

Collider searches for neutralino dark matter in relic-density-consistent SUSY models without gaugino mass universality

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in collaboration with

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Neutralino dark matter

- Dark Matter should be non-baryonic (no candidate in the SM), non-relativistic (cold), stable(or long-lived), weakly (or super-weakly) interacting matter
 - From the WMAP results, the cold dark matter density of the universe is $\Omega_{CDM}h^2 = 0.111_{-0.015}^{+0.011}$: (upper bound is a tight constraint on SUSY models containing DM candidates : DM may consist of several components)
 - In SUSY models with R -parity conservation
 - \Rightarrow the Lightest Supersymmetric Particle(LSP) is stable
 - \Rightarrow lightest neutralino \tilde{Z}_1 is the LSP in most of MSSM parameter space
 - $\Rightarrow \tilde{Z}_1$ is good candidate for Cold Dark Matter (CDM)
 - $\tilde{z}_1 = v_1^{(1)}\psi_{h_u^0} + v_2^{(1)}\psi_{h_d^0} + v_3^{(1)}\lambda_3 + v_4^{(1)}\lambda_0$
- Here, $R_{\tilde{w}} = |v_3^{(1)}|$, $R_{\tilde{B}} = |v_4^{(1)}|$ and $R_{\tilde{H}} = \sqrt{|v_1^{(1)}|^2 + |v_2^{(1)}|^2}$: W -ino, B -ino and Higgsino
- Number density is governed by Boltzmann equation,

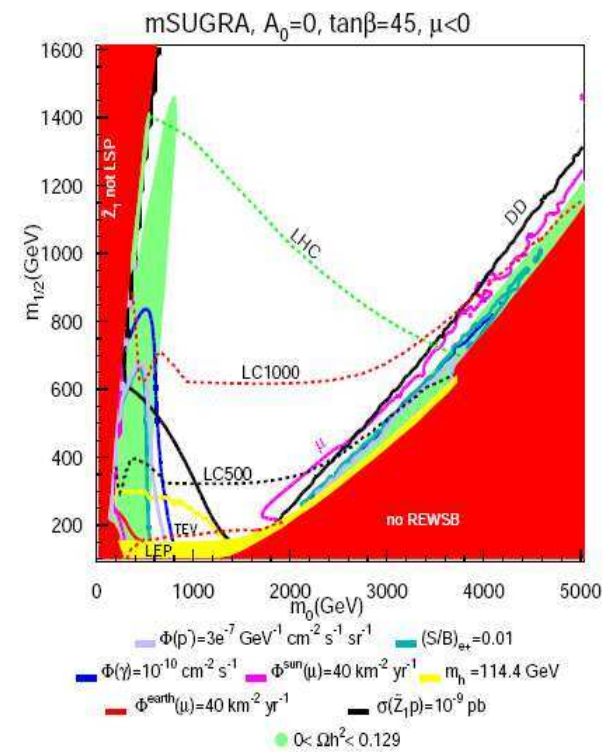
$$dn/dt = -3Hn - \langle\sigma v_{rel}\rangle(n^2 - n_0^2)$$
 - \Rightarrow requires evaluating many thousands Feynman diagrams
 - \Rightarrow high (co-)annihilation cross section implies low relic abundance

We assume,

- MSSM is an effective theory between the weak and GUT scale
- R -parity is conserved
- Neutralino LSP
- (near)degeneracy of first and second generation of SSB sfermions \rightarrow FCNC suppressed
- CP-violating phases in SSB suppressed \rightarrow CP contribution of SUSY is small

Review of mSUGRA

- **Parameter space : universal Soft Susy**
Breaking terms at $Q = M_{GUT}$
 $m_0, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
- **WMAP allowed Regions in m_0 - $m_{1/2}$ space**
 1. **$\tilde{\tau}$ co-annihilation region** at low $m_0, m_{\tilde{\tau}_1} \sim m_{\tilde{Z}_1}$
 2. **bulk region** at low m_0 and $m_{1/2}$, light sleptons (LEP2 excluded)
 3. **Higgs-funnel H, A resonance** ($2m_{\tilde{Z}_1} \simeq m_{A,H}$) at large $\tan\beta \sim 50$ or h -resonance at low $m_{1/2}$ ($2m_{\tilde{Z}_1} \simeq m_h$)
 4. **FP/HB region** at large m_0 , low $\mu \rightarrow$ mixed higgsino dark matter (MHDM)
 - ★ Region 1, 2, 3 \rightarrow Bino-like LSP



H.Baer et al. JCAP0408 (2004) 005

Motivations for susy models without gaugino mass universality

- **Limitation of mSUGRA**

- ★ all relic-density-consistent regions in mSUGRA are near the edges of theoretically (or LEP2 experiment) excluded regions
- ★ need to examine how already drawn conclusions from the mSUGRA model are affected by relaxing the universality assumptions
- ★ within R -parity conserved neutralino dark matter assumption, WMAP value provides a strong constraint reducing model parameter space by one unit

