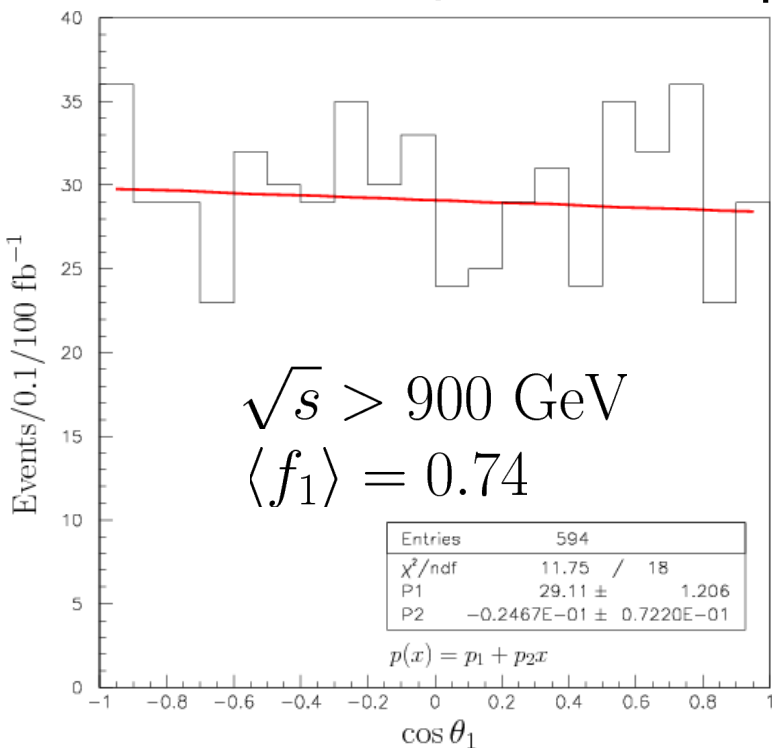
$$0 < f_1 < 1$$

Threshold production

Boosted production

$$1/3 < f_2 < 1$$

Boosted production
Threshold production



Theoretical value:

$$a_W = 0$$

► Flat distribution

False solutions are under control. Those are randomly distributed.

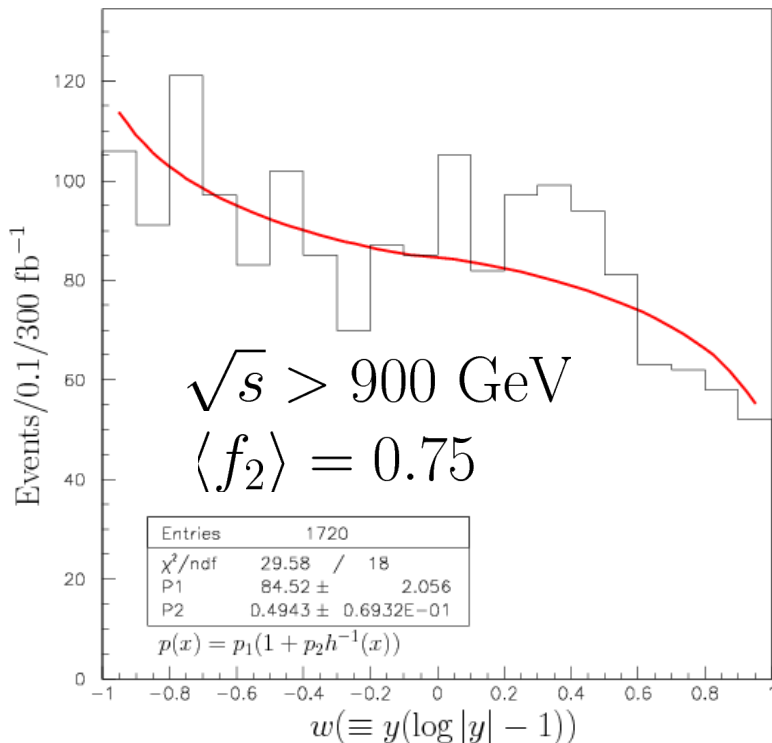
Angle-angle correlation

The $\cos\theta_1\cos\theta_2$ term gives a non-trivial correlation even if $a_W=0$.

By defining a variable:

$$w = h(y) \equiv y(\log y - 1) \quad y \equiv \cos \theta_1 \cos \theta_2$$

$$\rightarrow d\sigma \propto (1 + \underbrace{a_N}_{\text{red wavy}} \langle f_2 \rangle h^{-1}(w)) dw$$



Deviation from the flat distribution is a sign of **parity violation** and the **spin-spin correlation**.

The non-trivial distribution is diluted by false solutions by about a factor of two.

Combining with the a_N measurement by $Z1$ distribution, this will be an interesting test of spins!