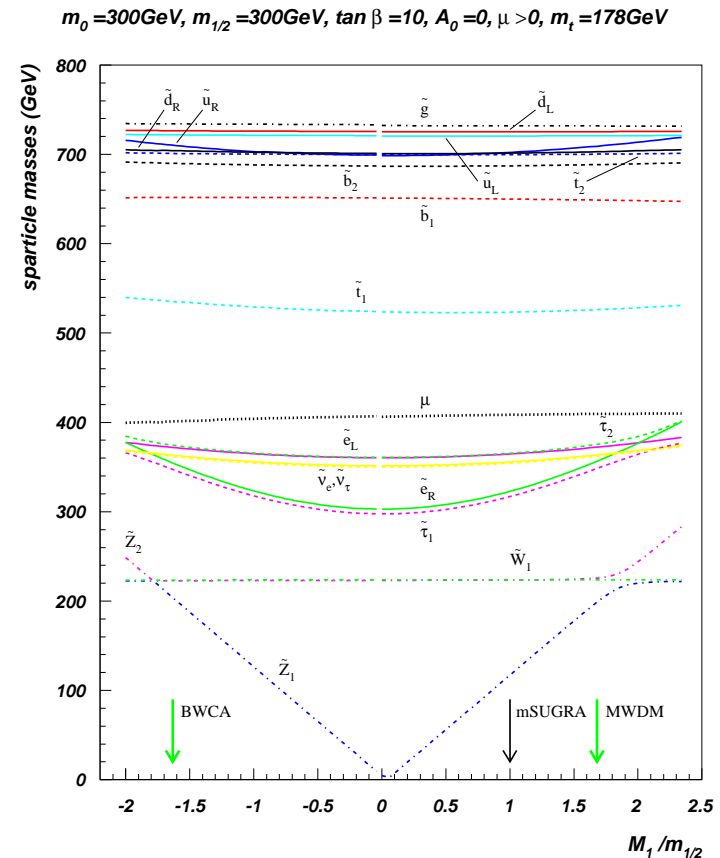
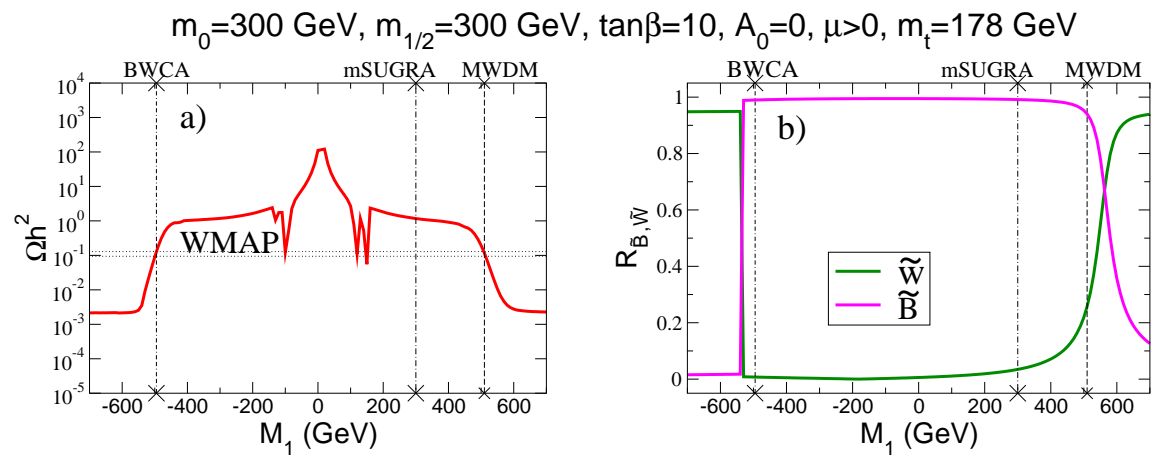
- **Motivation for non-universal gaugino mass models**

- non-minimal f_{AB} in SUGRA models,
e.g. $f_{AB} \ni 1, 24, 75, 200$ in $SU(5)$ SUSY GUTs
- various string models, e.g. KKLT model
- extra-dim SUSY GUTs with gaugino mediated SUSY breaking,
e.g. Dermisek-Mafi $SO(10)$ model

Non-universal gaugino mass models

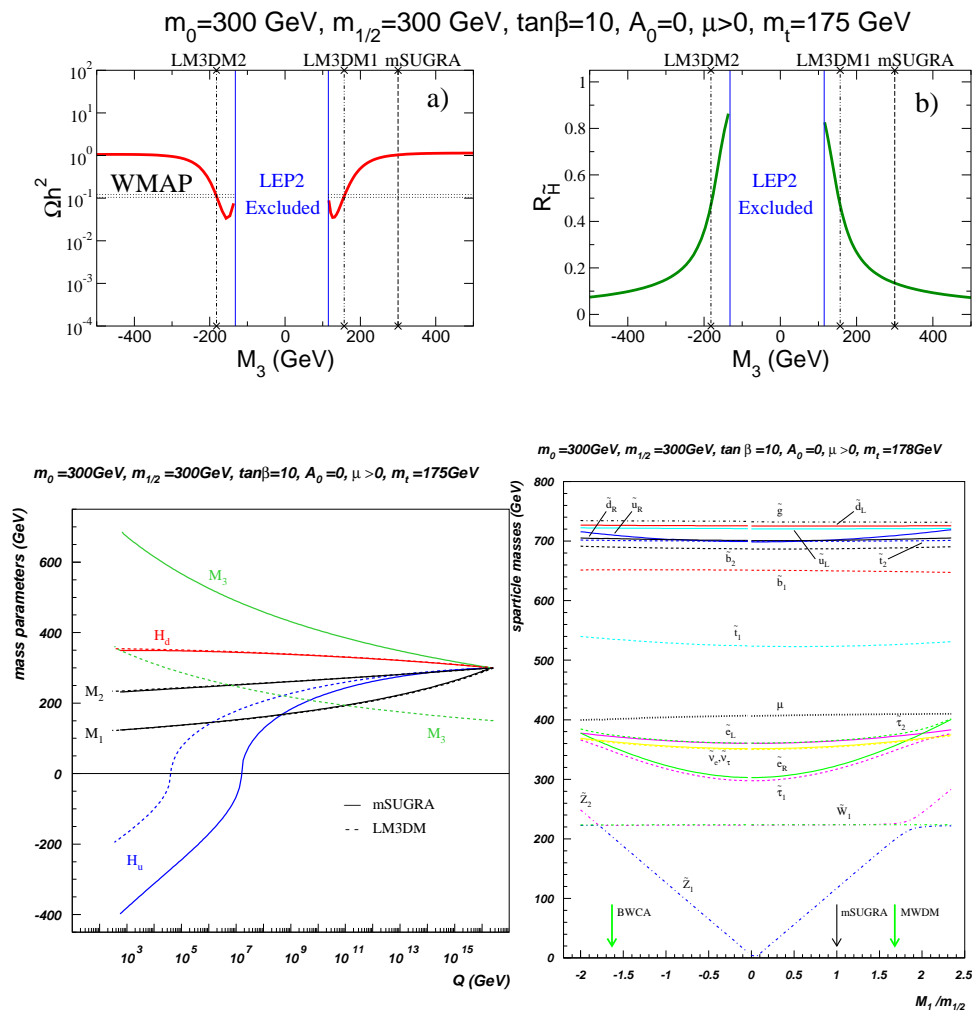
- **Relic-density-consistent** models obtained by adjusting
 - composition of neutralino (**WTN**: Well-Tempered Neutralino*)
 - masses of neutralino or other sparticles *:Arkani-Hamed et al. Nucl.Phys.B741, 108, 2006
- **mixed wino dark matter (MWDM1, MWDM2)**:
 $m_0, M_1(\text{or } M_2), m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
 - by increasing the wino content of the LSP by reducing the ratio M_2/M_1
 - $M_1 \neq M_2 = M_3 = m_{1/2}$ or $M_2 \neq M_1 = M_3 = m_{1/2}$
- **bino-wino co-annihilation Scenario (BWCA1, BWCA2)**:
 same as MWDM but M_1 and M_2 are in opposite sign
 - by allowing co-annihilation between high bino-like and wino-like states
- **low $|M_3|$ dark matter: compressed SUSY (LM3DM)**:
 $m_0, M_3, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
 - by increasing the higgsino content of the LSP by decreasing the gluino mass
 - $M_3 \neq M_1 = M_2 = m_{1/2}$
- **high $|M_2|$ dark matter: left-right split SUSY (HM2DM)**:
 $m_0, M_2, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
 - by allowing large M_2 mass
 - $M_2 \gg M_1 = M_3 = m_{1/2}$