Azimuthal angle distributions

For recent discussion,
[Buckley, Murayama, Klemm, Rentala '07]

$$d\sigma \propto \left[1 \pm \frac{\pi^2}{16} \langle g_1(\beta_A, \beta_B) \rangle \cos \phi_1 \pm \frac{\pi^2}{16} \underbrace{\eta_W}_{\text{red wavy}} \langle g_2(\beta_A, \beta_B) \rangle \sin \phi_1 \right] \frac{d\phi_1}{2\pi}$$

$$d\sigma \propto \left[1 \mp \frac{\pi^2}{16} \underbrace{a_N}_{\text{red wavy}} \langle g_1(\beta_B, \beta_A) \rangle \cos \phi_2 \mp \frac{\pi^2}{16} \underbrace{a_N \eta_W}_{\text{red wavy}} \langle g_2(\beta_B, \beta_A) \rangle \sin \phi_2 \right] \frac{d\phi_2}{2\pi}$$

$\sin\phi$ term measures **CP (or T)** violation.

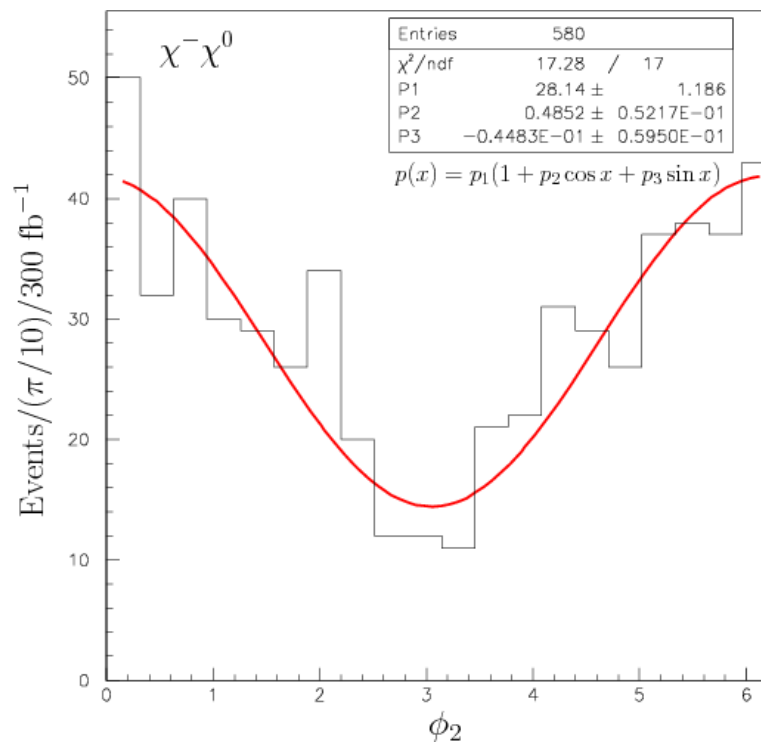
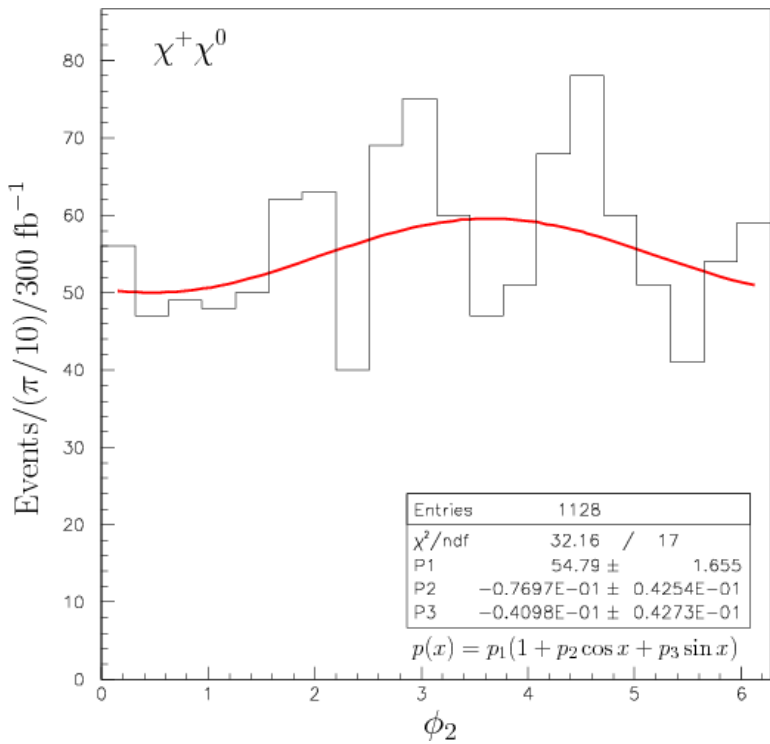
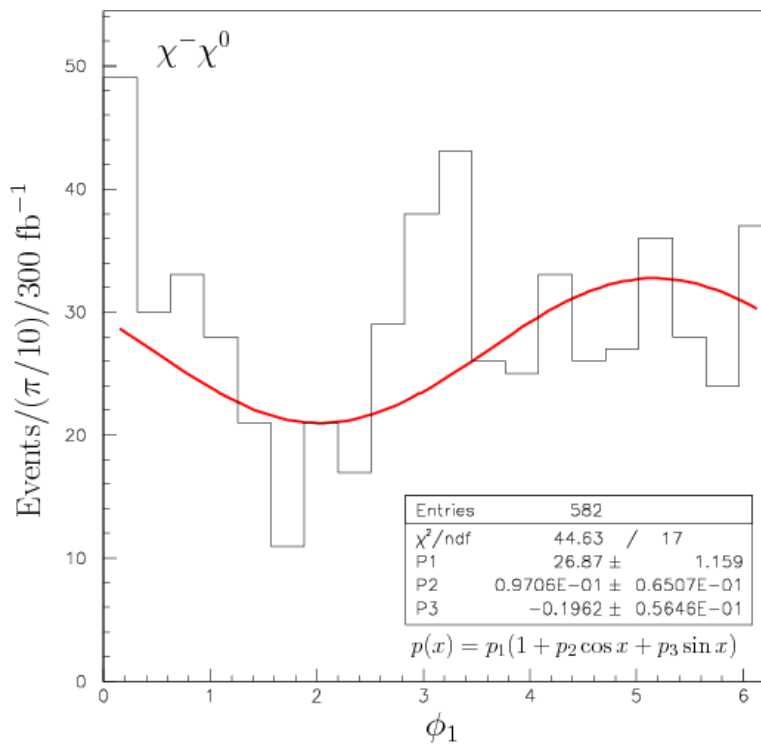
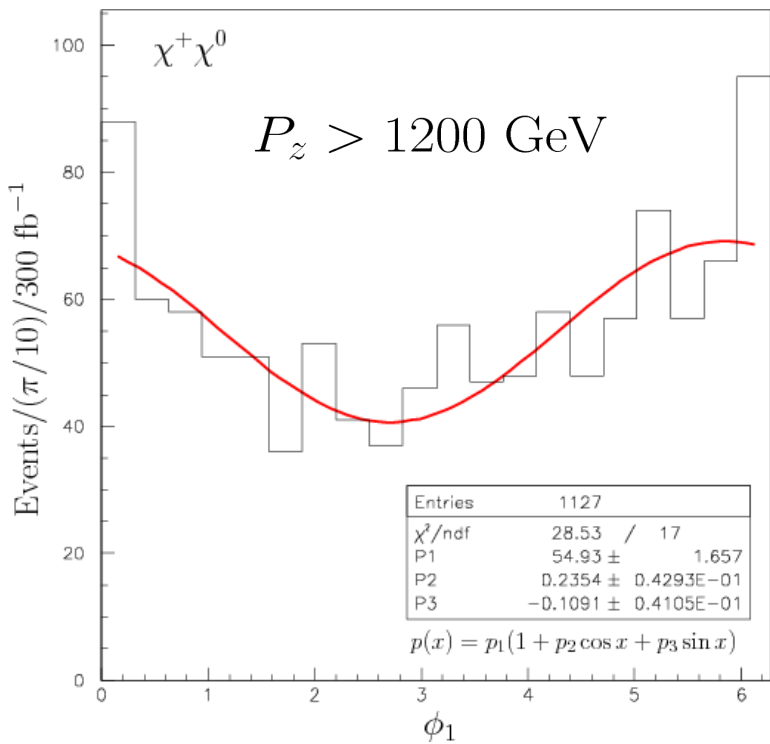
Signs of the coefficients are opposite for $\chi+\chi_0$ and $\chi-\chi_0$ productions.

Effective polarization of the beam through the W-quark interaction and the **parity violation in the decays** make the distribution possible.

We need to know the **direction of the initial (anti-)quark** to define the azimuthal angle. (we know it only statistically at the LHC.)

$0 < g_1 < 1$ \leftarrow **threshold** production
boosted production

$0 < g_2 < 0.31 \leftarrow \beta \sim 0.77$
Boosted and **threshold** production



Theoretical input:

$$\eta_{W=0}$$

Qualitatively OK.

One can eliminate (or understand) the fake distribution by using events with different charges.

$$\frac{\pi^2}{16} \langle g_1 \rangle = 0.51$$

$$\frac{\pi^2}{16} \langle g_2 \rangle = 0.16$$

Summary

- * In the long-lived stau scenario, it is possible to perform a detailed analysis of **exclusive processes**.
- * Masses of superparticles (not the mass differences) can be measured with a good accuracy.
- * Chargino-neutralino production is a good process to **test** supersymmetry.
- * **P and CP (or T) violation** can be measured. We can learn about model parameters such as gaugino/higgsino mixing and left-right mixing.
- * Study of neutralino-pair production will also be important.