NUGM Models - MWDM, BWCA



- ★ As $|M_1|$ ($|M_2|$) increases (decreases) past its mSUGRA value,
 - \tilde{Z}_1 becomes wino-like (MWDM) or bino-like but $m_{\tilde{Z}_1} \sim m_{\tilde{W}_1}$ (BWCA)
 - relic density decreases
 - WMAP $\Omega_{CDM} h^2$ value is reached

NUGM Models - LM3DM



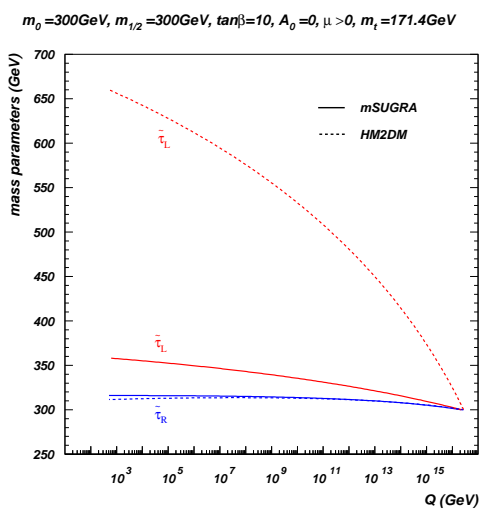
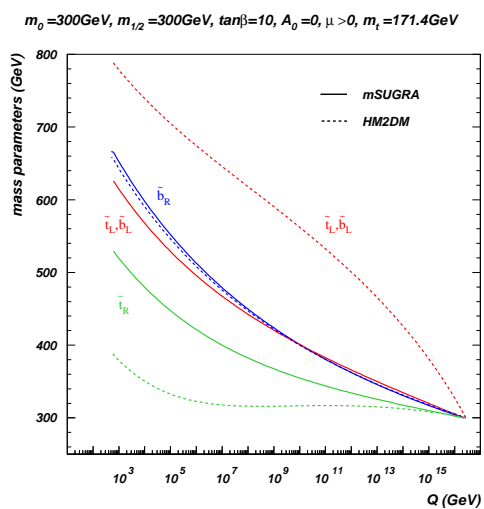
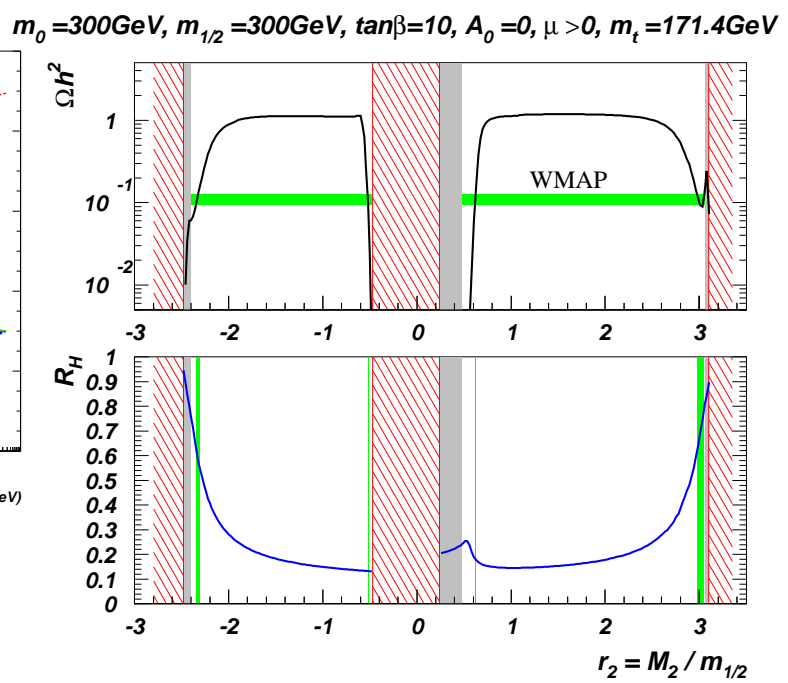
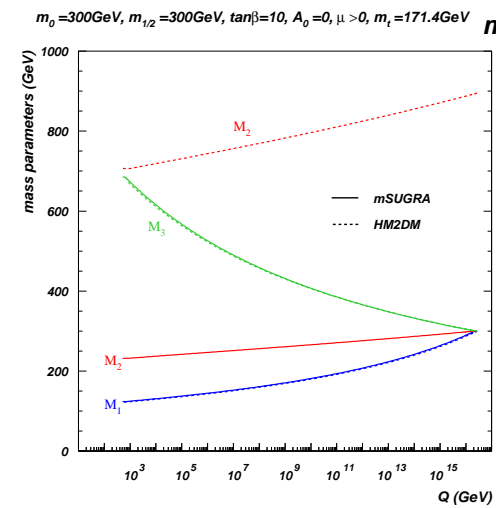
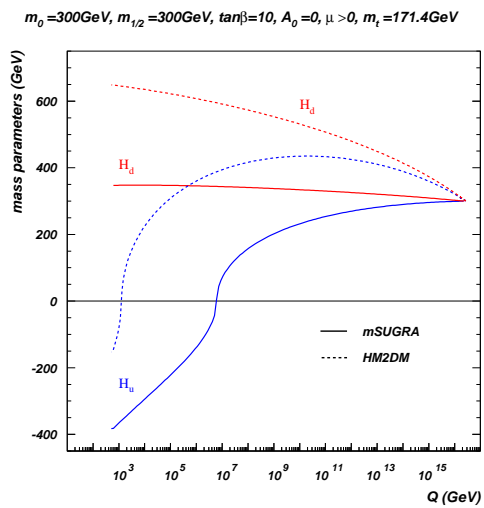
- Mild evolution of $m_{H_d}^2$ due to small Yukawa coupling f_b, f_τ
- Lighter squarks and gluinos \rightarrow reduced effect of f_t on $m_{H_u}^2$

\Rightarrow smaller μ

- $\frac{dm_{H_d}^2}{dt} \propto f_{b,\tau}^2 X_{b,\tau}, \frac{dm_{H_u}^2}{dt} \propto f_t^2 X_t$

- $$\mu^2 = \frac{m_{H_d}^2 - m_{H_u}^2 \tan\beta}{\tan^2\beta - 1} - \frac{M_Z^2}{2} \approx -m_{H_u}^2$$

NUGM Models - HM2DM



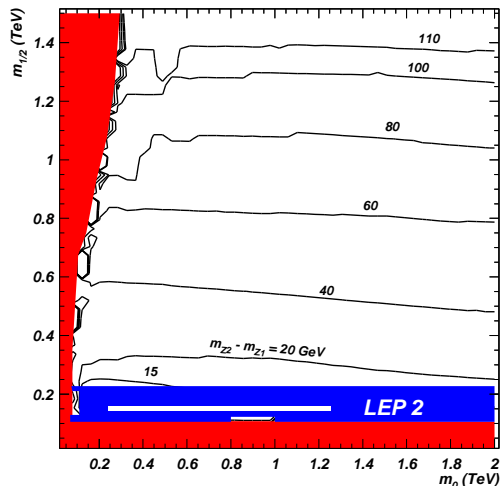
- large $M_2 \rightarrow$ reduced effect on $m_{H_u}^2$ at weak scale \rightarrow smaller $\mu \Rightarrow$ MHDM!
- large L-R splitting in squark and slepton sector

Benchmark Cases: $m_0, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu) = 300 \text{ GeV}, 300 \text{ GeV}, 0, 10, +1, m_t = 171.4 \text{ GeV}$

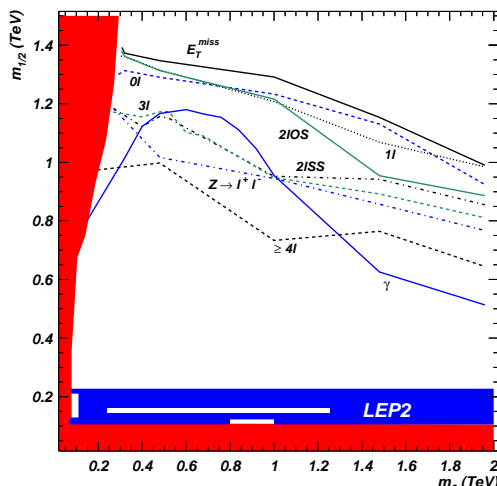
parameter	mSUGRA	MWDM	BWCA	LM3DM	HM2DM
special	—	$M_1(M_{GUT})$	$M_1(M_{GUT})$	$M_3(M_{GUT})$	$M_2(M_{GUT})$
value	—	490	-480	160	900
μ	385.1	385.9	376.6	185.3	134.8
$m_{\tilde{g}}$	729.7	729.9	731.7	420.2	736.4
$m_{\tilde{u}_L}$	720.8	721.2	722.0	496.9	901.8
$m_{\tilde{u}_R}$	702.7	708.9	709.9	467.0	696.3
$m_{\tilde{t}_1}$	523.4	526.5	536.3	312.2	394.3
$m_{\tilde{b}_1}$	656.8	656.0	658.9	443.2	686.4
$m_{\tilde{e}_L}$	364.5	371.5	371.4	366.1	669.3
$m_{\tilde{e}_R}$	322.3	353.3	352.2	322.6	321.3
$m_{\tilde{W}_2}$	411.7	412.4	404.5	282.9	719.7
$m_{\tilde{W}_1}$	220.7	220.8	220.0	152.5	136.5
$m_{\tilde{Z}_2}$	220.6	223.2	219.2	163.6	142.3
$m_{\tilde{Z}_1}$	119.2	194.6	201.7	105.5	94.8
m_A	520.3	525.9	518.6	398.3	670.7
m_{H^+}	529.8	535.3	528.1	408.7	679.8
m_h	110.1	110.2	109.8	106.0	111.9
$\Omega_{\tilde{Z}_1} h^2$	1.1	0.10	0.10	0.10	0.10
$\sigma_{SI}(\tilde{Z}_1 p)$	$2.1 \times 10^{-9} \text{ pb}$	$1.5 \times 10^{-8} \text{ pb}$	$3.1 \times 10^{-11} \text{ pb}$	$7.2 \times 10^{-8} \text{ pb}$	$3.4 \times 10^{-8} \text{ pb}$
$R_{\tilde{H}}$	0.15	0.25	0.16	0.50	0.67

Collider reaches in parameter space: BWCA

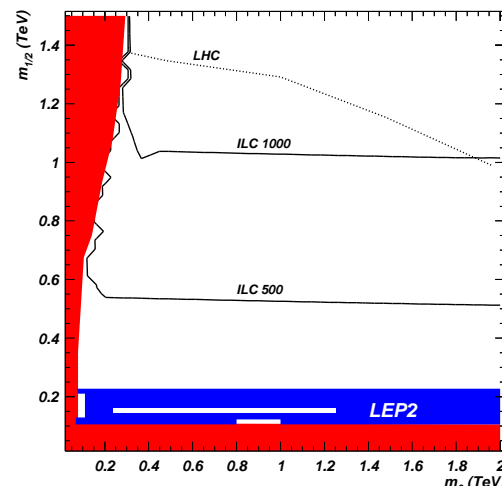
BWCA: $M_2 \neq m_{1/2}$, $\tan\beta=10$, $A_0=0$, $\mu>0$, $m_t=178$ GeV



BWCA: $M_2 \neq m_{1/2}$, $\tan\beta=10$, $A_0=0$, $\mu>0$, $m_t=178$ GeV



BWCA: $M_2 \neq m_{1/2}$, $\tan\beta=10$, $A_0=0$, $\mu>0$, $m_t=178$ GeV



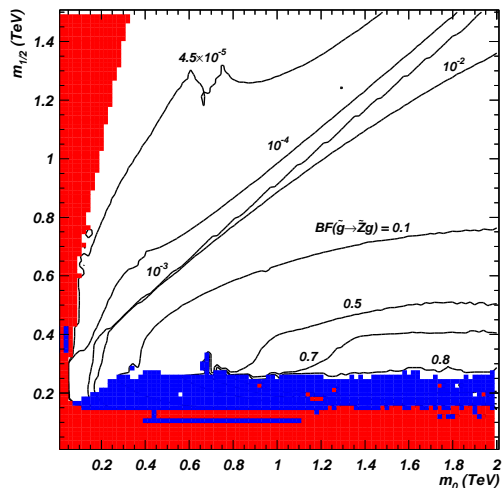
- $\tilde{Z}_2 - \tilde{Z}_1$ mass gap contour in $m_0 - m_{1/2}$ plane
- M_2 lowered at every point until $\Omega h^2 \rightarrow 0.11$
- Small $\tilde{Z}_2 - \tilde{Z}_1$ or $\tilde{W}_1 - \tilde{Z}_1$ mass gap $\Rightarrow \tilde{Z}_2 \rightarrow l\bar{l}\tilde{Z}_1 \Rightarrow m(l^+l^-)$ mass edges over all parameter space

- ISAJET event generator
- multijet + isolated leptons + E_T^{miss} signals in $m_0 - m_{1/2}$ plane (5σ for $100fb^{-1}$)
- $E_T^{miss} > 200GeV$, $p_T^{jet} > 40GeV$ ($n_{jet} > 2$), $p_T > 10GeV$ for muon $p_T > 20GeV$ for electron and photon, $|\eta| < 2.4$
- larger rate of isolated photon signal
refer [JHEP 0306 \(2003\) 054](#)

- LHC reach depends on gluino and squark mass
- ILC reach determined by kinematical accessibility of reactions $e^+e^- \rightarrow \tilde{W}_1\tilde{W}_1$ or $e^+e^- \rightarrow \tilde{l}^+\tilde{l}^-$
- $100fb^{-1}$ for both LHC and ILC
- ILC reach for $\sqrt{s} = 500$ GeV and 1000 GeV

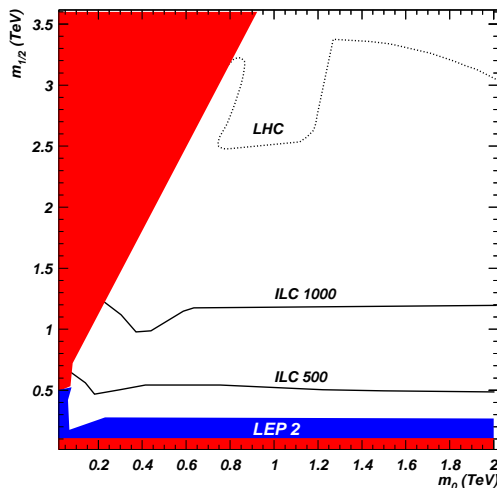
Collider reaches in parameter space: LM3DM

LM3DM: $M_3 \leq m_{1/2}$, $\tan\beta=10$, $A_0=0$, $\mu > 0$, $m_t=175$ GeV



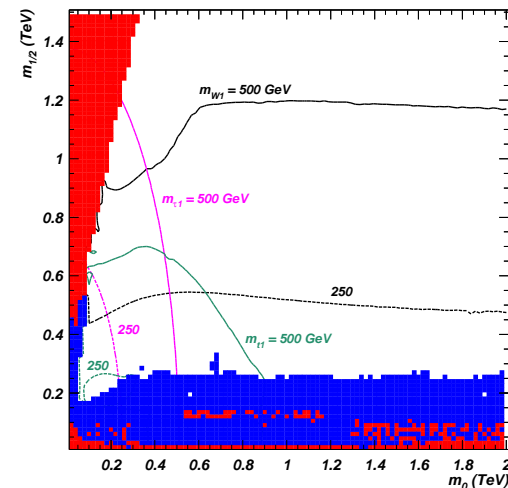
- Lighter gluinos expected in LM3DM \rightarrow larger pair production
- Heavy squarks at large m_0 and large higgsino component
- in lower right region, $\tilde{g} \rightarrow \tilde{Z}_i g$ are dominant

LM3DM: $M_3 \leq m_{1/2}$, $\tan\beta=10$, $A_0=0$, $\mu > 0$, $m_t=175$ GeV



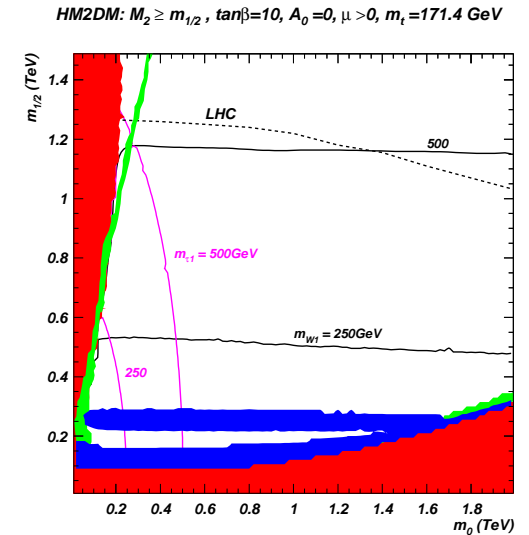
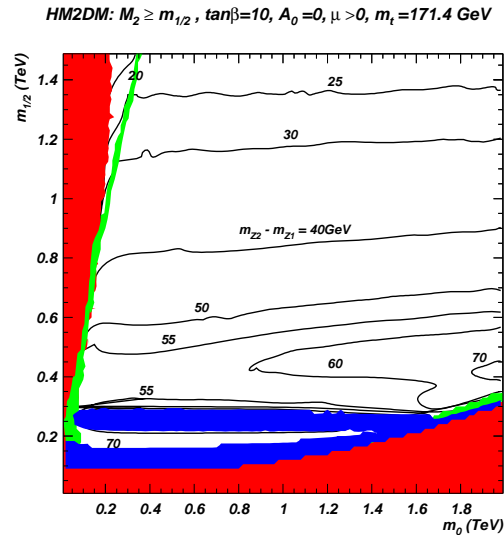
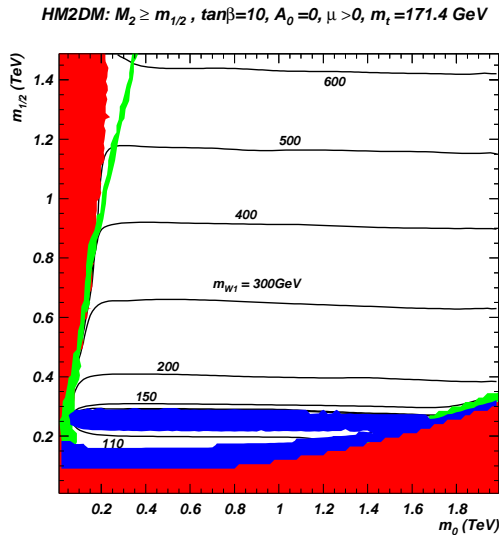
- Reduced squark and gluino masses \Rightarrow enhanced reach
- Small $\tilde{Z}_2 - \tilde{Z}_1$ or $\tilde{W}_1 - \tilde{Z}_1$ mass gap $\Rightarrow \tilde{Z}_2 \rightarrow l\bar{l}\tilde{Z}_1 \Rightarrow m(l^+l^-)$ mass edges over all parameter space

LM3DM: $M_3 \leq m_{1/2}$, $\tan\beta=10$, $A_0=0$, $\mu > 0$, $m_t=175$ GeV



- Enhanced $\tilde{W}_1^+ \tilde{W}_1^-$ production due to smaller μ
- Possible $\tilde{t}_1 \tilde{t}_1$ production
- All charginos and neutralinos accessible
- $\tilde{q} \rightarrow \tilde{g}q$ kinematically allowed \Rightarrow precise determination of \tilde{q} , \tilde{g} masses

Collider reaches in parameter space: HM2DM

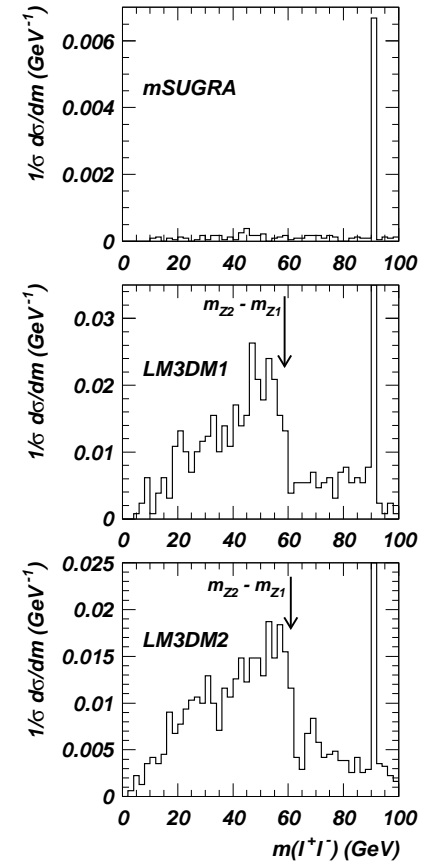
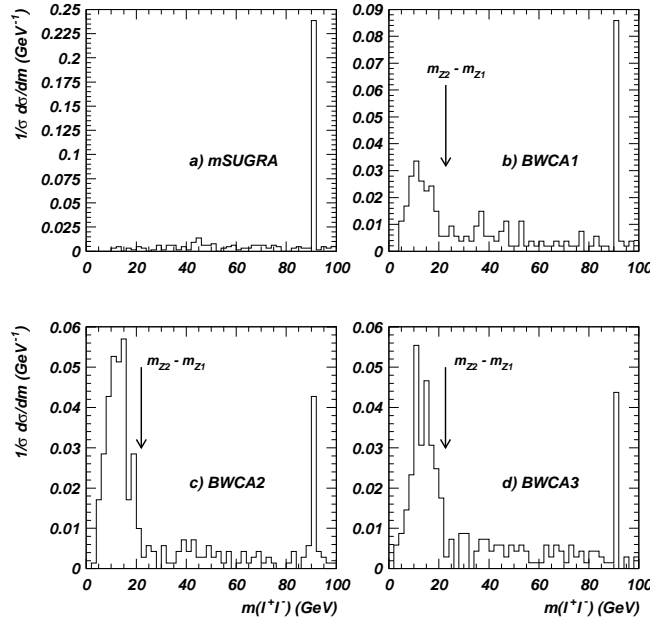
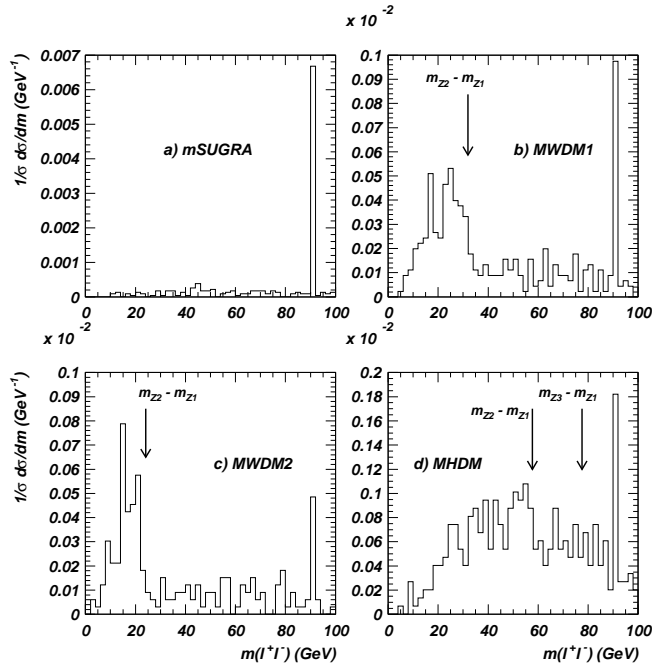


- $m_{\tilde{W}_1} \sim 1/2 m_{1/2}$, whereas $m_{\tilde{W}_1} \sim 3/2 m_{1/2}$ in mSUGRA
- relevant at ILC if $\tilde{W}_1 \tilde{W}_2$ production is possible
- mass gap is larger than 25 GeV and decreases with increasing $m_{1/2} \rightarrow$ distinguishable from other models
- LHC and ILC reaches in parameter space

SUSY signals at Colliders without non-universal gaugino masses

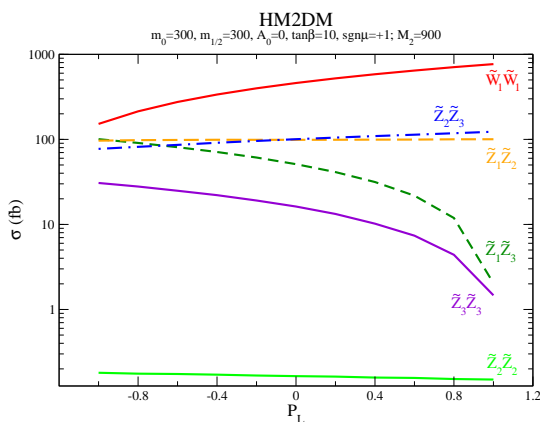
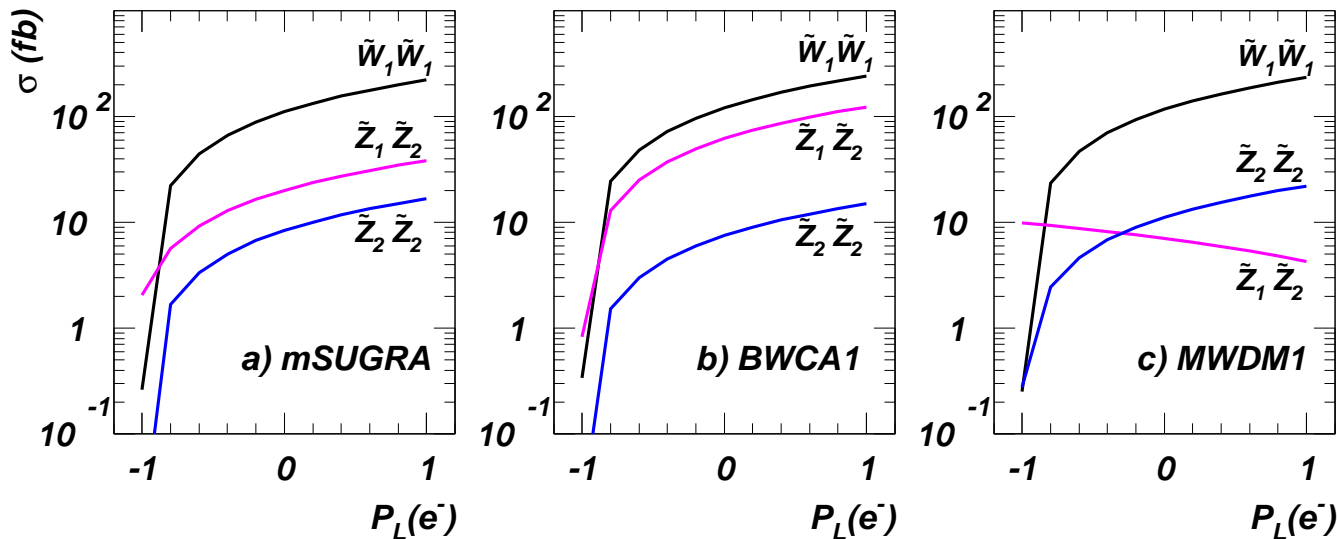
- CERN LHC and Fermilab Tevatron
 - If $\tilde{Z}_2 \longrightarrow \tilde{l}\bar{l}$, $\tilde{l}\bar{l} \longrightarrow \tilde{Z}_1\bar{l}l$ or $\tilde{Z}_2 \longrightarrow \tilde{Z}_1\bar{l}l$ are open ($l = e$ or μ)
 \implies good prospects for measuring the $\tilde{Z}_2 - \tilde{Z}_1$ mass gap at the CERN LHC and possibly at the Fermilab Tevatron
 - In the mSUGRA case, most of the parameter space has $m_{\tilde{Z}_2} - m_{\tilde{Z}_1} > 90$ GeV, \implies
 $\tilde{Z}_2 \longrightarrow \tilde{Z}_1 Z^0$ or $\tilde{Z}_1 h$ “spoiler” decays dominant
 - When the mass gap is much smaller
 - * spoiler decays are closed, 3-body decays are open
 - * $\bar{l}l$ mass edge always visible at LHC
- Linear e^+e^- collider(ILC)
 - $m_{\tilde{Z}_2}$, $m_{\tilde{W}_1}$ and $m_{\tilde{Z}_1}$ can be inferred from $\tilde{W}_1^+ \tilde{W}_1^- \longrightarrow \bar{l}\nu_l \tilde{Z}_1 + q\bar{q} \tilde{Z}_1$
 (dijet events)
 - $\tilde{W}_1^+ \tilde{W}_1^-$, $\tilde{Z}_1 \tilde{Z}_2$, $\tilde{Z}_2 \tilde{Z}_2$ production cross sections can be measured as a function of beam polarization
- **ISAJET program** (H. Baer, F.E. Paige, S.D. Protopopescu, and X. Tata)

Dilepton Distribution at LHC



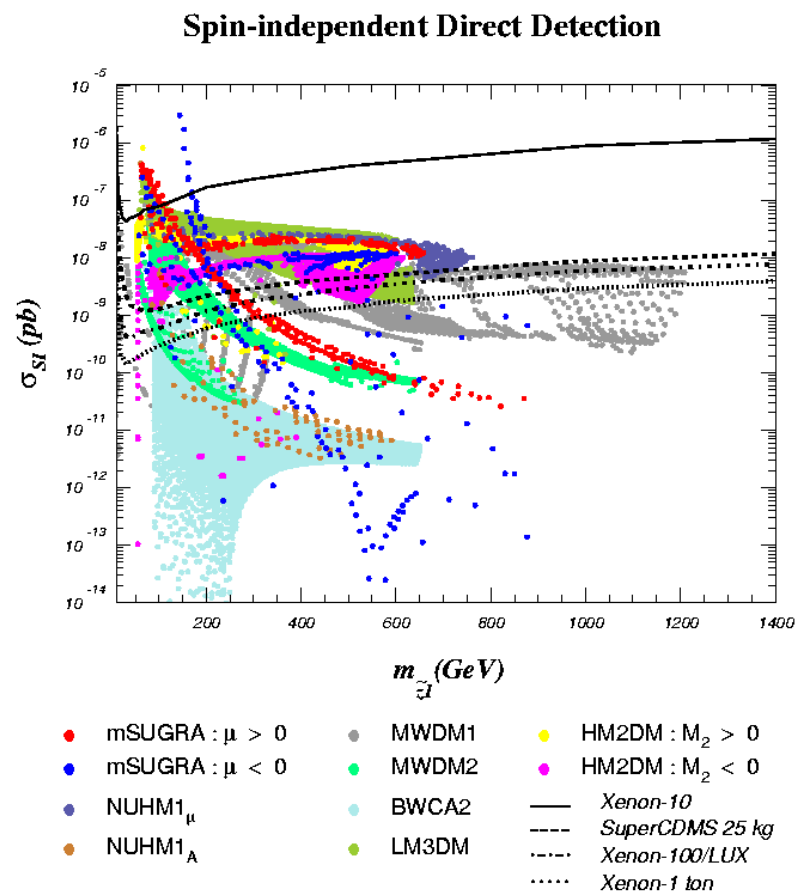
- ISAJET event generating program
- $E_T^{miss} > \max(100\text{GeV}, M_{eff})$, $E_T > 50\text{GeV}$ ($n_{jet} \geq 4$, hardest jet has $E_T > 100\text{GeV}$), $S_T > 0.2$, $M_{eff} > 800\text{GeV}$ LHC Point 5 from [PRD 55 \(1997\) 5520](#), [PRD 60 \(1999\) 095002](#)
- NUGM :
 Z^0 peak from $\tilde{Z}_3, \tilde{Z}_4, \tilde{W}_2$ decays + continuum distribution $m(l^+l^-) < m_{\tilde{Z}_2} - m_{\tilde{Z}_1}$

Cross Section for $\tilde{W}_1^+ \tilde{W}_1^-$ and $\tilde{Z}_i \tilde{Z}_j$ Production at ILC



- \tilde{W}_1 and \tilde{Z}_2 are mainly wino-like
 $\rightarrow \sigma(\tilde{W}_1 \tilde{W}_1)$ and $\sigma(\tilde{Z}_2 \tilde{Z}_2)$ are similar to one another
- $\tilde{Z}_1 \tilde{Z}_2$ process are quite different

Implications for direct dark matter detection



- models with **WTN** within reach of next generation of detectors
- models adjusted masses to get WMAP value below sensitivities of detectors

Conclusions

- Most of mSUGRA parameter space is excluded by WMAP bound
- New perspectives open with gaugino mass non-universalities in SUGRA
- If DM in nature is indeed composed of SUSY models with non-universal gaugino masses (MWDM($M_1 \sim M_2$), BWCA DM($M_1 \sim -M_2$), LM3DM($|M_3| \ll M_1 \simeq M_2$) or HM2DM ($|M_2| \gg M_1 \simeq M_3$))
 - $\tilde{Z}_2 - \tilde{Z}_1$ and $\tilde{W}_1 - \tilde{Z}_1$ mass gaps are reduced compared to the case with gaugino mass universality
 - SUSY can be discovered at Tevatron via squarks and gluinos
 - CERN LHC should be able to measure $m_{\tilde{g}}$ and $m_{\tilde{Z}_2} - m_{\tilde{Z}_1}$ mass gap from dilepton distribution from $\tilde{Z}_2 \rightarrow l\bar{l}\tilde{Z}_1$ decay; $\tilde{Z}_2 \rightarrow \tilde{Z}_1\gamma$ (spoiler 2-body decay closed)
 - At ILC, $\tilde{W}_1^+\tilde{W}_1^-$, $\tilde{Z}_1\tilde{Z}_2$, $\tilde{Z}_2\tilde{Z}_2$ production cross sections as a function of beam polarization should be able to measurable.
 - Direct and Indirect detection experiments may discriminate between these scenarios
- Where the neutralino composition is adjusted to give the WMAP value (WTN models),
 - neutralino is typically of the mixed bino-wino or mixed bino-higgsino states
 - enhanced neutralino annihilation rates \rightarrow direct detection scattering rates enhanced

MSSM RGEs

$$\frac{dm_{H_u}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 + \frac{3}{10}g_1^2 S + 3f_t^2 X_t \right)$$

$$\frac{dm_{H_d}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 - \frac{3}{10}g_1^2 S + 3f_b^2 X_b + f_\tau^2 X_\tau \right)$$

$$\frac{dm_{Q_3}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{1}{15}g_1^2 M_1^2 - 3g_2^2 M_2^2 - \frac{16}{3}g_3^2 M_3^2 + \frac{1}{10}g_1^2 S + f_t^2 X_t + f_b^2 X_b \right)$$

$$\frac{dm_{\tilde{t}_R}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{16}{15}g_1^2 M_1^2 - \frac{16}{3}g_3^2 M_3^2 - \frac{2}{5}g_1^2 S + 2f_t^2 X_t \right)$$

$$\frac{dm_{\tilde{b}_R}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{4}{15}g_1^2 M_1^2 - \frac{16}{3}g_3^2 M_3^2 + \frac{1}{5}g_1^2 S + 2f_b^2 X_b \right)$$

$$\frac{dm_{L_3}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 - \frac{3}{10}g_1^2 S + f_\tau^2 X_\tau \right)$$

$$\frac{dm_{\tilde{\tau}_R}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{12}{5}g_1^2 M_1^2 + \frac{3}{5}g_1^2 S + 2f_\tau^2 X_\tau \right)$$

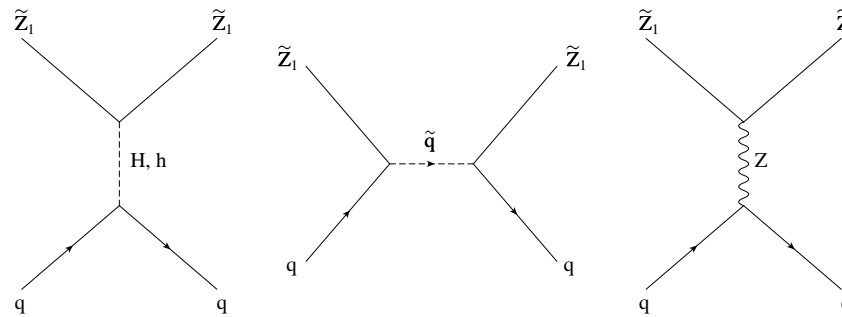
$$S = m_{H_u}^2 - m_{H_d}^2 + Tr \left[\mathbf{m}_Q^2 - \mathbf{m}_L^2 - 2\mathbf{m}_U^2 + \mathbf{m}_D^2 + \mathbf{m}_E^2 \right]$$

where $t = \log(Q)$, $f_{t,b,\tau}$ are the t , b and τ Yukawa couplings, and

$$\begin{aligned} X_t &= m_{Q_3}^2 + m_{\tilde{t}_R}^2 + m_{H_u}^2 + A_t^2 \\ X_b &= m_{Q_3}^2 + m_{\tilde{b}_R}^2 + m_{H_d}^2 + A_b^2 \\ X_\tau &= m_{L_3}^2 + m_{\tilde{\tau}_R}^2 + m_{H_d}^2 + A_\tau^2 \end{aligned}$$

Feynman Diagrams Contributing to Neutralino DM Detection

- Direct Detection



- Indirect Detection

